Reactor Handbook: Physics Volume 2



SELECTED REFERENCE MATERIAL
UNITED STATES ATOMIC ENERGY PROGRAM

Reactor Handbook: Physics



SELECTED REFERENCE MATERIAL
UNITED STATES ATOMIC ENERGY PROGRAM

- Google



THE LIBRARY
OF
THE UNIVERSITY
OF CALIFORNIA
LOS ANGELES

SELECTED REFERENCE MATERIAL UNITED STATES ATOMIC ENERGY PROGRAM

Reactor Handbook: Physics



UNITED STATES OF AMERICA

SELECTED REFERENCE MATERIAL ON ATOMIC ENERGY

VOLUME ONE Research Reactors

VOLUME TWO Reactor Handbook: Physics

VOLUME THREE Reactor Handbook: Engineering

VOLUME FOUR Reactor Handbook: Materials

VOLUME FIVE Neutron Cross Sections

VOLUME SIX Chemical Processing and Equipment

VOLUME SEVEN Eight-year Isotope Summary

VOLUME EIGHT Information Sources

VOLUME TWO

Reactor Handbook: Physics

UNITED STATES OF AMERICA GENEVA: AUGUST 1955



Foreword

Interchange of scientific and technical knowledge will greatly facilitate the work of the scientists and engineers whose skills will be devoted to the future development of the peaceful uses of atomic energy.

The United States has made available to the world's scientific community a large body of such data. In honor of this historic Conference and to stimulate further exploration and development of the beneficial applications of nuclear energy, the United States Atomic Energy Commission has prepared this special collection of technical data for the use of the delegates and the nations represented.

The purpose of this collection is to provide information concerning the ways that we have found in which fissionable materials can be put to work in nuclear reactors for research purposes and for the production of power and radioisotopes.

It is our sincere hope that this material will be of practical value to the men and women of science and engineering in whose hands the great power of the atom is becoming a benign force for world peace.

Reus L Shaun

Chairman, U.S. Atomic Energy Commission

Acknowledgment

This series of volumes was sponsored by the United States Atomic Energy Commission for presentation by the United States of America to the countries represented at the International Conference on Peaceful Uses of Atomic Energy.

The organizations which contributed material presented in these volumes are:

Argonne National Laboratory (University of Chicago)

Battelle Memorial Institute

Brookhaven National Laboratory (Associated Universities, Inc.)

Hanford Works (General Electric Company)

Knolls Atomic Power Laboratory (General Electric Company)

Los Alamos Scientific Laboratory (University of California)

Mound Laboratory (Monsanto Chemical Company)

National Reactor Test Station (Phillips Petroleum Company)

North American Aviation, Inc.

Nuclear Development Associates

Oak Ridge National Laboratory (Carbide and Carbon Chemicals Company)

Savannah River Laboratory (E. I. du Pont de Nemours & Co., Inc.)

University of California Radiation Laboratory

Westinghouse Electric Corporation

THE REACTOR HANDBOOK VOLUME 1 PHYSICS

DECLASSIFIED EDITION FEBRUARY 1955

Published by
TECHNICAL INFORMATION SERVICE
U.S. ATOMIC ENERGY COMMISSION

Contributors to the first edition:

BROOKHAVEN NATIONAL LABORATORY

KNOLLS ATOMIC POWER LABORATORY NORTH AMERICAN AVIATION, INC.

NUCLEAR DEVELOPMENT ASSOCIATES

OAK RIDGE NATIONAL LABORATORY VITRO CORPORATION OF AMERICA



Reviewed on behalf of the Atomic Energy Commission by a Review Board consisting of:

HARVEY BROOKS

Harvard University

P. F. GAST

Nucleonics Division
General Electric Company

J. P. HOWE

North American Aviation, Inc.

S. LAWROSKI

Argonne National Laboratory

M. C. LEVERETT

ANP Project
General Electric Company

W. H. ZINN, Chairman

Argonne National Laboratory

Program managed on behalf of the Division of Reactor Development and the Technical Information Service by:

D. F. MASTICK

Division of Military Application*

Coordination and editing by:

J. F. HOGERTON and R. C. GRASS

Vitro Corporation of America



^{*}Present address General Precision Equipment Corporation.

FOREWORD

With the rapid maturity of reactor technology and its growing application to industrial power reactors, there has developed an urgent need for a comprehensive and critical compilation of nuclear engineering data. At the request of Dr. L. R. Hafstad, Director of Reactor Development, and in accord with an over-all program for the organization and consolidation of AEC-developed technical information, the Commission's Technical Information Service has issued this Reactor Handbook for convenient reference use by scientists and engineers engaged on AEC reactor projects.

The material presented in this first edition of the Handbook represents the efforts of specialists in the various areas of reactor science and technology, and summarizes the accomplishments of the Commission's nuclear reactor program to date. Future editions are planned as continuing advances in this field may require.

The Commission extends its appreciation to all participants in the Reactor Program for the time and effort expended in the completion of this Handbook.

Lewis L. Strauss Chairman United States Atomic Energy Commission

REVIEW BOARD PREFACE

The Review Board was appointed by the Director of the Reactor Development Division in December of 1951. The Board found itself in agreement with the objective of preparing a reactor handbook at an early date, although it was recognized that this placed the effort under a considerable handicap as did the necessity of combining the efforts of numerous author groups.

The Board instituted a mechanism for review of the material as prepared by the author groups. In the work of review the members of the Board called upon many individuals in the various Laboratories for critical comments. Without this assistance the review could not have been performed in the two or three weeks usually available, and the members of the Board express their indebtedness and thanks to these reviewers.

The general format of the Handbook received consideration and the result is recognized as a compromise of what is most desirable in a handbook and what is practical under the present circumstances.

The ultimate success of the Handbook will depend a great deal upon the refinements in subject matter and presentation which will come about in subsequent revisions. It is expected that such revisions will profit enormously from suggestions from the users of the Handbook.

To the Editorial Coordinator, John F. Hogerton, to Donald F. Mastick who represented the Technical Information Service, and to William W. Galbreath who served as secretary, the Board expresses its appreciation for a cordial working relationship. Above all, thanks are due to the various author groups who made the task of review easier by their patience in receiving criticism and suggestions.

THE REVIEW BOARD

Harvey Brooks
Paul F. Gast
John P. Howe
Miles C. Leverett
W. H. Zinn, Chairman

EDITORIAL PREFACE

The purpose of the Reactor Handbook is to provide a condensed source of reliable data and reference information for those working in the reactor field. Work on this first edition, jointly sponsored by the Division of Reactor Development and the Technical Information Service, started in January 1952, with a fifteen-month publishing target. The authors, most of whom had heavy project commitments, had one month in which to plan their work, and three months to a year in which to survey the field and prepare their compilation. Those preparing large sections were called upon to submit their material in parts and were allowed on the average of one month for reworking a given part after review. The Review Board had the difficult task of reviewing the Handbook material in random increments, with two to three weeks in which to review a given increment. The schedule did not permit a second review following the author's reworking. The editors had from one to three weeks in which to prepare Handbook material for the publisher. To distribute the publisher's load at Oak Ridge, parts of sections were put into the publishing machinery while other parts were still in preparation by the authors.

To meet the schedule, it was necessary to make certain compromises which should be noted here:

- 1. A somewhat arbitrary approach has necessarily been taken on the problem of coverage, not only with respect to the subjects treated but also the data presented on a given subject. Before using a particular section for the first time, the reader should consult the author's preface which brings out any major limitations in the scope or treatment of the data presented.
- 2. The policy was adopted early in the program not to attempt a detailed <u>documentation</u> of the source of the data presented. Some specific references are given; however, source identification is restricted primarily to tables or figures which have been taken intact from project reports or the open literature.
- 3. It has not been possible to achieve the consistency one would like in the use of <u>units</u>. In general, the metric system is used where the data are considered to be of interest primarily to "scientists," and the English system is used where the data are considered to be of interest primarily to "engineers." An attempt has been made to include conversion factors in the body of tables and charts, and in some cases data are expressed in dual units.
- 4. To simplify page make-up and printing problems, the decision was made early in the program to eliminate the <u>background grid</u> from graphs. Data were to have been presented in tabular form in cases where it was considered important to retain accurate values. In actual practice some graphs have been reproduced with grid and it is felt that this practice can and should be extended in the next edition of the Handbook.

In the present edition of the Handbook, each volume is indexed separately. The organization is the same throughout. Sections are numbered consecutively within a volume; chapters consecutively within a section; and figures, tables, and formulae consecutively within a chapter.



EDITORIAL PREFACE

The first edition combines elements of a "Handbook of Chemistry and Physics," a Marks' "Mechanical Engineer's Handbook," a Mellor's "Treatise on Inorganic Chemistry," and an industrial data book. This result is in some degree inherent in a work that cuts across a number of scientific and engineering disciplines; however, greater unity of presentation should be possible in future editions.

The editors are most appreciative of the attention their problems have received from the Review Board and the author groups, and from Alberto F. Thompson and Donald F. Mastick of the AEC staff. They are most appreciative, also, of the cooperation of William W. Galbreath of ANL, W. H. Sullivan of ORNL and Dennis Puleston of BNL, who did much to advance the Handbook effort at their respective sites, and of R. L. Cummins, E. C. Schulte, and their publishing personnel in the Technical Information Service at Oak Ridge.

John F. Hogerton and Robert C. Grass VITRO CORPORATION OF AMERICA

CONTENTS OF VOLUME 1-PHYSICS

SE	CTION 1 - REA	ACTOR PHYSICS	xi
	Author's Pre	face	xiii
	Chapter 1.1	Experimental Methods	1
	Chapter 1.2	Nuclear Physics	61
	Chapter 1.3	Kinetic Theory of Neutrons	365
	Chapter 1.4	Reactor Statics; Theory and General Results	427
	Chapter 1.5	Reactor Statics; Experimental and Numerical Results	477
	Chapter 1.6	Reactor Dynamics	531
SE	CTION 2 - RAI	DIATION SHIELDING	617
	Acknowledgm	nents	618
	Author's Pre	face	619
	Chapter 2.1	Sources of Radiation	621
	Chapter 2.2	Permissible Levels of Radiation	629
	Chapter 2.3	Gamma-ray Attenuation	637
	Chapter 2.4	Neutron Attenuation	667
	Chapter 2.5	Geometry	677
	Chapter 2.6	Ducts Through Shields	695
	Chapter 2.7	Heat Generation in Shields	701
	Chapter 2.8	Shield Optimization with Respect to Weight	709
	Chapter 2.9	Shield Materials	715
ΑP	PENDIX 1		753
۱P	PENDIX 2		761
NI	æ		775

Section 1 REACTOR PHYSICS

Prepared by

NUCLEAR DEVELOPMENT ASSOCIATES

under the direction of

H. SOODAK

Author's Preface

This section of the Reactor Handbook has, like all other sections, been written on a brief time schedule, and it will be apparent to the reader that the present version is but a quick and incomplete rough draft. However, it is believed that the ultimate goal will be better served by publication of this material now, so that it can reach a larger group for criticisms and suggestions, rather than by a painstaking revision of the material within the smaller author group. This section is offered, therefore, as a first small contribution to a mutual effort.

Chapter 1.2, "Nuclear Physics," leans heavily on the data compilations of both the AEC Neutron Cross-section Advisory Group* under D. J. Hughes and the National Bureau of Standards group† under K. Way. It is assumed that the reader has access to the unclassified portions of these compilations. For estimating the values of cross sections in the absence of data, results of theoretical considerations are included here, particularly in the discussion of "Collision Reactions."

Chapter 1.4, "Reactor Statics — Theory and General Results," was the last chapter written and the preparation of the sub-sections "General Kernels" through "Non-uniform Media" was especially hurried.

Chapter 1.5, "Reactor Statics — Experimental and Numerical Results," is an extract of some of the most readily available project literature, but no attempt was made at comparative evaluation.

The theoretical material of Chapter 1.6, "Reactor Dynamics and Control," appears in general symbolic form in order not to restrict the validity to particular reactor models. Time did not permit the inclusion of many particular examples.

This section of the handbook was indexed lightly, the text containing more information than the index entries indicate.

Substantial contributions to this work were made by many persons outside the author group. We should like to thank particularly H. Paxton for a valuable compilation of Los Alamos critical data; K. T. Bainbridge and John Wiley and Sons, Inc., for permission to include a mass table from a forthcoming book; G. T. Seaborg for a new edition of the Table of Isotopes; D. J. Hughes of BNL for loan of the manuscript of his book on Pile Neutron Research; I. Kaplan and J. Chernick of BNL for discussions and data on lattice reactors; the Dow Chemical Company and Detroit Edison Company, and R. Ehrlich and H. B. Stewart of KAPL, for fast-reactor results; and H. Hurwitz, Jr., of KAPL for most helpful technical discussions and unpublished results which appear in many places throughout this section.

Harry Soodak March 31, 1953

^{*}AECU-2040, BNL-170, BNL-170A.

[†]NBS-499 and its supplements, now appearing in Nuclear Science Abstracts.

Note to the Declassified Edition

This section was originally prepared using data available up to about December 1952. Except for minor editorial treatment following deletion of classified material, the original presentation has not been revised in producing this declassified version.

Harry Soodak March 7, 1955

CHAPTER 1.1

Experimental Methods

Ira Pullman

NEUTRON SOURCES

NEUTRONS FROM NATURAL ALPHA EMITTERS

Neutrons can be produced by bombarding many of the light elements with alpha particles which are emitted by some of the natural radioactive elements. This is the oldest, cheapest, easiest, most reliable, and most compact method for obtaining neutrons with energies up to 13 mev and average intensity of 10⁷ neutrons/sec. Neutron yields obtained from thick* targets of various elements using alpha particles of 5.3 mev from a polonium source are given in Table 1.1.1. Beryllium furnishes the highest yield; the main reaction is:

$$Be^9 + He^4 \rightarrow C^{12} + n^1 + 5.76 \text{ mev}$$
 (1)

The neutron yields obtained by bombarding Be with alpha particles from U and Ra and its decay products are listed in Table 1.1.2.

Ra-Be SOURCES

The Ra- α -Be source is the most common type. A very compact form can be produced by slurrying finely ground beryllium powder in an aqueous solution of radium bromide, evaporating to dryness, and compressing the residual powder into pellet form. A pressure of 10 tons/sq in. yields a density of 1.75 gm/cm³. The pellet is then sealed in a gas-tight metal container to confine the radon decay product.

Because of the slow accumulation of the alpha-emitting decay products of radium, the intensity takes a few weeks to reach a steady state. The rate of increase is given approximately by:

$$A = A_0 \frac{1 + 5\left(1 - \exp{-\frac{t}{3.8}}\right)}{6}$$
 (2)

where: A_{ϕ} = equilibrium intensity t = time in days after sealing

It is assumed that the Ra alpha rays contribute one sixth of all the neutrons produced. At equilibrium, the source decays with the half-life of Ra²²⁶, 1600 yr.

The strength of a source as a function of its composition by weight is given approximately by:

^{* &}quot;Thick" means here of sufficient size to stop all α -particles.

¹References appear at end of chapter.

CHAP. 1.1 REACTOR PHYSICS

Table 1.1.1 — Po- α Neutron Yields from Thick Targets

(Anderson, Neutrons from Alpha Emitters, Prelim. Rep. No. 3, Nuclear Sci. Series, Nat. Res. Council, Dec. 1948)

Element	Yield, n/10 ⁶ alphas
Li	2.6
Be	80
В	24
С	0.11
N	.01
0	.07
F	12
Na	1.5
Mg	1.4
Al	0.25
Si	.16
Cl	.11
A	.38

Table 1.1.2 — Neutron Yields from Thick Beryllium Targets
(Anderson, Neutrons from Alpha Emitters, Prelim. Rep. No. 3, Nuclear Sci. Series, Nat. Res. Council, Dec. 1948)

Alpha emitter	\mathbf{E}_{α} , me v	Yield, n/10 ⁶ alphas
U	4.18	40
Ra	4.791	55
Rn	5.486	90
RaA	5.998	120
RaC'	7.680	200
Raf (Po)	5.298	80

$$A_0 = 1.7 \times 10^7 \frac{M_{Be}}{M_{Be} + M_{RaBr_2}} = neutrons/(sec)(gm Ra)$$
 (3)

When prepared in pellet form, sources with an A of 10^7 n/sec can be prepared in a volume of 6.5 cm³. Thus, near the surface, the neutron flux has the relatively high value of 6×10^5 n/(cm²)(sec).

Because of the various alpha energies, the neutron energy spectrum is continuous up to a maximum energy of 13.2 mev. The most probable energy is about 5 mev, and the average energy is about 2.5 mev. An alpha particle of zero energy would produce a neutron with 5.4 mev, Eq. (1), but large numbers of neutrons exist with less energy. These are associated with gamma rays and are produced by excited states of C^{12} . Neutrons are also emitted with energies below 1 mev and sometimes only a few electron volts. They are believed to come from another reaction:

$$Be^{9} + He^{4} \rightarrow C^{13}* \rightarrow Be^{9}* + He^{4}$$
 $Be^{9}* \rightarrow Be^{8} + n^{1}$
 $Be^{8} \rightarrow 2He^{4}$

The complete reaction is:

$$Be^9 + He^4 \rightarrow 3He^4 + n^1 - 1.62 \text{ mev}$$
 (4)

Finally, because the product nucleus C¹² has a low mass it attains significant velocities in the laboratory frame of reference and causes a large spread in the neutron energies.

The neutron spectrum from the $Ra-\alpha-Be$ source has not been measured in detail, especially at low energies. Above 1 mev, the best available spectrum is that given by Demers² and shown in Fig. 1.1.1.* The photographic plate method was used.

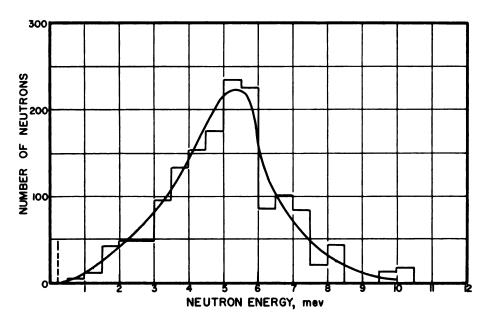


Fig. 1.1.1 — The Neutron Energy Spectrum from a Ra- α -Be Source. Reprinted from Dacey, Paine, and Goodman, Tech. Rep. No. 23, Lab. for Nuclear Sci. and and Eng., M.I.T. Oct. 1949.

Besides the non-homogeneous neutron energy, an important disadvantage of the $Ra-\alpha-$ Be source is its high gamma ray intensity which constitutes the main health hazard. One curie of Ra will produce 0.05 roentgen in 3.5 min at a distance of 1 meter. This is the maximum allowable dose for an 8-hr day. At 1 meter, the neutron flux from a 1-gm $Ra-\alpha-$ Be source is not dangerous.⁴

About 7000 photons are emitted for each neutron from sources prepared as described above. The great majority of these gammas are primary radiation emitted by Ra and its decay products since only about 1 in 10^4 alphas will disintegrate the Be nucleus. The gamma spectrum of a radium source is given in Table 1.1.3. (See also footnote ($\ddagger\ddagger$) of Table 1.1.5.)

Po-Be SOURCES

Where it is desirable to eliminate gamma activity, $Po^{210} - \alpha$ -Be sources may be used. One curie of Po in such a source will emit about 0.01 percent of the gamma radiation from

^{*}Demers' experiments are discussed by Dacey, Paine, and Goodman; see also Anderson, 1

CHAP. 1.1 REACTOR PHYSICS

Table 1.1.3 — Gamma Spectrum from Radium and Its Decay Products
(R. D. Evans and R. O. Evans, Rev. Mod. Phys. 20, 1948)

Transition	Energy per photon (hv), mev	Average quanta per alpha ray of Ra (r)	Total photon energy per alpha ray (rhv), mev
Ra → Rn	0.184	0.012	0.0022
RaB - RaC	.241	.115	.0277
	.294	.258	.0758
	.350	.4 50	.1575
RaC → RaC'	.607	.658	.4000
	.766	.065	.0498
	.933	.067	.0625
	1.120	.206	.2310
	1.238	.063	.0780
	1.379	.064	.0882
	1.761	.258	.4540
	2.198	.074	.1626
Total		2.290	1.789

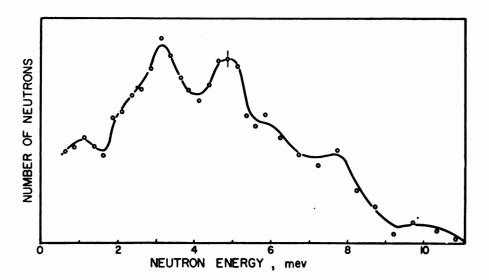


Fig. 1.1.2 — The Neutron Energy Spectrum from a Po- α -Be Source. Reprinted from Whitmore and Baker, Phys. Rev., 78, 1950.

a curie of Ra.⁵ The neutron yield is about $^{1}/_{7}$ of that of Ra $-\alpha$ -Be. The most recent spectrum reported⁶ is shown in Fig. 1.1.2. The photographic plate method was used, putting a lower limit to the energies detectable at about 0.5 mev. Po²¹⁰ is difficult to prepare and has the great disadvantage of a relatively short half-life (140 days). Po $-\alpha$ -Be sources can now be purchased from Oak Ridge.

Rn-Be SOURCES

Radon, because of its availability from hospitals, has been used as an alpha source. Since it is a gas, only about 100 mg of Be is needed to realize the full efficiency of the

EXPERIMENTAL METHODS CHAP. 1.1

source. To achieve the same yield using RaBr₂, about 13 gm of Be would be needed. However, Rn has a half-life of only 3.825 days, and therefore the neutron intensity decays rapidly.

Ra-B AND Po-B SOURCES

Boron is sometimes used as a target because the neutron energy distribution is smaller and more homogeneous. The yields, lower than those from Be, are listed in Table 1.1.4.

Table 1.1.4 — Neutron Yields from Thick Boron Targets

(Anderson, Neutrons from Alpha Emitters, Prelim. Rep. No. 3, Nuclear Sci. Series, Nat. Res. Council, Dec. 1948)

Alpha emitter	\mathbf{E}_{α} , mev	Yield, n/10 ⁶ alphas
Ra	4.791	15
Rn	5.486	30
RaA	5.998	40
RaC'	7.680	100
RaF	5.298	24

 $Ra-\alpha-B$ sources can be prepared in a similar manner to the $Ra-\alpha-B$ e sources described above. The intensity as a function of composition is given by:

$$A = 6.8 \times 10^6 \frac{M_B}{M_B + M_{RaBr_2}} = n/(sec)(gm Ra)$$
 (5)

Natural boron consists of two isotopes, 81.2 percent B¹¹ and 18.8 percent B¹⁰. The main reaction is:

$$B^{11} + He^4 \rightarrow N^{14} + n^1 + 0.28 \text{ mev}$$
 (6)

Neutrons are also produced by:

$$B^{10} + He^4 \rightarrow N^{13} + n^1 + 1.18 \text{ mev}$$
 (7)

but this is less favored than the reaction:

$$B^{10} + He^4 \rightarrow C^{13} + H^1 + 4.14 \text{ mev}$$
 (8)

The neutron energy spectrum using Ra is similar to that using Po^{210} , and an appreciable amount of low-energy neutrons is not believed to be present. The spectrum from a $Po-\alpha-B$ source is shown in Fig. 1.1.3. The neutrons were measured in a hydrogen-filled ionization chamber. The average energy of $Ra-\alpha-B$ neutrons is about 2.9 mev.

PHOTONEUTRON SOURCES USING RADIOACTIVE NUCLEI⁸

Some artificial and natural radioactive sources emit gammas of sufficiently high energy to eject neutrons from deuterium and beryllium, which have the lowest neutron binding energies of the elements. The main advantages of such sources compared with alpha-

CHAP. 1.1 REACTOR PHYSICS

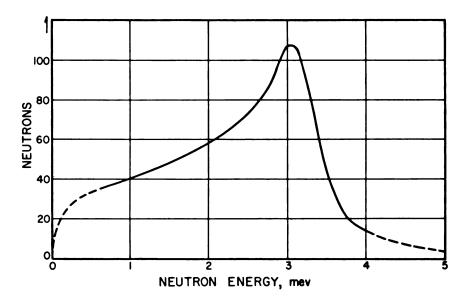


Fig. 1.1.3 — The Neutron Energy Spectrum from a Po- α -B Source. Reprinted from Anderson, Neutrons from Alpha Emitters, Prelim. Rep. No. 3, Nuclear Sci. Series, Nat. Res. Council, Dec. 1948.

neutron sources are that the emitted neutrons are monoergic if the gamma ray is monoergic and that the source strengths are easier to reproduce. However, the neutron yield is lower and the high-intensity, high-energy gamma radiation can be a health hazard and may interfere with detection of neutrons. The artificial radioisotopes have short half-lives (days or less), and sources utilizing them are not as permanent as those using natural radioactive materials.

The γ , n reactions in Be and D are:

$$Be^{9} + \gamma \rightarrow Be^{8} + n^{1} - 1.666 \pm 0.002$$
 (9)

$$D^2 + \gamma \rightarrow H^1 + n^1 - 2.226 \pm 0.003$$
 (10)

From conservation of energy and momentum, the energy of the neutrons is given by:

$$E_{n} = \frac{A-1}{A} \left[E_{\gamma} - Q - \frac{E_{\gamma}^{2}}{1862(A-1)} \right] + \delta$$
 (11)

where: E_n = neutron energy in mev

A = mass number of target nucleus

Q = threshold energy for reaction in mev

 $E_{\gamma} = gamma energy in mev$

 δ = a small energy spread containing the angular distribution; that is:

$$\delta \cong E_{\gamma} \left[\frac{2(A-1)(E_{\gamma}-Q)}{931A^3} \right]^{\frac{1}{2}} \cos \theta \tag{12}$$

where: θ = angle between gamma ray and neutron.

If the gamma rays fall upon the target in an isotropic manner, there is an inherent spread in the energy of the emitted neutrons which is given by:

$$\delta_{\max} = 2E_{\gamma} \left[\frac{2(A-1)(E_{\gamma} - Q)}{931A^3} \right]^{\frac{1}{2}}$$
 (13)

The fractional spread, δ_{max}/E_n , decreases with increasing neutron energy and is 5 to 10 times greater in deuterium than in beryllium. For 100-kev neutrons, the fractional spread is about 4 percent in Be and 25 percent in D. For 100-kev neutrons from Be, δ_{max} is generally negligible compared to other causes of energy spread. One can lower this inherent spread by collimating the gamma rays, but this greatly reduces the neutron yield per photon.

The spectra for some photoneutron sources are shown in Fig. 1.1.4 (see footnote (‡) of Table 1.1.5). The observed energy distributions (obtained with the source dimensions shown in Fig. 1.1.6) have a spread of about 20 to 30 percent full width at half-maximum, and the mean energy is 5 to 15 percent below the theoretical neutron energy. This smear-

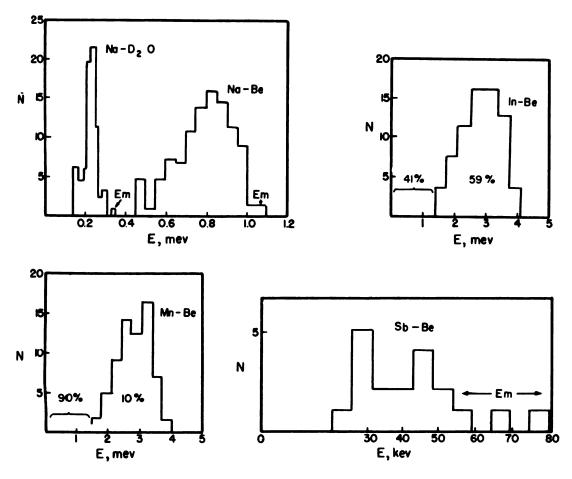


Fig. 1.1.4 — The Photoneutron Energy Spectrum from the Following Sources: Na²⁴-Be and Na²⁴-D; In¹¹⁶-Be; Mn⁵⁶-Be; and Sb¹²⁴-Be. Reprinted from Hughes and Eggler, Phys. Rev. 72, 1947.

Table 1.1.5 — Properties of Some Useful Photoneutron Sources

					Thorntool		Neutron yie	Neutron yield, n/(sec)(c)
Radioisotope	Half-life	Gamma-ray energy, mev	Photons per disintegration	Target	neutron energy, mev	Observed ave. neutron energy, mev	Standard source,* × 104	Source of Fig. 1.1.6, $^{63} \times 10^6$
NaM	14.8 hr	2.76	1.0	Be	0.97	0.83†	14, 12	2.4
		2.76	1.0	Ω	.27	.221,‡	29, 24, 27	2.7
Mn ⁵⁶	2.59 hr	1.81	0.25	Be	.14	.15†,‡	2.9	0.5
		2.13	.15	Be	.42	.30‡		
		2.7	.01	Δ	.25	.22†	0.3	.029
Ga ⁷³	14.1 hr	1.9	90.	Be	6.	.27†	5.9, 3.7	1.04
		2.2	.33	Be	4.			
		2.5	.26	ቘ				
		2.5	.26	Ω	.15	.13†	6.9, 4.6	0.64
As^{76}	26.8 hr	1.8	Low	ഷ	۲:	:		
		2.2	Low	æ	₹.	:		
Λ^{68}	105 days	1.85	1.0	Be	.16	.158\$	10	
	1	2.76	~0.01	æ	86.	.22%,96		
		2.76	~.01	Ω	.27	:	0.3	
In 116	54 min	1.8	<.03¶	æ	٦.	< 0.15‡	.82	.14
		2.1	52.	æ	.35	.3083		
Sb ¹²⁴	60 days	1.71	~.	Be	.03	[.035‡ [.024†,\$	19	3.2
La 140	40 hr	2.5	7.0	ቘ		.62†	0.23, 0.34	0.04
		2.5	~.04	Ω	.15	.13†	.68, .97	.062

0.04	.062		
0.23, 0.34			
134			

PHYSICS

3.5	9.5	1.2		0.1
.827\$.1978	:	:	0.1286,86
98.	8.	.085	.382	.10
8	Ω	Be	Ве	Ω
.35	.35	.258**	.074**	Low
2.6211		1.761‡‡	2.198	2.42
6.7 yr		1590 yr		
Ra 236 ##		Ra 226.		

* A standard source is defined as a gamma source of 1 curie placed 1 cm away from a target of 1 gm. The values are taken from Wattenberg.

Some of the sources have more than one value, as reported by different investigators

† The neutron energies were determined by measuring the scattering cross section in hydrogen (paraffin) which is a known function of energy. This is an integration method, and only an average energy can be obtained. The cylindrical source of Fig. 1.1.6 was used

†The neutron energies were determined from observing head-on proton collisions in a hydrogen-filled cloud chamber. 11 A differential spectrum could be obtained (see Fig. 1.1.4). The upper tails of the peaks give a maximum energy that in most cases agrees closely with the theoretical value 8 Neutron energies were determined from maximum pulse heights of recoil protons in a hydrogen-filled proportional counter. A differential spectrum could be obtained. Spherical sources were used

Hughes and Eggler 11 found the same order of intensity for low- and high-energy neutrons in In 116 (see Fig. 1.1.4). This is in disagreement with the intensity of the 1.8-mey gamma as reported by Slätis et al

**Ra²²⁸ (MsTh₁) and Ra²²⁶ are in equilibrium with their decay products. The photon and neutron yields are based on the number of disintegrations of †† A 1.80-mev gamma (6.5% of 2.62-mev gamma intensity) and a 2.20-mev gamma (8%) also reported⁸⁸ in ThC + ThC'' ‡‡ Latyshev⁸⁸ lists the following gamma-ray energies above 1.65 mev in RaC and their intensities relative to the 2.2-mev gamma: the parent source

2.42 mev 0.50 of 2.2-mev intensity
2.20 mev 1.00 of 2.2-mev intensity
2.09 mev 0.37 of 2.2-mev intensity
1.82 mev .41 of 2.2-mev intensity
1.76 mev 2.42 of 2.2-mev intensity
1.69 mev 0.40 of 2.2-mev intensity

gamma is not reported. However, since there is some neutron emission from a Ra-D source, the existence of this high-energy gamma would seem to be confirmed In Table 1.1.3, which was based on older measurements of Ellis and others, the distribution of the high-energy gammas is different and the 2.42-mev

ing is caused by scattering in the beryllium or deuterium which are good moderators. Reducing the target thickness unfortunately also reduces the yield. Table 1.1.5 lists the more important photoneutron sources and their neutron energies and yields. Only long-lived isotopes and only gamma-ray energies above 1.65 mev are given. The theoretical neutron energies were calculated from Eq. (11) using the latest values for threshold energies of Be and D as given in Eqs. (9) and (10).

MANUFACTURE OF PHOTONEUTRON SOURCES

To obtain a high neutron yield with minimum energy degradation in the source, the specific activity of the gamma emitter should be as high as possible. Thus, carrier-free sources with the highest possible atomic density are desirable. This generally means that the metallic form of the element should be used except in the case of sodium where fused NaF has a higher atomic density than metallic sodium. For thick sources or targets, attenuation of the gamma-ray intensity by the Compton effect may have to be considered. The Compton effect is about 10³ times more probable than the photodisintegration process; thus, even in an infinitely thick target, one can expect only 1 neutron per 10³ gammas.

Spherical, concentric sources in which a uniform thickness of target surrounds a sphere of the radioisotope give the highest yield in the smallest volume and will emit neutrons with spherically symmetric distribution. This is often of great value. Figure 1.1.5 shows

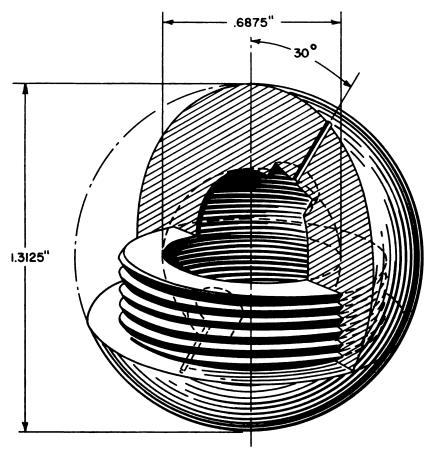


Fig. 1.1.5 — Design of a Spherical Photoneutron Source. Reprinted from A. Wattenberg, Photo-neutron Sources, Prelim. Rep. No. 6, Nuclear Sci. Series, Nat. Res. Council, July 1949. The shell is made of beryllium.



a design by the Bureau of Standards for this type of source. This shape has the disadvantage that it is difficult to change gamma emitters or remove the target material to determine effects of the gamma rays alone. A plug of beryllium may be cut out to facilitate removing the source.

A spherical source may also be made by dissolving the gamma emitter in D_2O or by preparing a homogeneous mixture of the source and Be. This method, of course, contaminates the target.

Concentric-cylinder-type sources are much easier to assemble and interchange although the yield is lower because of losses along the cylindrical axis and the neutron distribution is asymmetric. To a first approximation if the source is large, the number of neutrons will be proportional to the surface area of the target seen at the detector. Figure 1.1.6 shows the design of the cylindrical source used by Wattenberg¹⁰ and Hughes¹¹ in their measurements of neutron energies and yields.

Separating the gamma emitter from the target to collimate the gamma beam reduces the neutron energy spread and makes the geometry somewhat more reproducible. The neutron intensity drops rapidly, and the solid-angle factor becomes critical. The angular distribution of the neutron must be considered. The cross section for the photodisintegration of the deuteron is shown in Fig. 1.1.7. σ_{magnetic} is spherically symmetrical and σ_{electric} varies as $\sin^2\theta$; above 2.5-mev gamma energy, therefore, most of the neutrons will travel off at right angles to the gamma beam.

PARTICLE ACCELERATORS

Neutrons can be produced by bombarding many of the isotopes with charged particles in accelerators. Cockcroft-Walton and electrostatic generators are used to make neutrons with carefully controlled energies up to 20 mev. Higher-energy neutrons with a much broader energy distribution can be made in cyclotrons of various types and in linear accelerators. High-energy neutrons will not be discussed here since they are not produced in reactors.

The general non-relativistic analysis of a two-body collision with a target stationary in the laboratory coordinate system yields the following results for the neutron spectrum (see Fig. 1.1.8 for schematic diagram). By definition:

$$\mathbf{E_2} = \mathbf{0}$$

$$\mathbf{E_1} + \mathbf{E_4} = \mathbf{E_1} + \mathbf{Q}$$

$$E_i$$
 = kinetic energy of i-th particle (14)

 θ_1 varies from 0 to π .

As a good approximation for the masses, since $Q \ll 931$ mev in all cases:

$$M_1 + M_2 = M_3 + M_4 \tag{15}$$

The neutron energy in the laboratory coordinate system is given as a function of the incident-particle energy by the following equation which is derived from the momentum and energy conservation laws:

$$E_{3} = E_{1} \frac{M_{1}M_{3}}{(M_{3} + M_{4})^{2}} \left\{ 2 \cos^{2} \theta_{3} + \frac{M_{4}(M_{3} + M_{4})}{M_{1}M_{3}} \cdot \left[\frac{Q}{E_{1}} + \left(1 - \frac{M_{1}}{M_{4}} \right) \right] \right.$$

$$+ 2 \cos \theta_{3} \sqrt{\cos^{2} \theta_{3} + \frac{M_{4}(M_{3} + M_{4})}{M_{1}M_{3}} \left[\frac{Q}{E_{1}} + \left(1 - \frac{M_{1}}{M_{4}} \right) \right]}$$
(16)

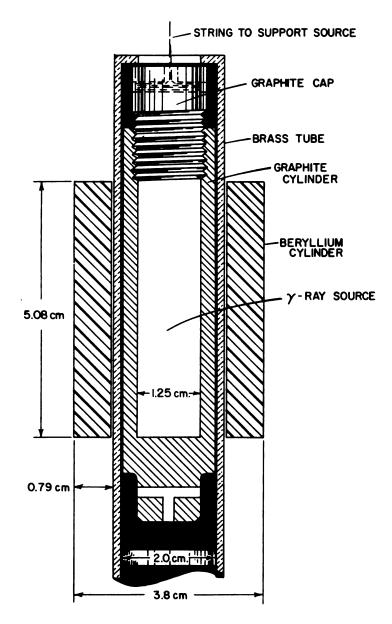


Fig. 1.1.6 — Design of a Cylindrical Photoneutron Source. Reprinted from A. Wattenberg, Photo-neutron Sources, Prelim. Rep. No. 6, Nuclear Sci. Series, Nat. Res. Council, July 1949. To use deuterium, the beryllium cylinder can be replaced by a thin-walled brass cylinder containing heavy water.

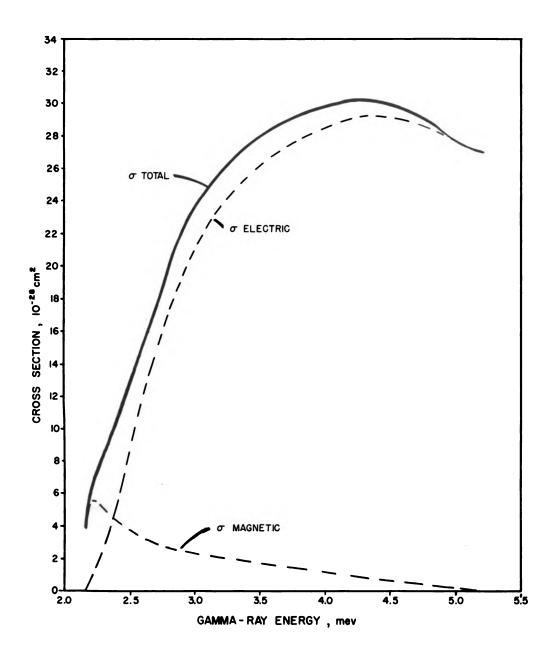


Fig. 1.1.7— The Cross Section for the Photodisintegration of the Deuteron as a Function of Gamma-ray Energy. Reprinted from A. Wattenberg, Photoneutron Sources, Prelim. Rep. No. 6, Nuclear Sci. Series, Nat. Res. Council, July 1949.

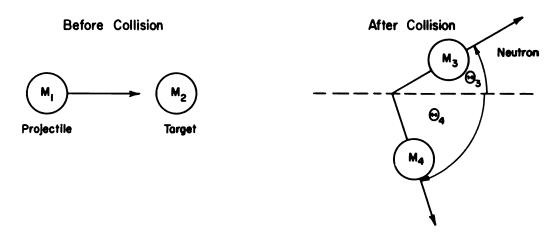


Fig. 1.1.8 — Schematic Drawing of a Two-body Collision in the Laboratory System.

It is assumed that the bombarding energy is not large enough to excite higher levels. For excergic reactions (positive Q), only the plus sign is used, and the neutron is monoergic at each angle θ_3 .

For endoergic reactions (negative Q), the reaction cannot proceed unless:

$$\mathbf{E_1} = \mathbf{E_{threshold}} = -\mathbf{Q} \frac{(\mathbf{M_1} + \mathbf{M_2})}{\mathbf{M_2}} \tag{17}$$

At the threshold, the neutrons are emitted only at $\theta_3 = 0$ and travel, together with the target residue, with the velocity of the center of mass. As E_1 increases, the neutrons are emitted into a cone in the forward direction with a limiting angle given by:

$$\cos \theta_3 = \sqrt{\frac{M_4(M_3 + M_4)}{M_1 M_3}} \left[\frac{M_1}{M_4} - 1 - \frac{Q}{E_1} \right]$$
 (18)

The energy of the neutrons at each angle θ_3 within the core is double-valued and is given by Eq. (16) with both plus and minus signs before the radical. When E₁ reaches the value:

$$\mathbf{E}_{1}' = \frac{-\mathbf{M}_{4}}{\mathbf{M}_{2} - \mathbf{M}_{3}} \mathbf{Q} \tag{19}$$

the neutrons are emitted in all directions with a unique energy at each angle, as in the case of positive Q.

The most important reactions now in use¹² having high-neutron yields and requiring low bombarding energies are shown in Eqs. (20), (21), and (23) to (28).

$$D^2 + D^2 \rightarrow He^3 + n^1 + 3.256(\pm 0.018) \text{ mev}$$
 (20)

For deuteron energies of 400 kev or less, the neutron energy will be $\simeq 2.5$ mev at 90°. The total cross section is of the order of 0.1 barn for E_D of 1 to 3 mev and decreases to 0.02 barn below 1 mev. As an approximate monitor for neutron intensity, the companion reaction $D(d,p)H^3$ can be used since the protons have nearly the same yield and angular distribution and have an energy of about 3 mev. The present usefulness of the D,D source

lies in its ability to provide neutrons in the energy range of 4 to 7 mev. Such neutrons are not available from $T(p,n)He^3$ and $Li^7(p,n)Be^7$ sources in existing accelerators with controlled voltages.

$$T^3 + D^2 \rightarrow He^4 + n^1 + 17.577 \text{ mev}$$
 (21)

This reaction can produce neutrons having energies from 12 to 20 mev. Because of the large value of the cross section at a few hundred kev, large quantities of 14-mev neutrons (about 10^8 n/ μ coulomb of deuterons) can be produced utilizing thick targets. The reaction can be accurately monitored by counting the alpha particles. The total cross section is given empirically as a function of incident deuteron energy, E, in mev by:

$$\sigma(\mathbf{E}) = \frac{58e^{-1.72/\sqrt{E}}}{\mathbf{E}\left[1 + \left(\frac{\mathbf{E} - 0.096}{0.174}\right)^2\right]} \text{ barns}$$
 (22)

for 0 < E < 2.5 mev

$$N^{14} + D^2 \rightarrow O^{15} + n^1 + 5.122 \text{ mev}$$
 (23)

This reaction has a differential cross section ranging from $\frac{1}{4}$ to $\frac{1}{2}$ of the D-D reaction. Its usefulness will be as a monoergic neutron source filling the energy gap between the D+D and D+T reactions.

$$C^{12} + D^2 \rightarrow N^{13} + n^1 - 0.281 \text{ mev}$$
 (24)

Yield is low, and there is a contamination of about 1 percent of high-energy neutrons coming from:

$$C^{13} + D^2 \rightarrow N^{14} + n^1 + 5.317$$
 mev.

The source has the advantage of a low threshold.

$$Li^{7} + H^{1} \rightarrow Be^{7} + n^{1} - 1.645 \text{ mev}$$
 (25)

The total cross section is about 0.2 to 0.5 barns for proton energies in the range 1.9 to 2.5 mev. To obtain usable yields of monoergic neutrons below 80 kev, it is necessary to use very large proton currents on thin targets and to observe at back angles.

$$T^3 + H^1 \rightarrow He^3 + n^1 - 0.764 \text{ mev}$$
 (26)

Large neutron yields near threshold. Monoergic neutrons up to 5 mev. Contamination by 20-mev gammas from proton capture by T³ can interfere with neutron detection. With the same tritium target, one can shift from low-energy neutrons to high-energy neutrons by changing from a proton beam to a deuteron beam.

$$V^{51} + H^1 \rightarrow n^1 + Cr^{51} - 1.50 \text{ mev}$$
 (27)

Very thin targets can be easily made, and with a well defined proton beam, monoergic neutrons in the range 2 kev to 20 kev can be produced. The energy is roughly independent of angle in this region. The neutron intensity is distributed more symmetrically than in the Li(p,n) reaction.

$$Sc^{45} + H^1 \rightarrow Ti^{45} + n^1 - 2.8 \text{ mev}$$
 (28)

This reaction is similar to the (V,p) reaction, and the yield at threshold is about 40 times as great.

REACTOR NEUTRON SOURCES13

The reactor can be used as an internal source by simply placing materials to be bombarded inside the reactor or by sending them through the reactor via a pneumatic tube (rabbit). ¹⁴, ¹⁵ The latter is used when the activities produced have a short half-life (order of seconds). It was applied to the measurement of delayed neutrons in fission. ¹⁵ External beams of neutrons can be obtained by piercing a hole or extending a thermal column (block of graphite) through the shielding of the reactor.

In a thermal reactor, the highest thermal flux is found inside the reactor, but the thermal column yields thermal neutrons with negligible contamination by intermediate neutrons. A material can be irradiated with the highest flux of fission neutrons by being placed inside a hollow lump of centrally located fissionable material. Thermal neutron contamination can be removed by wrapping the sample with Cd, but intermediate neutrons are still present. Fission neutrons free from intermediate neutrons are obtained by allowing thermal neutrons (from a graphite column) to fall on a plate of fissionable material. The sample or target may be wrapped in Cd and held against the converter plate. Fast neutrons (15- to 20-mev) may be obtained by placing a mixture of Li compound and D_2O inside the reactor. The neutrons are produced by the consecutive reactions:

$$\operatorname{Li}^{6}(n,\alpha)\operatorname{H}^{3}$$

 $\operatorname{H}^{2}(\operatorname{H}^{3},n)\operatorname{He}^{4}$

Samples may be irradiated by neutron fluxes of varying median energies by placing them inside variously designed filter arrangements as described later under "Filters."

Since the detailed space-energy distribution of the flux depends strongly on the particulars of the reactor, the following remarks are restricted to approximate results of a general nature. Some data appear in the Appendix which lists flux values inside several reactors

The energy integrated flux, $\Phi(r) = \int \phi(r) dE$, when averaged over the fuel-bearing regions of the reactor to give $\overline{\Phi}$, is related to the specific power and to the energy spectrum by the formula:

$$\bar{\Phi} = \frac{1.2 \times 10^{13}}{b} \frac{P}{M}$$
 (29)

where P is the power in kilowatts, M is the mass of fissionable atoms in kilograms, and b is the fission cross section in barns per fissionable atom averaged over the energy spectrum whose average integrated flux is $\overline{\Phi}$. Thus, in a thermal reactor, b is simply the thermal cross section, and:

$$\overline{\Phi}_{th} \approx 2 \times 10^{10} \, \frac{P}{M}$$
, for b ~ 600

while in a very fast reactor, $b \sim 2$ and:

$$\overline{\Phi} \approx 5 \times 10^{12} \frac{P}{M}$$
, for b ~ 2

It is seen that a fast reactor has a much larger flux for the same specific power. Equation (29) applies to the local core values of $\Phi(r)$ (as well as to the average, $\overline{\Phi}$) if P/M and b are regarded as local values. Thus, $\Phi(r)$ varies with position because of



buckling (variation in P/M) and because of variation in energy spectrum (variation in b). Bare reactor distributions for uniform loading in simple geometries are given in Table 1.4.3 and the maximum-to-average ratios, $\Phi_{\rm max}/\overline{\Phi}$, are listed in Table 1.1.6. The effect of a reflector is usually to lower the values of $\Phi_{\rm max}/\overline{\Phi}$ towards unity.

Table 1.1.6 — Maximum-to-Average Flux Ratios for Bare Reactors with Uniform Loadings in Simple Geometries

(CL-697, Chapter IVE; MonP-147)

Geometry	$\phi_{ m max}/\phi_{ m av}$			
Infinite slab	1.57			
Sphere	3.29			
Circular cylinder	3.64			
Rectangular parallelepiped	3.88			
Hemisphere	4.38			

The net leakage of neutrons into the reflector is equal to the excess of production over absorption in the core and is given by:

$$L = 3.3 \times 10^{10} \ \nu \, \frac{k-1}{k} \, \frac{P}{A} \tag{30}$$

where L is in neutrons per cm² per sec., P is the power in kilowatts, and A is the core surface area in square feet. ν and k have their usual meanings. If diffusion into the reflector is governed by a one-group theory, then the flux Φ at a distance s into the reflector is given by:

$$\Phi \approx \frac{L}{D\left(K + \frac{1}{a}\right)} \frac{e^{-Ks}}{1 + \frac{s}{a}} \tag{31}$$

where D and K are respectively the diffusion constant and inverse diffusion length of the reflector material, and "a" is the radius of the assumed spherical core.

If a hole of cross-sectional area A is pierced through the shielding and reflector terminating at the core-reflector boundary, a rough formula that gives the beam intensity at a distance r from the core-reflector boundary is:*

$$\Phi \approx \frac{LA}{4r^2} \tag{32}$$

where L is given by Eq. (30). If the hole terminates at a different position inside the reactor, the quantity L in Eq. (32) should be multiplied by the ratio of the flux at the termination position to the flux at the core reflector boundary. Also, the distance r is somewhat changed, when considering a fixed position outside the shield.

^{*}The product LA is the total leakage from the end face; $1/2\pi r^2$ is the fraction hitting a square centimeter at r if the leakage is directed uniformly, and $\pi/2$ is the factor measuring the forwardness of the leakage. The contribution to the intensity from the reflector lateral surface of the hole is small, especially when r is large compared to the reflector thickness.



The above considerations for a beam may be adapted to yield approximate formulas for the leakage into a thermal column. Rough formulas for the transmission through the column of both thermal and fast neutrons (T_{th}) and T_{th} appear below:

$$T_{th} \approx e^{-Kx}$$
 (33)

$$K^2 = \frac{1}{L^2} + \frac{2\pi^2}{A}$$

$$T_f \approx e^{-2\pi^{2\tau/\Lambda}} \left[1 - F\left(\frac{x}{2\sqrt{\tau}}\right) \right]$$
 (34)

where x is the length of the column, A the cross-sectional area (assumed square), L the thermal diffusion length, τ the age of the fast neutrons entering the column, and F the error function. The fraction, $T_{f,th}$ of entering fast neutrons which emerge as thermals is:

$$T_{f,th} \approx e^{\tau/L^2} e^{-x\sqrt{1/L^2 + 2\pi^2/A}}$$
 (35)

The above formulas for T_f and $T_{f,th}$ are based on plane-geometry age-theory* and neglect any $1/r^2$ attenuation.

The energy spectrum in a large thermal-reactor core consists of a thermal group† of flux Φ_{th} and of above-thermal neutrons of constant flux θ per unit logarithmic energy interval dE/E. Neglecting leakage, Φ_{th} and θ are related by:

$$\theta = \frac{\sigma_{a,th}}{\xi \sigma_{s}} \Phi_{th} \tag{36}$$

The cadmium ratio, C.R., is defined by:

$$C.R. = \frac{\text{activation of bare foil}}{\text{activation of Cd-covered foil}}$$

C.R.
$$\approx \frac{\theta \int_{0.4 \text{ ev}}^{\bullet} \sigma_{\text{act}} \frac{dE}{E} + \Phi_{\text{th}} \sigma_{\text{act,th}}}{\theta \int_{0.4 \text{ ev}} \sigma_{\text{act}} \frac{dE}{E}}$$
 (37)

and gives:

$$\theta \approx \frac{1}{C.R. - 1} \frac{\sigma_{act, th}}{\int_{0.1.17}^{\infty} \sigma_{act} \frac{dE}{E}} \Phi_{th}$$
 (38)

For a 1/v absorber ($\sigma_{act} = b/v$) and taking $E_{th} = 0.025$ ev, Eq. (38) becomes:

$$\theta \approx \frac{2\Phi_{\rm th}}{({\rm C.R.}-1)}$$

^{*}See Chapter 1.3 for a discussion of validity.

[†]In an approximate Maxwell distribution. See Chapter 1.3.

MOCK FISSION SOURCES

The U²³⁵ fission neutron energy spectrum (for fissions induced by thermal neutrons) can be represented approximately by the analytical expression (intensity normalized):¹⁶

$$\mathbf{F}(\mathbf{E}) = 0.475 \sinh \sqrt{2\mathbf{E}} e^{-\mathbf{E}} \tag{39}$$

This equation gives 0.72 mev for the most probable energy of a fission neutron; 2 mev for the mean energy; and 1.58 mev for the median energy.

The spectrum can be imitated¹⁷ by a source consisting of a mixture of sodium fluoroborate (NaBF₄) and sodium fluoroberyllate (2NaF·BeF₂) with a mole ratio of B/Be = 96/4 impregnated with Po. By carefully mixing and compressing to a pill, a source strength of 2×10^5 /(curie)(sec) can be attained.

PRODUCING MONOERGIC NEUTRONS BELOW 10 KEV

Above 10 kev in energy, photoneutron sources and charged particle accelerators are the best methods for obtaining monoergic neutrons. Below this energy, other methods are used. These include time-of-flight spectrometers, crystal monochromators, scattering filters, 1/v filters, and resonance filters. These methods do not produce neutrons directly but select neutrons out of a beam and then transmit them (or the remainder, in the case of absorbers) with the exception of the time of flight spectrometer. This instrument can only select neutrons. A general discussion of these methods is given by Hughes. 13

TIME-OF-FLIGHT SPECTROMETER

The neutron energy is determined by measuring the time the neutron takes to traverse a known distance. The neutrons are produced in bursts either by pulsing a charged accelerator source 18,19,20,21 or by rotating a mechanical chopper in front of a reactor neutron beam. 22,23,24 The time is measured by registering only those counts from a detector which take place after a known delay with respect to the time of the burst. Many such channels with known delays are operated simultaneously. This greatly increases the relative accuracy of the spectrum as well as reducing the time needed to go through the spectrum.

The neutron energy is related to the time of flight by:

$$\mathbf{E} = 5150/(t/m)^2 = \text{electron volts} \tag{40}$$

where: t = time in microseconds m = path length in meters

The customary manner for designating the resolution is the uncertainty in time measurement per unit path length (inverse velocity) with the units of microseconds per meter, $\Delta t/m$. Then the energy resolution is given by:

$$\frac{\Delta E}{E} = -2 \frac{\Delta t}{t} \tag{41}$$

and the energy spread by:

$$\Delta E = -0.028 E^{3/2} \frac{\Delta t}{m} \tag{42}$$

The energy resolution drops as \sqrt{E} which ultimately sets an upper limit to the usefulness of a given instrument. Δt is determined mainly by the burst and detection widths while the

path length, m, is limited by intensity considerations. If the burst width and detection widths are rectangular, then the resulting spread in time of flight for those neutrons detected will be triangular. Actual resolution functions are roughly triangular and the spread is generally given now by the full width at half maximum. (Formerly the width of the base was used.) The most efficient operation (maximum counting rate for a given resolution) is obtained when the burst time and detector time are made equal. Table 1.1.7 lists the

Table 1.1.7—Time-of-Flight Selectors Now in Operation for the Energy Region 10 ev - 10 kev

(Hughes, Conf. on Classified Nuclear and Reactor Physics at Oak Ridge, Sept. 1952,

ORNL-52-9-9)

Machine	Sample size	Δt,* μsec	Flight path, m	Resolution, µsec/m
Columbia cyclotron	Large	5	10	0.5
Argonne chopper	Small	5	20	.25
Oak Ridge chopper	Small	12	12	1.0
-		6	40	0.15
Brookhaven cyclotron	Large	2	7	.3
GE Betatron	Large	2	10	.2
Harwell el. acc.	Large	(†)	• • •	.5
Brookhaven chopper	Small	2	20	.1
		1	20	.05

^{*} Full width at half max. of resolution function, including burst width, counting channel time, detector length, and the like

machines useful in the range 10 ev to 10 kev with their resolutions in inverse velocity and their operating status. The Brookhaven fast chopper which has the highest resolution has an energy resolution of 0.4 percent at 10 ev and 14 percent at 10 kev.

In fast choppers, the shutter is a long, rotating, steel cylinder with slits down the outside edge which permit neutrons to pass when the slits line up with similar slits in a stationary collimator. In general, the counting rate per channel is independent of rotor speed because the fractional open time of the rotor is independent of motor speed. However, the burst width is reduced by increasing the speed so the resolution can be sharpened. The upper limit is set by mechanical strength considerations as well as intensity, i.e., the counting rate decreases with sharpening of the resolution. Speeds of 10,000 to 20,000 rpm are used. To increase the counting rate, the space between the source and detector is evacuated to eliminate air scattering of the neutrons. This adds an improvement of 5 to 6 percent per meter. It has also been suggested that a scintillation counter be used in place of the usual BF₃ detector which has a low efficiency at high energies (hundreds of ev).

For examining thermal neutrons and cold neutrons (<0.01 ev), a slow chopper is used. This is of simpler design since thin cadmium can be used to stop the neutrons and longer bursts are permitted. A slow chopper of more advanced design has been built at Brookhaven using curved neutron channel paths. This selects the velocity of the neutrons to some extent as well as letting them pass so the duty cycle can be increased. The lower limit to the energy which can be measured is set by the overlap between successive bursts. It can be reduced by slowing down the chopper but this reduces the resolution

[†] The minimum $\Delta t = 4\mu secs$, m = 10, giving a resolution of 0.4 $\mu sec/m^{21}$

because the burst width is increased. Measurements down to 0.0004 ev have been reported using the Brookhaven slow chopper (see Neutron Cross Sections, AECU-2040).

Pulsed cyclotron techniques suffer from two disadvantages compared to the mechanical shutter reactor method: They have less intensity, and they have a beam 50 to 100 times the size of the beam which can be used with a shutter. Much smaller sources (milligrams) can be used with the shutter method.

The time-of-flight spectrometer and the crystal monochromator have the highest resolution of all the low-energy-neutron sources. The following comparison is taken from Selove.²⁴

The variation of resolution with energy is the same for the crystal and the chopper. For a given available beam size at the reactor, the crystal can give higher counting rates than the chopper by a ratio of about $50/(\Delta E/E)$, where $\Delta E/E$ is the fractional energy resolution. The crystal also has an advantage over the chopper in giving an essentially monoenergetic beam, thus making possible activation measurements, for example, as a function of energy. Since the time-of-flight spectrometer can only select neutrons of a given energy, it can only be used to measure transmission through a sample. However, there are many points in favor of the chopper. It does not suffer from the higher-order contamination present in the reflected beam from a crystal (owing to overlapping of orders). (No longer true; see below). The lower counting rate of the chopper is offset by the possibility of measuring at as many as 50 to 100 energies simultaneously; moreover, the fractional background is much smaller for the chopper, especially at higher energies. For fixed construction, the resolution of a chopper is easily adjustable; that of a crystal is not. Finally, the problems in the development and construction of a chopper spectrometer appeared to be much simpler than for a crystal spectrometer of comparable performance, the most uncertain feature of the latter being to obtain a large crystal specimen of suitable composition, mosaic structure, and curvature.

CRYSTAL MONOCHROMATOR

Neutrons can undergo Bragg reflection from a crystal lattice in the same manner as X-rays. Only those neutrons will reflect which satisfy the Bragg equation:

$$n\lambda = 2d \sin \theta \tag{43}$$

where: λ = neutron wavelength

d = lattice spacing

 θ = glancing angle for the nth order reflection

The wavelength is related to the neutron energy in electron volts by:

$$\lambda = \frac{0.2861}{\sqrt{E}} = \text{Angstroms} \tag{44}$$

Neutrons in the thermal region have wavelengths corresponding to crystal-lattice spacings (a few Å).

Because of the finite range of incident angles $(\Delta \theta)$, there will be a corresponding range of reflected wavelengths $(\Delta \lambda)$ centered at the wavelength given by Eq. (44).

The resolution is a function of θ only and is given by:

$$\frac{\Delta \lambda}{\lambda} = \cot \theta \, \Delta \theta$$

$$\frac{\Delta E}{E} = 2 \, \frac{\Delta \lambda}{\lambda}$$
(45)

The lowest possible order is used because the crystal reflectivity varies as $1/n^2$. The reflectivity also varies as 1/E, and because of the high collimation needed (of the order of 0.1°), the intensity of the neutron source beam must be quite high. The method is feasible only with reactor neutron sources.

The crystals in use are LiF and, more recently, Be. The former has a d of 2.32 Å for the (111) plane and will give a resolution of 16 percent at 10 ev for a $\Delta\theta$ of 0.1°. A Be single crystal has an unusually small d of 0.75 Å for the (421) plane, and in the Brookhaven instrument using this crystal with a $\Delta\theta$ of 9 min, a resolution of 10 percent 50 ev and 1 percent at 1 ev is attained. Because of the loss in resolution, 10 ev is the present useful upper energy limit. The lower limit is the thermal region. Below 0.03 ev, the higher-order reflections coming from the intense thermal region cause too much interference. Recently, however, it has been shown that by taking advantage of the total reflection properties of mirrors for neutrons incident at very small glancing angles, it is possible to eliminate higher-order reflections in the beam from the crystal. In this way, the range has been extended to 0.005 ev or lower, depending on the intensity available. 16

Since the instrument produces a beam of monoergic neutrons, in contrast to the timeof-flight spectrometer, it can be used for activation and scattering experiments as well as measurements of total transmission.

To improve focussing and intensity, a bent-crystal spectrometer has been described. A quartz crystal is bent tangent to a Rowland circle with source and detector on the circle, as in the optical case. The lower energy limit is 0.03 ev because of higher-order reflections interfering, and the upper limit is 0.7 ev because of intensity losses and rise in background. An energy resolution of 2 percent at 0.028 ev is claimed. Samples of the order of milligrams can be examined.

FILTERS

Filtration by Absorbers

Filters of various elements can be used to absorb or transmit certain sections of thermal and resonance neutrons. The method is crude but simple and does not require high-intensity neutron sources. There are three cases of practical importance, based on a study of the Breit-Wigner equation for one-level capture cross section, $\sigma(E)$:

$$\sigma(\mathbf{E}) = \left(\frac{\mathbf{E}\mathbf{r}}{\mathbf{E}}\right)^{\frac{1}{2}} \frac{\sigma_0}{1 + \left(\frac{\mathbf{E} - \mathbf{E}\mathbf{r}}{\Gamma/2}\right)^2} \tag{46}$$

where: Er = energy of resonance level

 $\sigma_0 = cross section at Er$

 Γ = total width of level

Case 1: Γ ≫ E

For the $B^{10}(n,\alpha)Li^7$ and $Li^6(n,\alpha)H^3$ reactions, Γ is about 10^4 ev; these absorbers will therefore be 1/v in nature for all neutrons below 10^3 ev. This means that such neutrons are absorbed exponentially with absorber thickness and that the effect on the neutron distribution can be calculated.

Case 2: Γ ~ Er

For radiative neutron capture, $\Gamma \sim \Gamma r \sim 0.1$ ev. The condition $\Gamma \sim Er$ is equivalent to saying that a resonance occurs in or near the thermal region (examples: Cd, Gd, Sm, and Dy). Cd is the most common thermal absorber and below 0.1 ev has an average cross

EXPERIMENTAL METHODS CHAP. 1.1

section of about 3000 barns. Thus, the transmission of such neutrons through a 0.5-mm thick cadmium sheet will be less than 1 percent. The cut-off energy for cadmium is usually taken as 0.4 ev where the cross section is 300 b.

Case 3: $\Gamma \ll Er$

This implies that Er > 1 ev. Absorption is 1/v throughout the thermal region, and in the neighborhood of Er, the cross section rises steeply to orders of 10^3 to 10^5 barns. The important resonance absorbers and their energies are:

Rh 1.25 ev In 1.44 ev Au 4.9 ev Ag 5.1 ev

Filtration By Scatterers

The Bragg relation, Eq. (43), shows that the longest wavelength that can be reflected by a given crystal occurs when $\sin \theta = 1$:

$$\lambda_{\mathbf{m}} = 2\mathbf{d}_{\mathbf{m}} \tag{47}$$

where: d_m = maximum lattice spacing in the crystal

Neutrons of wavelength greater than λ_m are essentially not scattered at all (except for incoherent scattering which is usually small) and are removed from the beam only by capture.

Since capture cross sections vary as 1/v, filters for cold neutrons (<0.01 ev) must have a very low capture cross section. Also wavelengths greater than λ_m should be highly scattered so that a clean break can be achieved. Only graphite and beryllium oxide have these properties. Unfortunately, they both cut off in the same wavelength range, 4 to 7 Å (0.002 - 0.005 ev).

NEUTRON DETECTION

A variety of neutron detectors have been developed although slow-neutron detectors (up to 0.1 mev), and fast-neutron detectors cannot generally be used interchangeably. If it is desired to analyze the energy spectrum, the procedure becomes more elaborate, and efficiency is usually sacrificed. Only properties of the detectors will be discussed here, but a brief summary and bibliography for work done through 1950 is available.²⁷ References for construction details will be given throughout the section.

SLOW-NEUTRON DETECTORS

Ionization chambers and proportional counters containing boron either as a coating on the walls and electrodes or as a BF₃ filling can be made into highly efficient detectors. The reactions utilized are:

$$B^{10} + n^1 \rightarrow He^4 + Li^7 + 2.792 \text{ mev}$$
 (48)

$$B^{10} + n^{1} \rightarrow He^{4} + Li^{7}* + 2.314 \text{ mev}$$

$$Li^{7}* \rightarrow Li^{7} + 0.478 - \text{mev gamma}$$
(49)



The branching ratio of the two states may be strongly energy dependent.²⁸ At thermalneutron energies, the excited state is produced 93 percent of the time. The cross section is almost pure 1/v up to 10-kev neutron energies. This holds if pure B^{10} is used, but if normal boron is used, scattering will limit the 1/v effect to 1 kev. For a 1/v-absorber, the counting rate is proportional to the total neutron density, ρ (neutrons/cm³), since:

$$\mathbf{R} = \mathbf{N}\mathbf{V} \int \mathbf{n}(\mathbf{v}) \ \mathbf{v} \ \sigma(\mathbf{v}) d\mathbf{v} \tag{50}$$

but: $\sigma(v) = \sigma_0 v_0 / v$

therefore: $R = NV \sigma_0 v_0 \rho$ and $\rho = \int n(v) dv$ (51)

where: R = reaction rate in counts/sec

N = No. of B^{10} atoms per cc

V = sensitive volume of chamber in cc

n(v) = neutron density distribution in speed, i.e.

n(v)dv = no. of neutrons per cm³ with velocities between v and v + dv

v = neutron velocity

 $\sigma(v) = cross section in cm²$

 σ_0 , v_0 are at same arbitrary energy, say

E = 0.025 ev where $\sigma_0 = 3960$ barns, $v_0 = 2200$ meters/sec

Ionization counters are somewhat simpler to build and operate, but proportional counters offer better pulse discrimination against gamma-ray background, better energy resolution, and are less sensitive to electrical pick-up.* Boron is easier to handle and preserve than BF₃ gas which must be carefully purified;^{30,31} however, the gas should give cleaner pulse discrimination in a proportional counter. Using separated B¹⁰ will, of course, increase the detection efficiency by a factor of 5. In a B¹⁰F₃ counter, the detection efficiency can approach 100 percent if sufficiently large dimensions and high pressures are used. Typical dimensions for cylindrical BF₃ proportional counters are: diameter, 1 to 2 in.; length, 12 to 24 in.; gas pressure, 60 to 110 cm Hg; operating voltage, 2000 to 4000 v. To obtain high efficiency, the neutrons must be sent down the counter axially. An ultimate sensitivity of less than 1 neutron/sec can be attained. If the sensitive volume is accurately known, the absolute neutron density can be measured using Eq. (51).

At the other extreme in size, Lowde³² describes a 12-chamber ionization chamber that uses thin films of separated B¹⁶ isotope on alternate electrodes and which has an active volume of 0.4 cm³, over-all dimensions of about 1 by 2 in., and a thermal-neutron efficiency of 24 percent. The counter is filled with argon to 5 atm pressure and operated at 70 volts.

FISSION COUNTERS

If the gamma background is so high that the pile-up of electron pulses exceeds that of the alpha pulses from either B or BF₃, then the fission process can be utilized in place of boron since the fission fragments give much larger pulses. U²¹⁶ as enriched U₃O₈ or Pu²³⁹ can be placed on multiple-electrode ion chambers, and efficiencies comparable to or higher than those using boron can be attained. Rossi and Staub²⁹ describe a spirally wound electrode foil assembly which can have useful areas of several hundred square centimeters and occupies only one cubic inch. A much larger integrating type of fission ion chamber having multiple plates (also described by the above authors) is suitable for relative flux measurements in very dense slow-neutron atmospheres.

^{*} A study of the parameters involved and many constructional details for these types of counters as well as recoil and fission counters are given in Rossi and Staub.²⁹



EXPERIMENTAL METHODS CHAP. 1.1

INDUCED RADIOACTIVITY

Elements with a large activation cross section for the (n,γ) reaction and whose products are radioactive can be used in the shape of foils to detect slow neutrons. A big advantage of such foils is their complete insensitivity to gammas of less than 6 mev energy. Another advantage is the small space they occupy (a square inch or less in area and mils in thickness). However, they are not satisfactory for continuous monitoring purposes since the foils must be removed and counted. A list of useful detectors is given in Table 1.1.8 with

Table 1.1.8—Some Useful Neutron Detectors Based on Induced Radioactivity
(Data taken from Neutron Cross Sections, AECU-2040 and Nuclear Data, NBS Circular 499)

Element		σ,				Important	resonances
or isotope	Isotope		$\sigma_{ m act}$ (thermal), barns	Half-life o activity*		Energy,	Peak σ, barns
Mn ^{\$\$}	100	12.6 ± 0.6	12 ± 2	2.6 hr	β, γ	310	50‡
						2900	29
						8200	27
Rh ¹⁶³	100	150 ± 7	12 ± 2	4.3 min	0.08γ	1.25	4 500
			140 ± 30	44 sec	2.6 y		
Ag		60 ± 3				5.1	7700
Ag 107	51.9	30 ± 2	44 ± 9	2.3 min	2.8 β		
Ag 100	48.1	84 ± 7	2.8 ± 0.5	270 days	β, γ		
			110 ± 20	24.5 sec	β, γ		
In		190 ± 10				1.44	27500
						3.9	460
						9.1	125
In ¹¹³	4.2		56 ± 12	50 days	0.192y		
			2.0 ± 0.6	72 sec	2β		
In ¹¹⁵	95.8		145 ± 15	54 min	β, γ		
			52 ± 6	13 sec	?		
Dy		1100 ± 150			-	1.7	350
-,						5.5	300
Dy 164	28.2		2600 ± 300 f	1.3 min	0.109γ	0.0	000
-,	20.2		<1000 \$	2.4 hr	β, γ		
Dy 166	(2.4 hr half-life)		5000 ± 2000	81 hr	0. 4 β		
Au ¹⁹⁷	100	94 ± 1	96 ± 10	2.7 days	$0.97\beta \rightarrow 0.411$	y 4.9	15000
Au ¹⁹⁶	(2.7 days half-life		18000 ± 8000\$	3.3 days	β, γ	7.0	2000
	/a oals man-m	-,	TOOOR # 90008	Ja uays	F. 1		

^{*} Arrow means isomeric transition

their thermal-absorption and activation cross sections, the half-life of the resulting activity, the type of radiation emitted, and the more important resonances.

Indium is the most common element used for thermal (0.01 to 0.4 ev) and epithermal (>0.4 ev) neutrons. By measuring activities with and without a cadmium cover around the indium, thermal and epithermal neutrons can be separated since cadmium absorbs thermal neutrons strongly and is relatively transparent to neutrons above 0.4 ev. In using this

[†] Numbers are energies in mev; β , γ means complex spectrum

[‡] Mn resonances are mostly scattering

[§] Reactor neutrons

method, the following precautions and corrections should be made in order to interpret the counting rates correctly. 33,34

- (1) The 54-min activity is the one measured, and the foil should be allowed to stand at least 3 min before counting to allow the 13-sec activity to die out.
- (2) If the beta rays are counted, the optimum foil thickness for counting thermal neutrons is about 125 ± 25 mg/cm². With thicker foils, the counting rate drops because of internal absorption of betas and the "self-protection" of the absorber. The internal absorption effect can be reduced greatly if the gamma radiation (in a scintillation counter, for example) is counted instead of the beta rays (but see Note 4 below). The "self-protection" effect, which is the depression of the neutron flux around the absorber owing to the high absorption rate, can be corrected by Bothe's equation in the case of thermal neutrons. The factor by which the counting rate should be multiplied is:

$$\mathbf{F_{sp}} = 1 + \frac{\alpha}{2} \left[\frac{3R}{2\lambda_{tr}} \frac{\mathbf{L}}{R + \mathbf{L}} - 1 \right] \text{ if } R > 2\lambda_{tr}$$
 (52)

$$\mathbf{F_{sp}} = 1 + \frac{0.34 \ \alpha R}{\lambda_{tr}} \text{ if } R \ll \lambda_{tr}$$
 (53)

where: R = foil radius

 λ_{tr} = transport mean-free-path in the medium around the foil

 α = probability that a neutron will be absorbed by the foil on one transversal.

Bothe gives an expression for α as:

$$\alpha = 1 - e^{-\mu d} (1 - \mu d) + \mu^2 d^2 Ei(-\mu d)$$
 (54)

where: μ = neutron absorption coefficient in the foil material

d = foil thickness

Ei = logarithmic integral³⁵

A plot of α vs d is given in Fig. 1.1.9; μ should be calculated at the effective energy for absorption of thermal neutrons which, for a 1/v absorber and a Maxwellian speed distribution, is $E_{\rm eff} = 4/\pi$ kT or 0.032 ev at 20°C.

The neutron diffusion length (L) in the medium around the foil is given by:

$$L^{2} = \frac{\lambda_{tr} \lambda_{a}}{3\left(1 - \frac{2\lambda_{tr}}{5\lambda_{a}}\right)^{2}}$$

where: λ_a = absorption mean-free-path = $1/N_a \sigma_a$

 $\sigma_a = \sigma_{a,thermal}/1.128$, i.e., at E_{eff}

 λ_{tr} = transport mean-free-path = $\lambda_{s}/[1 - (\cos \theta)_{av}]$

 λ_s = scattering mean-free-path

 $(\cos \theta)_{av}$ = average over angles of incidence on the foil. Above 1 ev, the scattering is isotropic in the center of mass system and $(\cos \theta)_{av} = 2/3A$; A = mass no. Table 1.1.9 gives diffusion constants at thermal energies for various media.

The calculated value for F_{sp} agrees very well with experimental observations, usually to 1 percent or better. Neither equation for F_{sp} can be used for the case of a small foil in a highly absorbing medium, but fortunately, here F_{sp} is close to unity.

(3) The cadmium absorbs some of the higher-energy neutrons. The correction depends on both the cadmium and indium thicknesses. The correct counting rate can be determined experimentally by measuring the counting rate at the given indium thickness for different cadmium thicknesses and extrapolating to zero cadmium thickness. Figure 1.1.10 gives

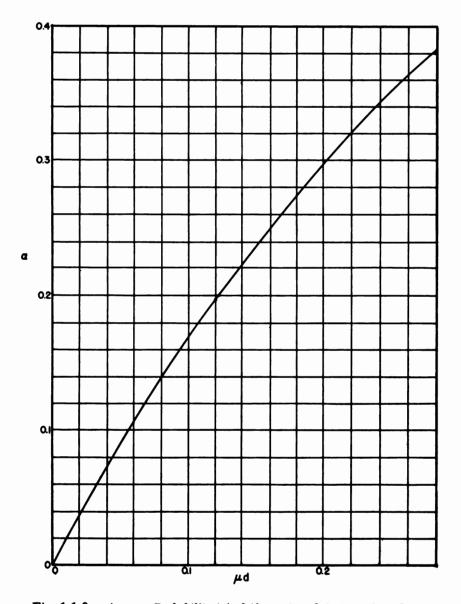


Fig. 1.1.9 — Average Probability (α) of Absorption of Neutrons in an Isotropic Flux Incident upon a Sheet of Material of Thickness d and Absorption Coefficient μ . Reprinted from Title. Nucleonics 9, No. 1, July 1951.

Table 1.1.9 — Diffusion Constants of Various Media

(Title.	Nucleonics,	9.	No.	1.	July	1951)
(* * * * * * * * * * * * * * * * * * *	ruciconics,	,	410.	-,	o u i j	1001,

Medium	Density, gm/c ³	L, cm	λ_{tr} , cm	λ _a , cm
Paraffin	0.895*	2.42 ± 0.04	0.395 ± 0.021	44.9 ± 1.9
Water	1.00	2.76	0.425	53.8
D ₂ O	1.1	171 ± 20	2.4	37,000
Be	1.8	31	2.6	1,100
Graphite	1.62*	50.2	2.7	2,800

^{*} Varies with the sample

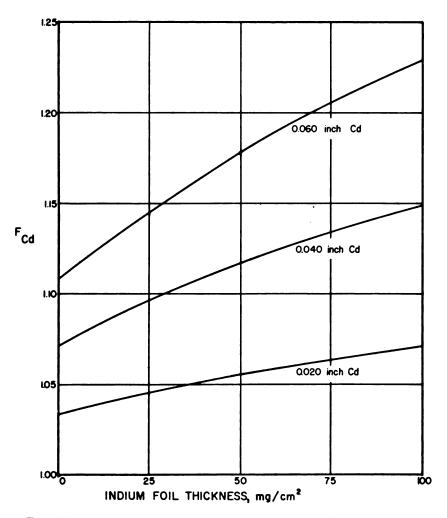


Fig. 1.1.10 — The Factor for Correcting Counting Rate of Indium Foils when Covered with Cadmium ($F_{\rm Cd}$) by Which the Counting Rate is to be Multiplied, Versus Indium Foil Thickness for Various Cadmium Thicknesses. Reprinted from Title, Nucleonics, 9, No. 1, July 1951.



EXPERIMENTAL METHODS CHAP. 1.1

F_{Cd} by which the observed rate is to be multiplied for indium thicknesses from 0 to 100 mg/cm² and for 3 cadmium thicknesses, 0.02, 0.04, and 0.06 in.

(4) If fast neutrons are present, the 4.5-hr isomeric state of In¹¹⁵ can be excited by inelastic collision. The level is at 0.37 mev and emits a gamma radiation which is 50 percent internally converted. The threshold is about 1 mev, and the cross section is constant at about 0.36 barn above 2.2 mev. This activation is usually small compared to the 54-min activity if short exposure times are used. Its effect on beta counting can be reduced somewhat by using a counter that is relatively insensitive to gamma radiation, e.g., a Geiger counter or an argon ionization chamber, of which the latter can be made the more stable.

The neutron-induced activity in the foil increases as:

$$C_0 = C_{0,sat} (1 - e^{-t/\tau})$$
 (55)

The counting rate can be corrected for decay back to the time at the end of exposure to neutrons and also to saturation activity by the equation:

$$C_{0,\text{sat}} = \frac{N}{\tau(e^{-t_1/\tau} - e^{-t_2/\tau})(1 - e^{-t/\tau})}$$
 (56)

where: t = length of exposure to neutrons

 t_1 = start of counting, measured from end of exposure

t₂ = end of counting, measured from end of exposure

 $N = number of counts (background subtracted) in time <math>t_2 - t_1$

 τ = mean lifetime of activity. For indium, τ = 77.8 min

Indium foils offer a sensitive method for slow-neutron detection, and intensities as low as 1 neutron/(cm²)(sec) can be measured. The lower limit is probably set by the natural activity of In¹¹⁵ which has recently been found to be a beta emitter with a half-life of about 10¹⁴ yr. Another sensitive method for thermal-neutron detection is to use manganese in an aqueous solution such as calcium permanganate.³⁶ The active Mn⁵⁶ precipitates out as MnO₂ by the Szilard-Chalmers process and can be filtered off and counted. With the source in the center of 11 liters of a 2.4 N solution of Ca(MnO₄)₂ surrounded by an external paraffin reflector, a detection efficiency of 8 percent and a sensitivity of about 1 neutron/sec can be obtained. This method is unaffected by gamma radiation provided the gamma energy is below the deuterium photoneutron threshold (2.23 mev). The deuterium in water limits the ultimate sensitivity.

Instead of using the Szilard-Chalmers reaction, $MnSO_4$ or CaI_2 can be dissolved in water and the active element precipitated out later. It may be easier and quicker, at the expense of sensitivity, to remove a small aliquot of the solution (after sufficient stirring) and treat this or count it directly. Although iodine has only half the activation cross section of manganese, the shorter half-life of I^{128} (25 min compared to 2.6 hr for Mn^{56}) makes iodine more convenient in some cases.

By using combinations of thermal and resonance absorbers, thermal-energy neutrons at energies of a few electron volts can be separated.

RESONANCE SCATTERERS

At higher energies of the order of a few hundred electron volts or a few kilovolts, neutrons can be detected by resonance scattering. The counter consists of BF₃ proportional counters embedded lengthwise in circles in a paraffin ring.^{37,38} The paraffin slows down the neutron and the detection efficiency is about 15 percent in the kilovolt region. The scatterer is placed in the center of the ring. Collimated neutrons must be used. For clear

interpretation, the scatter should have just one resonance or only a few widely-spaced resonances. Only a few elements satisfy this requirement. Table 1.1.10 shows three elements which may prove useful.

Table 1.1.10 - Some Useful Resonance Scatterers

Resonance		Total cross Neutron section at		Next-nearest resonance			
Element	energy, ev	width, ev	peak, barns	Energy, ev	Peak σ _t , barns		
Co	120	2.6	1100	6000	17		
Mn	345	13	50	2900	29		
Na	3000	170	50	55000	10		

PHOTOGRAPHIC EMULSIONS

Slow neutrons can be detected in a photographic emulsion by loading it with lithium and boron and counting the tracks of the reaction products under a microscope. 39,40,41 The reactions which will take place in an emulsion are listed in Table 1.1.11. Loading and developing of the emulsions must be done carefully to get uniform absorption and to be able to differentiate between alpha or triton tracks and proton tracks. Up to 72 mg B and 12 mg Li per cc of dry emulsion can be absorbed in 200 μ -Ilford C₂ plates from an aqueous solution of lithium tetraborate, and if separated B¹⁰ or Li⁶ is used, the detection efficiency approaches that of BF₂ counters; this is evident from the transmission curves of Fig. 1.1.11. The lithium and boron reactions can be easily distinguished by their different

Table 1.1.11—Neutron Reactions in Photographic Emulsions Loaded with Boron and Lithium Nuclei

(Kaplan and Yagoda, Rev. Sci. Inst. 23, 1952)

Reaction	$\mathbf{E_n}$	σ , barns	σN ,* cm ⁻¹
$B^{10}(n,\alpha)Li^7$	0.025 ev	3800 ⁸⁹	1.35
B ¹⁰ (n,p)Be ¹⁰	Thermal	< 0.289	$<7.1 \times 10^{-5}$
$B^{11}(n,\alpha)Li^8$	~1 mev	85 × 10 ^{-6 30}	1.31×10^{-7}
$Li^6(n,\alpha)H^3$	0.025 ev	910 ⁸⁹	6.96×10^{-2}
$\mathrm{Li}^{7}(\mathbf{n},\alpha)\alpha$	Thermal	0.033 ⁹⁰	3.18×10^{-5}
N4 (n,p)C4	Thermal	1.71 ⁹⁰	4.88×10^{-3}
H ¹ (n,p)	E	9.42/(E + 1) ^{91,92}	t

^{*}Based on the composition of Ilford C-2 plates loaded from a 10-percent lithium borate solution which picked up 3.56×10^{20} atoms of B^{10} and 7.65×10^{19} atoms of Li^6



[†] The loading process increases the normal hydrogen content of the emulsion by the addition of plasticizer and water of crystallization associated with the lithium borate compound. Measurements of neutron spectra from the ranges of proton recoil tracks are best made on a nonloaded plate

EXPERIMENTAL METHODS CHAP. 1.1

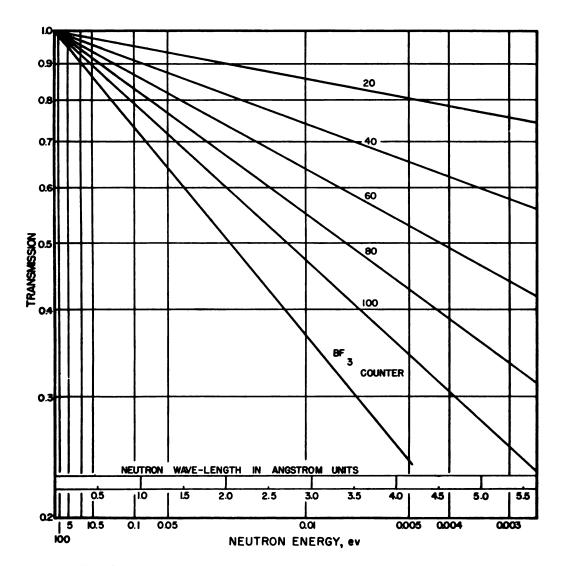


Fig. 1.1.11 — The Transmission in a Photographic Emulsion as a Function of Neutron Energy for 200-micron Ilford C2 B¹⁰-loaded Plates Containing Various Amounts of B¹⁰ in Milligrams per Cm³ of Emulsion. Reprinted from Blau. Ruderman, and Czechowski, Rev. Sci. Inst., 21, 1950. The cross section of B¹⁰ was taken to be $\sigma = 627^{-\frac{1}{2}}$ (E in ev). The transmission of a conventional BF₃ proportional counter, 10 cm long and filled to 50 cm pressure with pure B¹⁰F₃ is included for comparison.

lengths. The alpha and triton tracks from lithium are 180° apart and have a total length of about 44 microns while the alpha tracks from boron are 7 microns long. The proton recoils also present in the emulsion have a range of about 7 microns; therefore, tracks in a similar non-loaded emulsion must be counted and subtracted. Angular criteria, shrinkage factors (resulting from developing), and geometric escape factors are given in Kaplan and Yagoda. Either set of tracks can be used to obtain the neutron flux. The internal average deviation with B¹⁰ is 8 to 10 percent, with Li⁶, 10 to 15 percent, and between B¹⁰ and Li⁶, 10 to 15 percent. At sea level, the slow-neutron flux from cosmic rays was observed to be 240 ± 30 neutrons/(cm²)(day).

By selecting the proper emulsion, such as Ilford D_1 , the sensitivity to beta and gamma radiation can be kept relatively low. After an exposure of a D_1 plate to about 80 roentgens of gamma radiation the background was still low enough to allow short alpha or proton tracks to be counted easily.

SCINTILLATION COUNTERS

Efficient scintillation crystals and liquids used in conjunction with photomultipliers for detecting slow neutrons have only been reported very recently. Hofstadter et al⁴² have grown natural LiI crystals activated with 1 percent TII which will discriminate against gamma radiation by virtue of the much larger pulse height from the neutron reaction. Because of the large cross sections at thermal energies (910 b for Li⁶, 7.4 percent abundant, at 0.025 ev) a 1-cm-thick crystal of LiI will have almost 100 percent efficiency. By using a mixture of 7 percent Li⁶I and 93 percent NaI plus 0.1 to 1 percent TII, the pulse height can be greatly increased without loss of counting efficiency. An energy resolution of 7 percent is claimed.⁴³ Boron has not been successfully incorporated into crystals up to the present time, but Muehlhause and Thomas⁴⁴ have mixed an alkyl borate such as triethyl, tri-methyl, or tri-butyl borate with a terphenyl-phenyl-cyclohexane solution to get a scintillator which is 100 percent efficient for slow neutrons.

A combination of scintillation counter and induced activation techniques has been recently proposed by Grimeland⁴⁵ to measure absolute neutron densities. Advantage is taken of the 1/v capture cross section of Na²³ to activate a sodium iodide crystal mounted on a photomultiplier. The activity of Na²⁴ has a half-life of 15.06 hr while that of I¹²⁸ is only 25 min; the two activities can therefore be separated easily.

FAST-NEUTRON DETECTORS

Since the cross sections for fast neutrons are on the order of barns or fractions of a barn, fast-neutron detectors have a relatively low efficiency compared to thermal detectors, usually only a few percent or less. Most fast detectors are energy sensitive and can indicate the energy distribution to some extent. However, by surrounding the source with a moderator like water or paraffin of sufficient size, high-energy neutrons can be slowed down and detected by thermal counters or foils, or in the case of water, by dissolved manganese or iodine compounds as discussed under thermal neutrons. The efficiency in a water bath can be made to reach 100 percent, but the use of a bath is often awkward or impossible; a BF₃ proportional counter surrounded in a suitable manner is frequently used as a monitor for neutrons of all energies up to a few mev. 46,47 Such a counter is called a "flat-response" or "long" counter because the energy response is uniform between 1 and 5 mev and decreases to only 85 percent relatively at thermal energies. The neutrons are sent in axially. The lower efficiency at thermal energies is because of the higher probability that such neutrons will be reflected back from the paraffin and away from the counter. The absolute efficiency is about 1 percent or less.

PROTON RECOIL COUNTERS

Ionization and proportional counters filled with gases containing hydrogen atoms can detect fast neutrons by the ionization produced by the recoil protons. Hydrogen gas or methane is used, the latter having the advantage of a higher hydrogen content per molecule. Instead of a gas, a solid or liquid hydrogenous radiator can be put into an argon-filled counter. Glyceryl tristearate, $(C_{17}H_{35}CO_2)_3$ C_3H_5 , is preferred over paraffin because of its definite chemical composition. It can be evaporated to form thin, uniform layers of the order of microns. A great many types of such counters are described in Rossi and Staub, loc. cit. Skyrme et al⁴⁸ describe a cylindrical proportional counter filled with hydrogen or methane which can reproduce neutron-flux measurements to better than



5 percent in the energy range 0.1 to 1 mev. The efficiencies are of the order of tenths of a percent.

FISSION CHAMBERS

Fission chambers with coatings of pure thorium or separated U²³⁶ are useful for detecting energies above 1 mev.

THRESHOLD DETECTORS49

Activation of certain elements by (n,2n) or (n,p) reactions can be used to measure neutron energies and fluxes in the range 1 to 25 mev. The (n,2n) reaction offers a sensitive method for energy measurements above 9 mev while (n,p) reactions are suitable at lower energies. The latter reaction has a low cross section at threshold and thus is not a sharp detector. Tables 1.1.12 and 1.1.13 list convenient (n,2n) and (n,p) detectors and some quantities useful in correcting the observed counting rates.

The quantity measured by a threshold detector is:

$$I = \int_{B}^{\infty} F(E)\sigma(E) dE$$
 (57)

where: E = energy

B = threshold energy

F(E) = neutron flux distribution in energy

Experimentally, I is found from:

$$I = \frac{\lambda n_0}{Q[1 - \exp(-\lambda T)]}$$
 (58)

where: $\lambda = \text{decay constant of activity} = 0.693/\text{half-life}$

T = bombarding time

 $n_a = number$ of radioactive atoms at end of bombardment

Q = number of atoms of the reacting isotope per unit area perpendicular to the neutron beam

Ano is obtained from:

$$\ln\left(-\frac{dn}{dt}\right) = \ln(\lambda n_0) - \lambda t \tag{59}$$

where: $-\frac{dn}{dt}$ = rate of decrease of number of radioactive atoms

t = time after end of bombardment at which rate is measured

-dn/dt is obtained from the observed counting rate R measured in some counter by correcting for the geometrical solid angle the counter sees and for various scattering and absorption effects on the radiation counted. If betas are counted, correcting for self-absorption in the detectors is usually important. The absorption of the betas can be represented in an approximate manner by an exponential relationship:

$$\mathbf{F} = \mathbf{e}^{-d/\alpha} \tag{60}$$

where: F = fraction transmitted per unit incident intensity

d = absorber thickness

 $\alpha = 1/e$ thickness, a constant depending on maximum beta energy and approximately independent of the absorbing material

Table 1.1.12 — Convenient (n,2n) Threshold Detectors

(Cohen, Nucleonics 8, No. 2, Feb. 1951)

Other activities	None	20.5 min carbon (n, 2n)	20.5 min carbon (n,2n)	None	170 min (n,p)	3.9 min (n,p)	2.6 hr (n, γ) ; 72d (n, p)	26.8 hr (n, y)	2.3 min (n, y); 13h (n,p)	2.8 days (n,γ)	25 min (n, y)	Long
Approximate α,† mg/cm²	70	100	170	9	4 00	240	4	82	220	160	75	360
K-capture correction*	1.00	1.00	1.00	1.00	1.00	1.00	3.0	1.3	2.3	3.0	7.0	1.6
Convenient material	Graphite	Urea	Cellophane	Lif	(NH,)H, PO,	Crio	Ni metal	As ₂ O ₃	Ag metal	Sp. 03	NH,I	Pr_6O_{11}
Half-life	20.5 min	10.1 min	2.1 min	112 min	2.55 min	42 min	36 hr	16 days	24.5 min	16 min	13.0 days	3.5 min
Threshold, mev	20.2	10.6	16.5	10.4	12.3	13.4	11.7	10.3	9.6	9.25	9.45	9.4
Original nucleus	2 5	Z.	910	F19	ሚ	Crs	Zi Zi	Asts	Ag 107 ‡	Sp.121	III	Pr 141

*Calculated from $(F_{\beta}-Fk)/F_{\beta}$ where F_{β} and F_{β} are probabilities of eta^{\dagger} emission and K-capture, respectively

Table 1.1.13 — Convenient (n,p) Threshold Detectors

(Cohen, Nucleonics 8, No. 2, Feb. 1951)

Other activities	10.2 min (n, \gamma) 2.4 min (n, \gamma) 2.5 min (n, 2n) None 3.0 hr (n, 2n); 44 hr (n, p) 42.0 min (n, 2n)
Approximate α, mg/cm²	250 160 120 160 190 350 250
Convenient material	Mg metal Al metal (NH ₄)H ₂ PO ₄ Flower of sulfur Ti metal powder Cr ₂ O ₃
Half-life	14.8 hr 10.2 min 170 min 14.3 days 57 min 3.9 min 2.59 hr
Effective threshold, mev	.3.0 3.0
Energetic threshold, mev	2.1 2.1 1.1 1.0 1.1 2.8 2.1
Original nucleus	Mg ²⁴ Al ²⁷ P ³ S ²⁸ Cr ³ Pe ⁶

On integrating across the detector thickness, the factor by which the observed counting rate is to be divided is obtained:

$$\mathbf{F} = \frac{\alpha}{d_0} \left[1 - e^{-d_0/\alpha} \right] \tag{61}$$

where: $d_0 = detector thickness$

Absorption in the counter window is corrected for by using Eq. (60). Back scattering from the pan holding the detector is usually not important unless the betas are very high in energy and the detector very thin (correction is about 10 percent for 3 mev betas and zero-thickness detector). If other radiations are emitted in cascade with the betas and the counter is sensitive to them, corrections may have to be made in order to get the true absolute intensity.

In obtaining λn_0 care must be taken that other activities are not interfering. The counting rate vs time is plotted on a semi-log scale, and the activity which has the correct half-life is extrapolated back to zero time. Longer-lived activities are also extrapolated back to zero time and subtracted to give the true λn_0 . For accurate results, the counting rates should be measured over several half-lives of the various activities.

To determine the neutron flux, the energy spectrum must be known. The total flux over 3 mev can be obtained without a knowledge of the energy spectrum by using the (n,p) reaction on P^{31} or S^{32} . For phosphorus, $\sigma = 0.14$ barn, and for sulfur, $\sigma = 0.32$ barn.

PHOTOGRAPHIC EMULSIONS

By exposing emulsions such as Ilford C_2 edge-on and counting the proton recoils in the forward direction (making an angle of less than 10° with the neutron direction), Nereson and Reines⁵⁰ were able to obtain resolution of 10 to 20 percent in the range 0.5 to 1.5 mev. The efficiency per unit cross section is independent of energy in this energy range, but from 0.5 to 0.2 mev, the efficiency decreases because of the low grain counts in the proton tracks.

Using Li⁶-loaded plates, one can use the Li⁶ (n,α) H³ reaction to measure the neutron energy, although not the flux at present. ^{51,52} The energy is a double-valued function of the sum of the alpha plus triton tracks for each value of the angle θ between the alpha and triton; however, by counting only these tracks for which θ is 175° to 180°, a unique energy can be chosen, and a resolution of at least ±0.1 mev is claimed. Detection of energies from thermal up to 10 mev or more should be feasible. The method is well suited for energy measurements on monoergic neutrons within a medium where perturbations introduced by the detector must be minimized and where collimation cannot be achieved. For continuous neutron energy spectra, the capture cross section would have to be known (it is known only up to 0.7 mev) as well as the angular distribution of the reaction. Work on this is going on at present. ⁵³

Scintillation Counters

Hydrogenous materials such as anthracene or stilbene crystals or the many liquid organic scintillators can be used with good efficiency. For example, Jastram et al⁵⁴ claim that a solution of 2 gm/liter of terphenyl in xylene in a cylinder 6 cm long and 4 cm in diameter has an efficiency of 50 percent for 1- to 10-mev neutrons. However, such detectors are also fairly sensitive to gamma radiation. By applying coincidence techniques in which only those recoil protons which receive almost all the energy are counted, the resolution can be considerably improved and the gamma background greatly reduced, with a corresponding sacrifice in counting efficiency.

Molding a button of lucite mixed with ZnS produces a scintillator which can be made relatively insensitive to gamma rays by proper discrimination.⁵⁵ Table 1.1.14 gives efficiencies at some energies.

Table 1.1.14 — Neutron Detection Efficiencies for ZnS Scintillation Counter
(Hornyak, Rev. Sci. Inst. 23, 1952)

Background	Discriminator	Percent efficiency for neutrons of					
limitation	setting	14.2 mev	~4 mev	0.50 mev			
Tube noise	10	8.0	2.5	0.70			
$\mathbf{E}_{\mathbf{y}} < 3 \text{ mev}$	15	6.8	1.7	.28			
$\mathbf{E}_{\gamma}^{\prime}$ < 17 mev	30	4.0	0.86	.12			

STANDARDIZATION13,56

Measurement of absolute neutron source strengths and fluxes is difficult, and the accuracy is at best about 5 percent. Relative measurements can be carried out much more easily with accuracies better than 1 percent.

SOURCE STRENGTH

ABSOLUTE MEASUREMENTS

Boric Acid Bath

The source is surrounded by enough boric acid solution to absorb all the neutrons. The source strength is given by:

$$Q = 4\pi (M_B + M_H) \frac{\sigma_H}{\sigma_B} \int_0^\infty nv \sigma_B (1 + g) r^2 dr$$
 (62)

where: Q = neutrons/sec emitted by source

 M_R , M_H = moles of boron and hydrogen, respectively, per cc of solution

 $\sigma_{\rm B}$, $\sigma_{\rm H}$ = absorption cross section/mole of boron and hydrogen, respectively

 $\sigma_{\rm H}/\sigma_{\rm B} = 2270$ (Reference 57)

g(r) = neutrons absorbed/(cc)(sec) at the distance r at energies above the

cadmium cut-off per neutron absorbed at thermal energies

 $nv\sigma_{\mathbf{R}} = absorption rate of slow neutrons/(cc)(mole B) at r$

The fraction g is determined by measuring the counting rates of a small boron chamber at various distances in the solution with and without a cadmium cover.

The function nvo_B is measured in the following way. A BF₃ counter with accurately known counting volume and gas composition is placed in a thermal flux produced by some second-

ary source. The counting rate I_B of the chamber gives the neutron flux $(nv)_B$ at the counter by:

$$I_{B} = (nv)_{B} o_{B} N_{B} \tag{63}$$

where: N_B = moles of boron in the counting volume

The ratio of saturated activities of In or Mn foils at a position r in the bath, A_{th} , and at the BF₂ counter in the secondary flux, A_{B} , is equal to the ratio of the fluxes at the points.

$$\frac{nv}{(nv)_B} = \frac{A_{th}}{A_B}$$

Thus:
$$nv\sigma_B = \frac{A_{th}}{A_B} \frac{I_B}{N_B}$$
 (64)

and the integral in Eq. (62) can be evaluated by measuring A_{th} as a function of r. The foils must be thin enough not to disturb the neutron flux distribution. In this way, the Los Alamos No. 44 Standard Ra- α -Be Source was calibrated to yield a $Q = (5.9 \pm 0.3) \times 10^6$ per sec in Oct. 1944. The Q increases by 0.54 percent per year because of the growth of Po^{210} .

Production of Helium From Boron

Since one helium atom is produced for each neutron absorbed in B^{10} , a measurement of the amount of helium produced in a bath containing a known amount of boron will give the neutron source strength. Most sources are too weak to produce enough helium to be measured; therefore, the calibration is done indirectly by measuring the amount of helium produced by reactor neutrons and then measuring the relative neutron densities of the reactor and the source by some other method, such as activation of a manganese solution. In this way, the Argonne Standard Source No. 38 $(Ra-\alpha-Be)$ was found to have a $Q=(5.5\pm0.4)\times10^6$ per sec in Oct. 1944.

Balancing of Sub-critical Reactor With Calibrated Absorber

At Harwell, a source was calibrated by balancing the neutrons produced by the source with a sample of sodium. Determining the disintegration rate of the sample gives Q after making certain corrections, such as for the resonance capture of the fast neutrons.

RELATIVE SOURCE-STRENGTH MEASUREMENTS

If two sources are known to have similar spectra, they can be compared by setting up any suitable detector in a fixed geometry.

For sources with different spectra, all the neutrons must be captured or all slowed down to the same energy before detection. The following methods have been used.

Long Counter

The accuracy with such a counter is about 5 percent.

Infinite Medium

The sources are put into a standard graphite reactor and the slowing-down distribution is measured with indium or manganese foils. A standard reactor is a rectangular array of graphite from 5 to 7 ft on a side, 8 to 10 ft high, and covered with cadmium to keep out neutrons from the surroundings. The source is put on the center line 2 or 3 ft from one

end. The detecting foils are also placed along the center line. Such a reactor is also used for flux measurements (see below). For high accuracy, a source strength of 5×10^5 n/sec or greater is desirable:

$$\frac{\mathbf{Q}}{\mathbf{Q}^{\text{std}}} = \frac{\int_0^{\infty} \mathbf{q} \ \mathbf{r}^2 \ \mathbf{dr}}{\int_0^{\infty} \mathbf{q}^{\text{std}} \ \mathbf{r}^2 \ \mathbf{dr}}$$
(65)

$$\frac{\mathbf{q}}{\mathbf{q}^{\mathbf{std}}} = \frac{\mathbf{A}_{\mathbf{res}}}{\mathbf{A}_{\mathbf{res}}^{\mathbf{std}}} \tag{66}$$

where: r is the distance from the source along the center line

 A_{res} is the saturated foil activity owing to neutrons above the cadmium cut-off. For indium foils, the activity is produced by 1.44-ev neutrons; for Au, 4.8-ev neutrons; and for Mn, 300-ev neutrons. An analytic form for A_{res} (r) is needed to integrate the equation and is found, on the basis of Fermi age theory (see Chapter 1.3), by fitting the measured distribution to the sum of Gaussians, three usually being sufficient:

$$A_{res} = \sum_{i=1}^{3} A_i e^{-r^2/r_i^2}$$
 (67)

where A_i and r_i are empirical constants. When indium is used, corrections to the observed A_{res} have to be made for absorption in the cadmium of the 1.44-ev neutrons, for the sink effect of the indium, and for absorption in indium of higher resonances⁵⁸ (see also preceding discussion in this chapter).

If the two sources are not very different in their spectra, the relative source strengths are simply equal to the ratio of the saturated foil activities when measured at a properly chosen distance to in the standard reactor.

This method, while not as accurate as the integration method, is much faster and can measure weaker sources (down to 10⁴n/sec or less).

A water bath or paraffin sphere can be used to slow down the neutrons to thermal energies and the distribution measured with foils or small boron counters. The bath should be large enough to capture all the neutrons. A radius of less than 2 ft will be effectively infinite for neutrons up to fission energies. For high accuracy, a strength of 2×10^5 n/sec or more is needed. An equation similar to Eq. (65) is used with q replaced by A_{th} . The integrals are evaluated graphically until A_{th} r² becomes an exponential, and then A_{th} is fitted to the equation:

$$A_{th} = \frac{a}{r^2} e^{-r/\lambda_s} \tag{68}$$

for r up to ∞ . a and λ_s are constants.

Because of the steep distribution curve, the positions of the foil must be measured to better than a millimeter and the finite size of the foil taken into account; i.e., the root-mean-square distance from the center of the source to all parts of the foil is used. The disturbance of the neutron distribution caused by the sink effect of the foils will cancel out to a large extent in the ratio of the integrals if the same foils are used for both measurements.

A water solution of a manganese or iodine salt surrounding the source is stirred after irradiation to saturation to spread the activity uniformly throughout the solution. The ac-



tivity of an aliquot is measured. Then $Q/Q^{std}=A_s/A_s^{std}$. This method is the only one which is independent of the angular distribution of the neutrons.

Subcritical Reactor

If the reproduction factor, k, is slightly less than one, the flux of a source placed in the reactor is multiplied by 1/1 - k. When this flux is detected by a counter in the lattice, the counting rate is closely proportional to Q because the effectiveness of fast neutrons in the reactor does not depend strongly on their energy. The reactor carries out, in effect, an integration of the neutron distribution, and only one reading is necessary. However, if the spectra are very different, corrections for differences in leakage may have to be applied. This method is rapid and has an accuracy of 1 percent.

FLUX

Standard fluxes may be obtained by measuring reaction rates of known cross sections. 1/v detectors such as boron or gold will actually give the neutron density (see Eq. 51) from which a thermal flux can be obtained by multiplying by 2.2×10^5 cm/sec. Such measurements can be carried out with an accuracy of 2 to 4 percent.

The standard graphite reactor with a standard source is used to produce known fluxes. The distribution of resonance neutrons, A_{res} , is expressed by the semi-empirical Eq. (67). The slowing-down density is given by:

$$q_{res} = k_{res} A_{res} = \sum_{i=1}^{3} \frac{F_i Q}{(\pi r_i^2)^{\frac{1}{2}}} e^{-r^2/r_i^2}$$
(69)

where: Q = source strength

 F_i is the fraction of the Q n/sec emitted which are in the synthetic energy group having the range r_i :

$$\mathbf{F_i} = \frac{\mathbf{k_{res}} \mathbf{A_i} \pi^{\frac{1}{2}} \mathbf{r_i^{\frac{3}{2}}}}{\mathbf{O}} \tag{70}$$

k_{res} is evaluated from the relation:

$$\sum_{i} \mathbf{F}_{i} = 1 = \frac{\mathbf{k}_{res}}{\mathbf{Q}} \pi^{\frac{1}{2}} \sum_{i} \mathbf{A}_{i} \mathbf{r}_{i}^{3} \tag{71}$$

The thermal flux is given by:

$$(\mathbf{n}\mathbf{v})_{\mathbf{th}} = \mathbf{v_0} \sum \mathbf{n_i} \tag{72}$$

where: v_0 = thermal velocity = 2.2×10^5 cm/sec

$$n_{i} = F_{i} Q \sum_{j=1}^{\infty} \sum_{k=1}^{\infty} C_{jk} \frac{b_{jk}}{2} e^{-\frac{\left[r_{i}(th)\right]^{2}}{4L^{2}}} \left\{ \left[1 - \theta \left(\frac{z}{r_{i}(th)} + \frac{r_{i}(th)}{2b_{jk}}\right)\right] e^{z/b_{jk}} + \left[1 + \theta \left(\frac{z}{r_{i}(th)} - \frac{r_{i}(th)}{2b_{jk}}\right)\right] e^{-z/b_{jk}} \right\}$$
(73)

where:
$$C_{jk} = \frac{6}{\lambda v_0 a^2} \cos \frac{j\pi x_s}{a} \cos \frac{k\pi y_s}{a} \cos \frac{j\pi x}{a} \cos \frac{k\pi y}{a}$$

$$\frac{1}{b_{jk}^2} = \frac{1}{L^2} + \frac{\pi^2}{a^2} (j^2 + k^2)$$

$$\theta = \theta(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-y^2 dy}$$

$$r_i^2(th) = r_i^2 + 4 (\tau_{th} - \tau_{In})$$

$$4(\tau_{th} - \tau_{In}) = 268$$

$$\tau = \text{neutron age}$$

L = thermal diffusion length

 $\lambda = transport mean-free-path$

The reactor has its small sides of equal length with $a = \text{geometric length} + 1.42 \lambda$. The origin of coordinates is taken at the center at one end of the reactor. The source is at $(x_8, y_8, 0)$ and the foils are at (x, y, z). Since even a graphite reactor 8 to 10 ft high is not infinite in height for the thermal diffusion process for points very near the top, the observed neutron density near the top will be less than the value calculated from Eq. (73) by the factor:

$$1 - e^{-2(z_t - z)/b_{11}}$$

 $z_t = (z \text{ coord. at the top of the block}) + 0.71\lambda$. A reactor 5 ft wide will be effectively infifrom the sides for points along the axis (x = y = 0).

By measuring the thermal foil activity, A_{th} , at various points along the axis of the column and by comparing this with the calculated flux, $(nv)_{th}$, at these points, an average K_{th} such that $(nv)_{th} = K_{th}A_{th}$ may be obtained. This standardizes the foils for the measurement of thermal flux.

To convert from graphite to water:

$$\mathbf{K_{res}}(\text{water}) = \mathbf{K_{res}}(\text{graphite}) \frac{\lambda(\text{graphite}) \, \xi(\text{water})}{\lambda(\text{water}) \, \xi(\text{graphite})}$$
 (74)

MEASUREMENT OF FAST NEUTRON FLUX 59

For monoergic neutrons, hydrogen recoil counters with known sensitive volumes can be used. Three types of counters have been described: (1) Hydrogen-filled proportional or ionization counters or counters having a thin hydrogenous radiator. The ultimate limit to the accuracy is set by the accuracy of the elastic scattering cross section, which is equal to the total cross section at high energies, capture being negligible. This is known to 2 percent up to 1.5 mev and 5 percent up to 14 mev. The lower limit to the neutron energies that can be detected is about 200 kev. (2) Integration ionization chambers in which the current is measured and is directly proportional to the flux. The accuracy is about the same as the pulse-type counters, and this counter has the advantage of being able to detect neutrons down to tens of kev. However, background effects are more difficult to eliminate. (3) Photographic plates have been used, but errors in defining the solid angle and the concentration of hydrogen atoms makes the accuracy at best 15 to 20 percent.

If the neutrons are emitted by a reaction such as $H^2(H^2,n)He^3$ or $H^2(H^3,n)He^4$, an accurate estimate of the neutrons coming off at angle θ per unit solid angle with respect to the

incident particle in the lab system can be made by counting the helium atoms at the corresponding angle ϕ :

$$\sin \phi = \sqrt{\frac{\mathbf{M}_{n} \mathbf{E}_{n}}{\mathbf{M}_{He} \mathbf{E}_{He}}} \sin \theta \tag{75}$$

This method is potentially capable of the highest accuracy (about 1 percent) for neutrons above 3 mev using the d,d reaction and for neutrons above 13 mev using the t,d reaction.

Threshold detectors with known cross sections which vary smoothly with energy are suitable secondary standards. Fission detectors are convenient because of the ease in detecting the fission fragments. NP²³⁷ has a threshold of 0.4 mev, and natural U has a threshold about 1 mev.

Relative fluxes can be compared using the long counter (see discussion earlier in this chapter) or the various moderating media with a detector at one point, assuming the sources are isotropic.

For polyergic sources, fluxes can be measured by the methods just described for relative fluxes. The highest accuracy is obtained with a moderating medium. Care must be taken when using the long counter because it is energy independent only over a limited energy range.

The recoil particle method is suitable for measuring polyergic sources. The energy distribution of the primary neutrons, S(E), is related to the energy distribution of the recoil particles, H(E), by:

$$S(E) = \frac{E_r}{N\sigma(E)} \frac{dH(E)}{dE_r}$$
 (76)

where: E_r = energy of recoil

N = number of detecting nuclei/cm²

 $\sigma(E)$ = scattering cross section

The principal difficulty is to determine dH/dE_r . The various types of hydrogen counters are most suitable. One method that has been used successfully with about 10 percent accuracy is to count the recoils from a thin radiator in a photographic plate.

CROSS-SECTION MEASUREMENTS

The atomic cross section, σ , for a reaction produced by neutrons is defined as follows:

$$\sigma = \frac{\text{Events of given type per unit time per nucleus}}{\text{(neutron density) (neutron velocity)}}$$
(77)

The neutron can be isotropic or in a beam. Dimensions are in area units. A given type means absorption, scattering, and the like or the total cross section which involves the sum of all processes that can remove neutrons from the beam.

TOTAL CROSS SECTION

The total cross section, σ_t , is found very accurately by a transmission experiment using monoergic neutron beams. The transmission is defined as the ratio of neutron flux at distance x in the material to the initial flux and is given by:

$$T = \frac{(nv)_{x}}{(nv)_{0}} = e^{-N\sigma_{t}x}$$
 (78)

where N is the density of nuclei in the material. The beam intensity is measured by a detector with and without the sample in the beam. It is not necessary to know the detector efficiency because only the counting ratio is needed. The conditions for accuracy are:

- (1) Well collimated beam.
- (2) Uniform, accurately known, sample thickness.
- (3) Accurate knowledge of impurities, especially the water content and impurities with large cross sections.
 - (4) Small angle subtended by detector at absorber (to avoid scattered neutrons).

The most accurate measurements of σ_t as a function of energy have been made using time-of-flight spectrometers and crystal monochromators (see previous discussion).

ABSORPTION CROSS SECTION, σ_a

TRANSMISSION METHOD

If $\sigma_t \gg \sigma_s$, then $\sigma_t = \sigma_a$. If $\sigma_t > 500$ b, the error in σ_a will be less than 5 percent. This is the case with B, Cd, U^{235} , and Pu^{249} . If $\sigma_t \simeq 50-200$ b using a reasonable guess for σ_s will give σ_a with an error of about 10 percent.

SUBSTITUTION METHOD

This is a relative method used for 1/v absorbers. A source is surrounded first with the material of unknown σ_a and then with material of known σ_a , using enough material to absorb all the neutrons. The rate of neutron production will be the same in both cases, but the rate of absorption will depend on σ_a . The total number of neutrons present in each medium is found by measuring the density distribution using 1/v detectors. Then:

$$\frac{\left(\int_{\mathbf{v}} \mathbf{n} d\mathbf{v}\right)_{1}}{\left(\int_{\mathbf{v}} \mathbf{n} d\mathbf{v}\right)_{2}} = \frac{N_{2}\sigma_{\mathbf{a}_{2}}}{N_{1}\sigma_{\mathbf{a}_{1}}} \tag{79}$$

where: n = neutron density

N = density of absorbing atoms

For an isotropic source, it is only necessary to measure the activity, I, along one radius, plot Ir² vs r, and graphically integrate.

If σ_a (unknown) > 10 b, water is used for the standard, and the unknown is dissolved in water. Then:

$$\frac{\left(\int \text{ ndv}\right)_{\text{H}_2O}}{\left(\int \text{ ndv}\right)_{\text{soln.}}} = \frac{N_H \sigma_H + N_x \sigma_x}{N_H \sigma_H}$$
(80)

(The absorption of oxygen is negligible compared to hydrogen)

In this way, the ratios σ_{Li}/σ_H , σ_B/σ_H , and σ_{Mn}/σ_H have been measured.

If σ_a (unknown) ~ 10 b large volumes of concentrated solutions are usually needed. This can be avoided by the following modification of the method. Boron, because of its large cross section, is used as a standard in place of hydrogen. The source is kept at a fixed position outside the solution, the detector at a fixed position within. The concentration of boron atoms, N_B, which produces the same decrease in the slow-neutron density as is caused by a concentration, N_x, of the element x is determined. The cross section, σ_x , of this element is then given by $\sigma_B N_B = \sigma_x N_x$.



EXPERIMENTAL METHODS CHAP. 1.1

This modification is equivalent to the measurement of a single point on the activity integral curves discussed above. A basic assumption is that the fixed geometrical conditions and the low concentrations involved render negligibly any differences in the scattering properties of the elements investigated and any changes in the absorption and scattering properties of the water.

A further modification is necessary in order to study elements with $\sigma_a < 1$ b. Because σ_a of H(0.31 b) is comparable to the cross sections to be studied, water is replaced by a moderator of negligible absorption, i.e., graphite. A powdered sample of the element to be investigated is intimately mixed with graphite powder. The reduction in the neutron density by a known concentration of the element is compared with that produced by varying mixtures of boron and graphite powder.

CHANGE IN REACTOR REACTIVITY

Adding an absorber to a critical reactor will reduce the reactivity k by an amount Δk which, to a first approximation, is proportional to the absorption cross section. The method has been applied to thermal reactors in two variations; the <u>danger-coefficient</u> method and the <u>reactor oscillator</u> method. It is a relative method and requires absorbers with known cross section, such as boron or gold, which are 1/v and thus yield the thermal cross section. The unknown must also have the same cross section spectrum or else the cross section will just be some average value over the thermal-reactor energy regions.

In the danger-coefficient method, the reactivity change is measured by the position of a control rod which has been calibrated. The reactivity, in turn, is obtained from a measurement of the reactor period as observed on a sensitive galvanometer connected to a large BF₃ chamber in the reactor.

The change in reactivity is observed for both the unknown and a standard absorber placed near the center of the reactor, and the ratio is equal to the ratio of the cross sections. Instead of using boron as a standard, it is convenient to use thin cadmium wires about 1 mm in diameter. Cd is black to neutrons up to 0.4 ev and in an isotropic flux presents a cross section of $\frac{1}{4}\pi dl$, where d = diameter and l = length. To convert a cross section measured with cadmium as a reference to a thermal cross section, it must be multiplied by the calibration ratio between cadmium and boron. The following errors may be present:

- (1) Impurities with high cross section. This is probably the most important external source of error and, according to Hughes, 13 limits the accuracy to about 5 percent.
- (2) Perturbation of neutron density by high absorption. This is reduced by using thin or dilute absorbers and distributing them over many graphite cells.
- (3) Self-absorption. This effect is minimized by adjusting the thickness of the known and unknown to give the same absorption per unit area in each.
- (4) Scattering effects. By placing the absorber in a region of zero neutron-density gradient, i.e., in the center of a moderator cell symmetrical with respect to the fuel, there will be no change in the spatial distribution. However, the absorber (as a scatterer) will increase the slowing-down power of the moderator, the resonance escape probability, and thus the reactivity. This is important for materials of low σ_2 and low A but can be calculated if σ_8 is known.
- (5) In air-cooled reactors, barometric and temperature drifts and fluctuations change the amount of gas in the reactor and therefore the absorption and reactivity. Temperature drifts are slow and can be compensated for by measuring the unknown and standard in cycles. Pressure changes can be erratic and set the limit to the internal consistency of the measurements in such reactors. This is about 0.5 percent.

The reactor oscillator is a mechanical device for oscillating a sample between positions of different flux density. The change in reactivity is observed as an a. c. signal coming

from an ion chamber placed close to the path of the moving absorber. By proper design of the ion chamber and recording circuits, the signal because of a scattering event can be made quite different from one due to absorption. The two types can be put out of phase and the scattering signal almost completely cancelled out. Corrections for scattering have to be considered when the absorption cross section becomes less than 1 percent of the scattering cross section. The main advantage of the reactor oscillator is that much smaller amounts of materials can be used, of the order of milligrams instead of the grams to kilograms required by the danger-coefficient method. The materials can be oscillated in a region of the reactor containing only graphite so that resonance effects can be greatly reduced. As an estimate of the over-all error, measurements of the indium thermal cross section showed an uncertainty of 5 percent for a 150-mg sample and a 20 percent uncertainty with a 5-mg sample. ⁶²

ACTIVATION METHOD

By studying the induced radioactivity of a sample, the activation cross section can be measured. The activation may result from (n,γ) and (n,p) reactions, and thus the activation cross section may or may not be equal to the absorption cross section. If the product nucleus decays in a simple manner to a stable daughter, the activation cross section is:

$$\sigma_{act} = \frac{C_{a,sat}}{nvN}$$
 (81)

where: $C_{0,sat}$ = saturation activity at end of irradiation; see Eq. (56)

nv = neutron flux

 N_t = total number of atoms in beam

If the daughter of the product nucleus is also radioactive, the equation for $C_{\phi,sat}$ is more complicated.

If the flux is not known, relative measurements can be made. Then:

$$\sigma_{\mathbf{x}} = \frac{\mathbf{N}_{\mathbf{std}}}{\mathbf{N}_{\mathbf{x}}} - \frac{(\mathbf{C}_{\mathbf{0}, \mathbf{sat}})}{(\mathbf{C}_{\mathbf{0}, \mathbf{sat}})_{\mathbf{std}}} \sigma_{\mathbf{std}}$$
(82)

DEPLETION METHOD

Some of the elements have large absorption cross sections but the product nucleus is stable (Cd, Gd, Sm). The cross section can be obtained by irradiating in a reactor of known flux for a few months and analyzing the sample for initial and final nuclei concentrations in a mass spectrograph. The accuracy is poor because of uncertainties about the reactor flux. The method has also been applied to determining the cross section of Xe^{136} which has the largest absorption cross section known. Xe^{135} has a half-life of 9.2 hr and decays to the very long lived Cs^{135} (half-life > 10^6 yr) which can be considered stable. Two samples are put into similar counting chambers, and the ratio of activities before and after one of the chambers has been irradiated is taken. The non-irradiated sample decays according to:

$$I = I_a e^{-\lambda t}$$

and the irradiated sample according to:

$$\mathbf{I} = \mathbf{I}_{\bullet} \mathbf{e}^{-(\lambda + n \mathbf{v} \sigma)t}$$

from which o can be obtained.

EXPERIMENTAL METHODS CHAP. 1.1

MEASUREMENT OF DIFFUSION LENGTH

This method complements the other methods because it requires $\sigma_2 \ll \sigma_s$. A rectangular reactor of the absorber is built with square cross section. A source is put at one end, and the relaxation length along the central longitudinal axis is measured. This is the length for the neutron intensity to drop by a factor e:

$$\frac{1}{\text{relaxation length}} = \sqrt{\frac{1}{L^2} + \frac{2\pi^2}{a^2}}$$
 (83)

where: a = short edge length + 1.42 λ_{tr} L = $1/\sqrt{3\sigma_a}\sigma_{tr}$ = diffusion length λ_{tr} = transport mean-free-path = $1/N\sigma_{tr}$ σ_{tr} = transport cross section N = nuclei/cm³ (84)

 $\sigma_{\rm tr}$ must be known. Large quantities of the absorber are needed. Measurements on D₂O, graphite, and Be have been carried out. The method has been especially useful in assaying impurities in graphite that would increase the absorption.

SCATTERING CROSS SECTION

THE DIFFERENTIAL SCATTERING CROSS SECTION

The differential scattering cross section per unit solid angle at the angle θ with respect to the incident beam is given by:

$$\frac{d\sigma_{g}(\theta)}{dw} = \frac{(nv)_{\theta}}{(nv)_{0} NX\Delta w}$$
 (85)

where: $(nv)_{\theta}$ = scattered flux measured by a detector at the angle θ

 $(nv)_0 = incident beam flux$

N = density of scattering atoms

X = thickness of scatterer

 Δw = solid angle subtended by detector at the scatterer

The thickness must be small enough to present multiple scattering. The velocity of the scattered neutron will change with angle; therefore, the change in detector sensitivity with energy must be considered. Since the scattered neutrons are distributed over 4π radians, the scattering intensities are low and the accuracy is not as great as for σ_t .

RECOIL COUNTERS FOR DIFFERENTIAL CROSS SECTION

If the scatterer is a gas, conservation laws give a relationship between the distribution in angle of the scattered neutrons and the distribution in energy of the recoils, using an incident beam of monoergic neutrons. The recoil energy distribution can be measured by putting the gas in an ionization chamber or proportional counter. Instead of using recoils produced in a gas it is also possible to employ a thin radiator. Elastic scattering must be the only nuclear interaction because other reactions would change the energy distribution.

The differential cross section in the <u>center of mass system</u> at the angle ϕ as a function of the recoil energy distribution in the <u>lab</u> system is given by:⁶⁴

$$\frac{d\sigma_{g}(\phi)}{dw} = \frac{E_{n}A}{\pi(A+1)^{2}} N(E)$$
 (86)

where: N(E) = recoil particles per unit energy interval at energy E in lab system

 E_n = incident neutron energy

A = mass number of recoil particle

The relationship between the scattering angle, ϕ , of the neutron in the center of mass system and the recoil energy, E, in the lab system is:

$$E = \frac{2A}{(1+A)^2} E_n (1 - \cos \phi)$$
 (87)

The method has been successfully applied to hydrogen, helium, and oxygen. 65.66,67

METHOD OF POOR GEOMETRY

A poor-geometry scattering experiment in which the scatterer is a large disk placed halfway between the (point) source and (point) detector will give the cross section for scattering through angles larger than $\phi_{\rm m}$, the angle the scatterer subtends at the source or detector. The scattering disk must be thin, and the neutron source and detector response must be isotropic. The method is particularly useful for heavy elements and for small scattering angles of the neutrons.

The cross section is found from:

$$\frac{I}{I_0} = 1 - N \int_{\phi_m}^{\pi} \sigma(\phi) 2\pi \sin\phi d\phi$$
 (88)

where: the integral represents the partial total cross section for ϕ from ϕ_m to π

 I_0 = flux measured by detector without scatterer

I = flux measured by detector with scatterer

N = scattering nuclei per unit area

LARGE-ANGLE SCATTERING

For isotropic scattering, the amount of large-angle scattering (>90°) can be measured and compared with graphite whose scattering cross section is accurately known from transmission experiments.

THE TOTAL-SCATTERING CROSS SECTION

The total scattering cross section, σ_s , is obtained by integrating the differential cross section as defined by Eq. (85) over the unit sphere.

TRANSMISSION METHOD FOR TOTAL-SCATTERING CROSS SECTION

The scattering cross sections of the elements are > 1 b for thermal neutrons. If a rough absorption measurement indicates that σ_a is \ll 1 b, then $\sigma_t \simeq \sigma_s$. This method has been applied to H, D, Be, C, O, F, Pb, and Bi.

If $\sigma_a > \sigma_s$ and an accurate spectrum of σ_t vs E is obtained from velocity spectrometer measurements, it may be possible to analyze the curve into a constant scattering term plus a 1/v absorption term. The effects of crystalline structure and molecular binding on the scattering cross section are discussed in Chapter 1.2. Because of the interference effects at thermal energies, scattering cross sections of the atoms in a molecule are not additive.



EXPERIMENTAL METHODS CHAP. 1.1

INELASTIC SCATTERING CROSS SECTIONS

TRANSMISSION METHOD

The transmission is measured by putting a sphere of the scattering material round either the source or the detector. If the neutron source is not isotropic, the sphere should be put around the detector. Use of a sphere eliminates elastic scattering effects.

The detector is of the threshold type so that the experimental cross section is that for all neutrons degraded below the threshold energy, including absorption. By using detectors with different thresholds, a rough idea of the spectrum and of the contribution of absorption can be obtained.

The method gives the total inelastic cross section since the sphere has an integrating effect. To avoid geometric perturbations, the distance between source and detector should be more than three times the radius of the sphere. Errors from this effect are thereby reduced to less than one percent under the assumptions of isotropic scattering. A large plane of the scatterer may be used in place of the sphere, but the corrections are much greater.

In order to correct for scattering from the surroundings, variations in source strength, and the like, a monitor of the same detecting material is put to the side about halfway between the source and detector.

DIRECT SPECTRUM METHOD

The neutron energy spectrum is measured at different angles, and the complete inelastic scattering spectrum is thus obtained. Corrections for absorption are not necessary. This is the best method but requires sensitive detectors with known energy dependence. Results have been published for the scattering at about 90° for Fe using a photographic plate⁶⁹ and for Fe and Al using an anthracene scintillation counter.⁷⁰ The results for Fe agree within the experimental error which is about 25 percent. Measurements on the heavy elements are being performed at Los Alamos with a sphere around the source and a photographic plate for detector.⁷¹

GAMMA-RAY METHOD

The yield of gamma rays coming off as a result of inelastic scattering has been measured ⁷² by means of a pair of calibrated Geiger counters in coincidence. The neutron flux was measured with a proton recoil ionization chamber. If only one level is excited, the number of gamma rays can be correlated one-to-one with the scattering events and the cross section determined. If several gamma rays are emitted in cascade, the interpretation becomes more difficult.

FISSION AND CAPTURE CROSS SECTIONS AND α

FISSION CROSS SECTION, of

- (1) By using a known flux, one can measure $nv\sigma_f N$ by absolute counting in a fission chamber.
- (2) The sample is irradiated in a reactor with known flux, and a quantitative chemical analysis of the fission products is then carried out. From this, σ_f can be calculated.
- (3) The cross section is measured relative to that of U²³⁵, thereby eliminating the need to know the flux.

CAPTURE CROSS SECTION, oc

(1) A sample with mass number A is irradiated in a known flux and analyzed for the amount of A + 1 isotope formed in a mass spectrograph. This is the method used for U^{235} .

(2) If the A + 1 nucleus is radioactive, the amount of capture can be found from the decay process. This is done for Pu^{239} by counting the spontaneous fissions in Pu^{240} .

(3) σ_c can be found by difference:

$$\sigma_{\rm c} = \sigma_{\rm t} - \sigma_{\rm f} - \sigma_{\rm s}$$

MEASUREMENT OF $\alpha = \sigma_c/\sigma_f$

 σ_c and σ_f can be measured separately as described previously.

Danger Coefficient Method⁷³

The fission sample is inserted in the reactor, and the fractional change in reactivity, $(\Delta k/k)_1$, is observed:

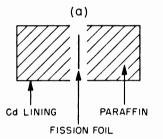
$$\left(\frac{\Delta \mathbf{k}}{\mathbf{k}}\right)_{1} = \Delta \mathbf{f}_{1} \left[\nu \mathbf{F}_{H} - (1 + \alpha) \mathbf{F}_{L}\right]$$
(89)

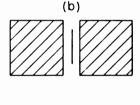
where Δf_1 is the fission rate of the sample, ν the number of neutrons emitted per fission, and F_H and F_L the importance functions (see Chapter 1.4) suitably normalized. F_H and F_L are found as follows:

A non-fissionable absorber is put into the reactor at the same place, and the reactivity change and absorption rate, Δa , are determined to get F_L :

$$\left(\frac{\Delta \mathbf{k}}{\mathbf{k}}\right)_2 = -\Delta \mathbf{a} \ \mathbf{F}_{\mathbf{L}} \tag{90}$$

F_H is obtained by two measurements. The fission sample is inserted in the reactor and is surrounded first by the cadmium-covered paraffin can shown in (a) below and then in the can shown in (b). In both (a) and (b), the over-all transmission is the same, but the inner Cd linings keep the thermal neutrons from reaching the sample in (b). The fission rates are measured for each case.





(a)
$$\left(\frac{\Delta k}{k}\right)_3 = \Delta f_3 \left[\nu F_H - (1 + \alpha) F_L\right] - \Delta a^1 F_L$$

(b) $\left(\frac{\Delta k}{k}\right)_4 = -\Delta f_4 \left[(1 + \alpha) F_L\right] - \Delta a^1 F_L$

 Δa^1 = absorption rate of paraffin and cadmium

The four equations can be solved for α :

$$\alpha = \frac{\left(\frac{\Delta k}{k}\right)_1}{\left(\frac{\Delta k}{k}\right)_2} \frac{\Delta a}{\Delta f_1} \frac{\Delta f_3}{\Delta f_4} + \frac{\left[\left(\frac{\Delta k}{k}\right)_4 - \left(\frac{\Delta k}{k}\right)_3\right] \Delta a}{\left(\frac{\Delta k}{k}\right)_2 \Delta f_4} - 1 \tag{92}$$

MEASUREMENTS OF REACTOR CONSTANTS

NEUTRON TEMPERATURE

The temperature, T, of neutrons is defined for thermal neutrons in a Maxwell distribution* by:

$$\mathbf{kT} = \frac{1}{2} \mathbf{M} \mathbf{v_0^2} \tag{93}$$

where v_0 is the most probable velocity. T can be found by measuring the energy distribution of the neutrons in a high resolution spectrometer, such as the crystal monochromator. T can also be found by measuring the average absorption cross section of a 1/v absorber using a 1/v detector. If:

$$\sigma_a = \frac{K}{v}$$

then:

$$\overline{\sigma}_{\mathbf{a}} = \frac{2}{\sqrt{\pi}} \frac{\mathbf{K}}{\mathbf{v}_{\mathbf{a}}} \tag{94}$$

To carry out the measurement, a transmission experiment is performed using boron as the 1/v absorber because the factor k in Eq. (94) is accurately known. A thin BF₃ detector is used also because of its 1/v nature. Such a detector will see the Maxwellian velocity distribution of the thermal neutrons, and therefore the observed cross section will be just the average cross section. Corrections have to be made for the constant scattering cross section, which is subtracted, and for the flux changes due to the finite absorber thickness ("hardening" of the beam). Temperature measurements carried out on beams inside and outside thermal columns have varied over about 100° . This variation is caused by nonequilibrium conditions as well as experimental uncertainties. The following results are quoted from Hughes. ¹³

330°K for a beam from the thermal column of the Argonne deuterium reactor.

287°K — same location as above but with a slightly different graphite geometry.

255°K for beam emerging from a shallow hole in the thermai column of the Argonne graphite reactor.

285°K — deep hole in the thermal column of the Argonne graphite reactor.

MEASUREMENT OF NEUTRON AGE

The neutron age is determined in the general case by measuring $\overline{r^2}$ and applying the relationship:

$$\tau = \frac{\overline{r^2}}{6} \tag{95}$$

^{*}See Chapter 1.3.

 r^2 is defined by:

$$\overline{\mathbf{r}^2} = \frac{\int_0^{\infty} \mathbf{A_S} \ \mathbf{r}^4 d\mathbf{r}}{\int_0^{\infty} \mathbf{A_S} \ \mathbf{r}^2 d\mathbf{r}}$$
 (96)

 ${\bf A_s}$ is the activity of a resonance foil, usually cadmium-covered indium. The source is placed near* one end of the moderating medium which should be sufficiently large in volume to thermalize the neutrons. For the important practical case of measuring fission-neutron age, the neutron source usually consists of an enriched uranium disk placed in and near the end of the medium with the medium placed on top of a thermal column. ${\bf A_s}$ is measured as a function of r, the distance from the source. To extend the limit of the integral to infinity, a plot of ${\bf ln A_s r^2}$ vs r is made. At large distances from the source, the slowing-down distribution will be given to a first approximation by the distribution of first collisions. This distribution will result in the activation decreasing exponentially:

$$A_{s} = \frac{k e^{-r/\lambda}}{r^{2}}$$
 (97)

A straight line will appear in the semi-log plot, and the constants k and λ can be determined.

The integrals can now be evaluated graphically up to some point, r_0 , which lies on the straight line and then evaluated analytically from r_0 to ∞ . The general form of the integrals is:

$$\mathbf{k} \int_{\mathbf{r}_0}^{\infty} e^{-\mathbf{r}/\lambda} \mathbf{r}^n d\mathbf{r} = k\lambda e^{-\mathbf{r}_0/\lambda} \sum_{i=0}^{n} \left[i!_n C_i \mathbf{r}_0^{(n-i)} \lambda^i \right]$$
(98)

where:
$$n = 0, 2, 4, ...$$

 ${}_{n}C_{i} = n!/[i! (n - i)!]$

At large distances, the counting rate in Cd-covered In foils may become very low. The counting rate may be improved greatly by using bare or Al-covered In foils. Where the first collision processes predominate, the counting rate with Al-covered In will be proportional to the Cd-covered In, and the proportionality constant can be evaluated by taking overlapping points. Activation from higher-energy neutrons can be checked by measuring with In covered with enough boron to remove the 1.44-ev resonance neutrons. The error in $\overline{r^2}$ from this effect is reduced when the ratio of the integrals is taken. The correction can be quantitatively made.⁵⁸ In another technique¹⁴ for eliminating the higher-energy activation, a single Cd-covered In foil is activated followed by a Cd-covered In sandwich consisting of three similar indium foils. The activity of the interior foil of the sandwich is subtracted from the single foil measurement, and the result is the activation of solely the 1.44-ev resonance.

To correct for the finite sizes of the source and detector, the following equation may be used: Case I. Circular source of radius a' and circular detector of radius a:

$$\mathbf{A}(\mathbf{r}_{0}) = \mathbf{A}_{m}(\mathbf{r}_{0}) - \left(\frac{a'^{2} + a^{2}}{4\mathbf{r}_{0}}\right) \left(\frac{d\mathbf{A}_{m}}{d\mathbf{r}}\right)_{\mathbf{r}_{0}}$$
(99)

^{*} But not so near $(<\sqrt{\tau})$ that the effect of the boundary is felt at the positions of measurement.

Case II. Rectangular source of dimensions 2a' by 2b' and rectangular detector 2a by 2b:

$$A(r_0) = A_m(r_0) - \left(\frac{a'^2 + b'^2 + a^2 + b^2}{6r_0}\right) \left(\frac{dA_m}{dr}\right)_{r_0}$$
 (100)

Case III. Circular source of radius a' and rectangular detector of dimension 2a by 2b:

$$A(r_0) = A_m (r_0) - \frac{4(a^2 + b^2 + 6a'^2)}{24r_0} \left(\frac{dA_m}{dr}\right)_{r_0}$$
 (101)

 $A_m(r_0)$ is the observed activity at the distance r_0 between the centers of the source and detector, and $A(r_0)$ is the ideal activity owing to point sources. Other combinations, such as point source and circular detector, can be obtained from the above equations by simple modifications. The assumptions used in deriving the equations require the use of foils and sources small in dimension with respect to r_0 . However, the equations have been shown to be valid for corrections up to 20 percent.

The same data used to obtain r² can be used for higher movements:

$$\overline{\mathbf{r}^{n}} = \frac{\int_{0}^{\infty} \mathbf{A_{s}} \ \mathbf{r}^{n+2} \ d\mathbf{r}}{\int_{0}^{\infty} \mathbf{A_{s}} \ \mathbf{r}^{2} \ d\mathbf{r}} \ n = 2, 4, 6, \dots$$
(102)

The accuracy decreases however with increase in n.

The above measurements give the age for the energy drop from the energy of emission to the resonance energy of the foil. The age from the resonance energy to thermal is calculated from:

$$\tau_{\rm th} - \tau_{\rm res} = \int_{\ln E_{\rm th}}^{\ln E_{\rm res}} \frac{\overline{\lambda_{\rm tr}^2}}{3\xi(1 - \overline{\cos \theta})} \, d \ln E$$

$$= \frac{\overline{\lambda_{\rm tr}^2}}{3\xi(1 - \overline{\cos \theta})} \ln \frac{E_{\rm res}}{E_{\rm th}}$$
(103)

where the symbols have their usual meaning.

If the neutron source is monoergic, the log of the slowing-down density plotted against the square of the distance from the source will give a straight line the slope of which is equal to $-1/4\tau$.

THE RESONANCE ABSORPTION INTEGRAL

The resonance absorption integral, $\int \sigma dE/E$, can be measured by activation of the substance when this gives unambiguous results (i.e., all neutrons absorbed produce the same radioactive isotope) or by using the reactor oscillator (see previous discussion, "Change in Reactor Reactivity").

In the activation method, 16 the cadmium ratio for the substance, x, is determined in a reactor (dE/E) flux, and the resonance absorption integral is given by:

$$\int_{E_{\phi}}^{\infty} \sigma \frac{dE}{E} = \frac{K(\sigma_{th})_{x}}{(CdR - 1)_{x}} - k (\sigma_{th})_{x}$$
(104)

where: $(o_{th})_x$ = thermal activation cross section for the substance (assumed known)

CdR = cadmium ratio

K = constant depending on flux only

k = constant related to epi-cadmium 1/v absorption

K and k are found by measuring the cadmium ratios of a substance with a standard having a known resonance absorption integral, such as gold or indium, and of a substance with pure 1/v absorption, such as boron:

$$K = \frac{\left(\int_{E_{\theta}}^{\infty} \sigma \, dE/E\right)_{std}}{\left(\sigma_{th}\right)_{std} \left[\frac{1}{\left(CdR - 1\right)_{std}} - \frac{1}{\left(CdR - 1\right)_{1/y}}\right]}$$
(105)

$$k = \frac{K}{(CdR - 1)_{1/v}} \tag{106}$$

The lower limit, E_0 , to the integral will be 0.4 ev if a 0.01-in. Cd shield is used around the sample in an isotropic flux or if 0.02-in. Cd is used in a collimated neutron beam. The lower limit to the dE/E flux may be set at 0.17 ev since this energy will divide equally the intensities of the Maxwellian and dE/E distribution. The resonance integral can be calculated to 0.17 ev if the absorption cross section is known. If it is 1/v as is usually the case, then:

$$\int_{0.17}^{0.4} \sigma_a \, \frac{dE}{E} = 0.69 \, \sigma_{th} \tag{107}$$

In the activation method, it is important that the sample be as free from water as possible because H causes moderation and additional thermal absorption. To reduce self protection, very thin samples must be used. If the sample has a CdR of less than 5, indicating a strong resonance, the sample thickness will have to be 0.1 to 0.2 mg/cm² or less.

In using the reactor oscillator, ¹³ the technique is similar to that described earlier under "Change in Reactor Reactivity." The samples are oscillated inside a cadmium tube and the amplitude of the reactor oscillation is calibrated with indium or gold. The advantages of the oscillator are that small samples can be investigated and that the total absorption is measured.

In measuring the resonance absorption of U²³⁸, thin foils of separated U²³⁸ may be activated. However, in actual reactors, the amount of uranium present is so large that the dE/E spectrum is depleted at the resonance energies, the amount of depletion depending on the shape and concentration of the uranium. Thus, an effective resonance absorption integral should be measured. This is done by putting the thin U²³⁸ foils in a sample of the homogeneous uranium-graphite mixture which is large enough to ensure equilibrium depletion at the resonance levels—usually about a liter in volume. For unhomogeneous reactors, the uranium slugs are slotted to receive small thin U²³⁸ foils. The effective integral is determined for various sizes of slugs in order to get semi-empirical equations of the type of Eq. (9).

MEASUREMENTS OF DIFFUSION LENGTH

The diffusion length, L, for thermal neutrons in a substance may be obtained by measuring the space distribution of the neutrons in a rectangular block of the material. The neutrons may come from a source such as $Ra-\alpha-Be$ placed in the material near one end in which case the arrangement is called a sigma pile, or by locating the block adjacent to the thermal column of a reactor. The latter method gives more accurate results because of the higher intensity and more complete thermalization of the neutrons. The flux is measured with small boron counters or, more usually, with indium or dysprosium foils. The usual precautions for preventing perturbations of the flux distribution by the foils must be taken. In the case of the sigma pile, the cadmium ratio should be taken to check on the constancy of the thermalization.



To prevent scattering of thermal neutrons back into the block, it is covered with cadmium. However, this will not keep out fast neutrons, and the only way to avoid this is to place the block far from the walls of the room, the equipment, and the like. In the sigma pile, the source should not be placed too near one end.

The flux distribution along the longitudinal axis (z axis) is given by:

$$nv (z) = \frac{2S}{abD} \sum_{j,k=1}^{\infty} e^{-z/B_{jk}} (j, k \text{ odd})$$
 (108)

where: S = source strength

a,b = extrapolated lengths of the reactor in x and y directions

D = diffusion coefficient

 B_{ik} = relaxation length for (j, k) harmonic

The diffusion length is related to the relaxation lengths by:

$$\frac{1}{L^2} = \frac{1}{B_{jk}^2} - \pi^2 \left(\frac{j^2}{a^2} + \frac{k^2}{b^2} \right) \tag{109}$$

Far enough away from the source, the first harmonic, B_{11} , will predominate, leaving just one term in the equation for the flux. A plot of log nv vs z will give a straight line with slope $-1/B_{11}$. Corrections may have to be made for:

- (1) Higher harmonics
- (2) End effects
- (3) Incomplete thermalization

The side dimensions of the reactor have to be large enough so that $\pi(1/a^2 + 1/b^2)$ is small relative to B_{11}^2 . The length of the reactor must be several relaxation distances to reduce higher harmonics and end effect and to enable an accurate determination of the slope to be made.

The correction for the next higher harmonics is given by:

$$1 + \frac{1}{B_{11}} e^{\lambda_z D_{12}} \left[B_{13} e^{-z/B_{13}} + B_{31} e^{-z/B_{31}} + B_{33} e^{-z/B_{33}} \right]$$
 (110)

The observed flux is to be divided by this factor. Since the correction is small, a trial and error method is used, the first rough measurement of B_{11} giving L from which the other harmonics are calculated by Eq. (109). The corrected values of the fluxes are then replotted and a better value of B_{11} thus obtained. The process is repeated until the value for L converges to the required accuracy.

At points near the end of the reactor, the flux will decrease from the straight exponential. The correction factor by which the observed flux is to be divided is approximately:

$$1 - e^{-2(C-z)/B_{11}} \tag{111}$$

where C is the extrapolated reactor length (in the z direction) measured from the source. Again an iteration method is used. For a determination of the extrapolation length, see "Measurement of Extrapolation Distance" which follows.

By using a pile with a square cross section, a by a, and by putting two sources of equal strength at the points $(\pm a/4, 0)$, the chief higher harmonics (j, k) = (1, 3), (3, 1), (1, 5), (5, 1) can be suppressed. The harmonic correction was thus reduced to 0.5 percent

at 3 ft along the longitudinal axis in the Brookhaven graphite sigma pile. Then, the thermal neutron flux along the z axis is given by:

$$nv(z) = \frac{3\sqrt{2} S B_{11}}{\lambda_{tr} a^{2}} e^{-z/B_{11}} \left[1 - \frac{1}{B_{11}} e^{z/B_{11}} \left(B_{33} e^{-z/B_{33}} + 2 B_{35} e^{-z/B_{35}} + B_{55} e^{-z/B_{55}} - 2 B_{17} e^{-z/B_{17}} \right) \right]$$
(112)

In actual practice at Brookhaven for measurements on the stacked moderator, the following equation was used to the neutron density:

$$n(z) = \frac{Ae^{-\sqrt{z^2+h^2}/L}}{\sqrt{z^2+h^2}} \left[1 - \sqrt{\frac{z^2+h^2}{(z+2z_0)^2+h^2}} \frac{e^{-\sqrt{(z+2z_0)^2+h^2}/L}}{e^{-\sqrt{(z^2+h^2)}/L}} \right]$$
(113)

where: h =separation between the two equal sources $z_0 =$ distance from source plane to boundary

 $\ln n\sqrt{z^2+h^2}$ is plotted against $\sqrt{z^2+h^2}$ to get L. The quantity in the bracket is small and can be evaluated by iteration.

If the neutrons are not completely thermalized, the neutron density will be a function of the age in a complicated manner; see Eq. (73). The correction to L is usually small (a few percent or less) and can be made a posteriori. The uncorrected L is calculated. Then, using this L together with the age as determined from the best available spectrum for the source, the neutron density is recalculated, and a more refined value of L is obtained by replotting $\ln n \sqrt{z^2 + h^2}$ as described above.

MEASUREMENT OF EXTRAPOLATION DISTANCE

The extrapolation distance which is theoretically equal to $0.71\lambda_{tr}$ can be found in several ways, all basically related to the end effect in a sigma pile. Measurements of the flux are carried out in the same way as for the diffusion length. After correcting for the higher harmonics, the longitudinal flux is represented by:

nv
$$\alpha e^{-z/B_{11}} (1 - e^{-2(C-z)/B_{11}})$$
 (114)

where: C = extrapolated reactor height above the source

C - z = Extrapolated distance

 z_0 = geometric reactor lengths above source

(1) In one method, the value of C which gives the best fit of the data to a straight line plot of:

$$\ln \frac{nv}{1 - exp\left(-\frac{2(C-z)}{B_{11}}\right)}$$

vs z is guessed by trial and error.

(2) In another method, ⁷⁸ flux measurements are made throughout the interior of the reactor and near the surface. An average value for B_{11} is obtained from points in the interior, and the negative exponential intensity, $N(0)e^{-z/B_{11}}$, is plotted past the surface on a semi-



 \log plot as a straight line. The observed intensities, N(z), near the surface are subtracted from the straight line to yield another line of opposite slope

$$N(0)e^{-z/B_{11}} - N(z) = Ke^{z/B_{11}}$$

We can assume $K = N(0)e^{-2C/B_{11}}$. The two straight lines are extrapolated to their intersection point which is at z = C and N(z) = 0.

(3) In a third method, ¹⁹ the flux is measured at three equally spaced points along the longitudinal axis at z, $z + \epsilon$ and $z + 2\epsilon$. The observed neutron fluxes are ϕ_1 , ϕ_2 , and ϕ_3 , respectively. Then, from the equations:

$$\cosh \frac{\epsilon}{B_{11}} = \frac{\phi_1 + \phi_3}{2\phi_2} \tag{115}$$

$$\tanh \frac{C - z - \epsilon}{B_{11}} = \frac{\phi_1 + \phi_3}{\phi_1 - \phi_3} \tanh \frac{\epsilon}{B_{11}}$$
 (116)

C can be obtained by trial and error, assuming a value for B11.

THE EXPONENTIAL PILE®

The exponential pile is a subcritical assembly built so that leakage prevents a chain reaction even if K becomes larger than 1. The pile is used to determine the optimum arrangement of the core elements once the basic constituents have been chosen. Since the pile is subcritical, it requires a neutron source such as Ra-Be or the thermal column of a full-scale reactor.

The exponential pile has the main advantage over a critical assembly in requiring less material; it also requires less shielding and fewer safety devices. However, besides having a lower flux available for activation measurements and necessitating extrapolation of many of the results to critical conditions, certain special effects in full-scale reactors cannot be simulated well in an exponential pile. These effects include reactor kinetics, reactor control, temperature effects, and poisoning by fission products.

In practice, a graphite pedestal is usually placed between the exponential pile and the neutron source. The graphite pedestal serves as a cheap method for ensuring more complete thermalization of the neutron and for damping out the higher harmonics.

The most important parameter which is measured in the exponential arrangement is the buckling. For a cylindrical shape:

$$B^2 = \frac{(2.405)^2}{R^2} - K^2 \tag{117}$$

 R^2 and K^2 are determined from radial and axial flux measurements using foils. The radial measurements are fitted to the radial solution of the diffusion equation:

$$\phi = \mathbf{A_1 J_0} \left(\frac{2.405 \mathrm{r}}{\mathrm{R}} \right) \tag{118}$$

which gives R. The axial measurements are fitted to:

$$\phi = A_2 \sinh K(t - z)$$

where t = extrapolated height of the system

 L^2 , the thermal diffusion area, can be measured in an exponential pile by replacing the fissionable material with a non-multiplying substance having the same absorption and scattering cross sections. For example, a 2.5-percent mercury in lead alloy has Σ_a and Σ_s within 10 percent of ordinary uranium. Then, L^2 is found from:

$$\frac{1}{L^2} = K^2 - \frac{(2.405)^2}{R^2} \tag{119}$$

The multiplication factor is then calculable from:

$$K = (1 + L^2B^2) (1 + \tau B^2)$$

where τ is the two-group neutron age. For further details see Ref. (80); the effect of gaps is discussed in Ref. (81).

MEASUREMENT OF MIGRATION AREA AND CRITICAL RADIUS

The experimental value of the migration area of a thermal reactor is best obtained from period measurements in loadings just above critical.⁸¹

The reactor period, T, is measured as a function of the leading radius, R, in a cylindrical geometry. From T, the excess reactivity, k_{ex} , is computed from the inhour equation, Eq. (36). k_{ex} is related to the loading radius and migration area, M^2 , by:

$$k_{ex} = (2.405)^2 M^2 \left(\frac{1}{R_c^2} - \frac{1}{R^2}\right)$$
 (120)

which is a specialized form of the equation:

$$k_{\rm ex} = M^2 B_{\rm ex}^2 \tag{121}$$

where: $B_{ex}^{2} = B_{c}^{2} - B^{2}$

A plot of k_{ex} vs $1/R^2$ is linear, the intercept yielding R_c and the slope, M^2 .

The critical radius can also be determined from an exponential experiment in which the maximum flux in the pile is measured as a function of the radius.

$$\frac{1}{(\text{nv})_{\text{max}}} = A \left(\frac{1}{R} - \frac{1}{R_c} \right) \tag{122}$$

where A is a constant.

MEASUREMENT OF MULTIPLICATION*

The multiplication, M, in the intensity of a neutron source due to a surrounding sphere of multiplying material is directly measurable as a ratio of intensities with and without the sphere. Such a measurement is useful mainly for fast assemblies, in which case corrections due to change in neutron spectrum (via fission and inelastic scattering) are not too large. The interpretation of such an experiment is very simple in a one-velocity transport approximation (see Chapter 1.4).

In this case, the multiplication is a function of σR , $\eta = 1$, and σ_{tr}/σ_a

^{*} Further references are given by Carlson.82

where: R = sphere radius

$$\sigma_a = \sigma_f + \sigma_c$$

$$\eta = \nu \sigma_{\rm f}/\sigma_{\rm a}$$

 σ_{tr} = transport cross section σ = total cross section

The formula for M is:

$$\mathbf{M} = 1 + \frac{\mathbf{P}}{\mathbf{Q}} \frac{1 - \mathbf{B}(1+f)\mathbf{Q}}{1 - \mathbf{B}(1+f)\mathbf{P}} \frac{f\mathbf{Q}}{1 - (1+f)\mathbf{Q}}$$
(123)

where:

$$f = \frac{\eta - 1}{1 + \frac{\sigma_{tr}}{\sigma_a}} \tag{124}$$

$$P = 1 - e^{-\sigma R} \tag{125}$$

$$\mathbf{Q} = \frac{\mathbf{P}}{\mathbf{K}} \left[(\mathbf{1} - \mathbf{B}) + \mathbf{B} \mathbf{K} \right] \tag{126}$$

Table 1.1.15 presents values of B and K for selected values of σR . For other values of σR , quadratic interpolation is suggested.

Table 1.1.15 — Values of B and K for Selected Values of σR (LA-1273, July 1951)

σR	В	K
0	0.3600	1.5136
0.4	.4 08 4	1.5763
.8	.4 571	1.6292
1.2	.5047	1.6729
1.6	.5509	1.7099
2.0	.5946	1.7405
2.4	.6 353	1.7661
2.8	.6728	1.7872
3.2	.7069	1.8053
3.6	.7 376	1.8201
4.0	.7650	1.8318
4.4	.7895	1.8422
4.8	.8111	1.8507

JELE: JELI

100

3 E S

L ..

1175.

that i

14.00 2

es baie

26.

Single

and the be

XX.

120

RESE

127

425.0

12 43

R'A

. .

4 12D

È:LM

* r =

4 B F

:381

Ma:

1:

REFERENCES

- 1. Anderson, Neutrons from Alpha Emitters, Prelim. Rep. No. 3, Nuclear Sci. Series, Nat. Res. Council, Dec. 1948.
- 2. P. Demers, Montreal Lab. Rep. Nos. MP-74 and MP-204.
- Dacey, Paine, and Goodman, Shielding Properties of Various Materials Against Neutrons and Gamma Rays, Tech. Rep. No. 23, Lab. for Nuclear Sci. and Eng., MIT, Oct. 20, 1949.
- 4. McCallun, Nucleonics 5, July 1949, p 11.
- 5. Spinks and Graham, Can. Jour. Res. 28A, 1950, pp 60-66.
- 6. Whitmore and Baker, Phys. Rev. 78, 1950, p 799.
- 7. H. Staub, MDDC-1490, as reported in Anderson, loc. cit.
- 8. A Wattenberg, Photo-neutron Sources, Prelim, Rep. No. 6, Nuclear Sci. Series, Nat. Res. Council, July 1949.
- 9. Mobley and Lauberstein, Phys. Rev. 80, 1950, p 309.
- 10. A. Wattenberg, Phys. Rev. 71, 1947, p 497.
- 11. D. J. Hughes and C. Eggler, Phys. Rev. 72, 1947, p 902.
- 12. Hanson, Taschek, and Williams, Rev. Mod. Phys. 21, 1949, p 635.
- 13. Hughes, Pile Neutron Research, to be published.
- 14. Hughes, Pile Neutron Research Techniques, Nucleonics 6, No. 5, 1960, p 38.
- 15. Hughes, Dobbs, Cahn, and Hall, Phys. Rev. 73, 1948, p 111.
- 16. WAPD-45, p 26 (classified).
- 17. AECD-3077.
- 18. Havens, Rainwater et al., Phys. Rev. 70, 1946, pp 136 and 154.
- 19. Ibid., 71, 1947, p 65.
- 20. Ibid., 83, 1951, p 1123.
- 21. Merrison and Wiblin, Nature 167, 1951, p 346.
- 22. Fermi, Marshall, and Marshall, Phys. Rev. 72, 1947, p 193.
- 23. Brill and Lichtenberger, Phys. Rev. 72, 1947, p 585.
- 24. Selove, Rev. Sci. Inst. 23, 1952, p 350.
- 25. ORNL Quart. Prog. Rep., ORNL-1164, Phys. Div., Sept. 20, 1951.
- 26. Bernstein et al, Phys. Rev. 87, 1952, p 487.
- 27. Jordan, Detection of Nuclear Particles, Annual Rev. Nuclear Sci., Vol. 1, Annual Reviews, Inc., Stanford, Calif., 1952.
- 28. Blatt and Weisskopf, Theoretical Nuclear Physics, John Wiley and Sons, New York, N. Y., 1952, p 497.
- 29. Rossi and Staub, Ionization Chambers and Counters, McGraw-Hill Pub. Co., New York, N. Y., 1949.
- 30. Cocconi Tongiorgi et al, Rev. Sci. Inst. 22, 1951, p 899.
- 31. Fowler and Tunnicliffe, Rev. Sci. Inst. 21, 1950, p 734.
- 32. Lowde, Rev. Sci. Inst. 21, 1950, p 835.
- 33. Title, Nucleonics 8, No. 6, 1950, p 5.
- 34. Ibid., 9, No. 1, 1961, p 6.
- 35. Jahnke and Emde, Tables of Functions, Dover Press, 1945.
- Graves and Proman, Miscellaneous Physical and Chemical Techniques of the Los Alamos Project, McGraw-Hill Pub. Co., New York, N. Y., 1952, p 135.
- 37. Langsdorf, Phys. Rev. 80, 1950, p 132A.
- 38. Hibden, Langsdorf, and Kelland, Phys. Rev. 85, 1952, p 595.
- 39. Yagoda, Radioactive Measurements with Nuclear Emulsions, John Wiley and Sons, New York, N. Y., 1949.
- 40. Kaplan and Yagoda, Rev. Sci. Inst. 23, 1952, p 155.
- 41. Blau, Ruderman, and Czechowski, Rev. Sci. Inst. 21, 1950, p 232.
- 42. Hofstadter et al., Phys. Rev. 82, 1951, p 749.
- 43. Schardt and Bernstein, Phys. Rev. 86, 1952, p 583A.
- 44. Muchihause and Thomas (private communication to Falk and Poss), Amer. Jour. Phys. 20, 1951, p 429.
- 45. Grimeland, Phys. Rev. 86, 1952, p 937.
- 46. Rossi and Staub, loc. cit., p 192.
- 47. Hanson and McKibben, Phys. Rev. 72, 1947, p 673.
- 48. Skyrme et al, Rev. Sci. Inst. 23, 1952, p 204.
- 49. B. L. Cohen, Nucleonics 8, No. 2, 1951, p 29.
- 50. Nereson and Reines, Rev. Sci. Inst. 21, 1950, p 534.
- 51. Keepin and Roberts, Rev. Sci. Inst. 21, 1950, p 163.
- 52. Roberts, Training Manual for Microscopists, LA-1303, 1951.
- 53. J. H. Roberts, AECU-2007, Sept. 1951.
- 54. Jastram et al., Phys. Rev. 81, 1951, p 327A.
- 55. Hornyak, Rev. Sci. Inst. 23, 1952, p 264.
- 56. Clinton Laboratories Training Program, Lectures on Experimental Nuclear Physics.
- 57. AECU-2040.
- 58. Graves and Froman, loc. cit., Chapter 2.
- 59. Rossi and Staub, loc. cit., p 129.
- 60. Anderson et al. Phys. Rev. 72, 1947, p 16.
- 61. Weinberg and Schweinler, Phys. Rev. 74, 1948, p 851.
- 62. Hoover, et al, MDDC-1664.
- 63. Ibid., Phys. Rev. 74, 1948, p 864.

- 64. Rossi and Staub, loc. cit., p 135.
- 65. Coon and Barschall, Phys. Rev. 70, 1946, p 592.
- 66. Hall and Koontx, Phys. Rev. 72, 1947, p 196.
- 67. Baldinger, Huber, and Proctor, Phys. Rev. 84, 1951, p 1058.
- 68. Barschall, Rev. Mod. Phys. 24, 1952, p 120.
- 69. Stelson and Preston, Phys. Rev. 86, 1962, p 132.
- 70. Poole, Philos. Mag. 43, 1962, p 1060.
- 71. Rosen, Los Alamos report, to be published.
- 72. Grace et al, Phys. Rev. 82, 1961, p 969L.
- 73. H. Hurwitz, KAPL, private communication.
- 74. KAPL-329 (classified).
- 75. ORNL-181.
- 76. Harris et al, Phys. Rev. 79, 1960, p 11.
- 77. BNL-77 (classified).
- 78. CP-3364 (classified).
- 79. Glasstone and Edlund, Elements of Nuclear Reactor Theory, p 126.
- 80. Reactor Science and Technology, Vol. 1, No. 2, TID-72, 1961, p 39 (classified).
- 81. BNL-60 (classified).
- 82. Carlson, LA-1273 (classified).
- 83. Russell, Sachs, Wattenberg, and Fields, Phys. Rev. 73, 1948, p 545.
- 84. A. O. Hamon, Phys. Rev. 75, 1949, p 1794.
- 85. R. D. O'Neal, Phys. Rev. 70, 1946, p 1.
- 86. G. Scharff-Goldhaber, Phys. Rev. 59, 1941, p 937.
- 87. H. Slätis et al, Phys. Rev. 78, 1950, p 498.
- 88. Latyshev, Rev. Mod. Phys. 19, 1947, p 132.
- 89. Nuclear Data, Nat. Bur. Stand. Circ. 499, Wash., D. C., 1960.
- 90. Chart of the Nuclides, Gen. Elec. Res. Lab., 1960.
- 91. E. Bretscher and E. B. M. Murrell, Brit. Rep. No. 137, 1943.
- 92. P. Demers, N. R. C. Canada, Rep. No. 1571, Montreal, 1945.

CHAPTER 1.2

Nuclear Physics

Mathew M. Shapiro

PROPERTIES OF STABLE NUCLEI

This chapter is concerned with some fundamentals, definitions, and concepts which are important in the design of nuclear reactors. The nomenclature used in this chapter is defined in Table 1.2.1.

A knowledge of the size, mass, and spin of nuclei is useful in making educated guesses of cross sections and other quantities of interest in reactor design. Unfortunately, it is necessary to make such estimates since all of the pertinent data have not been gathered.

SIZE

The short-range character of nuclear forces makes it possible to ascribe dimensions (to within about 10⁻¹³ cm) and shape to nuclei. The very small quadrupole moments of most nuclei lead to the conclusion that the nuclei are essentially spherical. The nuclear radius is given in terms of mass number A by:

$$R = r_0 A^{\frac{1}{3}} \cdot 10^{-13} \text{ cm}$$
 (1)

where r_0 is generally between 1.3 and 1.5. Table 1.2.2 gives some values of nuclear radii. These were obtained by fitting the schematic theory of Feshbach and Weisskopf¹ to neutron cross section data.* A different radius is usually required in the high- and low-energy regions.

MASS

The known masses of the neutral atoms are given in atomic mass units (amu) in Table 1.2.3. The mass of O^{16} is defined to be exactly 16 amu. From the Einstein energy-mass formula:

$$\Delta E = \Delta mc^2$$

one finds that 1 amu = 931 mev.

The binding energy is defined as:

$$B.E. = Zm_H + (A - Z) m_n - M$$
 (2)

^{*}Other estimates can be made from lifetimes for α -radioactivity (heavy elements), electrostatic interaction of protons in mirror nuclei (light elements), and charged particle cross sections. These are generally in agreement with Eq. (1).

¹References appear at end of chapter.

where m_H and m_n are the masses of the hydrogen atom and the neutron, respectively.

Another commonly used quantity is the packing fraction, f:

$$f = \frac{M - A}{A} \tag{3}$$

The relationship between f and B.E. is:

$$\frac{B.E.}{A} + f = 0.00853 + \left(\frac{1}{2} - \frac{Z}{A}\right)(0.00081) \text{ amu } = 7.94 + \left(\frac{1}{2} - \frac{Z}{A}\right) (0.755) \text{ mev}$$
(4)

An empirical formula proposed by Fermi for the isotopic mass is:

$$\mathbf{M_{A,Z}} = 1.01464A + 0.014A^{\frac{2}{3}} - 0.041905 \, \mathbf{Z_A} + \frac{0.041905}{\mathbf{Z_A}} \, (\mathbf{Z} - \mathbf{Z_A})^2 + \lambda \, \frac{0.036}{A^{\frac{3}{4}}}$$
 (5)

where:

$$\lambda = \begin{cases} +1 & \text{if A is even, Z odd} \\ -1 & \text{if A is even, Z even} \\ 0 & \text{if A is odd} \end{cases}$$

and:

$$Z_{A} = \frac{A}{1.98067 + 0.0149624 A^{2/3}}$$
 (5a)

The binding energy of a neutron added to the target nucleus gives the excitation of the compound nucleus formed by slow-neutron bombardment. It is useful, for example, in obtaining the total energy of capture γ rays. Table 1.2.3 contains known values of the binding energy of an additional neutron, (B.E.)₇.

$$(B.E.)_{Z.A} = M_{Z.A} + m_n - M_{Z,A+1}$$
 (6)

For a given A, very often several isobars of different Z are stable. The values of A-Z for stable nuclei are plotted vs Z in Fig. 1.2.1. The solid line is a plot obtained from Eq. (5a).

In Fig. 1.2.2, experimental packing fractions from Table 1.2.3 are plotted against A. The cusps which show up at low values of A are indicative of the special stability of α clusters. The effect of the greater stability of the so-called "magic" nuclei does not show up well on a plot of this type, but from other evidence,* it appears that nuclei with Z or N = 2, 8, 20, 50, 82, and 126 are particularly stable and abundant. (There is also evidence for a special effect at Z or N = 28.) It should be noted, however, that much of the evidence is somewhat marginal. In general, these "magic nuclei" have wider level spacings and smaller capture cross sections than their neighbors (see Fig. 1.2.16).

^{*}For a review of this evidence see References (4) and (5) and numerous more recent articles on nuclear shell structure.

SPIN

Every nucleus possesses an intrinsic angular momentum which can interact with that of other nuclei. It is measured in units of h and takes integral or half-integral values according to whether the mass number is even or odd, respectively. Known spin values for the ground state are given in Table 1.2.4.

SPONTANEOUS REACTIONS — RADIOACTIVITY

Nuclei that are unstable and decay by the emission of one or more particles (a photon is here regarded as a particle) are found in nature and can be produced artificially. Many of these have sufficiently long half-lives to be observable.

The amount of substance which decays in the very short time dt is proportional to the amount of the substance present. This is the radioactive decay law and may be mathematically expressed as follows:

$$\frac{dN(t)}{dt} = -\lambda N(t) \tag{7}$$

where N(t) is the number of nuclei remaining at time t and λ is called the disintegration constant. If the number of nuclei initially present (at t=0) is designated by N(0), then by integration of Eq. (7), the number present at time t is:

$$N(t) = N(0)e^{-\lambda t}$$
 (8)

The mean-life T is the reciprocal of λ :

$$T = \frac{1}{\lambda} \tag{9}$$

and is related to the half-life, the time required for half of the initial atoms to decay, by the relation:

$$T_{1/2} = T \ln 2 = 0.693T$$
 (9a)

The actual number of nuclei that will decay in a given time interval can only be given statistically. In this sense, Eqs. (7) to (9a) describe the mean behavior. If the number of disintegrations in time interval t which is small compared to the mean-life is much less than the total number of atoms present, it can be shown that the probability for m disintegrations, p(m), is given by the Poisson distribution law:

$$p(\mathbf{m}) = \frac{\overline{\mathbf{m}}^{\mathbf{m}} e^{-\overline{\mathbf{m}}}}{\mathbf{m}!}$$
 (10)

where \overline{m} is the mean number to be expected in the time interval. Conversely, if m decays are observed in a given time interval, Eq. (10) is also the probability that m is the mean number to be expected.

It often happens that the residual or daughter nucleus produced by the decay of the parent nucleus is itself radioactive. Consider a decay chain of the type:

$$A \xrightarrow{\lambda_A} B \xrightarrow{\lambda_B} C \xrightarrow{\lambda_C} D$$



Let N_A , N_B , N_C be the number of atoms of substances A, B, C present at time t, respectively, λ_A , λ_B , λ_C be their disintegration constants (reciprocal mean-lives), and let a primary source supply A at constant rate S. Then:

$$\frac{dN_{A}}{dt} = S - \lambda_{A}N_{A}$$

$$\frac{dN_{B}}{dt} = \lambda_{A}N_{A} - \lambda_{B}N_{B}$$

$$\frac{dN_{C}}{dt} = \lambda_{B}N_{B} - \lambda_{C}N_{C}$$
(11)

Eqs. (11) state that the rate of change of the number of nuclei of any substance in the radioactive decay chain is equal to the difference between the rate at which they are created and the rate at which they undergo decay.

Case 1: In the case where there is no primary source (S = 0) but where substances A, B, and C are initially present in the amounts $N_A(0)$, $N_B(0)$, and $N_C(0)$, respectively, Eqs. (11) have the solution:

$$\begin{split} N_A(t) &= N_A(0) \ e^{-\lambda_A t} \\ N_B(t) &= N_B(0) \ e^{-\lambda_B t} + \lambda_A N_A(0) \left(\frac{e^{-\lambda_A t}}{\lambda_B - \lambda_A} + \frac{e^{-\lambda_B t}}{\lambda_A - \lambda_B} \right) \\ N_C(t) &= N_C(0) \ e^{-\lambda_C t} + \lambda_B N_B(0) \left(\frac{e^{-\lambda_B t}}{\lambda_C - \lambda_B} + \frac{e^{-\lambda_C t}}{\lambda_B - \lambda_C} \right) \\ &+ \lambda_A \lambda_B N_A(0) \left(\frac{e^{-\lambda_A t}}{(\lambda_B - \lambda_A)(\lambda_C - \lambda_A)} + \frac{e^{-\lambda_B t}}{(\lambda_A - \lambda_B)(\lambda_C - \lambda_B)} + \frac{e^{-\lambda_C t}}{(\lambda_A - \lambda_C)(\lambda_B - \lambda_C)} \right) \end{split}$$

$$(11a)$$

Case 2: In the case where there is a primary source supplying A at constant rate S but where no other radioactive substance is initially present [that is $N_A(0) = N_B(0) = N_C(0) = 0$], then Eqs. (11) have the solution:

$$\begin{split} N_{A}(t) &= \frac{S}{\lambda_{A}} \left(1 - e^{-\lambda_{A}t} \right) \\ N_{B}(t) &= \frac{S}{(\lambda_{B} - \lambda_{A})} \left[(1 - e^{-\lambda_{A}t}) - \frac{\lambda_{A}}{\lambda_{B}} \left(1 - e^{-\lambda_{B}t} \right) \right] \\ N_{C}(t) &= S\lambda_{A}\lambda_{B} \left[\frac{1 - e^{-\lambda_{A}t}}{\lambda_{A}(\lambda_{B} - \lambda_{A})(\lambda_{C} - \lambda_{A})} + \frac{1 - e^{-\lambda_{B}t}}{\lambda_{B}(\lambda_{A} - \lambda_{B})(\lambda_{C} - \lambda_{B})} \right] \\ &+ \frac{1 - e^{-\lambda_{C}t}}{\lambda_{C}(\lambda_{A} - \lambda_{C})(\lambda_{B} - \lambda_{C})} \right] \end{split}$$

$$(11b)$$

These equations are valid only when B and C are produced and destroyed solely by spontaneous decay.*

More complicated problems can be solved by taking linear combinations of the solutions of the two cases presented.

^{*}The case when A and B are removed by other processes (e.g., neutron capture) has been treated by Van Wye and J. S. Beckerley⁶ and Rubinson.⁷



Case 3: A primary source supplies A at constant rate S for time τ . The source is then removed. The amounts of A, B, and C present t units of time after the source is removed can be found by calculating $N_A(\tau)$, $N_B(\tau)$, and $N_C(\tau)$ in Case 2 and then using these values for $N_A(0)$, $N_B(0)$, and $N_C(0)$, respectively, in Case 1 to calculate $N_A(t)$, $N_B(t)$, and $N_C(t)$.

B-DECAY

Some nuclei decay by the emission of either positively or negatively charged β particles or both. In this case, the energy spectrum of the emitted particles is continuous up to a maximum energy, E. For the reaction:

$$Z^{A} \rightarrow (Z+1)^{A} + \beta^{-} \tag{12}$$

the available energy is:

$$\mathbf{E} = \mathbf{M}_{\mathbf{Z},\mathbf{A}} - \mathbf{M}_{\mathbf{Z}+1,\mathbf{A}} \tag{13}$$

For the reaction $Z^A \rightarrow (Z-1)^A + \beta^+$, the available energy is:

$$E = M_{Z,A} - M_{Z-1,A} - 2m_e$$
 (14)

where m_e is the electron mass. The energy available for capturing an atomic electron (usually from the K shell) is:

$$\mathbf{E} = \mathbf{M}_{\mathbf{Z},\mathbf{A}} - \mathbf{M}_{\mathbf{Z}-1,\mathbf{A}} \tag{15}$$

Clearly, whenever positron emission is energetically possible, electron capture is also possible. In Eqs. (13) to (15) the masses M are those of the neutral atoms.

A summary of β -decay theory has been given by Konopinski.⁸

α-DECAY

Many nuclei with A > 208 (and a few lighter ones) are found to emit α particles spontaneously. The α particle energy is given by:

$$\mathbf{E} = \mathbf{M}_{\mathbf{Z},\mathbf{A}} - \mathbf{M}_{\mathbf{Z}-2,\mathbf{A}-4} - \mathbf{M}_{\alpha} \tag{16}$$

The mean-life of the nucleus against α -decay depends strongly on the α -particle energy. An approximate relation known as the Geiger-Nuttall law asserts that the logarithm of the disintegration energy is a linear function of the logarithm of the half-life. An empirical fit is:

$$\log E \text{ (mev)} = 0.86 - 0.013 \log T_{4, \text{ (sec)}}$$
 (17)

This gives the energy from the half-life quite accurately but can be wrong by several orders of magnitude when used the other way. A treatment of α -decay systematics is given by Perlman, Ghiorso, and Seaborg.

Nuclei which emit α -particles from the ground state will not generally emit them from an excited state unless the excitation energy is high enough to reduce the life time against α -emission to about 10^{-13} sec, the order of magnitude of that for γ -emission.

y-RAY EMISSION

The emission of a γ -ray signifies the transition between two states of the same nucleus. The energy of the γ -ray is, of course, the energy separation of the two levels. Since the intrinsic spin of a photon is unity (in units of \hbar) all γ -emission implies a change of spin (either in magnitude or direction) of the nucleus. Gamma-ray emission processes are



classified according to the multipole order of the transition. When the spin change is unity, we speak of a dipole transition; when it is two, of a quadrupole transition; etc. The type of transition, electric or magnetic, depends on the parity change. Dipole transitions are electric if there is a parity change and magnetic if there is not. Quadrupole transitions follow just the opposite rule. Weisskopf and Blatt¹⁰ give the following expressions for the probability of emission per unit time for electric radiation of multipole order 1:

$$P_{E} = \frac{1}{T_{E}} \cong \frac{4.4 \ (1+1)}{1[1 \cdot 3 \ \dots \ (2l+1)]^{2}} \left(\frac{3}{l\cdot + 3}\right)^{2} \left(\frac{\hbar \omega}{197 \ \text{mev}}\right)^{2l+1} \cdot (R \ \text{in} \ 10^{-13} \ \text{cm})^{2l} \ 10^{21} \ \text{sec}^{-1}$$
 (18)

and for magnetic radiation of multipole order 1:

$$P_{\mathbf{M}} = \frac{1}{T_{\mathbf{M}}} \cong \frac{1.9}{4.4} P_{\mathbf{E}} (R \text{ in } 10^{-13} \text{ cm})^{-2} \text{ sec}^{-1}$$
 (18a)

where $\hbar\omega$ is the energy of the radiation in mev and R is the nuclear radius.

It should be noted that the above expressions are only very rough estimates. The actual values are likely to be smaller than these estimates by factors up to 1000 or even higher in the case where the wave functions of the initial and final states overlap only slightly.

DATA

A new table of isotopes supplied by G. T. Seaborg is reproduced here as Table 1.2.4.

RANGE-ENERGY RELATIONS

In traversing matter, charged particles lose energy by radiation, by suffering nuclear collisions, and, most important, by ionizing atoms in the medium. In air, 32.5 ev is the energy dissipated per ion pair produced.

This figure is about the same for other media. The slowing down and transport of neutrons is discussed in detail in Chapter 1.3. Photons lose energy by means of the Compton effect, the photoelectric effect, and pair production. These mechanisms are discussed in detail in Section 1.2.

For charged particles, the number of ion pairs per unit path length increases rapidly as the velocity decreases, giving rise to a well defined range.

Electron ranges are usually given in terms of an areal density, milligrams of material per square centimeter. The range of electrons in aluminum¹¹ is given to within 5 percent by:

$$412E^{(1.265-0.0954 \text{ lnE})}$$
mg/cm²

if 0.01 < E < 2.5 mev, and by:

 $530E - 106 \text{ mg/cm}^2$

for E > 2.5 mev.

Theoretically, one would expect the range to be inversely proportional to the number of atomic electrons per unit volume. The range in mg/cm^2 would then be proportional to A/Z and roughly independent of the material.

The range of α -particles in air at standard conditions is given^{12,13} to within about 10 percent by:

$$R_{\alpha}(cm) = 0.56E \text{ (mev) for } 0 < E < 4 \text{ mev}$$



and by:

$$R_{\alpha}(cm) = 1.24E - 2.62$$
 for $4 < E < 8$ mev

Experimentally, it is found that the range of protons in air is given quite accurately by:

$$R_p(cm) = 1.007R_{\alpha}(3.971E) - 0.20$$

where E is the proton energy in mev and R α the range of α -particles in air at energy 3.971E.

Theory predicts that for given charge Z, the range depends only on the velocity. Hence, for all helium and hydrogen isotopes:

$$R_{Z,M}(E) = \frac{M}{M_0} R_{Z,M_0} \left(\frac{M_0}{M} E \right)$$

In substances other than air, the ranges of protons and α -particles¹⁴ are given to within 15 percent over the energy range of interest here by:

$$\overline{R}$$
 (E) [mg/cm²] = 0.56A^{1/3} R(E)_{air} [cm]

where A is the mass number of the stopping material.

The range energy relations for heavy particles is complicated and will not be treated here in general. A special case of interest is the range of fission products. Following neutron induced fission of U^{233} , U^{235} , or Pu^{239} , the most probable energy of the light fragment is about 92 mev and that of the heavier fragment about 60 mev. ^{15,16} In about 0.2 percent of fissions, an alpha-particle with a probable energy of about 14 mev is formed. Since about 30 ev is lost per ion pair created, about 6×10^6 ion pairs will be formed by the two fragments.

Range measurements of the fission fragments show a grouping about two values corresponding to the light and heavy fragments. In air, the ranges for the light and heavy fragments¹⁷ are 2.3 and 1.8 cm, respectively. The ranges in aluminum are 3.7 and 2.8 mg/cm². Segrè and Wiegand showed that the relative stopping powers for fission fragments in collodion, aluminum, copper, silver, and gold were roughly the same as for alpha particles. Not distinguishing between fission fragments, they give for the maximum range in several materials the values in Table 1.2.5. Hence, these values are for the most energetic (light) fragments.

THE FISSION PROCESS

As used here, the term "fission" means the splitting of a nucleus into approximately equal fragments. These particles emerge in a highly excited state. This results in the almost immediate emission of neutrons and γ -rays from them. The resulting fragments still have too great a neutron-to-proton ratio to be stable against β -decay, and they undergo a series of β -disintegrations before becoming stable nuclei. Sometimes these β -decays are accompanied by γ -emission and sometimes by neutron emission. These neutrons, appearing after one or more β -disintegrations have taken place, are the so called delayed neutrons.

The average number of neutrons, delayed and prompt, which appear in fission varies according to the fissionable element and probably the incident neutron energy.



FISSION THRESHOLDS AND CROSS SECTIONS

Presumably, any nucleus will undergo fission if its excitation energy is great enough. The amount of excitation required is given directly by the threshold for γ -induced fission. In some isotopes, fission occurs spontaneously. Thresholds for γ -induced fission and data for spontaneous fission are given in Table 1.2.6 for some isotopes.

Thresholds for neutron-induced fission in these heavy elements will be smaller by the amount of the binding energy of the neutron to the target nucleus. In some cases, thermal neutrons can produce fission, and in others, a threshold exists. The known neutron fission cross sections are shown as a function of energy in Figs. 1.2.3 to 1.2.12, which are taken from the report of the AEC Neutron Cross Section Advisory Group (BNL-170 and 170A).

THE FISSION FRAGMENTS

FISSION YIELDS

The immediate product from a fission is two fragments of which the most probable mass numbers are about 95 and 139; the probability of symmetrical fission is very small. Figure 1.2.13 shows the fission yields for slow-neutron fission of U²³⁶, U²³⁸, and Pu²³⁹ plotted vs A. The fission yield is the probability of forming a nucleus of mass A. The sum of the yields equals two since there are two fragments formed. Table 1.2.7 gives the fission yield of various isotopes formed after fission.¹⁸

KINETIC ENERGY

The kinetic energy of the pair of fission fragments depends upon the way the nucleus splits. The energy distribution of fission fragments has two peaks: one for the heavy fragment around 65 mev and the other for the light fragment at about 95 mev. There is a considerable spread around the peaks when the number of fragments having a given energy are plotted vs energy. The width at half maximum around the higher energy is 12 mev and around the lower energy is 20 mev. Table 1.2.8 gives the results of Brunton and Hanna¹⁵ and of Deutsch and Ramsey¹⁶ for the kinetic energy of the fragments.

The compound nucleus occasionally splits into three particles. In one out of 250,000 fissions, the three particles have approximately equal masses; in one out of every 550 fissions, an alpha particle with a maximum energy of 26 mev and a probable energy of 14 mev is formed; in one out of 76 fissions, an as yet unidentified short-range particle of low mass number is formed. The range of the fission fragments is discussed previously in this chapter.

TIME DEPENDENCE OF THE RADIATION FROM FISSION PRODUCTS

A modification of the Wigner and Way expression for P_8/P_0 , the ratio of the rate of heat generation after shutdown to the rate of heat generation during operation, has been obtained²¹ to fit available experimental data for natural uranium. The heat production owing to U^{239} and Np^{239} after shutdown is given in Eqs. (19a) and (19b):

$$\frac{\mathbf{P}(\mathbf{U^{239}})}{\mathbf{P_0}} = 0.0025 \left\{ e^{-\frac{\mathbf{T_s}}{2040}} - e^{-\left(\frac{\mathbf{T_s} + \mathbf{T_0}}{2040}\right)} \right\}$$
(19a)

$$\frac{P(Np^{239})}{P_0} = 0.0013 \left\{ e^{-\frac{T_s}{290000}} - e^{-\left(\frac{T_s + T_0}{290000}\right)} \right\}$$
 (19b)



where T_s = time in seconds since operation T_0 = operation time in seconds

The authors indicate $P(Np^{239})$ as given above may be low for T_S less than the Np^{239} decay time since new data point toward a value of 0.0023 instead of 0.0013 in Eq. (19b).

The Untermyer and Weills natural-uranium data fit is:

$$\frac{P_s}{P_0} = 0.1 \left\{ (T_s + 10)^{-0.2} - 0.87 (T_s + 2 \times 10^7)^{-0.2} \right\} - 0.1 \left\{ (T_s + T_0 + 10)^{-0.2} - 0.87 (T_s + T_0 + 2 \times 10^7)^{-0.2} \right\}$$
(20)

with the accuracy expected to be:

under 1 sec	large error
1 - 10 ² sec	± 50%
10 ² - 10 ⁴ sec	± 30%
10 ⁴ - 10 ⁶ sec	± 10%
10 ⁶ - 10 ⁸ sec	± 50%

The heat production for U²³⁵ can be estimated by subtracting Eqs. (19a) and (19b) from (20). The experimental data and graphs of the results can be found in the reference.

For the time dependence of γ rays, the reader should refer to Section 1.2. The distribution of energy per fission is given in Table 1.2.11.

THE CAPTURE-TO-FISSION RATIO

When the compound nucleus has been formed by neutron bombardment, fission does not always occur because it must compete with other processes. The most important one here is γ -emission, for this process represents a loss of the absorbed neutron. In the following, the ratio of the capture cross section to the fission cross section will be denoted by α .

PROMPT NEUTRON AND GAMMA SPECTRA

Emission of prompt neutrons and γ -rays is probably completed within 10^{-15} sec after fission. The energy distribution of the prompt neutrons from thermal fission has been measured by B. E. Watt, D. Hill, T. W. Bonner, R. A. Ferrell, and M. C. Rinehart (LA-718). The neutron kinetic energy varies over a range exceeding 18 mev. The distribution is fairly well represented from 0.1 to 18 mev by the formula:

$$n(E) = \sqrt{\frac{2}{\pi e}} \sinh \sqrt{2E} e^{-E}$$
 (21)

where n(E) is normalized to one neutron and E is in mev.

The energy distribution of the γ -rays is discussed in Sect. 1.2. The total γ energy is about 5 mev/fission. It is not clear whether there are five 1-mev photons or two 2.5-mev photons.

BETA DECAY AND DELAYED NEUTRONS

The fission fragments have too large a neutron-to-proton ratio to be stable against β -decay even after emitting some neutrons and γ -rays. They have to undergo about three successive β -disintegrations before achieving stability. Some isotopes have sufficient energy following a β -disintegration to emit a neutron. This neutron appears after a mean time at least as long as the mean lifetime of the longest-lived β -emitter preceding it in the

decay chain. The β -emitters that lead to the important delayed neutrons are those in Table 1.2.9. Table 1.2.10 gives a summary of the present knowledge of delayed neutrons from fission.

SUMMARY OF ENERGY RELEASE IN FISSION

Table 1.2.11 summarizes the distribution of energy from an average fission.

The kinetic energy of the fission products and of the β -rays appears as heat very close to the place where fission took place. This can be seen from the data presented in this chapter under "Range-energy Relations." The γ -rays have, relatively, much longer mean-free-paths, and their energy is more widely distributed throughout the reactor.

The neutrino energy is not useful for the generation of heat, and therefore, the heat production capacity from fission itself is about 191 mev/fission. On the other hand, approximately half of the fission neutrons will be captured parasitically in the reactor giving rise to capture γ -rays of approximately 7 mev total energy. This brings the available energy back to about 200 mev/fission.

COLLISION REACTIONS

LABORATORY AND CENTER-OF-MASS COORDINATES

Consider a particle of mass m_1 and speed v_1 striking a particle m_2 which is initially at rest. Let E be $\frac{1}{2}$ $m_1v_1^2$ and $p = m_1v_1$. The kinetic energy available for a nuclear reaction, E₀, is E less the kinetic energy of the center of mass:

$$\mathbf{E_0} = \frac{1}{1+\gamma} \mathbf{E} \tag{22}$$

where $\gamma = m_1/m_2$.

If one defines a reduced mass as $\mu = m_1 m_2/(m_1 + m_2)$, then $E_0 = \frac{1}{2} \mu v_1^2$. If the momentum of a particle of mass μ which has the kinetic energy E_0 is denoted by p_0 , then:

$$p_0 = \frac{1}{1+\gamma} p \tag{23}$$

If the polar axis is taken in the direction of the incident particle and if θ_0 and θ are the angles that its velocity vector makes with this axis after the collision in the center-of-mass system and in the laboratory system, respectively, then:

$$\tan \theta = \frac{\sin \theta_0}{\gamma + \cos \theta_0} \tag{24}$$

The differential cross sections in the center-of-mass system and laboratory system are related by:

$$\sigma(\theta) = \frac{(1 + \gamma^2 + 2\gamma \cos\theta_0)^{3/2}}{|1 + \gamma \cos\theta_0|} \sigma(\theta_0)$$
 (25)

If the reaction produces two new particles of mass m_3 and m_4 ($m_3 + m_4 = m_1 + m_2$), and an amount of energy Q is transformed from internal to kinetic energy, and if m_3 is the observed particle, Eqs. (24) and (25) still hold but with γ now being equal to:

$$\gamma = \left(\frac{\mathbf{m_1} \mathbf{m_3}}{\mathbf{m_2} \mathbf{m_4}} \frac{\mathbf{E_0}}{\mathbf{E_0} + \mathbf{Q}}\right)^{1/2}$$



NEUTRON CROSS SECTIONS

The interaction of neutrons with nuclei can often be explained in terms of the formation of a compound nucleus (likely exceptions are reactions involving light nuclei) which can exist only in more or less well defined energy states. When the kinetic energy of the incident neutron plus its binding energy falls within the width of an energy level of the compound nucleus, the probability of forming the compound nucleus is greatly increased. Cross sections for all processes associated with the formation of that level will exhibit a resonance behavior.

Generally speaking, the widths of nuclear levels are smaller than the spacing between levels in all nuclei at very low energies and in light nuclei even for energies of several mev. As the mass number of the nucleus increases and as the excitation energy increases, the levels become wider and more dense. Finally, for neutrons of sufficiently high energy impinging on heavy nuclei, the levels overlap and the cross sections become smooth functions of energy. In terms of this model of nuclear reactions, certain general properties of cross sections can be given. These, along with some empirical correlations, can be used as a basis for informed guesses when the desired cross section has not been measured.

In the following discussion, the neutron energy is divided into three regions: (1) less than 1 kev, (2) 1-500 kev, and (3) 0.5 to 10 mev. Neutron reactions show different qualitative behavior in these regions, but the regions are not well defined, and the transition from one into the other is of course gradual.

It is also useful to divide the target nuclei into three groups: (1) the light nuclei, 1 < A < 25; (2) the intermediate nuclei, 25 < A < 80; (3) the heavy nuclei, 80 < A < 240. There is considerable overlap among these categories, and many properties of one group can be extended into the neighboring ones. This grouping, convenient for discussion, is schematically indicated in Fig. 1.2.14.

REGION A. LIGHT NUCLEI 25, 26

Except for the (n,α) reactions in Li⁶ and Bi⁰ and the (n,p) reaction in He³, the scattering cross section is nearly equal to the total cross section and in fact differs from it only by the (n,γ) cross section until energies sufficiently high for inelastic scattering to set in are reached. Other than this, it is almost impossible to give any general rules describing nuclear reactions with these elements. Levels are few and far apart so that the cross sections in the neighborhood of these isolated resonance energies should have a dependence on energy given by the Breit-Wigner single-level formula discussed below. Some of the nuclear radii and the threshold energies are so small that charged-particle emission can occur even at energies near thermal. The first level is usually several mev above the ground state, and inelastic scattering tends to occur only at energies greater than a few mev.

REGION B. LOW AND INTERMEDIATE ENERGIES, INTERMEDIATE NUCLEI

The predominant reactions in this group are elastic scattering and radiative capture. Inelastic scattering is usually not possible since the first excited states of the compound nucleus are several hundred kev above the ground state. Reactions (n,p) and (n,α) are weak because of the coulomb barrier and threshold effects. The levels are well separated, and the capture and elastic scattering cross sections should be well represented by the Breit-Wigner one-level formula. This yields for the capture cross section:

$$\sigma_{a} = g_{jl} (2l + 1) \pi \lambda^{2} \frac{\Gamma_{n} \Gamma_{a}}{(E - E_{r})^{2} + \frac{\Gamma^{2}}{4}}$$
 (26)



and for the scattering cross section:

$$\sigma_{sc} = (2l + 1) g_{jl} 4\pi \lambda^{2} \left| \frac{\Gamma_{n/2}}{E - E_{r} + i\Gamma/2} + e^{i\delta_{l}} \sin \delta_{l} \right|^{2} + (2l + 1) (1 - g_{jl}) 4\pi \lambda^{2} \sin^{2} \delta_{l} + \sum_{l' \neq l} (2l' + 1) 4\pi \lambda^{2} \sin^{2} \delta_{l'}$$
(27)

for a resonance formed by neutrons having orbital quantum number 1.

 g_{jl} is a statistical factor;* π is the reduced wave-length of the neutron; Γ_n the width for elastic scattering of neutrons; Γ_a the absorption width; and $\Gamma = \Gamma_n + \Gamma_a$ the total width. E is the neutron energy and E_r the resonance energy. All dynamic quantities are in the center-of-mass system. The phase shifts δ_l are those which would be obtained for scattering from a "hard" sphere. The first three are given by the formulae:

$$\delta_0 = -x$$

$$\delta_1 = -x + \frac{\pi}{2} - \cot^{-1} x$$

$$\delta_2 = -x + \pi - \cot^{-1} \left(\frac{x^2 - 3}{3x} \right)$$
(28)

where:

$$x = R/x (1/x = k = 0.222 \sqrt{E(mev)} 10^{13} cm^{-1})$$

In the scattering formula, the first term on the right represents the resonance scattering and the coherent part of the potential scattering;† the second, the non-interfering portion of the potential scattering; and the last is potential scattering by neutrons having I values different from the resonant one.

Neutron widths in this energy region are given approximately by:

$$\Gamma_{\rm nl} = 0.15 \sqrt{\rm E} \ 10^{-3} \ \rm D \ T_{\rm l}$$
 (29)

where E is in ev and D is the order of the distance between levels of the same spin and parity. T_l is the transmission factor for penetration of the centrifugal barrier. The first three have the values:

$$T_0 = 1$$

$$T_1 = \frac{x^2}{1 + x^2} \qquad x = R/\chi$$

$$T_2 = \frac{x^4}{9 + 3x^2 + x^4}$$
(30)

$$g_{jl} = \frac{(2j+1)}{2(2l+1)(2l+1)}$$

^{*}If the spin of the target nucleus is I, that of the compound nucleus j, and the orbital angular momentum of the neutron l, then:

[†] Potential scattering refers to that portion of Eq. (27) which does not exhibit resonance behavior.

The capture width is generally of the order of 1 to 10 ev. If the end products have kinetic energies much greater than the incident neutron energy (as is often the case), Γ_a is relatively independent of energy. D varies very much from one nucleus to another, ranging from a few to several hundred kev. Because of the large level spacing, elastic scattering is usually the predominant process here even at thermal energies.

REGION C. HEAVY NUCLEI -LOW ENERGY

The only possible reactions in this group are those induced by l=0 neutrons. These are primarily elastic scattering, radiative capture, and neutron-induced fission. The coulomb barrier precludes the probability of charged-particle emission.

The total cross section often shows very close resonances. One finds distances between resonances of the order of 10 to 100 ev; often, however, none are found in certain isotopes. There are indications that even A nuclei have resonance spacings of much more than 100 ev and that the nuclei with "magic" numbers of protons and neutrons show very large resonance spacings (many kev).

The neutron width is expected to be much smaller than the capture width which, except for fission, is primarily due to (n, γ) processes. In all measured cases, it was found that:

$$0.03 \text{ ev} < \Gamma_r < 0.15 \text{ ev}$$
 (31)

The Doppler effect (cf., Chapter 1.6) can be important in this energy region. Because of the thermal motion of the target nuclei of mass A, the relative energy can be spread over an interval which is approximately:

$$\Delta E \sim 0.1 \sqrt{E} A^{-\frac{1}{2}} ev$$

where E is in ev. This can become of the order of resonance widths at several hundred ev. The thermal capture cross section can be very large owing to the 1/v law. Most elements exhibit thermal capture cross sections in excess of 5 barns with the exception of Ba, Sn, Pb, and Bi which are "magic" nuclei.

REGION D. HEAVY NUCLEI - INTERMEDIATE ENERGY

The low-energy region was characterized by the absorption width far exceeding the neutron width. The latter increases with energy as \sqrt{E} while the former is expected to be relatively constant in the intermediate energy range. For level spacings of the order of 10 ev, elastic scattering is expected to exceed capture at energies above several kev.

Since level spacings are only of the order of a few ev, one is generally interested in average values of the cross sections. The average value of the cross section for radiative capture is given by:

$$\langle \sigma(n,\gamma) \rangle_{av} = 2\pi^2 (R + \pi)^2 \frac{\Gamma_r}{D}$$
 (32)

For heavy nuclei, Γ_r/D is found to be of the order of 10^{-2} or 10^{-3} with the exception of "magic" nuclei which may show values a few hundred times less than this.

The value of the total cross section averaged over many resonances can be estimated from Fig. 1.2.15 for neutron energies from a few kev upward for the heavy nuclei. This cross section is primarily elastic scattering and radiative capture (except for the fissionable elements), inelastic scattering and charged particle reactions being unlikely below 0.5 mev.



REGION E. HEAVY AND INTERMEDIATE NUCLEI—HIGH ENERGIES

This group is characterized by the appearance of inelastic scattering and reactions involving the emission of charged particles somewhere in this energy range. Below the energy at which this occurs, the behavior is similar to that in the intermediate energy range. For a given energy in this region, the level spacing decreases with increasing mass leading to small neutron widths and an increase in radiative capture with A. This is shown in the measurements of Hughes which are reproduced in Fig. 1.2.16.

For a given nucleus, the (n,γ) cross section decreases with increasing energy once the threshold for inelastic scattering is passed. For energies exceeding about 2 mev, the reaction cross section (total cross section minus elastic scattering cross section) is predominantly inelastic.

In regions C, D, and E, the schematic theory of Feshbach and Weisskopf should be applicable. Figure 1.2.15 shows the total cross section vs energy. Figure 1.2.17 shows the transport cross section vs R/x, calculated by assuming the inelastic scattering to be spherically symmetrical, cf. Eq. (52).

Figures 1.2.15 and 1.2.17 should be valid at low energies if they are there interpreted as averaged over many resonances.

Figure 1.2.18 gives the reaction cross section according to the schematic theory. This curve is expected to be valid only when the compound nucleus can decay in many ways. This means that the reaction cross section is primarily the inelastic scattering cross section.

THE RECIPROCITY THEOREM²⁷

The reciprocity theorem permits the cross section of a nuclear reaction to be expressed in terms of the inverse process. Let the cross section for the reaction:

$$Be^9 + He^4 \rightarrow C^{12} + n$$
 (33a)

be $\sigma_{12}(E_1)$ where E_1 is the collision energy of the Be⁹ and He⁴ nuclei, and let the cross section for the inverse process:

$$C^{12} + n \rightarrow Be^{9} + He^{4}$$
 (33b)

be $\sigma_{21}(E_2)$. E_2 is fixed by the energy E_1 and the Q value of the reaction shown in Eq. (33a). The reciprocal relation between these cross sections is:

$$\frac{\sigma_{12}(E_1)}{\sigma_{21}(E_2)} = \frac{g_2}{g_1} \frac{p_2^2}{p_1^2} \tag{34}$$

where g_2 and g_1 are the statistical weights and p_2 and p_1 the relative momenta of the pairs C^{12} – n and Be^9 – He^4 , respectively.*

$$\frac{\mathbf{p_2^2}}{\mathbf{p_1^2}} = \frac{\mu_2 \mathbf{E_2}}{\mu_1 \mathbf{E_1}}$$

where μ is the reduced mass of the pair. All dynamic quantities are in the center-of-mass system.



^{*}The statistical weight is (2I + 1) (2I' + 1) where I and I' are the spins of the particles of a given pair. Hence, since the spin of carbon is zero and that of the neutron is $\frac{1}{2}$, $g_2 = 2$. When all of the constituents are particles (no photons), then:

The reciprocity theorem also provides a relation between the cross section for forming a compound nucleus with spin j by neutron bombardment and the width for decay of the nucleus by emitting a neutron with orbital angular momentum 1. This relation is:

$$\Gamma^{(1)} = \frac{\sigma_{\rm C}^{(1)} \ D_{\rm C}^{(j)}}{(21+1) \ 2\pi^2 \lambda^2} \tag{35}$$

where $\sigma_c^{(1)}$ is the cross section for formation of the nucleus by neutrons of orbital angular momentum 1, and $D_c^{(j)}$ is the density of levels with spin j.

LEVEL DENSITY FORMULA

In the preceding discussion, the distance between energy levels appeared quite often. The density of levels 1/D has been estimated by Weisskopf to be constant up to several mev above the ground state and then to rise according to the formula;

$$\frac{1}{D(E)} = Ce^{\sqrt{aE}}$$
 (36)

C and a are functions of A, and rough approximations are plotted in Fig. 1.2.19 for odd A nuclei. Little is known about level spacings for even nuclei except that they are much larger than for odd nuclei.

ELASTIC SCATTERING

COLLISION MECHANICS

Consider a neutron impinging on a nucleus of mass A. Taking the polar axis to be the initial direction of the neutron, the process of elastic scattering can be schematically represented by Fig. 1.2.20 in the laboratory system and Fig. 1.2.21 in the center-of-mass system.

The relation between θ and θ_0 is:

$$\cos \theta = \frac{A \cos \theta_0 + 1}{(A^2 + 2A \cos \theta_0 + 1)^{1/2}}$$
 (37)

Let us define:

$$\alpha \equiv \left(\frac{\mathbf{A} - 1}{\mathbf{A} + 1}\right)^2 \tag{38}$$

Then the neutron energy in the laboratory system before collision E_1 is related to that after collision by:

$$E_{2}/E_{1} = \frac{1}{2} \left[(1 + \alpha) + (1 - \alpha) \cos \theta_{0} \right]$$
 (39)

The greatest energy loss occurs for $\theta = \pi$ (backward scattering) when $E_2 = \alpha E_1$. Hence, the final energies lie between E_1 and αE_1 .

A quantity of interest is the mean logarithmic energy loss, ξ , which is defined as:

$$\xi \equiv \int_{\alpha E_1}^{E_1} \ln \frac{E_1}{E_2} g(E_2, E_1) dE_2$$
 (40)

where $g(E_2, E_1) dE_2$ is the probability of scattering from energy E_1 into the energy interval dE_2 about E_2 .

Another quantity of interest, the average value of the cosine of the scattering angle (where the average is taken over all possible collisions), is defined as:

$$\overline{\cos \theta} = \int \cos \theta \, \frac{\sigma_{\rm e}(\theta)}{\sigma_{\rm e}} \, \mathrm{d}\Omega$$

Isotropic Scattering

Isotropic scattering signifies that the differential cross section is not a function of θ_0 , i.e., that it is spherically symmetrical in the center-of-mass system. In this case, neutrons are scattered uniformly into the energy interval between E_1 and αE_1 ; i.e.:

$$g(E_2, E_1) = \frac{1}{E_1(1-\alpha)} \qquad \alpha E_1 \leq E_2 \leq E_1$$

$$= 0 \qquad E_2 < \alpha E_1 \qquad (41)$$

and it can be shown that:

$$\xi = 1 + \frac{\alpha}{1 - \alpha} \ln \alpha \tag{42}$$

For mass > 10, an approximation accurate to 1 percent or less is:

$$\xi \approx \frac{2}{A + \frac{2}{4}} \tag{43}$$

For isotropic scattering, the average value of the cosine of the scattering angle in the laboratory system is:

$$\overline{\cos \theta} = \frac{2}{3A} \tag{44}$$

Values of ξ , $1-\alpha$, $\ln 1/\alpha$, $\cos \theta$, and the average number of collisions required to thermalize 2-mev neutrons $[((1/\xi)\ln(2\times10^6/0.025))]$ are given in Table 1.2.12 for materials of interest.

Equation (41) gives the energy distribution of neutrons after one collision. The number of neutrons $N(n,E_2)$ having an energy between E_2 and E_2 + dE_2 after n collisions can be obtained:

$$N(n,E_2) = \frac{\left(\frac{1}{1-\alpha}\right)^n}{E_1(n-1)!} \sum_{k=0}^{\bar{k}} {n \choose k} (-)^k \ln \frac{\alpha^k E_1}{E_2}$$
 (45)

where \overline{k} is the largest value of k for which the logarithm is positive. The expression is, of course, zero for $E_2 < \alpha^n E_1$.

For $E_2 \ll E_1$, this becomes:

$$N(n,E_2) \approx \frac{\left(\frac{\xi-1}{\alpha}\right)^{n-1}}{E_1(1-\alpha)} \left(\frac{6}{\pi n}\right)^{l_2} e^{-12n\chi^2} \frac{\sinh 6\chi}{6\chi}$$

where:

$$\chi = \frac{\log E_1/E_2}{n \log^{1}/\alpha} - \frac{1}{2}$$
 (45a)

Results for mixtures are given in Marshak's review article. 28

Equation (45) is not valid when the scattering material is hydrogen ($\alpha = 0$). This case, however, admits of a closed solution. Equation (46) gives the probability that after n collisions with hydrogen nuclei, the neutron will have an energy between E_2 and $E_2 + dE_2$:

$$N(n,E_2) = \frac{1}{(n-1)! E_1} \left(\ln \frac{E_1}{E_2} \right)^{n-1}$$
(46)

Anisotropic Scattering

When the scattering is not isotropic in the center-of-mass system, Eq. (41) and those results which depend upon it do not hold. In general:

$$g(E_2, E_1) = 4\pi \frac{\sigma_{\Theta}(\theta_0)}{\sigma_{\Theta}} \frac{1}{(1 - \alpha)E_1} \qquad \alpha E_1 \le E_2 \le E_1$$

$$= 0 \qquad E_2 < \alpha E_1 \qquad (47)$$

where $\sigma_{\rm e}(\theta_{\rm e})$ is the differential elastic scattering cross section in the center-of-mass system defined so that:

$$\sigma_{\mathbf{e}} = 2\pi \int_0^{\pi} \sigma_{\mathbf{e}}(\theta) \sin \theta \ d\theta$$

For isotropic scattering in the center-of-mass system:

$$\frac{\sigma_{\rm e}(\theta_{\rm 0})}{\sigma_{\rm e}} = \frac{1}{4\pi}$$

The average logarithmic energy loss can still be computed from Eq. (40) in two cases of interest.* Let:

$$\sigma_{\mathbf{e}}(\theta_0) = \frac{\sigma_{\mathbf{e}}}{4\pi} + \frac{3}{4\pi} \sigma_1 \, \mathbf{p_1} \, (\cos \, \theta_0) + \dots$$

Then for a heavy nucleus where $(A - 1/A + 1)^2 \approx 1$ and $\theta_0 \approx \theta$:

$$\xi = \xi_0 \left(1 - \frac{\sigma_1}{\sigma_e} \right) = \xi_0 \left(1 - \overline{\cos \theta} \right) \tag{48}$$

where ξ_0 is the average loss in ln E for isotropic scattering. For arbitrary A, one can also find ξ if one restricts oneself to a $\sigma_e(\theta_0)$ containing only σ_e and σ_1 . The result in this case is:

^{*} Mathew M. Shapiro, unpublished.

$$\xi = \xi_0 - \frac{3}{2} \left(\frac{A+1}{2A} \xi_0 - 1 \right) \frac{1 - \frac{2}{3A} - (1 - \overline{\cos \theta})}{1 - \frac{3}{5A^2}}$$
(49)

For large A, this reduces to:

$$\xi = \xi_0 \left[(1 - \overline{\cos \theta}) \left(1 + \frac{3}{4A} \right) - \frac{1}{12A} \right] \tag{49a}$$

CROSS SECTIONS

Thermal values of the elastic scattering cross sections are contained in Table 1.2.17. The elastic cross section is expected to equal approximately the total cross section in the middle-energy region where (n,γ) cross sections are small. Near thermal energies, where radiative capture can be dominant and above the threshold for inelastic scattering, σ_e will be noticeably less than the total cross section. At energies high enough for the schematic theory to apply, the elastic scattering cross section approaches $\pi(R + \chi)^2$. χ is the reduced wavelength of the neutron.* This is half the asymptotic value of the total cross section. The total cross section as predicted by the schematic theory is given in Fig. 1.2.15.

Concerning the angular distribution of scattered neutrons, some experimental work on light elements has been done at Los Alamos. Their results for the differential elastic scattering cross section are given in Figs. 1.2.22 to 1.2.28. The most probable incident neutron energy was about 1.7 mev. Table 1.2.13 gives their values of $\sigma_e(1-\overline{\cos\theta})$.

Transport Cross Section

A derived quantity used in diffusion theory is the transport cross section, σ_{tr} . A commonly used definition of this quantity is:

$$\sigma_{tr} = 2\pi \int_0^{\pi} \sigma_{s}(\theta) (1 - \cos \theta) \sin \theta \, d\theta = \sigma_{s}(1 - \overline{\cos \theta})$$
 (50)

where σ_{g} is the scattering cross section (elastic + inelastic) other definitions are in use.

If the elastic scattering is isotropic and there is no inelastic scattering, one finds from Eq. (44):

$$\sigma_{\rm tr} = \sigma_{\rm e} \left(1 - \frac{2}{3A} \right) \tag{51}$$

By assuming the inelastic scattering to be spherically symmetric, one obtains:

$$\sigma_{tr} = \sigma_{in} + 2\pi \int_0^{\pi} \sigma_e(\theta) (1 - \cos \theta) \sin \theta d\theta$$
 (52)

Table 1.2.14 contains some measured values of σ_{tr} .

CRYSTAL EFFECTS 30, 31, 32 AND CHEMICAL BINDING

When the wavelength of thermal neutrons is of the same order of magnitude as the interatomic distances in crystals, the neutrons scattered from such crystals exhibit interference

^{*} $\pi = 4.5E^{-1/2}$ 10⁻¹³ cm. where E is in mev.

effects. Thus, the scattering cross sections for very-low-energy neutrons become energy dependent. The cross sections of Be and C in Figs. 1.2.29 and 1.2.30 illustrate this effect.

It is the coherent scattering cross section of the individual atoms that determines the interference properties of neutrons. (For coherent scattering, the scattered wave is capable of interfering with the incident neutron wave.) In analogy to the case of X-rays, these interference effects follow the usual Bragg law. For wavelengths larger than the Bragg cut-off wavelength (twice the largest lattice spacing), the coherent component of scattering vanishes leaving only the incoherent component.

Incoherent scattering (scattering in which the scattered wave does not interfere with the incident wave) makes up what is called "diffuse" scattering. This type of scattering does not contribute to interference effects. There are several reasons for incoherent or diffuse scattering:

- (1) There may be several isotopes of an element present in the crystal. The various isotopes can give rise to different scattering cross sections. The location of the extra isotopes in the crystal will be random and hence give rise to a random variation in cross section.
- (2) In nuclei with non-zero spin, another type of incoherent scattering is present. This is called "spin-dependent" incoherent scattering because it arises from variation of the cross section with the relative orientation of the neutron spin and the nuclear spin.
- (3) A third reason for incoherent scattering can be found in the magnetic interaction between neutrons and the atomic magnetic moments. The atomic moments are not aligned in the majority of crystals, and since the magnetic scattering is dependent on the relative orientation of neutron moment and atomic moments, a random variation in scattering power is present, and incoherent scattering results.
- (4) The coherent "crystal effects" are further decreased by another type of incoherent scattering resulting from temperature vibration of the atoms of the crystal. The magnitude of this reduction is determined by the temperature of the crystal, the wavelength of the neutrons, and the angle of scattering.

For wavelengths larger than the Bragg cut. off, the only scattering is incoherent. As the energy is increased, a large increase in cross section is observed (cf. Figs. 1.2.29 and 1.2.30) when the Bragg cut off wavelength is reached. Maxima in the cross section are observed as each new set of planes becomes active. At neutron energies above 0.1 ev, so many planes become active that the cross section varies smoothly with energy. When the neutron energy reaches several ev, the coherent scattering becomes small, but this is accompanied by a corresponding increase in the incoherent inelastic scattering so that the total scattering changes very little with energy. The inelastic scattering, where the lattice receives energy from the neutrons, increases with energy until the neutron energy is large compared to the chemical binding energy of the lattice. When this point is reached, the neutron is scattered as if the nuclei forming the lattice were free, and, barring nuclear resonances, the scattering cross section is constant with energy. This is called the free-atom cross section.

To summarize the process of a neutron losing energy in the crystal, several steps are considered. A fast neutron first slows down by dislocating effectively free nuclei until its energy decreases to the order of the energy of the crystal bond. At this point, it begins to make inelastic collisions with the lattice as a whole. It continues to lose energy in this manner until its wavelength exceeds the amplitude of the temperature vibrations of the nuclei of the crystal. At this stage, further cooling takes place very slowly because elastic collisions with the lattice become the most probable process. If in some manner the neutron loses still more energy, inelastic scattering becomes important again, but, in this case, the neutron absorbs energy from the lattice.

Figures 1.2.31 and 1.2.32 illustrate another effect that is most prominent in low A elements, namely, an increase in the scattering cross section for low-energy neutrons. This effect may have more than one cause. In the case of scattering by a gas, the thermal

motion of the molecules of the gas will cause neutrons to be "bumped" from their original direction and hence give rise to an increased scattering cross section. (This effect follows a 1/v law.) Superimposed on this is the so called chemical binding effect* owing to a changed reduced mass. This effect becomes important when the energy of the neutron is less than the energy of the chemical bond. In the case of a gas, this means that the mass of the neutron and molecule are used in calculating the reduced mass. In the crystalline case, it means that the mass of the neutron and crystal must be used in calculating the reduced mass (which is approximately the mass of the neutron).

If the molecule or crystal is composed of only one kind of atom, then the scattering cross section is increased over the free-atom cross section by the square of the ratio of the reduced mass of neutron and molecule (or crystal) to the reduced mass of neutron and one atom of the molecule (or crystal). Thus, for a crystal, this factor is $(A + 1)^2/A^2$. In the case of a diatomic molecule, it is $4(1 + A)^2/(1 + 2A)^2$.

 $(A + 1)^2/A^2$ times the free-atom cross section is known as the "bound-atom cross section."

The discussion above relates to the effect of crystalline structure and chemical binding on the total cross section. It is clear that the chemical binding will increase the transport cross section, because with the increase in effective mass, the scattering will become more isotropic in the laboratory frame. However, the details as to how chemical binding and crystal effects influence reactor behavior are not well known at this time.

INELASTIC SCATTERING

Inelastic scattering of a neutron leaves the target nucleus in one of its excited states. The energy of the emitted neutron is less than that of the incident neutron by this excitation energy.

DA TA

A summary of inelastic cross section data is presented in Table 1.2.15.

Recent measurements of the inelastic scattering of neutrons of about 1.85 mev energy on Fe show the existence of a level at 850 ± 50 kev above the ground state.⁴³ The measurements were made at 90° only. If the inelastic scattering is assumed isotropic, one is led to a cross section of 0.82 barns.

The distribution in energy of 4.3-mev neutrons inelastically scattered from tungsten is found to be practically constant in energy up to about 3.25 mev.⁴⁴ The inelastic cross section is estimated to be less than three fourths as large as the elastic cross section.

APPROXIMATE FORMULAS

When there are no data on inelastic scattering available, some crude guesses can be made provided that both the compound nucleus and the residual nucleus are sufficiently highly excited so that there are many levels lying below the level of excitation. This restricts the validity of the results to heavy nuclei. In this case, the theory predicts that the inelastically scattered neutrons are isotropically distributed.

Energy Distributions

Denote by E the energy of the incident neutron and by \overline{E} that of the inelastically scattered one. Let $D_R(x)$ be the distance between levels of the residual nucleus when excited

^{*}G. Placzek, Phys. Rev., 86, 377, 1952, discusses the scattering of neutrons by systems of heavy nuclei. G. Breit, Phys. Rev., 71, 215, 1947, and G. Breit and P. R. Zilsel, Phys. Rev., 71, 232, 1947, discuss the scattering of slow neutrons by bound protons.



an energy x above its ground state. Finally, denote by $\sigma_{c}(E)$, the cross section for forming the compound nucleus by a neutron of energy E. According to the statistical theory, the number of neutrons scattered from energy E to \overline{E} is proportional to:

$$\mathbf{f}(\mathbf{E}, \overline{\mathbf{E}}) = \overline{\mathbf{E}}\sigma_{\mathbf{c}}(\overline{\mathbf{E}}) \ \mathbf{D}_{\mathbf{R}}^{-1}(\mathbf{E} - \overline{\mathbf{E}}) \tag{53}$$

A plot of $\sigma_c(E)$ as computed from statistical theory is given in Fig. 1.2.18, to be used if no data are available. D_R^{-1} is expected to be relatively constant up to a certain energy E_0 (~3 mev) above the ground state and then to rise exponentially:

$$D_{\mathbf{p}}^{-1}(\mathbf{E}) = D_{\mathbf{0}}^{-1} \qquad \qquad \mathbf{E} \leq \mathbf{E}_{\mathbf{0}}$$
 (54)

$$D_{R}^{-1}(E) = D_{0}^{-1} e^{2(\sqrt{aE} - \sqrt{aE_{0}})} \qquad E \ge E_{0}$$
 (55)

The constants D_0 , E_0 , and a are to be adjusted from experiment. Lacking evidence for a, one can use Fig. 1.2.19 to estimate it for odd nuclei. (Cf. "Level Density Formula.")

For various limiting cases, simple expressions can be found for the dependence of f on \vec{E} . When the residual nucleus is left with excitation energy greater than E_0 , then:

$$f = \overline{E}\sigma_{\alpha}(\overline{E}) \exp \left\{ 2(\sqrt{a(E - \overline{E})} - \sqrt{a\overline{E_0}}) \right\} \qquad E - \overline{E} > E_0. \tag{56}$$

Figs. 1.2.33 to 1.2.36 show plots of Eq. (56) for Z = 30, 50, 70, and 90 when $E_0 = 0$; i.e., when the exponential formula is good down to the ground state.

If only low-energy emerging neutrons are considered, then:

$$f(\mathbf{E}, \overline{\mathbf{E}}) = \overline{\mathbf{E}} \sigma_{\mathbf{C}}(\overline{\mathbf{E}}) \exp \left\{ 2(\sqrt{a}\overline{\mathbf{E}} - \sqrt{a}\overline{\mathbf{E}}_{\mathbf{0}}) \right\} \exp \left\{ -\sqrt{\frac{a}{\overline{\mathbf{E}}}} \, \overline{\mathbf{E}} \right\} \qquad (\mathbf{E} - \overline{\mathbf{E}}) > \mathbf{E}_{\mathbf{0}} \qquad \overline{\mathbf{E}} << \mathbf{E} \qquad (57)$$

When $E - \overline{E} < E_0$, then Eq. (54) should be used for the level density and:

$$\mathbf{f} \propto \mathbf{E} \sigma_{\mathbf{c}}(\mathbf{E}) \qquad (\mathbf{E} - \mathbf{E}) < \mathbf{E}_{\mathbf{a}}$$
 (58)

When E is close to E_0 , one must take account of the change in level density below E_0 in Eq. (53). This results in a rise in f at the high-energy end of the neutron spectrum. Figure 1.2.37 shows a typical result with $E_0 = 3$ mev.

Equations (53) through (58) are, within the limits of the theory, good approximations to the emitted neutron distribution until E becomes large enough for the (n,2n) reaction to occur. This will add more low-energy neutrons to the spectrum.

Total Inelastic Cross Sections

The cross section σ_c for compound nucleus formation can be written as the sum:

$$\sigma_{c} = \sigma_{in} + \sigma_{ce} + \sigma_{f} + \sigma_{v}$$

of the inelastic, capture elastic,* fission, and radiative capture cross sections, from which it follows that:

$$\sigma_{in} = \frac{\sigma_{in}}{\sigma_{in} + \sigma_{ce}} \left(\sigma_{c} - \sigma_{f} - \sigma_{\gamma} \right) \tag{59}$$

^{*}Scattering in which a compound nucleus is formed, a neutron emitted, and the residual nucleus left in the same state as the target nucleus is called capture elastic scattering.

The statistical theory gives:

$$\frac{\sigma_{\text{in}}}{\sigma_{\text{in}} + \sigma_{\text{ce}}} = \frac{\int_{0}^{E-D_{\bullet}} \overline{E} \sigma_{c}(\overline{E}) D_{\mathbf{R}}^{-1} (E - \overline{E}) d\overline{E}}{\int_{0}^{E} \overline{E} \sigma_{c}(\overline{E}) D_{\mathbf{R}}^{-1} (E - \overline{E}) d\overline{E}}$$
(60)

which, together with Eq. (59) and Fig. 1.2.18 for $\sigma_{\rm C}$ directly determine $\sigma_{\rm in}$ in the case that the fission cross section is small (the radiative capture cross section is negligible in this case). For E \gg D₀, it follows that:

$$\frac{\sigma_{\rm in}}{\sigma_{\rm in} + \sigma_{\rm ce}} \approx 1 \tag{61}$$

and thus that:

$$\sigma_{\rm in}(E) \approx \sigma_{\rm c}(E)$$
 (61a)

which agrees well with 14-mev data in the absence of fission.

Deviations from Eq. (60) occur when the residual nucleus is left with excitation less than E_a . Then:

$$\frac{\sigma_{\text{in}}}{\sigma_{\text{in}} + \sigma_{\text{ce}}} = \frac{\int_0^{E-D_0} \overline{E} \ \sigma_{\text{c}}(\overline{E}) \ d\overline{E}}{\int_0^E E' \sigma_{\text{c}}(E') \ dE'} = \frac{g(x')}{g(x)}$$
(62)

where x is the value of R/x for neutron energy E and x' the value for energy E - D₆:

$$\frac{R}{\lambda(E)} = 0.222 \sqrt{E(mev)} R \times 10^{13}$$

The function g(x) is plotted in Fig. 1.2.38 for several values of $X_0 = 10^{13}$ R.

Equation (62) is a very rough approximation which neglects fluctuations due to spin differences and variations in level spacings.

In the case of light nuclei or "magic" nuclei where only a few levels are involved in the scattering process, the results depend strongly upon the spins and parities of the levels. A detailed treatment of this case and the statistical theory case is contained in Report NYO-636 and in a paper by Feshbach and Hauser. 46

(n,2n) REACTIONS

When the energy of the incident neutron exceeds the binding energy of the last neutron in the target nucleus, the (n,2n) reaction becomes energetically possible. Few measurements of (n,2n) cross sections have been made. The energy dependence has been obtained for the (n,2n) reaction in Cu⁶³ by Fowler and Slye⁴⁶ and in Cu⁶³, Ni⁵⁶, and Tl²⁶³ by Martin and Diven.⁴⁷ Cross sections at 14 mev have also been measured for a few elements by Forbes,⁴⁸ whose results are included in Table 1.2.16.

The Be (n,2n) reaction is of particular interest because the threshold of 1.7 mev is the lowest known. Many measurements of this cross section have been made, usually with (α,n) sources, but the results have not been particularly informative.

A compilation by A. H. Snell and published by Agnew⁵⁰ shows values ranging from 0.04 to 4.0 barns. The latter measurement is hardly credible, but the situation is nuclear at present.

Cohen⁵¹ has measured a large number of (n,2n) cross sections averaged over a broad spectrum of high-energy neutrons produced by the (d,n) reaction.

Most other measurements of (n,2n) cross sections have been at energies of 20 mev or more.

If one assumes that after the first neutron is inelastically scattered, competition to neutron emission from other processes is small, then every inelastic scattering that leaves the nucleus sufficiently excited will lead to the emission of a second neutron.

If we denote the threshold energy by E_b , then within the limits of the statistical theory* the (n,2n) cross section is given by:

$$\sigma(\mathbf{n}, 2\mathbf{n})_{\mathbf{E}} = \sigma_{\mathbf{i}\mathbf{n}}(\mathbf{E}) \frac{\int_{0}^{\mathbf{E}-\mathbf{E}_{b}} \mathbf{E} \sigma_{\mathbf{c}}(\mathbf{E}) \ D_{\mathbf{R}}^{-1} \ (\mathbf{E} - \mathbf{E}) \ d\mathbf{E}}{\int_{0}^{\mathbf{E}} \mathbf{E}' \sigma_{\mathbf{c}}(\mathbf{E}') \ D_{\mathbf{R}}^{-1} \ (\mathbf{E} - \mathbf{E}') \ d\mathbf{E}'}$$
(63)

This can be simplified in several limiting cases. For $E - E_b > \sqrt{E/a}$:

$$\sigma(n,2n)_{E} = \sigma_{in}(E) \left\{ 1 - (1+\gamma)e^{-\gamma} \right\}$$
 (64)

For E - E_h < $\sqrt{E/a}$:

$$\sigma(\mathbf{n}, 2\mathbf{n})_{\mathbf{E}} = \sigma_{\mathbf{in}}(\mathbf{E}) \frac{\sigma_{\mathbf{c}}(\mathbf{E} - \mathbf{E}_{\mathbf{b}})}{\sigma_{\mathbf{c}}(\sqrt{\mathbf{E}/2})} \left\{ 1 - (1 + \gamma)e^{-\gamma} \right\}$$
(65)

$$\rightarrow \sigma_{in}(E) \frac{\sigma_{c}(E - E_{b})}{\sigma_{c}(\sqrt{E/a})} \frac{a}{2E} (E - E_{b})^{2}$$
(66)

when:

$$E - E_h \ll \sqrt{E/a}$$

These formulae are not valid in the limit $E = E_b$. They agree with Eq. (63) to within 10 percent, however, as soon as k'R is of the order of 1 or greater. Here k' is the wave number of a neutron of energy $E - E_b(k' = 0.22 \sqrt{E - E_b} \times 10^{13} \text{ cm}^{-1}$, E in mev) and R is the nuclear radius.

REACTION PROCESSES

Reaction processes are those in which neutrons that are absorbed are not re-emitted. Examples discussed below are the (n,γ) , (n,α) and (n,p) processes. The (n,α) and (n,p) processes are all restricted to light nuclei at the neutron energies considered here because of the coulomb barrier and threshold effects. Thermal values of the reaction cross sections appear in Tables 1.2.17.

RADIATIVE CAPTURE (n, y)

The general behavior of (n,γ) cross sections was discussed in some detail under "Collision Reactions." When the energy levels are far apart, the Breit-Wigner single-level formula should give a good fit to the cross section at energies near the resonance energy.

Figure 1.2.39 shows the cross section near a resonance in Cd. Parameters for a Breit-Wigner fit (the resonance energy, level width, and the maximum value of the cross section) are shown on the figure. Figures 1.2.40 and 1.2.41 show two other (n,γ) resonance cross sections. Most (n,γ) cross sections obey the 1/v law far from resonances in the thermal region.

^{*}Cf. preceding discussion of "Approximate Formulas."

1

١

1. 7. 3. 2.

Radiative capture cross sections have been measured by Hughes et al, 36 using reactor neutrons with an effective energy of 1 mev. The cross sections are plotted vs number of neutrons in Fig. 1.2.16. Hughes notes that the energy dependence of the (n,γ) cross section in this neighborhood is approximately 1/E. The abnormally low cross sections of some of the nuclei shown are evidence of their "magic" character.

(n,a) AND (n,p) REACTIONS

Because both the coulomb effect and threshold values for charged particle emission increase with A, these reactions are generally limited to light nuclei for neutron energies of interest in reactors. Some of these cross sections in light elements can be quite large at thermal energies. Figures 1.2.42 to 1.2.44 show the data for the (n,α) reaction in Li, B, and Be.

The (n,p) cross sections of oxygen are of interest because of the activity of the product nuclei. Table 1.2.18 gives the threshold energy and the value of the cross section averaged over the fission spectrum in the case of O^{16} , and over energies much higher than the threshold in the case of O^{17} .

Table 1.2.1 - Nomenclature

A Z	Atomic mass number Nuclear charge number	θ	Angle of deflection in the laboratory system
M R	Mass of neutral atom Nuclear radius	θ•	Angle of deflection in the center of mass system
I T	Nuclear spin Mean-life of radioactive nucleus	$\frac{\sigma_{tt}}{\cos \theta}$	Transport cross section Average value of $\cos \theta$
T ₁ ,	Half-life of radioactive nucleus 1/T	σ _c (E)	Cross section for the formation of the compound nucleus by
α	Ratio of capture cross section to fission cross section. Also,		neutrons of energy E. Also called reaction cross section
	minimum ratio of final to ini- tial energies in an elastic scattering process	$\mathbf{X_0}$ $\mathbf{f}(\mathbf{E}, \overline{\mathbf{E}})$	10 ¹³ R(cm) Proportional to number of neutrons inelastically scattered
$\sigma_{\mathbf{e}}$ $\sigma_{\mathbf{e}}(\theta)$	Elastic scattering cross section Differential σ_e	Ę	from energy E to energy \overline{E} Average loss in logarithm of energy
$\sigma_{ ext{in}}$	Inelastic scattering cross section $\sigma_e + \sigma_{in}$	γ	$\sqrt{\frac{a}{E}} (E - E_b)$

Table 1.2.2 - Nuclear Radii

R × 10¹³, cm

	R × I)~, cm	
	Low energy	High energy	
Isotope	(kev)	(14-25 mev)	Reference
-	` '	•	
He ⁴	2.5	•••	(2)
Li [†]	2.7	• • •	(2)
Be ⁹	4.7-5.0	3.8	(2)
B ¹¹	3.5	3. 4	(2)
C12	4.5	3.8	(2)
O16	5.5	4.3	(2)
F ¹⁹	5.35	•••	(2)
Na ²³	5.65	•••	(2)
Mg ²⁴	4.75	4.5	(2)
Al ²⁷	5.5	4.6	(2)
Si ²⁸	4.8	•••	(2)
P ³¹	5.15	•••	(2)
S ³²	4.2	4.1	(2)
Cl	•••	4.7	(1)
K39	3.31	•••	(2)
Ca ⁴⁴	3.5	•••	(2)
Ti	4.75	5.0	(2)
V ⁶¹	6.5	5.3	(2)
Mn ⁵⁵	5.2	•••	(2)
Fe ⁶⁶	4.0	5.6	(2)
Co ⁵⁹	5.2	•••	(2)
Ni	4.7	•••	(2)
Cu	5.25	5.5	(2)
2n	5.55	5 .9	(2)
S e	•••	6.3	(1)
Zr	7.25	5.2	(2)
Ag	7.7	6.8-6.9	(2)
Cd	•••	7.2	(1)
In ¹¹⁵	7.3	•••	(2)
Sn.	7.5	7.4	(2)
Sb 121.123	7.5	7.3	(2)
I ¹²⁷	7.3	•••	(2)
Ta ¹⁸¹	7.9-8.0	•••	(2)
₩	7.7	•••	(2)
Au	•••	7.5	(1)
Hg Pb ²⁶⁶		8.3-8.4	(1)
Pb ²⁰⁰	7.5	7.8	(2)
Po***	7.5 – 7.6	7.8	(2)
	6.7		(2)
Bi	•••	7.9	(1)
Th U	8.7	8.5	(3)
U	•••	0.0	

Table 1.2.3 — Isotopic Weights, Binding Energy of an Additional Neutron, and Packing Fraction

[The first five columns of the following table are taken from K. T. Bainbridge, Part V of Experimental Nuclear Physics, Volume I, edited by E. Segrè,

John Wiley & Sons, Inc., New York (in press).]

				Error in		
Atomic		Mass	Isotopic weight	isotopic	Binding energy	Packing
number		number	relative	weight	of additional	fraction
(Z)	Symbol	(A)*	to O ¹⁶ †	× 10 ⁶ ‡	neutron, mev\$	× 10 ³ ¶
0	n	1	1.008982	3		8.982
1	H	$\frac{1}{2}$	1.008142	3	2.224	8.142
		<u>2</u>	2.014735	6	6.256	7.367
		3	3.016997	11		5.665
2	He	3 4 5	3.01697 7	11	20.56	5.659
		<u>4</u>	4.003873	15	-0.6601	0.968
			5.01356 4	215	1.929	2.713
		6	6.020474	27		3.412
3	Li	5				
		<u>6</u>	6.017021	22	7.243	2.837
		$\frac{6}{7}$	7.018223	26	2.036	2.603
		8	8.025018	30		3.127
4	Be	6				
		7	7.019150	26	18.88	2.736
		8	8.007850	29	1.666	0.981
		19	9.015043	30	6.809	1.671
		10 11	10.016711	28		1.671
5	В	9	9.016190	31	8. 433	1.799
		<u>10</u>	10.01611 4	28	11 .4 6	1.611
		<u>11</u>	11.012789	23	3.360	1.163
		12	12.018162	22		1.514
		13				
6	C	10	10.020605	300	13.66	2.060
		11	11.014916	24	18.71	1.356
		<u>12</u>	12.00380 4	17	4.946	0.317
		<u>13</u>	13.007473	14	8.1 6 8	.575
		14	14.007682	11		.5 49
		15				
7	N	12	10 000000	• •		
		13	13.009858	14	10.54	0.758
		14	14.007515	11 12	10.83 2.891	.537
		$\frac{15}{16}$	15.004863 16.010740	500	2.891 5.295	.324
		17	17.014035	500 500	5.295	.671 .826
		18	17.014035	500		.020
8	0	14	(14.013016)		13.25	0.930
0	J	15	15.007768	13	15.59	.518
		16	16.000000	Standard	4.142	.000
		17	17.004533	7	8.0 4 5	.267
		18	18.004874	17	4.072	.271
		19	19.009482	850	-,-,-	.499

Table 1.2.3 — (Continued)

Atomic		Mass	Isotopic weight	Error in isotopic	Binding energy	Packing
number		number	relative	weight	of additional	fraction
(Z)	Symbol	(A)*	to O ¹⁶ †	× 10 ⁶ ‡	neutron, mev§	× 10 ³ ¶
9	F	16				
		17	17.007486	11	9.122	0.440
		18	18.006670	18	10.42	.370
		19	19.004456	15	6.597	.234
		20	20.006352	19		.318
		21				
10	Ne	18	10 005015	50	10.50	0.410
		19	19.007915	53	16.79	0.416
		$\frac{20}{21}$	19.998860	23	6.753	0570
		21	21.000589	21 60	10.52 5.188	.0280 0786
		$\frac{\overline{22}}{\overline{23}}$	21.998270 23.001680	60	5.166	.0730
	NT-		23.001000	60		.0730
11	Na.	21	00.001001		10.00	0.0000
		22	22.001321	60	12.26	0.0600
		$\frac{23}{24}$	22.997139 23.998651	26 28	6.955 9.165	124 0562
		2 5 25	24.997789	26 115	5.105	088 4
			24.551105	110		0004
12	Mg	22 23	23.001113	. 325	16.20	0.0484
		24 24	23.992696	30	7.320	304
		2 4 25	24.993815	33	11.10	247
		26	25.990871	36	6.430	351
		20 27	26.9929 4 6	36	0.450	261
			20.552540	30		-,201
13	Al	25	05 000104	430	14.01	0.146
		26 27	25.996194 26.990140	430 33	7.720	-0.146 365
		2 <u>1</u> 28	27.990830	36	9.371	328
		29	28.989747	273	3.371	354
		30	20.303141	213		004
14	Si	27	26.995254	39	17.129	-0.176
		28	27.985837	37	8.472	506
		29	28.985719	45	10.60	492
		29 30 31	29.983313	38	6.596	556
		31	30.985210	41		477
		32				
15	P	29	28.989618	88	9.710	-0.358
		30	29.9 88170	107	12.60	394
		31	30.9 83622	38	7.926	528
		32	31.984091	36		497
		33 3 4				
16	۰		20 000005	110	14 51	-0 359
10	S	31 32	30.988865	110 35	14.51 8.645	-0 359 5 54
		32	31.982265 32.981961	35 38	11.33	547
		34	33.978773	36 44	6.890	624
		32 33 34 35	34.980354	50	0.000	561
		36	02,00007			
		37				

Table 1.2.3 — (Continued)

Atomic number (Z)	Symbol Cl	Mass number (A)*	Isotopic weight relative to O ¹⁶ †	Error in isotopic weight × 10 ⁶ ‡	Binding energy of additional neutron, mev§	Packing fraction × 10 ³ ¶
		35	34.980175	50	8.559	-0.566
		36	35.97996 4	58	10.54	557
		<u>37</u>	36.977624	7 7	6.109	605
		38 39	37.980044	84		525
18	A	35				
		36	35.978930	58	8.764	-0.585
		37	36.978499 37.974878	77 85	11.73	581 661
		38 39	31.914010	69		001
		40	39.975100	100	6.064	-0.622
		41	40.977569	100		547
19	K	37				
		38	37.981125	240	13.20	-0.497
		39	38.97593	130	7.759	617
		40	39.976578	130	9.984	586
		$\frac{\overline{41}}{42}$	40.974836	150	7.389	614
			41.975881	150		574
		43				
20	Ca	39	38.983515	420	15.90	-0.423
		40	39.975420	130	8.469	614
		41	40.975305	160	11.41	602
		$\frac{42}{43}$	41.972036	165 100	8.051 11.31	666 642
		43	42.97237 43.96920	100	11.31	700
		45	40.00020	100		
		46				
		47				
		$\frac{48}{49}$	47.96763	120		-0.674
21	Sc	41				
		42				
		43				
		44 45	44.97000	60		-0.667
		45 46	44.97000	60		-0.007
		47 4 8	47.96787	100	11.70	-0.669
		49	48.96428	190 200	11.70	-0.669 729
22	Ti	45	10.00120	200		123
		<u>46</u>				
		47	46.96700	1000	11.11	-0.702
		48	47.96405	190		749
		49				
		46 47 48 49 50 51				

Table 1.2.3 — (Continued)

Atomic number (Z)	Symbol	Mass number (A)*	Isotopic weight relative to O ¹⁶ †	Error in isotopic weight × 10 ⁶ ‡	Binding energy of additional neutron, mev§	Packing fraction × 10 ³ ¶
23	v	47 48 49	47.9 68 4 0	190		-0.658
		50	49.96215	500	10.80	-0.757
		51	50.95953	150	7.273	794
		52	51.96070	150		756
24	Cr	49	48.96540	220	13.40	-0.706
		50	49.95999	90		800
		51				
		52 53 54 55	51.95693	150		-0.828
25	Mn	56 51				
	 -	52 53	51.96202	150		-0.730
		5 4	53.95756	245	10.15	-0.786
		<u>55</u> 56	54.95564	140	7.254	807
			55.95 683	140		771
26	Fe	53	52.962 38	300	13.80	-0.710
		<u>54</u>	53.95654	230	8.828	805
		55 56	54.95604	140	11.32 7.627	799 842
		<u>56</u> <u>57</u> <u>58</u>	55.95286 5 6.9 5365	140 140	1.021	813
		59	(58.95350)	170		-0.788
27	Co	55	54.95974	140	10.16	-0.732
		56 57 58	55.95781	140		753
		<u>59</u>	58.95182	140	7.729	-0.817
		60 61 62	59.95250	140		792
28	NT	£7	E.C. 05710	200	11.70	0.751
28	Ni	57 <u>5</u> 8	56.95719 57.95360	300 200	11.70 9.01 4	-0.751 800
		<u>59</u>	58.95290	200	11.55	798
		<u>60</u>	59.94948	140	8.548	842
		61 62	(60.94928)	(150)		831
		63 64 65 66	63.94733	400		-0.823
	_					
29	Cu	58				
		59 60				

' ŀ

Table 1.2.3 — (Continued)

Atomic number (Z)	Symbol	Mass number (A)* 61 62	Isotopic weight relative to O ¹⁶ † 60.95168	Error in isotopic weight × 10 ⁶ ‡	Binding energy of additional neutron, mev§	Packing fraction × 10 ³ ¶ -0.792
		63 64 65 66 67	62.94862 63.94913 64.94749	200 400 210	7.887 9.889	-0.816 795 808
30	Zn	63 64 65 66 67 68 69 70 71	(63.94880)	400		-0.800
31	Ga	64 65 66 67 68 69 70 71 72 73				
32	Ge	66 67 68 69 70 71 72 73 74 75 76 77				
33	As	71 72 73 74 75 76 77				

Table 1.2.3 — (Continued)

Atomic number (Z)	Symbol	Mass number (A)*	Isotopic weight relative to O ¹⁶ †	Error in isotopic weight × 10 ⁶ ‡	Binding energy of additional neutron, mev§	Packing fraction × 10 ³ ¶
34	Se	71 72 73 74 75 76 77 78 79 80 81 82 83 84				
35	Br	75 76 77 78 79 80 81 82 83 84 85 86 87 88				
36	Kr	77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94				
37	Rb	81 82 83				

Table 1.2.3 — (Continued)

Atomic number (Z)	Symbol	Mass number (A)*	Isotopic weight relative to O ¹⁶ †	Error in isotopic weight × 10 ⁶ ‡	Binding energy of additional neutron, mev§	Packing fraction × 10 ³ ¶
		85 86 87 88 89 90 91 92	84.93100 85.93736 86.9295	1500 1000 2000	2.441 (15.680)	-0.812 728 810
38	Sr	94 95 84 85 86	85.935 4	1000	8.5 4 8	-0.751
		87 88 89 90 91 92 93 94 95	86.9352 87.93360 88.93398	1000 360 420	9.852 8.008	745 755 742
39	Y	86 87 88 89 90 91 92 93 94 95	87.93758 88.93712	360 420	8.791	-0.709 707
40	Zr -	89 90 91 92 93 94 95 96 97				
41	Nb(Cb)	90 91 92 <u>93</u> 94 95				

Table 1.2.3 — (Continued)

Atomic number (Z)	Symbol	Mass number (A)*	Isotopic weight relative to O ¹⁶ †	Error in isotopic weight × 10 ⁶ ‡	Binding energy of additional neutron, mev\$	Packing fraction × 10 ³ ¶
		96 97 98				
42	Мо	9 <u>2</u> 93				
		94 95 96 97	93.93522	1500		-0.689
		96	95.93 558	320	7.105	-0.671
		97 98 99	96.93693	440		650
		100 101	99.93829	330		-0.617
		102				
43	Tc	92				
		93				
		94 95				
		96				
		97				
		98				
		99				
		100 101				
		102				
44	Ru	95				
		<u>96</u>				
		97				
		9 <u>8</u> 99				
		100				
		101				
		<u>102</u>				
		103				
		104 105				
		106				
		107				
45	Rh	102				
		103				
		10 4 105				
		105 10 6				
		107				
46	Pd	100				
		101				
		102				
		103 104				
		104				

7

Table 1.2.3 — (Continued)

				Error in		
Atomic number	Comple al	Mass number (A)*	Isotopic weight relative to O ¹⁶ †	isotopic weight × 10 ⁶ ‡	Binding energy of additional neutron, mev§	Packing fraction × 10 ³ ¶
(Z)	Symbol	(A)+	10 O-4	× 10.1	neutron, mevs	x 10.1
		105				
		106				
		107				
		108	107.93690	500		-0.584
		169				
		110	109.94 098	620		-0.537
		111				
		112				
47	Ag	102				
		103				
		104				
		105				
		10 6 107				
		108				
		109				
		110	109.94218	440		-0.526
		111				
		112				
		113				
48	Cd	106				
		107				
		108				
		109				
		110	109.93911	440		-0.554
		$\frac{111}{112}$	111.93999	360	6.435	0.598
		112	112.94206	390	10.16	-0.5 36 51 3
		114	113.94013	440	5.104	525
		115	114.94363	670	9.768	490
		116	115.94212	46 0		499
		117				
		118				
49	I n	109				
		110				
		111				
		112				
		113		4		
		114	113.94329	440	9.498	-0.497
		115 116	114.94207 115.94398	670 700	6.584	50 4 483
		117	113.54350	100		403
50	a _					
50	Sn	111				
		$\frac{112}{113}$				
		113 114	113.94109	440	7 .94 3	-0.517
		115	114.94154	670	11.60	508
		116	115.93806	420	4.964	534
		117	116.94171	500		498

Table 1.2.3 — (Continued)

Atomic number (Z)	Symbol	Mass number (A)*	Isotopic weight relative to O ¹⁶ †	Error in isotopic weight × 10 ⁶ ‡	Binding energy of additional neutron, mev§	Packing fraction × 10 ³ ¶
		118 119 120 121	119.93904	460		-0.508
		122 123	121.94260	1260		-0.470
		$\frac{124}{125}$				
		126				
		127				
		128				
51	Sb	117				
		118				
		119				
		120				
		121				
		122				
		123				
		124				
		125 126				
		126				
		128				
		129				
		130				
		131				
		132				
		133				
		134				
		135				
		136				
52	Te	118				
		119				
		120				
		121				
		122				
		123				
		124 125				
		<u>125</u>				
		126 127	125.9427	1000		-0. 4 55
		127 128 129	127.9471	1000		-0.413
		130	129.9467	900		-0.410
		131	120.0101			~1210
		132				
		133				
		134				
		135				
		136				
		137				

7.

i

Table 1.2.3 — (Continued)

Atomic number (Z)	Symbol	Mass number (A)*	Isotopic weight relative to O ¹⁶ †	Error in isotopic weight × 10 ⁶ ‡	Binding energy of additional neutron, mev§	Packing fraction × 10 ³ ¶
53	I	124 125 126				
		127 128	126.946	1000		-0.425
		129				
		130				
		131				
		132				
		133				
		13 4 135				
		136				
		137				
54	Хe	124				
		125 126				
		127				
		$\frac{128}{129}$	128.94533	300		-0.424
		130				
		131				
		132 133	131.94729	1000		-0.399
		134 135				
		136				
		137 138				
		139				
		140				
		141				
		142				
		143				
		144				
55	Cs	145 130				
		131				
		132				
		133				
		134 135				
		135 136				
		137				
		138				
		13 9				
		140				
		141				
		142 143				
		143				

Table 1.2.3 — (Continued)

Atomic number (Z)	Symbol	Mass number (A)*	Isotopic weight relative to O ¹⁶ †	Error in isotopic weight × 10 ⁶ ‡	Binding energy of additional	Packing fraction × 10 ³ ¶
(4)	Symbol	(A)*	w 0°4	x 10.1	neutron, mev§	X 10-1
56	Ba	130				
		131				
		132 133				
		134 134				
		135				
		136 137				
		137				
		138 139				
		140				
		141				
		142				
		143				
		144				
		145				
57	La	137				
		138 139				
		140				
		141				
		142				
		143				
		144 145				
Eo	_					
58	Ce	135				
		136 137				
		138				
		139				
		140 141				
			140.95335	1100		-0.331
		142 143				
		146				
		147				
59	Pr	140				
		<u>141</u>				
		142				
		143				
		1 44 1 45				
		146				
		147				
60	Nd	141				
		143				
		144	143.95607	750		-0.305
		142 143 144 145 146				
		146				

*E*33

. F

i Ŀ

Table 1.2.3 — (Continued)

Atomic number (Z)	Symbol	Mass number (A)*	Isotopic weight relative to O ¹⁶ †	Error in isotopic weight × 10 ⁶ ‡	Binding energy of additional neutron, mev§	Packing fraction × 10 ³ ¶
		147 148 149 150 151	148.96775 149.96878	800 780	7.403	-0.216 208
61	Pm	143 144 145 146 147 148 149				
62	Sm	144 145 146 147 148 149 150 151 152 153				
63	Eu	147 149 150 151 152 153 154 155 156 157				
64	Gd	152 153 154 155 156 157 158 159 160				
65	Тъ	152 153 154 155				

Table 1.2.3 — (Continued)

Atomic		Mass	Isotopic weight	Error in isotopic	Binding energy	Packing
number		number	relative	weight	of additional	fraction
(Z)	Symbol	(A)*	to O ¹⁶ †	× 10 ⁶ ‡	neutron, mev§	× 10 ³ ¶
		159				
		160				
		161				
66	Dy	156				
	-3	158				
		159				
		160				
		161				
		162				
		163				
		<u>164</u>				
		165				
67	Ho	160				
		161				
		162				
		163				
		164				
		165				
		16 6				
68	Er	162				
		163				
		164				
		165				
		166				
		167 168				
		169				
		170				
		$\frac{170}{171}$				
69	Tm					
	4111	166				
		167 168				
		169				
		170				
70	Yb					
	10	168				
		169 170				
		170 171				
		172				
		173				
		174				
		175				
		176				
		177				
71	Lu	170				
		171				
		172				
		<u>175</u>				

3.£.Z.?

Table 1.2.3 — (Continued)

Atomic number (Z)	Symbol	Mass number (A)*	Isotopic weight relative to O ¹⁶ †	Error in isotopic weight 10 ⁶ ‡	Binding energy of additional neutron, mev§	Packing fraction × 10 ³ ¶
		$\frac{176}{177}$				
72	Hf	174 175 176	175.9923 4	1000		-0.0435
		$\frac{\overline{177}}{\overline{178}}$	1 77.9 9381	1230		-0.0348
		$\frac{179}{180}$	180.00440	2000		+0.0244
73	Ta	176 177 178 180 <u>181</u> 182				
74	w	179 180 181				
		182 183 184 185 186 187	182.0038 183.00321 184.0060	2100 580 2100	8.912 5.765	0.0209 .0175 .0326
75	Re	183 184 <u>185</u> 186 <u>187</u> 188				
76	Os	184 185 186 187 188 189 190 191 192				
77	Ir	190 <u>191</u> 192 <u>193</u> 194	194.02637	1000		0.136
78	Pt	190 191 192				

Table 1.2.3 — (Continued)

Atomic number (Z)	Symbol	Mass number (A)*	Isotopic weight relative to O ¹⁶ †	Error in isotopic weight × 10 ⁶ ‡	Binding energy of additional neutron, mev\$	Packing fraction × 10 ³ ¶
		193 194 195 196 197 198 199	194.02403 195.02642 196.02744	1000 800 600	6.137 7.413	0.124 .135 .140
79	Au	191 192 193 194 195 196 197 198 199 200				
80	Hg	196 197 198 195 200 201 202 203 204 205	203.03550 205.03980	** ** **		0.175 0.194
81	AcC'' ThC'' RaC''	203 198 199 200 201 202 203 204 205 206 207 208 209 210	203.03499 204.03697 205.03792 206.04021 207.04189 208.04676 209.05044 210.05537	** ** ** ** ** ** ** ** ** **	6.519 7.478 6.230 6.798 3.828 4.936 3.772	0.172 .181 .185 .195 .202 .225 .241
82	Pb	199 200 201 202 203 204 205 206 207	204.03612 205.03831 206.03859 207.04034	** ** ** **	6.323 8.102 6.733 7.375	0.177 .187 .187 .195

Table 1.2.3 — (Continued)

Atomic number (Z)	Symbol	Mass number (A)*	Isotopic weight relative to O ¹⁶ †	Error in isotopic weight × 10 ⁶ ‡	Binding energy of additional neutron, mev#	Packing fraction × 10 ³ ¶
	·			•		
		208	208.04140	#	3.866	0.199
	D.D	209	209.04623	≠	5.243	.221
	RaD AcB	210 211	210.04958	#	3.782	.236
	ThB	211	211.05450	* *	5.188	.258 .273
	IIID	212	212.057 9 1 (213.06268)	•	3.921 4.964	.213 .294
	RaB	214	214.06633	*	4.504	.310
83	Bi	197				
		198				
		199				
		200				
		204				
		206				
		207	(207.04285)		6.817	0.207
		208	208.04451	#	7.441	.214
		209	209.04550	≠	4.629	.218
	RaE	210	210.04951	#	5.113	.236
	AcC	211	211.05300	#	4.378	.251
	ThC	212	212.05728	*	5.160	.270
		213	213.06072	#	4.136	.285
	RaC	214	214.06526	#		.305
84	Po	203				
		205				
		206				
		207	000 04550			
		208 209	208.04558		6.575	0.219
		210	209.04750	≠ ≠	7.655	.227 .230
	AcC'	211	210.04826 211.05234	<u>*</u>	4.56 4 6.007	.248
	ThC'	212	212.05487	*	4.312	.259
	Inc	213	213.05922	*	5.914	.278
	RaC'	214	214.06185	, , ,	4.098	.289
	AcA	215	215.06643	7 4	5.793	.309
	ThA	216	216.06919	#	4.312	.320
		217	(217.07354)	84	5.364	.339
	RaA	218	218.07676	#		.352
85	At	207				
		208				
		210				
		211	(211.05317)	*	5.029	0.252
		212	(212.05675)	*	6.035	.26 8
		213	(213.05 92 5)	7 4	4.880	.278
		214	214.06299	#	5.914	.294
		215	215.06562	*	4.592	.305
		216	216.06967	*	5.960	.323
		217	217.07225	*	4.517	.333
		218	218.07638	*		.350
86	Em	212	212.05621	*		0.265
		215	215.06562		6.612	.305
		216	216.06750	*	4.592	.312

Table 1.2.3 — (Continued)

Atomic number (Z)	Symbol	Mass number (A)*	Isotopic weight relative to O ¹⁶ †	Error in isotopic weight × 10 ⁸ ‡	Binding energy of additional neutron, mev§	Packing fraction × 10 ³ ¶
		217	217.07155	#	6.537	0.330
		218	218.07351	*	4.405	.337
	An	219	219.07776	*	6.342	.355
	Tn	220	220.07993	*	4.713	.363
		221	(221.08385)		5.77 4	.379
	Rn	22 2	222.08663	#		.390
87	Fr	217	(217.07221)	7 4	5.355	0.333
		218	218.075 44	p#	6.472	.346
		219	219.07747	#	5 .206	.354
		220	220.08086	#	6.361	.368
		221	221.08301	*	4.890	.376
		222	(222.08674)	#	12.80	.391
		223	(223.081 97)	*	-2.074	.368
		224	(224.09318)	*		.4160
88	Ra	219	219.07824	*	7.189	0.357
		220	220.0795 0	*	5.327	.361
		221	221.08276	;	6.742	.374
		222	222.08450	*	5.215	.381
	AcX	223	223.08788	*	6.379	.394
	ThX	224	224.09001	==	5.169	.4 02
		225	225.0 9344	*	6.221	.415
	Ra	226	226.0957 4	*	4.564	.424
		227	227.09982	≠	6.221	.440
	MsTh ₁	228	228.10212	#		.448
89	Ac	221				
		222	222.08692	*	6.798	0.392
		223	223.08860	*	5.690	.397
		224	224.09147	*	6.733	.408
		225	225.09322	*	5.299	.414
		226	226.09651	#	6.556	.427
	Ac	227	227.09845	#	5.001	.434
	MsTh ₂	228	228.10206	*		.448
90	Th	223	223.09036	*	7.617	0.405
		224	224.09116	*	5.895	.407
		225	225.09381	#	7.022	.417
		2 26	226.09525	=	5. 467	.421
	RdAc	227	227.09836	=	7.012	.433
	RdTh	228	228.09981	=	5.588	.438
		229	229.10279	*	6.565	.449
		230	230.10472	=	5.149	.455
	UY	231	231.10817	=	6.342	.468
	Th	232	232.11034	#	5.122	.476
	****	233	233.11382	#	5.867	.488
	UX ₁	234	234.11650	#	4.759	.498
		235	235.12037	*		.512
91	Pa	226	226.09823	*	7.152	0.435
		227	227.09953	#	6.063	.438
		228	228.10200	#	7.143	.447
		229	229.10331	#	5.867	.451

Table 1.2.3 — (Continued)

Atomic		Mogg	Isotopic weight	Error in	Dinding on organ	Dooking
number		Mass number	relative	isotopic weight	Binding energy of additional	Packing fraction
	Symbol	number (A)*	to O ¹⁶ †	weight × 10 ⁶ ‡		× 10 ³ ¶
(Z)	Symbol	(A)+	10 O-7	x 10.1	neutron, mev§	x 10-1
		230	230.10599	*	6.649	0.461
		231	231.10783	≠	5.4 58	.467
		232	232.11095	*	6.919	.478
		233	233.11250	*	5.23 4	.483
		234	234.11586	*	5.867	.495
		235	235.11854	*		.50 4
92	U	227	227.10166	≠	7.748	0.448
		228	228.10232	*	6.156	.44 9
		229	229.10 469	*	7. 580	.457
		230	230.10553	*	5.895	. 4 59
		231	231.10818	#	7.161	.4 68
		232	2 32.109 4 7	#	6.072	.472
		233	2 33.11193	p#	6.631	.4 80
	UII	234	234.11379	*	5.342	.4 8 6
		235	235.11704	7	6.426	.49 8
		236	236.11912		5.392	.505
		237	237.12231	#	5.923	.516
	UI	238	238.12493	≠	4.862	.525
		239	239.12869	#		.538
93	Np	231	231.11026	*	6.407	0.477
		232	(232.11236)	p#	7.562	.484
		233	233.1132 2	#	6.072	.486
		234	(23 4 .115 6 8)	*	6.919	.494
		235	235.11723	*	5.625	.499
		236	236.12017		7.050	.509
		237	237.12158	*	5.048	.513
		238	238.12514	#	6.351	.526
		239	239.12730	≠	5.830	.533
		240	240.13002	≠	6.053	.542
		241	241.13250	#		.550
94	Pu	232	232.11338	;	6.342	0.489
		233	(233.11555)	≠	7.794	.496
		234	234.11616	*	6.240	.496
		235	235.11844	≠	7.264	.504
		236	236.11962	≠	6.221	.507
		237	(237.12192)	#	6.724	.514
		238	238.12368	*	5.709	.520
		239	239.12653	#	6.416	.529
		240	240.12862		5.644	.536
		241	241.13154	≠	5.951	.546
		242	242.13413	≠	5.318	.554
•-		243	243.13740	#		.565
95	Am	239	239.12740	≠	5.728	0.533
		240	(240.13023)	#	7.171	.543
		241	241.13151	#	5.215	.546
		242	242.13489	≠	6.528	.557
		243	243.13686	#		.563
96	Cm	238	238.12713	#	6.240	0.534
		239	239.12941	*	7.403	.541

Table 1.2.3 — (Continued)

Atomic		Mass	Isotopic weight	Error in isotopic	Binding energy	Packing
number		number	relative	weight	of additional	fraction
(Z)	Symbol	(A)*	to O ¹⁶ †	× 10 ⁶ ‡	neutron, mev§	× 10 ³ ¶
		240	240.13044	*	6.696	0.544
		241	(241.13233)	*	6.528	.549
		242	242.13420	≠	5.811	.555
		243	243.13694	≠	5.960	.564
		244	244.13952	*		.572
97	Bk	243	243. 13860	*	5.923	0.570
		244	(244.14122)	#	7.366	.579
		245	245.14229	*	5.402	.581
		246	246.14547	*		.591
98	Cf	243	(243.14131)	*	7.617	0.582
		244	244.14211	*	6.901	.582
		245	(245.14368)	*	6.733	.586
		246	246.1454 3	×		.591

^{*} Numbers underlined are isotopes which occur naturally

Table 1.2.4 — See page 158.

Table 1.2.5 — Maximum Ranges of Gross Fission Recoils (Segrè and Wiegand, Phys. Rev., 70, 808, 1946)

Material	Range, mg/cm ²
Collodion	2.6
Al	3.7
Cu	5.2
U ₃ O ₈	10.0
11	12.6

[†] Figures in parentheses () indicate an uncertainty in the value since the only available input data are uncertain

[‡] All errors marked ≠ are ~ 1000 based on Pb208 error

[§] See Eq. (6)

¹ See Eq. (3)

.'r

'ir fr

> ilan Ir

> > 1,

Table 1.2.6 — Spontaneous and Gamma-ray-induced Fission Data

(Column 2 data from LA-1010, Chapter 6, Emilio Segrè, Table 6.3-14; column 3 data from W. Koch, Phys. Rev., 77, 329, 1950)

	Spontaneous fission decay constant,	Gamma-ray-induced fission threshold,
Isotope	fissions/(gm)(sec)	mev
Ra ²²⁶	(< 0.6)	
Th ²³⁰	<3.8 × 10 ⁻⁴	
Th ²³²	4.2×10^{-5}	5.4 ± 0.2
Pazi	5 × 10 ⁻³	0.1 2 0.2
U ²³²	16	
U ²³³	$< 2 \times 10^{-4}$	5.2 ± 0.3
U ²³⁴	< 9 × 10 ⁻³	3.2 2 3.3
U ²³⁵	$(3.0 \pm 1.7) \times 10^{-4}$	5.3 ± 0.3
U ²³⁶	$(-6 \pm 16) \times 10^{-2}$	
U ²³⁸	$(6.90 \pm 0.24) \times 10^{-3}$	5.1 ± 0.2
Np ²³⁷	$\leq 1.4 \times 10^{-3}$	
Np ²³⁹	<11	
Pu ²³⁸	2.14 × 10 ³	
Pu ²³⁹	1.0×10^{-2}	5.3 ± 0.3
Pu ²⁴⁰	4.61×10^{2}	
95 ²⁴¹	(46)	

Table 1.2.7 — Fission Yields*
(Coryell and Sugarman, Radiochemical Studies: The Fission Products, Book 2)

		Slow-	Slow-neutron fission		Fast-neutron fission			σ _a , bt
Nuclide	Half-life	U ²³⁶	Pum	Uma	Th ²⁰¹	U ²²⁶	Pu ²²⁰	(2200 m/sec)
Zn ⁷²	49.0 hr	1.5 × 10 ⁻⁶	1.1 × 10 ⁻⁴		1.3 × 10 ⁻⁴			
Ga ¹³	5.0 hr	1.0 × 10 ⁻⁴						
Ge ^{ff}	12 hr	3.7×10^{-3}		0.008	0.091	4.3×10^{-3}		
As ^{tt}	40 hr	9.1×10^{-3}		.018				
Ge ¹⁸	2.1 hr	0.02						
As ⁷⁸	90 min	.02						
Se ⁸¹	57 min	.008						
Se ⁸¹	13.6 min	.133						
Br ⁸²	36.0 hr	3.5×10^{-5} (1)						
Se ¹³	25 min	0.21						
Br ⁸³	2.4 hr	.48	0.080	0.70	2.4			
		.40						
Kr ⁸³	Stable	.586						205 ± 10
Br ⁸⁴	33 min	.65						
Kr84	Stable	1.09						< 2
Kr ⁸⁵	4.36 hr	33% of Kr ⁸⁸						
Kr ⁸⁵	9.4 yr	0.317						< 15
	,.	.24						
Kr ⁸⁶	Stable	2.09						<2
Rb ⁸⁶	19.5 days	3.1×10^{-5} (i)						
		1.8×10^{-4} (i)						
Kr ⁸⁷	78 min	70% of Kr86						
Sras	53 days	4.6	1.8	5.6	6.0	3.3		
	00,0	3.2		4.1				
Sr**	19.9 yr	2.3			5.9			≥ 1.0 ± 0.6
Sr ⁹¹	9.7 hr	5.0	2.3		5.7			-1.0 - 0.10
Y ⁹¹	57 days	5.9	2.8	4.1	•••			
-	J. 22,5	4.0	2.5					

Table 1.2.7 — (Continued)

		Slow-ne	utron fissio	a	Fast-n	eutron fission	n	a ht
Nuclide	Half-life	U ²²⁶	Pu ²⁹⁰	Uzza	Thm	U ²³⁶	Puzz	σ_a , b† (2200 m/sec)
8r ³²	2.7 hr	5.0						
Yes	16.5 min	5						
Zr ^{ss}	65 days	6.0 6.4; 3.2	5.6	5.7		7.3	5.6	
Zr ^M	17.0 hr	6.2	5.3	3.9	4.9		5.2	
Mo ⁸⁶	67 hr	6.1 6.2	6.1	4.7	2.65	5.9	5.9	
Rh ¹⁰²	210 days	<5 × 10 ⁻⁷ (i)	0.1	4.1	2.03	3.5	3.5	
Ru ¹⁶²	42 days	3.7		0.85	0.18	7.4		
	12 ULYS	3.7 0.84	5.5	.21	0.16	7.9		
Ru ¹⁶⁵	4.5 hr	.9						
Rh 165	36.5 hr		3.7		0.07			,
Rts 106	1.0 yr	0.52	4.7	0.24	.052	2.7		
	•	.15		.064				
Pd 100	13 hr	.028	1.0	.047	0.047		1.7	
		.017						
Ag ¹¹¹	7.6 days	.018	0.27	0.022	0.044	0.072		
•		.016	••••	.015		• • • • • • • • • • • • • • • • • • • •		
Pd112	21 hr	8.3 × 10 ⁻³	0.10	.014	0.058			
		0.011	0.20	.014	******			
Cd115	43 days	8 × 10 ⁻⁴	3 × 10 ⁻³	0.001		6 × 10 ⁻³		
Cd156	2.33 days	0.011	0.045	.016	0.053	0.057		
		.020	0.040	.010	0.000	0.00.		
Cd ¹ ff	2.83 hr	.010						
Sm 121	26.4 hr	.014	0.041	0.018				
Sm 123	130 days	1.2 × 10 ⁻³	0.041	2.5 × 10 ⁻³				
	,	8.5 × 10 ⁻⁴		2.0 ~ 10				
3n ¹²⁵	10.0 days	0.012	0.068	0.054				
	33.5 4	4.4 × 10 ⁻³	0.000	0.001				
3b ¹³⁵	~ 2.7 yr	0.023						
	•	.017						
Sm (126)	70 min	.1						
50 ¹²⁷	93 hr	.094	0.37	0.092		0.12		
Te ¹²⁷	90 days	.033	•	.067		• • • • • • • • • • • • • • • • • • • •		
		.015						
Te ¹²⁰	32 days	.19		0.22				
	J, J	.09		0.22				
Xe ¹²⁰	Stable	<4 × 10 ⁻⁴						45 ± 15
Te ¹³¹	30 hr	0.44						40 - 10
1 131	8.0 days	2.8	3.6	2.7	0.65			≥ 600 ± 300
	0.0 0.5	2.23	3.4	2.4	0.03			- 000 2 000
Xe ¹³¹	Stable	2.80		•.•				120 ± 15
Te ^{cas}	77 hr	4.4	4.9	4.9	1.6			150 - 10
	******	4.9	4.0	4.0	2.0			
		3.4						
		2.1						
Xe ^{CM}	Stable	4.17						< 5
Te ¹³⁰	66 min	4.5						•
I ₁₃₈	22.4 hr	4.6	5.0					
		1.2 (i)	•••					
Xe ¹³⁸	5.27 days	6.29						
Catas	Stable	103% of Ca ¹³⁷						29.0 ± 1.5
Tem	44 min	6.9						
I ₁₀₄	52.5 min	5.7						
140		1.0 (1)						
Xe ¹³⁴	Stable	7.41						< 5
lat	6.68 hr	5.6	5.5					-
Xe ¹³⁶	9.2 hr	6.71						3.5×10^6
0.12		0.3 (1)						
Caus	2.1 × 10 ⁶ yr	128% of Ca ¹³⁷						≥ 15 ± 8
I ₁₃₆	•	110% of Cs ¹³⁷						,
Xe ¹³⁴	86 sec	3.1	1.9	1.7				
Calle	Stable	6.14	·-					<5
~~~	13.7 days	$6.2 \times 10^{-3}$ (1)	0.09 (1)					

Table 1.2.7 — (Continued)

		Slow-	neutron fissi	on	Fast-neutron fission			σ _a , bt
Nuclide H	Half-life	U ²³⁶	Pu 239	Uzzz	Th 222	U ²³⁶	Pu ²⁰⁰	(2 <b>200</b> m/sec)
Cs 137	33 yr				5.8			
Ba 130	85.0 min	6.3	5.4			5.1		≥4 ± 1
		6.1						
Ba 140	12.80 days	6.17	5.36	6.0	5.5	6.1	5.0	
		5.82		6.7		4.2		
		5.6						
Late	40.0 hr	<0.2 (i)						≥3 ± 2
Ba ¹⁴¹	18 min	4.6						
Ce ¹⁴¹	30 days	5.7	4.9		~6			
La ¹⁴³	19 min	~3.8						
Ce ¹⁴³	33 hr	5.4	5.1					
Nd143	Stable	5.40						290 ± 30
Ce ¹⁴⁴	275 days	5.3	3.7	3.4	6.2			
		2.9		2.2				
Nd ¹⁴⁴	Stable	4.64						$4.8 \pm 0.5$
Nd ¹⁴⁶	Stable	3.62						52 ± 4
Nd ¹⁴⁶	Stable	2.81						$9.8 \pm 0.8$
Nd ^{M7}	11.0 days	2.6						
Pm ¹⁴⁷	~4 yr	~0.6		0.6				≥ <b>6</b> 0 ± 20
Nd 148	Stable	1.64			•			$3.3 \pm 1.0$
Pm 148	47 hr	1.3						
Nd 150	Stable	0.658						$2.9 \pm 1.5$
Sm ^{15 1}	~ 1000 yr	.445						≥7000 ± 2000¶
Sm 152	Stable	.279						≥ 150 ± 40
Sm 163	47 hr	.15	0.39	0.078			0.48	
Sm 154	Stable	.0908						≥5.5 ± 1.1
Sm 156	25 min	0.031	0.21					
Eu 156	2.0 yr	~ .03						≥ 14000 ± 4000¶
Sm 156	~ 10 hr	.012						
Eu 156	15.4 days	.013	0.12			0.063		
		.014						
Eu (151)	15.4 hr	$7.4 \times 10^{-3}$						
Gd 187	Stable	0.0150						160000 ± 60000¶
Eu (158)	60 min	2 × 10 ⁻³						
Gd ¹⁵⁸	Stable	0.0084						≥4±2
Gd 180	Stable	.0027						≥ 1.5 ± 0.5

[°] The independent or direct yield is designated "(i)." Other yields are total values, i.e., the independent yield plus the yield from precursors in the decay chain. Some of the yields given in the table were measured relative to 8.0-day I¹⁹¹. C. D. Coryell (private communication) now believes a better value for 8.0-day I¹⁹¹ is 3.1% (compared to the old value of 2.8%). Hence, all yields based on I¹⁹¹ should be increased by the factor 1.107. For detailed references, see Reference (18) 1 Values of  $\sigma_a$ 's taken from Reference (19) unless otherwise noted

The value for the total yield of Xe¹⁸ is still somewhat in doubt. The value of 6.7% quoted here is from WAPD-RM-96 for reactor neutrons

Table	1 2	.8 Kinetic	Energy of	the Fission	Fragments

	U223	U ²³⁶	Pu ²³⁹
Most probable energy of light			
fragment, mev	91.2	92.7	93
Most probable energy of heavy			
fragment, mev	55.5	59	65
Width of high energy peak, mev	14	12	12
Width of low energy peak, mev	22	20	20
Most probable total kinetic			
energy, mev	147.5	151.5	156
Most probable mass ratio	1.60	1.49	1.32

Table 1.2.9 —Beta-emitters Having Neutron-emitting Daughters

Isotope	Half-life, see
Br ⁸⁷	55 <b>.6</b>
I ¹³⁷	22.0
Br ⁽⁸⁹⁾ *	4.51
(Te ¹³⁶ )*	1.52

^{*} Data in parentheses are uncertain

Table 1.2.10 - Delayed-neutron Data

		Yield per 10 ⁴ prompt neutrons					
Mean life of delayed neutrons,*	Energy of delayed neutrons,† kev	Thermal fission			Fast fission		
sec sec		U-235*	U-233‡	Pu-239\$	U-238¶	Th-232**	
80.2	250	2.5	1.8	1.4	10.8	43.7	
31.7	570	16.6	5.8	10.5	90.3	102.0	
6.51	412	21.3	8. <b>6</b>	12.6††	60.2	97.0	
2.19	670	24.1	6.2	11 0++	120.4	61.1	
0.62	400	8.5	1.8}	11.9‡‡	38.5	16.5	
.07		2.5					
	TOTA	L 75.5	24.2	36.455	[320]¶¶	[320]¶¶	

^{*} Hughes, Dabbs, Kahn, and Hall, Phys. Rev., 73, 111, 1948

[†] Average of values from Hughes et al (footnote *) and Burgy, Mon S-29, 1945

[‡] Hughes, Dabbs, and Kahn, CP-3147, 1945; absolute value based on U-233/U-235=0.33, excluding 0.07 sec mean life

¹ Redman and Saxon, CK-P-2318, 1944, and Feld and de Hoffman, LA-231, 9145; absolute value based on Pu/U-235 = 0.5, excluding 0.07 sec mean life

¹⁸un et al, Phys. Rev., 79, 3, 1950; fission by neutrons of maximum energy 14 mev. absolute yield is approximate based on 0.08  $\pm$  0.03 delayed neutron per fission and  $\nu\sim2.5$ 

^{**} Based on 7.5 sec mean life

^{††} Based on composite 1.6 sec mean life

**^{‡‡}** Ratio of percentage yield of delayed neutrons for fast and thermal fission =  $Y_F/Y_{Th}$  = 0.93 ± 0.07, ORNL-517, 1949

^{§§} Value uncertain

Table 1.2.11 — Distribution of Energy in Slow-neutron Fission of U²³⁵
(BNL-152, Jan. 1952)*

	Instantaneous, mev	Delayed, mev	Totals, mev
Localized in space	Fission-product kinetic energy = 168 ± 5	Fission product betas = 7*	~ 175
Spread out in space	Neutron kinetic energy = 5 ± 0.5 Fission gammas = 4.6 ± 1	Fission product gammas = 6*	~16
Total	~ 178	13 ± 2	~ 191
Neutrino energy, 11 m	nev (not available as heat source) ²⁴		~11

Total ~ 202 mev

Table 1.2.12 — Collision Parameters

Element	W		1 ~	low 1/m	202.4	Number of collisions from 2 mey to thermal
Element	M	ξ*	$1-\alpha$	$\log_e 1/\alpha$	cos θ	2 mev to thermal
Н	1	1.000	1.000	•••	0.667	18
D	2	0.725	0.889	2.20	.333	25
He	4	.425	.640	1.022	.167	43
Li	7	.268	.438	0.575	.0954	67
Be	9	.209	.360	.446	.0743	86
С	12	.158	.284	.334	.0556	114
0	16	.120	.220	.250	.0417	150
Na	23	.0845	.165	.174	.0290	213
U	238	.00838	.0167	.0169	.00280	2148
Large M	A	$2/(A + \frac{2}{3})$	4/(A+2)	4/(A + 2)	²/ ₃ A	9A + 6

*
$$\xi = 1 + \frac{\alpha}{1 - \alpha} \ln \alpha$$
;  $\alpha = \left(\frac{A - 1}{A + 1}\right)^2$ 

Table 1.2.13 —  $\sigma_e(1 - \overline{\cos \theta})$  for Some Light Elements (LA-1339)

Scatterer	$\sigma_{\mathbf{e}}(1-\overline{\cos\theta})$ , b
Ве	1.01
С	1.47
Al	1.70
Cr	1.93
Fe	1.60
Ni	1.40
Cu	1.43

^{*}The organization of the table was suggested by a table of John R. Stehn based on data from Old and Weil, TID 65, 1948. The division of the beta and gamma fission product is also from the latter source

Table 1.2.14—Transport Cross Sections

(H. Feshbach, AECD-2904, The experimental work was done by Barschall, Battat, Bright, Graves, Jorgensen, and Manley at Los Alamos)

Transport cross sections, barns, for neutron energy of

Element	0.2 mev	0.6 mev	1.5 me <b>v</b>	3.0 mev
Ве		3. <del>4</del> 0	1.40	
B ¹⁰		3.9	2.1	
B ¹¹		2.1	2.2	
С		2.8	1.8	
Al	•	3.0	1.7	1.4
Fe	3	2.0	2.2	2.0
Pb	7	3.4	3.4	3.8
w	6	4.7	4.7	4.1
Au	6.4			
Ta*			3.9	
Cu*			2.2	
Ni*			2.3	
Co*			2.2	

^{*}These data not contained in AECD-2904

-70

2

ı

ţ

Table 1.2.15 — Inelastic Cross Sections

(NYO-636, Final Report of the Fast Neutron Data Project and Byster and Carter, private communication from Los Alamos)

Element	Incident neutron energy (E), mev	Approximate threshold energy of detector $(\mathbf{E}_{\mathbf{t}})$ , mev	Cross section for scattering from energy E to below $E_t$ , $\sigma_{in}$ (E, $E_t$ ), * barns	Reference
Be	14	3	$0.16 \pm 0.07$	(35)
		11	.82 ± .03	
В	14	3	.24 ± .04	(35)
		11	.69 ± .10	
С	2.5	2.5	< 0.006	(36)
_	14	11	$0.85 \pm 0.02$	(35)
F	2.5	2.5	$.62 \pm .01$	(36)
Mg	2.5	2.5	1.0 ± .15	(36)
Al	Fission-	0.4	0.12	(37)
	spectrum	.7	.37	
	neutrons	~3 3	.73	(05)
	_14	11	0.62 ± 0.07 1.06 ± .05	(35)
8	2.5	2.5	1.06 ± .05 0.44 ± .06	(98)
Fe	Fission-	2.5 0. <b>4</b>	.265 ± .04	(3 <b>6</b> ) (3 <b>7</b> )
re	spectrum	.7	0.70	(31)
	neutrons	~3	1.30	
	1.5	0.5	0	(38)
	2.0	.9	0.6	(00)
	3.0	.75	.3	
	•••	1.50	.7	
		2.25	1.1	
	14	2	$0.78 \pm 0.03$	(35)
		3	1.21 ± .03	
		11	$1.45 \pm .02$	
Co	1.5	0.5	(0)	(38)
		.9	(0.2)	
		1.3	(.8)	
Ni	Fission-	0.4	.286	(37)
	spectrum	.7	.72	
	neutrons	~3	1.43	
	1.5	0.5	(0)	(38)
		.9	(0.1)	
•	<b></b> .	1.3	(.6)	4
Cu	Fission-	0.4	.31	(37)
	spectrum	.7	.91	
	neutrons	~3	1.56	(0.0)
	1.5	0.5	(0.3)	(38)
		.9	(.6)	
	3.0	1.3	(.9)	
	ა.ს	0.75 1.50	(.6) (1.3)	
		2.25		
Zn	Fission-	2.25 0. <b>4</b>	(1.5) <b>0.313</b>	(37)
<b>-</b> 111	spectrum	.7	.95	(37)
	neutrons	.1	.50	

11203

œ

Element	Incident neutron energy (E), mev	Approximate threshold energy of detector $(E_t)$ , mev	Cross section for scattering from energy E to below $E_t$ , $\sigma_{in}$ (E, $E_t$ ),* barns	Reference
As	Fission-	0.4	0.86	(37)
A.B	spectrum	.7	1.67	(37)
	neutrons	~3	2.03	
Zr	Fission-		2.00	
	spectrum			
	neutrons	~3	1.70	(37)
Cd	Fission-	0.4	0.67	(37)
	spectrum	.7	1.54	
	neutrons	~3	2.08	
	14	2	$1.14 \pm 0.04$	(35)
		3	$1.66 \pm .07$	
	<b>-</b> 11	11	$1.89 \pm .06$	(a.m.)
Sin	Fission-	0.4 .7	$0.38 \pm 0.05$	(37)
	spectrum neutrons	.₁ ~3	1.15	
Ta	1.5	~ 3 0.5	2.07	(20)
14	1.5	.9	(1.4) (2.0)	(38)
		1.3	(2.7)	
w	Fission-	0.4	1.09	(37)
••	spectrum	.7	2.18	(01)
	neutrons	~3	2.75	
	1.5	0.5	0.9	(38)
		.9	2.1	,,
	3.0	.75	1.4	
		1.50	2.4	
		2.25	2.8	
Au	Fission-	0.4	1.01	(37)
	spectrum	.7	2.06	
	neutrons	~3	2.68	
	3.0	0.75	(2.1)	(38)
		1.50	(2.8)	
		2.25	(3.0)	41
	14	2 3	$1.47 \pm 0.10$	(35)
		3 11	2.06 ± .09	
Pb	Fission-	0.4	2.51 ± .04	(27)
	spectrum	.7	0.25 ± .07 0.745	(37)
	neutrons	~3	2.24	
	1.5	0.5	0	(38)
		.9	0.4	(00)
	3	.75	.7	
		1.50	1.2	
		2.25	1.6	
	2.5	1	0.55	(39)
		2.5	$1.3 \pm 0.5$	(40)
	14	2	$0.91 \pm .06$	(35)
		3	2.29 ± .04	
		11	2.56 ± .04	
	14.5	3	$2.20 \pm .17$	
		11	$2.29 \pm .12$	

Table 1.2.15 — (Continued)

Element	Incident neutron energy (E), mev	Approximate threshold energy of detector $(E_t)$ , mev	Cross section for scattering from energy E to below $E_t$ , $\sigma_{in}$ (E,E _t ),* barns	Reference
Bi	Fission-	0.4	0.20 ± .05	(37)
	spectrum	.7	0.743	
	neutrons	~3	2.33	
	2.5	1	0.64	(39)
	14	2	$1.03 \pm 0.11$	(35)
		3	2.28 ± .08	
		11	$2.56 \pm .05$	

^{*}The values in parentheses have not been corrected for the effects of multiple scattering in the target

Table 1.2.16 — (n,2n) Cross Sections at 14 Mev

Target isotope	Cross section (isotopic), barns
Cu ⁶³	0.51
Cu ⁶⁵ Cu ⁶⁶	.97
As ¹⁰⁷	.56*
As ¹⁰⁹	1.00
U ²³⁸	$0.4 \pm 0.3\dagger$

^{*} For production of 24.5-min isomer † See reference (49)

Table 1.2.17 — See page 351.

Isotope	Threshold energy, mev	σ (n,p)	Reference		
O16	9.5	0.014 mb	(52) (53)		
O17	7.9	.010 b*	(54)		

TYSICS

ŧ

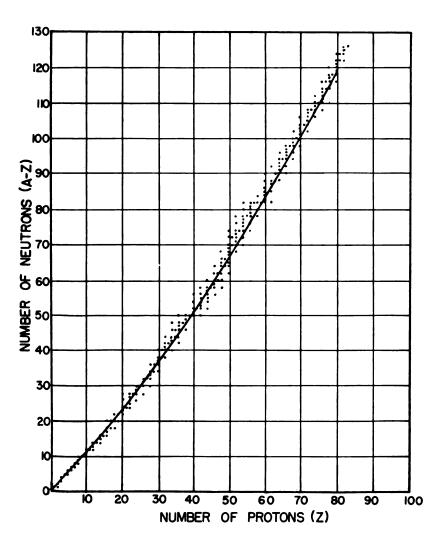


Fig. 1.2.1 — Number of Neutrons (A-Z) vs Number of Protons (Z) for Stable Nuclei. Solid line is a plot of Eq. (5a). Reprinted from the Elements of Nuclear Reactor Theory, by S. Glasstone and M. Edlund. Copyright, 1952. By permission from D. Van Nostrand Company, Inc., New York.

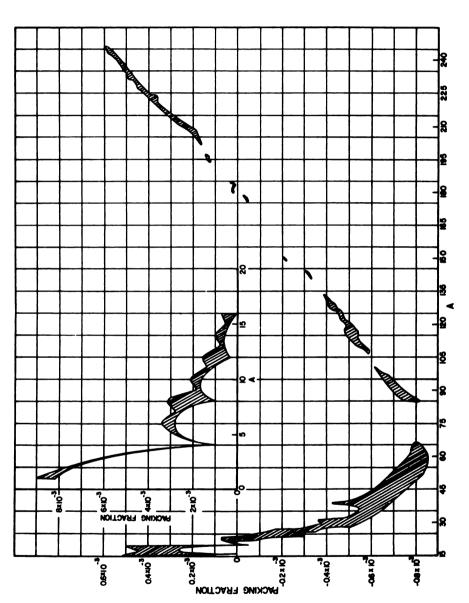


Fig. 1.2.2 — Packing Fraction Versus A. Submitted by Nuclear Development Associates, Inc., Jan. 15, 1953. The packing fractions of several isobars of a given A are available from Table 1.2.3; the spread of packing fraction values is illustrated.

116

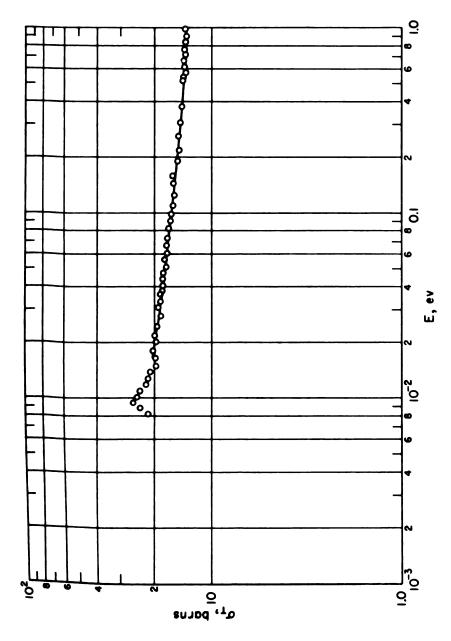


Fig. 1.2.3 - Total Cross Section of 99 Th²³². Reprinted from BNL-170.

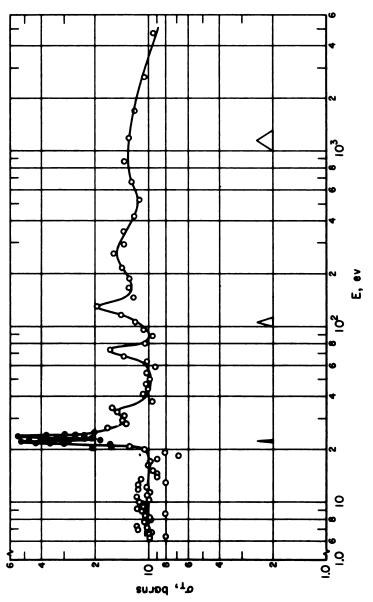


Fig. 1.2.4 — Total Cross Section of aThith. Reprinted from BNL-170A.

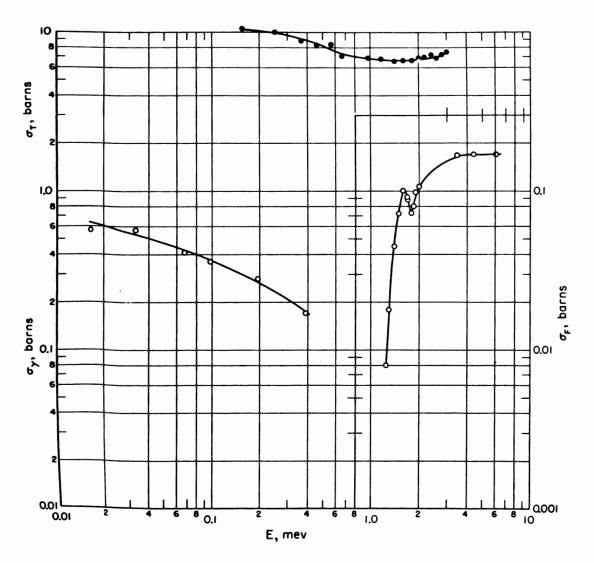


Fig. 1.2.5 — Total, Capture, and Fission Cross Section of  $_{90}\mathrm{Th}^{232}.$  Reprinted from BNL-170.

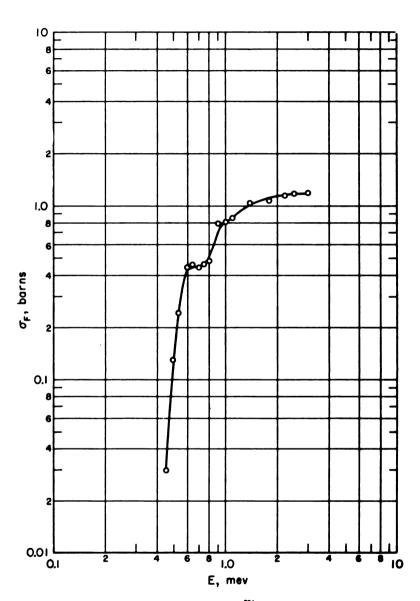


Fig. 1.2.6 — Fission Cross Section of MPa²³¹. Reprinted from BNL-170A.

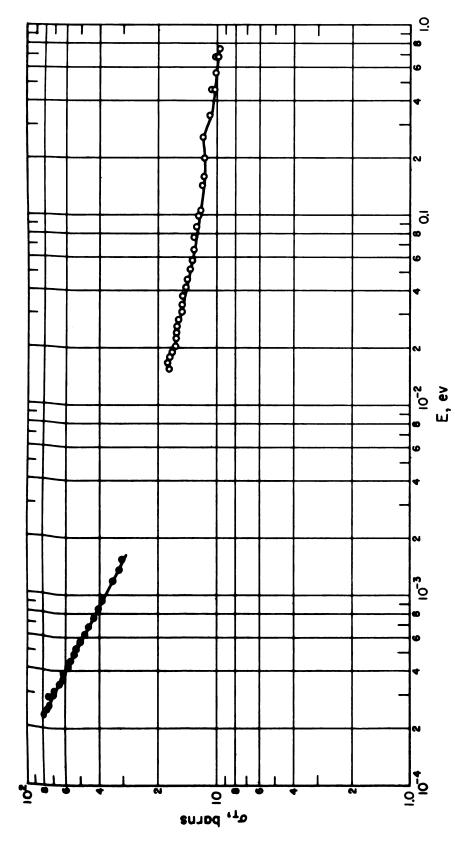


Fig. 1.2.7 — Total Cross Section of Uranium. Reprinted from BNL-170.



Fig. 1.2.8-Total Cross Section of Uranium. Reprinted from BNL-170A.

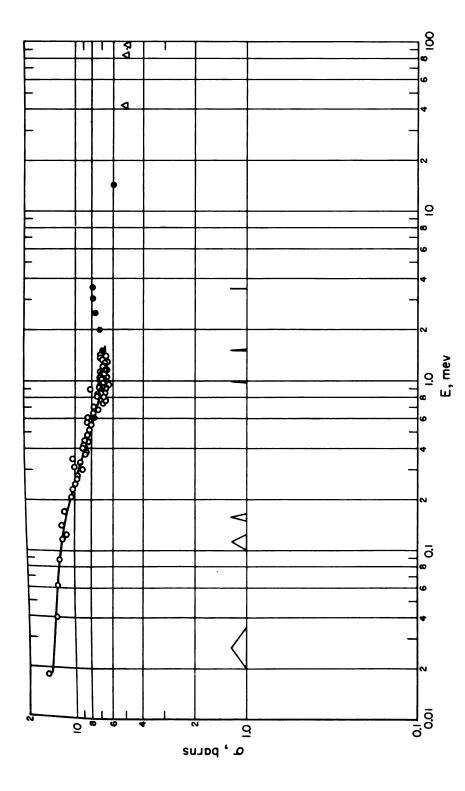


Fig. 1.2.9 — Total Cross Section of Uranium. Reprinted from BNL-170.

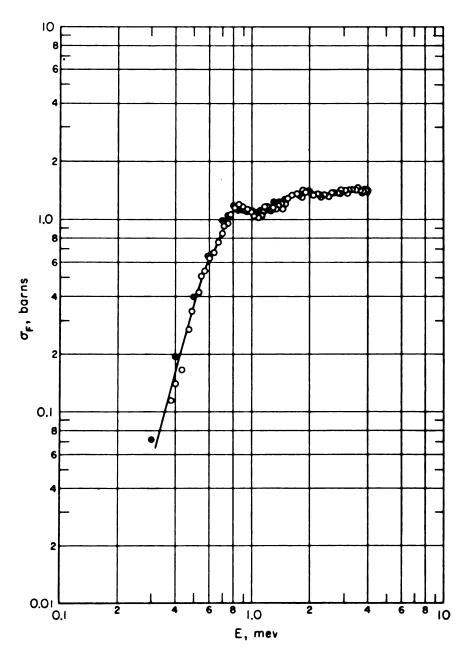


Fig. 1.2.10 — Fission Cross Section of  $_{22}$ U²³⁴. Reprinted from BNL-170A.

Digitized by Google

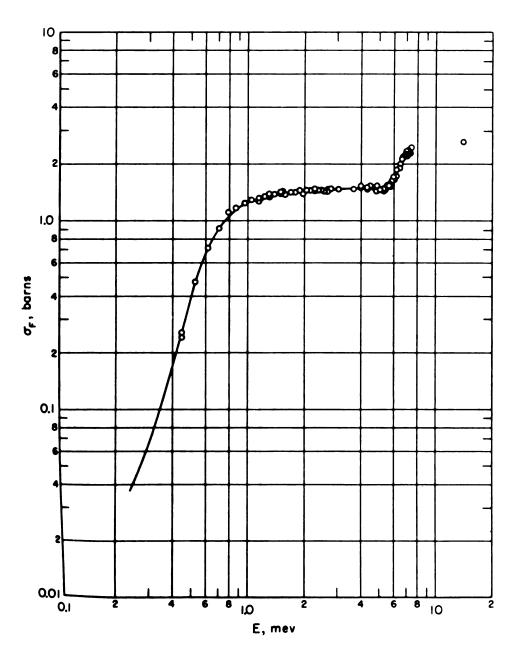


Fig. 1.2.11 — Fission Cross Section of  $_{80}Np^{237}$ . Reprinted from BNL-170A.

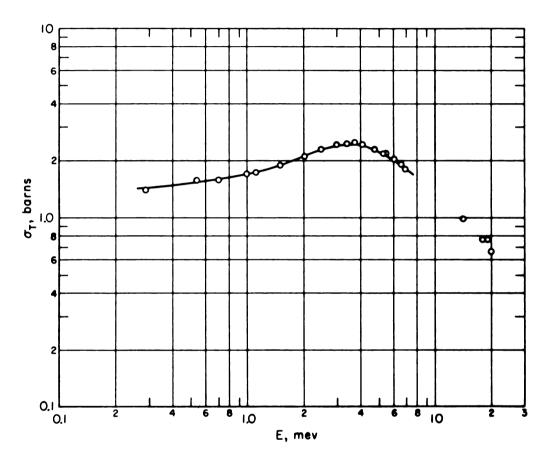


Fig. 1.2.12 — Total Cross Section of 1H3. Reprinted from BNL-170A.

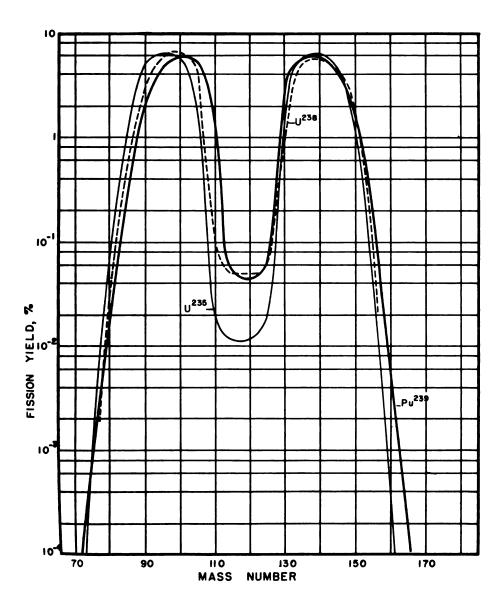


Fig. 1.2.13 — Fission Yields for Slow-neutron Fission of U²³⁵, U²³⁸ and Pu²³⁹ versus A. Reprinted from Radiochemical Studies: The Fission Products, Book 3, edited by Coryell and Sugarman, McGraw Hill Book Company, Inc., New York, 1951; U²³⁸ from paper number 219 by Steinberg and Freedman, and U²³⁶ and Pu²³⁹ from Appendix B.

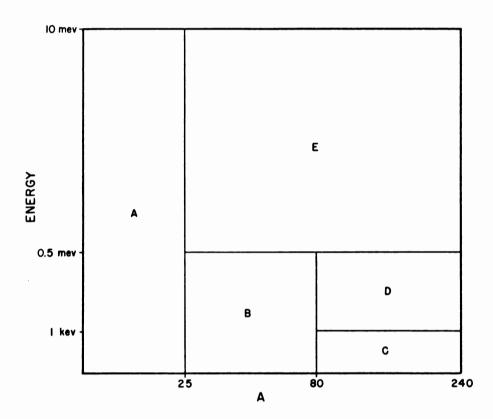


Fig. 1.2.14—Schematic Classification of Nuclear Reactions According to Energy Region and Category of Target Nucleus. Submitted by Nuclear Development Associates, Inc., Jan. 15, 1953.

Region A. Light Nuclei

Region B. Low and Intermediate Energies, Intermediate Nuclei

Region C. Low Energy, Heavy Nuclei

Region D. Intermediate Energy, Heavy Nuclei

Region E. High Energies, Heavy and Intermediate Nuclei

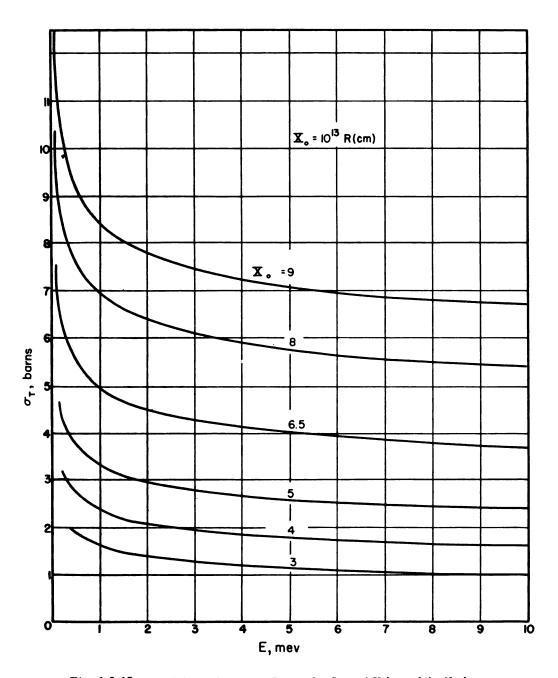


Fig. 1.2.15—Total Cross Section vs Energy for Several Values of the Nuclear Radius. Reprinted from NYO-636.

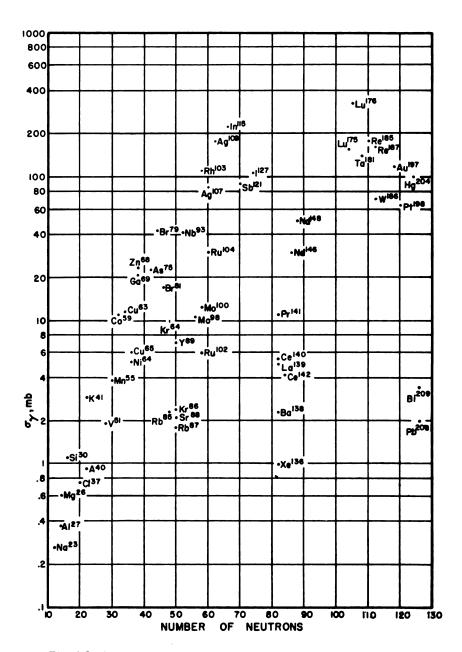


Fig. 1.2.16—Radiative-capture Cross Sections vs Number of Neutrons. Reprinted from Pile Neutron Research, by D. S. Hughes. Copyright, 1953. By permission from Addison-Wesley Press, Inc., Cambridge.

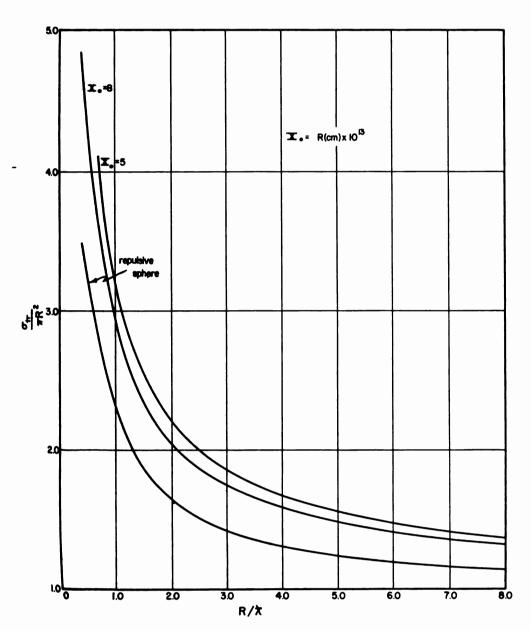


Fig. 1.2.17 — Transport Cross Section as a Function of  $R/\!\lambda$  for Various Values of the Nuclear Radius. Reprinted from ORNL-433.

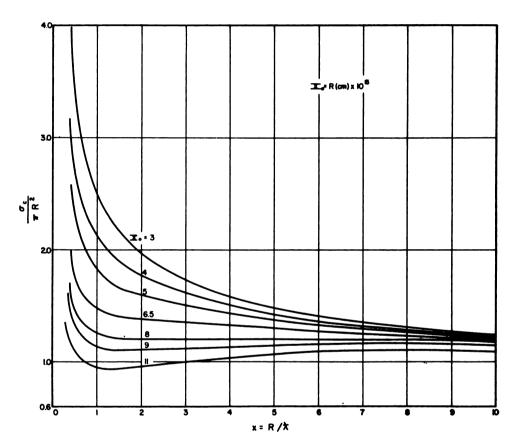


Fig. 1.2.18 — Reaction Cross Section as a Function of R/ $\hbar$  for Various Values of the Nuclear Radius. Reprinted from NYO-636.

130

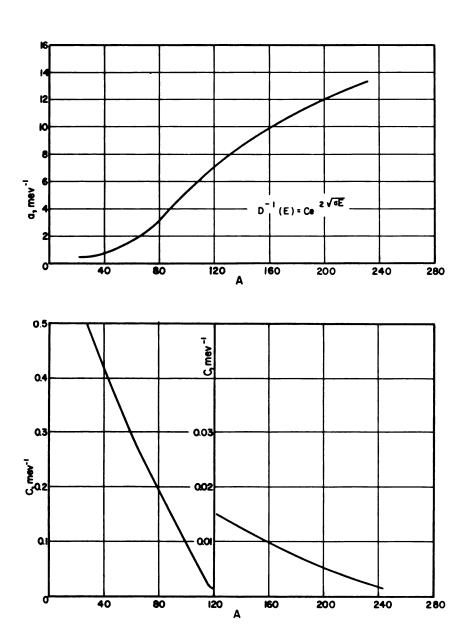


Fig. 1.2.19 — Interpolation Curves of Constants a and C for Odd A Nuclei. Reprinted from NYO-636. These constants are parameters in the formula  $1/D(E) = Ce^{2\sqrt{aE}}$  for estimating the distance between levels D(E). Even A nuclei are expected to have level separations 100 to 1000 times greater.

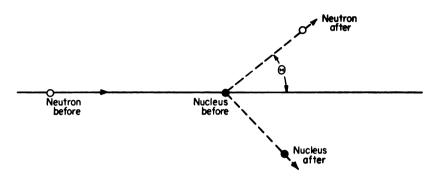


Fig. 1.2.20—Neutron Scattering in Laboratory System. Submitted by Nuclear Development Associates, Inc., Jan. 1, 1953.

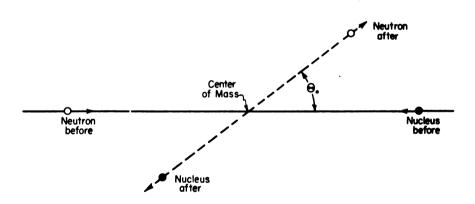


Fig. 1.2.21—Neutron Scattering in Center-of-Mass System. Submitted by Nuclear Development Associates, Inc., Jan. 1, 1953.

130

Fig. 1.2.22—Differential Elastic Scattering Cross Section for Beryllium. Reprinted from LA-1339. Ordinate gives the differential elastic scattering cross section in barns per unit solid angle.

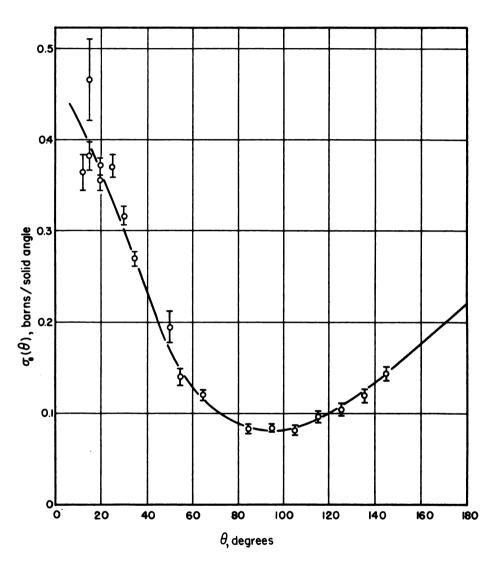


Fig. 1.2.23 — Differential Elastic Scattering Cross Section for Carbon. Reprinted from LA-1339. Ordinate gives the differential elastic scattering cross section in barns per unit solid angle.

Digitized by Google

303

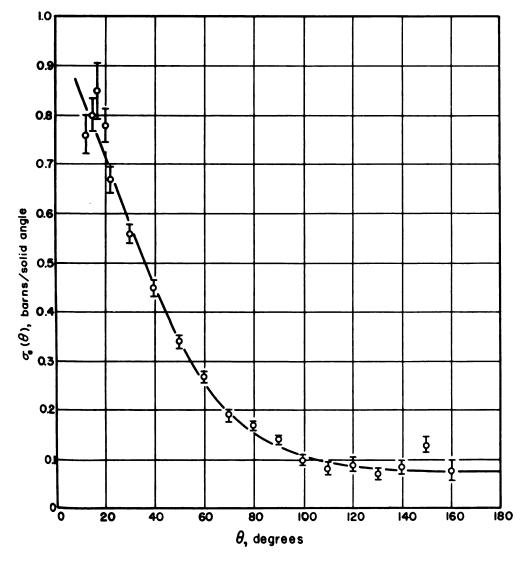


Fig. 1.2.24—Differential Elastic Scattering Cross Section for Aluminum. Reprinted from LA-1339. Ordinate gives the differential elastic scattering cross section in barns per unit solid angle.

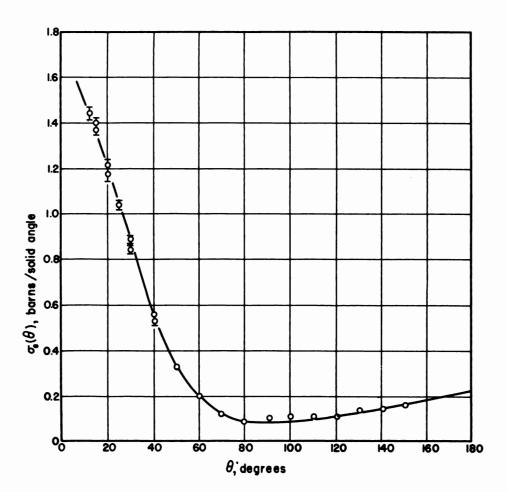


Fig. 1.2.25—Differential Elastic Scattering Cross Section for Chromium. Reprinted from LA-1339. Ordinate gives the differential elastic scattering cross section in barns per unit solid angle.

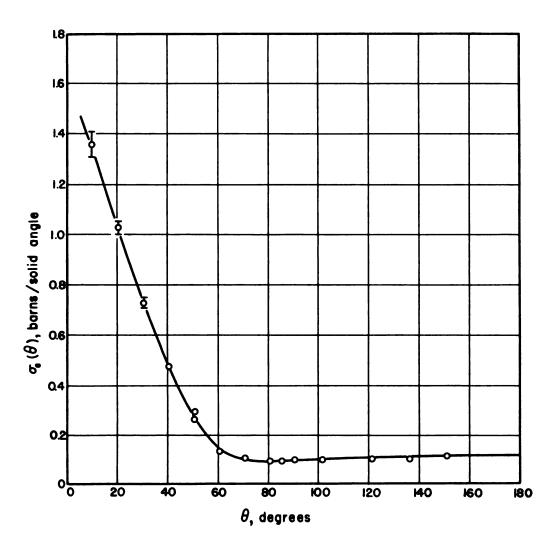


Fig. 1.2.26—Differential Elastic Scattering Cross Section for Iron. Reprinted from LA-1339. Ordinate gives the differential elastic scattering cross section in barns per unit solid angle.

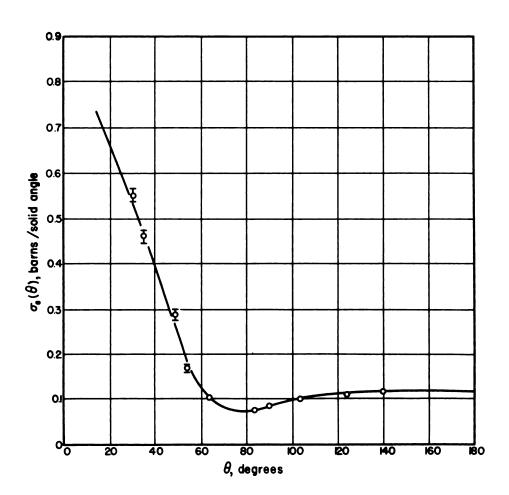


Fig. 1.2.27—Differential Elastic Scattering Cross Section for Nickel. Reprinted from LA-1339. Ordinate gives the differential elastic scattering cross section in barns per unit solid angle.

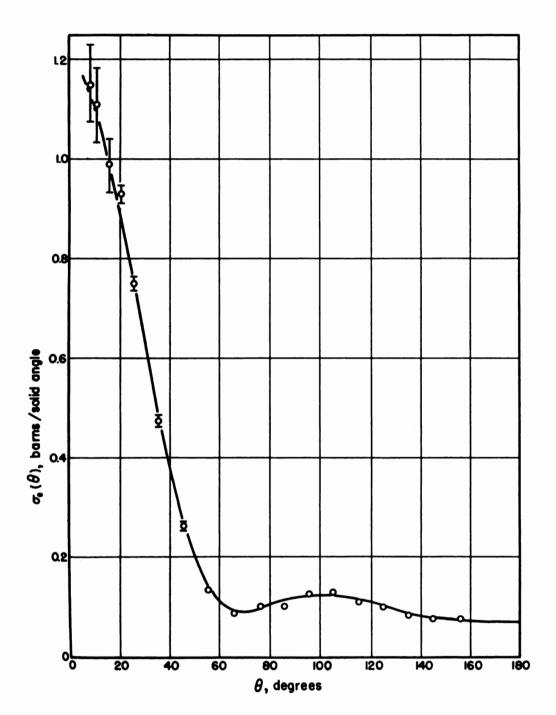


Fig. 1.2.28 — Differential Elastic Scattering Cross Section for Copper. Reprinted from LA-1339. Ordinate gives the differential elastic scattering cross section in barns per unit solid angle.

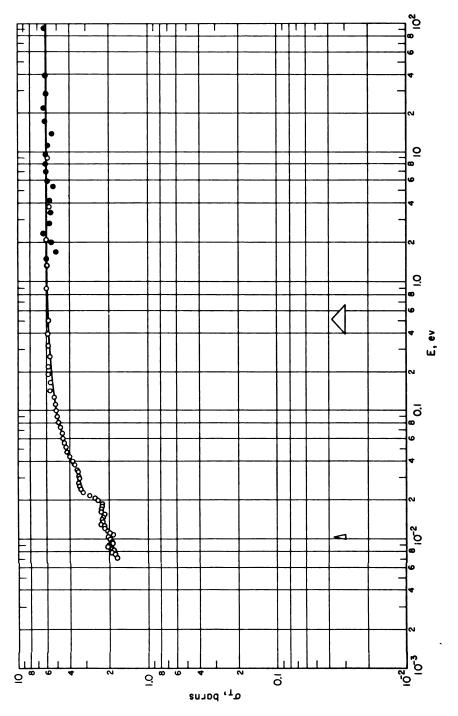


Fig. 1.2.29 -- Total Cross Section of Be. Reprinted from AECU-2040.

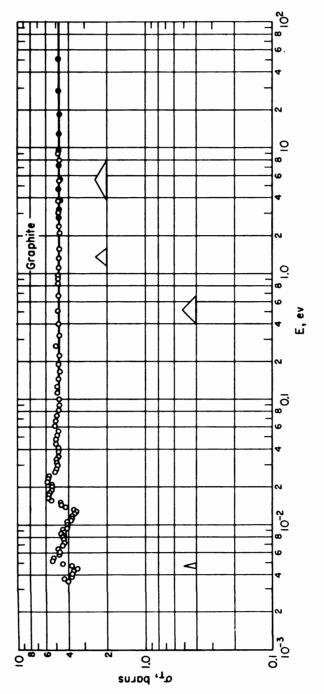


Fig. 1.2.30 — Total Cross Section of C. Reprinted from AECU-2040.

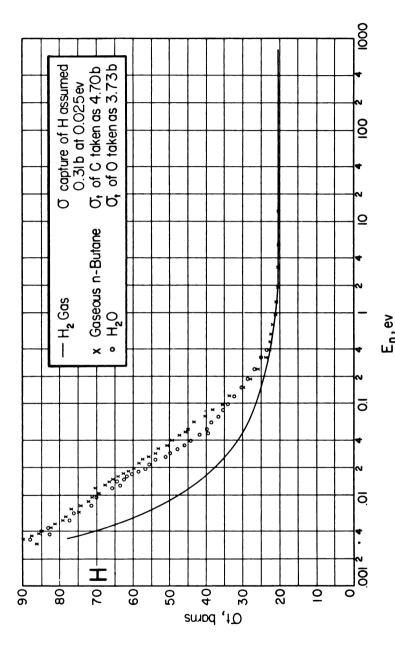


Fig. 1.2.31—Total Cross Section of Hydrogen. Reprinted from R. K. Adair, Rev. Mod. Phys., 22, 249, 1950.

13

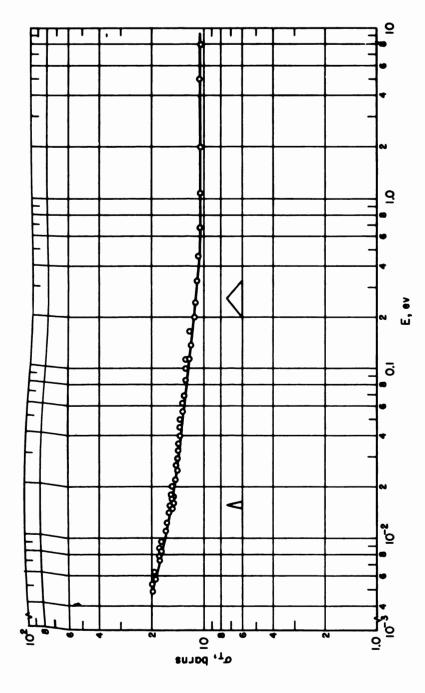


Fig. 1.2.32 - Total Cross Section of D.O. Reprinted from AECU-2040.

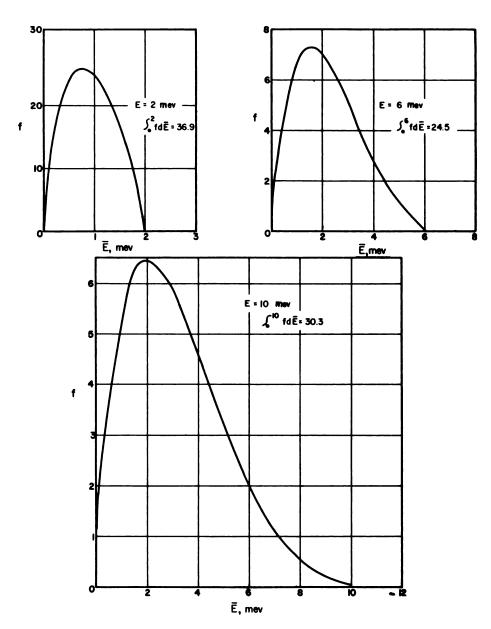
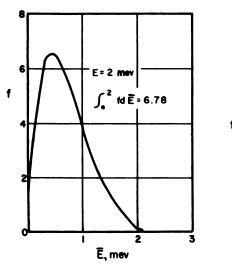
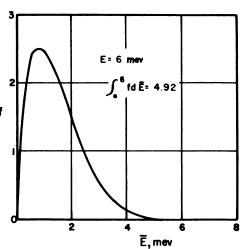


Fig. 1.2.33 — Theoretical Energy Distribution of Neutrons Inelastically Scattered by Zn. Reprinted from NYO-636. Incident neutron energy is  $\overline{E}$ , and scattered neutron energy is  $\overline{E}$ . Parameters used in Eq. (56) are: (Z = 30, A = 64); a = 1.8 mev⁻¹;  $r_0$  = 1.5 × 10⁻¹³ cm;  $E_0$  = 0.





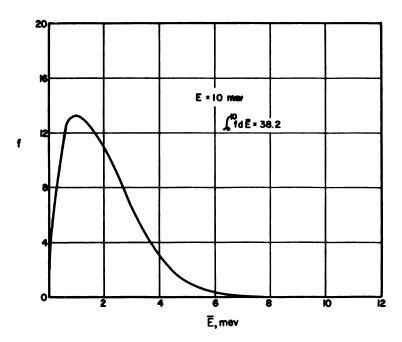
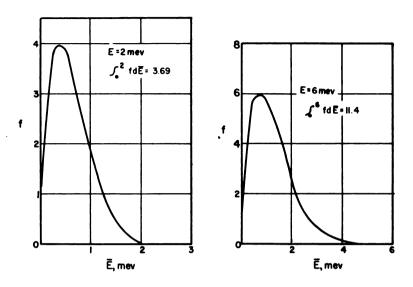


Fig. 1.2.34 — Theoretical Energy Distribution of Neutrons Inelastically Scattered by Sn. Reprinted from NYO-636. Incident neutron energy is E and scattered neutron energy is E. Parameters used in Eq. (56) are: (Z = 50, A = 120);  $a = 6.8 \text{ mev}^{-1}$ ;  $r_0 = 1.5 \times 10^{-13} \text{ cm}$ ;  $E_0 = 0$ .



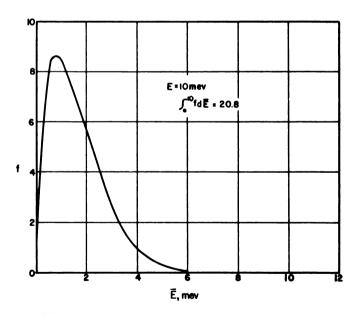


Fig. 1.2.35 — Theoretical Energy Distribution of Neutrons Inelastically Scattered by Yb. Reprinted from NYO-636. Incident neutron energy is E, and scattered neutron energy is E. Parameters used in Eq. (56) are: (Z = 70; A = 174);  $a = 10.7 \text{ mev}^{-1}$ ;  $r_0 = 1.5 \times 10^{-13} \text{ cm}$ ;  $E_0 = 0$ .

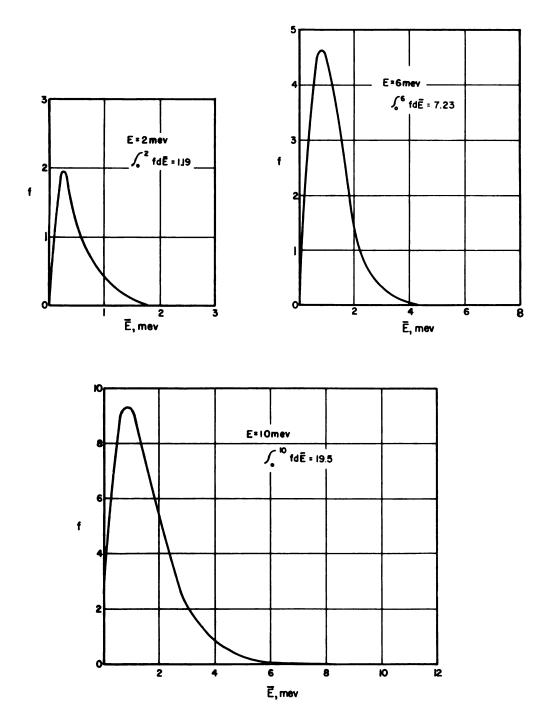
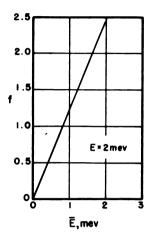
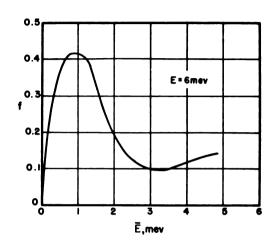


Fig. 1.2.36 — Theoretical Energy Distribution of Neutrons Inelastically Scattered by Th. Reprinted from NYO-636. Incident neutron energy is E, and scattered neutron energy is E. Parameters used in Eq. (56) are: (Z = 90; A = 232);  $a = 13.2 \text{ mev}^{-1}$ ;  $r_0 = 1.5 \times 10^{-13} \text{ cm}$ ;  $E_0 = 0$ .





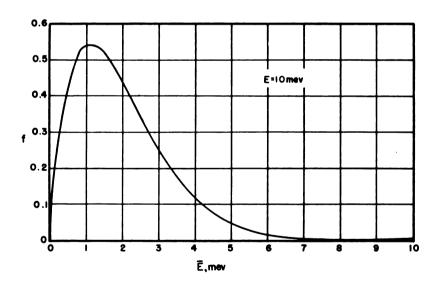


Fig. 1.2.37 — Theoretical Energy Distribution of Neutrons Inelastically Scattered from Sn for Various Incident Energies. Reprinted from NYO-636. Parameters used are: (Z = 90; A = 125); a = 6.8 mev⁻¹;  $r_0$  = 7.5 × 10⁻¹³ cm;  $E_0$  = 3 mev.

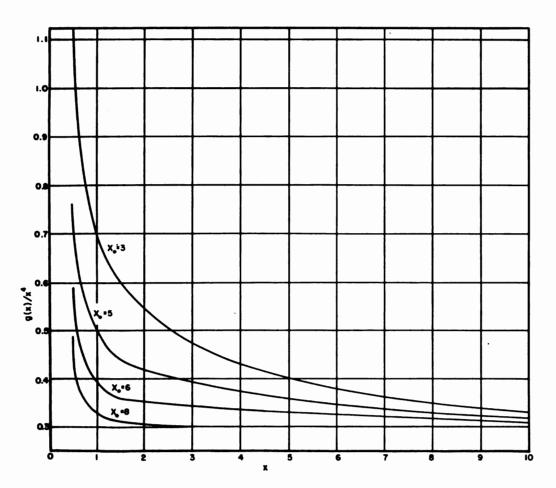


Fig. 1.2.38 — $g(x)/x^4$  vs x for Several Values of the Nuclear Radius. Reprinted from NYO-636.

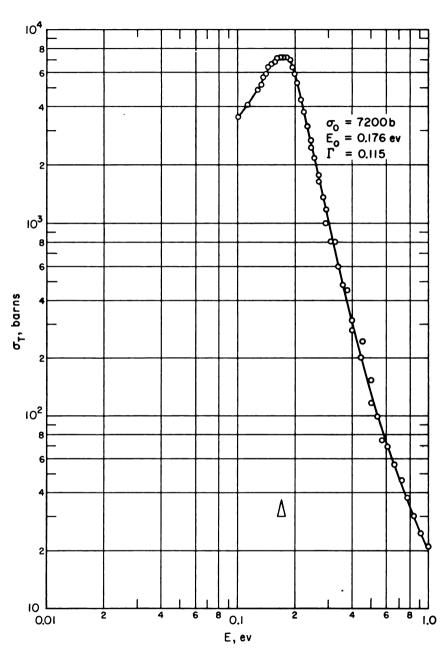


Fig. 1.2.39 — Total Cross Section of Cd. Reprinted from AECU-2040.

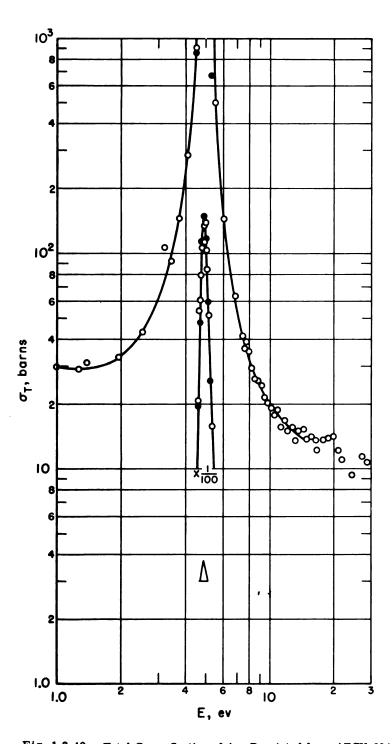


Fig. 1.2.40 — Total Cross Section of Au. Reprinted from AECU-2040.

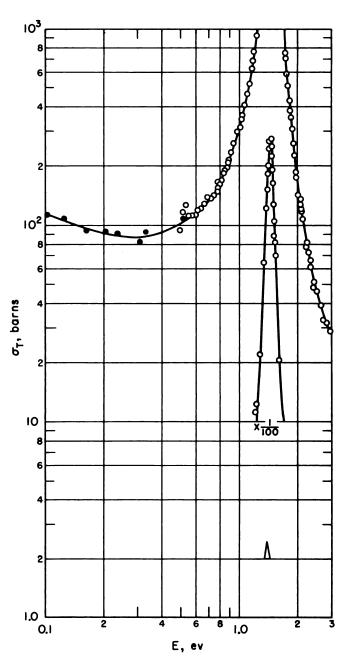


Fig. 1.2.41 — Total Cross Section of In. Reprinted from AECU-2040.

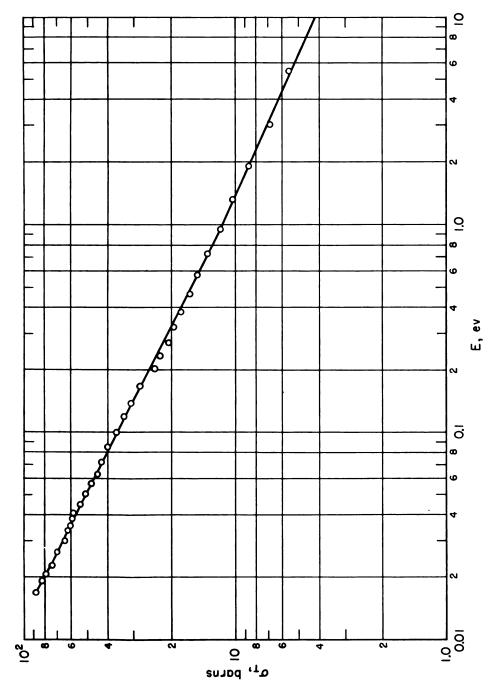


Fig. 1.2.42 — Total Cross Section of Li. Reprinted from AECU-2040.

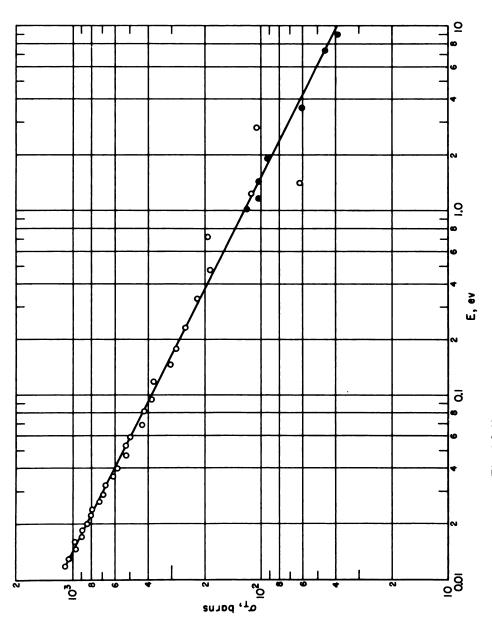


Fig. 1.2.43-Total Cross Section of B. Reprinted from AECU-2040.

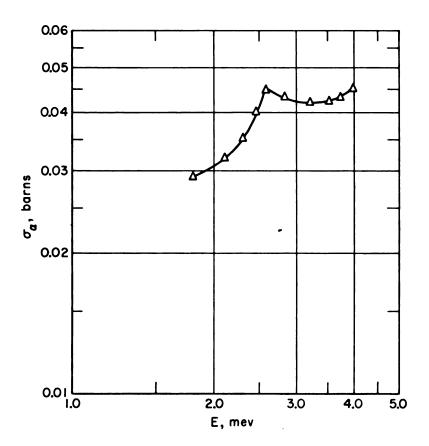


Fig. 1.2.44 — Cross Section for Be $(n,\alpha)$  Reaction. Reprinted from AECU-2040.

# Table 1.2.4 — Table of Isotopes

J. M. Hollander, I. Perlman, and G. T. Seaborg Department of Chemistry and Radiation Laboratory University of California, Berkeley, California

#### December 1952

The following table represents a complete list of all the radioactive and stable isotopes of the elements, together with a number of their salient features, as recorded in the literature or by private communication by approximately December 1952.

A primary objective has been to retain as much of the compactness of the previous editions as is consistent with an adequate coverage of the multitudes of nuclear data presently available.

A new system of references has been employed. Each paper is represented by the code symbol of the first author, followed by the year in which the paper was published. If two or more papers by one author have appeared during a single year, these are distinguished by the small letters a, b, c, etc. following the main reference. For example, 16H is the code symbol given to O. Hahn; thus, the references 16H41, 16H41a, and 16H4lb represent three papers published in 1941 of which O. Hahn is the first author. The code symbols given to the authors are arranged alphabetically only with respect to the first letter of their names.

A description of the entries in the various columns is given below, followed by a table listing some frequently used abbreviations.

## **ISOTOPE**

The first column lists the atomic numbers, chemical symbols, and mass numbers of the nuclear species. Separate entries have been made for each nuclear state whose half-life has been experimentally determined. Metastable excited states are denoted by the superscript "m" following the mass number, and for those cases in which two or more isomeric states are known, they are distinguished by the use of the superscripts "m₁", "m₂", etc.

## CLASS AND IDENTIFICATION

The degree of certainty of each isotopic assignment is indicated by a letter, according to the following code:

- A Element and mass number certain
- B Element certain and mass number probable
- C Element probable and mass number certain or probable
- D Element certain and mass number not well established
- E Element probable and mass number not well established or unknown (mass number not listed means that it is unknown)
- F Insufficient evidence
- G Assignment probably in error

Data which have been shown to be in error have in general been eliminated from the table. A few isotopes have been quoted so widely in the literature, however, that it was felt some reference



NUCLEAR PHYSICS CHAP. 1.2

should be made to them. For these cases the G rating has been adopted, and reference made both to the original work and to that which has supplanted it.

The means by which the mass assignments were made are next tabulated. In general, several references are given here, the first of which denoted the probable discoverer of the isotope (except in the cases of the old natural radioactivities). Following this, references are given to the paper or papers which contributed most significantly toward giving the isotope its best or present rating. Some indication of the experimental methods used in making the various assignments may be had from the following symbolism:

chem	Chemical separations, establishing uniquely the chemical identity (atomic number) of the isotope
genet	Proven genetic relationships (by chemical or other means) with other isotopes whose mass assignments

are presumably known

# genet energy Proof of isobaric relationship with an identified nuclide by observation of identical energy levels following decay of both, implying decay to the same product

excit Loosely refers to energetic considerations which have aided in making the mass assignment. Some of these might be:

- (1) Excitation or yield experiments to establish the nuclear reaction which produces the isotope
- (2) Bombardments with low energy particles, in which possible products are few
- (3) Mass calculations, or other estimates or measurements of Q values
- (4) In a few cases, use of fission yield data in making assignments

cross bomb

Studies of yields of the isotope in several different
types of bombardments, in which the target elements
as well as the projectiles have been varied

n-capt
Cases where bombardments with slow neutrons
(n-\gamma reactions) have provided key evidence in the
mass assignments

sep isotopes The use of target elements enriched or depleted in a certain isotope

mass spect Identification of the mass number by means of a mass spectrograph

resonance neutron activation Identification of a nuclear isomer by observing both isomers upon irradiation with filtered neutrons

decay charac Identification of expected or predicted decay characteristics

### PERCENT ABUNDANCE

The relative isotopic abundances for the elements are given in accordance with the "best values" listed in the report (1B50) by K. T. Bainbridge and A. O. Nier. In some of the light elements,

reference is made also to papers which discuss source variations in isotope abundances.

#### TYPE OF DECAY

The observed modes of decay have been listed for all radioactive nuclei. In cases of branched decay between two or more modes, the branching ratios are listed wherever they are known. Symbols used are:

- β Negative beta particle (negatron) emission
- β⁺ Positive beta particle (positron) emission
- a Alpha particle emission
- EC Orbital electron capture. It may be assumed that x-rays have been observed or actually identified in virtually all cases of orbital electron capture listed. If the ratio of L electron capture to K electron capture has been determined, it is given here as L/K.
- IT Isomeric transition (transition from upper to lower isomeric state of same nucleus)
- n Neutron emission

When experimenters have searched for and failed to find a particular mode of decay, this is indicated, for example, as "no  $\beta^+$ ". Experimental upper limits are frequently given, but no theoretically predicted limits have been quoted.

Among the heavy alpha emitting isotopes, calculations by means of closed radioactive decay cycles have shown that many of these isotopes are thermodynamically stable against  $\beta^-$ ,  $\beta^+$ , or EC decay. This has been indicated by the term " $\beta$  stable," followed by an abbreviation for the principle of conservation of energy, which is used in the calculations.

## HALF-LIFE

Half-life values are listed without qualification where the determination has been a direct measurement of decay rate. In other cases, the experimental methods have been described with the aid of the following symbols:

sp act Determination by weighing a long lived isotope of known purity

delay coinc Measurement of the time interval between two successive nuclear events (such as  $\beta^-$  and  $\gamma$  emission) thus establishing the lifetime of the state responsible for the second event. By this method, half-lives between  $10^{-3}$  s and  $10^{-10}$  s have been determined.

NUCLEAR PHYSICS CHAP. 1.2

yield Estimation of half-life from the amount of activity

resulting from a nuclear reaction whose cross

section (or yield) is known or estimated

genet Measurement of the half-life of a parent activity

by determining the yield of a daughter activity as a function of time, where periodic chemical separations of daughter from parent have been

performed

An attempt has been made to list the best value or values first. However, in a few cases where many values of comparable precision have been reported, and no choice seemed obvious, an average value for the half-life has been listed; this is explicitly stated, and references are given to all the papers whose values contributed to that average. Also, among the natural radioactivities an average value is often used which was taken from an international committee summary report (1C31).

# PARTICLE ENERGIES

The particle energies are followed by other relevant information pertaining to the decay scheme, and by a description of the experimental methods used in obtaining the data. In cases of complex alpha structure or several partial beta spectra, the relative abundances of the various groups within that mode of decay are given in parentheses.

Beta particle energies correspond to the upper limits of the spectra.

Alpha particle energies have been quoted only where the investigator has actually measured them. Where he has determined only the relative abundances of alpha groups or the energy differences between groups, this has been indicated as in the example:

meaning that 75 percent of the alpha particles lead to a state 50 kev above the ground state, and that 15 percent of the alpha particles lead to a state 80 kev above the ground state.

The term "long range a" is the classical designation for alpha particle groups emitted from excited states of the listed nuclide, and the energies therefore are not included in the  $Q_{\bf q}$  value, which applies to the ground state to ground state transition. These alpha groups occur in competition with gamma ray emission, following the beta decay of the parent nuclide.

Conversion electron energies are listed only when it is not known in which shell internal conversion takes place or when no attempt was made by the experimenter to relate the electrons with observed or unobservable gamma rays; in all other cases, entries are made in the column for gamma transitions.

Experimental methods are described as follows:

abs Absorption

Magnetic deflection (magnetic spectrograph or spect spectrometer or counter with magnetic field) Measurement of pulses produced by a scintillating scint spect crystal or solution ion ch Measurement of pulse sizes in ionization chamber or proportional counter c' ch Cloud chamber (with magnetic field in case of beta particles) coinc abs Beta and gamma coincidence counters with absorbers Coincidence counters arranged with a spectrometer coinc spect or spectrometers

## **GAMMA TRANSITIONS**

Gamma transitions are described by the following information, insofar as reliable data permit:

Energy of the gamma quantum. When internal conversion electrons form the basis for the energy determination, the energy listed in this column is always that of the corresponding gamma ray transition.

Abundances of gamma rays. This may be given as the number of unconverted gamma rays emitted per 100 disintegrations. Where an absolute abundance has not been determined, often the relative unconverted gamma ray abundances have been measured. These are tabulated as  $\gamma_1/\gamma_2/\gamma_3 \approx 2/1/5$ , for example.

Internal conversion coefficients. These are given for each gamma transition as the ratio of the number of conversion electrons emitted to the number of unconverted gamma quanta emitted, and are expressed as  $e/\gamma$ . Where conversion coefficients for individual electron shells have been determined, they are denoted as  $e_K/\gamma$ ,  $e_L/\gamma$ , etc.

Conversion coefficient ratios. Where the ratios of internal conversion coefficients in several electron shells have been measured, they are listed as K/L, L/M, K/L+M, K/L/M, L_I/L_{II}/L_{III}, etc.

Gamma rays associated with short lived isomers have been listed as entries both of the isomer and of its parent.

When an author states that gamma radiation is present, but reports no energy determination, this is indicated by the symbol "\gamma". Conversely, when attempts to find gamma radiation have failed, this has been indicated by "no \gamma".

X-rays have been mentioned only when they are the prominent radiation observed in measuring an activity, or when the observation and identification of x-rays has been crucial in the characterization of an isotope.

The symbols used to describe the methods employed for the determination of gamma ray energies or for the elucidation of decay schemes are as follows:



NUCLEAR PHYSICS CHAP, 1.2

spect Secondary electrons observed with magnetic spectrograph or spectrometer

spect conv Internal conversion electrons observed with magnetic spectrograph or spectrometer

scint spect Measurement of pulses produced by a scintillating crystal or solution

cryst spect Direct measurement by diffraction of gamma

rays with a bent crystal spectrometer

abs Absorption of the gamma rays

abs conv Absorption of internal conversion electrons

abs sec Absorption of secondary electrons

coinc Studies of coincidences or lack of coincidences

 $(\gamma-\gamma, \gamma-conv, conv-conv, \beta-\gamma, etc.)$  with coincidence counters, and, in some cases,

spectrometers

coinc abs Coincidence studies using absorber techniques

cl ch recoil Secondary electrons observed in cloud chamber

with magnetic field

pair spect Magnetic analysis of positron-electron pairs

produced by gamma rays in a thin radiator

Be-γ-n, D-γ-n, or D-γ-p reactions Measurements of neutron or proton energies from these reactions

#### DISINTEGRATION ENERGY AND SCHEME

The disintegration energy, or Q value, of a nuclear transformation is defined as the mass difference (expressed in Mev) between the initial and final systems under consideration. For radioactive decay processes, Q is equal to the sum of the particle kinetic energy, nuclear recoil energy, and the energy of any gamma rays necessary to de-excite the final nucleus to its ground state. For positron decay, the energy equivalent to  $2 \text{ m}_0 \text{c}^2$  has been included in the Q value. Where Q values have been estimated or calculated by the authors of this compilation, the special reference "HPS" is used; otherwise, reference is made to the paper from which the quoted value is taken. In most instances Q values have been obtained from decay data; where this is not the case, the method is indicated.

Energy level diagrams have been drawn in many cases; these are not necessarily complete representations of the data, but sometimes include only those features which are reasonably well established and unambiguous. Heights of the various energy levels above the ground state are indicated at the side of the drawing. Similarly, the total angular momentum (spin) and parity of the states have been included in some cases, where these quantum numbers could be inferred with some confidence from determinations of conversion coefficients, K/L ratios, ft values, etc. We have relied heavily on the interpretation of decay data by Goldhaber and Hill (18G52).

For  $\beta$ ,  $\beta$ , a, or EC decay, the percentage figures given in the decay drawings total 100% for each mode of decay, thus expressing only the relative abundances of various groups within that mode of decay. (Branching ratios between the several modes of decay are found in the "Type of Decay" column.) In the case of gamma radiation, however, the percentages given refer to the fraction of the total disintegrations of that isotope which give rise to the gamma ray and its conversion electron. This has been done because of the difficulty of assigning a gamma ray to a particular mode of decay.

Measured values for the mechanical or spin moment I of stable or long lived isotopes have also been given in this column. Except as supplemented by more recent data, the values given here are taken from the compilation by Mack (87M50).

## METHOD OF PRODUCTION AND GENETIC RELATIONSHIPS

The observed nuclear reactions (giving the target element, projectile, and outgoing particle, in order) by which the radioactive isotopes are formed, and the corresponding references are listed (p - proton, n - neutron, a - alpha particle, d - deuteron, t - triton,  $\gamma$  - gamma ray or x-ray,  $\tau$  - electron,  $\pi$  - pi meson, C - carbon ion). In cases in which the target material is not the naturally occurring element, but one enriched or depleted in a particular isotope, the isotope responsible for the reaction is indicated. No means for identifying the source or energy of the projectile is given.

In nuclear reactions with high energy projectiles, multiple particle ejection is common. Rather than attempt to state definitely the path by which the product nucleus was reached, these spallation reactions are briefly represented by the abbreviation "spall" followed by the symbol of the target element. High energy fission reactions are similarly represented by the words "spall-fission," and thermal or low energy neutron fission simply by "fission."

The criterion for listing genetic relationships has been with few exceptions that these relationships be demonstrated experimentally; for example, by chemical "milking" of daughter activities, analysis of growth-decay curves, or in the case of short lived isomers, by delayed coincidence experiments. The listing of these parent-daughter relationships gives some warning to the reader as to what he may expect in the way of radiation from a given isotope, since a sufficiently short lived daughter's radiation will usually be observed with that of the parent.

A few further abbreviations are listed below:

NNES-PPR	Volumes of the National Nuclear Energy Series,
	Plutonium Project Record, McGraw-Hill Book
	Co., Inc., New York

	Properties listed in brackets have not been observed
LJ	directly, but have been inferred from other
	experimental data

est, calc Estimated or calculated from theoretical or empirical considerations

HPS Refers to the authors of this compilation



NUCLEAR PHYSICS CHAP. 1.2

lim Experimental upper limit

emuls Photographic emulsion

A considerable fraction of the effort necessary to produce this table consisted of abstracting the literature and organizing the data over the past few years. We are greatly indebted to Marjorie Hollander for her efficacious handling of this work, and in addition for her preparation of the drawings.

It is a pleasure to acknowledge the generous help and constructive criticism which we have received from our friends and colleagues, and to thank many of the authors whose measurements are cited for their aid in evaluating data familiar to them. We are especially grateful to Dr. Gerhart Friedlander for his invaluable assistance in checking the entire draft.

We would also like to express our appreciation to Mildred Davis for the speed and accuracy with which she prepared the manuscript.

The compilation of this table was supported by the U. S. Atomic Energy Commission.

125

Inner	2	Perrent	Twend		Energy of radiation in Mey	ation in Mer		Method of renduction and
V 2	identification	abundance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
001	A recoil nuclei, conservation of mornentum (18C32); observation of n-c reaction (4F32, 87H33)		6 (18C35, 26S50)	12, 8 m (2R51); 10-30 m (26S50)	0.78 p-p ⁻ spect coinc (2R5))		0, 0, 7823 (16L51) n. 1 = 1/2 (87M50)	Be-a-n (18032); spall reactions in general; fission (92H39, 27A39, 118539); parent H ¹ (26S50, 2R50)
ጌ_		99. 9849 - 99. 9861 (diff sources) (52K51); 99. 9851 (1V38)					н³, 1 = 1/2 (87М50)	
H ₂		0.0139-QQS1 (diff sources) (52KS1); 0.0149 (1Y38)					H ² , 1 = 1 (87M50)	
£	A chem, sep isotopes, excit (6A39, 6A40a)		p (6A39, 6A40a)	12.46 y genet (12.36); 12.4 y sp act (11.51); 12.1 y genet (8N47)	0. 01795 spect (101.52b); 0. 0183 ion ch (12(49); 0. 0194 spect (26491); 0. 0198 ion ch (244491); 0. 0186 (72549, cair from 12.49); 0. 0180 abs bream satrahlung Zr, Ta (17059), 21C48, 35K3lb, 5151)	BO Y (18C46)	О _р 0. 019 ( <b>НРS</b> ) Н ³ , I = 1/2 (87М50)	D-d-p (6A39, 6A40a); D-n-y (1344); Lin-r (4040); Lin-r (4040a, 6A40a); B-n-t, N-n (2004); spall reactions (13B52)
2.He.3		1.3 x 10 ⁻⁴ (atmos), 1.7 x 10 ⁻⁵ (wells) (7A46,					на ³ , 1 = 1/2 (87MSO)	
H.		-100					He 4, I = 0 (87M50)	
**	A chem (23B36, 23B36a); cross bomb, excit, chem (27S46)		p* (23B36b)	0.823 e (9A50); 0.82 e (27H49); 0.84 e (12R49); 0.85 e (27846)	3. 50 spect (16 W52); 3. 2 abs (12R49); 5. 5 abs (27846); 5. 2 abs (23B36b, 16K48, 2P50, 35A50)	no y (16K48, 27546)	၀န် 3. so (16Ws2); ၀န် 3. ss (36Ds2)	Be-n-a (23B36, 9P37, 27S46, 16K48, 2P50); Li-y-p (25B47, 44S52a)
L T	A excit (4E49)	7.52 (17138)	IT· (4E49)	5.2 x 10 -14 s Doppler broadening (4E49)	•	-0. 48 spect (4E49)	Li ⁶ , I = 1 (87M50)	B-n-a (4E49)
۲,		92.48(171.38)					Li ⁷ , I = 3/2 (87M50)	

Li_n-v (15K36, 10P46, 28H47); Li-d-p (22C35, 5D35, IF37, 26B37, ILB7, IHS0, IYS0); spall C, N, Ne, A, Kr, Xe (13W50); Bn-v-p (13047, 44552a, 40T52); Bn-v-2p, B-v-2p (44552a)	Be-d-2p (20G31); B-p-3p, B-d-3pn (20G31); B-y-2p (46S2a); C-d-4pn, C-p-4p (20G51); C-p-4p (78H52)	Li-d-n (13R38, 14R38, 14R38a, 4742); 4747, 159H39, 39H40); B-p-a (14R38a, 17M39); B-d-an (12M46); B-b-an (12M46); Cu, Ag, Au (74M51), Al,	Be-p-d (12T49); Be-y-n (18C35, 40H49); O-y-2a (18M5), 53L52)		Be-d-p (12M46a, 19L47); Be-n-y (28H47a, 13A50, 11B50a); B-n-p (9E-d3); C-n-a (28H46)	B-y-2n, B-y-3n (44552a); B-p-t (6A50); Be-p-2n (6A50); C-p-m (6A50); C-y-p3n (4452a);	epail reactions (33B52)	
Qp 13. 99 (9V32)	A 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(51850)    (51850)   Be ⁷   18,   CC   O.479   CC   O.479   O	Q 0.078 (41C51); QQ 0.089 (12T49); QQ 0.103 (40H49); QQ 0.085 (23C50)	Be , I = 3/2 (100S51, 77H51)	О <mark>,</mark> 0.56 (нРS)	Q ⁺ 18 (calc from 6A50)	B ¹⁰ , I = 3 (87M50)	B ¹¹ , I = 3/2 (87M50)
no y (13837, 26B37); y (very weak) β-y coinc (3V5la)		0. 479 spect (4E48, 11749); 0. 478 spect (11449); 0. 485 spect (17489); coinc abs (4242); (4242); (474, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174, 1174			no y (12M47, 19L47, 28H49)			
6.: 13 (-90%), -6 (-5%), -3 (-5%) spect (1H50); c43 (-2%) B-y coinc abs (5V51a); 12.0 c1 ch (26B37); abs (3O47); two a's: total energy 3.2, 7-9 c1 ch			energy of each a in center of mass system: 0.019 spect (4IC51); 0.045 spect (12T49); 0.051 ion ch (40H49); 0.043 range emula (23C50)		0.555 spect (15F52); 0.560 spect (13A50); abs (12M46s, 12M47); 0.553 ion ch (11F49s); others (28H49, 16W49, 41H49, 11B50s)	p*: 13.7 abs (6A50); spect (44S5a)		
0. 825 e (1851);	0.168 a (20G51); 0.170 a (78H52); 0.19 a (44S52a)	52.93 d (45.84); 53.61 d (58.6.5); 54.3 d (55.847); 54.5 d (27.849)	<pre>&lt;2 x 10⁻¹⁴ photo-dia Ol6 emula Ol6 emula &lt;5 x 10⁻¹⁶ photo-dia Ol6 emula (18M52): 10⁻¹⁵ 10⁻¹⁷</pre>		2. 5 x 10 ⁶ y sp act + mass spect (12M47); 2. 9 x 10 ⁶ y yield (28H47a)	0.46 s (102B52a); 0.61 s (44S52a)		
6. 2a (111.37)	6, n (20G51, 78H52)	EC (13R38)	20		p ⁻ (12M46a)	p ⁺ , 2a (6A50)		
				100 (6N37)			18.45 - 18.98 (13748)	81. 02 - 81. 55 (13 T 48)
A excit (2235, 111.37); n-capt, sep isotope, genet (28H47)	B excit, cross bomb (20G51)	A chem, cross bomb, excit (13R38)	A observation of Be-y-n reaction (18C35)		A chem (12M46a); chem, mass spect (11P46)	A excit, cross bomb (6A50)		
ື້າ	្ន	, a	о В	Be ⁹	т 10	8 ⁸ 8	B 10	II G

]	1000	1	Topic		Reserved redistrict in May	belos la Mos		1
Z	identification	abandance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
5.B12	A excit (22C35a, LF36)		p (22C35a)	0.027 s delay coinc (3.148, 3.085); 6.022 s delay coinc (25B39)	13. 43 spect (1H50); 12. 15. 16. (15448); 12. c. c. h. (26837); -9 (-4%) coinc abs (5V51a)	-4. 5 p-y coinc abs (5V51)		B-d-p (22C35a, IF36, 30BS1); Cld-d-q (32F50b); NI5-n-q (3J68a)
or _D ,	A chem, sep isotops (28548, 28549)		p ⁺ (28549)	19.1 a (28549)	2. 2 abs (28549)	0.72 (-100%), 1.05 (-2%) scint spect (28552)	0.72 2 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	B-p-m, B ¹⁰ p-m (28548, 28549, 28523; C-y-žn (44552a)
۹,	A excit (22C34, 25H34); chem, excit (33B39)	-	p+ (22C34)	20.4 m (3094); 20.5 m (2994); 20.5 m (2994); 20.0 m (79944, 4D5))	0. 99 apact (7544a); 0. 981 apact (14741); 0. 95 cl ch (5D40)	no y. p.y coine (7846a)	Q. 0 (HPS)	Be-e-2a (12M46b); Be-He3-a (1P52); Be-He3-a (1P52); Be-Te (2625, 273, 1P36); Be-Te (2625, 233, 333); Cy-an (10846, 12P46, 2550, 5551, 22252, 44522); C-a-2a (1P77, 10654, 30852); C-a-an (5747); C-a-an (5747); C-a-an (12M46b, 6747); N-p-a (13839); N-p-a (13839); N-p-a (13839); N-q-a (10846, 6147); N-q-a (10846, 6147); N-q-a (10846, 6147); N-q-a (10846, 6147); N-q-an (21731a); O-m-a-2a (12M472); O-m-a-2a (12M473); O-m-a-2a (12M473); O-m-a-2a (12M473); O-m-a-2a (12M473); O-m-a-2a (12M473);
21 ₂ :		98.892 (limestone CO ₂ )(6N50)					C ¹² , 1 • 0 (87M50)	
<del>შ</del> ა		1.108 (1imestone CO ₂ )(6N50)					C ¹³ , 1 = 1/2 (874450)	
<b>t</b>	A chem, cross bomb, axcit (16.84)		p (1K40)	9566 y weighted 1250, 1144, 12160, and 20143, and 20143, all by sect (1143), 11744, 31144, 11744, 31144, 11744, 1144	0.155 spect (15F49, 18W50); 0.156 spect (2EC47a), 0.154 spect (2EC47a), 0.155 dan ch (10A47); 00.055 dan ch (10A47a); 00.055 dan ch (10A47a); 00.055 dan ch (10A47a); 00.045 calorimetric (12.52)	no y (16R41)	Qp 0.155 (HPB) C ¹⁴ , I = 0 (87M50) (O+) C 14 (O+) (1+) (90852, 90852e)	C-d-p (16840, 16841); C-m-r (20145); N-m-p (1684); O-m-n (19847)

C ¹⁴ -4-p (32MS0, 32MS0 <b>s</b> , 32MS2); not found by: C ¹⁴ -n-y (1Y60)	C-p-n, C ¹² -p-n (6A49, 6A50); N-y-2n (33P52)	B.e.n (4C34, 8E33, 18R37); C.dn (2CC34, 33H35, 2Y35, 26C35, 1F36); C.py (13H35, 2G35); C.ppn (11A50); N.nh. (11P37, 34H43); Nyn (10B46, 12P49, 22E52, 44S24; Oyp3n (16K47); Oyp3n (16K47); Nyn (14K42);			N-n-y (28446a, 41F52); N-d-p (1F36); O-n-p (7C37, 26543, 35B47, 18M51a); F-n-c (22L34,16F34, 3N36, 2N36, 9P37)	paul O. F. Na, Mg, Al. Si, P. S. Cl, K (27048, 18K48); Cl ⁴ -a-p (18S1); O-n-p (18S51); Ol ⁶ -y-p (18S51); F-y-2p (44S52a)
	Be C.	Q₊ 2. 26 (HPS)	N ¹⁴ , I = 1 (87M50)	N ¹⁵ , I = 1/2 (87M50)	C _p 10.3 (35B47) N ¹⁶ (2.)  Row (4-7) (2.7) (3.7) (4.7) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (1.6) (	Q _p 8.7 (6A49a)
5. 5 p-y coinc aba (32H52)		no y >0.135, <0.700 (10L47, 7846a)			γ 6.13, γ ₂ 7.10 (γ ₂ /γ ₁ 0.08) pair spect (1845ia); 6.2, 6.7 abs sec. cl ch pair (35B46)	·
6. 8 abs (32H90a)	p [±] : 16.6 abs (6A49); a: -4 total energy of three a's (6A50)	1. 24 spect (7545); 1. 25 spect (26048s); 1. 20 spect (1148); others (21L39, 53K43)			-10.3 (-20%), -4.3 (-40%), -3.8 (-40%) c1 ch (35847); 10, 3.5 abs (27546); 10 c1 ch (28146a)	f. 3.7 p-recoil coinc abs (6.649a); n. 9 (mean) O ¹⁶ recoil in on ch (6.449a); 1.0 (mean) p recoil in cl ch (36.449)
2. 4 e (32H50a)	0.0125 s delay coinc (6A49)	9. 93 m (5W394) 10. 1 m (7S45) 10. 2 m (2BC464)			7 35 e (35847); 7.5 e (28446a); 7.3 e (27546)	4.14 a (18K48); 4.15 a (32S51)
(32H50)	p. p.s. (6A50)	p* (22C34)			j6F34)	p¹, n (18K48)
			99. 635 (6NSO)	0.365 (6N50)		
C excit, sep lectopes (32H50)	A excit, sep isotopes (6.649)	22C34)			A excit (221.34, 16F34)	A chem, cross bomb (6.449a, 18K48, 27C48)
<b>5</b>	2124	ELN.	ž	S N	ڗؙؖٚ	r _z

Leosope	Class and	Percent	Type of	7H 74-11	Reegy of redistion is Mev	letion in Mov		Method of production and
	identification	spendence	Accep		Particles	Gamma-transitions	man the Alexan mandament	genetic relationships
B Ch (24	chem, excit (28549)		p ⁺ (28549)	76.5 a (28549)	1.8 abs (28549)	2. 3 coinc abs sec (28549)	Q ₆ 5.1 (28549)	N-p-n (28549); O-y-2n (44552a)
						,	2.3	
<	chem, excit (22L34a, 12M35); excit (1F36, 19K39)		p ⁺ (221.34a)	118. 0 = (2P49); 126 = (12M35, 37B39); 127 = (35D51)	1, 683 ppect (36850); 1, 68 abs (28549)	во ү (2Р50b)	¢, 2. 70 (HPS)	C-a-n (19839); N-d-n (121.144, 12M3, IF 36, 15850; N-p-Y (2D38, 19503); O-y-n (3T839, 34143, 10846, 12P32, 44592a); O-n-Za (1P37); O-n-Za (1P37);
		99. 759 (air 02) (6N50); 046/018 -4% (13T49, 1846)					O ¹⁶ , I = 0 (87M50)	
		0.037 (air O2) (6N50)					0 ¹⁷ , 1 = 5/2 (3A51)	
		0. 204 (air O2) (6N50)					o ¹⁸ , 1 = 0 (91MS1)	
<	n-capt (22M43)		p ⁻ (22M43)	29. 4 a (IIF 44a); 29. 5 a 27. 0 a (35 B 4 7 a)	4.5 (30%), 2.9 (70%) abe (35%4), 2.5 (11744); 4.1 abe (11744); -3.2 abe (34H45)	1.6 abe (UF44a)		O-n-y (12A15, 2846, 2847); F-n-p (12A15, 3N36)
<	cross bomb (19 W34, 8E34a); chem, excit (12N35, 37H35, 2D38)		p ⁺ (12N35)	70 e (12N35, 2P50c); 60 e (46H52); 66 e (46L51); 72 e (12P48); 74 e (2D38)	1. 72 spect (2P50c); 1. 7 abs (46L51); 2. 1 c1 ch (17K36)	no y (2P51, 51R51)	Q [‡] 2. 74 (HPS)	N-a-n (19W34, 8E34a, 18R37); O-d-n (12N35, 1F36, 2P50c); O-p-y (2D38); F-y-2n (10B46, 12P48, 86H32)

NUCLEAR PHIBICS							Ci
O-g-pn (274%); O(6-pn (2038); O-4a-p (1978) 2040. 2044)); O-4n (1978); F-n (1978); F-n (1978); F-pn (1948); F-p-pn (1948); N-q-a (1988); N-q-a (1988); N-q-a (1988); N-q-a (1988); N-q-a (1984); O-4 (1988); A-4 (1988); A-4 (1988); A-4 (1984); A-4 (1984); A-4 (1984); A-4 (1984); A-4 (1984);		F -d-p (22C35, IF 36, 33S50, 3J50, 13M50, 13M52c1; F n-y (3M36, 2S47, 2IK50); Na -n-a (3M36)	F-p-n (21W39, 47B514, 34552)				Ne -n-y (41F52); Ne -d-p (22W40); Ne 2d-p (14P40, 36B50s, 2P50s); Ne -n-p (12A35, 3N36, 9P37, 23B37); Mg -n-e (12A35)
Op 1. 67 (19851)	F19, I = 1/2 (87M50)	Qp 7.04 (13452b) F20 (2+) (13452b) (13452b)	Q _p 3. 20 (HPS)	Ne ²⁰ , I = 0 (87M50)	Ne ²¹ , I = 3/2 (87M50)	Ne ²² , I = 0 (87M50)	G _p 4. 21 (2P90a) BAZ+) Ne ²³ B3% 6 (3AZ+) O (1AZZ+) O (1AZZ+) O
RO Y (16K48, 47B49)		1. 631, no 2. 5 y (lim 0. 25) spect, Be-y-n reaction (13.45.2b); 1. 64, no 2. 5 y spect, y-y-coinc (47.20); 1. 64, 2. 5 (weak) spect, abs sec (1340); 2. 2 cl ch recoil (38840); y (coinc with 5. 0 p²) p-y-coinc (21.C40, 3350)	no y (21W39, 34S52)				-3 abs (2P50a)
0. 649 spect (19R5); 0. 635 spect (47B49); others (3Y38, 9K4), 20K45, 38H48)		5, 4), no - 7 p ² (lim 1,5) spect (13,52b); 5, 35 (975), 6, 7 (3,5) spect (47,20); 5, 0 spect, abs (3750); others (38,540)	2.18 spect (34552); 2. 2 c1 ch (21W39); 2. 3 abs (26549)				4, 21 (-93 %), 1.18 (-7 %) apact (36550a); 4, 3 aba (35846a, calc from 1440); 4.1 aba (14P40)
112 m (2637, 1244, 1244, 115 m (3443); 107 m (2D36)		10.7 e (32G35) 12 e (22G35)	18. 2 • (28549); 18. 5 • (34552); 20. 3 • (21W39)				40.2 a (38850a); (38844a); (34844a); 40 a (12A35, 23837)
p ⁺ (26537)		p' (22C35)	p+ (21W39)				p (14P40)
	100 (1A20)			90.92 (6N50a)	0. 257 (6N50a)	8.82 (6N50a)	
A chem (2637); chem, sep isotope, excit (2D38)		A excit (12C35, 1F36, 3N36)	A cross bomb, excit (21W39)				A excit (12A35); cbam (23B37, 9P37)
2	F 19	F 20	10 Ne 19	02. N	Ne 21	Ne 22	ž, 23

Isotope	Class and	Percent	Type of	חבות ווער	Energy of radiation in Mev	ecion in Mev		Method of production and
V 2	identification	abundance	decay	ATT-THE	Particles	Gamma-transitions	Distangration energy and scheme	genetic relationships
11 Na 20	A excit (6A50)		p*. a (6A50, 4455la)	0.385 a (102.852a); 0.23 e (4455la)	3.5 < p ⁺ < 7.3 est (4455la)		Na ²⁰ Na ²⁰ /AS.8	Ne-p-n (6A50); Na-y-3n (44551a, 44552a)
Na 21	A excit (29C40a)		p ⁺ (14P40)	22. 8 s (34552); 23 s (29C40a)	2.50 spect (34552); 2.53 spect (52851b)	no y (34552)		Ne ²⁰ -p-y (40B47); Ne-p-n (52540a); Ne-d-n (14P40); Ne-g-e (14S52); M-2-g-e (14S52);
Z 2 Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z	A chem, excit		6 ⁺ -100≴, mo EC (21G46)	2. 6 y (23149); 2. 8 y (36539)	0. 542 spect (23M50); 0. 575 spect (21046); -1. 8 (0. 06%) spect (56W22); -1. 8 (0. 004%) c. ch (25M49); others (23L37, 2039)	1. 277 spect (13A40); 1. 30 (coinc with pt) spect, p-y 1. 3 spect (2039) others (8551)	O _p 2. 84 (HPS) Na 22, 1 = 3 (87M50) Na 22, 1 = 3 (87M50)  -100%  O (HPS)	Mg*-pa (1758); 2137, 24M37); Med*-n (1773); 23137, 24M37); Med*-n (23137); Med*-n (23137); Mg*-da (23137); Mg*-da (23137); Mg*-da (23137); Mg*-da (23137); Mg*-da (23137); Pe (45852); Cu (42851a)
Na 23		100 (37836a)					Na. 23, I = 3/2 (87M50)	
2 %	A chem, excit (16F34, 1L35)		p. (1L35)	15. 06 h (39551); 115.06 h (39551); 115.06 h (39550); 115.06 h (39551); 23 w 49)	390 spect, coinc (7846b, 7847); .t. 7 spect (24139); .t. 7 (0.003 %), no 5.5 g°, spect (1573); im 4.15 g°, 0.01% spect (22G50); others (42H48)	γ ₁ 1. 3679, γ ₂ 2. 7535 spect (12H52); $Q_{\beta}$ 5. 53 (HPS) γ ₁ 1. 380, γ ₂ 2. 758 spect (7546b); $N_{\alpha}^{2}$ γ ₁ = 4 (10 1. 380, 2. 758 spect (20R49); γ ₂ (4.γ) 3. 10 ² (4.850b); γ ₃ (4.γ) 3. 10 ² (4.850b); γ ₄ (coinc with γ ₂ ) spect (8H50); γ ₄ (coinc with γ ₂ ) spect (8H50); γ ₇ (coinc with γ ₂ ) spect (3H50b); γ ₇ (coinc with γ ₂ ) spect (15H51); γ ₇ (0.955); γ ₈ (0.955); γ ₈ (0.955); γ ₉ (0.955)	(4+) No24 (4+) (4+) (4+) (4+) (4+) (4+) (4+) (4+	Na-d-p (11.25, 2V36a); Na-n-y (12.45, 2S47); Mg-d-a (35145); Mg-n-p (12.435); Mg-v-p (10.046, 42.1447, 22.52.2); Al-n-p (10.046, 30.047); Al-n-p (10.046, 30.047); Al-y-ap (10.046, 20.047); Al-y-ap (10.046, 22.52.2, 4.55.2); Sl-y-n-p (10.046); Sl-y-n-p (10.046)
2 Z	B excit (34H43a)		p. (34H3a)	58 e (35B47a); 62 e (12P4a, 10B46, 34B45a); 60 e (21R44)	3.7 (-55%), 2.7 (-45%) abs (35&47a); 3.4 abs (34844a); 3.3 abs (21844)	>0. 5 (weak) abs (35B47a)	Q. 3.7 (35B'7a)	Mg-v-p (34H44a, 10B44, 22E52); Mg-n-p (14H44a, 35B47a); Al-vbp (10B46, 12P4a, 22E52, 42B52)

:	-	_		_	_		-	
C 3 3 7 2 1	12 Mg ²³ A excit, cross bomb (21W39)		p* (21W39)	11. 9 a (34H43); 12. 3 a (52B5la); 11. 6 a (21W39)	2. 99 scint spect (52B5la); 2. 8 cl ch (2lW39)	no y (21W39)		Na-p-n (21W39, 2D40); Mg-y-n (34H42, 34H43, 10B46, 25B47, 27M49, 22E52)
ž,		78. 60 (24W48)					Mg ²⁴ , I = 0 (87M50)	
Ng 25		10.11 (24W48)					Mg ²⁵ , I = 5/2 (87M50, 3A5la)	
Mg 26		II. 29 (24W48)					Mg ²⁶ , I = 0 (87M50)	
Mg 27	A chem, excit (12A35, 35H35)		p ⁻ (35H35)	9. 45 m (3852); 9. 6 m (10E43); 10. 0 m (32C39); 10. 2 m(35H35)	1.80 (80%), 0.9 (20%) spect (43848); 1.8 cl & (1084) 32C39); 1.7 ab (28848); -1.8 (coinc with y) \$-y coinc (35847a)	γ ₁ I. 01, γ ₂ 0. 84 (γ ₁ coinc with γ ₂ ) spect, γ-γ coinc (43B48); I. 02, 0. 84, 0. 64 spect (4181); I. 05 cl ch recoil (10E43)	G _p 2. 64 (43B48) Mg ²⁷ And 185	Mg-d-p (15H35); Mg-n-y (12A35, 2847); Al-n-p (12A35, 16F34, 74M52)
Mg 28	A chem, genet (371.53)		p (37 <u>L53)</u>	21. 2 b (37 <u>1.53)</u>	0.3-0.4 abe (37L53)	<0.1 abs (371.53)	(43848)	spall Cl, parent Al ²⁸ (37 <u>1.53)</u>
13A1 ²⁴	A excit, decay charac (102B52)		<pre>p⁺ or EC, a (p?) (102B52a)</pre>	2.3 • (102B52)				Mg-p-a (102B52)
A1 ²⁵	B excit, sep isotopes (39B48)		p ⁺ (39B48)	7.3 . (39.848)				Mg ²⁵ -p-n (39B48)
A126	A excit (17534); cross bomb (34H3, 39B48)	100 (1850)	p ⁺ (17 <u>F</u> 34)	6.5 e (30K51); 6.3 e (39B48); 7.0 e (21W39, 14A48, 12P48; 7.2 e (25W48)	2.8 abs (14448); 3.0 cl ch (21W39); 3.4 abs (35B46a, calc from 17F34)		A1 ²⁷ , 1 = 5/2 (87M50)	Na-a-n (17534, 24M37); Mg-p-n (21W39); Mg-p-n (39848); Mg-p-y (21C39, 16746); Al-y-n (34H41, 34H42, 34H43, 10846, 25847, 12P48, 22E52)
A1 ²⁸	A chem, excit (4C34, 4C34b, 16F34); chem, crose bomb (12A35)		p* (12M35a)	2. 27 m (106.85.2b); 2. 07 (40548); 2. 30 m (10E43)	2. 865 spect (29M52); 2. 5 (coinc with v) coinc abs (35B47a); 3. 01 spect (43B48); no 4. 6 F (29M51)	1. 782 spect (29M52); 1. 80 spect (43B48); 1. 80 bbs sec (15B47a); 1. 82 spect (414)	A 128	Mg-a-p (8E36, 18R37); Al-a-p (12M35a, 29M32); Al-a-y (12M35, 25M32); 50H3, 29M32); Si-a-p (12A35, 35B47a); Si-y-p (10B46, 42H47); P-n-a (12A35) daughter Mg ²⁸ (37L58)
							(10E43, 29M52)	

Percent	Type of Half-life	91.	Bartiles	lation in Mev	Disinsegration energy and scheme	Method of production and generic relationships
'a	6.7 m (3.28.39) 6.56 m (6.7 m (3.28.39)	(41549): 2 32B39)	%) (both coinc bs (41549): 139)	1. 2 (-80%) (-20%)	Op 3.8 (41549) A129 70-60% (41549)	Mg-a-p (8236, 32839, 14H39, 41549); Al-a-b (112551); Si-n-p (21P43); Si-y-p (10846, 42H47, 12P48); P-y-2p (10846, 12P48)
<u>*</u>	6* (30M40) 4.9 e(12E4), 29C40a); 4.5 e (25W48); 5.4 e(52B5la)		3.48 scint spect (\$2B\$la); 3.5 cl ch (33B40); 3.7 cl ch (30M40)			Mg-a-n (12E41); Al-p-n (22K39, 30M40, 29C40a, 33E40, 76C51); Si-y-n (34H44, 25E47, 25W48)
		•			Si ²⁸ , I = 0 (87M50)	
					31 ²⁹ , I = 1/2 (87M50)	
_					Si ³⁰ , I = 0 (87M50)	
<u>'a</u>	p (12N35e) 2. 62 b (33C39, 55 W5); 2. 65 b (2005a); 2. 6 b (461.50); 2. 8 b (12N37, 15.40); 15.40)	~ ã	1. 471 spect (29M52a); 1. 486 spect (47W52); 1. 48 abs (55W51)	0.17, 0.52, -1 (weak) (?) abe (80C52); no y (12N37)	Q° 1.47 (29M52a)	84-d-p (12N35a, 12N37, 17K36); 81-n-v (12A35, 2547); 81-H63-2p (1P52); P-n-p (12A35, 1P37); S-n-a (42836, 33C38); spall Fe (45R52)
<u>*                                    </u>	p ⁺ (21W41) 4.57 e (30R52 4.6 e (21W41)	30R52);	4.57 e (30852); 3.6 cl ch (21W41) 4.6 s (21W41)	1.28 (2.5%), 2.42 (0.5%), scint spect, y-y coinc (30R52)		Si-p-n (21W41); Si-d-n (14D48); P-y-2n (?) (10B46)
<u>*a</u>	p ⁺ (4C34) 2.55 m(	33C38); 31C38); 31C38)	2.55 m(18837); 3.5 spect (24M41); 2.18 m(33C38) 3.4 sbe (35B46s, calc from 17F34); 3.0 cl ch (33B40)			Ai-a-n (17F34, 4C34, 18R37); Si-p-n, 18B59, 18B40); Si-Ha ³ -p (6A39, 1P52); P-n-2n (1P37); P-y-n (1R39, 10B46, 12P48); S-d-a (4C354); Cl-y-an (85HS2)
					P ³¹ , I = 1/2 (87M50)	

81-d v (11283); 81-n-p (10738); 91-h-p (10738); 9-d-p (12837); 9-n-v (2847); 8-n-p (12837); 8-n-p (12838); Gl-n-n (12838); Gl-v-n-n (12838); Gl-v-n-n (12838);	epail Fe (45R52), Cu (32M46, 42B5la) S-n-p (44B31, 13J52b, 58W52); S-v-p (44B51, 13J52b); Cl-v-a, Cl. v-2p (44B51, 13J52b)	S-n-p (10C40a, 6245, 35B46b); Cl.n.a. (6245, 34H45, 35B46b)	Si-e-n (19K40, 12E41, 12E41a); P-p-n (21W41); S-y-n (34H41, 34H42, 34H43, 25B47, 27M49)	
Q, 1. 702 (HPS) P32 P32 OH	(HPS) Q _p 0. 27 (44851) P33 (3/2+)	(4455i, 13J32b)	S ³² , I = 0 (87M50)	8 ³³ , I = 5/2 (87M50) 8 ³⁴ , I = 0 (87M50)
во ү (17К36, 7846b)	BO Y (4455), 58W52)			
44.30 d (12C39., 1.701 spect (average of 44851, 49B50); 29M52a,1313Zb, 8H3b, 16A50, 14.35 d (23K48) 18W50a,10L49,7846b); 14.07 d (31M40); E (average) 0.70 ion ch (77C52) 14.60 d (38S51)	25.4 d (58W52); 0.27 spect (44551); 24.8 d (13J52b); 0.26 spect (13J52b); 25. d (44851) 0.25 abs (58W52)	[2.4 a (35B46b); 5.1 (75K), 3.2 (25K) abs (35B46b)	3.85 cl ch (21W41); 3.87 cl ch (12E4la); 4.1 scim spect (52B5la)	
45.50 (12C38, 1, 45.550); 14. 35 d (23K48); 14. 60 d (3853);	25. 4 d (58W52); 0 24. 8 d (13352b); 0 23. d (4483l)	12. 4 (195B46b); 5 12. 7 e (10C40a)	3.18 e (12E41); 3.2 e (21W41, 52B51a); 2.6 e (27M49)	
p [*] (211.37)	6' (13.35.b.) 44531)	6 ⁻ (6245)	p ⁺ (21W41)	
			95.018 (meteoritic aufur) (7.0450a); torrestrial;	\$12/\$34 variation \$5,6 (41750) 0.750 (metooritic sulfur) (76,650s) 4.215 (metooritic sulfur) (76,650s)
p ³² A chem, n-capt (12A35)	A chem, cross bomb (44851)	B excit (10C40a); chem, excit, cross bomb (35B46b)	A excit, cross bomb (21W4), 12E41)	
7	£	<u>-</u>	16 ⁸³¹	

Cl-d-p (31G4), 10O47, 2847); Cl-d-p (31G4)		Cl-d-p (17K36, 2V36a); Cl-n-y (12K35, 14K40, 19A4), Z547); Cl37-n-y (14K40); K-n-a (47H37); spall Fe (45K52), Co (29W52), Cu (32K446, 42B5a); spall-fracion Cu (42B51)	A-y-p (49H49, 49H50); ppail Fe (45R52), Co (29W52), Cu (32M44a, 42B5la), As (48H49)	S-a-n (19K40, 45548); C1-p-n (21W41)	S-a-n (28W41, 28W44); Cl-d-Zn (28W41, 28W44); Cl-p-n (28W41, 28W44, 47B51a); K-d-a (28W41, 28W44); Ca-n-a (28W41, 28W44);		A-n-y (32K52); K-n-p (48B50, 8Z52)
Qp 0. 714 (16 W 49b, 18 F 9.2) C136, 1 = 2 (87 M 50, 27 J 51) (12) C136 (12) C136 (10-4) (16 W 4.9 9.0)	C137, I = 3/2 (87M50)	G ₂ 4. 81 (H ² S) (E ² ) C ₁ 38 (E ² ) C ₁ 38 S ₂ 38 G ² S ₂ 15	(10L50, 15H46) Op. 3.3 (49H50) C139 750 1.70	(49H50) Q ⁺ 5.4 (HP5) A ³⁶ , I = 0 (87M50)	$Q_{EC}$ -0.8 continuous $\gamma$ spectrum (38A52); $Q_{EC}$ 0.816 p-n threshold (51R50)		о <mark>,</mark> 0.57 (нРS)
no y (16W49m)		γ ₁ 2.15, γ ₂ 1.60 (γ ₁ /γ ₂ = 1.3) spect (15H46); γ ₁ 2.19, γ ₂ 1.64 (γ ₁ coinc with γ ₂ ) spect, coinc (414); spect, coinc (414); z.15, 1.65 spect (21C40a); no 3.75 γ (lim 0.03%) Be-γ-n reaction (33M49)	1.35, 0.35 (coinc with 1.65 pr) coinc abs sec (49H50)		no y, Cl K _a -x (28W44)		no y > 0. 3 (lim 0. 1%) (48B50)
0, 714 apect (15F52); 0, 66 abs (10047); 0, 64 abs (31G41); others (16W49b, 16W51)		4.81 (53%), 2.77 (16%), 1.11 (31%) apect (10L50); 5.0, 2.8, 1.1 apect (27W39); spect, coinc abs (27W41); 5.2 (53%), 2.70 (11%), 1.19 (36%) spect (15H46)	55.5 m (49H49); 1.65 (93%), 2.96 (7%) abs (49H50) 1 h (32M48a, 48H49)	4.38 cl ch (21W41); 4.41 cl ch (12E41a)			0.565 spect (48B50)
4.4 x 10 ⁵ y sp act 8 p act 1.6 x 105 y sp 2.0 x 105 y yield (2,8147b); 2.10 y yield (10C47)		37, 29 m (31C50); 37, 5 m (47H37, 21C40a); 37, 0 m (2Y36a, 5S45); 38, 5 m (15H46)	55.5 m (49149); -1 h (32M48a, 48149)	1.88 s (12E41a); 1.84 s (45S48)	35.0 d (56M52);		-265 y sp act (8Z52)
(4.14); no p ⁺ (lim 0.01%) (16.W49a); (lim 0.03%) (14.149)		p (17K36)	β ⁻ (49H49)	β ⁺ (12E41a, 21W41)	EC (28W44, 346R52); EC (L/K 0.087) (17P49)		p (48B50)
	24. 6 (6N36)			0.337 (6NSO)		0.063 (6N50)	
A chem, n-capt (31G4)		A chem, n-capt (12A35); chem, sep isotopes (14K40)	chem (32M48a); chem, excit (49H49)	A excit (21 W41, 19K40)	A chem, cross bomb (28W41)		B chem, excit (8252)
98.10	C137	C138	C139	18 A 36	A37	*,	

Isomosi	Class and	Percent	Type of	20.20	Beergy of rad	Reserry of radiation in Mev		Method of production and
V Z	identification	abundance	decay	Helf-tire	Particles	Gamma-transitions	Disignagration energy and scheme	genetic relationships
18A40		99. 600 (6N50)					A ⁴⁰ , I = 0 (87M50)	
₹,	A chem, excit (26536)		p_ (26836)	109 m (15 B46c); 110 m (26S36)	109 m (18B46c); 1. 245 (-100 %) spect (16B50); 110 m (26836)   1.18 (99. 3 %), 2. 5 (0. 7 %) abe, coinc abs (15B46c); others (26836, 17K36)	1. 37 c1 ch recoil (23836); 1. 3 (coinc with 1. 2 p') p·y coinc, abs sec (35846c); y (s/y -0) spect coav (36849)	Qp 2.5 (35B46c) (772-) A41 (772-) A41 (772-) K4m (772-) K4m	A-d-p (26336, 16849, 16850); A-n-y (26336); K-n-p (47H37, 13846c); parent K ^{dim} (4E52)
₹<	A chem, genet (32K52)		p ⁻ (32K52)	P3. 5 y (32K52)			(35 <b>B</b> 46c, 4E52)	A-n-y (sec order reaction) (32%52); parent K ⁴² (32%52)
19 ^K 37	C excit (27L48) A chem, cross bomb (47H37, 14H37)		p* (52851a)	1. 3 a (27L48); 1. 2 a (52B51a) 7. 7 m (47H37, 18R37, 56G51); 7. 5 m (24R47); 7. 6 m (12P48)	1.3 a (27L48); 1.2 a (52B5la) 1.2 a (52B5la) 1.2 a (52B5la) 1.3 m (47H37, 2.8 apect (56G5l); 18R37, 56G5l); 2.5 abs (24R47); 7.5 m (24R47); others (18R37) 7.6 m (12P48)	2.16 scint spect (1875)); -2.1 abs sec (24R47)	••• Cl 30	K-y-2n (27L48, 52B5la) Cl-a-n (47H37, 18R37, 14H37, 24R47); K-p-n (1971, 50G51); K-y-p (14H42, 34H43, 12P48, Ca-d-n (47H37)
ж 39		93.08 (6N50); K39/K41 variations (8LC43)					K ³⁹ , I = 3/2 (87M50)	

11705, 54C06)	(4E52)			A-a-pn (11049); K-d-p (47H37); K-a-y (12A35, 47H37, 2547); Ca-n-p (71H35, 47H37); Sc-n-a (71H36, 47H37); spall Co (19W\$2); Cu (\$7G51); daughter A ⁴ Z (32K\$2)		7, 30W40)	, 25W48,	
natural source (1705, 54C06)	daughter A ⁴¹ (			A-a-pn (11049); K-d-p (47H37); Ca-n-p (71H35, Sc-n-a (71H36, spall Co (79W5)	A-a-p (11C49)	Ca-n-p (30W37, 30W40)	Ca-y-n (34H43, 25W48, 27M49)	
Q ₀ 1.33 (HPS) Q _{EC} 1.63 (26850, HPS) K ⁴⁰ 1.4 (87M50) K ⁴⁰ 1.4 (87M50)  (46	(72-) K 41m	(3/2+) + 0 (4E52, 18G52)	K ⁴¹ , I = 3/2 (87M50)	Qp 3.6 (HPS) (2) (2) (2) (2) (2) (3)	(HPS)		:	Ca 40, I = 0 (871450)
1. 46 acint apact (IIB50b, 25G3la); 1. 46 acint apact (18180); 1. 47 cint apact (18180); 1. 54 (with EC) ab, coinc (42H6); 1. 55 abs (25G4); 1. 55 abs (25G4	-1. 3 acint apect (4E52)			. 51 apect (7547c); 50 apect (6547); 5 (17%) acint apect (351.52a)	-0.4 abs (11C49)			
. 33 spect (18752); . 1. 6 spect (18.55a); . 1. 6 secum spect (18.50c); . 1. 5 spect (18.50c); . 1. 2 secim spect (25.551); . 2 8 scim spect (25.551)				3.58 (75%), 2.04 (25%) spect (7587c); 3.60.1.9 spect (6847); 3.50.1.9 spect (6847); 3.5 (-70%) (not coinc with y), 3.1.8 (-30%) abs., coinc (35847s)	0.81, 0.24 spect, abs (11049)		5.1 scint spect (52B5la)	
p. ep act EC): EC): 2x 109 y (47840; (47840; (47840; (47880); 24850); 24850); (17051,17051ab, 24850); (17051,17051ab, 24850); (17051,17051ab, 24850); (17051,17051ab, 24850); (17051,17051ab, 242 x 109 y 244 x 109 y 245 x 109 y 247 x 108 x 109 y 24850); (17051,17051ab, 24	6.7 x 10 ⁻⁹ s delay coinc (4E52)			2. 44 h (7847c); 12. 5 h (38551, 351.54 h (47H37)	22. 4 h (11049)	18 m (30W37)	1.06 s (34H43)	
11.4 (13.0); 14.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6 (14.5); 17.6	IT (4E52)			f (17K36)	p* (11049)	8 (30W37)	β ⁺ (34H43)	
0. 0119 (6Ns)			6.91 (6N50)					96.97 (6N38a)
A chem (1705, 54C06); Chem, mass spect (15537)	A genet (4E52)			A chem, n-capt (12A35); chem, cross bomb (71H35, 71H36)	B chem, excit (UO49)	E chem, excit (30W37)	B excit (34H43, 27M49)	
ž ž	K ⁴ la		¥,	4×	£ ⁴	‡ <u> </u>		ş

laceope	Class and	Percent	Type of	70 70	Energy of radiation in May	listion in Mev	i	Method of production and
V Z	identification	abandance	decay	am. mu	Particles	Gamma-transitions	Designation operate and scheme	genetic relationships
20°Ca 41	B chem, n-capt		EC (60851)	1.1 × 10 ⁵ y yield (60B52a)		K Kg -x (60B51)		Ca-n-y (49S51, 60B51)
	(60B51)							
Ca 42		0. 64 (6N38a)						
ۍ څ		0.145 (6N38a)						
<b>\$</b>		2. 06 (6N38a)						
***	A chem, excit, cross bomb (30W40)		p (30W40)	152 d (36M47); 180 d (30W40)	0. 254 spect (23M50a); 0. 255 scint spect (24K50); 0. 260 bas (25948); 0. 26 abs (50550); E (average) 0. 075 ion ch (77C52)	no y (29548, 37M49, 25K46); others (52M51)	Q _p 0. 254 (HPS) CQ ⁴⁵ CQ ⁴⁵ (77.2-)	Ca-d-p (30W40); Ca-n-y (30W40, 2547); Sc-n-p (30W40, 25446); Sc-d-2p (51H48); Ti-n-c (3C46, 53H48); spall Fe (45R2), Cu (42B51a); spall-fission Bi (11G49)
<b>9</b>		0.0033 (6N384)					(HPS)	
Ç 0	A (36M47); chem, genet (42B5la)		p_ (36M47)	4.8 d (42B5la); 5.8 d (36M47)	1. 2 abs (42B5la); 1. 1 abs (36M47)	1. 3 abs (36M47)		Ca-d-p (36M47); spail Fe (45R52), Cu (42B5la); parent Sc ⁴⁷ (42B5la)
<b>\$</b>		0.185 (6N38a)		tp. >2 x 10 ¹⁶ y sp act (28J52)				
	A chem, n-capt, sep isotopes (38M50)		p^ (38M50)		-2. 7 abs (38M50)	hard (38M50)		Ca ⁴⁸ -n-y, Ca-p-y (38M50)
	A excit (12E41)		p ⁺ (12.E41a)	0.873 s (98M52); 0.87 s (12E41)	4. 94 cl ch (12E41)			Ca-d-n (12E41, 12E41a); Ca-p-y (39T52)
	A chem, excit (17F35)		p ⁺ (17£35)	3. 92 h (53H45); 4 h (30W40m)	1.18 (72%), 0.77 (28%) spect (93H52); 1.12 abs, spect (53H45); 1.4 cl ch (30W37a); abs (30W40a)	0.375, no bigher y (lim 15%) spect (93H52); 1. 65 abe (53H65); 1. 0 abe (30W40a)		Ca-a-p (17F35, 30W40a); Ca-d-n (30W37a, 53H45); Ca-p-n (2D3a, 53H45); Ca (42B31a) Cu (42B31a)
<b>2</b>	A chem, excit cross bomb (30W37a)		IT (30W40a)	2. 44 d (53H45); 2. 4 d (49B50); 2. 2 d (30W40a)		0. 271 spect, spect conv (49B50); 0. 269 spect conv (51842); 0. 26 spect conv (51H41); 0. 28 abs conv (51H45)	(4,7+) Sc ⁴⁴ m ₀₂₇ (2,3+) Sc ⁴⁴ O EC, 6+	K ⁴¹ -c-n (49B50); K-c-n (20W40a, 53H43); Ca-d-n (30W31a, 53H42,53H43); Ca-p-n (2D38); Ti-d-a (30W37b); Ti-d-a (45B52); Co (29W52), Ca (42B5ka)
<b>*</b>	A chem, excit (10C38)		653 H45)	3. 92 h (53H45); 1 4. 0 h (60B50); 4. 1 h (30W40n, 1 51B42)	. 463 spect (49B50); . 45 spect (51B42); . 5 sbs (39C56, 30W40s)	1. 16 spect spect comv (49B50); 1. 18 coinc abs sec (39C50)	Q ⁺ 3.64 (18G52) (1,2+) (0+) (18G62)	K ⁴¹ -a-a (49B50); K-a-n (30W40a, 53H43); Ga-d-n (30W3'a, 51542, 53H43); Sc-n-b-n (31B3a, 53H43); Sc-n-b-n (31B3a, 53H43); Sc-y-n (37B39); Ti-d-a (53H44); spall Co (27W52), Cu(42B31a);

	Sc-n-y (18G48, 38MS1)	2.01 Ga-q-p (30W40a); Sc-d-p (30W37c, 30W39; Sc-n-y (71H35, 30W37c, 2547); Ti-n-p (30W37b; 63H48); Ti-n-p (30W37b; 63H48); spall Fe (45R52), Cu (42B5ia)	Ca-a-p (53145a); Ca-d-n (53145a); Ca-p-y (53145a); Ti-y-p (22255); Ti-n-p (63148); Ti ⁴ 9-d-a (26K49); spall F (45R52), Cu (42B5la); daughter Ca ⁴⁷ (42B5la);	Ca.p.n (53H43); Ca.d.n. (51542, 26M42, 53H43. 26m43a); Tin.p. (30W37b, IP37, 30W40a, 2.6M43a); Tifo.d.a. (26K49); Tid.e. (35H44); V.n.a. (30W37b, IP37, 30W40a); spall Fe (45R52)	Ca-d-n (30W40a); Ti-n-p (30W40a); Ti-y-p (42H47, 22E52)	Ca-a-n (45548)  Ca-a-n (21A41); Sc-p-n (21A41, 11750, 27K50); Sc-d-Zn (21A41, 11750; Tin-Zn (21A41); Tin-Zn (21A41); Tin-Zn (21A41); Tin-Zn (21A41); Tin-Zn (21A41); Tin-Zn (21A41); Tin-Zn (42181); Tin-Zn (42181); Tin-Zn (42181);
Sc45 1 = 7/2 (87M50)	17+) Sc46m 0.142	(2+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (		Qp 3.87 (74551a)  Sc 48  Sc 48  -3.3  (68H52)		Q ⁺ 2.04 (HPS) T145 0.45 (HT50)
	0. 142 (K/L -10) spect conv (82B52); 0.135 scint spect (38M5))	(200-48); (200-48); (	y (26K49)	Y ₁ 1.33, Y ₂ 0.98, Y ₃ -1.0 scint apact, y-y coinc (68H92); 1.32, 0.95, no. 2.3 y (lim 0.1%) scint spect (69H82); 1.33, 0.96 apact (6P46); 1.35 apact (6M44, 26M43a); 1.35 abs (53H45a)	no y (30 <b>W</b> 40m)	0.45 (weak), (no 0.8 y) spect (HT50); 0.80 spect, abs (27K50)
_		0. 36 spect (22F47, 40M47, 20P48); 0. 36 sab (3259); 0. 34 sab (14N90); 1. 2 (-0.5 %) spect (19P31); 10. 2 (-0.5 %) spect (19P31); 10. 1. 5 % (11m 0.05 %) spect 10. 1. 5 % (11m 0.06 %) spect 10. 1. 5 (-2. %) spect (20P48); sbe (14N50)	0. 61 abs (26K49)	). 64 spect (51942); ). 57 abs (53H45s, 26K49)	1.8 abs (30W40a)	1. 02 (296%), 0. 57 (44%) spect (11750); 1. 00 spect (27K50); 1. 2 cl ch (21A41)
	19. 5 • (38M51)	84 d (19P51)	3. 43 d (26K49)	26K49)	•	0.6 e (45548) 3.09 h (27850); 3.08 h (21A41); 3.08 h (21A41)
	IT (18048)	p', no EC (40447); (40447); (30W39); no p' (lim no p' (lim (41M51)	p ⁻ (53H45a)	p ⁻ (30W37b)	p_ (30W40a)	(27K\$0)
100 (281.50)						
	A n-capt, resonance neutron activa- tion (18G48)	A n-capt, chem (71136); chem, excit, cress bemb (30W37c)	A chem, cress bomb (53H45a); sep isotopes (26K49)	A chem, excit (30W37b); asp isotopes (26K49)	ø	A chem. cross bomb. excit (21A4)
\$	, \$4 y	\$c.	Sc 47	& + os	\$ \$	T1145

	Pag. 2017		Tone of		Basery of rad	Reserv of radiation in Mev		Marked of sendoning
V Z	identification	abundance	decay	Half-life	Particles	Gemme-transitions	Disintegration energy and athems	genetic relacionahips
22 ^{T146}		7. 95 (6N38a)						
T147		7.75 (6N38a)						
Ti 48		73. 45 (6N38a)						
T149		5. 51 (6N38a)					Ti ⁴⁹ , I = 7/2 (?) (29.352)	
Ti 50		5. 34 (6N38a)						
Ti ⁵¹	B n-capt (2547)		p (2547)	5.82 m (3552); 5.75 m (2552); 6 m (24549a, 38M50, 2847)	1. 7. 1. 35 (coinc with 0. 32 y) scint   0. 320, 0. 910 (weak) scint spect (38M52); 2. 2 (-305), 1. 9 (-70%) abs, spect (0. 32 scint spect (38M51s, 60K52); 1. 6 abs (24949s)	0.320, 0.910 (weak) scint spect (ZBS2); 0.32 scint spect (38MSla, 60KS2)	see Cr 51	Ti-n-y (2547, 38M50)
23V ⁴⁶	E excit (98M52)		p ⁺ (98M52)	0.40 . (98M52)	>6.0 scint spect (98M52)			Ti-p-n (98M52)
<b>6</b>	A chem, excit, cross bomb (12042); chem, sep isotope (26K49)		p ⁺ (30W37b)	3 m (26K49, 12O42, 30W37b)	1.7 abs (26K49); 2.0 abs (35B46s, calc from 30W37b); -1.9 abs (12O42, 30W37b)	y (26K49)		Ti-d-n (30W37b, 12O42); Ti-p-n (12O 42) Ti ⁴ f-p-n (26K49) spall Fe (45R52)
**	cross bomb (10W37c, 30W37b)		6 58%, EC 46; 42% (21G46); 6 2% (30W39, 53H44)	16. 0 d (30W3Tb)	16. 0 d (30W 37b.) 0.69 (-95 K)0.8 (-5 K) spect (43R 25.). 0.72 spect (6746); 0.72 spect (6746); 0.6 abs (33H44). 1. 0 cl ch (30W 37b.)	γ ₁ 0.99, γ ₂ 1.32 (γ ₂ coinc with γ ₁ ). γ ₃ 2.29 (γ ₃ /γ ₂ = 0.017) scint spect (69M52); γ ₁ 0.99, γ ₂ 1.32, γ ₃ 2.22 scint spect, β ₂ γ ₃ γ ₄ γ ₂ coinc with γ ₁ , both coinc with β ⁴ ) spect, β ₂ γ ₃ γ ₄ (2.20 scint), coinc (6P46); γ ₁ (γ ₂ ≥ 10 ⁻⁴ ), γ ₂ (s/γ 8 × 10 ⁻⁵ ), spect conv (7252); γ ₃ 2.22 (-28), no 2.3 γ (11m 0.5%) scint spect (18752); γ ₁ (0.99, γ ₂ 1.32 spect conv (20R49); γ ₁ (coinc with γ ₂ ) γγγ coinc (34352)	(4) (43R52) (13,44) (40 (13,44) (22) (18) (19) (19) (19) (19) (19) (19) (19) (19	Sc-a-n (30W37c); T1-d-n (30W37c); C1-d-n (20W37b, 1872); Cr-d-a (30W37b, 6P46); spail Fe (45K52), Cu (32M48, 42B51a); daughter Cr ⁴⁸ (45R52)
<b>\$</b> ,	D chem (30W39, 29T40); excit (43H49, est from 10C49)		EC (30W39)	635 d (10C49) -600 d (30W39)		0 . 119, 0. 081 spect conv (10C49)		Ti-d-n (30W39); V-n-2n (?) (10C49)
05^		0. 24 (43H49, 28L49)					Q 1.18, Q 2.39 (23352); V ⁵⁰ , I = 6 (56K52)	

NUC	LEAR PRI	BICS	'									CHAP. 1
	V-n-y (12A35, 30W37b, 1937, 2847, 9049, 28R50, 50H51); V-d-p (30W37b); Cr-n-p (30W37b, 1937); Cr-y-p (42H47); Cr-y-d-a, (15N50);	Mn-n-a (12A35, 30W37b, 1P37) V-n-y (25R50)	V-n (10C49)	Cr ⁵⁴ -y-p (88H52)	spall Fe, parent V ⁴⁸ (45R52)	Ti-a-n (12042); Gr-n-2n (12042); Gr-y-1 (34444, 12749); epail Fe (45R52), Co (29W52).	Cu (32M48, 42B5la, 74M52), As (48H50)	Ti-a-n (30W40b); V-p-n (16B45a); Cr-d-y 130W40b, 22A40); Cr-n-y (30W40b, 25A7); Cr-n-A (45R50); apall F (45R50); daughter Mn ⁵¹ (50B50)				Cr -n (18D40, 22A40, 2847); Cr -d (22A40)
V ⁵¹ , 1 = 7/2 (87M50, 97B51c)								, \$	(36M5io, i4552 a, 35L52)	Cr ⁵³ , I = 3/2 (97B51)		
	1. 5 abs (42M47); 1. 3 abs (28048); -1. 5 y with V ⁵² (25R50)	1. 5 abs (42M47)				0, 18, 1, 55 abs (12042)		0.330 (-3%, eg/y -0.02), spect spect core (16B45a); 0.22 (8%, e/y very small) acint spect, x-y coinc (351.52); 0.32 spect, spect core (18K49); 0.32 spect, core (43M46); 0.32 spect core (43M46); others (52M5), 28K49, 13A50b)				
	2.1 abs (3D40a); 2.6 cl ch (4Y42); conv: 0.25, f' with V52, abs, f'-y, f-conv coinc (25R50)	2. 7 cl ch (4¥42)		-0.6 abe (88HS2)		41.9 m (12042); 45 m (34H44)						
	3.76 m (3852); 3.74 m (42M47); 3.75 m (12A35)	2. 6 m (25R50)	16 h (10C49)	23 h (88HS2)	-23 h (45R52)	41. 9 m (12042); 45 m (34H44)		27. 8 d (351.52); 26. 5 d (30W40b.)				-2 h (18D40)
	p" (12A35); IT (25R50)	p (25R50)		р (вень2)	EC (45R52)	p+ (12042)		EC (16B45s, 30W40b); no p+ (16B45s, 28K49, 35L52)				
99. 76 (43H49. 28L49)							4. 31 (24W48)		83. 76 (24W48)	9. 55 (24W48)	2. 38 (24W48)	
	A chem, n-capt (12A35); cross bomb, excit (30W37b)	F n-capt (25R50)	F V ⁵² : (10C49); V ^{50m} : (43H49)	B chem, sep isotopes, excit (88H52)	B chem, genet (45R52)	A chem, excit, cross bomb (12042)		A chem, excit, cross bomb (100 40b); chem, genet (50B50)				G not found: sep inctopes, excit, cross bomb (15N50); cbem, excit (32M50)
18,4	v 52(m?)	۸۶۶	v52,50m	۸۶۶	24Cr 48	ې 2	Cr.50	ې د	Cr 52	Cr. 53	<b>2</b> 2	S. C

	100		7		Passar of radiction in More	arion in Mar		
Z	identification	abandance	decay	Half-life	Partocles	Gemma-transitions	Disintegration energy and scheme	genetic relationships
49. 25 Mn 50	E excit (39T52, 98M52)		p* (98M52)	0. 28 a (98M52); -0.5 a (39T52)	>6.3 scint spect (98M52)			Gr-p-2n (39T52); Gr-p-n (98M52)
Kn 51	A chem, cross bomb (12L37, 12L38); chem, genet (50B50)		p ⁺ (121.37)	44.3 m (50B50); 46 m (12L38)	2. 4 abs (135346a, calc from 121.18); 2. 0 abs (121.38)			Cr-d-n (121.38, 50B50); Cr-p-y (2D18, 5D39); Fe-y-p2n (42552); epail Fe (45R52); Cu (32M48, 42B5la, 44M52); parent Cr ⁵¹ (50B50)
Mn ^{52m}	A chem (19D37); chem, excit, cross bomb (12L37, 12L38)		p ⁺ 99+ <b>K</b> . IT (?) -0.05 <b>K</b> (1047)	21. 3 m (40H40; 21 m (12L38, 19D37)	2. 66 spect (1047); 2. 2 cl ch (40H40)	1. 46 (coinc with \$\rightarrow\$) spect, \$\rho_*\psi\$ coinc (1047); 0. 392 (0. 05 \rangle ) (with II ?) spect conv (1047)	Qp 5.1 (1047)	Cr-p-n (40H40); Fe-d-a (19D37, 12L38); Fe-y-pn (22E52, 42552); daughter Fe ⁵² (32M48)
Mn 52	A chem, excit, cross bomb (12L37, 12L38)		ес 65%, р* 35% (21G46)	6. 0 d (29H50); 6. 2 d (84H51); 6. 5 d (12L38); 6 d (32M48)	0.58 spect (6P46); 0.75 abs (19748); 0.77 cl ch (40H40)	γ ₁ 0.73, γ ₂ 0.94, γ ₃ 1.46 (γ ₁ coinc with γ ₂ and γ ₁ , all coinc with β ² ) spect, β-γ coinc (6P46)	Qp 4.7 (6P46) Mn52m 0.39	Cr-p-n (40H40); Cr-d-n (6P46); Fe-d-a (12L36); ppal Pe (45R52), Co (29W52), Cu (3ZM6, 4ZB51a, 74M52), As (48H50); apall-fission U (6F51)
							00+)	
M 54m	F sep isotopes (40C51)		p (40C51)	2.1 m (40C51)			(18G52, HPS)	Fe ⁵⁴ -n-p, Fe ⁵⁴ -d-2p (40C51)
ž.	A chem, excit, cross bomb (12L37, 12L38)		EC (6A38); no pt, no pT (12L30, 20D44)	310 d (12L.38)		0.85 abs (121.38)	Mn54 C 84 C 0 84 C (2004)	V-e-n (12L38); Gr-d-n (12L38); Gr-yn (2D40); Fe-d-a (12L38, 20D44); epall Fe (45R52), Cu (42B51a)
Mn 56	A chem, n-capt (12A35)	100 (37836m)	p_ (12A35)	2, 576 h (106B52a); 2, 59 h (12L38,	2. \$1 (50%), 1. 04 (30%), 0. 65 (20%) \(\begin{array}{c} \empty 0. 822, \empty 2. 1. 77, \empty 3. 06 \\ \empty \empty  \text{660%}, \empty  \text{73, 0. 95} \\ \empty  \text{74} \empty   \text{73, 0. 95} \\ \empty  \text{74}    \text{75, 0. 95} \\ \empty  \text{75, 0. 95} \\ \em	$y_1$ 0. 822, $y_2$ 1. 77, $y_3$ 2. 06 $(y_1/y_2/y_3^2 = 10/3/2)$ spect (7546c);	Mn 55, 1 = 5/2 (97B51a) Qp. 3.63 (7546c) Mn 36	Cr-a-p (18R37); Mn-n-y (12A35, 2547, 9049, 50H31);
				9890)		(γ ₂ /γ ₃ = 1.0) spect (9531); γ ₁ 0.65, γ ₂ 1.81, γ ₃ 2.13 (γ ₁ /γ ₂ /γ ₃ ) = 10/3/2) spect, β-γ -2.7 (-0.1%), -3.0 (-0.2%) D-γ-p ion ch (9850)	8	Mn-d-p (12.138); Fe-d-o (12.138); Fe-n-p (12.135); Fe-y-p (12.1352); Co-n-d-pn (22.132; Co-n-d (12.132); Cu (32.146, 42.132; Co (29.1452); As (481450)
Ma ⁵⁷	B chem, cross bomb (112851)		p (112851)	7 d (112851)	1. 0 spect (112851)		(7946c, 4E43c)	Mn-a-2p, Cr-a-p (112851)

NUCLEAR PHYSIC	8								CHAP. 1.2
Cr-a-2n (23F51); Fe-y-2n (42S22); spall Fe (45R52), Co (29W52), Cu (13M46, 21S9, 23F51, 42B51a, 74M52); parent Mn52m (32M48); not parent Mn52 (11m 5%) (23F51)	Cr ²⁰ —an (15N50); Cr-a-n (16R37, 12L34a); Fe-n-2n (12L34a); Fe-n-1n (14H44, 34H44, 52B51, 22E34, 45251; Fe ²⁴ y-n (12P49); spall Cu (32M448, 42B51a, 74M42)		Mn-d-2n (51H48); Mn-p-n (2V40, 16B46b); Fe-d-p (12L39a); epail Co (93M51), Cu (42B51a, 93M51); daughter Co55 (12L41)		daughter Co ⁵⁷ (20D50)		Fe-d-p (12138a, 20042); Fe n-v (26542, 4W43, 2547); Co-n-p (11213a, 2146); Co-d-p (17748); spall Cu (132448, 51850, 42851a, 74427). As (481490); Bi (11C49), U (6F51)		epail-(ission U (6F51)
(0+) Fe ³² (Cc, 8+ Mn ⁵² Mn ⁵² (23F3I, HPS)			Q _{EC} 0.21 continuous y spectrum (94M51, 94M51a)		*** Co ⁵⁷		Fe 59 - 50%   - 50%   1.30	(HPS)	
no y >0. 5 acint spect (23F51)	no y (ISNSO)		no y (6P46a); -0.07 (0 002%), Ma K-x (16B46b)		0. 014 spect (20D50)		γ ₁ 1. 295. γ ₂ 1. 097 spect (I2H50); γ ₁ 1. 29, γ ₂ 1. 10 (not coinc with γ ₁ ) spect, γ ₂ 0. 10 spect (20μ42); 1. 30, 1. 10 spect (20μ42); γ ₁ (ε _K /γ 0. 84 x 10 ⁻⁴ ), γ ₂ (ε _K /γ 1. 45 x 10 ⁻⁴ ) spect conv (91B52); 0. 199 (2. 5%, coinc with 1.1 γ) scint spect, γγ γ coinc (44M52); others 152M51)		
6.3 h (32F42b); -0.55 abe (32M48); 7.8 h (32M48) -0.6 abe (23F51)	2. 5 scint spect (92851); 2. 6 abs (15N50)						0. 460 (-50\$), 0. 237 (-50\$) spect, p.y coinc abs (20042); 0. 45, no 0. 26 p² spect (48Mši)		-1. 5 abs (6F51)
6.3 h (23F32b); 7.8 h (32M48)	8.9 m (18R37, 12L38a)		2. 94 y (53B50); 3. 0 y (53S51)		1.1 x 10 ⁻⁷ a delay coinc (20D50)		45.1 d (5353); 47.1 d (22T5)); 45.5 d (29C43); 46.d (54547)		8.4 h (6F51)
EC 60%, p* 40% (33F5))	p ⁺ (18R37)		EC, no p ⁺ (16B46b, 94M51)		IT (20D50)		p (12L38a)	-	p (6F51)
		5. 84 (6 741)		91. 68 (6V41)		2.17 (6V41)	0. 31 (6V41)		
A chem, genet	A chem (18R37); chem, excit, cross bomb (12L38a)		A chem, excit (121.39a)		A genet (20D50)		A chem, excit, cross bomb (121.38a)		E chem (6F51)
26F 52	<b>₹</b>	7.5	2.	Fe ⁵⁶	F•57m	Fe ⁵⁷	# # 82 92	9	B.

	L				Washington by Man	instead in Mee		
V Z	identification	abundance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
27Co54	E excit (981652)		p ⁺ (98M52)	0.18 = (98M52)	>7, 4 scint spect (98M52)			Fe-p-n (98M52)
s v	A chem (19D37); chem, cross bomb, genet (12L41)		p+-60%, EC -40% (calc from 20049)	18. 2 h (19D37)	1. 50 (-50%), 1. 01 (-50%) spect (20D49); 1. 50 spect (24L39)	γ ₁ 0. 477 (γ/ρ [‡] 0. 3, e/γ 0. 0007), γ ₂ 0. 935 (γ/ρ [‡] 1. 4, e/γ 0. 0005), γ ₃ 1. 41 (γ/ρ [‡] 0. 3, e/γ 0. 00004) spect, spect conv, ρ-γ coinc (20049); others (85551)	Q _p 3.45 (20D4)) C ₀ 55 -507, F ₀ -507, F	Fe-d-n (19D37, 12L41, 20D49); Fe-p-y (12L386, 12L41); Mi-y-pail Fe (45R52), Co (29W92), Cu (32M48, 42B51a, 74M52), An (48H50); parent Fe ⁵⁵ (12L41)
ို့ လ	A chem, excit, cross bomb (12L41)		EC. p ⁺ (4E43a, 28C42)	72 d (12L41); 80 d (28C42)	1. 50 (coinc with $\gamma_1$ and $\gamma_2$ ) spect (4E43a); 1. 2 abs (12L41, 28C42)	$Y_1$ 0. 845, $Y_2$ 1. 26 (coinc with $Y_1$ ), $Y_3$ 1. 74, $Y_4$ 2. 01, $Y_5$ 2. 55, $Y_6$ 3. 25 $(Y_1/Y_2/Y_3/Y_4/Y_5/Y_6$ 1. 0.0 5.0. 2.0. 1.0. 2.0. 2) spect, $Y_6$ 2. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.	Qp 4.6 (4E43a)	Fe-d-2n (12L4), 16.141, 21P42, 4E43a); Fe-a-np (12L41); Co-p-pan (29.482); Ni-q-np (42552); Ni-q-np (45552); Aughter NiSC (44552);
C. 52	A chem, excit, cross bomb (12LA)		0 (121.41)	270 d (12L41)	0. 26 abs (12L41)	0.119, 0.131 spect (4E43a); 0.117 (e/v large, K/L 7), 0.130 (e/v large, K/L 7) spect, spect conv (2IP42); with Fe57m: 0.014 spect (20D50)	Q ⁺ _p 1.4 (HPS) (778-) Co ⁵⁷ (778-) B ⁺ B ⁺ Co ¹³ (778-)	Fe-d-n (12L38b, 22P38, 54B39, 12L41); [LL41); Fe-p-v (12L41); parent Fe ⁷ 7m (20D50); daughter Ni ⁵⁷ (23F52)
Co.58m	A chem, excit (\$5550)		II, no p [†] (55.550)	9.2 h (25C50); 9.0 h (37A52); 8.8 h (55S50)		0. 025 (e/y large, K/L 1. 9) spect conv (55S50)	E L .	Mn-a-n, Co-d-p2n, Co-n-2n, Ni-n-p, Ni-d-2p (55550); Fe-88-p-n (37A22); Co-y-n (25C50); spall Cu (55550, 74M52)
<b>ຮ</b> ວິ	A chem, excit, cross bomb (12L41)		EC 85%, p [†] 15% (21046)	72 d (12L41)	0. 4 abs (12L41)	0. 81 apect, B-y coinc (20D44); -0. 81 (e/y 0.0003) apect conv (55559); 0. 6 abs (12L41)	(1,2+) (18G52) (2+) (0+) (18G52)	Mn-a-n (12138), 12L41); Fe-d-n (12138), 22P38, 54B39, 12L41); Fe-58-o-n (17A52); Fe-p-n (12138); Fe-p-y (12L41); Fe-p-y (12L41); Go-p-nn (12W42); Nn-n-p (7798, 12L41, 20D44); Napali Cu (51850, 42B51a, 74M52), Aa (48H50)
C. 59		100 (453441)					Co59, I = 7/2 (87M50, 97B51d)	

NUCLEAR PHYSICS		,		CHAP. 1.2
Co-n-v (6H17a, 12L37, 12L4), 20D42a, 2447); Co-d-p (15H37b, 12L4)) Co-d-p (12H37b, 12L4) (12L4, 20D42a, 15N42); (12L4, 2D42a, 15N42); (2L4, 2D42a, 12N4); (2L4, 2D	Co-a-2b (112551); Co-t-p (29448); Nn-y-p (12948, 56551, 22525); Nn-d-p-a (23947, 23949); Nn-d-an, Cu-n-an (23947, 23949); Cu-y-2b (12948); Cu-y-2b (12948); pahl 1C u (12448); quantification Ag (42851);	Ni ⁶² -n-p (23P49) Ni ⁶² -n-p, Ni ⁶⁴ -d-a (23P4º)	N, 64 -np (23P49)	Fe-a-2n (32W52); F54-a-2n (44552); apall Zn (32W52); parent Co ⁵ 6 (44552, 32W52)
Q' 2.89 (HPS) (24) COOM 0.059 (34) COOM (2.50 (24) COOM (2.8) (HPS) (2005), 2952, 18652)	Q° 1. 4 (HPS)			
0 0589 (K/L 4.6) apect conv (42C50); 0.054 apect conv (20D4); 0.056 apect conv (20D4); 1, 1316, 1,715 cryst apect (29L49); 1, 1316, 1,715 apect v-y coinc (16D51); 1, 2x 10 ⁻⁴ ) apect conv (29F52); 1, 7x 10 ⁻⁴ ) apect conv (29F52); 1, 173 x 10 ⁻⁴ ) apect conv (31W50, 31W50); 1,173 x 10 ⁻⁴ ) apect conv (31W50, 31W50); 2, 3 x 10 ⁻⁴ , apect conv (31W50, 31W50); others (17B50, 44M50a, 13A49, 36A52, 37D51, 89B50a, 85S51)	-0.5 aba (56551); no y (23P49, 29K48)	1.3 (coinc with 6") abs, β-γ coinc (23P49) γ (23P49)		1 ₁ 0 17, γ ₂ 0. 28, γ ₃ 0. 48, γ ₄ 0. 81, γ ₅ 0. 96, γ ₆ 1 33, γ ₇ 1 58. γ ₈ 1. 13, γ ₇ 1 58. γ ₈ 1. 13 (γ ₁ /γ ₂ /γ ₃ /γ ₄ /γ ₄ /γ ₇ /γ ₇ γ ₈ 1. 0.0 0.0 0.4 0.8 /0.10 0.5/0.15,0.0 0.14, 0.77, >1.4 acint apect (44552); (32.952)
1. 56 spect (6P47); 1. 35 spect (15N42); 1. 28 spect (2D45); 0. 306 spect (29F52); 0. 318 spect (31W50a); 0. 310 spect (43M47)	1. 42 (-55%), 1. 00 (-45%) abs (36531); 1. 3 abs (23P49)	13. 9 m (23P49) 2. 3 abs (23P49) 3. 6 m (23P49)		
10 1 m (106852b); 10.7 m (12L41) 5.27 y (22T51); 5.37 y (12L41, 5.3850, 3.8551)	99.0 m (36531); 105 m (23P49); 110 m (48H50)	13. 9 m (23P49)	-5 m (23P49)	6. 4 d (4652); 6. 0 d (32W52)
II 99.%. 6 0. 28% (20D5) p (27R37)	p' (23P47)	p (23P49) p (23P49)		EC - 100%, no f* (1m 1%) (44552)

A n-capt (6H37a); chem, excit, cross bomb (12L4) A n-capt (17S16); chem, excit, cross bomb (12L41)	A chem, excit, cross bomb, mass spect (23P47)	A chem, sep isotopes (23P49) E cross bomb, (28P49) F cross bomb, (29P49) F cross bomb, sep isotopes (23P49)	A chem (12.W52); dem. sep isotope, genet (44.552)
e ၈၈ ၁	<b>3</b> 00	3 3 3 3 3	28 Ni S6

CHA.		`			e.	; <del>ë</del>
Method of production and genetic relationships	Fe-a-n (12L18c, 14D41, 15N42a, 46M49, 23F50, 43C51); Co-p-3 n(29F25); Ni-n-2n (12L38c, 14D41, 15N42a, 80M52); Ni-H8-3a (19F22); Ni-H9-3a (19F22); Ni-H9-3a (19F23); Spall Cu (13EM44, 12P68, 12P69, 12F52); Parent Co (13EM46, 42B51a, 74M52), As (48H90);	Fe-a-n (44C45); Co-d-2n (48B3); Ni-n-y (44C45, 33W50); Ni ²⁶ -n-y (48B5!); Ni-d-p (44C45)			Ni-n-y (23F49, 33W49,33W50, 48B51); Ni ⁶² -n-y (48B51)	Nid-p (121.36c.15N42a); Nin-y (4617b. 14D41, 15N42a, 20y (4645d); Cup (4646d); Cup (4646d); Cub (4613.b); Cub (4643.b); Cud (4613.b); Znn (4613.b); Znn (4613.b); Spall Cu (74448, 51B50); Spall Cu (74482.b) Spall Cu (74492.b) Bi (11C49), U (6O48, 6F51)
Distangration energy and scheme	1.91 (43CS1) NiS7	(43051)				G ₂ 2.10 (7349) NI ⁶⁵ S778 (3/2-) (7349)
Energy of radiation in Mer Gamma-transitions	1, 91, γ ₂ 1.38 (γ ₂ /γ ₁ = 6) spect (43C31);   1, 90, γ ₂ 1.39 (γ ₂ /γ ₁ = 5) scint spect (44S2);   0.128 spect (44S2);   0.128 spect (578);   0.120, 1.9 scint spect; spect conv. β-γ coinc (23F50)	Co-K-z, no y (33W50, 33W51); Co-K-z (48B51, 23F49)				1. 49. 1.12, 0.37 spect, β-γ, γ-γ coinc (7549); othere (54W51)
Energy of rad Particles	0. 845 spect (43C51); 0. 845 spect (23F50)				0. 067 ion ch (48B51); 0. 063 ion ch (33W49)	2.10 (57%), 1.01 (14%), 0.60 (29%) 1.49, 1.12, 0.37 spect, 6-y. y-y coinc (7549); others (54W51)
Half-life	12L3&c)	8 x 10 ⁴ y 8 x 10 ⁵ y 8 x 10 ⁵ y -3 x 10 ⁵ y -3 x 10 ⁵ y			85 y yield (48B51); 61 y yield (33W51)	2.564 b (57549); 2.6 h((2L)9c, 46M49)
Type of decay	p ⁺ 50%. EC 50% (23F50)	EC (23F49)			6 (23F49, 48B51)	p ⁻ (6H37b)
Percent abundance		67.76 (24W48)	26. 16 (24W48) 1. 25 (24W48)	3.66 (24W48)		l. 16 (24 W48)
Class and identification	A chem, excit, cross bomb (12L38c)	A chem, cross bomb, n-capt (44C45); chem, sep isotopes, n-capt (48B5)			A chem, n-capt, sep isotopes (48B51)	A n-capt (6R35); cham, asp isotopes, excit (\$4546, 45C46)
lectope Z	28 Ni 57	N: 58 N: 59 N: 59	09 19 1X	Ni 62	Ni 63	Ni 65

MUCI	LEAR PR	BIC	0			ChA	P. 1
spall As (48H50); spall-fission Ta (22N52); Bi (11G49), U (6F51);	parent Cu ⁶⁶ (11G49) Ni.pn (5D39); Ni5bp-n (30L47)	Ni-p-n (39T52, 98M51)	Ni-p-y (5D39); Ni58-p-y (30L47)	Ni.p-n (30L47); Ni60-p-n, Ni60-d-2n, Ni ⁵⁶ -s-pn (30L47); epail Cu (42B5ia), As (48H48a)	Nid-n (6T37a); Nip-n (Nip-v (5838, 5D39); Nip-n (30L47); Nip-l (1822); Nip-l (1837, 2825); Cny-zn (1874, 2282); p-all Cu (32M48, 4282); p-all Cu (32M48, 4285); v-all (1848); v-all (184	Co-a-n (18837); Ni-p-n, Ni-p-v (18838); Ni60-a-pn (48C50); Cu-n-h (6H7b, 80M52, S0B52); Cu-p-n (49C50); Cu-p-n (17B99, 34H43, 34H43b, 55581, 225849, 12P48, 22J50, Cu-a-n (17B99, 34H43, 34H43b, 55581, 225849, 12P48, 22J50, S0B51, 22E3, 22E3, 22E3, S0B51, 22E3,	
					Qp 2.23 (13056) Guel 1.015 FC FC 0.653 FW FC 0.655 FW		Cu ⁶³ , I= 3/2 (87M50)
•				l. 5 abs (30 <u>L</u> 47)	γ ₁ 0.655 (γ/β ⁺ 0.25, σ/γ - 0), γ ₂ 0.284 (γ/β ⁺ 0.05, σ/γ 0.015), γ ₃ 0.076 (γ/β ⁺ 0.01, σ/γ large) spect, spect conv (13050); γ ₁ (175, γ ₂ (135, γ ₁ (-0.65)) (calc from 28C51, 13050); 0.652, 0.279, 0.070 (K/L - 10) spect, spect conv (56B50)	0. 56 abs (19 <b>T</b> 47)	
		3.04 a (98MS1); 2.6 a (39T52)		24. 6 m (30Ld7)   1. 8, 3. 3 (45%) abs (30Ld7)	1, 25 (96%), 0.55 (4%) spect (13050); 1, 23 spect (16B45b)	2. 92 apect (61H50); abe (30K50); 2. 83 apect (25B49)	
56 h (11G49, 48H50)	7. 9 m (5D39); 10 m (30L47)	3.04 = (98M51); 2.6 = (39T52)	81 • (5D39, 30L47)	24. 6 m (30L47)	3. 33 b 5. 4 b (6.173 k) 1. 18 k 37 28 K 50 k 3. 3 k (46 H 5 0)	10.1 m (30L47); 10.0 m (18R37); 9.9 m (12P48); 10.5 m (6H37a)	
p. (11049)	ρ ⁺ (5D39)	p+ (98M51)	p* (5D39)	p* (301.47)	p* 68%, EC 33%(2803); 23%(2803); 28% (5880); 25%(36H49)	p* (6H37a)	
						***************************************	69.1(57847)
A chem, genet (11G49)	B chem (SD39); chem, excit, sep isotopes (30L47)	C excit (39T52, 98M51)	E chem (5D39); excit, sep isotopes (30L47)	A chem, excit, sep isotopes, mass spect (30L47)	A chem, excit chem, excit chem, excit, sep isotopes (30L47, 29K50)	excit (6HJ7a); excit. crose bomb (18R37, 56S18, 17B39); chem, sep (1sotopes (30L47)	
ş			\$ ₀	ş		79 0° 0° 0° 0° 0° 0° 0° 0° 0° 0° 0° 0° 0°	ۍ <b>و</b>

Method of production and passets relationships	Ni-p-n (56316, 5D39); Ni-Hd ³ -p (1P52); Cu-d-p (2V3); Cu-n-v (6H37b, 2547); Cu-n-x (6H37b, 2447); Cu-p-n (13R64, 42B54); Cu-q-p n (13R64), 34H44, Cu-p-n (12H54), 24H2b; Zn-n p (1EA52, 56131, 22E2); Zn-v-p n (55531, 22E2); Zn-v-p n (55531, 22E2); spall (Cu (12M48, 42B54), A (48H50); spall-fission Bi (66B51), U (6F51)		Cu-n-y (12A35, 2847, 9049, 50481); Cu-d-p (11L40); Zn-n-p (6H370); Ga-n-a (7C37); daughter Ni ⁶⁶ (11G49)	Ni ⁶⁴ a-p (29K50); Cu-a-2p (11253); Cu-a-2p (1253); Zn-q-p (29K50); Zn-q-p (29K50); Zn-q-p (29K50); Zn-q-p (29K50); Zn-q-p (29K50); Zn-q-p (29K50); Dall-fision Bi (11C49,66B51), U (6F51)	Ni-He ³⁻ⁿ (1P52); Ni ⁶⁰ -e-2n (48G50); Cu-p-2n (48G50); Zn-y-2n (58S1, 2ZE52, 42S52); apail Cu (13ZM64, 6H90, 5HB50, 42BS1a), Ae (48H90);
Distinguishes energy and others	Co + 0 + 0 + 0 + 0 + 0 + 0 + 0 + 0 + 0 +	Cu ⁶⁵ , I = 3/2 (87M50)	13F5la) 6 7 7 7 104 104 7 5la, 30R5l)	Z	Z C C A B
ation in Mer General crossitions	γ (with EC) coinc (16B46a); γ (1% of EC) (HPS, cale from 20D47, 27450, 28830); 1.34 (weak) spect (17K46); 1.35 (γ/φ² o. 0.25) apert (20D47); 1.35 (γ/φ² o. 0.25) apert (20D47); 1.36 (γ/φ² o. 0.25) apert (20D47); 1.36 (γ/φ² o. 0.32) abe (10°52); 1.36 (γ/φ² o. 0.32) abe (27K50), 1.36 (γ/φ² o. 0.32) abe (27K50), 1.36 (γ/φ² o. 0.32) apect conv (47M48); γ (a/γ <0.005) spect conv (47M48)		1. 044 (γ/β* 0.10, «/γ <3 × 10 ⁻³ ) ppect, spect conv (2375la); 1. 05 scint spect (30R3l, 94M5la)	0.191 (a/y 0.01, K/L - 8), 0.096 (a/y 0.09, K/L 7.4) scint spect, spect conv, p-y coinc (80552)	(61H50) # spect com
Bangy of radiation in Mov Particles G	p: 1 apact (28C48c, 13O49); 0.571 apact (28C48c, 13O49); 0.58 apact (28C49c, 13C41); 0.58 apact (28C48c, 13O49); 0.644 apact (28C48c, 13C49); 0.65 apact (42C41); 0.66		2. 63 (91%), 1.5 (9%) spect (2.2.5.18) (2.2.5.18) 2. 7 (-94%), 1. 65 (-6%) scint spect, \$-y coinc (30.85)	7.38 (67%), 0.57 (33%) spect (80523); 0.54 abe (29%50)	0.66 spect (61H50)
Half-life	12. 80 h (29.850): 12. 74 h (39.851): (3.951): 12. 8 h (27.36): 48H50)		5.10 m (3352); 5.17 m (3385)); 5.17 m (3085)); 5.18 m (4C54); 5.2 m (23F5)a)	94. 5 h (29K50); 64. b h (00552); 65. b (11059); 61. b (48H50)	9. 33 h (61H30); 9. 5 h (32M48)
Treed	EC 42%, p ¹ 39%, p ⁴ 39%, p ⁴ calc from and from K/p ⁴ and K/p		p (12A35)	p [*] (11G49)	EC -90%, p ⁺ -10% (61H50)
Percent		30. 9 (57847)			
Class and identification	A chem, n-capt (12A35); eactt (2V36); chem, eactt (5D39)		A n-capt (12A35); excit (7C37)	A chem (IIG49); Chem. cross Chem., sep isotopes (29K50)	A chem, genet (32M48); excit (48G50)
ed z	3	Ça 65	<b>9</b>	o o	30 ^{Zn} ⁶²

NUCLEAR PHYSICS				(
Ni-a-n (18837); Ni6-a-n (48G50); Cu-p-n (38S38, 5D39, 47B.)b, 48G50); Cu-d-A-n (31B.9, 12P47); Zn-y-n (37B.9, 12P49, 5SS51, Zn-y-n (37B.9, 12P49, 5SS51, Zn-y-3n (32M.48, 51B.50, 42B51ay, An (48H50)		Cu-d-2n (22P38); Cu-p-n (58B38,47B51b); Cu-p-n (58K51); Zn-d-p (12L39); Zn-n-y (42S39,2847); spall Cu (42S51a), As (48H50); daughter Caés (12L39b)	daughter Ga ⁶⁷ (48B53, 47M52)	
2n63 2n63 2n63 2n63 2n63 2n63 2n63 2n63	Zn ⁶⁴ , I = 0 (87M50)	45% Zn65 45% L12 55% L12 (3/2-) 0 (21G460, 24F51, 95M52)	$Z_{n}^{66}$ , $I = 0 (87M50)$ $a \in G_{n}^{67}$ $(1/2 -)$ $Z_{n}^{67m} = 0.092$ (8/2 -) $0.092(48B53)Z_{n}^{67}, I = 5/2 (87M50, 38D52)$	$2n^{68}$ , I = 0 (87M50)
0.960 (-8%, e/y 2 x 10 ⁻⁴ ), 1.89 (-4%, e/y -0), 2.60 (-0.9%, e/y -0) spect conv. abe. y-y coinc (34H47)		1.120 spect conv (48M49); 1.125 spect, spect conv (12H50); 1.114 spect (48M49); 1.112 (4/y 2.3 x 10 ⁻⁴ ) spect conv (11W50); 1.127 scrim spect (25C31a); 1.12 scrim spect (13C9); 1.12 scrim spect (13C9); 1.14 (46 for EC) x - coinc (21C6a); 1.15 (47 of EC) x - coinc (21C6a); 1.16 (47 of EC) x - coinc (21C6a); 1.17 (47 of EC) x - coinc (21C6a); 1.18 (47 of EC) x - coinc (47C50) 1.21 (coinc with p², e/y - 0.1) 1.21 (coinc with p², e/y - 0.1) 1.22 (coinc with p², e/y - 0.1) 1.23 (coinc with p², e/y - 0.1) 1.24 (coinc with p², e/y - 0.1) 1.25 (coinc with p², e/y - 0.1) 1.25 (coinc with p², e/y - 0.1) 1.26 (47C50)	0. 092 (e _K /y 0.63, K/L 7) scint spect (48B53); 0. 092 (e/y 0.6) scint spect (47M52)	
38. 5 m (34847, 2. 16 (92%), 1. 40 (7%), 0. 5 (-1%) 0. 960 (-8%, e/v 2 m 10 ⁻⁴ ), 1. 89 (-4%, e/g -0), 2. 60 (-0. 5%, 3. 5 m (5039) 2. 32 spect (14T4) (-4%, e/g -0) spect, spect conv. ab., y-v coinc (34H47)		0. 32 spect (48M49); 0. 32 spect (6P47)		
		245 d (12239); 245 d (12238)	8.5 x 10 -6 a dalay coinc (47M52)	
8 ° 93%, EC 7% (34H47)		EC (K) 97.5%, 6* 2.5% (1952), 41952, 41952, 6.794%, p* 0.7% (salc from 30G51, 24F51, 24F51, 24F51,	IT (47M52, 48B53)	
	48 89 (1B50)		27. 81 (IBSO) 4. 11 (IBSO)	18. 56 (1850)
A chem, excit (37837, 6H37b, 18R37)		A chem (22P38); chem, excit, cross bomb (12L39)	A genet (4853, 47452)	
Z ⁿ 63	Zugar 2	Sugar Parkers	2n67m Zn67m	2ne8

C.	IA.	P. 1.2				REACTOR PHYSICS
Method of production and	generic relationships	Zn-d-p (121.39, 14K39, 6V39); Zn-n-y (6T38, 121.39, 2847); Ga-n-p (121.39); e-pail Ad (48H50); parent Zn ⁵ (14K39) Zn-d-p (121.39, 14K39, 6V39); Zn-n-y (6H56, 6T38, 2847, 650+61, 621.39); Ga-d-a (121.39); Ga-n-p (121.39);	daughter Zn ^{69m} (14K39) Zn-n-Y, Ge-n-a (28H46b)	As-p-(11235); apail As (48H50); apail-itssion Bi (11C49), (16191); fission Th (21731), U (60831), Pu (61851a); perent Ca ⁷² (60851).	Cu-Ha ³ -n (1P52); 2n-drn (6A39, 12L39b); 2n-p-y (2D40); parent 2n ⁶⁵ (12L39b)	Cu-a-n (50M37, 18R37, 10L50a); Zn-pn (59B3, 49M50); apall Cu (second order reaction) (42B51a, 29W52), apall -fission Sn. Ba (42B51); daughter Gebb (48H40)
	LANGUAGENCOD COCKET AND SCHOOLS	(1/2-) Zn ^{69m} 0.44 (1/2-) Zn ⁶⁹ 0.44 (1/2-) (1/2-) (1/2-)	Q 0.90 (HPS, 12L39)			0° 5.16 (23751a.) 60° 60° 77° 77° 77° 77° 77° 77° 77° 77° 77° 7
action in Mer	Gamma-transitions	0. 437 (e/y 0. 049) spect conv (91852b); -0. 436 (e/y -0. 065) spect conv, ecint spect (23152); 0. 439 (e/y -0. 04) spect, spect conv (2414); 0. 440 spect (2804); 0. 450 (e/y -0. 06) (16144) no y (121.39)		۲ (6055)	0.054, 0.117 spect conv (6V39)	γ ₁ 1. 05, γ ₂ 1. 7, γ ₃ 2. 2, γ ₄ 2. 75 coinc with γ ₁ 1, γ ₅ 3. 3, γ ₆ 4. 25, γ ₇ 4. 8 (γ ₁ /γ ₂ /γ ₃ /γ ₄ /γ ₃ /γ ₆ /γ ₇ 3. 7, γ ₆ 4. 25, γ ₇ 4. 8 (γ ₁ /γ ₂ /γ ₃ /γ ₄ /γ ₃ /γ ₆ /γ ₇ 3. 7, γ ₆ 3. 2, γ ₆ 3. 2, γ ₆ 3. 2, γ ₆ 3. 2, γ ₇ 3. 2, γ ₇ 2. 3, γ ₈ 3. 3, γ ₈ 3. 41, γ ₉ 3. 78, γ ₉ 3. 3. 3. 3. 3. 3. 3. 3. 3. 3. 3. 3. 3.
Reergy of reduction in Mer	Particles	0.897 spect (23D52); 0.914 spect (91852b); others (14K39, 12L39, 35B46a)	2.1 abs (28H46b)	-0.3 (95%), -1.6 (5%) abe (60651)	2. 2 (25A52)	4.144 (87%), 1.4 (4%), 0.88 (7%), 0.40 (2%) prect (49M52) 0.40 (2%) prect (49M52)
10-16 116-		13. 6 h (12L.39) 57 m (12L.39); 51 m (481480); 52 m (7H49)	2. 2 m (28H46b)	49. 0 h (60551)	15 m (6A38, 12L39b)	9.45 h (10.56a); 9.4 h (1833, 9.2 b (49.85); 9.2 b (49.85) 50.M37)
Type of	decay	IT (14K39) 6 (6H37b)	p (28H46b)	p (60851)	EC (6A38); 6 > >50% (25A52)	6 6 4% EC (49M2); 649M21; 646% EC (10L50a)
Percent	sbandsnoe		0.62 (1B50)			
Class and	identification	A chem, excit (6738); cross boxet, cross boxet (12139, 14K39) A chem, n-capt (1817b); chem, excit, cross bomb (12139, 14K39)	ы	A chem, genet (60546, 6055)	A chem, genet (121.3%)	A chem, axett (50M37,18R37a)
Intende	V Z	30 ^{Zn69} m	2n 20 21 21 21 22 22 22 22 22 22 22 22 22 22	. uz	31 Ge 65	*6

NUCLEAR PHYSICS		CHA	AP. 1
Cu-te's (1283); Cu-te's (1283); Cu-te's (6A3); Cn-te (6A3); Cn-te (590A3); Cn-te (590A3); Cn-te (590A3); Cn-te (6A382); spall Cu (second order reaction) (42851s), daughter Ge [§] (48149); parent Zn [§] Tm (48853, 47M82)	Cu-a-n (18837, 50M37); Zn-p-n (2D38, 59838, 49M50); Zn-d-n (31G38, 6V39); Ca-n-n (18728, 6V39); Ca-n-n (1874), 77839, 12P48); Ca-y-n (12P49, 42852); Ca-d-u (42541); Ga-d-u (42641); Ga-d-u (42641); Ga-d-u (42641); Ga-d-u (42641); Ga-d-u (42641);	Zn-p-m (2D38); Zn-q-p (500418); Gn-n-y (12A45, 2547); Gn-n-zn (1P37); Gn-d-n (42541); Gn-n-n (42541); An-y-nn (45142); pall An (48150)	
(44853)	(E,1+) (GGBB (1+1) (GGBB (1+1) (GGBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBB		Ca. ⁷¹ , 1 = 3/2 (87M50)
1, 0.090 (eg/γ 0.074), γ 2 0.092 (with Zn67m, eg/γ 0.63. K/L 7), γ 3 0.182 (eg/γ 0.011, K/L -12.9), γ 2 0.206 (eg/γ 0.012, K/L -12.9), γ 2 0.206 (eg/γ 0.0029), γ 3 0.206 (eg/γ 0.002), γ 3 0.206 (eg/γ 0.206 (eg/γ 0.002), γ 3 0.206 (eg/γ 0.00	1. 10 apect (49M52)		
	1. 88 (-96%), 0. 77 (-4%) spect (49M52); 2. 0 abs (35B46s, calc from 50M37); 1. 9 abs (18R37, 50M37); cl ch (50M37)	1. 65 spect (\$6H48); 1. 62 abs (6JB47); -1. 6 cl ch (42539a)	
77.9 h (22751);	12P48)	20. 3 m (61B47); 20 m (12A35)	
EC (6A38); no p' (14m 0.05); (47M52); no p' (49M52, 4853)	9+-85%. EC -15% (49M52)	p² (2.038)	
	60.2 (3348)		39.8(3148)
A chem, excit (50M384, char), char), char, excit, cross bomb (6A38)	A chem, excit (37837); chem, excit (18837)	A chem, n-capt (12A35); cham, excit (2D38)	
5 _d	3, 3,	0, 40	8

Import	Clear and	Percent	Type of		Energy of radiation in Mev	iation in Mev		Method of production and
V Z	identification	sbundance	decary	Ami-ma	Particles	Gamma-transitions	Dissategration energy and scheme	genetic relationships
31 Ga 72	A chem, n-capt, excit (12.38a, 42539)		p ⁻ (42539)	14.3 h (26M43a, (26M3); 14.1 h (42539, 9B50)	3.15 (9%), 2.52 (8%), 1.5 (11%), 0.9 (32%), 0.6 (40%) apact (56446), 2.17 (8%), 1.7 (?) (3%), 1.5 (7%), 1.00 (26%), 0.74 (23%), 0.6 (?) (25%) apact (14M48)	1 ₁ 2. 491, γ ₂ 2. 508 (γ ₁ /γ ₂ 0. 63) apect (12H22): 2. 51 (26%), 2. 21 (35%), 1, 87 (6%), 159 (5%), 1. 20 (73 (42%), 1. 05 159 (5%), 0. 64 (100%), 0. 68 (42%), 0. 63 (4%) apect, apect conv (56H48): γ ₁ γ ₂ 2. 50 (15%), γ ₃ 2. 18 (33%), γ ₄ 1. 81 (10%), γ ₃ 2. 18 (33%), γ ₄ 1. 30 (γ ₄ + γ ₄ γ ₂ 25%), γ ₈ 1. 10 (15%), γ ₉ 0. 335 (100%), γ ₁ 0. 691 (5%), γ ₁ 0. 631 (44%) apect, apact conv (144468): 3. 4 (-0.0.0%), 3. 1 (-0.1%) Dγ-p sion ch (9850)	Qp 4.0 (56H48,14M48)  Gq72  Gq72  97  97  97  97  97  97  97  97  97	Ga-d-p (121.38a); Ga-n-y (42.31q, 2547, 605.51); Ga-n-y (42.81q, 605.51); Aa-d-op (16.47); Aa-y-Ha ² Aa-y-pn (45.H2); Aa-y-Ha ² Aa-y-pn (45.H2); T1 (21.47b); T1 (21.47b); T2 (21.47b); T3 (21.47b); T3 (21.47b); T3 (21.47b); T4 (21.47b); T5 (21.51); T5 (21.5
G. 73	B chem, excit (60546, 6055))		p (60551)	5. 0 h (60551)	].4 abe (60551)	0.0135, 0.054 spect conv (17J5la)	(17.2-) Go ⁷³ (17.2-) Go ⁸	Ge-n-p (60551); Ge-v-p (12P43); As-v-2p (12P43); As-c-d-p (112551); ppall-fission Bi (11G49); fission U (60551)
32 Ce 66	A chem, genet (48H49)		p ⁺ (?) (48H50)	-150 m (48H50)				<pre>apall Cu (second order reaction) (4.281a), spall Ge (48H49), As (48H50); parent Ga66 (48H49)</pre>
5,0	A chem, genet (48H49)		p ⁺ (48H50)	21 m (48H50)				apall Cu (second order reaction) (42851s), spall Ge (48H49), As (48H50); parent Ga ⁶⁷ (48H49)
<b>9</b>	A chem (50M38); chem, genet (48H48b)		EC (48H48b)	250 d (48H50)			_	apall Cu (second order reaction) (428)a), spall As (48H48a, 48H50); Zn-c-Zn (50M38); parent Ga ⁶⁸ (48H48a, 48H50)

\$ 5	A chem (50MJ8); chem, exclt, cross bomb, (51M48)	20. 55 (3146a)	EC -67%, p ⁺ -33% [51348]; [630438]	39. 6 h (51M48); 39. 7 h (12D42); 40 h (48H30); 37 h (50M38)	39. 6 h (51M48); 1. 215 (88%), 0. 610 (10%), 0. 22 39. 7 h (12D42); 40 h (48H50); 37 h (50M38)	1. 610, 1. 340, 1. 12, 0. 870, 0. 576, 0. 388, 0. 090 spect, firty coinc (10H51)	Qp 3.36 (10H31) Ge69  2.1 2.1 2.1 3.2c.) (10H51) Ge70, I=0 (35T49)	Zn-a-n (50M18, 51M48), Ga-d-2n (1384a, 51M48, 10H51); Ga-p-n (12D42); Ga-y-n (42S41, 51M48); Ga-y-n (54H44, 42S52); spall As (48H50)
	A chem, excit, cross bomb (13541a); sep isotopes, n-capt (22850)		EC, no p ⁺ (51M48, 26M49)	II. 4 d (51M48); III. 3 d (12D42); II d (26M49, I3S4ia)		no y (13541a, 26M49, 51M48); Ga K.x (2547, 51M48, 26M49)	(3.2-) (HPS)	Ga-d-2n (13541a, 51M48); Ga-pn (12D42); Ge-n-y (12541, 51M48); Ge-n-y (12647, 51M48, 26M49); Ga-70-n-y (12850); spall Ae (48H50); daughter Ae ⁷¹ (48H49)
Ge 72m	A genet (28B48)		IT (28B48)	2.9 x 10 ⁻⁷ e delay coinc (\$2M51); 5 x 10 ⁻⁷ e delay coinc (28B48)		0.7 (e/y very high) coinc abs conv (28B46, 52M51)	G. ⁷²	daughter Ga ⁷² (18550b); daughter As ⁷² (14550b)
2.5		27. 37 (3148a)					$Ge^{72}$ , I = 0 (35T49)	
6,3		7. 67 (3148a)					Ge ⁷³ , I = 9/2 (35T49)	
₹. °5		36.74 (31482)					Ge ⁷⁴ , I = 0 (35T49)	
Ge 75m	A excit (9F52); crose bomb, n-capt, sep isotopes (91S52c)		IT (9F52)	42 = (9F52); 48 = (91S52c)	conv: 0.14 abs (9F52)	0.175 acint spect (91552c); -0.150 acint spect (24C52)		Go ⁷⁴ -n-y (91552c); Go-n-y (9F52, 24C52); Ao-n-p (9F52, 91552c)
₂ ه	A chem, excit, cross bomb (1354la); n-capt, sep isotopes (22R50)		p (13541a)	E2 m (\$1M48); 89 m (13S41a); 79 m (22R50)	1.137 (85%, not coinc with y), 0.644 (15%) spect (91552c); 1.2 abs (13541a); 1.3 abs (22R50)	0.265 (e/y very email), 0.418, 0.572, other y's spect, spect conv, scint spect (31552c); 0.25 (-10%, (22R50); no y (31M48)	Q _p 1.14 (9155.2c)	Ce - 74 - n.y (22850, 91852c); Ce - ny (42539, 42541, 13541); Ce - n. 27 + (42541, 13541a); Ce - n. 27 + (42541, 13541a, 51844a);
2.		7.67 (31484)					Ge ⁷⁶ , I = 0 (35T49)	
	E n-capt (24C52)		IT (24C52)	-0.35 • (24C52)		-0.06 scint spect (24C52)		Ge-n-y (24C52)

	7	Bernan	7		Banny of rad	Reserv of reduction in Mey		Marked of paraduceine and
Z	idendiscation	shedeece	decay	Half-life	Particles	Gamme-transitions	Distangration energy and scheme	genetic relationships
32Ge 77m	A cross bomb, genet, n-capt (23447); sep isotopes (22850)		p -50%, IT -50% calc (42F52); p'. IT (14M52)	59 a (23A47); 57 a (22R50)	2. 8 abs (23A47)	0. 38 acint apect (14M52)	(1/2-) G ₀ 77m 0.36 (7/2+) G ₀ 77 0.36	Ge-n-y, parent As ⁷⁷ (23A47, 22850); Ge ⁷⁶ -n-y (22R50)
ç	A chem, excit, cross bomb (13541a)		6 (42541)	12 h (13541a, 61551, 22R50)	2.196 (42%, coinc with y), 1.379 (65%), 0.71 (23%) spect (91852); others (14M52, 61851, 22R50, 26M49)	0.042, 0.073 (coinc with 0.213 and 0.264 yl, 0.213, 0.264, 0.368, 0.418, 0.564, 1.105, 1.75 spect, 6-y, y-y coinc (91552); 0.209, 0.268, 0.300, 0.327, 0.366, 0.408, 0.425, 0.466 spect cour (91522); 0.6, 0.3 (coinc with 6') aba, 6-y coinc (22850)	G _E 2. 46 (91552) (3/2-) (91S52, HPS)	Ge-n-y (22R50); Ge-n-y (42S9, 42S41, 2547); Ge-d-p (42S41, 13S4a, 88S52); Ge-n-c (13S4a); finsion Th (27S5), U (61S46, 61S31), U233 (61S48); parent As ²⁷ (61S46, 61SS1)
2	B chem, genet (61346, 61351)		p_ (61851)	2.1 b (61851)	-0.9 abs (61351)	y (61851)		ission U. parent As (61851)
33 <b>As</b> 70	D chem (48H49, 48H50)		(48H30)	52 m (48H50)				As-d-pén, daughter Se (48H50); not found: Ge 70-p (37A52)
4	A chem (42841); chem, genet (48H49); mass spect (104B52)		EC (48150); EC, p [†] (51M48a)	60 h (48H50); 50 h (51M48a)		0. 162 spect cany (\$33M50)		Ga-a-2n (53M50); Ga-d-n (51M48a); Aa-d-pin (48H50); parent Ge ⁷¹ (48H49)
2	A chem, excit (14M47); chem, excit, esp isotopes (51M48a)		EC, p [†] (51M48a)	26 h (51M484, 2V40); 27 h (48H50)	3. 34 (19%), 2. 50 (62%), 1. 84 (12%), 0. 67 (5%), 0. 27 (2%) spect (53M50); 2. 8 abs (14M47, 51M48a)	0, 835, others up to 3. 0 (weak) apect (\$3M50)	Q _p 4.36 (53M50)  A _{0.72} (50)	Ga-a-n (14M47, 51M48a, 53M50); A-a-a (2V40); A-a-a-ben (48850); So ⁷⁴ -a-a (51M48a); daughter So ⁷² (48H48a)
٤.	A chem (42539b); chem, excit, cross bomb, sep isotopes (51M48a); mass spect (1735a)		EC (4E43b); no p' (4E43b, 51M48a)	76 d (51M48a); 90 d (42839. 53M50)		0. 0135 (L/M 5. 4), 0. 0539 (K/L+M 5. 6) spect conv. conv-conv coinc (1738a, 17352); 0. 052 spect conv (4E43b, 53M50)	48.73 (18.72+) 657 W52)	Ga-d-n (42339b, 4E43b); Ga ⁷ O _{*n-p} (51M48a, 53M50); Ga-n-p (51M48a, 53M50); Aa-d-p3n (48H50); 8e ⁷ O-p-n (53F51)

Ga-a-n (\$1M48a); Ga-d-n (\$23%, 4284), 2142) Ga-d-n (\$25%); Aa-n-2n (\$4C38, 423%b); Aa-d-p2n (\$4C38, 423%b); Sa-d-a (\$12740); Br-y-an (\$5H\$2); spall-fission Bi (ilC49)		Ge-p-n (2V40); Ae-d-p (6T36, 48C38); Ae-n-y (12A35, 48C38, 9C49, 50H51); Se-n-p (42H47); Se-d-c (23F40); Br-n-c (48C38); Br-y-an, Br-y-He³ (85H52)	Br-y-a (88H52);  spail-fission Bi (11C49), Th [7N642], U (655);  fission Th (21T5), U (61551), U233 (61S48); daughter Ca ⁷⁷ (61551); 22R5Q not parent Se ⁷⁷ m (lim 2%)(56M50a)	Br-n-a (2637a, 48C38, 42339, 64B5); Br-y-Ha ³ (65H52); Se-n-p (42339b); fission U, daughter Ge (61346, 61S5)
9 1.36 (1731) 9 2.55 (1735)) 4874 8974 (0+) (0+) (1735) (1735)	A. 1 = 3/2 (87M50, 29J52)	Q _p 3.1 (HPs) (2-) As ⁷⁶ (2-) Qs (2-) Qs (2-) Qs (2-) Qs (1-) Qs (1-	Qp 0. 70 (43C5la)  (3/2-) As ⁷⁷ (7/2-) Se ^{77m} (1/2-) O.162  (1/2-) O.162	Q 4.1 (7455la)
Y ₁ 0. 596, Y ₂ 0. 635 (Y ₁ /Y ₂ = 4) spect, 97 coinc (1751); 0. 593 spect (20M50); 0. 582 spect (20D4)		0. 55, 1. 20, 1. 70 spect (7547d); 0. 557, 1. 22, 1. 78 (weak) spect (16.848); 0. 558 (eg./ v) 0. 002) spect conv (7752); 1. 72, 1. 25, 1. 164, v4. 2. 15 (v1/v2/v3/v4 = 1/0. 4/weak/weak) spect (43.846); 0. 58, 1. 20, 1. 76, 2. 02, no. 2. 3- 2. 7, (lim 0. 01%) scine spect, v-y coinc (62.851); v1. 0. 55. v2. 0. 646, v3. 1. 210, v4. 1. 410, v5. 2. 0. 646, v3. 1. 210, v4. 1. 410, v5. 2. 0. 6(v1/v2/v3/v4/v4); 1. 27. 0. 568 (es/v-0), 1. 25 (es/v-0) spect, spect conv (54.849).	no y (43C3la, 13J9l)	0. 27 abs (42539b); no y coinc with 4. I ff (74551a)
h.; (51%), 0.69 (49%) spect (1751); 1.45 (47%), 0.82 (53%) spect (53450); 1.45 (17%), 0.92 (89%) spect (1751); 0.92 (89%) spect (1751); 0.96 spect (53M50)		.04 (60%), 2. 49 (25%), 1. 29 (15%) apect (7347d); .15 (45%), 2. 27 (234%); .15 (40%), 2. 7 (-30%), 1. 1 (-30%) apect, 6-y coinc (3948)	0. 700 spect (43CSia); 0. 679 spect (13ISI); no conv (43CSia, 13JSI)	4. 1 (-70%), 1. 4 (-30%) aba (61891); 1. 4 cl ch (42839b)
17.5 da (\$1M48a); 19.0 d (4BH50); 16 d (42539b)		26. 8 h (344442); 26. 3 h (144440); 26. 1 h (3748)	38 h (18H50, 2175.); 40 h (61551)	90 m (61851, 64B51); 80 m (48C38); 65 m (26S37a, 42S39b)
9 53%, p* 47% (1733); p: -67%, p* -33% (533650)		6. no 6.; 6.1 lim 0.03 (6.1841); 7. (1841); 8. (16.848) (16.848)	p ⁻ (61S51)	p (26537a)
	100 (6N37)			
A excit (48C39); Chem, excit (42839b)		A chem, n-capt (12.435)	A chem, genet (61846, 61551)	B chem (26837a); excit (48C38)
2,	A. 75		£ .	<u>۔</u> پو

- Landers	L		True of		Reserve of re-	Beery of raduction in Mey		
V Z	identification	abundance	decay	Half-iire	Particles	Gamma-transitions	Distangention energy and scheme	genetic relationships
33Ae ⁷⁸	F chem (64B51)			-40 m (64B51)			Q+ 2. 70 (62S51)	Ge-a-n (49C48, 62551);
٤,	D chem (65B50)		p ⁻ (11V52)	9 m (65B50); 10 m (11V52)	-2.1 <b>abs</b> (11V52)		<b>1</b>	Ge 70-a-n (49C48); As-d-4n (48H50); epail-fission Bi (66B51)
						•		
34.8e 70	D chem (48H49, 48H50)		p* (48H50)	-44 m (48H50)				
\$ 12	A chem, genet (48H48a)		EC (48H50)	9.7 d (48H50)				
Se ^{7,3(m?} )	A chem (48H48a); chem, excit, sep isotopes (49C48)		6. EC, IT 20% (?) (62591)	7.1 h (49C48, 62551); 6.7 h (48H50)	1.68 (1%), 1.318 (88%), 0.750 (10%), 0.25 (1%) spect (6255)	Y ₁ 0. 0671 (conv in Se, K/L. 7. 6), Y ₂ 0. 361 (K/L. 8. 6), Y ₃ 0. 860, Y ₄ 1. 310 (Y ₁ /V ₂ /Y ₃ /Y ₄ = 10/163/	Q¢ 2. 70 (62551)	Ge-a-n (49C48, 62331); G70-a-n (49C48); As-d-dn (48H50); spall-fission Bi (66B31)
						11/8) spect, spect conv (62551)		
\$. *		0. 87 (24W48)					8e ⁷⁴ , I = 0 (55G50)	
27. 27.	A cham, excit (2De0, 4K42); esp isotopes, n-capt (10C50)		EC, no p ⁺ (26F47, 49C48, 10C50)	127 d (49C48); 128 d (10C50); 115 d (26F47); 120 d (48H50)		Y ₁ 0.067, Y ₂ 0.077, Y ₃ 0.098 (K/L-11, e/y -8), Y ₄ 0.124 (e/y -0.3), Y ₅ 0.138 (e/y -0.1), Y ₆ 0.203, Y ₇ 0.269 (e/y -0.9),	2673 EC 0.405	As-d-2n (2D40); As-d-2n (4K42, 26F47, 49C48, 48H50); Se-n+y (2847, 26F47, 11T48, 1372a); Se ⁷⁴ n-y (10C50)
						$(e/v - 0.001) (v_2/v_3/v_4/v_5/v_7/v_5/v_7/v_5/v_1) = 0.16/-0.007/-0.02/0.1/0.70/-0.05/0.14) spect,$	30 SO	
						apect conv, y-y coinc (13.352a); 0.025, 0.066, 0.081, 0.097, 0.121, 0.136, 0.199, 0.265, 0.280, 0.305, 0.402 apect conv	(3.2-)	
•						(105.0) 0.0%, 0.099 (7), 0.123, 0.137, 0.257, 0.283, 0.405 spect (11748); 0.98 (47, karge), all other y (47, very small) spect, spect cow (25845);	6880701	
<b>8 2</b>		9. 02 (24W48)					3e ⁷⁶ , I = 0 (55G50)	

	Sec and	Decrees	Topony		Energy to wood	Resear of radiation in Mar		Marked of contract of
V Z	identification	sbandence	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
35 Br 74	D chem (13H51)		p ⁺ , EC (i3H51)	-35 m (13H51)				Cu-C-3n (13H51)
Br 75	B chem, cross bomb, sep isotopes (35 W48)		p ⁺ , EC (35W48)	1.6 h (13H51); 1.7 h (35W48)	1. 70 (46%), 0.8 (20%), 0.6 (15%), 0.3 (19%) spect (25F52); -1.8 abs (13H51)	-0.6 aba (25F52)		Cu-C-2n (13H51); Se ⁷⁴ -d-n (35W48); 3e ⁷⁴ -p-y (35W48, 25F52)
Br 76	A chem (48H48); chem, excit (13H51); chem, sep isotopes(25F52)		g ⁺ (48H48)	17. 2 h (25F52); 16. 5 h (13H51); 15. 7 h (48H48)	3.57 (46%), 1.7 (10%), 1.1 (11%), 0.8 (14%), 0.6 (19%) apect (25752); 3.5 apect (13H51)	1. 2, 0. 96, 0. 75, 0. 68, 0. 42, 0. 37, 0. 33, 0. 25 spect, spect conv (25F52); -2 abe (48H48)	Q\$ 4.6 (28F52)	As-a-3n (48H48, 13H51); Se76-p-n (25F52)
Br 77	A chem, sep inotopes (35 W48)		EC 95%, p [*] 5% (35W48)	57 h (48H48, 13H51); 58 h (35W48)	0.336 spect (43C51); 0.36 spect (48H48); abs, spect (35W48)	$Y_1$ 0.160, $Y_2$ 0.237, $Y_3$ 0.284, $Y_4$ 0.298, $Y_5$ 0.520, $Y_6$ 0.641, $Y_7$ 0.813 $(Y_1/Y_2/Y_3/Y_4/Y_5/Y_6/Y_7$ = 0.6/20/0.2/0.2/0.2/100/8.6/25) = spect; spect comy (45C3); 0.160, 0.334, 0.399, 0.521 spect comy, $x_1 - y_2 - y_3 -$	EC Br77	As-a-2n (48H48, 13H51, 43C51); Se ⁷⁴ -a-p (15W48); Se ⁷⁶ -a-n (15W48); parent Se ^{77m} (43C51, 43C51b)
							0.320	
Br 78	A chem, excit (26537a)		p* (2633a)	6.4 m (26537a); 6.5 m (13H51)	2. 4 abs (35B46a, calc from 26837a); 2. 3 abs (26837a)	0 . 108, 0. 046 spect conv (6V39)	Ť	As-a-n (26537a, 13H51); Se-d-n (26537a); Se-p-n (5958a, 6799); Br-y-n (7C37, 37599); Br-n-2n (6H37)
Br 79		50. 52 (9W46)					Br 79, I = 3/2 (87M50)	
80m	A chem, n-capt (12A3); chem, excit, cress bomb (26S37a)		IT (24839)	4. 58 h (41M51); 4. 5 h (26S77a); 4. 4 h (59B38)		0.049, 0.037 (e/y-1.3) ion ch (12.826) 0.048, 0.35 spect conv (33.120); 0.049, 0.037 spect conv (6V39); 0.049 (L/LIII .0) spect conv (3.145.2h; 0.048 (e/y very large), 0.037 (e/y-1) abs (35.040); others (52.W5)	n 0.086 0.037	8e-d-2m (38 W48, 25F52); Se-p-n (59B M8); Se-p-n (59B M8); Br-n-(24A36, 24837a, 24839, 34C46, 22471; Br-q-n (37B39); Br-n-n (17B39); Br-n-2m (1P37); Br-n-1m (1P37);
e k	A chem, n-capt (12.43); chem, excit, cross bomb (26.37a); chem, genet (24.539)		6 - 92%, 6 - 92%, 8 - 93%, EC - 5% (Calc from 41M5), 28R50); 6 - 6 - 6 - 6 - 6 - 6 - 6 - 6 - 6 - 6	18 m (2637a, 24339)	p.: 1.99 (85%), 1.1 (15%) spect (144.22); 1.97 (80%), 1.1 (11%), 0.7 (9%) spect (259.52); 0.99 spect (34.54); 0.87 spect (34.51); 1.0 spect (160.49); 0.73 abs (63.847)	> 0, 6 abs (21D40); <0.5 abs (2637a, 59B38); no y (34L52)	(25F9.2) (25F9.2) (0+) (1669.2, HPS)	3e-p-n (59B38); Br-q-9(2637a, 34G46, 2547, 9G49); Br-d-p (2637a); Br-d-p (17839); Br-n-2n (1977); daugher Br 80m (24339, 21D40, 6484)

_	Se-p-n (59B)8, 6R4la); Se-d-n (268378, 56M51); Br-n-y (13K93, 26878, 2847); Br-n-g-g-g-g-g-g-g-g-g-g-g-g-g-g-g-g-g-g-	Se-d-n (26537a, 25F32); Rb-y-c (69955a); spall-(isacion Ta (22952), Hg (63524); Pb (13P47a), Ing-d-c (6653), Th (7N49a, U (6048); Th (7N49a, U (6048), Z1751, 72B5), U (20140, Z1751, 72B5), U (20140, Z1751, 72B5), U (20140, Z1751, 72B5), Pu (32K4a, G1551a); Z0140, Sparent v _x 83m (20140, 65540, 57M41, 31053a)	Rb-n-a (70B43); spall-(faston Bi (13P47a), U (6F3); flaston Th (72B51), U (22D39, 16H39a, 16H39b, 55540, 57M41, 70B43, 32K51); daughter Se ⁸⁴ (33G51b)	fission U (65540, 70843, 66543, 63549); parent Kr ⁸⁵ (66543, 63549)	fission U (65540, 26547, 615447, 61547, 61547, 61547, 615440); Pu (14847); parent Kr ⁸⁷ (70843, 66543, 61547, 61547, 61549)	fission U, parent Kr 88 (6)349)
Br ⁸¹ , 1 = 3/2 (87M50)					(1)/2-) Br 87 (1)/2-) Br 87 (1)/2-	(67551)
	γ ₁ 0. 547, γ ₂ 0. 608, γ ₃ 0. 692, γ ₄ 0. 766, γ ₅ 0. 823, γ ₆ 1. 031, γ ₇ 1. 312 spect conv. spect (7849); γ ₁ 0. 535, γ ₂ 0. 602, γ ₄ 0. 750, γ ₆ 1. 220, γ ₇ 1. 292, γ ₈ 1. 445, γ ₇ 1. γ ₂ γ ₇ γ ₄ γ ₈ 2. 77. 5. γ ₁ 0. 0. 850, 40) spect (16052); 1. 0. 45, 1. 306, 1. 483 spect (571814); 1. 7. 2. 0 (0. 495) Bα-γ·n reaction 0. 71, 0. 03 sha conv (69844); others (32 MS);	no y (26837a, 33G5la); -0.046 (?) cl ch (50W52)	0. 89, 1. 89 acint spect (10 <u>L52d)</u>	по ү (63849)	y-y coinc (67851)	
	20D42b)	0.940 spect (23D51); 0.94 spect (25F52)	4.68 (40%), 3.56 (9%), 2.53 (16%) 0.89, 1.89 acint spect (10L52d) 1.72 (35%) spect (23D51)	2. 5 abs (63549)	p': (6755); n (mean); 0.25 abe paraffin (26148a); 0.30 p recoil in cl ch (71546)	
	35.87 h (31C50); 35.07 (6B550); 35.1 h (35W51); 35.7 h (35S51)	2.33 h (20140, 4945la); 2.4 h (3305la, 26537a)	30 m (65540); 32 m (23051); 33 m (32:(5))	3.00 m (63S49); 3.0 m (65S40, 70B43)	55.6 a (n) (2846a); 55.0 a (n) (4847); 56.1 a (F [*] ) (63549)	15. 5 • (63849)
	p* (33K35); no EC or p* no EC or 05K) no EC or 05K) no p* (lim 0,02K) (41M51)	p. (26537a)	p ⁻ (22D39)	p ⁻ (65840)	p. p. n (-2% of disinte- grations) (1915ia)	p ⁻ (63849)
49. 48 (9W46)						
	A chem, n-capt (13315); chem, excit, cross bomb (26537a)	A chem, excit (26537a)	A chem (22D39); chem, excit (70B43)	A chem (65840); chem, genet (66843;	A chem (65540, 2584); chem, genet (70B43, 63549)	A chem, genet (63549)
, a	20 L	8 8	2 td		75 gr	B. B.

									L. <i>4</i>
V Z	identification	shundanos	decay.	Half-life	Particles	General Camparana	Disinsegration energy and scheme	Method of production and generic relationships	
35Br 89	D chem (63847a)		p'. p'n (26547a, 28148a)	4. 51 e (n) (28146a); 4. 45 e (n) (34R47)	n (mean); 0.43 abs paradíin (28H46a); 0.65 p recoll in ct ch (71B46)			fission U (63847a, 26547a, 63549), U225 (14847, 28446a); parent Kr ⁸⁹ (7), parent Kr ⁸⁸ (7)	2
36 ^{Kr} 77	D chem, sep leotopee (35W48s)	0. 354 (6N5Oa)	EC 70%, p [†] 30% (35 W48a,	1.1 b (35W48a)	1.7 abs (35W48a)	y (35 W48a;		Se-e-n, Se ⁷⁴ -e-n (35W48e)	
Kr 79m	D chem (29C40b)		IT (?), no 6 ⁺ (29C40b)	55 • (29C40b)		0.127 spact conv (29C40b)	•	Br-p-n (33B40a, 29C40b)	
K, 73	A chem (29C40b); chem, esp isotopes (35W48a); mass spect (104.B52)		EC 95% (L/K 0.27), p ⁺ 5% (12852); 12852); EC (K) - 90%, p ⁺ - 10% (6783); EC (6783); EC - 96%, p ⁺ - 2% (35W48a)	34. s h (12852); 34 h (33840a, 35 W48a, 29C40b)	0.595 spect (67B31); 0.6 abe (58H31)	0, 263 (e/v, -0.02), 0.044 spect conv (67B31); 0, 2 abs (58H31)		5e-e-n (52C41); 5g ⁷⁶ -e-n (55W48e); Br-d- 2h (5C40); Kr-d-p (56S)7e, 59C40b; Kr-n-y (58H51, 67B51)	
Kr 80		2. 27 (6N50a)							
Kr 81m	A chem (29C40b); genet (7K50)		II, no p* (29C40b)	13 e (29C40b); -10 e (7K50)		0.193 spect conv (7K50); 0.187 spect conv (29C40b)	(1/2-) Kr81 0.19 (7/2+) Kr81 0.19	Br-p-n (33B40a, 29C40b); daughter Rb ⁸¹ (7K50)	
× ×	A chem, mass spect (28R50a)		EC (28R50a)	2.1 x 10 ⁵ y ap act (28R50a)		0.012 abs, Br K-x (28R50a)	(3/2-)(18652)	Kr-n-y (28R50a)	
Kr.82		11. 56 (6N50m)					Kr ⁸² , 1 = 0 (871/50)		
Kr 83#	A chem, genet (20140); mass spect (67B50)		II (20140)	114 m (67B51a, 21R46); 113 m (20L40)		0.0322 (a/y very large, K/L+M 0.35), 0.0093 (a/y very large, L/M - 3) spect conv (67851a); 0.032 (K/L 0.32), 0.009 (a/y -10) ion ch (91852); 0.046, 0.029 spect conv (2H41)	(1/2-) Kr 83m (1/2-) C O O O O O O O O O O O O O O O O O O	Se-a-n (\$2C41); Kr-d-p (\$2C41); Kr-n-y, Kr-x raye (37W45); fission U, daughter Br ⁸³ (20L40); daughter Rb ⁸³ (\$3C50)	REACTOR
χ. 8-7		11. 55 (6N50m)					Kr ⁸³ , I = 9/2 (87M50)	flesion U (mass spect)	Pn:
7		56. 90 (6N50a)					Kr ⁸⁴ , I = 0 (87M50)	fission U (mass spect)	BICB

Se-q-n (35 W 48a); Kr-d-p (26837a, 52C4); Kr-n-v (21R45, 58H51); Rb-n-p, Sr-n-o (70B43); ffesion U, daughter Br ⁸⁵ (6643, 5384)	K-n-v (58H51); fission U (13T47, 58H5la)	fission U (mass spect) (13747, 13748a); daughter Br ⁸⁷ (2% of dis) (26547, 63549)	Kr-n-y (21R46, 58H51); Kr-d-p (26537a); Rb-n-p (70843). (70843, 66543); daughter Br ⁸⁷ (66543, 70B43, 63549)	fission Th (20L39, 25A39), U (6H39, 16H40a, 36G40, 16H40b); Paren RB68 (20L39, 25A39, 6H39, 16H40a, 36G40, 16H40b); daughter Br ⁸⁸ (63S49)	fission U, parent Rb89 (36G40, 66S40, 16H40b, 16H43, 17B51, 35K51a); spall-fission U (10S1); fission Pu (26AS1)	fission U, ancestor Sr (24DSIa, 24DSI); fission Pu (26A5I); parent Rb ⁹⁰ (35KSIa)	fission U, ancestor Y 91 (16490c, 1785), 44D51a, 24D51); spall-fission U (11051); fission Pu (26A51) parent Rb9lm (35K51a)	fission Th (16H40), U (16H40s, 16H40s, 16H40b, 16H43), Pu (26A51); ancestor Y ⁹² (24D51)	fission U, ancestor Y 93 (70551); spall-fission U (11051); fission Pu (26A51)
(9/2+) Kr85m Q3i Q6 1.00 (9/2+) Kr85 Q3i Q6 1.00 (9/2+) Kr85 Q85m	500,186	Kr ⁸⁶ , I = 0 (87M50)	Q _p 3.6 (30752a) Kr ⁸⁷ (3/2-)	(307520)					
0.150 (e/y 0.057, coinc with p ⁷ ), 0.305 spect coav, p·y coinc (67B50a, 67B51d); 0.17, 0.37 ab= 188H51)	o 54 (coinc with 0. 15 ft") seint spect, abs. ft -y coinc (\$250)		(30T52a)	0.028 (coinc with 0.5 p°, e/y -0.1, K/L+M 8) spect conv, 5-y coinc (30T52b)					
0. 855 apact (67P5id); 0. 85 abs (70B43a); 0. 95 abs (56H51); 0. 75 abs (34K49)	0. 695 (994%), 0.15 (0.65%) spect, 6-y coinc abe (8250); 0.74 abs (58HSta)		3. 63 (75 %), 1. 27 (25 %) spect (30752a); others (34K49, 70B43a)	2. 77 h (34K49); 2. 8 (20%), 0. 9 (12%), 0. 52 (68%) 2. 8 h (36G40, spect (30752b); 63S49) 2. 4 (weak), -0.5 ab* (4J48,34K49)	4.0 abs (13K5la); 3.9 calc from average recoil energy (35K5l)	3. 2 abe (35K5la)	-3.6 abe (35K5la)		
4. 36 h (34k49); 4. 4 h (35W48a); 2. 5 h (36H3), 2.6537a); 4. 6 h (21R46, 66543)	9. 4 y (13T48a); -10 y (58H51a)		78 m (34K49); 5m (6654), 53549; 74 m (2637a)	2. 77 h (34K49); 2.8 h (36G40, 63S49)	3.18 m (35K51a); 2.6 m (24D51); 2.5 m (16H43a)	33 e (35K5la, 32K46)	9.8 • (24D51); 10 • (35K5la); -6 • (11O51)	3.0 • (24D51)	2.0 • (24D51)
6 77%, II 23% (67851d)	(\$8H8) g		p (26837a)	p ⁻ (20L39)	p ⁻ (36G40)	6 (24DSla)	6 (16H40c)	p (16H40a)	p ⁻ (16H42)
		17. 37 (6N50a)							
A chem (26337a); chem, mase spect (34K49)	A chem (59H5la); chem, mass spect (13T47)		A chem (26537a); chem, mass spect (34K49)	A chem (6H39); c.em., genet (2OL39); chem., mass spect (34K49)	A chem, genet (36G40, 66S40); mass spect (35K51a)	A chem, genet (24D5la); mass spect (35K5la)	A chem, genet (16H40c); mass spect (35K51a)	B chem, genet (16H40a, 24D51)	B chem, genet (16H42, 70851)
Kr. 85m	Kr 95	Ж. Ж.	X e	X 28 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	ž.	Kr 90	16 T	Kr 42	Kr. 93

	Pris and	1	Tomas		Reserv of rad	Recey of radiation in Mey		Meshed of renduction and
V Z	identification	abundance	decay	Half-life	Particles	Gamme-transitions	Distangration energy and echanic	genetic relationships
36 Kr 94	B chem, genet (16H43a, 24D51)		p* (16H43a)	1.4 • (24D51)				fission U, ancestor Y ⁹⁴ (16H43a, 24D51)
Kr 95	A chem, genet (24D5la)		6 (24D5la)	short (24D5la)				fission U, ancestor Zr 95 (24D5la)
Kr 97	B chem, genet (26A51)		p_ (26.A51)	-1 • (24D51)				fission U, ancestor 2r ⁹⁷ (26A5i, 24D5l); fission Pu (26A5l)
1								
37Rb 81	A chem, mass spect (10R49)		EC 87%, p ⁺ 13% (7K50)	4.7 h (7K50)	0.990 spect (7K50)	0.95 abs (7K50)		Br-a-2n (10R49, 7K50); parent Kr ⁸¹ (7K50)
Rb 82m	B chem, genet (54L52)		p* (54L52)	1. 25 m (54L52)	-3 abs (54L52); see Sr			daughter Sr ⁸² (54L52)
RP PS	A chem (59H40); chem, mass spect (10R49)		EC 94%, B*6% (7K50)	6. 3 h (7K50)	0. 773 (76%), 0.175 (24%) spect (10H52); 0. 670 spect (7K50)	0.188, 0.248, 0.322, 0.390, 0.423, 0.465, 0.558, 0.610, 0.690, 0.768, 0.818, 1.020, 1.314, 1.464 spect conv. spect (10H5.)		Br-a-n (59H40, 10R49, 7K50); Kr-d-2n (59H40); not daughter Sr ⁸² (lim 0.01%) (54L52)
37 ^{Rb} ⁸³	A chem, mass spect (7K50)		EC (7K50)	83 d (53C50); 107 d (7K50)		-0.45, -0.15 spect conv (53C50)		Br-a-2n (7K50); daughter Sr ⁸³ (53C50); parent Kr ^{83m} (53C50)
Rb 84m	B chem (59H40); chem, excit (9F50a)		IT, EC (weak) (79C52); EC (9F50a)	IT, EC (weak) 23 m (9F50a); (79C52); EC (9F50a)		$y_1$ 0. 463 (not coinc with $y_2$ or $y_3$ ), $\gamma_2$ 0. 239, $\gamma_3$ -0. 239 (coinc with $\gamma_2$ ), $\gamma_4$ 0. 890 $(y_1/\gamma_4 = 7)$ scint spect, $\gamma$ - $\gamma$ - $\gamma$ -coinc (19C52)	Rb84m 0.463 (2-) Ayel -0.24 EC	Br-a-n (\$9440); Rb-n-2n (9F50a, 79C52)
48 44	A chem, cross bomb (63B47); chem, mass spect (7K50)		EC, 6 ⁺ , 6 ⁻ (?) (7850, 73B50); EC/6 ⁺ -13 (7K50); 6 ⁺ /6 ⁻ -6.2 (73B50)	34 d (7K50); 38 d (73B50)	p*: 1.629 (19%), 0,822 (18%), 0.373 (?) (13%) spect (10H52); 1.5 spect (7K50); 1.3 abs (73B50)	0.890 scint spect, spect conv (10H52); 0.85 abs (7K50); 0.8 abs (73B50)	(EC.9)	Br-a-n (7K50, 73B50); Kr-a-pn, Kr-d-2n (73B50); Br-n-ân (63B47); Sr-d-a (63B47)
1				4			(0+) (10H32, 79C32)	<b>S</b>
Rbeam	A genet (14552)		IT (14552)	0.9 x 10 s delay coinc (14552)		0.513 spect, spect conv (11T5), 14S52)	see Sr and Kr	daughter Sr (14852)
26 ds		72. 15 (6N50a)					Rb ⁸⁹ , I = 5/2 (87M50)	fission U (mase spect) (38W52)
Rb 86m	B chem, excit, n-capt (9F51)		IT, no EC (12P52); EC (9F51)	0.99 m (12P52); 1.06 m (9F51)		0.57 acint apect (12P52); 0.78 abs (9F51)		Rb-n-y, Rb-n-2n (9F51)

NUCLEAR PHYSICS				CHAP. 1.2
Rb-n-v (26537a, 69538, 2547); Rb-v-n (34444); Sr-d-a (2244ia); spall-frasion Bi (iliG49, 6685)), fission U (2F5ia)	natural source (1705, \$4006); fission U (mase spect) (18W52); parent Sr ⁸⁷ (mass spect) (16H37a, 8M37)	Rb-n-y (2637a, 1P37, 69538, 2547); fission Th (25A39); Ps (2G39); fission U, dauphter K-88 (6H39, 20L39, 36G40, 16H40a, 16H40b)	fission U, daughter Kr 89 (16640, 16640), 17851; 16443, 17851; parent 89 (15640, 16440a.	fission U. daughter Kr 90, parent Sr ⁹⁰ (24D51a, 24D51, 35K51a)
Rb 66, 1 - 2 (98851) Cp 1. 8 (5248) (2-) Rb 86 (2-) Rb 86 (04) (04) (04) (5248, HPS)	(3.72-) Rb ⁸⁷ (3.72-) Rb ⁸⁷ (3.72-) Rb ⁸⁷ (9.21) (2.1051, 73M52)	Cee y 88 (2-) Rb 86 (2-) Rb 86 (1-) Rb 86 (1	(2851, 30752b, HPS)	
. 076 spect (55M50); 1. 081 spect (5248); 1. 12 (coinc with \$2) coinc abs sec, 5-y coinc (15348); others (85551)	no y (21CS1, 79MS2, 50L52)	2. 8, 1. 86, 0. 90 spect (2B51); v ₁ 3. 0. v ₂ 1. 7 (y/V ₂ - 1/10) abs sec, 6-y coinc (37G51)	y (35B462)	Y (35K51a)
β ₁ 1. 82 (80%), β ₂ 0. 72 (20%) spect   .076 spect (55.48);   .081 spect (52.48);   .081 spect (52.48);   .081 spect (52.48);   .081 spect (56.48);   .081 spect (53.48);   .081 spect (53.48);	. 275 spect (21C51); scint spect (50L52); . 270 scint spect (11B50s); there (36K35, 34T52, 3.139, 14O41, 12546)	5.30 (78%), 3.6 (13%), 2.5 (9%) apect (30T52b); 5.31 (66%), 3.29 (19%), 2.0 (15%) apect (2583); 5.20 (-66%), 3.6 (-17%), 1.8 (-17%) abs (37G51)	4.5 abs (35£46a, culc from 36G40); 3.8 abs (36G40)	5.7 abs (35K5la)
19. 5 d (2H4la)	6.0 x 10 l0 y ap act (37H48 37K49.s.c. 2 x 10 l0 y ap act (19M52); 6.4 x 10 l0 y ap act (21C5); 7.6 x 10 l0 y y (55C3); calc (21C5); 6.3 x 10 l0 y y yield (65S3); 6.3 x 10 l0 y y act (10E46)	17. 8 m (36.040, 28.51); 17. 7 m 17. 7 m 18.04.22); 18.44.21; 18.m (16.14.40, 26.517a)	15.4 m (36G4Q; 15.5 m (16H40b)	2.74 m (35K5la)
6 (2.841a); 80 6 (11mm 90 002.50; 61.M51); 80 EC (11m 90.06.50; (12.P52)		p. (16H39a.)	6 (36G40)	p (35K5ia)
	27. 85 (6NSO _{b.} ) p ⁻ (1TOS, 54CO6)			<u> </u>
A chem, n-capt (2657a); chem, excit (2H4ia)	A chem (1705, 54C06); chem, genet (16H37a, 8M3); chem, mass spect (40H37)	A chem (26537a); chem, genet (20139, 36G40, 16H39a)	A chem, genet (36G40, 66S40)	A chem, genet (35K5la)
2 4	R	** ***	R S S S S S S S S S S S S S S S S S S S	06 da

1	Las and	- Berry	Twee		Freeze of radi	Energy of radiation in May		Market of the state of the state of
V Z	identification	abundance	decay	Half-life	Particles	Gemma-transitions	Disintegration energy and scheme	genetic relationships
37Rb ⁹¹	A chem, genet (35K5la)		p (35K5la)	1. 67 m (35K5la); [ahort] (24D5la, 17B5l, 1105l, 24D5l, 16H40c)	4. 6 abe (35K5la)	y (35K5la)		fission U, daughter Kr91, parent Sr ⁹¹ (13651a); ancestor Y ⁹¹ (24D51a, 16H40c)
Rb 91	A chem, genet (35K5la)		p* (35K5la)	14 m (35K5la)	3.0 abs (35K5la)	y (35K5la)	•	fission U, daughter Kr ⁹¹ , parent Sr ⁹¹ (35K5la)
Rb ⁹²	D chem. genet (16H40a)		6 (16H+0a)	80 e (16H40a); [shord] (17B\$1, 24D\$1)				fission U, daughter Kr ⁹² (24D51); ancestor Y ⁹² (16H40a, 16H40c, 16H40,16H43, 24D51)
Rb93	[B] genet (16H42, 17B51)		[p_] (16H42)	[short] (17B51, 24D51, 24D51a, 16H42,16H43)				fission U, daughter Kr ⁹³ (1785i, 24D5i, 24D5is); ancestor Y ⁹³ (16H42, 16H43, 17B5i)
Rb 94	[B] genet (16H43. 16H43a)		[6-] (16H43, 16H43a)	[short] (24D51, 16H43, 16H43a)				fission U, daughter Kr ⁹⁴ , ancestor Y ⁹⁴ (16H43, 16H43a, 24D51)
Rb95	[A] genet (24D5la)		[6] (24DSIa)	[short] (24D5la)				fission U, daughter Kr ⁹⁵ , ancestor Zr ⁹⁵ (24D5la)
Rb 97	[A] genet (24D51)		[p] (24D51)	[short] (24D51)				fleeion U, daughter Kr97, ancestor Zr97 (24D51); fleeion U ²³⁵ , Pu (26A51)
38 ^{Sr} ⁸¹	B chem, genet (53C50)		EC, p* (53C50)	29 m (53C50)	conv (53C50)			epail Rb, parent Rb (53C50)
Sr 82	A chem, excit (53C50); mass spect (97M52)		EC, p+ (?) (53C50)	27 d (97M52); 25 d (53C50)	p ⁺ with Rb ^{82m} (54L52); 3. IS spect (53C50)	0, 95, -0, 40, -0, 15 spect conv, abs (53C50)		epail Rb (53C50); daughter Y 82 (78C52); parent Rb 82m not parent Rb 82 (lim 0.01%) (54L52)
Sr 83	A chem, genet (53C50); mase spect (97M52)	(\$1.09) 45 O	EC, B [↑] (53C50)	33 h (97M52); 38 h (53C50)	1. 15 spect (51C50); 1. 35 abs (97M52)	0.040, 0.074, 0.101, 0.151, 0.165 spect conv (53C50)		epail Rb, parent Rb ⁸³ (53C50); daughter Y ⁸³ (78C52)
8r 85m	A chem, excit (2D40a)		IT 86%, EC 14% (14S52)	70 m (2D40a)		0. 0075 (e/y very large), 0.150 (with EC), 0.225 (e/y 0.03), K/L -5.5), 0.231 (e/y -0.04) acint spect, spect conv. x-y coinc (4522); 0.233, 0.152 spect conv (1151)	*** Kr ⁸⁵ (W2-) Sr 85 m C(233 (Pre-) 1 1602 C(225 (87**) 52 80 (87**) 75 C(225)	Rb-p-n (2D40a); Rb-d-2n (11751); Sr ⁸⁴ -n-y (14S52)
80 20 20	A chem, excit (2D40a)		EC (3515), IIT51); no p* (IIT51)	65 d (11751); 66 d (2D40m)		~*	(3/2-) (14552, 18652)	Rb-p-n (2D40a); Rb-d-7a (11751, 35L51, 2E52); parent Rb ⁵⁵ m (14552); daughter Y ⁶⁵ (78C52)

NUC	CLEAR PHYSICS						CHA
	Rb-p-n (2D39); Sr-n-n (2D40a, 15R40, 5FX40a); Sr-x rsys, Sr-e-e (37W45a); Sr-n-y (71S37, 2D39, 3SR40, 2S47, 2S47a, Aughter Y (8 (2D39, 2D40a, 5M40, 18H5b, 58M5);		Sr-d-p (71537, 71539); Sr-n-y (71537, 71539, 2547); Ya-p (4258); pall-fission Pt (2747b), Pb (13947a), Bi (2747b, IIGA9, 66851), Th (71094), U (6648, 11057, 5751); U (6648, 11057, 5751);	(38C48, 61S48), U ²³⁵ , (38C46), Pu (28F51); fiasion U, daughter Rb ⁸⁹ (36C40, 16H40a, 16H40b, 16H43, 38C46)	apall-fission Bi (11C49), Th f7N4ai; Th f7N4ai; (13648), U233 (13648), U233 (13648), U233 (13648), U233 (13648), U333 (13648), U3442 (13648), U3442, U34422, U34	Zr-n-a (66543a); spall-friesion P (1247b), Hg (**) (5352), Pb (11947a), Bi (11947a, 11947, 6685i), U (**) (1345i), U (**) (1345i), Pu (\$12848, 2885i); fasion U, parent Y9lm, parent Y9lm, parent Y9lm, (46044), (4643, 2875a); Z875a); Z875a);	
Sr 86, 1 = 0 (87M50)	(1/2-) Sr ^{87m} 0.390 (19/2+) 0.390	Sr ⁸⁷ , I = 9/2 (87M50) Sr ⁸⁸ , I = 0 (87M50)	0, 1.46 (101.49)	(1/2-)	Q _p 0.6 (HPS) (04) Sr90 (104) Sr 90 (104) Sr 90 (104	0p 2. 66 (40A52)	(40452)
	0. 188 (K/L+M 5. 79) spect conv (19G52); 0. 390 (eV, v. 20, V.L+M 6. 9) espect conv. x-conv color (19M5); 0. 188 (K/L+M 5. 5) spect conv (19B5); 0. 194 (K/L 7. 2) spect conv (18H5); 0. 194 (K/L 7. 2) spect conv (18H5); 0. 86 spect conv (12H1)		no y (1NS1, 71539, 71537); othere (52MS1)		no y (33GSic. 39G43)	0 . 551 (with Y ^{91m} , K/L+M 6. 0), 0. 64, 0. 64, 0. 74, 1. 1025, 1. 1, 13 (coinc with 0. 630 Y) spect, i-th spect, y-y coinc (40A52)	
			1. 463 apect (10L49); 1. 48 apect (17N44); 1. 5 apect (72549, 4W44, 11R47); cl ch (71539)		0. 61 apect (47M48a); 0. 54 apect (23L50); 0. 53 apect (24R49); 0. 6 abs (38G46, 33G51c)	2.665 (26%), 2.03 (4%), 1.36 (29%), 1.09 (13%), 0.62 (7%) apect (40A52); 3.2 (-60%), 1.3 (-40%) abs (28F5la)	
	2. 80 h (58M5), 6H5ib); 2. 75 h (2D40a)		53 d (IN51); 54 d (361.39); 55 d (71539, 11G49)		19. 9 y (28P50)	9, 7 h (28F51a); 10 h (16H43)	
	IT (2D40a)		p ⁻ (71 <u>\$</u> 37)		p' (18N51)	p (40G41)	
9.86 (6N3Bb)		7. 02 (6N38b) 82. 56 (6N38b)					
	A chem, excit (713.7); chem, excit, cross bomb, genet (2D40a)		A chem, excit (71537); chem, mass spect (60H48)		A chem, genet (16H42); chem, mass spect (60H48), 38 W 5.)	A chem, genet (40C41); chem, excit (66S43a)	
3,96	e	Sr 87	8 r		06 ts	Sr 91	

			,		Warner of marinifactor of second	listics in Mes		Market of confession and
Y Z	identification	abundance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
38Sr ⁹²	B chem, genet (40G41)		p* (40G41)	2. 7 h (40G41)				apall-fission Th (7N49a); fission Th (72BS1), U (16H6da, 16H43, 16H43a, 3XK51a, 17BS1), Pu (2XK4b); parent Y9 ² (40G41, 58HS1b)
Sr 93	B chem (36L39); chem, genet (16H43)		p_ (36L39)	7 m (36L39)				fission U (36L39, 16H42, 16H43); parent Y93 (16H43, 16H43a)
Sr. 94	B chem, genet (16H43, 16H43a)		p (16H43, 16H43a)	-2 m (16H43, 16H43a)				fission U (16H43, 16H43s, 24D51); parent Y94 (16H43, 16H43s)
Sr 95	[A]genet (24D5la)		6 (24D51≜)	short (24D51a)				fission U, ancestor Zr95, descendent Kr95 (24D51a)
Sr 97	[A] genet (24D51)		<b>6</b> (24D51)	short (24D51)				fission U, ancestor Zr97, descendent Kr97 (24D51, 26A51)
39 Y 82	B chem, genet (78C52)			70 m (78C52)				spall Y. parent Sr ⁸² (78C52)
γ,83	B chem, genet (78C52)			3.5 h (78C52)				spall Y, parent Sr 83 (78C52)
¥84	B chem, excit, aep isotopes (36R49)		p ⁺ , EC (36R49)	3.7 h (36R49)	2.0 abs (36R49)	y (36R49)		Sr ⁸⁴ -d-2n, Sr ⁸⁴ -p-n (36R49)
¥85	B chem, genet (78C52)			5 h (78C52)				spall Y, parent Sr85 (78C52)
39 Y 86	B chem, excit, sep isotopes (53C51)		p ⁺ (53C51)	14. 6 h (53C51, 8H51b)	1.80 (-50%), 1.19 (-50%) spect (8H51b)	l. 4 abs (8H5lb); -l. 3 abs (53C5l)		Sr-p-3n, Sr ⁰⁸ -p-3n (53C51); spail Nb, daughter Zr ⁸⁶ (8H51b)
γ ⁸⁷ m	A chem (71839); chem, excit, cross bomb (2D40a)		IT (2D40a); no B*(8H5lb)	14 h {2D40a, 8HSib,58MSi}		0.381 (K/L+M 5.41) apect conv (59G21); 0.384 (e/v .28) apect conv, ion ch, conv-x colnc (58M51); 0.389 apect conv (8H51b); conv >1 (58M51); conv >1 (8H51b)	(1/2-) Y87m 0.384	Sr-d-n (71539, 2D40a, 58M50, 58M51); Sr-p-n (2D40a, 58M51); epail No. dunghter Zr ⁶ f (8H51b); parent Y ⁶ f (58M50, 8H51b, 58M51)
,	A chem (71539); chem, excit. cross bomb (2D40s)		EC 99+%, p0.3% -0.3% (36MS)); EC, p' (weak) (36R50)	80.0 h (58M51); 80 h (2D40a, 8H51b)	0.7 apect (58MS), 36RS0)	0. 485 (e/y 0. 0035) spect conv, scint spect, y-x coinc (58M51); 0. 390 (with Sr 87m)	(1/E-) Syd7m C.875 (1/E-) Syd7m C.390 (9/E+) C.390 (2/E+) (58M51)	5r-p-n (2D40a, 58M5)); 5r-d-n (71539, 2D40a, 5.8M51, 58M50) 5r-d-a-p (58R50); spal (70, 100, 100, 100, 100, 100, 100, 100, 1

Sr-d-2n (29P40, 2H42, 41G44, 17B50); Sr-p-n (2D40a); Y-n-2n (2H42, 10046); daughter Zr ⁸⁸ (8H51b)	Sr-d (71537, 71539); Sr-p (2040b, 2040a); Y-n (71537)	Y-n-n, daughter Zr ⁸⁹ (18G51)	Y-d-p (71537); Y-n-y (71537, 4258, 2547); Z-n-p, Zr-d-a (42540); Nb-n-a (42518a, 42540a); ppall-fission Pt. T1 (2T47b), Bi (13p47, 11C49); fission T1, (2T47b); fission U, daughter Sr 90 (16H42, 16H43, 38C46, 18N51)	Zr-n-p (66543a); fission U, daughter Sr ⁹¹ (40G41, 16H43, 28F51a)	Zr-n-p (66543a); spall Sb (37L50); U (11051); U (11051)
Cp 3.70 (6P48)  Cp 3.70 (6P48)  F(4-1)  F(4-1)	\$	(1/2-) (1/2-) (1/8-52) (18652)	Q _p 2.18 (10L49) (2-) +90 (0+) (14B49)	*ee Sr ⁹¹ (9/2+)	(1/2-) 491 0.29.1% 1.4 0.00% (10L49) (5/24) (5/24) (10L49) (5/24) (10L49, 28F 5ig, 40A52)
0.908 (e/y 0.0003), 1.853 (e/y 0.0001), 2.76 spect conv. spect (EP48); -0.9 (e/k/y 0.00034), -1.85 (e/k/y 0.00017) spect conv (44M52b); -0.908, 1.89 spect, y-y-coinc (2504); -1.87 Be-y-n reaction (17541); 2.8 (-1%) D-y-n reaction (41G44)		0. 913 spect conv (73531); 0. 917 spect conv (8451b); -0. 9 (K/L+M 7.0) spect conv (79852); 0. 92 (e/y, 0. 01) spect conv, scint spect (74551, 18G51)	no y (13GSic, 74B49, 39G43); 1.4 (0.4%) abs (115S52); others (52M5i)	0.551 (K/L+M 6.00) acint spect (59G52); 0.61 (e/y - 0.1) abs, abs conv (28F51a)	1. 2, 0. 2 (both <0.1%) abs. coinc abs sec, y-y coinc (10L/4)
0.83 spect (6P48)			2. 18 spect (101.49); 2. 24 spect (121.50); 2. 25 spect (748.49); 2. 2 spect (948.43); 2. 2 spect, abs (13.55); E (average) 0. 90 ion ch (77.52)		1, 537 spect (101.49); 1, 54 spect (150.49); 1, 55 spect (16.W49c, 24K49); 1, 56 spect (16.K50, 96.W52)
105 d (2D404);	2.0 h (71S39)	-14 (18G51)	61 h (37B46, 71837); 62 h (18N51) 65 h (18N51)	51.0 m (28F5la); 50 m (40G4l)	61 d (38C46, 101.49); 16 H (40C41, 16 H (40C)
EC (2D40a), EC 99+%, 6 0.19% (6P48)	6 (71537)	IT (18G51)	p ⁻ (71537)	IT (40G41)	g (16H40c)
		(6501) 001			
A chem (2D40a); chem, excit (2H42); mas spect (60H48)	G not found: chem, cross bomb, sep isotopes (36R49)	A chem. genet (18G51)	A chem, excit, cross bomb (71837); chem, mass spect (60H48)	A chem, genet (40G41)	A chem, genet (chedoc, ibl443); chem, mass spect (72851a, 60H48)
® ® ⊁	¥88	т ⁸⁹ т	06 X	т 16 <b>ү</b>	16 Å

- Second	Con and	Percent	Type of		Reserved radiation in Mer	ation in Mev		
V Z	identification	abundance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
39 Y 92	B chem (36L39); fission fragment range (32K48)		p_ (36L39)	3.60 h (40A52a); 3.5 h(28A43, 16H43a, 36L39)	3. 60, 2. 7, 1.3 spect (40.65a); 3. 5 abs (58.95b); 3. 4 abs (40.64b); 3. 6 abs (70.843a)	0. 6 abs (40C41); 0. 7 - 1. 1 abs (58H51b)		Zr-n-p (42540, 66543a, 28A43); fission Tb (16352); fission Tb (72251), Pu (12K48); fission U, daughter Sr ⁹² fission U, daughter Sr ⁹²
Y 93	B chem (16H43, 72B46, 72B51b, 70S51); fission fragment range (32K48)		p (72B51b)	10. 0 h (72B51bk 11. 5 h (16H43)	10. 0 b (72B51bk 3. 1 abs (72B51b) 11. 5 b (16H43)	0.7 abs (72B5lb)		apall-fission U (6048); fission Th (72851), Pu (32k48); fission U, daughter Sr ⁹³ (16443, 16443a, 72851b)
**	B chem (16H43, 16H43a); fission fragment range (32K48)		p (16H43, 16H43a)	16. 5 m (75B49); 20 m (24D51b, 16H43)	5.4 abs (75B49)	l. 4 abs (75B49)		Zr-n-p (66543a); flasion U (16H43,16H43a, 24D51b), Pu (32K48); daughter Sr ⁹⁴ (16H43,16H43a)
¥95	B chem, sep isotopes, excit (20K49)		6 (20K49)	10.5 m (20K49); <1.5 h (70S51)				Zr ⁹⁶ -y-p (20K49)
76Å	[A] genet (24D51)		p (24D51)	short (24D51)				fission U, descendent Kr., parent Zr97 (24D51, 26A51)
	[B] chem, genet (8H51b)		EC (8H51b)	-17 h genet (8H5lb)				spall Nb. parent Y ⁸⁶ (8H51b)
2,87	A chem, excit, sep isotopes (36R49); chem, genet (8H51b)		B. EC (36R49)	94 m (8H5lb); 120 m (36R49)	2.10 apect (8H5lb); 2.0 abs (36R49)	0.65, 0.35 abs (36R49)		Sr-a-n, Sr ⁸⁴ -a-n (16R49); spall Nb, parent Y ⁸⁷ m (8H51b); Mo-y-an (85H52)
Zr 88	B chem, genet (8H51b)		EC (8HSIb)	85 d (8H52)		0.406 spect conv (8H51b)		spall Nb, parent Y ⁸⁸ (8H51b)
2. 89 m	A chem, excit (2D40a)		IT, p* (weak)	1. 5 m (2D40a)	2.5, -0.85 (both weak) (p ⁺ /0.59 y = 0.004) spect, scint spect, p-y coinc abs (73551, 73552)	0.586 (e/y 0.07, K/144M 5.4) acint apect, apect conv (79852, 73851); 1.53 (-7%) acint apect (73552)	0 -3.4 Zr 89m	'-p-n (2D40a); Zr-n-2n (?) (28A43); Zr-y-n (73SSI)
2r 89	A chem, excit (42538, 2D40a)		EC -75%, p+-25% (18G51)	79. 3 h (74551); 77 h (8H51b); 78 h (2D40a); 80 h (itO43)	0, 910 spect (8H51b); 0, 905 spect (74551); 0, 890 spect (73551)	v (with Y89m); 0.92 (e/v 0.01) spect conv, acint spect (Y851); 0.913 spect conv (3451); 0.917 spect conv (8451b); -0.9 (K/L+M 7.0) spect conv (79B52)	(8.24) 12.00 6.15 1.53	Y-d-Zn (1104), 18G51); Y-p-n (2D40a); Zr-n'n (4258, 42540); Zr-y' (73551); spall , y (8H51b); Mo-n-c (42540); parent Y ⁸⁹ m (18G51)
							(W.P.) 0.913	
22,90		51. 46 (24W48)					(73851, 73S52, HPS)	

flesion U (6.1550, 76.1950); parent N6.93m (33.053)	Zr-n-v (42540, 2547); Zr-d-p (42540, 20151); Mon-a- (42540); Th (7M49a); Th (7M49a); Th (7M49a); Fu (28F51); Giasion U, parent (-1%) Nb ^{95m} ; parent (-99%) Nb ⁹⁵ (22F61); ITSSia, 20151, 6ISSIb)	Zr ⁹⁶ n-v (50B50a, 26M52); Zr-n-v (42340, 2547); Mo-n-a (42340); papil-fasion Bi (6B51), Th (7N49a), U (6047); Iffasion T (21751), U (2047); bi H4lab, Pu (32K48) parent Nb ^{97m} (50B50a); descendent Kr ⁹⁷ (24D51)	Zr-n (24C52)	Zr-d-Zn (20151); Zr ⁹⁰ -d-Zn (29K49); Mo-d-a (20151); Moy ² -d a (29K49, 76B49b); Moy-pn (22E3); daughter Mo ⁹⁰ (43D52)
2, 1 - 5/2 (87M50) Q 0.063 (33G53) (3/2+) Zr93 (3/2+)	2, 95 3/2+) Z, 95 3/2+) Z, 95 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2-) 1/2> 1/2> 1/2> 1/2> 1/2> 1/2		(97E+) 4Nb 0	
no y (33G53)	0.721 (e/y 0.0024), no 0.92 y gett, apett conv (5552); 0.73, 0.92 (7) apett conv (17N31); 0.88 abe (17B51a); 0.91 coinc abe sec (26M48a); others (52M51)	with Nb 97m; 0.747 (e/m; conv, p-y coinc, y-y coinc, p-conv coinc (\$0890a)	-0. 50 scint spect (24C52)	0.14, 1.14, 2.23 acint spect (76B5id); 2.0 abs (29K49)
0.063 scint spect (33G53)	(5523): (5523): (0.39 (98%), -1.0 (2%) spect (1781): 0.365 (95%), -0.06 (weak), -1.1 (weak) spect (8531b): 0.4 (96%), -1.0 (2%) abs (1785.31): 0.40 abs (26.8488): 0.40 abs (26.8488): 0.40 abs (26.8488):	1. 91 spect (50B50a); 1. 9 abs (75549); 2. 2 abs (32K51b); 2. 5 abs (26M52)		15. D h (29K49); 1. 2 abs (29K49); 15 h (76B49b); -1. 7 abs (76B49b)
9.5 x 10 ⁵ y sp. act (33G53)	65 4 (1785ia, 38G46); 66 4 (2G48); 63 4 (42540)	17. 0 h (50B50a, 26M52, 32K51b, 2G40)	0.83 m (24C52)	15. 0 h (29K49); 15 h (76B49b); 18 h (20J51)
6 (61550)	p' (42540)	6 (2G40)	IT (24C52)	p [→] (20151)
11. 23 (24W48) 17. 11 (24W48)		2. 80 (24W48)		
B cham (61350)	A cham (2G40, 42840); cham, genet (39G5)	A chem (2G40); chem, n-capt, chem, sept. fobs0a, 26M52)	E (24C52)	A chem, excit, cross bomb (2035); chem, sep isotopes, cross bomb (76849)
2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	\$	2r 96 2r 97	E. 12	06 qu 14

Isotobe	Class and	Percent	Type of	- 14 11¢	Energy of rad	Energy of radiation in Mev		Method of production and
Y Z	identification	abundance	decay	TIMIL-TIME	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
Nb 91m	A chem, excit. (20151); chem, sep isotopes (16051)		IT (76B49b)	64 d (76B49b); 60 d (20J5l)		0.1045.(e/y -50, K/L 2.1) spect conv, scint spect (16031); 0.105 (K/L+M 2.1) spect conv (4P51); Nb x (76B49b, 16051)	(9/2+) Nb9Im (1/2-) (1/2-)	Zr ⁹⁰ -d-n (16051); Zr-d-n (20351); Mo ⁹⁴ -d-an (76B49b)
NP ₉₁	B genet (16051)		(16091) [EG]	long (16051)		Z; x (16051)	(5/24)	$\left[ Z_1^{90}$ -d-n, daughter Nb $^{91m} \right]$
Np 92	B chem, excit (8352a)		EC (8J52a)	-13 h (8J52a)		2.35 scint spect (8J52a)	(18 G 52)	Nb-p-pn (8152a)
NP 92	A chem, excit (42538a)		EC, no β ⁻ (lim 0.05%) (4P5l); EC, no β ⁻ (8J52a)	10.1 d (29K47); 9.8 d (60M48); 11 d (42S40a, 42S38a)	0 (7); 1, 3 cl ch (42540a), abs (29K47); 0.6 abs (59M44)	0.930 (with EC) spect (4P51); 0.933, 1.84 (weak) scint spect (18T52); 1.0 abs (59M4, 29K47); Zr-x (1P45)		Y -a -n (1P45); Zr -p -n (59M44); Nb-v-n (60M48, 22E52); Nb-n-2n (4233a, 42540a); Nb-d-c (37W46, 29K47); Mo-n-p (42804);
Nb 92	G not found: chem, excit (76B49b)		p (37W46)	21.6 h (37W46)			E 6914	Nb-d (37W46)
Nb ^{93m} Nb ⁹³	B genet (33G53)	100 (37S36a)	IT (33G53)	3.65 y (33G53)		0.0292 (e/y very large, K/L 0.14) spect conv (33G53)	(9/2+) $(9/2+)$ $(9/2+)$ $(9/2+)$ $(9/2+)$ $(9/2+)$ $(9/2+)$ $(9/2+)$ $(9/2+)$ $(9/2+)$ $(9/2+)$ $(9/2+)$ $(9/2+)$ $(9/2+)$ $(9/2+)$ $(9/2+)$ $(9/2+)$	daughter Zr ⁹³ (33G53)
Nb ^{94m}	A n-capt, excit (1P37, 42538a, 18G46b, 29K46)		IT 99+%, β -0.1% (18G46b)	6. 6 m (42S40a)	6. 6 m (42540a) 1.3 abs (18G46b)	0.0415 (e/y large, K/L/M = 0.31/ 1.00/0.36) spect conv (42C50); 0.056 (e/y large) abs conv (18G46); 0.9 (weak) scint spect (36M51a); Nb K.~x (18G46b)	(3,4-) Nb94m (6,74) Nb94 0,042	Nb-n-y (1P37, 42518a, 42540a, 18G46a, 18G46b, 2547); Nb-d-p (29K46, 37W46)
26.00	[A] n-capt (18G46b); chem, n-capt (63H52)		[p](18G46b)	>5 x 10 ⁴ y yield (63H52); >>100 y yield (18G46b, 18G48a)			(18652)	Nb-n-y (18G46b)
NP 95m	A chem (13E46, 13E5la); chem, genet (61S5lb)		IT (61SS1b)	90 h (61851b, 62H49); 84 h (5852)		0.231 (e/y very large) spect conv (5552); 0.232 (K/L+M -3.5) spect conv (4P91); 0.216 (e/y very large) spect conv (6AH49); Nb K-x (6IS51b)	see Zr95 (04) 00 00 00 00 00 00 00 00 00 00 00 00 00	Mo ⁹⁷ -d-a (76B49b); fission U, daughter (-1%) Zr-95 (62H49, l7B51a, 20J51, 61S5lb); spall-fission U (6F51); parent Nb ⁹⁵ (61S5lb, 19L51)
26 an	A chem (39G46, 39G51); chem, excit, cross bomb (20J51)		g (39G51)	35 d (13E51b); 37 d (20J51)	0.160 spect (29F52); 0.159 spect (35S1b); 0.48 spect (25S1b); 0.146 spect (22H49); 0.15 spect (17N5ia); others (26M48b)	0. 745 (e/y 0. 0024) spect, spect conv (5552); 0. 758 (e/y 0. 002) spect, spect conv (52H49); 0. 77 (e/y 0. 0016, K/L = 4) spect conv (29F51); 0. 77 spect, spect conv (17N51a); 0. 75 spect conv (11847)	Qp 0.91 (5852) (9/24) (5552)	Mo ⁹⁷ -d-a (76B49b); Mo-d-a (20J3); spall-fission [66B5]), U (65S); fission U, daughter (-99%) Zr ⁹⁵ (62H49, ITB51a, 61S51b)

Zr 96 -p-n (29K492); Mo 98 -d-a (76B31); spall-fission Bi (66B3); fission U (68C51a)	Mo ⁹⁸ -y-p (50B50a); daughter Zr ⁹⁷ (50B50a)	Mo-n-p (42840); Mo-y-p (428447, 12P46, 22E52); fission U (2C40, 32K51b), Pu (32K51b); spall-fission U (6F51)	Mo ¹⁰⁰ -d-a (76B49b)	Mo ¹⁰⁰ -y-p (23D50)	spall Nb (43D52); parent Nb ⁹⁰ (43D52)	Mo-y-n (37839, 25848, 22852) 22852, Mo-n-2n (6137, 42538, 42540, 30852); Mo-y-z-n (25849); Mo ² Z-y-n (23049)	Mo ⁹² -y-n (23D49); Mo-y-n (25W48)		Zr 90-a-n (2985a); Zr-an (128854); Nb-d-10 (128854); Nb-d-2n (12885, 176B52b); Nb-d-2n (12885a); Mo ⁹ -n-2n (12885a); Mo ⁹ -n-2n (12885a); Mo ⁹ -n-7n (121049); Mo ⁹ -y-n (121049); Mo ⁹ -
Q, 3.16 (4P51, 74851a)  se Tc 96  NB 96  F 87% 61% 63%  (4P51)  (4P51)	(1/2-) Nb ^{97m} (1/2-) Nb ^{97m} (1/2-) Nb ^{97m}	(777+) (577+) (18652)						Mo ⁹² , I = 0 (87M50)	
0. 216 (7%, e/v <23 × 10 ⁻³ ), 0. 238 Q _p 3. 16 (4PS1, 74SS1a) (10%, e/v < 16 × 10 ⁻³ ), 0. 543 set Tc? 96 (27%, e/v 4 × 10 ⁻³ ), 0. 560 (61%, e/v 1.7 × 10 ⁻³ ), 0. 560 (61%, e/v 1.7 × 10 ⁻³ ), 0. 804 (6%, e/v 1.2 × 10 ⁻³ ), 0. 804 (6%, e/v 1.2 × 10 ⁻³ ), 0. 804 (6%, e/v 1.2 × 10 ⁻³ ), 1. 0. 804 (6%, e/v 1.2 × 10 ⁻³ ), 1. 0. 804 (6%, e/v 1.2 × 10 ⁻³ ), 1. 187 (32%, e/v 0.3 × 10 ⁻³ ), 1. 187 (32%, e/v 0.3 × 10 ⁻³ ), paet conv, spect 0. 3 × 10 ⁻³ ), spect conv, spect 0. 455, 0. 545, 0. 9, 1. 105, 1. 189 (4PS1) (4PS1)	0.747 (e/y 0.015, K/L 34) spect, spect conv, 8-y coinc, y-y coinc, 8-conv coinc (50850s)	0.665 (e/y -0.0015) apect, apect coay (50B50a); 0.7 aba, fi-y coinc (26M52)			-0.1, other y's abs (43D52)	no y (23D49)	0. 3 abs (23D49)		0. 262 (K/L 2. 9), 0. 69, 1. 51 apect, apect cover (ARS), 0. 265 (K/L 2. 8), 0. 7, 1.5 apect conv., exin apect (13.50b); 1. 7 (e/Y 9), 0. 70 (e/Y 0.005), 1. 7 (e/Y -0) abs., abs. conv. apect conv., conv. y coinc (2985 0a); 1/ 0. 29, 1/ 2, 0. 69, 1/ 3, 1.46 (1/1/2/ 1/ 2, 0. 1/1/1) acint apect (76.55 2b) others (8552)
0. 750 (92%), 0. 37 (9%) spect (4P5)); 0. 686 (92%), 0. 37 (9%) spect 0. 75 spect (76B51)		1, 267 apect (50B50a); 1, 35 abe (75549); 1, 4 abe (32K51b, 26M52)		3. 2 abe (23D50)		3.7 abs (23D49); 2.7 cl cb (42S40)	2.6 abs (23D49)		
23.35 h (29K49a); 22.9 h (76B51)	60 a (50B50a)	72.1 m (26M52); 74 m (50B50a); 75 m (2G40)	30 m (76B49b)	2. 5 m (23D50)	5.7 h genet (43D52)	15.5 m (23D49, 25W48); 17 m (29K49, 37B39, 42S38]	75 e (23D49); 73 e (25W48)		6, 95 h (16852b); 6, 75 h (29K50a)
p (29K49a)	IT (50B50a)	p" (2G40)	p (76B49b)	p (23D50)	β ⁺ , EC (43D52)	p ⁺ (42S38)	p* (23D49)		IT (29K50a)
								15. 86 (9 W46)	
A chem, excit, sep lsotopes (29K49s)	A chem, excit, sep isotopes, genet (50B50s)	A chem, genet (2G40)	E chem, sep isotopes (76B49b)	<b>£</b>	B chem, genet (43D52)	A excit (37B37a); chem, excit (42S38); chem, ep isotopea, excit (29K49, 23D49)	B chem, sep isotopes (23D49)		D chem, excit (29K46); cross bomb, exp leadopre (29K50a); chem, excit (76B52b); possibly Mo2m or Mo94m (HPS)
g ez	ж ^{97ш}	76 de 1	<b>8</b>	ž	42 Mo90	Mo 91	Ke 91	Mo 92	₩о дзн

						Latin in Man		1
Z A	Class and identification	Percent	lype of decay	Half-life	Purticles	Gemma-transitions	Disintegration energy and scheme	genetic relationships
42Mo93	B chem, n-capt (76B49)		EC (76B49)	>2 y (76B49)		Nb K-x (76B49)		Mo-n-y (76B49)
Wo %		9.12 (9W46)					Mo ⁹⁴ , I * 0 (87M50)	
Mo 95		15. 70 (9W46)					Mo ⁹⁵ , I = 5/2 (87M50)	
Mo.96		16. 50 (9W46)					Mo ⁹⁶ , I = 0 (87M50)	
Mo 97		9.45 (9W46)					Mo ⁹⁷ , I = 5/2 (87M50)	
Mo 98		23. 75 (9W46)					Mo ⁹⁸ , I = 0 (87M50)	
K°3	A chem, n-capt, excit (42538, 42540)		6 (42538)	67 h (13S39); 68. 3 h (10C49); 63. 5 h (25W48);		Y ₁ 0.040, Y ₂ 0.181 (K/L 5), Y ₃ 0.367, Y ₄ 0.741, Y ₅ 0.780	Q ₆ 1.37 (2B50a) Mo ⁹⁹	Zr-a-n (14E46); Mo-d-p (13539); Mo-n-y (42538, 13539, 61M47,
				64 h (42540)	(62M51); 1. 25, others, spect (54M51); 1. 2 abs (32K51c)	$(\gamma_3/\gamma_4/\gamma_5 = 10/100/14)$ apoct, apoct conv (2850a); 0.728, 0.360 (weak) 0.182 (weak)		
•						0.179, 0.168 apect conv (10C49); 74 0.745, 75 0.780, 76 0.850 (v./v./v. = 100/50/30) apect	9-	epail Sb (37L50); epail-fission Pt, Tl (2T47b), Bi (13P47, IlG49, 66B51), Tr, (78402),
						(\$4M\$); with Tc99m; 0.0018, 0.140 (62M49, 62M\$1); 0.142 (63M\$1)	81 8 18 18 18 18 18 18 18 18 18 18 18 18	fission Th (184394, 7285), 2175), U-53 (165346), U (164199, 24540, 22K51c), Pu (32K48, 28F51); parent TC97m (13539, 24540, A74449, 31741, 13539, 24540,
							(18652)	
<b>K</b> 0100		9.62 (9W46)					Mo ¹⁰⁰ , I = 0 (87M50)	
Mo.101	A chem, n-capt (42540); chem, n-capt, aep isotopes (61M47a)		f" (42340)	14. 6 m (3M41); 14 m (16H41b)	1, 2, 2, 1 abe (31R52); -1, 0, 2, 2 abe (3M41); 1, 9 abe (42540)	0.191 (K/L-6), 0.960 (coinc with 1.2 p) apect conv. scint apect, p-v, v-v coinc (31852); 0.15 acint apect (38M51a)		Mo-n-y (42840b, 42840, 24840a, 3M41, 2847, 50H51); Mol ¹⁰⁰ n-y (61M47a); parent T ¹⁰¹ (42840b); (fastion U, parent T ^c 01 (43840a, 37841, 16H41, 16H41b,
Mo 102	D chem (16H41)		p (16H41)	12 m (16H41); 11 m (76B49a)				fission U. parent Tc ¹⁰² (16H4), 16H4lb, 76B49a)
Mo.105	B chem, genet (70B43b)		p (70B43b)	-5 m (66547)				fission U, ancestor Rul05 (70B43b)
43Tc92	D chem, sep isotopes (61M48)		p+, EC (76B52c)	4. 3 m (76B52c)	4. 1 abs (76B52c)	1. 3 abs (61M48)		Mo ⁹² -d-2n (61M48)
1c 92	D chem, excit, sep isotopes (29K48a)		EC (29K48a)	43.5 m (62M50); 47 m (29K48a)		0.389 spect, spect conv (62M50); 1.50 abs conv (29K48a)		Mo ⁹² -d-2n, p-n (29K48a); Mo-p-n (62M50)

Mo 92 -d-n (29K48a, 61M48); Mo-d-n (13539); Mo-pr-y (5D39, 29K8a; not parent (7h) Mo 93m (7655a)	Mo-p-n (42G47, 34H48, 62M50); Mo ⁹⁴ -d-Za (61M48a); daughter Ru ⁹⁴ (12V52)	Mo-d-n (12C37, 12C39, 14E46); Mo-p-n (14E47); Mo95-d-Zn (61M48b)	Mo-a-p, Mo-p-n, Mo ⁹² -a-p (1E48); Mo ⁹⁵ -d-2n (61M48a); Mo-p-n (62M50)
Qp 3.1 (76881a) T _G 93	(3+30 (62)450) (3+3) (13+3) (13+3) (13+3) (13+3) (13+3) (13+3) (13+3)	(1/2-) T _C 95 m (1/2-) T _C 95/ (1/2-) T _C 9	(9.7±+)
1. 34 (coinc with p*) scint spect, p-y coinc abs (788514); 2. 00 abs (29K48a); 2. 4 abs (61M48)	0. 674 (e/y - 10 ⁻³ ), 1. 85, 2, 73, 3. 27 spect, spect, cony (62MSO); 0. 9 abs (61M48a)	1 ₁ 0. 810 (e/γ 0. 001), γ ₂ 0. 201 (e/γ 0. 036), γ ₃ 0. 370 (e/γ 0. 002), γ ₄ 1. 02 (γ ₁ /γ ₂ /γ ₃ /γ ₄ = 0. 3/0. 7/0. 4/0. 03) spect, spect, 0. 0390 spect conv (62M50s); 0. 090 spect conv (62M50s); 0. 00. 20, 0. 56, 1. 03 schall (10 9 spect (7585s); 0. 6, 0. 2 abs (14587, 61M48s) (1)	0. 762 (-90%), 0. 932 (-5%), 1. 071 (-5%) apect conv. y-y colac (62M40); 0. 76, 1. 07, no 0. 93 y acint spect (76B54d); 0. 78 abs (1E48)
0. 800 spect (76.85ia); 0. 83 abs (29K48a)	2. 41 (coinc with y) spect, p-y coinc (62M50); 2. 5 abs (61M46a)	0.4 cl ch (62M50)	
2.75 h (29K48a) 2.7 h (51M48, 5D39)	50 m (61M48a); 60 m (61M48a)	60 d (62M50); 52 d (14E47); 62 d (12C39)	20.0 h (iE48); 20 h (6iM48a)
EC 93%, p ⁺ 7% (29K48a, 76B51d)	62MS0)	EC 96+%, IT -1%, 64 0. 2-0, 6% (62M50, 62M50a)	EC (1E48); no p* (62MS0)
A chem (13639); chem, excit, sep indopes (29K48s)	B chem, excit (42647); ebm, excit, eep isotopes (61M48a)	A chem (12C37, 12C39); chem, sep isotopes (61M48b)	A chem, sep isotopes (IE48, 61M48s)

Tc95m

	7				Bearing of section	Barrers of and indicate in Man.		
V Z	identification	abundance	decay	Half-life	Purticles	Gamma-transitions	Disintegration energy and scheme	Method or production and genetic relationships
43Tc 96m	B chem, excit (62M50); chem, excit, sep isotopes (62M52)		IT (62M50)	51.5 m (62M50)		0.0344 (K/L 1.2) spect conv (62M50); Tc K-x (62M50)	(+6,6)	Mo ⁹⁶ -p-n (62M52); Mo-p-n (62M50)
7c%	A chem (15E39); chem, excit, cross bomb (14E47); chem, excit, sep isotopes		EC (61M48b); no β* (62M50)	4. 20 d (31C50); 4. 35 d (62M50); 4. 2 d (61M48b); 4. 3 d (14E47)			(s, e+)	Nb-a-n (14E47); Mo-p-n (15E39, 14E47, 62M50); Mo-d-n (14E47, 13S39); Mo ⁹⁶ -d-2n (61M48b)
	(61M48B)		-			γ ₅ = 0.17/1.00/0.82/1.00/0.0052, spect, pect conv. γ·γ coinc (6.2450) 1.65, 1.89, 2.39 (?) (all weak) acint spect (76B51a)	(3,4+)	
							(62M50, 7685la ,62M52, 18652)	
Tc97#	A chem (22P37, 12C37); chem, genet (61M47b); excit, sep isotopes (61M48b)		IT (2H41, 14E47)	90 d (61M48b); 91 d (2H41); 95 d (14E47)		0.0958 (K/L+M l. 6) spect conv (62M50); 0.097 (K/L - 2) spect conv(2H41); 0.097 (K/V very large) abs conv (61M48b); 0.108 (e/y large) abs conv (14E47)		Mo ⁹⁷ -d-Zn (61M4Bb); Mo-d-n (12C37, 2ZP37, 1ZC39); Mo-p-n (14E47); daughter Ru ⁹⁷ (61M47b)
Tc 97	[A] genet (76B51b)		[EC] (76B51b)	>10 ⁴ y yield (76B51b)				[daughter Tc ^{97m} ] (76B51b)
т. 69т	A chem, genet (13839)		IT (13839)	6.04 h (1852); 5,9 h (33G51e); 6.6 h (13539)		0.1403 (K/L 7.7), 0.1423 (-1%, K/L -2.5) appert conv (5.M515); (f.K/L -2.5) appert conv (5.M515); (f.Y -2.7)/(0.1), K/L/M4N -1.4)/(0.1), 0.0016 (4.V very large) appert conv (6.M49, 6.M51); (f.K/L -9) appert, appert conv (5.M508); (f.K/L -10) appert conv (5.M451)	(W.E+) TC 99 M. (M.E.)	Ru-n-p (76B47); fission Th (72B51), U (24840, 16H41, 34C51e); daugher Mo99 (13S19, 24840, 6ZM49, 34C51e, 6JM51); parent Tc99 (13S19, 16H41)
1,9	A chem (25146, 33546); chem, mass spect (3147)		p_ (25L51, 5385la)	2.12 x 10 ⁵ y sp act (30F51); 2.2 x 10 ⁵ y sp act (26F51)	0. 290 spect (15F32); 0. 292 spect (37F3); 0. 296 spect (39W52); 0. 30 spect (24K50s)	no _Y (61M47, 53551a, 30 <b>F</b> 51)	0, 0, 29 (15552, 23751) (574+) (62M51, 63M51, 18652) Tc99, 1 = 9/2 (48K51)	fission U (3147, 251.5), 53851a); daughter Tc 99m (13839 i6H41); descendent Mo ⁹⁹ (61M47)
Tc 100	A sep isotopes (64H52); sep isotopes, n-capt (76B52)		p ⁻ (64HS2)	15. 8 e (76B52); 17. 5 e (64H52)	2. 8 abs (76B52); 2. 4 abs (64B52)	0. 55 acist apact (76B52c)		Mo 100 p n (64H52); Mo p n (2D40); Te ⁹⁹ .n y (76B52)

Mo'00 d.n (61M48); Atty-p (12P48, 60M48); Rh-y-p (12E25); Rh-y-p (12E25); Rh-y-p (12E25); Rh-y-p (12E35); Rh-y-p (12E35); Rh-y-p (12E48); Rh-y-p (12P41); Rh	fission U, danghter Mo ¹⁰³ C parent Ru ¹⁰⁵ (70B43b) Q [fission U, parent Ru ¹⁰⁷ ]	•	Mo-a-2n, parent Tc ⁹⁴ (12V52)	Mo-a-n, Mo ⁹² -a-n (1E48); Ru-n-2n (1E48); Ru-y-n (60M48)		Mo ⁹⁴ a. n (1E48); Ru-d-p (2284); Ru-n-y (23846); Ru-y-n (1E48); Ru-y-n (06048); apall Sb (371.50);					Ru-d-p (121.36, 23851); Ru-n-y (23851, 7D38); Ru-y-n (60M48); spall So (371.26); Bi (101.649); Bi (101.649); U (31.3 (396.48, 618.48), U (31.48, 396.38, 51.38); Z35511), Pu (28.78); Parent Rh (13.78); Y	. 1.
Mo ¹⁰⁰ .d-n (£1M49); Atty-p (12P48, 60M Rhy-p (12P22); (1asion Ü, daughter; (2A540a, 37B4), 16); 3M41); daughter Mo ¹⁰² (166); T6B49a)	fission U. parent R. [fission U.	(708435)	Mo-a-2n,	Mo-a-n, M Ru-n-2n (1 Ru-y-n (60		Mo 94 a.n (1E48); Ru-d-p (23S46); Ru-n-y (23S46); Ru-n-2n (1E48); Ru-y-n (160448); apail Sb (37L50); parent Tc 97m (61					Ru-d-p (12L. Ru-n-y (235) Ru-y-n (60M epail 35 (37) epail-fission Bi (11649); fission Th (1 U23 (38C4) U (504), SW 23551f), Pu	
								Ru ⁹⁹ , I = 5/2 (19052)	Ru ¹⁰¹ , I = 5/2 (19052)		Qp 0.75 (38KSIc)	
0 . 307 (coinc with 6', K/L -6) spect conv, 6-y coinc, scint apect (31852); 0. 56 (weak) 0. 30 (coinc with 6'), 0. 56 (weak) e. 26 cint spect (38M51a); no 0. 56 y (31852)				1.0, 0.5 abs (1E48)		0. 217 epect (\$3M50a); 0. 23 abe (23S46)					0.498 (coinc with 0.22 p°, e/y-0.01) spect, spect come, p-y-coinc (18K9) 18K15(1); 0.498 spect (46K521); 0.498 (k/Y) 0.006, K/L 6.5) spect, spect come (53M504); 0.499 (k/L 8.5), 0.611 (k/L 4), 0.295 (r), 0.635 (k/L 4), 0.295 (k/L 6), 0.611 (k/L 4), 0.295 (come) (10C52); with Rh/D3m; 0.040 (18K50, 23E52, 52M5); y7W4K 10C53;	31 113, 10032)
14.0 m (3M41, 1.20 (>94%) abs: p-y coinc (76B340, 1.30 tocinc with p'. K/L-6) 1614b); abs (42840); apset conv. p-y coinc, scint 14.5 m (12P40); abs (3M41) c. 30 (coinc with p'), 0.56 (we see the spect poinc); abset coinc, scint poinc, scint poinc, scint poinc, p-y coinc (78B5 coinc (78B5); abset coinc, p-y coinc, p				1. 1 abs (1E48)							0.217 (-99%), 0.698 (-1%) spect (198K50, 238K31c); 0.222 (94%), 0.694 (6%) spect (53M50a); 0.53K50a); 0.670 (weak) spect (79500); 0.350 (50%), 0.655 (50%) spect (15448); 0.2 (92%), 0.7 (8%) abs. β-γ coinc (26M50)	
14.0 m (3M41, 16H4b); 14.5 m (12P48); 16.5 m (60M48); <25 o (76B49a); <25 o (76B49a);	ebort (70B43b)	(70 <b>B</b> 43b)	-57 m genet (12V52)	1.65 h (1E48)		2. 8 d (23846, 60M48)					39. 8 d (3885); 41 d (3351); 41 d (3351); 42 d (3845); 45 d (3842, 60 Md8)	
	p (70 <b>B</b> 43b) [p] (70B43b)		EC (12V52)	EC, p*(1E48)		EC (23846)					p (5N42)	
					5. 7 (16E43)		2. 2 (16E43)	12. 8 (16E43) 12. 7 (16E43)	17. 0 (16 <b>E4</b> 3)	31. 3 (16E43)		18. 3 (16E43)
A chem, gmot (42540b)	B chem, genet (70B43b) [E] genet (70B43b)		D chem, genet (12V52)	A chem, cross bomb, sep isotopes (1E48)		A chem, excit (23946); chem, cross bomb, sep isotopes (IE48)					A excit (121.36); 26.mn (5N42, 39G46); chem, excit (2381, 23851b)	
	Tc. ¹⁰³				Ru %	Rug 7	8°°3	Ru 100	Ru 101	Ru 102	Ru 103	<b>3</b> 010

	7	a de la constante de la consta	T.		Francisco of radiation in May	in Mer		Market of tenders
V Z	identification	abandance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
44 Ru 105	A chem (24541); chem, excit (23551c)		p [*] (5N41)	4.5 h (7659), 23551d, 23551a); 4.4 h (77845)	1. 150 apact (23D51); 1. 15 apact (90552); 1. 3 abs (23S51d, 23S51a, 77B45)	0.726 (coinc with \$\beta\$) spect, \$\beta\$-y coinc (23551d); 0.75 & be (23551d); 0.7 abs (77845); with RhlO5m; 0.130 (29451, 23D51a, 90552)	Q _p 2. 01 (23D5.1) Ru 105 Ru 105 (1/2.5.) (1/2.5.) (1/2.5.) (1/2.5.) (1/2.5.) (1/2.5.)	Ru-n-y (7D38, 23851c); Ru-d-p (12.15, 23851c); spall 28, 637.126, 23851c); spall-ifesion Pt (2147b), Hg (r) (63852), T1 (2747b), Hg (r) (63852), T1 (2747b), Hg (r) (6386, F21); fission Th (2484, 72851); fission Th (2484, 72851); TR845, 76851, 23851d); descendent Mollo (708843b), parent Rhlo5f, 70843b, ancestor Rhlo5 (70843b), ancestor Rhlo5f (23851); ancestor Rhlo5f (23851);
Ru 106	A chem (39G46, 33G46a); chem, mass spect (60H48)		8 (139G51a, 33G5E)	1. 0 y (33G5E, 66S46)	0.0392 spect (16A50); 0.038 spect (3P50b)	no y (76551æ, 16A50)		spall Sb (37L50); spall-fis ston Bi (11C49). Th (77N49A). (1 (6F5)]; fission Th (72B51, 2151). U.233 (18C48, 6L849). U (13C51). parent Rh ² D6 (13C51); parent Rh ² D6 (13C51).
Ru 107	D chem (70B43b, 33G51g)		p (70B43b)	4 m (33GS1g. 70B43b)	-4 abs (70B43b)			fission U, parent Rh 107 (13G5lg, 70B43b)
45 Rh 99	D chem (1E49)		β ⁺ (90S52)	4.5 h (90S52)	0. 74 spect (90S52)			Ru-p-n (1E49, 90S52); Ru-d-n (1E49, 90S52)
Rh 100	B chem (2355le); chem, genet (37L48)		EC -95%, B ⁺ -5% (37L48)	19.4 h (37L48); 3.0 21 h (23SS1e)	3. 0 spect (37L48)	1. 2 abs (37L48); 1. 8 abs (23S5ls)		Ru-d-n (23S5le); daughter Pd ¹⁰⁰ (37L48)
Rh 101	B chem, excit (23S51g)		EC (23551g)	4. 3 d (37L48); 5. 9 d (23S51g)		0.300, 0.148 spect conv (90552); 0.35 spect conv. abs (37L48)		Ru-p-n (90552); Ru-d-n (2355lg, 90552); daughter Pd ¹⁰¹ (37L48)
Rh ¹⁰²	A chem, excit (64M41)		β', β ⁺ (64M41); EC (?) (23S51h)	210 d (64M41); 215 d (15H47)	p; 1. 0 c1 ch (15H45); p;: p:: 1 c1 ch (15H45)			Ru-d-n (2355lh); Rh-n-2n (64M41, 15H45); Rh-y-n (60M48, 22E52)
Rh 103m	A chem, excit (9F44); chem (33G46a, 30GH); chem, genet (23S5lb)		17 (9F44, 37W45)	57 m (33G5lf); 56 m (53M50a); 52 m (9F47); 45 m (37W45)		0.0400 (K/L-M 0.2) spect conv. B-v coinc (18K60, 18K31c); 0.0404 (e/v very large) spect conv (19M50a); 0.0396 (K/L 0.1) spect conv (10C52); conv (31W45); 0.042 abs conv (9F47)	(72±+)—Rh 103m (1/2-) Rh103 † 0.040 (18652)	Rh-d-pn, Rh-p-p (15H48); Rh-n-n (9F44); Rh-e-e-, Rh-x rays (37W45); (1385ion U, daughter Rul (2385ib); 53M50a)
Rh ¹⁰³		100 (57C43)					Rh ¹⁰³ , I = 1/2 (49K50)	

NUCLEA	in Ph	10100					CHAP.
Ru-p-n (2D40); Rh-n-v (12A3), 19G46, 2847, 50H51); Pd-y-p (42H47); parent Rh ¹⁰⁴ (17P38, 9F47)	Rh-n-y (12A35, 17P38, 34G46); daughter Rh ¹⁰⁴ m (17P38, 9F47)	daughter Ru ¹⁰⁵ , parent Rh ¹⁰⁵ (23D51)	Ru-d-n (235511, 90552); Rh-t-p (25448); Pd-y-p (12P48); pall-fission U (6F51); fission Th (72851, 21751); descendent Ru ¹ 05 (5N41, 77845, 76551, 23551c); daughter Rh ¹ 05m (23D51)	ffesion U, daughter Ru (38646, 33055ff); ffesion Pu (28F5i)	Pd-y-p (22E52); fission U, daughter Rulo7	[fission U, parent Pd 109] (77351)	Rh-d-5n (37L48); spall Sb (37L48, 37L50); perent Rh ¹⁰⁰ (37L48)
	<b>6</b> 00	(1/2-) Rh O5 (1/2-)	Q ₆ 0.570 (HPS) Q ₆ 0.570 (HPS) (8/2+) (186522)	(1.47   1.1452) (1.47   1.1452) (1.47   1.144 (1.44   1.444 (1.44   1.444 (1			
0. 05.2 scint spect (38M51); scint spect, ion ch (31K51); others (28A43a, 14O40, 15H47)	0.04, 0.18, 0.95 abs, abs conv (58C47)	0.130 (e/y -3, K/L 1.5) acint apect, apect conv (29.55); 0.127 apect conv (90552)	0.322 (-10%, coinc with 0.26 p ⁷ ), 0.157 (very weak), 0.080 (?) a cint spect, 6 v coinc abs (7685a); (7685a); 0.320 (-35) a cint spect (23D5la); 0.3 (-6%, not coinc with 0.6 p ⁷ ) abs, 6 v coinc (26M5); 0.3 (weak) abs (23551i)	y ₁ 0. 513 (e _K /γ 0. 004, K/L 8), γ ₂ 0. 624 (e _K /γ 0. 002), γ ₃ 0. 87, γ ₄ 1. 045, γ ₅ 1. 5, γ ₆ 2. 41 (γ ₁ /γ ₂ /γ ₃ /γ ₄ /γ ₅ /γ ₆ = 100/53/3 (6/2. 5/1) spect, scint spect, scint spect, scint spect, scint spect, scint spect, oz, γ ₃ 0. 73 (17%), 1. 25 (17%) spect conv (13A2); 0. 510, 0. 622 spect conv (16C32); 0. 510, γ ₅ γ ₇ γ ₇ coinc (6F47a); 0. 5 (4K/γ 0. 005), -0. 7 (e _K /γ 0. 005), -0. 7 (e _K /γ o. 003) spect conv (44M50); others (39A32)			0.09, 1.8 abs (371.48)
	2.6 spect (15H47); 2.3 abs (18843); cl ch (32C39); 2.5 abs (28M40)		0.570 (-56%), 0.25 (-4%) spect (23.55, 23.55a); 0.57 spect (96.52); 0.26 -10%, 6.7 coinc abs (76.85.2a)	3.53 (68%), 3.1 (11%), 2.44 (12%), 2.0 (3%), others (6%) spect (13.45%), 2.30 (18%) spect (6F47a); abs., p-y coinc (15.149), 3.5, -2.3 abs., p-y coinc (15.149)	l. 2 abs (70B43b)		
4.4 m (32C39); 4.7 m (38M51, 58C47); 4.3 m (9F47)	44 e (12A35, 17P38)	45 = (23D51)	36. 5 h (23851c); 37 h (77845); 34 h (5N41)	30 = (33G5L/);	26 m (33G51g); 24 m (70B43b)	<1 h (77851)	4.0 d (37L48)
IT (17P38, 28A43a)	p (17P38)	IT (23D51)	p. (5N41)	6 (33G5И)	p (70 <b>B4</b> 3b)	[p] (77851)	EC (37148)
A n-capt (12A3S)	A n-capt (12A35); genet (17P38)	A chem, genet (23D51)	A chem, genet (5N41); chem, genet (2355)c)	A chem, genet (33G46a, 33G5M)	D chem, genet (70B43b)	[A] genet (77551)	B cham, excit (37L/48)
Rh 104m	Rh 104	Rh 105m	R. 105	8 106	Rh ¹⁰⁷	Rh 109	46 Pd 300

	700	1	Thread		Energy of rad	Eperary of radiation in Mev		Method of senduction and
Z A	identification	abundance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	generic relationships
46 Pd 101	B chem, genet (371.48)		EC 90%, p [†] 10% (37L48, 1E49)	8 h (37L50); 9 h (1E49)	2. 3 spect (37L48); 0. 5 abs (1E49)	no y (37L48)		Ru-a-n (1E49); Rh-d-4n (37L48); spall Sb (37L48, 37L50); parent Rh ¹⁰¹ (37L48)
Pd 102		0.8 (37S36m)						
Pd 103	A chem, genet (48B46a); chem, excit (36M47)		EC (48B46a)	17. 0 d (36M47, 48B46a)		Rh Kx (36M47, 53M50a); no y (36M47, 53M50a); with Rh103m; locs (36K50, 53M50a, 79S50, locs 2)		Rh-a-p3n (53M50a); Rh-d-2n (36M47); 71L48); Rh-p-n (36M47); Pd-n-y (48B46a, 78850); pall Sh (37L50); paren Rh(93m (48B46a, 33M50a)
Pd 104		9. 3 (37536a)						
Pd105m	E excit (9F52a)		IT (9F52a)	-23 e (9F52a)		0. 20 (e/y -0. 4) (9F52a)		Pd-n-2n, Pd-n-n (9F52a)
Pd 105		22.6 (37S36a)					Pd ¹⁰⁵ , I = 5/2 (99B51)	
901 Pd		27. 2 (375364)						
Pd 107	B chem (26P49a)		p (26P49a)	-7 x 10 ⁶ y sp act (26P49a)	-0.04 abs (26P49a)			fission U (26P49a)
801Pd		26.8 (375364)						
Pd 109m	D n-capt (31K51); excit, cross bomb, n-capt (9F52a)		IT (31K51, 9F52a)	4.8 m (9F52a)		0.173 scint spect (31K51); 0.160 (s/y -0.6) (9F52a)		Pd-n-2n, Pd-n-y (9F52a); Ag-n-p (9F52a)
Pd 109	A n-capt (12A35); chem, excit (39K37); chem, mass spect (37R46, 67B49a)		p [*] (39K37)	13.6 h (11M53); 13.1 h (25W48); 13.b (39K37, 77S51); 14.1 h (60M48)	0.961 spect (20K52); 0.95 spect (7849b, 38K5/c); others (2H46, 39K37, 77851)	with Ag 109m; 0.087 (s/y 3t), K/L-M 1.3) apert corn (1349b); no y (1753l); others (52M51)	0, 1.05 (HPS)	Pd-v-n (12P48, 60M48, 25 W48, 22E52) 2EE52) Pd-d-p (13943); Pd-n-y (12A35, 39K37, 2547, 9049, 26H51); Ag-d-p (2H66, 112531);
							38 0.087	Agn-p (4738b). Ag-t-He J (4738b). apail Sb (371250), Ta (22N82); apail-fission Bi (11054), fission Th (21731), U233 (61548), Pu (13581), parent Agl09m (24841, 7849);
Pd 110		13. 5 (37836a)						77851)
mII pq	B chem, genet (66M52)		IT 75%, P. 25% (66)M52	5.5 h (66M52)		0.16, 1.77 scint spect (66M52)		Pd-d-p, parent Ag 11 (66M52)
Pq 111	A n-capt (12A35); chem, genet (24S41)		p ⁻ (39K37)	22 m (66M52); 26 m (24341)	2. 13 apact (20K52); 2. 15 apact (66M52); 3. 5 aba (70B43b)	0. 38, 0. 56, 0. 65, 0. 73 scint spect (66M52)		Pd-d-p (12A35, 39K37); Pd-n-y (12A35, 39K37, 2S47); epail Sd (37L50); epail-fission Bi (66B3); fission Th (24S4), U (24S4); 5Ndba;
-		_	_	_	-	_	_	parent Ag (39K3/, 2454!)

leosope	Class and identification	Percent	Type of decay	Half-life	Bearly of radiation in Mer	section in Mev	Distangration seargy and scheme	Method of production and generic relationships
40gV-4	A excit (37B37a, 6H3); chem, excit, cross bomb (39K37, IP38)		p* (19K37); p* (7) - 2% (79B51)	24.0 m (79531); 24.5 m (1938); 24.4 m (5038); 24.3 m (60M48)	p ⁺ ; 1.95, 1.5 spect (79B51); 2.0 abs (4878b); 1.9 ct ch (1P38) 67 (7); 0.45 spect (79B51); -0.5 (weak) spect conv (79B51)	-0.5, >0.6 (weak) spect com, scint spect, abs (7955) no y (4738b, 1P38)	EC/ (1+1) Aq 106	
<b>76</b> 10€	A chem, excit, cross bomb (39K37, IP36)		EC (\$5H44)	8. 2 d (IP38); 8. 3 d (46549); 7. 5 d (39K37)		0.220, 0.409, 0.511 (K/L 8), 0.620, 0.717, 0.815, 1.04, 1.24, 1.55 spect conv (61152); 0.515, 0.722, 1.04, 1.54 spect (53M50b); 0.72, 1.06, 1.63 spect (20D42c)	(2+) (2+) (2+) (2+) (3+) (3+) (3+) (4+) (4+) (4+) (4+) (4+) (4+) (4+) (4	A4-6-7 (19346); A4-6-7 (19346); C4-1-p (1938) Rh-6-1 (1938) (1938) B4-6-1 (1938) (1938); B4-6-1 (1938) (1938); A4-6-7 (1938) (1939); A4-6-1 (1938) (1939); spall \$8 (171.50)
Ag 107m	A chem, genet (6.440, 2H4lb)		IT (6A40)	44.3 e 16B454, 16B47); 44 e (40W51)		0.094 (e/v -16, K/L 0.92) spect conv (16B47); 0.093 spect conv (6V39, 2H41)	cd ¹⁰⁷ Ag ^{107m} (7/2+) Ag ^{107m} (1004) (1/2-) (10052)	Ag-n-a (9744); Ag-n-a (9744); Ag-n-a (9744); Ag-n-a (9095); Ag-n-y- (4098); Ag-n-y- (4098); Ag-n-y- (4096); Ag-n-y-y- (4096); Ag-n-y-y-(4097); Ag-n-y-y-y-y-y-y-y-y-y-y-y-y-y-y-y-y-y-y-
Ag 108	A chem, n-capt (12A35): avrit cross	51. 35 @4W48)	6 98.5%, EC	2.3 m (12A35, 12P48, 60M48.	1. 5 scint spect (45G52)	0.45, 0.66 schat spect (12P52); 0.43, 0.60 scint spect (45G52)	Ag ¹⁰⁷ , I = 1/2 (87M50)	Pd-p-n (2D38, 17E39); Ag-n-y (12A3, 2744, 2547, 9O49, 50H31, 36551);
A <b>g</b> 109m	A chem, genet (2H4lb)			37839); 2. 4 m (97-44) 39. 2 e (16846c, 16847); 40 e (40WS), 37W448b)		0.0875 spect conv (10C50b); 0.087 (e _K /1 - 6, K/L+M 0.75) spect conv (34H32); 0.087 (e/y All, K/L+M 1.3) spect conv (7849b);	(7/2+) Aq 109m (1/2-) 0.088 (1/2-) 0.088	Ag 107 v (19548); Ag 107 v (19748); Ag v (1978) (1244); Ag v (1978) (1244); Cd-n-p (1978) (1978); Ag v (1978) (1978); Ag v (1974);
A£ 109		48.65 (24W48)				0.08/ spect conv (£146, 1624/)	Ag 109, I = 1/2 (87M50)	daugher Cd ¹⁰⁷ (£H415, 18545C, 2H46)

NUCLEAR PHYSICS				CHAP. 1.2
Pd-d-2n (44G50); Ag-n-y (15R18, 12L38d, 30A38, 14M38, 2547); Ag-109, -q. (16G46d); Ag-109, -d-p. (16G46d); Ag-10, -d-p. (16G46d); Ag-10, -d-p. (16G46d); Ag-10, -d-p. (16G46d); Ag-10, (16G46d); Ag-10, (16G46d); Ag-10, (16G46d);	Ag-n-v (12A3546G36,9F44,2547); Ag109-n-v (9F44a); Cd-n-p (15P38); Cd-v-p (42H46a, 42H47); daughter Ag10m (56M50)	Pd-d-n, parent Cd ^{lllm} 2 (80552)	Pd-d-n (398/37, IP38, 9249); Pd-a-p (19738); Ag-a-p (19738); Ag-a-p (2984/3-); Cd-n-p (19738); Cd-n-p (19738); Td-y-p (47147, 230493); spall 5(37126); Ta (2208/2); spall 5(3126); Ta (2208/2); spall 5(3126); Ta (2208/2); Th (7049a); U (6048, 6F51); U (6) (13185); Th (7049a); U (6048, 6F51); U (6) (13185); Th (7040a, 7040a, 648, 6781); parent Cd llimi (13554c); daughter PdllI (1398/37, 2484); 17350); daughter PdllIm (66M52)	Cd-n-p (1P38); Cd-y-p (42H47); In-n-a (1P38); spall Sb (37L50); spall-fisten Bi (66B51), U (6047, 6F31); fisteion Th (21T51), U233 fisteion U, daughter Pd 112 fisteion U, daughter Pd 112 fisteion U, daughter Pd 112
(1, 2+) (10+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+) (1, 2+)	<mark>ஷ</mark> ் 2. 90 (HPS)		(17.150, 13.ESIC, 66.MSI, 66.MSIO, 1895.2	
0.116 (a/Y vary large, K/L.1.3), 0.556 (a/Y 0.0023), 0.676, 0.706, 0.739, 0.814, 0.885, 0.935, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369, 1.369	0. 66, -0.9 (weak) scint spect (45G5la)		(e/y -0.015) (v ₂ /y ₁ - 8) epect, epect conv. 6-y coinc. y-y coinc (1750); 0.33 (-6.5 %) abs (78S50)	0. 625, 1. 40 (40A52b); 0. 86 abs (77851); no y coinc with 3. 5 p ⁻ (7485is)
with Ag 110.  0.08 (-58 %), 0.30 (-35 %),  2.16 (-35), 2.86 (-35 %),  others (?) speet (13 %),  0.86 (-58, 0.35 oct (13 %),  2.89 (-2 %), speet (13 %),  0.99 (-2 %), speet (13 %),  0.97 (coinc with y), 0.57  (coinc with y), 0.97  6.97 coinc (44 %),  0.99 coinc (44 %),  0.99 speet (11 % 47)	2. 24 (-60%), 2. 82 (-40%) scint spect (45G5la)		1. 04 (91%), 0. 80 (1%), 0. 70 (8%) spect (17350); 1. 06 spect (66MS), 33MS0b); 1. 1 (93.%), 0. 7 (6. 5%) abs (78550)	4. 2 scint spect (27P5la); 3. 6 abs (7785l); 3. 5 abs (7485la)
270 d (44050, 10C50a; 225 d (121.38d)	24. 2 a (42H46a); 22 a (12A35, 1P38)	[<5 m] (80S52)	7. 6. d (61851c); 7. 5. d. (1715c), 39K37, IP38)	3.20 h (74854); 3.2 h (IP38)
p. IT (7849c., 16639c); 100530c); 117 253c; 11	6 (1P38)		6 ⁻ (39K37)	p. (1P38)
A chem, n-capt (358.8); esonance neutron (186.46.); chem, esp isotopes n-capt (186.46.); chem, mass spect (678.49a)	A n-capt (12A35); aep iaotopes, n-capt (9F4a); chem, genet (36M50)	F genet (80S52)	A chem excit (39K37); chem, excit, cross bomb (1P38)	A chem, excit, cross bomb (IP38)
Mol Market	Ag 110	Ag ^{III} m	, F	۸ <b>و</b> 112

		-	[		it	11.21.11		
V Z	identification	abandance	decay	Half-life	Particles (	Gamma-transitions	Disintegration energy and acheme	Method of production and genetic relationships
4748113	A chem (21T47); chem, sep isotopes, excit (23D49s)		p (21T47)	5.3 h (21T47, 23D49a)	2.0 scint spect (27PSis); 2.1 abs (23D69a); 2. 2 abs (21T47)	no y (21T47, 23D49a)	۵ ً 2.0 (HPS)	Cd ¹¹⁴ v-p (23D49a); Cd-y-p (23D49a); spall-fission Bi (66B51), U (6F51) fission U (21747)
¥.	B chem (21T47, 66547); chem, excit, sep isotopes (23D49a)		6 (23D49a)	2 m (23D49a); 3 m (66S47)	hard p* (23D49a)			Cd ¹¹⁴ -n-p (23D49a); fission U (2IT47, 66847)
٧٤ 113	A chem (21747, 66547); chem, excit, sep isotopes (23D49a)		p ⁻ (21T47)	20 m (23D49a, 66847); 21 m genet (1W52); 22 m (21T47)	-3 abs (2/T47, 23D49a)	no y (23D49a)		Cd-y-p (23D49a); Cdll6-y-p (23D49a); fleeion U (21T47, 66847); parent (91%) Cdll5, parent (9%) Cdll5m (1W52)
	B chem, excit (32,52)		p ⁺ (32.52)	59 m (32.352)	0.93 spect (32,352)	0.0666 (K/L+M -10), 0.0835 (K/L+M -15), 0.124, 0.134, other y's spect conv (32J52)		Ag-p-4n (32J52); parent (24 m) Ag ¹⁰⁴ (32J52)
	B cross bomb (44G50); chem, excit (32J52)		EC, 8 ⁺ (44G50)	57 m (44G50); 55 m (32J52); 65 m (54K52)	1. 68 spect (32352); 1. 5 abs (44G50)	0.0255, 0.0494, 0.0525, 0.262, 0.293, 0.308, 0.312, 0.317, 0.321, 0.341, 0.347, 0.433, 2.1 apect (32.352)		Pd-a-n (44G50); Ag-p-3n (32J52, 54K52); Cd-n-2n (44G50)
Cd 104	A chem (5D39); chem, n-capt, sep isotopes (2H46)	1. 215 (281.48)	EC 99+%, p ⁺ 0.31% (16B45d, 55B50)	6.7 h (5D39)	0. 32 spect (16 <b>B454</b> , 16B45e)	0. 846 (0.4%, e/y -10 ⁻³ ) spect, spect corv (168454, 16845s); 0.7 abs (2144); with Ag107m; 0.094 (16845c, 16847, 6V39, 2H4))	Q+ 1. 43 (16B454) Cd 107 (18.7.77+) CG 107 EG 11. 43 (16B454)	Ag-p-n (5D39, 6V39); Ag-d-2n (9K39, 6A40, 9K40b, ZH41b, Ag-n-p3n (2H46); Cd ¹ 06-n-y (2H46, 18C46d); apail Sd (3TLS0); maall-diasion U (6F51);
							m20 DV (*24)	parent Ag ¹⁰⁷ m (6A40, 2H4lb, 16B45c, 2H46, 16B47)
Cd 10		0.875 (281.48)					(18652)	
§ 5	A chem (9K40b); chem, n-capt, asp isompes (2H46)		EC (L/K 0.28) (0.28) (0.28) (0.28) (0.28) EC (16B46c); no p*(26D51)	470 d (44G50); 330 d (16B46c)		with Ag 109m; 0.0875 spect coav (10C50b); 0.087 (sp/y -6, K/L+M 0.75) spect coav (34H52); 0.087 (sr/y -M, K/L+M 1.3) spect coav (7849b)	16 calc (38	Pd-a-n (44G50); Ag-d-7. (0X40b; JH41b, 44G50); Ag-a-pn (2H46); Cd10B-a-y (2H46; 10G50b, 99G51); parent Ag109m (2H41b, 16B45c 2H46, 16B46c)
							(18652)	

NUCLEAR PHYSICS									
	Pd ¹⁰⁸ (2H48); Pd (66M51); Ag pn (2H48, 66M51); Gd -n - or Cd -n - y (27D38,	Cd-vv (MF4), 37W45b, 2473) Cd12-n-2n (66M51); Cd-v-v (37W45b); Cd10-n-v (1664a, 52M51); flesion U (5040a, 5N40b);	spall-fission U (8F51); parent Cd ^{111m} (20056, 52M51); daughter (0.01%) In ¹¹¹ (66M51a) daughter Cd ^{111m} 2 (20050, 52M51); 52M51); daughter In ¹¹¹ (20049, 53B50); daughter Af ¹¹¹ (13E51c)	•			Cd-d-p (60C50); Cd-n-y or Cd-n-n (60C50); Cd112-a-p (60C50); Cd112-n-y (59C51); fission U236 (1952)		
Cd ¹¹⁰ , I = 0 (87M50)	600 Ag 111 and In 111 Cd IIImg Cd 396	(5/2+) <u>Gd^{IIIm}, 0.246</u>	(17150, 13E5ic, 66M31,	:	Cd ¹¹¹ , 1 = 1/2 (87M50)	Cd ¹¹² , I = 0 (87M50)	Mrs — Cd   3m   B"   Mrs — Cd   3   Mrs — Cd   3	(18652) Cd ¹¹³ , I = 1/2 (87M50)	Cd ¹¹⁴ , I = 0 (87M50)
	γ ₁ 0.150 (a/γ - 3, K/L 2.0), γ ₂ 0.246 (a/γ 0.064, K/L 5.1) spect conv (66,M51, 66,M51a); γ ₁ (e/γ 2.3) (calc from 14951,	66M53); Y ₁ 0.149, Y ₂ 0.247 acint spect (1883); Y ₁ 0.146, Y ₂ 0.235 spect conv (15H48a)	0. 247 acint apact (52M51)						
							0.59 scint spect (59C51); 0.5 abs (60C50)		
	48. 6 m (66M51); 48. 7 m (37W45b)		8 x 10 ⁻⁸ s delay coinc (20D50, 52M51);	10 x 10-8 a delay coinc (13E5ic)			5.1 y (60C50)		
	IT (31F41, 37W45b)		IT (20D49a)				p (60C50)		
12. 39 (281.48)					12. 75 (281.48)	24. 07 (281.48)		12. 26 (281.48)	28. 86 (281.48)
	A chem (27D38); chem, sep isotopes, n-capt (18G48a)		A genet (20D494)				A chem, excit (44C49); chem, excit, sep isotopes (60C50,59C51)		
ខ្លា	Cd ^{IIIm} 2		Ca ^{llim} l		3	Cd 112	Cd ^{113m}	Calls	Cd ¹¹⁴

V Z	Chass and identification	Percent shundance	Type of decay	Half-life	Particles Control of Political Control of Co	Gemma-transitions	Disintegration energy and scheme	Method of production and genetic relationships
46Ca115m	A chem (10C39); chem, excit (2547b); chem, e-p isotope, n-capt (10C50b)		6 (10C39)	43 d (2547b, 10C50b); 44 d (33G5lb)	1. 61 (-99%), 0. 7 (-2%), -0. 3 (weak) spect (61H5&2); 1.5 abs (2547), 10C50b, 1W52); 1.4 abs (20, 0.4 (coinc with y,~1%) & -y coinc abs (4.7650) 1.7 abs (33G3tb); -0.8 (-1. 4%) abs (13E5ig)	0.46, 0.50, 0.96, 1.28 scint apect, y-y coinc (61452a); y 0.48, y 0.94 (coinc with y 1, y 1.30 (not coinc with y 1 or y 1.30 (not coinc with y 1 or y 1.40 (y /y w 13/100/40) ecint a pect, y-y-coinc (13E.52), othera (56C49, 52MS)]	Q ² 1. 63 (61H32a) Cq ⁴ 15m (11/2+) Cq ¹¹⁵ m (17/2+) Gq	Cd-d-p (10C39); Cd-n-y (2547, 2547b); Cd ¹¹⁶ -n-y (10C50b); Cd ¹¹⁶ -n-y (10W22); Cd ¹¹⁶ -n-p (2547b); pall 3b (37L50); pall 15a (37L50); pall 15a (37L50); finsion Th (2175), U (6748, 6F51); finsion Th (2175), U (67481), Du (33C51h, 28F51); daughter (9%) Agl ¹⁵ (1W52)
51182	A chem (10037); chem. genet (18038); chem. sep isotopes n-capt (10050b)		p (10C37)	53 h (1W22); 54 h (10C50b); 56 h (24140, 67M51a)	1.11 (56%), 0.58 (42%) spect (101.2.2); 1.11 (-60%), 0.59 (-40%) spect (14.12.2.); 2.5 (-15%), 0.5 (-15%) p-y coinc abs (197.2.); others (26.M49s, 10C50b, 67M51a)	0.335 (with hilsm), 0.360, 0.500, 0.61.45 0.525 scint spect, Y-y coinc (6.1452a) 6.142 spect (28050); 0.326, 0.344, 0.349, 0.353, 0.359, 0.713 spect conv (10C50k) with highsm; apect conv (10C50k) 0.334 (10L52, 24L40, 61149, 611452a, 28050, 20K51)	(61H3Za) (1/45 (1/45 - 1/47 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 ) (1/45 - 1/47 )	Cd-d-p (10C37, 10C39); Cd-n-y (18C38, 14M37, 2547); Cd-n-y (10C508); Cd-n-x (18C38); Cd-y-n (60M48); In-n-p (2547b); pall-fission Th (TM49a), fission Th (21751); fission Th (21751), U333 (61548), U233 (1W22, U (61548), U234 (1W22, U (61548), U234 (1W22), parear In ¹³⁷⁷ (19C38, 10C39);
Cd 116		7. 58 (28148)					Cd ¹¹⁶ , I = 0 (87M50)	5N40b, 67M5la, 1W52, 10L52); daughter (91%) Agll5 (1W52)
Cd ¹¹⁷ m	A chem, excit (10C39)		П (SICS2a)	3.0 h (51C52a); 2.9 h (25A52); 2.8 h (24L40); 2.7 h (67M51b)		with Cd ¹¹⁷ (§1G52a): -1. 2 abs (\$5A52)		Cd-d-p (10C39, \$1C52a, 25A52); Cd-n-y (14M37, 18C38, 2547, \$15(2a); \$1C52a); fission U (6F51); fission U (8F51); fission U (8F31); parent h ¹¹ (18C38, 24L40, \$7M51b); parent h ¹¹ (18C38, 24L40, \$7M51b); parent h ¹¹ (18C38, 24L40,
ca ¹¹⁷	A chem, genet (31C52a)		p (51C52a)	-50 m (\$1C52a)	-1. 6, -3.0 abs (51C52a)			Gd-n-y, Gd-d-p, parent In 117 parent In 117 (\$1052a)
49 In 107	A chem, sep isotopes (68049); mass spect (97M52)		p ⁺ (68M49)	30 m (97M52); 33 m (68M49)	-2 spect (68M49)			Cd ¹⁰⁶ -p-y. Cd ¹⁰⁶ -d-n (68M49)
In 108	A chem, sep isotopes (68M49); mass spect (97M52)		p ⁺ (68M49)	50 m (97M52, 66M51); -55 m (68M49)	2. 31 spect (66M51); 2. 2 abs (37L50); -2 spect (68M49)	0.285 (<5%, K/L 33) spect conv (66M51)	Q+ 3.3 (66M51)	Cd ¹⁰⁸ -d-2n (68M49); daughter Sn ¹⁰⁸ (68M49, 37L50, 66M51)

Ag-a-2n (25747,48046. 66M51); Cd ¹⁰⁶ -a-p, Cd ¹⁰⁸ -d-n, Cd ¹⁰⁶ -p-y (68M49)	Ag-a-3n (48G48, 66M51)	Agra-n (19K39a, 25T47a, 48G48); G4-p-n (58B39); C4-d-In (24L40)	Ag-a-v (112851); Ag-a-v (112851); Ag-a-b (26145); Cd-a-p (68185); Cd-a-p (68185); Cd-a-p (68185); Cd-a-p (68185); Da-a-m (10C39); Da-a-m (10C39); Darant (0.01%) Cd lllm2 (66M51a); parent Cd lllm1 (20D49a, 63B50)
	eil.deil.	04 3.92 (61049)	(1,2+)
0.427, 0.347, 0.209 (K/L 3), 0.006 (K/L 0.9) spect conv (66M51)	0.119 (with IT, K/L 4.5), 0.935, 0.885, 0.665 spec coav (6543); 0.119 (weak), 0.937, 0.837, 0.654 spect coav (3585)	0.654 apect comv (35851); 0.677 (s/y 0.005) apect, apect comv (61C49)	0.172 (-100%, e/y 0.12, K/L 6.6), 0.247 (-100%, e/y 0.064, K/L 6.6), 0.247 (-100%, e/y 0.064, K/L 6.6), 0.247 (-100%, e/y 0.064, K/L 6.6), 0.173 (e/y 0.09, K/L - 8), 0.247 (e/y 0.09, K/L - 8), 0.247 (e/y 0.09, K/L - 8), 0.247 (e/x 0.09, F/L 6.6), 0.247 (e/x 0.09,

68M49) 6	EC 99+%, IT 5-0.3% (66M31)	(61C49)	EC (24140); 2. no p* (111m) 2. 0. 06.5); 1 (6.6451); no p* (46C48)
4.3 h (68M49); 4.2 h (66M51); 6.5 h (25T47); 5.2 h (48G48)	5.0 h (66M51); 4.9 h (35B51); -5 h (48G48)	66 m (58B39, 35B5); 65 m (48G48)	. 4 (66M5)); 17 4 (58B39, 10C39)
0.75 abs (68M49); -2 (weak) (25T47)		2. 25 spect (61C49)	

A chem, excit (2574); chem, mass apect (46G48); chem, excit, sep isotopes (68M49)	A chem (48C48); chem, genet chem; genet Agil0 (66M5la, 35B51)	A chem (\$6B39); chem, excit, mass spect (48G48)	A chem (10C39); chem, excit (23T47a, 46C48); mass spect (48C48)
4 10 10 10 10 10 10 10 10 10 10 10 10 10	II0m	P. IIO	Ħ _A

	AP. 1.	-	2		_		REACTOR PHISICS
Method of production and	More responsible	Ag-a-n (81842, 25147a); Cd-a-n (24L0); Cd-p-n (58199); h-n-2n (81842, 25147a); parant h ¹¹² (81842, 25147a, 90250)	Ag-a-n (81842, 25747a); In-n-2n (81842, 25747a); daughter In ^{112m} (81842, 25747a, 49G50)	In ¹¹³ -n (31K52)	Cd-p-n (\$8B39); Cd-d-n (24L40); In-n-n (\$5C48); In-y-y (IID47); daughter Sn ^{II 3} (\$8B39, 24S40a)		Cd-p-n (\$8B.91); Cd-d-n (24140, 46M49); In-n-y (241.27); 14M18, 46M49); In-n-y (241.40); In-n-2n (241.40); pall Sb (371.50); parent In II4 (49G50)
Distangration energy and scheme		(4 ±) III	(18652)		(N/2+)	In 113, I = 9/2 (87M50)	(24)
ation in Mev	Gamas-transitions	0 .154 (s/y >4) spect conv (61C49); 0.16 spect conv (88B39); 0.16 (s/y large) abs (25T47a)		0.153 scint spect (31K52)	0.392 (K/L+M 4. 2.) spect conv (59G52); 0.393 spect conv (10C51a); 0.39 spect conv (58B39); 0.39 (K/L 5. 4) spect conv (24L40); 0.39 (K/L 5. 4) spect conv (24L40); (62C52); 0.39 (K/ 0. 55) scrit spect (62C52); 0.39 (K/ 0. 35, K/L 5. 4) spect conv, ion ch (65T5);		γ ₀ with In!!  γ ₀ with In!!  γ ₁ 0.190, γ ₂ 0.552, γ ₃ 0.722, γ ₄ 1.27 (γ ₁ /γ ₂ /γ ₃ /γ ₄ = 100/18.6/  18.6.1.2 1 pect (18.25.1)  18.6.1.2 1 pect (18.25.1)  γ ₁ 0.192 (e/γ 4. Σ. K.L. 1.0) spect conv. scin spect (18.25.1);  γ ₂ 0.192 (e/γ 4. Σ. K.L. 1.0) spect conv. (19.25.1);  γ ₃ 0.191 spect conv. (10.26.1);  γ ₄ 0.191 spect conv. (10.26.1);  γ ₅ 0.191 spect conv. (10.26.1);  γ ₆ (κ/L. 1.30) spect conv. (10.26.2);  γ ₇ (ε/γ 4) spect conv. (10.26.2);  γ ₇ (κ/L. 1.6) spect conv. (10.26.2);
Reegy of radiation in Mev	Particles		p.; 1.74 spect (61C49); 1.7 spect (24L40) 0.67 spect (61C49)				
Half-life		20.9 m (35B52); 20 m (56B39); 23 m (25T47a)	14. 5 m (35B52)	2. 5 • (31K52)	104 m (24L40) 105 m (58B39)		(\$EB39) b 64
Type of		IT (81842, 25T47a)	6, 6, EC (25147a, 61C49); F/6 2.7 (61C49)	IT (31K52)	IT (58B39)		(82552)
Percent						4. 23 (24W48)	
Class and		A chem (58B39); chem, crose bomb, excit (81842); chem, excit (25T47a)	A chem, cross bomb, excit (81842); chem, excit (25147a)	E (31K52)	A chem, excit, genet (58B39)		A chem, n-capt, excit (24L37, 14M38)
Isosope		49 li 2m	In 112	£	m 113 m	EII uI	e Pil

25W48 0)	); 41W49); 70M49. [SN40a); 10C39.		34046,	34G46,	2	ம். க் ~
Cd.p.n (88B)9); In-n-2n (24L37, IP37); In-y-n (37R37a, 7C37, 25W48 12.E25); In II3.n-y (18G48a); daughter In II4m (49G50)	Cd-d-n (241460); hn-nn (18C38, 52768); hn-p (18B39), 58B39a); hn-q-a (18L39); hn-q-a (18L39); hn-q-y (17P38a, 64C39, 70M49); hn-y-y (17P38a, 64C39, 70M49); hasion Th (21751), U (5N46a); daugher Cd-ll5 (18C38, 10C39)	natural source (71M50)	Cd-p-n (8839); br-n-y (12A35, 14M38a, 34G46, 2847, 50H51); br-d-p (24L37)	Cd-p-n (2D40); h-n-y (12A35, 24L37, 34G46, 2547); h-d-p (4L37); Sn-y-p (42H47)	daughter Cd ¹¹⁷ (51C52a)	Cd-d-n (10C39, 24L40); Sn-y-p (42H47); fission U (5Nd0a, 5N40b, 67M51b), Pu (32K48); daughter Cd.17m (18C38, 24L40, 67M51b); daughter Cd.117 (51C52a)
Cd.p.n In-n-2: In-y-n 22E5. In ¹¹³ -n daughte	Cd-d-r In-p-p In-e-e In-e-e In-y-y 83S51 fission daught	natura			daughte	Cd-d-n Sn-y-p fission 67M51 daughte 24L46 daughte
Qp 1.98 (25,152) Qp 2.07 p-n threshold (66M51)	Q ₆ 0.83 (HPS) (I/2-) III5m 0.334 (I/2-) III5   0.334	Q 0. 6 calc (11849) Inils, 1 = 9/2 (87M50) (18652)	Q 3.36 (5550)   In   6	(HPS) (GPS) (GPS) (GPS) (GPS) (GPS)		
	0.335 (s/v 0.98, K/L+M 3.76) apet conv (10.12.5.9562); 0.388 (s/v -1, K/L 5.0, K/L+M 4.0) apet conv (24.140); 0.35 (K/L 5.3) apet conv (20K5); 0.37 apet, apet conv (61149); 0.35 apet (28050)		2. 090 (25%), 1. 487 (21%), 1. 274 (15%, e/v 5. 7 x 10-4), 1. 055 (54%, e/v 8.4 x 10-4), 0. 06 (25%), 0.137 (3%) apect conv (5550); 0. 137 apect conv (11550a); others (20042c, 46C40, 24L40, 1845, 42W47)	no y (14M38m)		0.161, 0.558 scint spect (20K51)
0.: 1.944 spect (25,152); 1.98 spect (34,L40); 2. 01 spect (8851a); 2. 0.5 abs (46,M49) pt+: 1. 1 abs (25,52); 0. 65 spect (56,B49a)	0. 83 spect (11849)	0.63 abs (71M50)	1. 00 (51%), 0. 87 (28%), 0. 60 (21% apect, β-γ coinc (5550); 0. 85 apect (10C39); c1 ch (48C40); 0. 7 β-γ coinc abs (258448d)	2.95 aba (13 <b>B46a, caic from</b> 241-40); 2.8 cl ch (10C39)	••• In 117	with In 17m (7) (51552a); 1.75 spect (20X51); 1.73 spect (10X59); 1.95 abs (67M51b) with In 17; 0.7 abs (51C52a)
72 • (24L37, 58B39)	4. 50 h (IID47); 4. 53 h (24L40)	6 x 10 ¹⁴ y ap act (71M50); -10 ¹⁴ y ap act (63C51)	53. 93 m (57849); 54. 31 m (38R50); 54. 05 m (50G47)	13 e (12A35, 10C39)	-70 m (51C52a)	-2. 5 h (51G52a); 1. 95 h (24L40); 1. 90 h (67M5lb)
p 697%, EC 93%, p 93%, p 94%,	IT (24139), 6- (11B49); IT 95%, 6- 5% (10L52)	63C51)	6 (241.37)	6 (24137)	IT, p (SIC524)	p (10C39)
		95. 77 (24W48)				
A excit (7637, 37837a, 241.37); n-capt, sep tiotopes (18646a)	A chem, excit (18G38)	A chem, sep isotopes (71M50)	A chem, n-capt (12A35); chem, excit; n-capt (24L37)	A n-capt (12A35); excit, n-capt (24L37)	A chem, genet (51C52a)	A chem, excit (10C39)
	In 115m	111 In	In 116 m	911 ui	m ¹¹⁷ m	In 117

Isotope	O Bes	Percent	Type of	Half-life		Energy of radiation in Mev	Distangrados energy and scheme	Method of production and
ر د	identificacion	*Demograpios			Particles	Gamma-transitions		
49 ^{In} 118	B excit, sep- isotopes		p (23D49b)	4. 5 m (23D49b) 1. 5 abs (23D49b)	1. 5 abe (23D49b)	y (23D49b)		Sn119 - y - p (23D49b)
ęn ai	B chem, excit, sep isotopes (23D49b)		p* (23D49b)	17. 5 m (23D4%)	2.7 abs (23D49b)	во γ (23D49b)		Sa ¹²⁰ -y-p (23D49b)
50 ^{Sn} 108	B chem, sep isotopes (68M49)		EC (68M49)	4.0 h (66MS1); 4.5 h (68M49)				Cd106-a-2n (68M49); Cd-a-2n (66M31); parent In106 (68M49, 37L50, 64M31);
. Ill	B chem, sep isotopes (AAHA9)		EC -71%, p+-29%	35.0 m (66H49); 35.m (66M51)	1. 51 spect (66M51): 1. 5 abs (66H49)			epail Sb (37L50) Cd-a-3n (66M51); Cd ¹⁰⁸ -a-n (66H49)
Sn 112		0.95 (1B50)						
Sn ¹¹³	A chem, excit (56B39, 12L39c)		EC, no 6 ⁺ (58B39); EC (L/K -0.8) (26T51)	112 d (19N50); 118 d (10C514); 105 d (58B39)		with In 113m. 0. 393 (10C5la, \$8B39, 24L40, 62C52, 24T51); 0. 401 (weak), 0. 255 (weak) spect conv (10C5la);	Q _{EC} 0.43 calc (26T51)	Cd-a-n (12L.39c); In-p-n (58B39); In-d-2n (55C47); Sn-d-p (12L.39c); Sn-y-n (60M48);
						no 0.09 y (65C47, 26T51, 10C51a, 63M51a, 28B51)	(1/2-) In   3 m	Sn.n.y (2847, 28B51); Sn.lt., vy (19N50, 63M51a, InCSta); spall Sb (37L50); parent In 113m (58B39, 24840a)
Sn 114		0. 65 (1B50)						
8n 115		0.34 (1850)					8n ¹¹⁵ , I = 1/2 (87M50)	
Sa 116		14. 24 (1B50)		_			Sn ¹¹⁶ , I = 0 (87M50)	
Sn 117m	A chem (12L39c); chem, sep isotopes, cross bomb (68M50)		IT (68M50)	14. 0 d (10C51a): 15 d (19N50)		0.159 (e/y very hirge, K/L 2. 2), 0.162 (e/g/Y 0.10) spect conv. e-y coinc, x-y coinc (63M50); 0.156 (e/g, x-y coinc (63M50); 0.156 (e/g, x-y coinc (53M50); 0.157 (k/L 2. 2) spect conv (10C31a); (61H50a); 0.152 (K/L 2. 4) spect conv (19N50)	(3/2+) (1/2+) (1/2+) (63M50, 18652)	Cd ¹¹⁴ -a-n (68M50); Cd-a-n (12L39c); Sn ¹¹⁶ -n-y (53M50,19N50); Sn ¹¹⁶ -n-, Sn ¹¹⁸ -n-2n (68M50); Sn ¹¹⁷ -n-n (68M50,19N50); spall Sb (37L50)
Sn 117		7.57 (1850)					8n ¹¹⁷ , I = 1/2 (87M50) 8n ¹¹⁸ , I = 0 (87M50)	

	A cham, n-capt, esp isolope (63M50)	8. 58 (1850)	IT (63M50)	- 250 d (63M50p - 245 d (19N50)		γ ₁ 0. 0653 [K/L 0. 5], L/M -4), (C/H 1); γ ₂ 0. 0242 (L/M -4) spect conv (G/H 1); γ ₂ 0. 0238 (ε/γ -7) scint spect, lon ch γγ y colnc (2895)); γ ₁ 0. 065, γ ₂ 0. 024 scint spect, lon ch conv (1783b); γ ₁ 0. 064 (K/L 0. 82) spect conv (19930)	(11/2-) Sn ^{119m} 0.089 (3/2+) 0.024 (1/2+) 0.024 (1/351b, 2885t, 18632) 8n ¹¹⁹ , 1 = 1/2 (87M50)	8n 118 n.y (63M50, 19v50, 1785lb, 28B51)
Sn 120		32. 97 (1B50)					Sn ¹²⁰ , I = 0 (87M50)	
Sn2lm	E sep isotopes, n-capt (19N50)		(19NSO)	>400 d (19N50)	0. 42 epect (19N50)			Sn ¹²⁰ -n-y (19N50)
9n 121	A chem, excit (121.9c); chem, asp isotopes (37.1.48a)		p_ (12L.39c)	27. s h (19N50); 28 h (23D49c); -27 h (6F51)	0.383 apact (23D49c); 0.4 aba (37L48a); 0.35 aba (39L49)	no y (23049c, 37L48a, 7N49b); others (52M51)	(3224) Sn  2  Q ₆ 0.36 (23249c) (5x24) (18652)	5n-d-p (121.39c); 5n-n-y (121.39c, 2547); 5n20-d-p (371.48a, 391.49, 7N49b); 5n20-n-y (391.49, 23D49c, 19N50); 5n-d-n (319.49); 5n-1-n-n (391.49); 5n-1-n-n (391.49); U (6048, 6F51)
Sn 122		4. 71 (1B50)						
Sn 123	A chem (12L39c); chem, aep isotopes, excit (7049b, 39L49, 19N50)		p ⁻ (12L.39c)	39. 5 m (23D49c); 40 m (12L39c, 19L49, 19N50); 41. 5 m (60M48); 39 m (7N49b)	1. 26 spect (23D49c); 1. 3 abs (39L49); 1. 1 abs (19N50)	0.153 spect conv. β-e coinc (23D-9c); 0.153 scint spect (76B51c); others (32M51)	Op1.4 (HPS)	Sn-d-p ((21.39c.); Sn-n-y (2547); Sn-n-A ((1971); Sn-y-n (60448, 7149); Sn ¹²⁴ -n-y (23049c, 39L49, 19350); Sn ¹²⁴ -n-2n (39L49)
Sn 123	A chem (40146, 40151); 60151); inotopes, cross bomb (39149)		p (40L51)	136 d (38G51); 125 d (10C51a); 126 d (10C51a); 7N49b; 40L51); 126 d (19N50)	1. 42 spect (24K50b); 1. 3 abs (39L49)	38GS1)	Q1.4 (HPS) (72+) 0.153 (72+) 0.153 (186.52)	Sn. 122. Sn. 122. d-p. Sn. 124. n. 2n. (39. 449); Sn. 124. d-t. (7149b); Sn. 124. d-t. (7149b); Sn. 125. d-t. (7149b); pall. (fission Th. (7149b), (16. fission U. (85. fission U. (65. fission U. (86. ft. 40. 15)); U. (25. fission U. (38. ft. 40. 15)); U. (38. ft. 40. ft
Sn 224		5.96 (1B50)		double p ⁻ decay:(lower limit, by ap act) >2 x 10 ¹⁷ y (41452, 12F 52, 70H 52); >10 ¹⁷ y 25P 52, 10 ¹⁸ y (41L51, 25P 52)				

	7		7		Recent of rad	Recent of radiation in May		Water of section 1
V Z	identification	abundance	decay	Half-life	Particles	Gamas-transitions	Disintegration energy and scheme	generic relationships
508n ¹²⁵	A chem, excit, n-capt (1213¢); chem, sep teotopes (2305¢a, 39L49, 19N50)		(121.39c)	9. 5 m (19N50); 9. 8 m (39L49)	2.04, 1.17, 0.51 (?) spect (2315508); 2.06, -0.5 abs (19N50)	0.326, others 21 (weak) spect, spect cany (23D50a); 0.36 (coinc with 2, 06 6) abs, 6-y coinc (19N50); 1.37 (weak) scint spect (76B51c)	Q ₆ -2.4 (HP8)	8n-d-p (121.39c.); 8n-n-y (121.39c, 23547, 2547); 5n ¹²⁴ -n-y (391.49, 23D50a, 19N50)
8n 125	A chem (12L.39c); chem, excit, asp isotopes (35L.49); chem, esp isotopes, n-capt, genet (9N50)		p ⁻ (121.39c)	9. 4 d (19N50); 10. 0 d (19149); 9. 5 d (7N49b)	2.37 (-95%), 0.40 (-5%) spect (61H50); (61H50); (2.3) spect (24K50); (26M52a); (26M52a); others (65C47, 7N49b, 39L49, 77551a)	1. 90 ecint epect, abe (76B5id); 1. 67 coint abe sec (26M52a)	0 ₅ - 2. 4 (HPS)	5n-n-y (12139c, 2847); 5n-d-p (12139c, 65647); 5n124-n-y (1314a, 19430); 5n124-d-p (1314a); 5n11-fission Th (7764a), U (6951); fission U23 (6154a, 3653), U (16643b, 77551a), U235 (13653);
Sn 126	B chem, genet (80B51)		p_ (80B51)	-50 m yield (80B51)				parent Sb ¹²⁵ (19N50); not parent Sb ¹²⁵ (7N49b) (fasion U ²³⁵ , parent Sb ¹²⁶ (80B51)
Sn 127	A chem, genet (80B51)		p (80B51)	1. 5 h yield (80B51)				fission U ²³⁵ , parent Sp ¹²⁷ (80B51)
51.20 116	A chem, excit, mass spect (27T49)		p ⁺ (27T49)	60 m (27T49)	-1. 45 apact (27T49)			In-a-3n (27T49)
88 II7	A chem (12L.39d); chem, excit, mass spect (27T49)		EC (65C47)	2.8 h (65C47, 27T49)		0.156 spect conv (27T49)		In-a-2n (27T49); Sn-d-n (12L39d, 65C47); Sn-p-n (65C47); epall I (*) (51W52)
Sp. 118	B excit (27R40)		p ⁺ (37L48a)	3.5 m (37L48a); 3.6 m (27R40)	3.1 abe, spect (37L48s)			In-a-n (38L39, 27R40); Sn-p-n (2D40); daughter Te ¹¹⁸ (37L48a)
SI 48	A chem, cross bomb (65C47); chem, excit, mass spect (27T49)		EC (65C47)	5.1 h (65C47, 27T49)	e -0. 2 abe (65C47)	0. 260 spect conv (27T49); 1. 5 abs (65C47)		In-a-n (65C47, 27T49); Sn-d-n (65C47)
Sp. 119	B chem, crose bomb (65C47)		EC (65C47)	39 h (65C47, 37L48a)		no y (65C47); Sn K-x (65C47, 37L48a)		Sn-d-n, Sn-p-n (65C47); spall Sb (37L48a); daughter Tell9 (37L48a)
<b>SP</b> 120	D chem, sep isotopes (371.48s)		EC (371.48a)	6.0 a (371.48a)		-1.1 abs (37L48a)		Sb-d-p2n (37L48a); Sn ¹²⁰ -d-2n (37L48a); pgall-fisaion Bi (11G49); not found: Sn-p, Sb-y (47B31); Sb-x rays (30K5la)

NUCLEAR PHIMES							Chap. 1.
Sn-d-n (121.394); Sn-p-n (47850); Sn-p-n (47850); Sn-12n (1P37, 6137, 21.344, 7C.37) Sp-n-2n (137839, 12P48, 27M49, 25.9448, 22.850); Sb-p-pn (23.846)		Sb-n-y (38M47); Sb ¹²¹ -n-y (38M51, 31K51)	Sn-d-2n (12L39d); Sn-p-n (47B51); Sh-q-n (12L39d); Sb-q-n (12L39d, 47B51); Sp-n-y (12A35, 12L39d, 2847, 50H51); spall Sb (37L50), I (*)(51W52); spall-fission Bi (11C49)		Sb-n-y, Sb ¹²³ -n-y (38M47)	Sb-n-y, Sb ¹²³ -n-y (38M47)	Sn-p-n (4785)); Sn-d-x (121.394); Sn-d-x (121.394, 54H3, 42K45); Sp-n-y (121.394, 2547); Sp-n-y (121.394); Tp-d-n (121.396); I-n-n (121.396); I-n-n (121.396);
(0+) (47850)	Sb ¹²¹ , I = 5/2 (87M50)	25,122 007	(18G52) (18G52) (19G52) (19G52) (18G52)	Sb ¹²³ , I = 7/2 (87M50)	Q _p 2.92 (HPS) Sb ²⁴ m ₂ Ocies		(c+) (c+) (c+) (c+) (c+) (c+)
Y ₁ 0.90, Y ₂ 1.30, Y ₃ 2.20 (Y ₁ /Y ₂ /Y ₃ - 0.08/0.35/0.04) (s/y very small) spect (47B50)		0.068 scint spect (38M51); 0.059, 0.074 ion ch (31K51)	0. 568 spect (28C48d, 28K48); 0. 57 spect conv (IIR47); 0. 56 (e _K /y 0. 0049), 0. 68 (51G52)		0.0185 (e/y very large) (18G50)	0.012 (e/y very large) (18G50)	0.121, 0.607, 0.653, 0.730, 1.706, 1.708, 2.04 spect; spect conv. (26.464, 101.509); 0.61 y (40-50.5, eg/y 0.0043) spect; spect conv. (44.45.2.1); 0.61 y (eg/y 0.0036) spect; conv. (44.45.2.1); 0.603, 1.005, ey/ -0.002), 0.650, 0.603, 1.005, ey/ -0.002), 0.650, 0.603, 1.005, ey/ -0.002), 0.650, 0.603, 1.105, ey/ -0.002, 0.650, 0.651, 1.67, 2.07 spect; 118.47, 113.49b); 0.598, 0.645, 0.817, 1.67, 2.07 spect; 118.47, 1.4440, 42.W47, 5.2M51, 815551, 89522, 39D51, 39D51a, 42.K465, 47.M47)
l. 70 epect (47 <u>8</u> 50)			β ₂ 1.46 (coinc with γ) β-γ coinc spect (23451); δ ₁ 1.94, β ₂ 1.36 spect (43446); β ₁ 1.8 β ₂ 1. 2 abs, coinc abs (264480); β ₁ 1.8 abs (14440)			3. 2 abs (38M47)	b ₁ 2. 291 (21%), b ₂ 1. 69 (7%), b ₃ 0. 95 (7%), b ₄ 0. 66 (26%), b ₅ 0. 50 (26%), b ₅ 0. 50 (36%), b ₅ 10.20b); b ₄ 0. 62 (44%), b ₅ 1. 00 (9%), b ₄ 0. 65 (44%), b ₅ 0. 65 (44%), cothera (5444), 47M47, 43M46, 14M40, 37W47)
16.4 m (22350); 16.6 m (12P48); 17 m (6H37, 12L394)		3.5 m (38)447)	2. 8 d (121.39b);		21 m (38M47)	l. 3 m (38M47)	(P6 q (1717)84)
677850)		IT (38M47)	p' (12L394)		IT, p [*] (38M47)	IT, p (38M47)	f (121.39d); no ft no EC (101.50b)
	57. 25 (24W48)			42.75 (24W48)			
A chem, excit (17839, 64137, 7C37); chem excit, crose bomb (12L37a)		A chem, n-capt, sep isotopes (38M47)	A chem (12A35); chem, cross bomb (12L394)		A chem, n-capt, sep isotopes (38M47)	A chem, n-capt, sep isotopes (38M47)	A chem (121.37a); chem, excit; cross bomb (121.39d)
35, 120	171 es	Sb ^{122m}	\$6,12\$	Sb 123	Sb 124m2	Sb ^{124m} 1	\$2 ₁₂

V Z	Class and identification	Percent abundance	Type of decay	Half-life	Backy of radiation in Mev	ation in Mev Gamma-transitions	Distangration energy and scheme	Method of production and generic relationships	CILA
51.80.125	A chem (121.39d); chem, n-capt (84651)		p (67C51)	-2.7 y (40 <u>1514)</u>	0. 616 (18%), 0.299 (49%), 0.128 (31%) spect (78494); 0.61% others (7) spect (28K49); others (38C44); 26K496, 15.149, 26K496, 84851)	0.637, 0.601, 0.465, 0.425, 0.115, 0.515, 0.155, 0.115, 0.515, 0.425, 0.646 (weak, e/v ery small), 0.464 (weak, e/v ery small), 0.464 (weak, e/v ery small), 0.431 (weak) spect, spect conv. coinc. (28K49); with T-125m; 0.125 (weak) 7.125m; 0.10, 0.03 (28B52, 10CS1a, T-3494, 28K49, 67H49a)	(175494) (175494) (175494) (175494) (175494) (175494) (175494)	Sn-d-n (12L39d); Sn-n-v, T decay (7549d, 23F46, 46481); span-d'esion Th (7N49a); (6754, 46L51a, 84531); parent T-l-tam (25F4, 28K49); parent T-l-tam (23F4, 2015); not daughter (9.4 d) Sn 25 (19N50); not daughter (9.4 d) Sn 25 (19N50);	I . 1.0
38 126	B chem, excit (80B51)		p* (80B51)	9 h (80B51)	-1 abe (80B51)	0.90, -0.4 (both coinc with p) scint spect, p-y coinc (80B51)		fission U ²³⁵ , daughter Sn 126 (80B51)	
£	E chem (80B51)		p (80B51)	10 m (80B51)				fleeion U ²³⁵ (80B51)	
Sp-126	D chem (38G46)		p (38G46)	28 d (38G46); -30 d (80B51)	1. 9 (38G46)			fission U (38G46), U ²³⁵ (80B51)	
Sb 127	A chem, genet (32A39)		p (32A39)	93 h (76SS1b); 95 h (38G46)	1. 2 abs (7685lb); 0. 8 abs (38G46)	0.72 abe (76851b)		ficeion U ²³³ (61548), U ²³⁵ (18G51, 80B51), U (32A39, 38G46, 7é§§B), Pu (32K48);	
								perent Te ¹²⁷ (32A39, 33G51i); perent (84 %) Te 127, perent (16 %) Te 127m (78B48); daughter Sn ¹²⁷ (80B51)	
<b>8</b> 129	A chem, genet (32A39)		p ⁻ (32A39)	4. 2 h (32A39)				fission U (32A39), Pu (32K48); parent Te ¹²⁹ (32A39)	
<b>36</b> 130	D chem, excit (fission yield) (80B52)		p_ (80B52)	40 m (80B52)				fission U ²³⁵ (80B52)	
<b>8</b> 130	D chem, excit (flesion yield) (30P52a)		p_ (80B52)	12 m (30P52a); 10 m (80B52)				fission U (80B52, 30P52s)	1007
E &	A chem, genet (30P51, 68C51)		p (30P51)	23.1 m (30P51); -20 m (68C51)				fission U, parent Te 131, parent Tel 31m (30PS1, 68CS1)	
SP 132	B chem, genet (32A39)		p^ (32A39)	2 m (30P51); -5 m (32A39); -2 m (68C51)				ficeion U (32A39, 30P51, 68C51); parent Te ¹³² (32A39, 30P52a)	
251.08	B chem, genet (30P51)		p (30P51)	4. 4 m (30P51); 4. 2 m (68C51)				fission U (30P51, 68C51); parent Tel33m (30P51)	

flesion U (30P5), 68C51)	opail Sb (37L48a), I (e) (51W52)	Sb-d-5n, parent (4 m) Sb 118 (37L48a, 37L50); eahl 1 (a) (51W52);	spall-fission Bi (ilG49)  20-d-4n, parent Sb (371.48a, 371.50); spall-fission Bi (ilG49)		Tellin Sb-d-Jn (13840); 43850; 48E46a, 43850; 14E46a, 43850; 14E46a, Sb-p. (13540, 14E46a); spall Sb (37120); Tel ²⁰ n-y (10C5la); parent Tel ²¹ (82B46)	SS-4-2m (1AE46a); SS-4-2m (1AE46a); SS-p-m (14E46a); daughter Tellm (82B46); daughter Till (74M50) 7H52)		-0.248 T ₂ 122. _{10.7} (67149, 43K50, 12,122. _{10.7} (67149, 43K50, 10.59)	
					(1.75-)	1901)	# E E E E	- (-44/1) - (-44/1)	o o
		no y (7) (37L48a)	1. 6 abe (371.50)		γ ₁ 0.082 (a/y very large, K/L 0.75), γ ₂ 0.213 (a _K /γ 0.09, K/L 7.3) (γ ₂ coinc with γ ₁ ) spect coar, coar-γ coinc, coar-coar γ ₁ 0.0018, γ ₂ 0.214 spect coar (10C5la); others (47H49, 81844, 82844,	$v_1$ 0. 306 (13%, $e/v$ -0. 018, $K/L+h$ $v_1$ 0. 306 (13%, $e/v$ -0. 018, $K/L+h$ $b_1$ $v_2$ 0. 573 (87%, mot colac with $v_1$ $e/v$ 0. 009, $K/L+h$ $b$ ) apact conv. etin spect (67HS2); 0.575 spect conv (10CS1s); -0.61 ( $e/v$ 0. 004) spect conv (43KG) 0. 5 abs (14K46s)		γ, 0.0825 (eγγ very large, K/L 0.69), γ ₂ 0.199 (e _K γ' 0.18, K/L 8.9) (γ, coinc with γ ₂ ) spect conv γ-conv coinc, conv-conv coinc, be (33K50); conv-conv coinc, γ ₁ 0.087, γ ₂ 0.199 spect conv (10.53a); γ ₂ (eγγ' 0.19) spect conv (53K52a); γ ₂ (eγγ' 0.19) scint spect (53K52a); so 0.23 γ (lim 0.5\$) scint spect	(68H51); others (4K42a, 67H49, 20D50,
			conv: 0.2, 0.5 spect conv (37L48a)						
-50 e (30P51); 45 e (68C51)	2. 5 h (371.48a)	6.0 d (371.48a)	4. 5 d (371.48a)		154 d (67H3Id); 143 d (14E46a); 125 d (13840); 140 d (10C5ia)	17 d (14E46a); -16 d (82B46)	7	121 d (10C51a)	
p (30P51)	p+ (371.48b)	EC (371.48a)	EC (371.48m)		IT (14E46a)	EC (14E46a)	7	(6886)	
				0.089 (1850)			2. 46 (1850)		
D chem (30P51)	D chem (371.48a)	B chem, genet (37L48a)	B chem, genet (37L/8a)		A chem, excit, cross bomb (13840); chem, a-capt, sep isotopes (10C5is)	A chem, genet (14E46a, 82B46)		A cham, n-capt, applications (67H49)	
<b>36</b> 134136	\$17°478	Teus	T. 119	T. 120	T. 121m	T. 121	Te,122	•	

	7		Tree of		Baerry of rad	Sasegy of radiation in Mey		Method of production and
V Z	identification	spendence	, and	Half-life	Particles	Gemma-transitions	Desempration energy and ethems	generic relationships
52Te 124 Te 125m	A chem, genet (23F48)	4. 61 (1B50)	IT (23F48)	58 d (67H49a, 67H5ld)		0.110 (e _K /y -160, K/L+M 1.15), 0.0355 (e _K /y -11.7, K/L/M = 7.3/1.0/0.16) spect core, or ch. ecint spect, x-y coinc, x-x coinc (25852); 0.110, 0.0333 spect core (10C51a);	25, 25 (11/2-) Te ^{[25m} 0145	Te 124 n-y (67149); daugher 59. ¹²⁵ (23F48, 28K49); not daugher 1 ¹²⁸ (iim 0.05%)
						0.110 (K,LaM. 1.1), 0.035 spect conv (18449); 0.110 (K,L. 1.2) spect conv (18449); 0.109 (e/v. >100. K/L1.5, L/M -3.5) spect conv (671449); other (67149, 238 50a, 52M5); 28649)	(372+) 0.035 (1/2+) 0.035 (1/2+) 0.035	
Te 125		6.99 (1850)					Te ¹²⁵ , I = 1/2 (87M50)	
Te 126		18. 71 (1B50)					Te ¹²⁶ , I = 0 (87M50)	
Те 127 т	A chem, excit, genet (13540)		IT (13540)	115 d (10C51a); 90 d (13S40)		0.0885 (K/L. 0.75) spect conv (67H49, 67H49a); 0.0887 spect conv (10C5la); 0.086 (e/y very large, K/L. 0.75) spect cnv (2H41)	(11/2-) Te 127m 0.099 (3/2+) Te 127 0.099	Te-n-v (13540, 2547); Te-d-p (13540); Te-lo-n-v (671449); fission U (38046, 33GS1i, 43.948), UZ3 (61548, 38G48, 36GS1), UZ35 (16348, 38G48, 43.945); parent Te-l ²⁷ (13540, 33GS1i, 43.945);
T•127	A chem (28738, 32A39); chem, excit, cross bomb (13840)		6 (32A39)	9.3 h (13 <b>54</b> 0)	0. 7 abs (13GSii)	no y (33G511)	(+2/5)	Te-n-y (13840, 2547); Te-d-p (28738, 13640); Te-n-z n (28738); Te-n-p (13840); fission U (12A59, 13540, 43W48, 13540, 43W48);
Te 128		31. 79 (1850)					Te ¹²⁸ , I = 0 (87M50)	daugher Solet (32A39, 33G511), (84%) (78B48)

T. 129m	A chem, genet (13540)		IT (13S40)	33, 5 d (10CS1a); 32 d (13S40, IN91a)		0.1060 spect conv (10CSia); 0.106 (K/L -1) spect conv (67H49); 0.102 (e/y very large, K/L -1) spect conv (2H41)	(11/2-) Te ¹²⁹ m 0.106	Te ¹²⁸ n.y (67149); Te-n-y (11540, 2547); Te-n-y (11536); Te-n-1536 (28T18); Te-y-n (255 W8); Hission U (16143), 38G46, 43 W48, 1NS1a, 30P51a), U233 (18G4); 18G51); U233 (18G51); U334 43 Parent Te ¹²⁹ (13540, 38G46,
Te 129	A chem, excit (37B39, 13S40)		6 (13540)	72 m (13540); 70 m (32A39, 33G511); 67 m (25W48)	l. 8 spect (IR47); l. 7 abs (33G3li)	0.3, 0.8 abs (33G5li)	(344,529)	Te-n-y (13540, 2547); Te-d-p (13540, 28738); Te-y-n (131839, 28748); If asion Th (72181); 161430, 386246, 41948, (1818); Aughter Te ^{2,270} (13540, 38646, 43195);
re ¹³⁰		34. 49 (IBSO)		double beta decay; -10 ²¹ y Xe ratios, mass spect (3150b)			Te ¹³⁰ , I = 0 (87M50)	(CARC)
Te 131m	A chem, genet (13540)		IT (13840)	30 h (32A39. 13S40)		0.177 (K/L 2) spect conv (2H41)	171-0-177 (3/2+) 16/31 0.177 (3/2+) 16/31 0.177 3/3-4 0.16	Te-n-y (13540, 2547); Te-d-p (13540); spal-fission U (6F51); fission U (6F51); 3254d 43,945; 30P513; parent Te ¹³¹ (32A39, 1354); 43,951)
T. 131	A chem, excit (13540)		p ⁻ (13S40)	24.8 m (37G52); 25 m (13S40)	2.0 (-55%), 1.4 (-45%) abs. p-y coinc (37G52)	0.16, 0.7 abs (37G52)	(18652,37652)	Te-d-p (13540); Te-n-y (13540, 2547, 37G52); finsion of (132A39); daughter Te ¹³¹¹ (12A39, 13540, 4395); parent 131 (32A39, 13540, 30P31, 68C51); daughter Sb ¹³¹ (30P51, 68C51)
Te 132	B chem (32A39); fission fragment range (32K48)		6 (32439)	77. 7 h (30P5la): 77 h (32A39)	0. 22 spect (10L51a); 0. 3, -0.1(?) abs (1N51b); -0. 3 abs (70B43a)	0. 22 abs (INS1b)		Te-a-2p (112551); spall-fission Th (7N49a); fission Th (16H39a, 72B5), 21751, U (32A39, 16H39a, 16H39a, Nixib, 30P51a), Pu (32K4B); daughter Sb ¹³² (32A39, 30P52a); parent 11 ³² (2A39, 16H39a, 16H39a, 1N51b, 44W51)

- Indiana	Class and	Percent	Type of		Energy of rac	Energy of radiation in Mey		Method of recoduction and
V Z	identification	abuadance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
52Te 133m	A chem, genet (32A39)		IT (30P52)	63 m (30P52); 60 m (32A39, 16 W40)		- 0.4 acint spect (30PS2); with Te ¹³³ : 0.6, 1.0 abs (30P52)	(11/2-) Te 133 m O.4 (3/2+) Te 133 O.4	fission U (32A39, 16H39a, 24S40, 16W40, 30P51), Pu (32K48); parent Te 133 (30P52);
Te ^{l33}	A chem. genet (30P52)		6 (30P52)	2 m (30P52)	2.4 (-30%), 1.3 (-70%) abs (30952)	0. 6, 1.0 abe (30P52)	**************************************	ancestor (133 (32A39, 16H39a, 24540, 16 W40, 16 W44, 30P51); daughter Sb ¹³³ (30P51) daughter Te ^{133m} (30P52); parent 1 ¹³³ (30P52a)
							3.0 (3.05%)	
1. T.	B chem, genet (32A39)		p (32A39)	44 m (30P5la); 43 m (32A39)				fission Th (9P40), U (32A39, 16H39s, 30P5ls), Pu (32K48); parent 1 ¹³⁴ (32A39, 16H39s, 30P5ls)
T• 135	[A] genet (22D40)		6 (22D40)	<2 m (33G51j, 32K51e, 22D40)				fission U, parent 1 ¹³⁵ (33G51j, 32K51e)
ů	E chem (16H43b)		6 ⁻ (16H43b)	-1 m (16H43b)				fission U (16H43b)
53 ¹ 20	D chem (74M50)		p ⁺ (74 <b>14</b> 50)	30 m (74M50)	4.0 abs, spect (74M50)			spail Sn (second order reaction) (74M5); Sb-a-5n (74M50)
71.	B chem, genet (74M50)		6 ⁺ (74M50)	1. 8 h (74M50) 1. 8 h (74M50)	1. 2 abs, spect (74M50); 1. 2, 4.0 (weak) (40D52); conv: 0. 185 spect (74M50)			spall Sn (second order reaction) [14M5]); Sb-a-4n, parent Te 2] [14M50]; daugher Xe ¹² (17T52, 8H52b, 40D52)
27 ¹	A chem, excit (74M50); sep isotopes (7Y51)		p ⁺ (74M50)	3.6 m (7Y51); 3.4 m (40D52); 4 m (74M50)	3.6 m (7Y51); 2.9 abs (74M50); 3.4 m (40D52); 3.1 abs (7Y51) 4 m (74M50)			Sb-a-3n (74M50); Te ¹²² -p-n (7Y51); daughter Xe ¹²² (37T52, 8H52b, 40D52)
1 ₂₂ 1	A chem, excit (74M50); chem, esp isotopes (14M49)		EC (74M50)	13.0 h (14M49); 13 h (74M50)		0. 159 spect, spect conv (14M49)		spail Sn (second order reaction) (74MS1); Sb-e-2n (74MS9); Sp ¹²¹ -e-2n (14M49); daugher Xe ¹²³ (37T52, 8H32b, 40D52)

NUCLEAR PHYSICS			CHAP. 1.
spall &n (second order reaction) (74451); Sb-e-n (121.38e, 74450); Sb-e-1n (74450); Sb-e-1n (74450); Te-p-n (2040); spall-fission Bi (11G49, 66B51)	Sb-a-2n (74M50); Te-d-u (1784a); Jepall-fission Bi (11G9, 6651); daughter Xe ¹²⁵ (67B51b); not parent Te ^{125m} (lim 0.05%)	reaction (74451); Sb-an (12L38e; 74450); Tr-d-n (12L38e; 74450); Tr-p-n (12D40); I-n-2n (12L38e; 28T38, 12P51); I-y-n (12P40, 27k440, 3050); spall-fission Bi (11G49, 66B31)	1-n-y (12A35, 28T38, 2847, 7846, 9049, 50H31); Te-d-2n (12L38e); Te-p-n (2D40)
28 124 124 124 124 124 124 124 124 124 124	Q _{EC} -0.13 calc (38M52) Q _{EC} -0.13 calc (38M52) (M2+) 125 (M2+) 125 (M2	Cp 1.27 (12P51) (12P51) (12P51, 855516)	1 ¹²⁷ , 1 = 5/2 (87M50) O _p 2.0 (7846) FC   128 EC   17846
0.603, 0.73, 1.72, 1.95 spect, spect conv (143449); no y coinc with 2.2 p ⁺ , p-y coinc (85831); y-y, p-y coinc (37349)	0.035 ion ch (23F5lb); 0.0355, no 0.109 y spect conv (67B5lb)	with \$\beta\$.  0.382 spect conv. \$\theta\$-\$\text{v}\$ coinc (1229);  0.395 spect, spect conv (14M49); with EC; 0.64 (wask) scint spect, x-\$\text{v}\$ coinc, \text{v}\$ coinc, \text{v}\$ coinc (12P5));  others (6955)	0. 428 (7%) spect (7546)
4. 5 d (74M50); 2. 20 (51%), 1. 50 (44%), 0. 7 (5%) 4. 0 d (12L.39e, gpsect (14M69); 2D40) 2. 1 spect, abs (74M50)		p: 1. 268 (27%), 0. 85 (73%) spect (14849); 1. 24 (-25%), 0. 85 (-75%) spect (12P5); 0. 865 spect (23M5la)	2. 02 spect (7346)
4. 5 d (74M50); 4. 0 d (12L39e, 2D40)	60 0 d (23£51b); 56 d (17R46a)	13. 0 d (121.38e); p.: 13. d (281.38) 1 1 0	24. 99 m (69141)
EC - 70%, 8 30% (74M50)	EC (L/K 0. 23) (28M5); EC (L/K 0. 3) (23F5ib); no p* (13G47)	EC -58%, p ⁻ -40%, p ⁺ (?) -2%(12P5))	F 95.0%, EC+ pt 2.0% (28850); EC/F 0.063 (41M51a)
	•		100 (6N37)
A chem, axcit, cross bomb (121.38s)	A chem (17846a); chem, excit (33647); genet (67B5lb)	A excit (28738); chem, excit, cross bomb (121.38e)	A chem, n-capt (12A35)
*21.1	1125	921	127 128

CHAP. 1.2 REACTOR PHYSICS

Teorone	Class and	Percent	Type of	******	Energy of rad	Energy of radiation in Mev		Method of production and
Y Z	identification	abundance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
53 ¹ 29	A chem, n-capt (32K47)	,	p ⁻ (32K47)	1.72 × 10 ⁷ y space (32KSL); 3 × 10 ⁷ y sp act (26P49b)	0.12 scint spect (38M5.2); 0.12 abs (26P49b); 0.12 ion ch (83B-90); 0.13 abs (32K5!!)	0.039 (coinc with β', e _K /γ - 6, K/L - 40) ion ch, β-γ coinc (83B50)	$1^{129}$ , $1 = 7/2$ (87M50) $(772+)$ $1^{129}$ $(772+)$ $(72+)$ $(72+)$ $(72+)$ $(72+)$ $(72+)$ $(72+)$ $(83850, 30752, 18652)$	fission U (32K47, 26P49b, 83B50)
130	A chem, cross bomb (12L38e)		β ⁻ (12L38e)	12.6 h (12L38e)	12.6 h (12L38e) 1.03 (-60%), 0.61 (-40%) spect (33R43)	0.744 (ε _K /γ 0.003), 0.667 (ε _K /γ 0.004), 0.537 (ε _K /γ 0.007), 0.417 (coinc with 0.6 β ⁻ ε _K /γ 0.012) (ε _K > ε _L for all γ's) spect, spect conv, β-γ, γ-γ coinc (33R43)	130 60% 60% 1.95 (33R43)	Te-d-2n (12L38e); Te-p-n (2D40); 1 ¹²⁹ -n-v (32K47); Cs-n-a (16W40)
if.	A chem (12L38e); .chem, genet (13S40)		p (12138e)	8.141 d (39551a); 8.05 d (106.952); 8.04 d (18551); 8.04 d (18551)	0.815 (0.7%), 0.608 (87.2%), 0.335 (9.7%), 0.508 (87.2%), 0.506 (2.8%), spect, f-y coinc (8B52); 0.810, 0.606, 0.335, 0.250 spect, f-y coinc (2445), 0.35, 0.250 spect, f-y coinc (2445), 0.870, 0.606, 0.339 spect (40R22); E. (average) 0.189 ion ch (77522); see also:(60C52, 11B52, 8Y51, 20N51, 10C51b, 30T51, 11B51, 22F50, 28K49, 44M48, 25D42), yy	0.080 (2.2%, coinc with 0.284 y, chirk 13.1m2), 0.284 (5.3%, k./l.7), 0.183 (coinc with x.6.3m2), 0.284 (5.3%, k./l.7), 0.284 (5.3%, k./l.2), 0.284 (5.3%, coinc with 0.089 f. cwix with 0.608 f. cwix vith 0.354 (80%, coinc with 0.356 f. cwix vith 0.256 f. cwix vith 0.256 f. cwix vith 0.285 y, cwix vith 0.386 f. cwix vith 0.283 y, cwix (69523a); f. cwix vith 0.386 f. cwix vith 0.283 y, cwix (69523a); f. cwix vith 0.386 f. cwix vith 0.283 y, cwix (69523a); f. cwix vith 0.285 f. cwix vit	(72+1)31 (72+1)31 (9/2,7/2+) (9/2,7/2+) (9/2,7/2+) (9/2,7/2+) (9/2,7/2+) (9/2,7/2+) (9/2,7/2+) (9/2,7/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (9/2+) (	Te-d-n (121.38e, 33R41a); spall-frastion Th (7189), U (16F4), 6047, 6F5); frastion Th (2175), U (132A39, 12851g), U234 (1747, 38G48, 61548, 38G5), U234 (1747, 38G5), Pu (28F5); daughter Te-l ³ f (121.38e, 23A39, 16H39a, 13540, 30F5), 66C5); parent (-1%) Xe ¹³ lm ² (48B49, 67B50b);
132	B chem, genet (32A39)		6 (32A39)	2. 4 h (32 <b>A</b> 39); 2. 3 h (16H39a)	2. 2. 0. 9 abs (IN51b); 1. 5 abs (75S49); -1. 4 abs (70B43a)	$\gamma_1$ 0.69, $\gamma_2$ 1.41, $\gamma_3$ 2.0 $(\gamma_1/\gamma_2/\gamma_3)$ = $3J/4/11, \gamma_4$ -0.8 (very weak) scint spect, $\gamma$ - $\gamma$ coinc (46M51); 0.6, 1.4 abs (IN51b)	31-	spall-fission U (16F4), 6047); fission Th (72B5), 21751), U (32A3), 16H39a, 9P40, 38G46, INSI), U U333 (38G48); daughter Te ¹³² (12A39, 16H39a, 16H39e, INSIb, 44W51)

### ### ### ### ### ### ### ### #### ####	spall-(faston Pb (21'47b), U (f6F41, 524'), ffaston U (52.49, 16H39a, 24540, 16W40, 30P5), 23551k), Pu (28F5); daughter Tel33 (32A3'9, 16H39a, 24540, 16W40, 16W45, 30P5); parent Xel33 (24540, 16W40, 16W45); parent (2.45, Xel33m (8Z5), 24K51a) spall-fission U (16F4); ffastion Th (22D39), U2355 (1V47, 38G53), U (16H39a, 32A39, 9P40, 9P40, 32L49, 32K51h, 30P51a), Pu (12K40,	268 2) 22.39 30951a 32.39 30951a ppall-(ataion U (6047); fission Th (72951), U (24540, 16040, 22240, 18045, 69475, 30551, 328519; 24.8519; parent (-307), X-135m; (-707), Xe ¹³⁵ (6947b); parent Xe ¹³⁶ (40G40, 16048); parent Xe ¹³⁶ (24540, 22D40, 40G40, 16045);	fination U (65540, 66543, 84549), U233, Pu (845549) fination U (65540, 66543, 26547, 34847, 61547a, 63549), Pur (34847), parent Xe ¹³⁷ (66543, 63549) fination U, ancestor Ca ¹³⁸ (63549)	fission U, parent Xe ¹¹⁹ ancestor Ba ¹³⁹ (63549). I-p-7n (37T52, 8H52b, 40D52); parent I ²¹ (37T52, 8H52b, 40D52); T-p-6n (37T52, 8H52b, 40D52); parent I ²² (37T52, 8H52b, 40D52); q0D52)	I-p-5n (37T52, 8H52b, 40D52); parent 1 ¹²³ (37T52, 8H52b, 40D52)
-------------------------------------------	---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------	------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------	--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------	----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------	-----------------------------------------------------------------------------------

0.53 (94%), 0.85 (5%), 1.4 (1%) scint spect, Y.Y. coinc (48B49a); 0.53 spect (6P47b); 0.55 abs (23S5lj)	>2. 2 (weak) D-y-n reaction (32L49); >1 abs (32K51h)	1. 8. 1. 27 spect (6P47b); 1. 5 abs (23551j); 1. 6 abs (32K51c); 2. 4 (1.1%) abs (32L49)	A 7 or ire anger abla (84640	69M65							
1 1 (-91%), 0.4 (-9%) abs (30P52a); 1.4 (-9%) 0.5 (-6%) abs. p-y conc (48B49a); 1.4 abs (23S51))	1. 6 (-70%), 2. 8 (-30%), hard β (weak) abs (30P52a); 1. 5-1. 75, 3. 5-4. 2 abs (32L49)	0. 5 (35%), 1. 0 (40%), 1. 4 (25%) 1. 4 abs (22K5)s; 1. 5 abs (23S5))	6 5 abs (84540)		n (mean): 0.56 abs paraffin (28H48a); 0.67 p recoil in cl ch (71B46)						
20.5 h (106B52); 22.4 h (30P51a)	52.5 m (30P5la); 51 m (32L49); 54 m (32A39)	6. 68 h (6P47b); 6. 7 h (33G5l), 32K5le)	86 . (84549)		22. 0 s (n) (28H48a); 22. 5 s (n) (34R47); 19. 3 s genet (63S49)	5.9 . (63549)	2. 7 . (63549)	40 m (40D52); 70 m (37T52); -60 m (8H52b)	19. 5 h (37T52); 20. 0 h (40D52); 19 h (8H52b)	2.1 h (37T52); 1.7 h (40D52); -2 h (8H52b)	
6 (32A39, 16H39a)	p ⁻ (32 <b>A</b> 39)	6 (22D40, 24S40)	A. (65540)		of disintegrations) (191.51a)	p (63S49)	p (63S49)			β ⁺ (40D52)	
											0.096 (6N50a)
A chem (32A39); chem, genet (16 W40)	B chem (32A39); fission fragment range (32K48)	A chem, genet (22D40, 24S40)	(6,540)		A chem (65540, 26547); chem, genet (66543, 63549)	A chem, genet (63S49)	A chem, genet (63S49)	B chem, genet (37T52, 8H52b, 40D52)	A chem, genet (37T52, 8H52b, 40D52)	A chem, genet (37T52, 8H52b, 40D52)	
Eq.	134 I	1 ¹³⁵	136		1137	I ₁₃₈	139	54 Xe 121	Xe 122	Xe 123	Xc 124

2	Page 250	Percent	Twee of		Essenty of rad	Esergy of radiation in Mey		Merhod of sanduction and
V Z	identification	abandance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
54 Xe 25	A chem, sep isotopes (33A50); chem, mass spect (67B5lb)		EC, no p [†] (67B51b, 33 <b>A</b> 50)	18 h (67B51b); 20 h (33 <b>A</b> 50)		0.054 (K/L4.3), 0.096, 0.106, 0.187 (K/L4.6), 0.243 spect conv; 0.460 scint spect (67B5lb)		Te ¹²² -a-n (33ASO); Xe-n-y (67BS1b.); parent 1 ¹²⁵ (67BS1b)
Xe126		0.090 (6N50a)						
Xe 127	D chem (29C40b)		IT (?) (29C40b)	75 • (29C40b)		0.125, 0.175 spect conv (29C40b)		I-p-n (29C40b)
Xe 127	A chem (29C40b); chem, sep isotopes (33A50); mass spect (67B51c)		EC (67B51c)	34 d (29C40b); 32 d (33A50); 25 d (67B51d)		0.057, 0.145, 0.170, 0.200, 0.365 spect conv. scint spect (67B51c)		Te ¹²⁴ -a-n (13A50); I-p-n (29C40b); I-d-2n (11042); Xe-n-y (44C44, 67B51c); daughter Ce ¹²⁷ (13F50)
Xe 128		1. 919 (6N50a)						
хе 129т	A chem, mass spect (67B51c)		IT (67B5lc)	8.0 d (67B5lc)		0.196 (K/L+M 2.1) spect conv (67B51c); 0.040 (K/L+M 4.3) spect conv	(II.72-) Xe ^{129m} 0.236	Xe-n-y (67251c)
Xe 129		26. 44 (6N50a)	_			132.100, 32.100)	(772+)	
							<del>_</del>	
xe 130		4. 08 (6N50a)					(30752, 18652)	
Xe ^{131m} 2	A chem (44C44); chem, genet (48B49); mass spect (67B50b)		IT (48B49, 44C44)	12. 0 d (67 <b>B</b> 50b)		0.163 (K/L+M 1.9, L/M 3.4) apect conv (67850b, 6785ic); 0.163 (K/L+M 1.7) apect conv (8731); 0.163 (e/y -20) abe conv, abe (48849)	134   134	Xe-n-n (44C44); daughter (-1%) 1 ¹³¹ (48B49, 67B50b); not daughter Ca ¹³¹ (43C31c); daughter Ca ¹³¹ (70C50)
Xe ^{131m} 1	A genet (14G51a)		IT (14GSla)	4.8 x 10 ⁻¹⁰ s delay coinc (14G51a, BB52a)		0. 080 scint spect (14G51a, 8B52a)	(11/2-) Xe ^{13/mg} (0.163	daughter 1 ¹³¹ (14G51a, 8B52a)
							- I	
Xe I31		21. 18 (6NSOA)					Xe ¹³¹ , I = 3/2 (87M50)	fission U (mass spect) (13T47)
xe ¹³²		26. 89 (6N50a)					Xe ¹³² , I = 0 (87M50)	fission U (mass spect) (13T47)

NUCLE	AR PHYSICS						CHAP.
Xe-n-y (67B5la); faston U (24K50c, 67B50c); daughter (2.4%) ! ¹³³ (8251, 24K5la)	Te-a-n (52C41); Xe-d-p (52C41); Xe-n-p (52C41); Ca-n-p (16W40, 44C44); Ba-n-a (16W40, 66C41); A4C44, 16W45); A4C44, 16W45); A4C44, 16W45, A4C4, 16W46, A4C4, 16W4	fission U (mass spect) (13T47)	Xe-n-2n (21R43); Xe-n-y (21R43, 21R46); Ba-n-a (66S43b); fiasion U (40C40, 16W45, 13T47); daughter (136, 1135 (6044b); parent Xe 136, 1135 (6044b);	Xe-n-v, Xe-n-2n (21843); Xe-d-p (52C41); Ba-n-a (16W40, 66S43b, 16W45); fission U (24S40, 22D40, 49B51); 40G40, 16W45); daughter 1 ¹³⁵ (24S40, 22D40, 40G40, 16W45); parent Ca ¹³⁵ (16W45); parent Ca ¹³⁵ (63S4a); parent Ca ¹³⁵ (14G53)	fission U (mass spect) (13747); daughter 1 ¹³⁷ (-6% of dis) (19251a)	Xe-n-y (21R43, 66543b, 63549). fission U (66543, 63549, 31G51k); daughter 1 ¹³⁷ (66543, 63549); parent Ca ¹³⁷ (21T51b, 33G51k)	fission U (16H39s, 16H40s, 36G4n, 66S43b); parent Cs ¹³⁸ (16H39s, 36G40, 66S43b)
(II/2-) Xe ¹³³ m (II/2-) Xe ¹³³	(18G52) (18G52) (1772+) — QOBI (772+) — QOBI	Xe ¹³⁴ , I = 0 (87M50)	(II./2-) Xe ^{135m} 0.52	(\$2.8 + 0.25 (7.2 + 0.25) (7.2 + 0.25) (18G52, 14G53) Q ₆ 1.15 (67B51)	Xe ¹³⁶ , I = 0 (87M50)		
0.233 (K/L 2.9) spect conv (6785ia); 0.235 (a _K /Y 4.2) spect conv, acint spect (24K5ia)	with C ₈ 133m; 0 08! (K/L 5.9) spect conv (67850c); 0.08 γ (e _K /γ 1.8, K/L+M 6.0) acint spect, β-γ delay coinc (1463); 0.08 z let (64851)		0, 52 apact (6P47b); 0, 5 (e/y -0, 2) aba, aba conv (16W45, INS1c)	with C _a 135m; 0.250 (e _{RC} /γ 0.05) spect cdnv, βconv coinc (67B5), 67B5id); 0.246 (K/L T. 0) spect conv, a cint spect, β-γ delay coinc (14G5); 0.25 spect (6P47b)			
	0. 34 apect (6/1850c); 0. 34 abe (18251); 0. 35 abe (13251e)			0. 905 spect (6/7951); 0. 93 spect (6P470); 0. 95 abs (10843a); 0. 9 abs (16W45); 1. 0 abs (7N51, 58H51c)		-4 abe (66843, 70B43e)	
2. 3 d (67B5la); 2. 1 d (24K5la)	5. 270 d (76M59); 5. 3 d (18E51)		15. 6 m (21843) 15. 3 m (6P47b) 13 m (1N51c)	9. 13 h (60B52k 9. 2 h (7NS1, \$8H51c); 9. 1 h (30T49)		3.9 m (63849); 3.8 m (66543); 3.4 m (21R43)	17 m (36 G40)
IT (24K50c)	p (22D40)		IT (16 W 45)	p (24540)		p (66S43)	p (16H39a)
		10. 44 (6N50a)			8. 87 (6N50a)		
A chem (24K50c); mass spect (67B5ia)	A chem (20139, 22D-40, 24840); chem; excit (16 W40); mass spect (13T47, 30T49)		A chem, genet (40G40, 16W45)	A chem (24540, 22D40); clbw10; mass spect (30T49)		A chem (66S43); mass spect (30T49)	A chem (16H39a); mass spect (30T49)
Xe Library	×,133	Xe134	х•135m	X ₆ 135	x•136	x•137	Xe 138

	7	9	Therese		Freeze of radiation in Mee	listion in Mer		
Z A	identification	abundance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
54 Xe 139	A chem, genet (16H39a, 6H39)		p_ (16H39♣, 6H39)	41 s (24D51)				fission Th (25A39, 16H40); fission U, parent Cs139 (16H39a, 6H39, 16H40a);
								ancertor bary, (10H392, 6H39, 24D51); daughter 1 ¹³⁹ (63S49)
Xe 140	A chem, genet (16H40a)		p (16H40a)	16.0 • (24D51); 9.8 • (11O51)				fission Th (16H40); fission U, ancestor Ba ¹⁴⁰ (16H40a, 24D5la, 24D51, 11O51)
Xe 141	A chem, genet (17B51)		p ⁻ (17B51)	1. 7 • (32K46, 11051); 3 • (24D51)				fission U, ancestor La ¹⁴ (1785); fission U, ancestor Ce ¹⁴¹ (24051a, 24051, 11051)
Xe 143	A chem, genet (17B51)		p (17B51)	1.0 • (24D51)				fission U, ancestor Ce 143 (1785), 24051);
* *	A chem, genet (24D5la)		p (24D5la)	-1 s (24D51)				fission U, ancestor Ce (24D5la, 24D5l)
\$5 ^C 812\$	A chem, mass spect (73M52)		p ⁺ (73M52)	45 m (73M52)	2. 03 apect (73M52)			1-a-6n (73M52)
Cs 127	A chem, mass spect (33F50)		p ⁺ (33F50)	5. 5 h (33F50)	l. 2 spect, abs (33F50)			I-a-4n (33F50); parent Xe ¹²⁷ (33F50); daughter Ba ¹²⁷ (37L52)
C. 128	B chem, genet (33F51)		6+ EC (37L52)	3.8 m (37L52); 3.1 m (33F51)	3.0 abs (33F50a, 32T50, 37L52)			daughter Ba ¹²⁸ (33F51, 37L52)
Cs 129	A chem, mass spect (33F50)		EC, no β ⁺ (33F50)	31 h (33F50)	conv: -0.3 abs (33F50)	-0.5 abs (33F50)		I-a-2n (33F50); daughter Ba ¹²⁹ (33F50a, 32T50)
C. 130	A chem (27848); chem, excit (91552a); chem, mass spect (73M52)		β ⁺ , EC, β ⁻ (β ⁺ /β ⁻ 27. 5) (91S52a)	30 m (91552a); -30 m (27848, 33F50)	6 ⁺ : 1.97 spect (91552a); 6 ⁻ : 0.442 spect (91552a)	no y (91552a); Xe K-x (91552a)	Q ₆ 0 442. Q ₆ 2.99 (91552a) (14) C ₅ 30 (04)	I-a-n (27R48, 33F50, 91552a)
C. 131	A chem, genet (1247a); chem, mass spect (7K49)		EC, no 6* (28F47, 43C51c, 38K5id)	9 6 d (1Y49); 10.2 d (3.2K47a.); 10.0 d (5Y47)		no y (43CSic, 32K47a, 38KSid, 113S2A, Xe K.× (43CSic, 5Y47, 1Y49, 32K47a, 28F47); -0 i aba conv, aba (5Y47, 1Y49)	EC, p ⁺ (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10+) (10	1-a-y (112551); daughter Ba ¹³¹ (2X47a, 5Y47, 1Y49, 43C51c); not parent xc ^{131m} 2 (43C51c); parent (?) Xc ^{131m} 2 (70C50)
Ce 132	B chem, excit (44C44)		EC (44C44)	7.1 d (44C44)		0 668 scint spect (10L5la); 0 62 abs, abs conv (44C44)	(18652)	Ca-n-2n (44C44, 10L51a)

C. 138m	A genet (14G53)		IT (14G53)	6.0 × 10-9 delay coinc (14G53)		see Xe ¹³³ ; -0.081 (e _K /y 1. 8, K/L+M 6.0) -0.081 w pect, 6-y delay coinc (14G33)		daughter Xe ¹³³ (14G53)
C. 133		100 (6N37)					Cs ¹³³ , 1 = 7/2 (87M50)	
C. 13477	A chem, n-capt (12A35, 77M35); chem, excit, n-capt (45K40)		IT (6P47, 18G48a, 42C50)	3. 2 h (5545); 3 h (45K40)		0. 128 (K/L/M = 64. 3/100/18.6) spect conv (42C50); 0. 128 (e _K /Y 2. 2) acint spect (14S5); 0. 128 (L _H /L _{HI} -1) spect conv (63M28); o. 128 (44.7, 18C48, 5945)	(44) 6 34 0.28 (44) 6 34 0.28 (44) 6 4 6 4 6 4 6 6 6 6 6 6 6 6 6 6 6 6	Cs-n-y (12A35, 77M35, 45K40, 2647); Cs-d-p (45K40)
C. 134	A n-capt (30A38); chem, n-capt, excit (45K40)		6 (45K40); no EC (lim 4%) (31W50); no EC (lim 5%) (7548); no p4 (lim 0.009%)	2. 3 y (33G51£) 1. 7 y (45K40)	0 648 (15%), 0.09 (25%) spect (20P5); 0.65 spect (31W50); 0.65 spect (31W50); 0.66 (-72%), 0.09 (-28%) spect (4E47); 0.06 (-0.08 (-24%) spect (87552);	/y 0.005), 0.567 (e _K /y 0.601 (e/y 0.005, K/L 1994 (e/y 0.002, K/L 1994 (e/y 0.002, K/L 4.5), ask, K.L 6.2), 1.365 (/L 6.1) epect conv		Cs-n-y (30A38, 69938, 45K40, 2847); Cs-d-p (45K40); Ba-d-a (51H43)
			(41M51)				(+0)	
						1.024, $v_5$ 1.11, $v_6$ 1.35 ( $v_1/v_2/v_3/v_6 = 0.35/0.94/1.0/0.017)$ spect (88531); $v_1$ 0.37, $v_2$ 0.07 ( $v_1/v_2/v_3/v_3/v_3/v_3/v_3/v_3/v_3/v_3/v_3/v_3$	(87552)	
						no 1.96 y (lim 10-4%) Be-y-n reaction (23W50); Robers (7548, 20P9), 6P47, 20D50, 8B99, 45W50, 17B50, 44M5a, 8SSS1, 8SBS0, 39R81, 61K\$2)		
C. 135m	A genet (14G53)		IT (14G53)	2.8 x 10-10 delay coinc (14G53)		0.248 (K/L 7.0) spect conv, scint spect, \$P-y delay coinc (14G53)	see Xe ¹³⁵	daughter Xe ¹³⁵ (14G53)
Ce.135	A chem, genet (63849a); chem, mass spect (3149a)		p (63549a)	3.0 x 10 ⁶ y sp act (8Z49); 2.1 x 10 ⁶ y yield (63S49a)	0. 21 abe (63549a); -0. 19 abe (8249)	no y (63849a, 8249)	Ca ¹³⁵ , I = 7/2 (87M50)	daughter Xe ¹³⁵ (63549a); ffeeion U (8249, 38W52)
C _a 13¢	A chem (33G46, 33G51m); chem, excit (33G49)		p ⁻ (33G51m)	13. 7 d (33G49)	0. 28 p-y coinc abs (28F5lb)	-0. 9 abs (33G49); 1. 2 f-y coinc abs (28F5lb); two y's (33G49)		La.n.a (44C44, 33G49); pahl-fission Th (7N49a), U (625); fission Th (21751), U233 (147c.a, 18G51), U235 (147c.a, 13G51m), Pu (28F51b, 33G51m)

Isosops Z	Chee and identification	Percent	Type of decay	Half-life	Baricles	Energy of radiation in Mer	Distangration energy and scheme	Method of production and
55 Ca 137	A chem, genet (78M43); chem, mass spect (60H6s, 3149a)		p" (78M41)	33 y (33GSla, 38W52)	p ₁ 0. 523 spect (16A50); p ₁ 0. 51 (92%), p ₂ 1. 17 (8%) spect (10L51); p ₁ 0. 521, p ₂ -1. 2 spect (20P49); p ₁ 0. 518, p ₂ -1. 18 spect (15O49); others (31WSI, 10L49, 31T48)	with Be 137m; 0.6616 cryst spect (100M52); see Be137m; others (10150d, 79B52, 31W51, 06B52, 40K52, 14M49e, 31T48, 20P49, 15C49)	C ₂ 137, 1 = 7/2 (87M50) O ₂ 1.2 (HP5) (77E+) (77E+) (17E+) (17E+) (17E+) (17E+) (17E+) (17E+) (17E+)	epail-fission Th (7N99a); fission Th (2175), U (60148, 3149a, 33GSin, 38WS2), U233 (38GSi), 20351, U235 (38GSi), Pu (28FSi); daughter Bal ^{37m} (13E48, 31748); daughter Xe ³³⁷ (21751b,
C. 138	A chem (16H39a, 6H3); chem, mass spect (30T49)		p ⁻ (16H39a)	32.9 m (19E51); 16H39(2); 16H39(2); 32 m (13G51s, 36G40)	3.40 (coinc with 1.4 y), -2.9, -2.0 spect, β-y coinc abs (101.52a); 2.68 spect (307.49); 2.65 abs (35.846a, calc from 36G40)	γ ₁ 0. 463, γ ₂ 0. 98, γ ₃ l. 44 (coinc with γ ₁ and γ ₂ ) spect conv. acint spect, β-γ, γ-γ coinc (101.52a); l. 2 abs (33G5lk, 19E5l)	(3W54, 10L51)  *** La 13  Q	Ba-n-p (66543b); fission Th (25A39, 16H40), Pa (2039), U (6H39, 16H40a); daughter Xe-138 (16H40a, 36C40, 66543b); descendent 1 ¹³⁸ (63549)
C ₈ 139	A cham, genet (16H39a, 6H39)		p' (16H39a)	9.5 m (63850); 10 m (25A39, 6H39); 7 m (16H40a)			(101.52e)	(iesion Th (25A39), U (16H39a, 6H39, 16H40a, daughter Xe.139 (16H39a, 6H39, 16H40, 16H40a); desenatont 11 ² 9 (16H39a, 6H39,
C. 140	A chem (16H40a); chem, genet (63S50)		p (16H40a)	66 . (63850)				16440, 16440a, 63850) fission U (16440a, 63850); parent Ba ¹⁴⁰ (63850)
O. M.			[6] (17B51)	short (17B51, 24D51, 11O51)				[daughter Xe ¹⁴¹ ] (1795), 24D5), 11051); fancasher 1-140,1788)
24 2 2 3 3 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	D chem. genet (16H42a) [A] genet (17B51) [A] genet (24D51a)		p ⁻ (16H42a) [p ⁻ ] (17B51) [p ⁻ ] (24D51a)	-1 m (16H42a) abort (17B3i, 24D5i, 11O5i) abort (24D5ia, 24D5i)				

Ca-d-8h, Ca-p-7h (17152); parent Ca ¹² (17125) Ca-d-7h (13725); Ca-p-6h (13750a, 12750, 371251; parent Ca ¹² (13750a, 12750); parent Ca ¹² (13750a, 12750); parent Ca ¹² (13750a, 12750); parent Ca ¹³ (13760a, 12750a)	Ca-p-n (2D40); Ca-d-An (10C41, 67HSia, 67HSib); Ba-y-n (60448); Ba-n-y (5Y48); By (11540) Pb (11947a); parent Ba 13 (5Y48) Ba-n-y (33K47a); daughter Ba 133m (5Y48)
	(3.72+) (6.7451b, 18652)
	0.276 (eg/v - 3) spect conv. exist spect (67H51a); 0.0117 (ey-v 130) y-y coinc, ion ch (67H51b); 0.276 (K/L. 3. 2) spect conv. (10C41) 0.320 (e/y 0.02), 0.085 (e/y 0.3, K/L - 10) abs, abs conv, cl ch (5748); 0.36 abs, abs conv (32K47a)

hard 6 [*] (32750)		
-12 m (37L52) 2. 4 d (33F50a, 32T50) 1. 8 h (32T50) 1. 8 h (32T50) 11. 7 d (3747)	38.8 h (46W43a); (46W43a); 38.9 h (3Y48)	
EC (37L52) 32T50 32T50) EC (32K47a); no p* (5Y47, 28F47)	IT (10C41)	
(486N6) 101.0	0. 097 (6N3 <b>8</b> b)	2.42 (6N3@b)
A chem, genet (371.52) B chem (337.50a, 327.50) (327.50, 337.50a) A chem, n-capt, excit (32K47a)	A chem, excit (10C41, 2D40) A chem, n-capt, excit (13K47a); chem, genet (5Y48)	-, -
56 Ba 128 Ba 129 Ba 130 Ba 131	Ba 132 Ba 133m Ba 133m	Ba 134

1	700 200	Perrent	Twent		Energy of rac	Energy of radiation in Mey		Marked of mendaction
Z	identification	abundance	decay	Half-life	Particles	Gemma-transitions	Disintegration energy and acheme	genetic relationships
56 ^{Ba} 35m	A chem (45K40); chem, n-capt, sep isotopes (67H5la)		IT (46W43, 5Y48)	28.7 h (5Y48)		0.269 (e _K /y - 3.5, K/L - 2) spect cony, acint spect (67H5la); 0.267 spect cony, spect, acint spect (39C5la)	(11/2-) Bo 135m (11/2-) 0.269 (32-1) 0.269	Ba-n-y, Ba-n-2n (45K40); Ba-d-p (46W43, 39C51a); Bal34-n-y (67H51a); spall-fission U (6O47)
Ba 135		6. 59 (6N38b)					Ba ¹³⁵ , I = 3/2 (87M50)	
Ba 136		7. 81 (6N38b)					Ba 136, I = 0 (87M50)	
Ba. ^{137m}	A n-capt (12A35); chem, genet (31T48, 13E48)		IT (31T48)	2.60 m (14M49a); 2.63 m 2.53 m 2.5 m (13E48);		onv	eee Ce ¹³⁷	Ba-n-2n (IP37 45K40); Ba-n-y (I2A35); daughter Ca ^{[37} (13E48, 31748)
Ba 137		11. 32 (6N38b)				Conv (444418.); 10) apect conv (15049); (6.63 (eV) 0.14) apect conv. x-conv coinc (31148); 0.66 apect conv (20P49)	Ba ¹³⁷ , I = 3/2 (87M50)	
Ba 138		71. 66 (6N38b)					Ba 138, I = 0 (87M50)	
В. 139	A chem, n-capt (12.45); chem, excit (17.38a)		p ⁻ (1P37a)	85.0 m (2405k1); 84 m (2405k8); 86 m (1P37a; 16H40a)	2. 3 abs (32K511, 70B43a)	0.163 (26%, e/y 0.20, K/L=6), 1.05 (10%) spect conv. aba, coinc (9248); -0.163 (eK/y 0.28) acint spect (92M52e)		Ba-d-p (1P37a, 45K40, 92548); Ba-n-y (12A35, 1P37, 2547, 1Y49a); Lan-p (1P3Ba); Ce-n-a (46W43); papil-fresion U (y) (42L40), U (6F51); U

Ra-n-y (second order reaction) 1245(14); pall-frasson Th (6047); 784991, U (6648, 6F5)); (188100 Th (7285), 21751); U (1619), 6149, 16140a, 36640, 36646, 63550, 19631, 48951, 115514, 115514); U 23 (61548, 38651), U 235 (18651), Du (12448, 18551) descendent Xel-40 (16140a, 17851, 24051, 24051a, 11051); parent Lal-40 (16190, 16193a, 16440a, 36640, 16144a,	fission Th (16H39c, 16H19), U (16H42s, 52C51, 52C51s); photo-fission U (42L40); daughter Cel ⁴ l (16H42s); parent La ⁴ l (16H42s); descendent Xe ^{14l} (17B5), 11C51, 24D51)	fission Th (16H39c, 16H39), U (16H42a); photo-fission U (42L40); daughter Cs ¹⁴² (16H42a); parent La ¹⁴² (16H42a)	fission Th (16H39c), U (16H39c, 16H39, 16H42s, 24DS1, 17BS1, 11OS1); [descendent Xe ¹⁴³ ] (17BS1, 24DS1)	[fission U. descandent Xe ¹⁴⁴ ancestor Ce ¹⁴⁴ ] (24D51, 24D51a)	spall Ba (53G51)	spall Ba (53G51)	Cs-a-4n (21N50); daughter Ce ¹³³ (93551)	daughter Ce ¹³⁴ (93S51)	Ca-a-2n (73C48, 21N50); Ba-d-n (81M42, 46W43b); Ba-p-n (46W43b); daughter Ce ¹³⁵ (73C48)
Q ₀ 1.05 (43R81) (0+) B ₀ (40 (0+) B ₀ (40 (0									
0. 0296, 0.132, 0.162, 0.304, 0.537 apect conv (10CStc); (10.160, 0.310, 0.535 apect (15L49), 0.03, 0.16, 0.31, 0.54 apect, apect, apect conv, actint apect, vycoint (86549, 43853); others (4WS), 26M49c)	۲ (32G51)					l. 0 abs (53G51)	0. 8 abs (21M50)	no y (93S51)	0. 76 (weak) abs (73C48); 0. 88 abs (46W43b)
1, 022 (60%), 0, 480 spect (86B49, 43R5); 1, 05 spect (4W5); 0, 99, 0, 47 spect (35L49); 1, 0 (-75%), -0, 4 (-25%) abs (13E5ig)	2. 8 abs (32L48)				1. 6 abe (53G51)	3. 5 abs (53G51)	-1. 2 abs, spect (21N50); conv: 0. 26 spect conv (21N50)	2. 7 abs, spect (93S51)	
12. 80 d (13. ESU. 77 SA 7)	18 m (16H42a, \$2G51)	6 m (16H42a)	<0.5 m (16H42a)	ahort (24D5i, 24D5la)	58 m (53G51)	4. 5 h (53G51)	4. 0 h (21N50)	6.5 m (93S51)	19 h (21N50); 19. 5 h (73C48)
p ⁻ (16H39±)	6 (16H42a)	p" (16H42a)	p ⁻ (16H42a)	p. (24D51)	p* (53G51)	<b>β</b> [†] (\$3G51)	EC, p (weak)	p ⁺ -44%, EC -56% (93S51)	EC (81M42, 73C48)
(i6H39, l6H39a)	A chem. genet (16H42a)	D chem, genet (16H42a)	B chem (16H39)	[A] genet (24D51)	A chem, mass spect (53GSI)	A chem, mass spect (53G51)	A chem, mass spect (21N50)	B chem, genet (93S51)	A chem (81M42); chem, excit (73C48); chem, mass spect (21N50)
4 0	Ba 141	Ba 142	Ba 143	ž	57La131	La 132	<u>.</u> 3	F 13	ž.

CHAP. 1.2 REACTOR PHYSICS

Method of production and	-	Ca-a-n (21NSO, 36R50a); Ba-d-n (3M47); Ba135-d-n, Ba136-d-2n (36R50a)	[daughter Ce ¹³⁷ ] (3148b, 73C48)	natural source (11B50f, 18P51)	S	M50)	Ba-d-y (?) (46 W43b); La-d-y (P197a, IP38a, 81M42, 46 W43b); La-n-y (82M35, IP38a, 40C42, 81M42, 46 W43b, 2547); Ce-n-p (46 W43b, 2547); Gen-p (46 W43b); U16139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 161139, 1611
Disintegration energy and scheme	Distriction on the			see Cs 138	HPS)	La ¹³⁹ , I = 7/2 (87M50)	(1+1) (0+1) (43R53)
ation in Mev	Gamma-transitions			$Y_1$ 1.39, $Y_2$ 0.81, $Y_3$ 0.54 $(Y_1/Y_2/Y_3 = 1/0.65/0.3)$ scint spect (18PS1); 1.0, 0.54 scint spect (11B50f)			$\gamma_2$ 0.3286, $\gamma_3$ 0.4867, $\gamma_4$ 0.8151, $\gamma_5$ 1.596 apect (12H52); $\gamma_4$ 0.033, $\gamma_2$ 0.335, $\gamma_3$ 0.490, $\gamma_4$ 0.820, $\gamma_5$ 1.600, $\gamma_6$ 2.50, $\gamma_7$ 0.003, $\gamma_5$ 0.335, $\gamma_3$ 0.490, $\gamma_7$ 0.003, $\gamma_5$ 0.335, $\gamma_3$ 0.49, $\gamma_7$ 0.093, $\gamma_2$ 0.335, $\gamma_3$ 0.49, $\gamma_4$ 0.937, $\gamma_4$ 0.335, $\gamma_3$ 0.49, $\gamma_4$ 0.827, $\gamma_5$ 0.49, $\gamma_6$
Energy of radiation in Mev	Particles	2.1 spect (21N50); abs (3M47); 1.8 abs (36R50a)		1.0 abs (65M52a)			1.32 (-70%), 1.67 (-20%), 2.26 (-10%), 0.0ther ad.; 3 (very weak) spect (86.849, 43.83); 0.90. 1.40, 2.12 spect (1046); 1.45, 2.2 spect (49%)ia); others (46 W43b, 37.846)
Half-life	am.mw	9.5 m (21N50); 9.0 m (36R50ab) 10 m (3M47)	>400 y yield (73C48); >30 y yield (3148b)	-2.0 x 10 ¹¹ y sp act (18951); -7 x 10 ¹⁰ y sp act (85M52a)			40.0 h (72B5id, 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 985), 98
Type of	decay	EC -67%, p ⁺ -33% (21N50)		EC (18P51); \$7 -6% (85M52a)		*	p. (1P38a)
Percent	abundance			0.089		99.911	
Class and	identification	A chem (3M47); chem, excit, sep isotopes (36R50a)	C mass spect (3148b)	A chem, mass spect (3147a)			A n-capt (82M35); chem, eacht, chem, eacht chem, mass spect (60H48)
Isotope	V Z	57La136		La 138	9	La 139	La 140

La-n-y (second urder reaction) (3.2-49); fission (4.0-29); U (16H4Za, 3.2KSi)); daugher Ba ¹⁴¹ (16H4Za); fescendent Xe ¹⁴ (17RSi); parent Ce ¹⁴¹ (50RSi, 23DSib)	fission Th (16H39c), U (16H42a, 32K51)); daughter Bal42 (16H42a)	fission U (16H42a, 16H43b, 54G51);	[descendent Xe 144, parent Ce 144] (24D51a)	La-p-7n (93S51); parent La ¹³³ (93S51)	La-p-6n (93SS1); epail Ta (22NS2); parent La ¹³⁴ (93S ₅ 1)	La-d-6n (73C48); La-p-5n (93S5); spall Ta (22N52);	parent Larry (15(48)	La-d-4n (73C48); La-p-3n (93SS1); Ce ¹³⁶ -n-y (67HS1c. I.KS1); [parent La ¹³⁷ ] (3148b, 73C48)		Ba-a-n (1P43, 1P48); La-d-Zn (1P43, 36M47, 1P48); Ce ¹³⁸ , new (67181c, 11K51); Ce-n-y (83M50); epall-fission Bi (1IG49); daughter Pr ¹³⁹ (93S31)	
Lo ¹⁴ 1	(23051b)							Ce ¹³⁷ Ec	(IIKSI, HPS)		
1. 3-1. 6 (?, weak) scint spect, β-γ coinc (23DSlb)	y (32K51J)			1. 8 abs (93S51)	К-ж, по ү (93S51)			0.257 (K/L -4) spect conv (67H5ic); 0.253 (K/L -10) spect conv (11K51)		. 0 166 (K/L -10), 0. 275 spect conv (IIK5)); 0 166 (K/L ≥4) spect conv (67H51c); -0.8 abs (IP48)	
3.7 h (32K51j); 2.43 (-95%), 0.9 (-5%) spect 3.5 h (16H42a) (23D51b)				l. 3 spect, abs (93S51)		0.81 spect (93S51)					
3.5 h (16H42a)	74 m (16H42a); 77 m (32K51j)	-19 m genet (54G51); -15 m (16H43b)	short (24D5la)	6. 30 h (93S51)	72.0 h (93S51)	22 h (93551)		36 h (73C48)		140 d (1P43, 1P48)	
6 (16H42a)	p ⁻ (32K51j)	p (54G51)	[b] (24D51a)	EC, 6 [†] (93551)	EC (93551)	EC, 6 41% (93S51)		EC, no p ⁺ (73C48)		EC (36M47)	
							0.193 (3147a)		0. 250 (3147a)		88.48 (3147a)
A chem (16H42a); chem. genet (50B51, 23D51b)	D chem (16H42a)	A chem, genet (54G51)	[A] genet (24D5la)	A chem, genet (93551)	B chem, excit (93S51)	A chem, genet (73C48)		A chem, excit (73C48); n-capt, sep iscopes (67HSic)		A chem (IP43); chem, excit, cross bomb (IP48, 36M47); n-capt, sep isotopes (67H51c)	
ē.	747 145	£ 41	ž.,	58Ce133	Ce 134	Ce 135	Ce 136	Ce 137	Ce 138	Ce 139	Ç 140

leomos	Class and	Percent	Type of	חיותוני	Energy of radiation in Mev	iation in Mev		Method of production and
V Z	identification	abundance	decay	ATILITIES .	Particles	Gamme-transitions	Comments on Change of the Comments of the Comm	genetic relationships
58 Ce 141	A chem (16H40c); chem, excit, n-cap, cross bomb (1P4), 72B3(c); chem, mass spect (60H48)		p ⁻ (16H40c)	33.1 d (49W49); 32.5 d (3FS0c); 30.6 d (IP48)	0. 581 (33%), 0. 442 (67%) spect (3F 50c); 0. 44 (71%) spect (38K51c); 0. 44 (71%) spect (36K51c); 0. 54 (70%), 0. 41 (70%) spect (35248a); 0. 55 spect, 6 -y coinc abs (11749a); 0. 55 spect, 6 -y coinc abs (11749a); 0. 55 spect (36M49e, 94550, 1P48, 37B46)	0. 145 (e _K /y 0.25, K/L 5.5) spect conv. spect (1F50c);  -0.14 (e _K /y 0.46) scint spect (80452a);  0.42 (e _K /y 0.48) scint spect (1735a);  0.45 (K/L -7) spect conv (67451c);  0.146 (e _K /y -0.33, K/L 6.5) spect conv (18451, 11749a);  0.146 spect conv (11851, 11749a);  0.146 spect (17851a);  0.146 spect (17851a);  0.146 spect (17851a);  0.146 spect (17851a);	00 0.58 (3F50c) (772-) Ce  4  (772-) 33% 67% (772+) 0.145 (372+) 0.145	Ba-q-n (1P43, 1P48); Ce-d-p (1P43, 1P48, 72B51e, 50B31); Ce-n-y (1P43, 1DC48a, 72B51e); Ce-n-x (1P43, 1P48, 72B51e); Pr-n-p (1P43); Pr-n-p (1P43); Pq-all-fisacion Bi (1D(40), U (6F51); U (16H40c, 50B51), U235 (1B40c, 50B51); U (16H40c, 50B51), U235 (1B40c, 50B51); U (16H40c, 2BB51); U (16H40c, 2BB
្ន		11. 07 (3147a)						
c, t,	A chem (63546, 1P43); chm, cross bomb (1P48); chem, genet (12851e); mass spect (3148b)		p' (63546)	33 h (72851e, 95550, 37846); 34 h (38551c); 36 h (4849, 1P43)	$\beta_1$ 1. 39, $\beta_2$ 1. 09, $\beta_3$ 0. 71 ( $\beta_1/\beta_2/\beta_3$ = 1. 0/1, 3/1. 0) spect (50B52); $\beta_1$ 1. 37, $\beta_2$ 1. 09, $\beta_3$ 0. 37 (?) ( $\beta_2/\beta_1$ 1. 4) spect (38K51c)	0.035, 0.126, ~0.160, 0.289, 0.356, 0.660, 0.720 spect, spect conv. scint spect (50822) y ₁ 0.057 (KL - 1), y ₂ 0.683 (K/L - 6), y ₃ 0.649, y ₄ 0.705 (Y ₂ /Y ₃ /Y ₄ = 4.5/I/1) spect, spect conv. β-γ coinc (38K51, 38K51, 38K51, 0.0575 (K/L - 1), 0.291 (K/L - 10), 0.0475 (K/L - 11), 0.291 (K/L - 10), 0.148 spect conv (11K51);		Ce-d-p (1P43, 1P48, 72851e); Ce-n-y (1P43, 37846, 1P48, 72851e); Ce ⁴ K-n-y (11K51); spall-fission Th (7N49a), U (6048, 6F51); fission Th (72851), U (17851, 44051, 63531), Pu (32K48); daughter La ⁴ 3 (4642, 37846, 72851e); Grescedent Xe ⁴ 3 (1P851, 24051)
, o	A chem (16H40c); chem, mass spect (60H48)		6 (16H40c)	282 d (53551); 275 d (50B51a); 290 d (19.141)	0.300 (70%), 0.170 (30%, coinc with 0.134°, with 0.134°, with 2.30°, o.304 (70%) apect (19P5.); o.304 (70%) apect (19P5.); coinc (24K5.); others (70C5., 17N5.1b, 6P47, 26M50a)	0.0337, 0.654, 0.0807 (e/y large, K/L -4), 0.100, 0.134 (K/L -9) spect conv. spect (19P2); 0.041, 0.047, 0.054 (K/L cl), 0.081 (K/L -5), 0.095, 0.101, 0.135 (k/L -10) spect conv (11K5); 0.0547, 0.079 (K/L 6.3), 0.134 (K/L 8.3), 0.231 (K/L 1.7) spect conv (10C52); 0.0547, 0.052 (K/L 6.3), spect conv (40K5); 0.695, 1.50, 2.18 spect (15T50); others (13A52a, 2E51)	0-10-10-10-10-10-10-10-10-10-10-10-10-10	ppil-fission Th (7N49a), U (6046); U (6046); Grasion Th (21751), U (16H40c, 7084a, 24051, 7N51a, 5085ia), U 233 (38G51), 6158 (38G51), U 255 (38G51), pr (28851); pr (28851); Pr (28851); descendent Re ¹⁴⁴ (16H43b, 39G43, 7N51a);
Ç i45	G not found: (78C52a)			-1. 8 h (72В5Ц)				not found: fission U (78C52a); fission U (24D51, 72B5U); parent Pr ¹⁴⁵ (72p5U)
Ce 146	D chem, genet (40G43)		p ⁻ (40G43)	14.6 m (53S45); 11 m (40G46)	-0.9 abs (78C52a)	soft y (78C52a)		fission U, parent Pr (40G43, 16H43b, 53S45, 40G46)

59Pr 137	B chem, mass spect (44D52)		p ⁺ (44D52)	1.4 h (44D52)	1. 8 (44D52)			Ce-p-4n (44D52)
Pr.138	A chem, excit (93551); chem, mass spect (44D52)		EC -90%, p ⁺ -10% (93S51)	2. 0 h (9355), 44D52)	l. 4 abs, spect (93S51)	0. 2, -0. 5, 1. 3 abs (93S51)		Ce-p-3n (93SS1, 44DS2)
Pr 139	A chem, genet (935si); chem, mass spect (44D52)		EC -94%, p6% (93551)	4.2 h (44D52); 4.5 h (93S51)	1. 0 abs spect (93S51)	1 0 abs (93S51)		Ce-p-2n (93S51, 44D52); parent Ce ¹³⁹ (93S51)
Pr 140	A excit (1235); excit (1738a)		p * 58%, EC 42% (88B52)	3. 4 m (29D42); 3. 5 m (1P38a)	2. 23 apect (86.B5.2)	no y (88B52)	0¢ 3.25 (68B52) (1+) Pr 140 (0+) (0+) (0+) (68B52)	Ce -p-n (93581); P-n-2n (12A35, IP38a, 29D42); Pr-y-n (14H45, 12P49); daughter Nd ¹⁴⁰ (2W49, 8BF52)
Pr 141		100 (3148c)					Pr ¹⁴¹ , I = 5/2 (87M50)	
Pr 142	A n-capt (12A35, 82M35)		p (29D42); no p or EC (lim 0.5%) (28R50b)	19. 2 h (37B46); 19. 1 h (13J50); 19. 3 h (29D42)	2. 15 (-96 %), 0. 64 (-4 %) spect (11350); (11350); 2. 23, 0. 66 spect (41850); 2. 13 spect (96 M2, 290-42); 2. 22, 0. 22 abs. p-y coinc abs (26 M494); (25 M494); (15 J49)	γ ₁ 0.135, γ ₂ 1.59 (γ ₁ /γ ₂ <0.2) spect, spect conv (41R50); 1.58 spect (1350, 13152); 0.134, 0.329, 0.490, 0.624 spect conv; 2.1 abs (10C48); 1.5 coinc abs sec (15149)	Og 2. 23 (13.350, 26.M49d)	La-a-n (29042); Ca-p-n (29042); Pr-a-p (29042); IP 3a_2 29042, 2871); Nd-n-p (IP 37, IP 38, 18, 18, 18, 18, 18, 18, 18, 18, 18, 1
Pr 143	A chem (72851g, 19144); mass spect (60H46s)		p ⁷ (72B51g. 19J44)	13. 7 d (15F49a); 13. 8 d (72B51h); 13. 5 d (1P48)	13. 7 d (15F49a); 13. 8 d (72B51h); 13. 5 d (1P48)  0 920 spect (11T49a); 0 92 spect (18F51); 0 92 spect (38F51); 0. 84 abs (26M49e)	no y (72851g, 72851h, 1P48)	О 0.93 (НРS)	Ce-d-n (1P48); spall-frasion U (6F51); frasion U (16H3b, 19144, 72B51g), i'u (28F51) daughter Ce ¹⁴³ (1P43, 37R46, 72B51e)
* · · · · · · · · · · · · · · · · · · ·	A chem, genet (7NS)a, 16H43b, 39G43)		p [*] (7N51a)	17.5 m (7N51a., 77551b); 17 m (16H43b)	2.97 (>99%), other p's (<1%) apect (19952); 2. 32 (<1%, other with 0.69 y), 0.81 (<1%, ppect, p -y coinc (24852); 2. 95 (-95%), 0.87 (-5%) apect (101525); 2. 97 (-90%), 2.3 (-5%), 0.86 (-5%) apect (13A52a); 2.97 apect (15A52a); 2.99 apect (6P47); 7.99 (17815b, 19144, 50B51a, 7.0843a, 16H43b, 26M50a, 70C52)	1.9 (19. 2) (1.9, 1.5, 1.4) (1.9, 1.9, 1.9, 1.9, 1.9, 1.9, 1.9, 1.9,	ορ 3.0 (13A52a, 19P52) Pr 144 (0-) Pr 144 2-99% (1/4) (0+) (0+) (1/4) (HPS)	fission Th (21751). Pu (28F51); spall-fission U (6F51); daughter Ce ¹⁴⁴ (16H43b, 39G43, 7N51a)
Pr 145	G not found: (78C52a)			4. 5 h (72BSE)				not found: fission U (78C52a); fission U (72B51f); daughter Ce ¹⁴⁵ (72B5If)
Pr 146	D chem (40G43)		p (40G43)	24. 0 m (20K5la); 24. 6 m (53S45a); 25 m (40G46)	3.8 abs (78C52a); -3 abs (53S45a)	0. 490, 0.78 scint spect (20K5la); I. 4 abs (53545a)	·	fission U, daugher Ce ¹⁴⁶ (40G43, 16H43b, 53S45, 40G46)

HA	P.	1.2										ACTO	OR PHYSICS
Method of production and	genetic relationships	Pr-p-4n (93551)	Pr-p-3n (93551); ancestor Ce ¹³⁹ (93551)	Pr-p-2n (9353); Pr-d-3n (2W49); parent Pr ¹⁴⁰ (2W49, 88B52); spall-fission U (6F51)	Pr-p-n (47K42, 2W49); Pr-d-2n (2W49); Nd-n-2n (IP38a, 47K42); Md-n-47K42);		fission U ²³⁵ (mass spect)	fission U ²³⁵ (mass spect)	fission U ²³⁵ (mass spect)	fission U235 (mass spect) (3150a)	Nd-d-p (47K42); Nd-n-y (37B46 54M47, Nd-n-y (37B46 54M47, finsten U (6M51); spalldisten U (6F51); parent Pml ⁴⁷ (84M47, 84M51s)	U ²³⁵ -n-fission (mass spect)	Nd-n-2n (IP38a); Nd-d-p (IP38a); Nd-n-y (IP38a, 37846, 84M5lb); parent Pm ¹⁴⁹ (42K52)
	District the second second						Nd ¹⁴³ , I = 7/2 (97B50, 88M51)		Nd ¹⁴⁵ , I = 7/2 (97B50, 88M51)		OF 0.92 (31852) Nd 47 Nd 47  Nd 47  (31852, 2E516, HPS)		Q. 1. 5 (31R52)
ation in Mev	Gamma-transitions		l. 3 abe (93S51)	Pr K-x (88B52)	1. 2 (weak) abs (2W49)						0.0918 (K/L, z 6.4) spect conv (6.3M52); γ ₁ 0.0918 (e/γ - 0.9, K/L+M 6.5); γ ₂ 0.309, γ ₃ 0.391, γ ₄ 0.520 (γ ₁ /γ2/γ3/γ4 = 66/1/2/32) spect (38K51a); γ ₁ (K/L/M = 7.55/1/0.096) spect conv (91524); 0.0912 (K/L - 6); 0.121, 0.197, 0.231, 0.260, 0.273, 0.301, 0.18, 0.394, 0.441, 0.332 (K/L - 6) (all weak except 0.091 γ) spect conv, γγγ, β-γ conv (3182); 0.0918 (coinc with 0.38 f), 0.320, 0.534 spect conv, β-conv coinc (2E51a);		0.030, 0.097 (K/L 0.9), 0.112, 0.114 (F/L-5), 0.124, 0.186, 0.196, 0.211 (K/L-7), 0.226, 0.240, 0.266 (K/L-10), 0.424, 0.538, 0.650 spect, spect conv, scint spect, coinc (31852);
Energy of radiation in Mer	Particles	-2.4 abs (93S51)	3.1 abe, spect (93551)		0. 7 abs (2W49); 0. 8 abs (47K42)						0.83 (-60%), 0.60 (-15%), 0.3) (-25%) spect (2E54s); 0.78 (-65%), 0.35 (-32%) spect (38K51s); 0.83, 0.60, 0.38 spect (31R52)		1. 5, 1. 1, 0, 95 spect (31R52); 1. 5 abs (84M91b); 1. 6 abs (37B46)
חיית וועי	um-mu	22 m (93S51)	5. 50 h (93SS1)	3.3 d (2W49)	2. 42 h (2W49); 2. 5 h (47K42)				. ,		ll. 3 d (average (3.182, 2E51a, 38K51a, 8AM51, 37B46)		2. 0 h (37B46, IP38a); 1. 8 h (31R52); 1. 7 h (84M51b)
Type of	decay	p ⁺ (93551)	EC -90%, p+ -10% (93S51)	EC (88B52)	EC -98%, 6 -2% (2W49)						6-4M51) 84M51)		6 (1P38a)
Percent	abandance					27.13 (3148c)	12. 20 (3148c)	23. 87 (3148c)	8. 30 (3148c)	17. 18 (3148c)		5. 72 (3148c)	
Class and	identification	D chem, excit (93551)	A chem, genet (93S51)	A chem, excit, genet (2W49)	A excit (47K42); chem, excit (2W49)						A chem, genet (84M47,84M51a)		A excit (IP38a); chem, genet (84M51b)
Isosope	٧ z	8E PN 09	981 _{bN}	Nd 140	Nd 141	Nd 142	Nd 143	₹ PN	S <b>P</b> 1 PN	N4 146	491 P.N.	8 +1 PN	641 PN

NUCLE	EAR PHYSICS										CHAP. 1.
(18150a)	Nd-n-v (84M51b); Nd-150-n-v, parent Pm ¹⁵¹ (31R52)	Nd ¹⁴² -p-2n (34F52)	Pr-a-2n (2W50a, 34F52); Nd-p-n (43L52a)	Pr-a-n, Pr-a-2n (34F52); Nd ^{143, 144} -p-n (34F52); Nd-p-n (43L52a)	Nd-p-n (43L52a)	daughter Sm 145 (65B51, 26P52)	Nd ¹⁴⁶ -p-n (34F52); Nd-p-n (43L52a)	fission U (19G43, 72B51, 77B51, 77B51, 8A451a), U233 (18G48, 3A62), U235 (1150a, 38G51); daughter Nd ⁴⁷ (84M47, 84M51a); Gament Sm ¹⁴⁷ (42R50)	Nd-p-n (47K4)); Nd-f8-p-n (43,122, 3455); Nd-d-2n (47K42, 47K43); Nd-a-p (47K42); Pm ¹⁴ 7_ny (26947); spall-fission U (655);	Nd ¹⁴⁸ -p-n (43L52, 34F52); spall-fission U (6F51)	Nd 150-p-2n (34F52); Nd-d-n, Sm-n-p, Sm-y-p (44L4); fination U (84M47, 84M51c), Pu (32K48); epall-fination U (6F51); daughter Nd ¹⁴⁹ (42K52)
								O ₆ 0.223 (HPS)			
	0.085, 0.110, 0.117 (h/L 4), 0.421, 0.73, 1.14 spect com, scint spect, β-γ, γ-γ coinc (1872); Pm K-κ (31852)		0.95 abs (2W50a)	0.65, 0.44, 0.17 scint spect (34F52)		Nd K, L-x (65B51, 26P52)		no y (84M47, 84M512, 77551c)	-0.8 abs (26P47)	0.9 abs (6F51); 1. 0 abs (34F52); 0.5 abs (43L52)	0. 285 (coinc with \$\beta\$, K/L \$\\ \ell\$, -1. 3 (week) perct conv. abs, \$\beta\$, coinc (31852); no  (38854a); -0. 2 (coinc with \$\beta\$) \$\beta\$- coinc abs  [26M49i); others (52M5i)
	1. 93 epect (31.R52)	2. 4-2. 8 spect (34F52)			0.45 (431.52a)		0.7 abs (34F52); 0.75 (43L52a)	0. 223 spect (10L50c); 0. 227 spect (16A50); 0. 229 spect (16A50)	-2. 5 abs (26P47); 2 abs (47K43)	2.4 (weak), 0.6 spect (6F51); 2.7 (weak), 0.7 abs (34F52); 1.7, 0.6 abs (43L52)	1. 05 spect (18K51a, 31R52, 14F52); others (26M49f, 37B46, 84M51c)
>2 x 10 ¹⁵ y sp act (85M52); >10 ¹³ y sp act (21G52)	15 m (51C52); 12 m (31R52, 84M51b)	20 m (34F52)	250-280 d (43L52a); 285 d (2W50a)	200-400 d (34F52); 300-350 d (43L52a)	14-18 d (43L52a)	-30 y yield (65B51)	-1 y (34F52); 1-2 y (43L52a)	2. 6 y (53551); 2. 3 y yield (3150a)	5.3 d (47K43, 26P47)	42 d (34F52); 43 d (6F51); 48 d (43L52)	54 h (34F52); 55 h (3147b); 50 h (31R52, 38K51c); 47 h (34M51c, 16W42, 44L41)
6 (?) (85M52, 3L34)	p [*] (31R52)	6 ⁺ (34F52)	EC (2W50a)	EC (34F52)	p ⁺ (43L52a)	EC (65B51)	β ⁻ (?) (34F52)	p ⁻ (39G43, 72B5li)	p ⁻ (47K43)	p (431.52)	p (84M47, 84M51c)
5. 60 (3148c)											
	B n-capt (84M5lb); sep isotopes. n-capt, Pm K-L-M difference (31R52)	B chem, excit (34F52)	D chem, excit (2W50a)	D chem (34F52)	F sep isotopes (43L52a)	A chem, genet (65B51, 26P52)	B chem, excit (34F52)	A chem (84M47, 84M51a); mass spect (60H48)	A chem, n-capt, mass spect (26P47)	B excit, sep isotopes (43L52); chern (6F51)	A chem (84M47, 84M51c); chem, mass spect (3147b)
OST PN	151 PN	61 Pm 141	Pm 42143	Pm <b>H</b> 344	Pm 145	Pm 145	Pm 146	Pm 147	Pa 148	Pm 148	Pa 149

	7	Permit	Tone of		Energy of rad	Energy of radiation in Mey		Marked of section 1
Z Y	identification	abnodasce	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
61Pm150	A excit, sep isotopes (431.52); chem, excit, sep isotopes (31.52); chem, excit, sep isotopes (34F.52)		β [−] (43 <u>15</u> 52)	2. 7 h (431.52, 34 <b>F</b> 52,47K43)	2. 01 (-70%), 3. 00 (-30%) spect (34952); 2.4 abs (43L52)	1.4, 0.3 abs (34F52)		Nd-p-n, Nd-d-2n (47K43); Nd ¹⁵ 0-p-n (34F52, 43L52)
Pm ¹⁵¹	B genet, Sm K-L-M differences (31852)		p ⁻ (31R52)	27.5 h (31R52)	l. l abs (31R52)	0.065 (K/L 0.3), 0.066 (K/L 0.3) 0.070 (K/L 0.3), 0.100 (K/L-5), 0.116, 0.144 (K/L -9), 0.163 (K/L -7), 0.168 (K/L -9), 0.177 (K/L -9), 0.208 (K/L -1), 0.374 0.240, 0.275 (K/L >10), 0.340 (K/L -9), 0.715 spect conv.		daughter Nd ¹⁵¹ (31852); fission U (51C52)
Ę	E (1P38a); chem (6F51)		p (IP38a)	12. 5 h (6F51, IP38a)				Nd-d- (1938a); spall-fission U (6F51)
6.25m ¹⁴³	E chem (65B50)			8 m (65B50)				Sm-y-n (65B50)
\$ms		3.16 (3148d)						
Sm 145	A mass spect (3147c); chem (65851); chem, sep isotopes, n-capt (26P52)		EC (65B51, 31R52)	-410 d (65B51); >150 d (10C48b); >72 d (3147c)		0,061 (K/L l. 0) spect conv (31892)		Sm 144 n-y (26952); Sm nny (3147c, 10C48b, 65851); parent Pm ¹⁴⁵ (6585), 26P52)
Sm 147	A chem (71H32); sep isotopes, mas spect (40 W50); chem, genet, mass spect (42R50)	15. 07 (3148d)	3L33)	(1/2 corrected for abundance of Sm147 (HPS):  1. 4 x 10 ¹¹ y sp act (45,147);  1. 5 x 10 ¹¹ y sp act (7,2445);  1. x 10 ¹¹ y sp act (7,2445);  2. x 10 ¹¹ y sp act (7,2445);	2. 18 ion ch (10350); 2. 14 range emula (74C46); 2. 1 range emula (73H49); 2. 0 c.l ch (72H35); others (92B49)		Sm ¹⁴⁷ , I = 5/2 (88M51) Sm ¹⁴⁷ , I = 5/2 (88M51)	natural source (71H32, 3L33, 72B48, 1D48); daughter Pm ¹⁴⁷ (42R50); disting U ²⁵³ (mass spect) (3150a)
Sm148		11. 27 (31484)						
Sm 149		13. 84 (31484)					Sm ¹⁴⁹ , 1 = 7/2 (105B52); Sm ¹⁴⁹ , 1 = 5/2 (88M51)	fission U ²³⁵ (mass spect) (3150s)
Sm150		7.47 (3148d)						

Sm-n-y (3147c); fission U (84 M49); fission U 235 (mass spect) (3150a)	fission U ²³⁵ (mass spect) (3150a)	Nd-a-n (47K42); Sm-n-y (71H36, 198a, 44L41, 16W42, 60H46, 2847, 51W51); Sm-n-Zn (1P38a, 47K42); Sm-q-p (44L41, 47K42); Sm-q-n (44L41); pgall-(fasion Th (7N49a), U (6F51); Ifasion 123 (61S48), U235; Pu (51W51); parent Eu!53m (52M50)	fission U ²³⁵ (mass spect) (3150a)	Sm-n-y (12A35, 82M35, 71H36, 1P38a, 44L41, 2547, 3147c, 51W51a); Sm-d-p (44L41, 47K42); fination (123 §51W51a); Pu (51W51a); parent Eu ¹ 55 §3147c)	fission U (SIWSIb); spall-fission U (6FS1); parent Eul56 (SIWSIb)
Sm ¹⁵¹ 0020 (33W-92)		(+) Eu 53m (+) Eu 53m (+22 +) 0.174 (145 52 a)		0 2 2 (31R52)	(3IR52)
0. 019 (coinc with \$\bar{b}\$) ion ch, \$\bar{b}\$-y coinc (33 \bar{b}\$2); 0. 021 ion ch (17850); 0. 021 scint spect (39 \bar{b}\$2); no y (84 \bar{b}\$4); others (52 \bar{b}\$2);		$(e_{K}/Y 1.2, coinc with \gamma_2 or \gamma_4), \gamma_3 0. 530, \gamma_4 0. 6 (\gamma_1/\gamma_2/\gamma_3/\gamma_4) 2. 100, 2551, 0/0. 3) acint apect, \gamma_2 coinc (1452a); 0. 69 (e_{K}/Y 3.8), 0. 103 (e_{K}/Y 1.2, K/L-6), 0. 103 (e_{K}/Y 1.2, K/L-6), 0. 103 (e_{K}/Y 0.65, K/L-6), 0. 530 (e_{K}/Y 0.65, K/L-6), 0. 500 (e_{K}/Y 0.65, K/Y 0.65, K$		γ ₁ 1.05 (K/L 3.6), γ ₂ 0.246 (coinc with γ ₁ , K/L -8) (γ ₁ /γ ₂ -1) spect, spect conv, γ-γ coinc (31R52)	
0. 076 apect (16A50, 19W52b); 0. 079 apect (24K46e); 0. 074 apect (84M49); no conv (31R52)		0. 80, 0. 70 (coinc with 0.101 y) acins apect, 6-y coinc (87B52); 0. 66 (-67%), 0. 80 (-33%) apect (11H50); 0. 70 apect (17S1); 0. 8 apect (18F52); 0. 78 abe (82E48); 0. 73 abe (51W51)		1. 8 (coinc with both y's) abs. β-y coinc [11852]; 1. 9 abs (51W51s); 1. 8 abs (47K42)	0.9 abe (51W51b)
73 y (7K52); -120 y yield (3150a)		47 h (\$1 W\$1, 37B46. 47K42,31R52)		23.5 m (31R52); 25 m (51W5la); 21 m (1P38a)	-10 h (51W51b)
p ⁻ (3147c)		6 (47K42)		6 ⁻ (47K42)	ß (SIWSIb)
	26. 63 (3148d)		22. 53 (3148d)		
A mass spect (3147c, 3150a); chem (84M49)		A n-capt, excit (1978a); (1978a); mass spect (60146, 3147b); chem (51 W51)		B n-capt (12A35, 82M35); chem (51W51a)	A chem, genet (\$1W5lb)
151 8 151	Sm 152	Sml53	Sm 154	Sm 155	Sm 156

1	Proc and	Person	Twe of		Energy of rad	Bacray of radiation in Mey		Marked of search services and
Y Z	identification	spragaece	A CO	Half-life	Particles	Gamma-craneitions	Disinsegration energy and scheme	genetic relationships
63 Eu 144	C excit, sep		p ⁺ (74H52)	18 m (74H52)	2. 4 spect (74H52)			Sm ¹⁴⁴ -p-n (74H52)
	A chem, genet, sep isotopes, excit (74H51)		EC (74H51)	5 d (74H51)	comw: 0.2 abs (74H51)			Sm ¹⁴⁷ -p-3n (74H51); daughter Tb ¹⁴⁹ (74H51)
	C excit, sep isotopes (74H51)		EC (74H51)	38 h (74H51)	сопи: 0.4 аbs (74Н51)			Sm 144 -a-pn, Sm -d-3n (74H51)
	B chem, excit, sep isotopes (74H51)		EC 99+%. a -10-3%. no p+ (74H51)	24 d (74H51)	a: 2.88 ion cb (74H51) conv: 0.2 abs (74H51)			Sm ¹⁴⁷ -p-n (74H51); Sm-d-2n, 3n (42R52)
	A chem (84M51d); excit, sep isotopes (74H51, 86M52)		EC, no p* (74H51)	59 d (86M52); 54 d (2W50b); 50 d (74H51); 53 d (84M51d)	conv: 0.4 abs (74H51, 2W50b)	0.57 scint spect (74H52); 1.0, 0.4 abs (84M51d, 2W50b); 0.7 abs (86M52)		Sm -p-n (74HS1, 86MS2); Sm-p-n (2W50b); Sm-d-n (47K43, 84MS1d)
Eu 149	E sep isotopes, excit (74H52)			-120 d (74H52)		-0.4 acist spect (74H52)		Sm ¹⁴⁹ -p-n (74H52)
Eu 150	A chem, excit (65B50); chem, excit, aep isotopes (74H52); excit, eep isotopes (66M52)		6 [*] (86M52)	15. 0 h (2 <b>W50b)</b> 15 h (65 <b>B</b> 50); 13. 1 h ( <b>66M</b> 52)	1. 8 spect (2.W5Ob); 0. 8, other β's (66M52)			8m ¹⁵⁰ -p-n (74H52, 86M52); Sm-p-n (2W50b); Eu-y-n (65B50)
Eu 151		47. 77 (43H48)					Eu ¹⁵¹ , I = 5/2 (87M50)	flasion U (mass spect) (3150s)
	A n-capt, mass spect (3147d); chem (64M49a)		EC, B [*] (60H49)	13 y (7K52); 5. 3 y yield (60H49)	1.58, others spect (11450); 1.56, o.75 spect (68648); 1.7 (-20%), o.9 (-80%) abs (641449a)	0.122 (conv in Sm), 0.123 (conv in Gd), 0.244, 0.344, 0.720, 0.944, 1.066 spect conv (IIK3), 10C30c), 1.246, 0.344 spect conv (4XK2); 0.121 (colse with 0.344 sp. 0.244, 0.121 (colse with 0.344 y), 0.244 (colse with 0.344 y), 0.244, 0.344 (sor colse with 0.344 y), 0.344, 0.344 (sor colse with 0.344 y), 0.444, on the colse with 0.344 y), 0.344, 0.344 (sor colse spect (3F45)), obbs: 0.11K50, 68648)		Eu-n-y (3167d, 2547)
Eu 152	A n-capt (82M15); n-capt, excit (125&4); man spect (60H46, 60H49)		(60H49)	9. 2 h (1P38a, 60H49); 9. 3 h (37B46)	1.880, 0.55 (?) (weak) spect (11H50); 1.88 spect (20T39)	γ ₁ 0. 122 (coav in Sm,K/L - 4), γ ₂ 0. 344 (coav in Gd,K/L - 10) spect coav (11K3); 0. 122, 0. 336 (coinc with β) pair spect, β-γ coinc (10783); 0.120 (coinc with β) or 0. 8 γ), 0. 40, 0. 42 (and coinc with β) γ spect, spect coav, β-coav, γ-γ coinc (11H30); coher s (5.2 W3), 20739, 10C50c, 35F50, 23R39)	Eu 152 Pr	Eu-n-v (82M35, IP38a, 71H36, 5F41b, 2847, 60H49); Eu-n-En (IP38a); Eu-d-p (5F39, 5F41b)

Eu 153m	A genet (52M50)		IT (52M50)	3.0 x 10 ⁻⁹ e delay coinc (\$2M50)		0.069 (e _K /y 3.8), 0.103 (e _K /y 1.2, K/L+M 3.5) acint spect (52M52e)	(IIKS), IIH50) Eu ^{153m} 0.173	daughter Sm ¹⁵³ (52M50)
Eu 153		52. 23 (43H48)					(6/2 +) - 1 - 0 (18G52) Eu ¹⁵³ , I = 5/2 (87M50)	fission U (mass spect) (3150a)
Eu 154	A n-capt (69338); mass apect (31474 60H49); chem (84M49a)		6 (60H49)	16 y (7K52); 5.4 y yield (60H49)	1.9 (-10%), 0.7 (-40%), 0.3 (-50%) abs (64M49), calc from 60H49); 60.7 (coinc with hard y), 0.3 abs, 6.7 (coinc with hard y), 0.3 abs, 6.7 (coinc abs (64M498)); with E.19% and E.19%; 1.88, 0.90, 0.5%, 0.1% apect, 6.7 coinc abs (24K504); 1.186, 26K48, 11150, 317847)	0.336, 0.778, 1.116 spect conv (IIK51); with Eul54 and Eul55; 0.085, 0.101, 0.725, 1.005, 1.288 spect (245304); 0.122 spect conv (43K52); others (26K48, 10C48b)		Eu-n-y (69538, 5F9), 5F4lb, 2847); Eu-d-y (5F4lb, 26K48); Eul ²⁵ (fission product)-n-y (84K49 _a ); fission U (24K50d)
Eu 155	A chem (51 W5lc); mass spect (60H49)		p (51W51c)	1. 7 y (31852); yield (60H49); 2. 0 y (\$1W51c)	0.154 (80%), 0.243 (20%) spect, β-γ, γ-γ coinc (84M49a); see Eu ¹⁵⁴ 6's (24K50d)	0.066 (weak), 0.067 (K/L-8), 0.106 (K/L-8), 0.132 (weak) 0.065, 0.099 crit abs Pb, Pt (81M49a); 0.094 crit abs Tl, Hg (51W51c); 0.015 ion ch, B-y coinc (33W52); see Eu ¹⁵⁴ y's (24K50d)		Sm-d-n (4744); Eu-n-y (second order reaction) (60H4); spall-fission T (7N49a); fission U (51W5)c, 84M49a); daughter Sm ¹⁵⁵ (3147c)
Eu 156	A chem (51W51b); mass spect (3147b, 3147c)		6 (SIWSIb)	15.4 d (51W51b, 3147c)	-0.5 (60%), 2.4 (40%) abs (514/51)	2.0 abs (514/51b)		Eu-n-y (second order reaction) (3147c); pgall-(saion Th (7N49a), U (6048, 6FS)); fission U (51.K51b), Pu GEFS1); daughter Sm ¹⁵⁶ (51.W51b)
Eu 157	D chem (51W51d)		(51W51d)	15.4 h (51W5ld)	-1.0 (-75%), -1.7 (-25%) abs (51W51d)	0.6, 0.2 abs (51W51d)		spall-fission Th (7N49s); fission U (51W5ld), Pu (32K48)
Eu 159	D chem (51W51d) F excit (65B50)		6 (SIWSId)	60 m (51W51d) 20 m (65B50)	2.6 abs (51W51d)	y (Siwsid)		flasion U (51W5ld) Gd-y-p (?) (65B5U)
64 Cd 148	B chem, excit, sep isotopes (42R52)		a, EC (?) (42R52)	>35 y (42R52)	a: 3.16 ion ch (42R52)			Sm-a-3n, Sm ¹⁴⁷ -a-3n (42R5.2); Eu-p-4n (42R5.2); eaall Dy (42R5.2)
Cd 149	B chem, excit, sep isotopes, cross bomb (74H51)		EC 99+%, a -10-3% (42R52)	9 d (74H51)	a: 3.0 ion ch (74H51); conv: 0.35 abs (74H51)			Sm-a-2n, Sm ¹⁴⁷ -a-2n (74451, 42852); Eu-p-3n (74451)
S 150	D chem (42R52)		a (42R52)	long (42R52)	a: 2.7 ion ch, range emule (42R52)			Eu-d-3n (42R52)
Sa 151	F chem, excit (63H50)	0 20 (1860)	EC, no p [†] (63H50)	150 d (63H50)		0.265 (e/y large) abs (63H50)		Eu-d-2n (5F41b, 26K48, 63H50)
251 B	A mass spect (3147c); chem, n-capt (63H50)		EC, no β ⁺ (63H50)	236 d (63H50); 225 d (24K49a)		0.104 (K/L 5.2) spect conv (10C5C) 0.100 spect conv. abs (24K49a); 0.106 (e/v >0.9) abs (63H50); others (10C48b)		Eu-d-2n (63H50); Gd-n-y (314°c, 10C48b, 24K49a, 63H50)

- Indian	200.00	Dement	Tunend		Energy of rad	Energy of radiation in May		
V Z	identification	abundance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	Method of production and genetic relationships
154								
64043		2.15 (IE50)						
S4155		14. 73 (1B50)						
25 B		20.47 (1B50)						
و ₁₅ 3		15. 68 (1B50)						
Gd 158		24.87 (1B50)						
ed 159	B n-capt (2547); chem (65B49, 63H50)		p (26K48)	18. 0 h (65B49, 65B50, 26K48); 17. 9 h (24K49b) -24 h (63H50)	0. 9 abs (26K48, 65B49)	0.055, 0.38 abs (65B49); -0.3 abs (26648); others (52M51)		Gd-n-y (2547, 24K49b, 65B49, 63H50); Gd-d-p (26K48); Gd-y-n (65B50)
09180		21. 90 (1850)						
<u></u>	C n-capt (3146); n-capt, excit (65B49)		6 (38M49)	3.6 m (65B49, 24K49b); 3.5 m (26K48); 3.3 m (38M49); 4.5 m (3146)	l. 5 abs (24K49c); -2 (38M49)	0.37 abs (24K49c); -0.07 (38M49)		Gd-n-v (3146, 26K48, 65B49, 38M49, 24K499); parent Tb ¹⁶ (24K49b, 24K49c)
65 Tb 149	A chem, mass spect (42R50)		a, EC (?) (42R52)	4.1 h (42R52)	a; 3.955 spect (42R52); 3.95 ion ch (42R52)			spall Gd, Dy (3T49, 42R52), Tb, Yb (42R52); parent Eu ¹⁴⁵ (74H51)
Tb 151	D chem, excit (42R52)		a, EC (7) (42R52)	19 h (42R52)	3. 44 ion ch (42R52)			spall Eu (42R52), Gd, Tb, Dy (42R52)
Tb 153	B chem, excit (2W50c)		EC (2W50c)	5.1 d (2W50c)		1.2, 0.2 abs (2W50c)		Eu-a-2n (2W50c)
Tb 154	B chem, excit (2W50c)		EC 99+%, p ⁺ -0.5% (2W50c)	17. 2 h (2W50c)	2. 6 spect (2W50c)	1. 3 abs (2W50c)		Eu-a-n, Eu-a-3n (2W50c); Gd-p-n (2W50c)
Tb 155	D chem, excit (2W50c)		EC (2W50c)	190 d (2W50c)		1. 4 abs (2W50c)		Eu-a-2n (2W50c)
Tb 156	B chem, excit (2W50c)		EC >75%, 6 ⁺ <25% (2W50c)	5.0 h (2W50c)	-1. 3 abs (2W50c)			Eu-a-n (2W50c); Gd-p-n (2W50c)
Tb 157	B chem, excit, cross bomb (2W50c)		EC (2W50c)	4.7 d (2W50c)		1. 4 abs (2W50c)		Gd-p-n (2W50c)
Tb 159		100 (43H48)					Tb ¹⁵⁹ , I = 3/2 (87M50)	
75 160	A n-capt (37843); mass spect (3147c); chem (6FS1)		p* (37B43); no p* (82B50)	73. 5 d (37846); 71 d (82850); 76 d (10C50d)	0.860 (43%), 0.521 (41%), 0.396 (16%) spect (82B50); -0.90 p'(coinc with 0.085 y) scint spect, p-y coinc (52M52)	0.962, 0.876, 0.410, 0.191, 0.175, 0.296, 0.282, 0.215, 0.195, 0.087, 0.0196, 0.176, 0.093, 0.087, 0.970, 0.886, 0.100, 0.200, 0.970, 0.886, 0.100, 0.200, 0.085 apect conv (82B50); with Dylbóm; 0.085 (eg/y 1.7) ecint spect (52M52a); others (10C48b)		Gd-d-2n (26K48); Tb-n-y (37B45, 37B46, 2847); spall-fission U (6F51); parent Dyloom (52M52, 52M52a)

<

Dyleom

Dy 160

Dy 162 Dy 163 Dy 164

Dy 161

66Dy<153

Dy <153 Dy <153

Dy 156 Dy 158 Dy 159

Tb162,163

Tb 161

<

165m

<

Dy 165

	77.70		7		Freeze of radio	Freeze of redistion in Mer		
V Z	identification	abandance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
99, 166	A chem, genet (24K49d)		p (24K49d)	82 h (65 B 50a); 81 h (24 K 49d)	0. 2 abs (65550a); 0. 4 abs (24K49d)			Dy-n-y (second order reaction) (24K494, 6856a); spall-fission U (6F51); parent Ho ¹⁶⁶ (24K494, 65R50a)
67 Ho	E excit (42R52)		a (42R52)	4 m (42R52)	a: 4.2 ion ch (42R52)			Dy-p (42R52)
Ho 160	C excit (2W50c)		EC 99+%, 6 -0.5% (2W50c)	22.5 m (2W50c)	-1, 3 abs (2:W50c); conv: 0.2 abs (2W50c)	-1.2 abs (2W50c)		Tb-a-3n (2W50c)
Ho 161	B chem, excit (2W50c)		EC (2W50c)	4.6 h (2W50c)	conv: 0.1 abs (2W50c)	1.1 abe (2W50c)		Tb-a-2n, Dy-p-n, Dy-d-n (2W50c)
<b>3</b> 0 162	B chem, excit (2W50c)		EC -85%, p -15% (2W50c)	65.0 d (2W50c)	f.: 0.8 spect, abs (2W50c); conv: 0.1 abs (2W50c)	-1 abs (2W50c)		Tb-a-n, Dy-p-n, Dy-d-2n (2W50c)
Ho 16 3	B chem, excit, cross bomb (2 #50c)		EC (2#50c)	5. 20 d (2W50c)	conv: 0.4 abs (2W50c)	-0.5, 1.4 abs (2W50c)		Dy-p-n, Dy-d-n, Dy-d-2n (2W50c)
Ho 164	A excit (1938a)	100 000	6 (2W50c)	34.0 m (2W50c); 41.5 m (25W50)	0. 95 spect (2W50c)	no y (2W50c)	165 7/2 . 691.601	Dy-p-n (2W50c); Ho-n-2n (IP38a, 25W50); Ho-y-n (25W48)
2		106 (59120)					no . 1 = 7/2 (8/M50)	
990	A n-capt (71H36); mass spect (3147d); chem (24K49b)		p. (71H36)	27.3 h average of (24k49), 31674, 37846, 22G49, 10C49a, 31A50)	27.3 h average   1.84 (-89%), 0.55 (-11%) spect (2004); (7550a); (7550a); 22G49; (186 pect (20049); 1.64 (186%), 0.66 (14%) spect (100549, 11.65 (186%)); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (196%); 1.55 (1	0.080 (e _K /\(\psi\) 1.9, K/L+M 0.25), 1.38 (coinc with 0.08 \(\psi\) scint agest, \(\psi\) \(\psi\) coinc with 0.08 \(\psi\) scint agest, \(\psi\) \(\psi\) coinc (1855.a); 0.081 (k/L.0.07, L/\(\psi\) L/\(\psi	(1-) Ho (1-) - 543 J (1-) (1-) (1-) (1-) (1-) (1-) (1-) (1-)	Ho.n.y (71H36, 1938, 1M40, 2547); ppall-frasion U (6F51); daughter Dy166 (24K49d, 65B50a); parent E-166m (57M50a, 92M52a, 63M52)
₹ 91.94	B chem, excit (65B52)		¢ (65B52)	>30 y (65B52)	1.1 (-8%), 0.28 (-46%), 0.18 (-46%) abs (65B52)	0. 212 (coinc with 1.1 \$), 0. 280 (coinc with 0.73 and 0.83 y), 0. 725, 0.830, 0.095 (very weak) scint spect, y-y, \$\beta_{-y}\$ coinc (65852)		Ho-n-y (65R52)
Ho ^{857,169}	E excit (65B50)			96 m (65B50)				Er-y-p (65B50)

spall-fission U (6F51)		epall-fission U (6F51)		Dy-a-3n (2W50d); Ho-p-n (6SB50b, 29K52); Ho-d-2n (2VK52)	ese Ho 166 (52M50a, 63M52, 52M52a) (2+) 60 (52M50a, 63M52, 52M52a)	(04) 0 0 (18652)	Er ¹⁶⁷ , 1 = 7/2 (97B51b)		Er-y-n (65B50); Er-n-y (45K48);		5), Er.n.y (71H36, 1P38a, 24K48, 37B46, 23N15);  parent Tm ^[7] (24K48);  parent Tm ^[7] (10D48)  h	Er-n-y (38M49a, 45G51)						Ho-a-3n (2W49a);	Ho-a-3n (2W49a); Freen (2W49a)	Ho-a-3n (2W49a); Er-p-n (2W49a);	Ho-a-3n (2W49a); Ep-n-n(2W49a);	Ho-a-3n (2W49a); Er-p-n (2W49a); daughter Yy-166 (6F51)
				1. 1 abs (2W50d); no y (65B50b)	0.081 (e _K /y 1.9) acint apect (52M52a): 0.081 (K/L 0.07) apect conv (63M52)				no y (24K48, 11K51)		0.113 (K/L-10), 0.118 (K/L-0.5), 0.126 (K/L-2), 0.176, 0.295 (K/L-10), 0.308 (K/L-10), 0.420, no 0.8 y spect conv (11K51); g and 0.31 y), 0.31 (coinc with 1.05 g and 0.31 y), 0.31 (coinc with 1.05 g), 0.81 spect, spect conv, p-y coinc (24K48); 0.1 (e/y 1.3) p-y delay coinc	(10D48) 0. 210 (e _K / _Y 0. 55) acint apect (45G51, 24G51a)						l. 7 abs (2W49a)				
				сову: -0.2, 1.1 (weak) abs (29К52)					0.33 spect (24K48); 0.33 scint spect (11B49a)		1.49 (-6%), 1.05 (-72%), 0.67 (-22%) spect, β-γ coinc (24K48)						•	β . 2.1 apect (2W49a);	p*: 2.1 spect (2W49s); conv: 0.24 -1 smect shs (2W49s)	β ⁺ : 2.1 spect (2W49a); conv: 0.24, -1 spect, abs (2W49a)	β*: 2.1 spect (2W49a); conv: 0.24, -1 spect, abs (2W49a)	p [‡] : 2.1 spect (2W49a); conv: 0.24, -1 spect, abs (2W49a)
-17 h (6F51)		-65 h (6F51)		10.0 h (65B50bk 9.9 h (29K52); 11.2 h (2W50d)	1. 7 x 10-9 e delay coinc (52M50a)				9.4 d (24K48); 9 d (65B50)		7. 5 h (24K48, liK5l)	2.5 s (38M49a, 45G51)		,	,	,		7.7 h (2W49a)	7.7 h (2W49a)	7.7 h (2W49a)	7.7 h (2W49a)	7.7 h (2W49a)
p* (?) (6F51)		p ⁺ (?) (6F51)		EC (65B50b)	IT (\$2M50a)				p (24K48)		p (24K48)	IT (38M49a)	_				*	EC 99+%. B	EC 99+%, B+	EC 99+%, B*	EC 99+%, B + -0.5% (2W49m)	EC 99+%, B ⁺ -0.5% (2W49a)
	0.136 (60H50)		1. 56 (60H50)			33. 41 (60H50)	22. 94 (60H50)	27. 07 (60H50)		14. 88 (60H50)												
D chem (6F51)	•	D chem (6F51)		A chem, excit (65B50b); excit (29K52)	A genet (52M50a)				E chem. n-capt (24K48)		B n-capt (71H36, 23M35); chem (24K48)	E n-capt (38M49a)					:	B chem, excit	B chem, excit	B chem, excit (2W49a)	B chem, excit (2W49a)	B chem, excit (2W49a)
	Er 162	Er 163	Er 164	Er 165	Er 166m	Er 166	Er 167	Er 168	Er 169	Er 170	Er 171	E E					991	97 m166	96 Tm 166	69Tm ¹⁶⁶	69 Tm 166	, 166

	Sleen and	Bernesi	Tune of		Freeze of radiation in More	intion in Max		100 mm
Isotope Z A	identification	abundance	decay decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	Method of production and genetic relationships
69 ^{Tm 167} B	B chem, excit (2W49a)		EC, no B [†] (2W49a)	9.6 d (2W49a)	conv: 0.21 abs (2W49a)	0.22, 0.95 abs (2W49a)		Ho-a-2n (2W49a); Er-p-n (2W49a); spall Ta (2W49a);
Tm168	A chem, excit (2W49a)		EC, 6 (?) -2% (2W49a)	85 d (2W49a)	conv: 0.16, 0.5 abs (2W49a)	0 21, 0.85 abs (2W49a)		Ho-a-n (2W49a); Er-p-n (2W49a); Tm-n-2n (2W49a)
Tale ⁹⁸	A genet (10D48)		IT (10D48)	all delay coinc: 0.658 x 10-6 (27F50); 0.67 x 10-6 (75M51a); 0.7 x 10-6 (52M51); 0.60 x 10-6 (14551a)		see y's of yb ¹⁶⁹		daughter Yo ¹⁶⁹ (10048, 27F50, 52MS1, 14SS1a, 7SMS1a)
Tm169		100 (71.50)					Tm ¹⁶⁹ , I = 1/2 (87M50)	
- 13 170 P	A n-capt (23N36, 71H36); Chern (24K48a)		0 (37846a); 0 5C (11m 0 3%); 0 1%); 0 0%) (14G52)	129 d (24K49b); 120 d (42C50); 127 d (37E46a)	0.968 (76%), 0.884 (24%) spect (46524); pect (146524); 0.386 (-10%) spect (15F49); 0.970, 0.88 spect, \$6-y coinc (44829); 0.90 spect (16A50); others (14G49, 22G49a, 97550, 9549a)	0.084 (3%, eg/y1 6, K/L/M = 1/2,6/0.75) apect conv. f-y conc (14G52); Y (-3%, e/y 9, 4, K, L4M 0.22) x-y conc, x-y 9, 4, K, L4M 0.22) x-y conv., s-cnn apect (1850); 0.085 (K'. 0.16, L†/L/H 12, L10, R/L/M 15, R/L/M 15	0p 0.970 (36F49) (I-) Tm ¹⁷⁰ 90 (2+) Yb ¹⁷⁰ (I8652)	Tm-n-y (71416, 23036, 2847t Tm-d-p (24K48a); parent Yb ^{170m} (8P50, 52M5 ² a, 14G52)
	B genet (10D48)		IT (10D48)	2.5 x 10 ⁻⁶ s delay coinc (10D48)		0. 113 (e/y 1.3) spect conv, 6-y coinc (10D48); 0. 113 (e/y large) spect conv, 6-y coinc (24K48)		daughter Er ¹⁷¹ (10 <b>04</b> 8)
	B chem, genet (24K48)		6 (24K48)	680 d (24K49b)	0.10 spect (24K48a)			daughter Er 171 (24K48)
Tm172(?)	E chem (6F§1)		p^ (6F51)	2-3 d (6FSI)				spall-fission U (6F51)
1m,171	E excit (65P50)			19 m (65B50)				Yb-y-p (?) (65B50)
70 YP 166	D chem, genet (6F51)	0.140 (1B50)	EC (6F51)	62 h (6F51)				epall-fleeion U, parent Tm ¹⁶⁶ (6F51)

ä :												C
Tm-d-2n (24K48a); Yb-n-y (34A45, 37B46a, 3148a); spall-dasion (16F51); spall-dasion (16F51); 52M51, 14S51a, 75M51a)	daughter T ^{m170} (8B50, 14G52, 52M52a)						Yb-n-y (34A45, 37B46a, 3147f, 24K49b); Yb-y-n (65B50)		Yb-n-y (82M35, 71H36, 1P38a, 37B46a, 3147f); parent Lu ^{177m} (52M49, 52M51)	<u>,                                     </u>	Yb-n-y (38M49a, 38M49)	Yb-n-y (31K51)
	124) Yb170m 0.084	(18652)	Yb ¹⁷¹ , I = 1/2 (87M50)		Yb ¹⁷³ , I = 5/2 (87M50)				Y6 ¹⁷⁷	Lu 177m	(18652)	
Y ₁ 0. 023, Y ₂ 0. 064, Y ₃ 0. 095, Y ₄ 0. 110 (e/Y 1. 6), Y ₅ 0. 120, Y ₆ 0. 131 (e/Y 0. 2), Y ₇ 0. 143, Y ₈ 0. 160, Y ₉ 0. 178 (e/Y 0. 8), Y ₁₀ 0. 198 (e/Y 0. 4), Y ₁₁ 0. 308 Y ₁₁ z 1. 3/2. 1/2. 0/1. 0/1. 7/0. 6) spect, spect conv. delay coinc (75 M52) e. 0. 0. 100, 0. 131, 0. 177, 0. 0. 0. 0. 0. 0. 0. 177, 0. 109, 0. 130, 0. 177, 0. 109, 0. 130, 0. 177, 0. 109, 0. 130, 0. 177, 0. 109, 0. 130, 0. 177, 0. 109, 0. 130, 0. 177, 0. 109, 0. 130, 0. 177, 0. 109, 0. 130, 0. 177, 0. 198, 0. 307 scint spect, delay coinc (1455)a)	0.0841 (e _K /Y 1.6, K/L/M = 1/2.6/ see Tm ¹⁷⁰ 0.751 spect conv, β-y coinc (14G2E); 0.085 (k/Y 1.5) scint spec' (\$2M52s)						0.138, 0.259, 0.283, 0.396 spect conv (10C50e); others (52M51)		0. 150 (K/L 3) spect conv, β-γ coinc (52M51)	0. 212, 0. 104 (?) scint spect (31K51); (31K51); (20. 200 abs (38M49a); Vh. Ky. (38M40)	- 0.025, Yb L-x abs (38M49a)	0.455 scint spect (31K52)
							0.50, 0.13 abs (37B46a); 0.45 cl ch (34A45)		1, 3 abs (37B46a); 1, 2 cl ch (34A45)			
31. 8 d (49 W49); 32. 4 d (10CSo); 33. d (37B46a, 75M51a)	1. 57 x 10 ⁻⁹ a delay coinc (14G52); 1. 6 x 10 ⁻⁹ a delay coinc (52M52a)						102 h (3147f); 99 h (37B46a); 101 h (34A45)		1.8 h (52M51); 1.9 h (34A45); 2.4 h (37B46a)	6 • (38M49a, 31K51)	50 . (38M49a)	0.15 e (31K52)
EC (37846a)	IT (8B50)						p ⁻ (34.445)		p [*] (37B46a)	IT (38M49a)	IT (38M49a)	
		3.03 (1B50)	14. 31 (1B50)	21. 82 (1B50)	16. 13 (1B50)	31. 84 (IB50)		12. 73 (1B50)				
A n-capt (37846a); Cham, excit (24K46a)	A genet (8B50)						A n-capt (37B46a, 34A45); mass spect (3147f); chem (24K49b)		B n-capt (82M35, 71H36); chem (24K49b)	E n-capt (38M49a)	E n-capt (38M49a)	E n-capt (31K51)
	rb 170m	Ye 170	78,171	YP 172	Yb173	¥21.67	yb 175	42 ex	Yb 177	E _q ,	E q.	e £

			,		,	Parent of Linited in Man		
V Z	identification	apradance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	Method of production and genetic relationships
71 La 170	B chem, excit (2W51)		EC (2W51)	1.7 d (2W51)		- 2.5 abs (2W51)		Tm-a-3n, spall Ta (2W51)
E_3	B chem, excit (2W51)		EC (2W51)	8.5 d (2W51)		-1. 2 abs (2W51)		Tm-a-2n, Yb-p-n, spall Ta (2W51);
E ₃	D chem, excit		EC (2W51)	-600 d (2WSI)		-1 abe (2W51)		daughter HT*** (2W51) Tm-a-2n (2W51)
271 mJ	B chem, excit (2W51)		EC (2W51)	6. 70 d (2W51)		l. 2 abs (2W5l)		Tm-a-n, Yb-p-n (2W51); daugher Ht ¹⁷² (2W51)
211 m	B chem, excit (2W51)		6+, EC (?) (2W51)	4.0 h (2W51)	1. 2 abs (2W51)			Tm-a-n, Yb-p-n, Lu-p-p3n (2W51)
E ₁₃	B chem, excit (2W51)		EC (2W51)	-500 d (2W51)		- 0. 2, 0.8 abs (2W51)		Yb-p-n, Lu-p p2n (2W51); daughter HI ¹⁷³ (2W51)
ž.	A chem, excit (2W51)		EC -80%. 6-20% (2W51)	165 d (2W51)	p ⁻ : 0.6 abs (2W51)	-1 abs (2W51)		Lu-n-2n, 1.u-d-p2n, Lu-p-pn, Hf-d-a (2W51)
2 ¹ 3		97. 40 (60H50)	_				Lu ¹⁷⁵ , I = 3/2 (87M50)	
_{Lu} 176m	A n-capt (77M35a, 82M35); chem, excit (2W48)		p. no IT (17552)	3.67 h (34445); 3.7 h (37B46a)	3. 67 h (37846s); 1. 1. 2. 2 (17852); 3. 7 h (37846s) 1. 3 c1 ch (34445); 1. 2 abg (9F43)	0.0589 (K/L _{II} /L _{III} = 0.24/0.71/1.00 aper conv (6.3M2); 0.089 (e _K /v _I .3) acint apec; p-v delay coinc (52M52c); apect (1752)	(12) _Lu176m	Lu-d-p (2W51, 2W48); Lu-n-y (77M58, 82M35, 71H56, 9F43, 37R46a, 14A45, 2S47, 2K49b, 31A50a); Lu-y-y (1ID47a, 65R50); parent H ¹⁷ 0m (52M526)
5. 1.3	A chem (52H38); mass spect (8M39)	2. 60 (60H50) p', no EC (17552a)	p, no EC (17552a)	7.5 x 10 ¹⁰ y sp act (3L39a)	0.40 abe (9F47a, 9F43)	0. 270 scint spect	1 »7 (67M50)	natural aource (52H38, 8M39)
							(18652)	
E 14	B genet (52M49)		IT (\$2M49)	1.3 x 10 ⁻⁷ e delay coinc (52M49, 52M51)		0.150 (K/L.3) scint spect, β-y coinc (52M5), 52M49)	0.150 0.150 0.150	daughter YD ¹⁷⁷ (52M49, 52M51)
12	A n-capt (71H36); mass spect (3147f); cbam, excit (2W48)		p (37846a)	6.8 d (37846a, 2 W48); 7.0 d (30049); 6.6 d (9F43, 34A45)	0. 495 (65%), 0.37 (17%), 0.17 (18%) spect (30049); 0.475 spect (31A50a)	0.112 (eg/y'0.81), 0.206 (eg/y 0.04), 0.318 (-5%) scint spect, y y coinc (52MS2d), 0.112, 0.206, 0.317 (yesy weak) spect, spect cony (30D49); 0.112 (K/L/M = 1/2/0.5), 0.205 spect cony (31AS0a); 0.113, 0.209 spect cony (10C49a); others (52MS1)	Q-6 0.49 (HPS)	Lu-n-y (71H36, 9F43, 34A45, 37B46a, 2547, 24449b, 31A50a); Lu-d-p (2W48) ·
T. T	D chem (65B50)			22 m (65B50)				H-y-p (65B50)

Lu-p-6n (2W51)	Yb-a-3n, Lu-p-5n (2W51); parent (8.5 d) Lu ¹⁷¹ (2W51)	Yb-a-2n, Yb-a-3n, Lu-p-4n spall Ta (2W51); parent (6.7 d) Lu ¹⁷² (2W51)	Yb-a-n, Yb-a-2n, Yb-a-3n, Lu-p-3n (2W51); parent Lu ¹⁷³ (2W51)	Lu-d-2n, Lu-p-n (2W49b); H-n-y (12H51a); H-1 ⁷⁴ -n-y (82B51)	daughter Lu ^{176m} (52M52c)	0) H. n., (9F44b, 9F46, 38M51); H. 178-n., (38M51b, 82B51) S0) H. 179-n., (82B51)
					24 Lu 176 Hf 176m (2+) Hg 176m	(0+177, 1 = 1/2 or 3/2 (87M50) H1 ¹⁷⁸ , 1 = 0 (87M50) (972-)————————————————————————————————————
no y (2W51)	1.4 abs (2W51)	-0.28, 0.8 abe, spect conv (2W51)	-1 abs (2W51)	0.089, 0.113, 0.228, 0.318, 0.345 (17,L.4.9), 0.431 spect core (82.852); 1. 5 abs (2.W49b)	0, 089 (e _K /y 1, 3) scint spect, β-y coinc (52M52c)	0.160, 0.217 acint spect, spect conv (82851); conv (82851); conv-y coinc (884851b); d.150 (47 very large, K/L 0.9) spect conv (18148a); e.220 acint spect (31K51) c.220 acint spect (31K51) c.42 spect conv y-conv coinc (82851)

2.4 spect (2W51)													
112 m (2W51)	16. 0 h (2WSI)	-5 y (2W51)	23.6 h (2W51)		70 d (2W49b)	1.35 x 10 ⁻⁹ e delay coinc (52M52c)				19 a (9F44b, 38M51b)		5.5 h (82B51)	
¢ (2W51)	EC (2W51)	EC (2W51)	EC (2W51)		EC (2W49b)	IT (52M52c)				П (9F46)		IT (82B51)	
				0.18 (75H49)			5.15 (75H49)	18. 39 (75H49)	27. 08 (75H49)		13. 78 (75H49)		35. 44 (75H49)
D chem (2W51)	B chem, genet, excit (2W51)	B chem, genet (2W51)	B chem, excit, genet (2W51)		A chem, excit (2W49b); n-capt, aep (82B5); mas apect (12H51a)	A genet (52M52c)				A n-capt (9F44b); n-capt, sep isotopes (82B5), 38M51b)		B chem, n-capt, sep isotopes (82B51)	
75HL170	1111	Ha 172	ът,173	₽ ₁₁ 74	ж175	н г ^{176т}	9 ₂₁ JH	нг177	Hr178	H 73 m	ни 179	т _{180т}	нт₁80

- I	Clear and	Perrent	Type of		Energy of radiation in Mey	iation in Mev		,
V Z	identification	abundance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and acheme	Renetic relationships
181 ^{H122}	A chem, n-capt (111418); mass spect (121451a); app isotopes, n-capt (62851)		p (71H38)	45 d (10C50f. 22R50); 47 d (43B48a)	0. 408 apect (29F52); 0. 410 apect (4550); 0. 460 apect (41C49); 0. 460 apect (43B48a)	10.133, γ2 0.136, γ3 0.134, γ2 0.136, γ3 0.134, γ2 0.136, γ3 0.134, γ3 0.134, γ3 0.134, γ3 0.135, γ3 0.13	(1,72,5,72+) (1,72,5,72+) (1,72,5,72+) (1,72,5,72+) (1,72,5,72+) (1,72,5,72+)	H-n-y (71H18, 2547); 12(-100-n-y (82B51); Tan-p (54M51); parent Tallin! (4E50, 63B50, 52M51); parent Tallin2 (10D48, 4E50, 63B50, 52M51);
£	E (24C52)		IT (24C52)	-3.5 a (24C52)				Hf-n (24C52)
73 ^{Ta} 176	B chem, excit (2W48, 2W50e)		EC (2W50e)	8.0 h (2W50e)	conv: 0.1, 0.2, -1 abs (2W50e)	-2 abs (2W50e)		Lu-a-3n (2W50e); spall Ta (2W48); daughter W ¹⁷⁶ (2W50e)
Ta 177	B chem, excit (2W48, 2W50e)		EC (2W50e)	53 h (2W50e)	conv: 0.1 abs (2W50e)	-1.4 (weak) abs (2W50e)		Lu-a-2n, Lu-a-3n, Hf-p-n (2W50e); epail Ta (2W48); daughter W ¹⁷⁷ (2W50e)
Te 178	B chem, excit (2W50e)		EC -97%, p ⁺	2.1 h (2W50e)	p*: -1 abs (2W50e); conv: -0.1 abs (2W50e)	1, 3-1, 5 abs (2W50e)		Lu-a-n, Hf-p-n, Ta-p-p3n (2W50e)
T. 178	B chem, genet (2W50e)		EC -94%, B*	9.35 m (2W50e)	p*: 1.06 spect (2W50e); conv: 0.08 spect conv (2W50e)	-1, 5 abs (2W50e)		Hf-p-n (2W50e); daughter W ¹⁷⁸ (2W50e)

Lu-a-n, Hf-p-n, Ta-p-p2n (2W50e) (2W50e) Ta-n-2n (1P37, 17038, 2W50e); Ta-y-n (27M49, 55S51, 95B51); Ta-p-pn (96B49, 2W50e); W ¹⁸² -y-pn (83M51)	daughter jy ¹⁸¹ (10D48, 4B48. 4E50, 63B50, 52M51)	daughter H ¹⁸¹ (4E50, 63B50, 52M51)		Ta-n (24C49, 45G50, 31K51)	Ta-n-y (2547,15H48a, 2W50e)
FC - 50%	(1/2,3/2-) Hf  8  (1/2,3/2-) Hf  8  p	0.480	Tall I = 7/2 (87M50)	F	H
-0.7 (weak) abs (2W50e)  Y ₁ 0.093 (K/L-0.15), Y ₂ 0.102  (Y ₁ + Y ₂ : e/Y -5), Y ₃ 0.2, Y ₄ 0.4  (Y ₃ and Y ₄ very weak) spect  conv. scint spect, β-Y, x-Y  coinc (95B5);  1.3 abs (2W50e)	see y's of H ¹⁸¹	sec v's of Ht ¹⁸¹		Ta L-x (45G50, 31K51)	0.180 (K/L 0.25) spect conv (15H48a); 0.180 (e _K /y 0.8) scint spect (14S5)
(2W50e) (2W50e) (2B50e); (95B51); (95B51); (2W50e); (2W50e); (2W50e); (2W50e); (2W50e); (2W50e); (2W50e); (2W50e); (2W50e); (2W50e); (2W50e); (2W50e); (3B731)					16. 2 m (15448a) p̄ ⁺ : 0.6 abs (2W50e) 16. 2 m (2547)
-600 d (2W50e) 8. 15 h (95B51); 8. 00 h (2W50e); 8. 2 h (17038)	2.2 x 10-5 s delay coinc (10D48, 4E50, 63B50); 2.0 x 10-5 s delay coinc (4B48)	1. 2 x 10 - 8 a delay coinc (4E50); 1. 1 x 10 - 8 a delay coinc (5B50); 1. x 10 - 8 a delay coinc (5B50); 1 x 10 - 8 a delay coinc (52M51)		0.33 a (24C49, 45G50,31K51)	16. 5 m (15H48a) 16. 2 m (2S47)
EC (2 W 50e)  EC - 79 %, p - 21 %, no p (1 im 0, 0.05 %)  (95 B 51)	IT (10D48)	IT (63B50)		IT (45G50)	IT (15H48a); IT -95%, 6- -5% (2W50e)
			100 (24W48)		
D chem, excit (2W50e) A chem, excit (17038)	A genet (10D48)	A genet (63B50)		E n-excit (24C49, 24C52)	A chem, n-capt (2547, 15H48a)
Ta 179	Ţ. 181m2	T. 181m1	Ta 181	Ę.	Tal82m

	100	Person	Tomand		France or France	Process of radication in Man		
V 2	identification	abnodance	decay	Hall-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
73 Ta 402	A chem, n-capt (37F36, 17O36)		p (76H40)	11 d (21 E5 2. 3851); 11 d (9549¢); 11 d (2547; 11 Z 43)	0. 525, other g's, spect (7J49); 0. 53 spect (86B49a); others (IIR47, 7J47, 24N47)	11.0.065714, γ2 0.067736, γ3 0.084667, γ4 0.11009, γ5 0.11366, γ6 0.11640, γ7 0.15241, γ8 0.15677, γ9 0.15205, γ10 0.19931, γ10 0.22205, γ12 0.22977, γ13 0.26409, γ14, 1.12, γ15 1.188, γ16 1.223 (real interne) γ19, γ2 100, γ3 6, γ4 46, γ5 9, γ6 2, γ7 43, γ8 14, γ9 19, γ10 9, γ18 17 γ12 24, γ13 27, γ14 352, γ18 17 γ12 24, γ13 27, γ14 352, γ18 17 γ16 314) στγκε spect (100λ42); 0.058 0.065, 0.067, 0.046, 0.058 0.067, 0.046, 0.058 0.067, 0.046, 0.058 0.067, 0.027, 0.113, 0.139, 0.122, 0.122, 0.113, 0.139, 0.121, 0.122, 0.121, 0.139, 1.219 spect, spect conv (100516); 0.222, 0.243, 0.256, 0.264, 0.229( γ1), 0.299 (γ1), 0.324, 0.220, 0.320, 0.342, 0.352, 0.220, 0.320, 0.342, 0.352, 0.280, 0.320, 0.342, 0.352, 0.580, 0.320, 0.342, 0.352, 0.580, 0.320, 0.342, 0.352, 0.580, 0.320, 0.342, 0.352, 0.563, 0.607, 0.624, 0.728, 0.763, 0.763, 0.728, 0.728, 0.763, 0.764, 11847, 1004-96, 1226, 0.763, 0.764, 11847, 1004-96, 1226,		Ta-n-v (37F 36, 17038, 76H40, 2547, IM48); Ta-d-p (17038, 11243, 31850); W-d-a, W-n-p (33T51)
Ta 183	B chem, excit (65B50)		p_ (2W50f)	5. 2 d (65P52c); 6. 0 d (83M51); 6. 1 d (7 W50f)	0. 6 scint spect (65P5.c); 0. 6 abs (2W50f, 83M5])	0.24 scint spect (65B52c); y (3W50f)		W-n-p (7W50f, 65P5/c); W-y-p (65B50, 83M51)
Ta 184	B chem, excit (65P52c)		β (65B52c)	9.3 h (65B52c)	1.4 abs (65B52c)	0.410, 0.86, 1.10 scint spect (65B52c)		W-n-p, W ¹⁸⁴ -n-p (65B52c)
T. 185	A chem, excit (65B50); excit, sep isotopes (23D50)		۴ (23050)	48 m (83M51, 65B50)	1. 6. 0. 15 (conv?) abs (83M51); 1. 7 abs (23D50)			W-y-p (65850, 83M51); W ¹⁸⁶ -y-p (23D50)
	B chem, genet (2W50e)		EC 99+%, 6 ⁺ -0.5% (2W50e)	80 m (2W50e)	6*: -2 abs (2W50e); comv: -0.1, -0.2 abs (2W50e)	-1. 3 abs (2W50e)		Ta-p-6n (2W50e, 22N52); parent Ta ¹⁷⁶ (2W50e)
w177	B chem, genet (2W50e)		EC (2W50e)	130 m (2W50e)	conv: 0.13, -0.4 abs (2W50e)	-0.5, 1.2 abs (2W50e)		Ta-p-5n (2W50e, 22N52): parent Ta ¹⁷⁷ (2W50e)

EC (2W50e) 30 m (2W50e) [C (2W50e) [C (2W50e) [C (2W50e) [C (2W47) [C (2W46)				parent 9. 4 m fa178 (2W50e)
EC (2W47) 140 d (2W47)  EC (2W47) 140 d (2W47)  IT (23D50) 1.85 m (23D50)  IT (23D50) 1.85 m (23D50)  p^*(64M40) 73.2 d (9548a);  p^*(64M40) 24.1 h (5F40a);  p^*(64M40) 24.1 h (5F40a);				Ta-p-3n (2W50e)
EC (2W47) 140 d (2W47)  IT (38M49) 5. 5 e (38M49, 24C52a)  IT (23D50) 1. 85 m (23D50)  \$\begin{align*} \begin{align*} a				Ta-p-3n (2W50e)
EC (2W47) 140 d (2W47)  IT (3BM49) 5.5 e (3BM49, 24C52a)  IT (23D50) 1.85 m (23D50)  P (64M40) 73.2 d (9548a);  P (64M40) 24.1 h (5F40a);  24.0 h (64M40);				
IT (38M49) 5.5 e (38M49, 24C52a)  IT (23D50) 1.85 m (23D50)  \$\begin{align*} \begin{align*} \beg		0.030, 0.600, 0.800 scint spect (13A50b); 1.8 (weak) abs (2W47)		Ta-d-2n (2W47); Ta-p-n (96B49); W-n-y (13A50b, 31L51); mo ne
24C52a) 24C52a) 1. 85 m (23D50) 73. 2 d (9548a); 75 d (5F40a) 24. 1 h (5F40a); 24. 0 h (644440)			W ¹⁸² , I = 0 (87M50)	
1. 85 m (23D50) 73. 2 d (9548a); 75 d (5F40a) 24. 1 h (5F40a); 24. 0 h (64M40)	conv: 0.08 abs (38M49a)	0.12, 0.17 scint spect (24C52a)		W182-n-y (38M49);
1. 85 m (23D50) 73. 2 d (9548a); 75 d (3F40a) 24. 1 h (5F40a); 24. 0 h (64M40)			W ¹⁸³ , I = 1/2 (87M50)	
1. 85 m (23D50) 73. 2 d (9548a); 75 d (5F40a) 24. 1 h (5F40a); 24. 0 h (64M40)			W ¹⁸⁴ , I = 0 (87M50)	
73.2 d (9548a); 75 d (5F40a) 24.1 h (5F40a); 24.0 h (64M40)	corv: 0.075 scint spect (23D50)		981 M ~ 245)	W ¹⁸⁶ -y-n (23D50)
24.1 h (5F40a); 24.0 h (64M40)	0. 428 spect (68548); 0. 43 spect (20P48, 9548s); others (23545s)	no y (10L52c, 23S45a, 65C47a); othere (10C49, 4B49, 52M51)	(10L32c)	W-n-y (64)440, 5F40m, 2547, 10C49); W-n-2n (64)440, 5F40m); W-d-p (5F40m);
24. 0 h (5F40a); 24. 0 h (64M40)			W ¹⁸⁶ , I = 0 (87M50)	Re-d-a (5F40a)
	24. 1 h (5F40a); 1. 33 (30%), 0. 63 (70%) spect 24. 0 h (64M40); (20048); 1. 32 (24%); 1. 32 (24%); 1. 340. 65 spect (15148b); others (23545s, 43M46)	0.07200, 0.13425, 0.4795, 0.6189, 0.6881, 0.6861 cryst apect (100MS2); 1, 0.072 (coinc with y2, delay coinc with y1, y2, delay coinc with y1, y2, 0.134 (coinc with y1, y2, 0.480 (eg/y 0.022, delay coinc with y4 or y6), y4, 0.52 (coinc with y4 or y6), y4, 0.52 (coinc with y4 or y6), y4, 0.52 (coinc with y4 or y6), y4, 0.55 (coinc with y4 or y6), y4, 0.68 (or coinc with other y*s), y6, 0.69, y7, 0.775 (coinc with y2), y6, 0.68 (not coinc with other y*s), y6, 0.69, y7, 0.775 (coinc with y2), y6, 0.69, 0.69, 0.707 apect conv (2149); 0.20, 0.64, 0.652 apect conv, 0.707 apect conv (2149); 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619, 0.619,	Q 1.33 (HPS) W187 W187 (14552a) (14552a)	W-n-y (12A35, 77M35b, 64M40, 5540a, 2547, 10C49); W-d-p (5540a, 20P48); a-pail (6048); a-pail (167m (10D48, 4E49, 52M51)

1	Pos and	Percent	Type of		Energy of rad	Energy of radiation in Mev		Marked of receivering
V Z	identification	abundance	decay	AITI-ITIU	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
74W188	A chem, genet (37L51)		p ⁻ (37L51)	65 d genet (37L51)				W-n-y (second order reaction) (13A50c, 37L51, 37L51a); paren R ₂ 88 (371.51 371.51a)
75 Re 182	B chem, excit (2W50g); chem, sep isotopes (31D50)		EC (2W50g)	12.7 h (2W50g): 14 h (3ID50)		0.110, 0.127, 0.222, 0.250, 0.346 spect conv, spect (2W50g)		Ta-c-1n (2W50g); W-p-n (2W50g); W ¹⁸² -d-2n (31D50); daughter Os ¹⁸² (93S50)
Re 182	D (182) chem, excit (2W50g); (183) chem, sep isotopes (31D50)		EC (2W50g)	64.0 h (2W50g); 67 h (31D50)		0,110, 0,127, 0,222, 0,250, 0,346 spect conv, spect (2W50g)		Ta-a-3n, W-p-n (2W50g); W ¹⁸² -d (3lD50)
Re 183	B chem, excit (2W50g)		EC (2W50g)	155 d (33T51); 120 d (93S50)		0.081, 0.252 spect conv (2W50g)		Ta-a-2n, W-p-n (2W50g); W-d-n, W-a-p (33T51); daughter Os ¹⁸³ (93550)
Re 184	A chem, excit (5F40a); chem, excit (2W50g)		EC (2W50g)	50 d (2W50g, . 33T51)		0.159, 0.206, 0.244, 0.784, 0.89 spect conv (4W52); 0.043, 0.159, 0.205, 0.285 spect, spect, conv (2W50g); 1.0 abs (33T51, 29C40)		Ta-a-n (2W50g); W-a-pn (33T5!); W-p-n (2W50g); W-d-n (2OC40, 5F40a, 33T5!); Re-n-2n (2W50g, 5F40a)
Re 184	B chem, excit (2W50g)		EC or IT (2W50g)	2.2 d (2W50g)		0.043, 0.159 spect, spect conv (2W50g)		Ta-a-n (2W50g); W-p-n (2W50g)
Re 185		37.07 (24W48)					Re ¹⁸⁵ , :1 = 5/2 (87M50)	
R 186	A n-capt (8K35); n-capt, excit (95959); chen, n-capt, mass spect (43H47)		6 - 95%, EC - 5%, no 6+ (lim 10-5%) (44M51): 6 - 91%, EC - 9% (82551a)		92.8 h (24G47); 1.07 (80%), 0.93 (20%) spect (44M5); 1.07 (44M5); 1.070 (73%), 0.942 (27%) spect (82551a); 1.090 (67%), 2.095 (30%), 0.64 (3%) spect (22G49a); 1.053 spect (10L49); 1.07 spect (86B49a)	with \$\beta\$:  \[ \pi_137 \cdot \ext{ek} \gamma \cdot 0.35, \ \text{KL} \m = \pi_1 0.37 \cdot \cdot 0.35, \ \text{KL} \m = \pi_2 0.37, \ \cdot 0.627, \ \cdot 0.627, \ \cdot 0.624 \\ \text{apect}, \text{apect}, \ \cdot 0.34 \\ \text{v}_0 0.136 \cdot \ext{ek} \gamma \cdot 0.37, \ \ext{KL} \m = 0.6 \left( \lore 0.37, \ \ext{ek} \gamma \cdot 0.37, \ \ext{KL} \m = 0.6 \left( \lore 0.37, \ \ext{ex} \gamma \cdot 0.37, \ \ext{ex} \gamma \cdot 0.37, \ \ext{v}_0 0.123 \left( \lore 0.37, \ \ext{ex} \gamma \cdot 0.45, \ \ext{K} \gamma \cdot 0.6 \left( \lore 0.32 \left( \lore 0.37, \ \ext{ex} \gamma \cdot 0.45, \ \ext{K} \gamma \cdot 0.6 \left( \lore 0.32 \left( \lore 0.37, \ \ext{ex} \gamma \cdot 0.45, \ \ext{K} \gamma \cdot 0.6 \left( \lore 0.32 \left( \lore 0.32 \lore 0.37, \ \ext{ex} \gamma \cdot 0.6 \lore 0.6 \lo	Co (1-) Re 186 (1-	W-d-Zn (5F40a); W-p-n (12940); Re-y-n (12P48); R R-y-n (12P48); R R-n-y (8K13, 99539, 5F40a, 8F40, 2547); R R-n-Zn (9939, 8Y40, 5F40a); R R-n-Zn (9939, 8Y40, 5F40a); R R-n-Zn (9639, 8Y40, 5F40a); Parent Oalléfin (5ZM51a)



m/81.	A games (10048)		- T	6 1 2 10-7			781	187
				5.5 x 10 ⁻⁷ a delay coinc (4B49); 5.5 x 10 ⁻⁷ a delay coinc (52M51)		0.133 (eg/Y 453.4, K/L - 5) ecint spect (52M52b); see Y's of W187	Re W. Re 187m 0.206	daugster W (10D48, 4P49, 52M51)
Re 187	A chem (25N48)	62.93 (24W48)	p ⁻ (25N48)	4 × 10 ¹² y ap act (25N48, 63S48)	0, 400 ion ch (42D52); 0, 043 abs (25N48)	no y, no x (42D52)	(5/2+) Re 187 + 0 (14552a) (14552a)	natural source (25N48, 63S48)
Rе ¹⁸⁸ т	C n-capt, sep isotopes (63M52d, 63M52b)		IT (63M52d)	22 m (63M52d); 17 m (65B50)		0.0635, 0.092, 0.106 spect conv. scint spect (63M52b)		Re ¹⁸⁷ -n-y (63M52b); Oa-y-p (?) (65B50)
Re 188	A chem, n-capt (12A.35); n-capt, excit (993.9); chem, n-capt, excit (574a); mass spect (43H47)		p (99539)	16. 9 h (37 <u>151);</u> 18. 9 h (24 <u>G</u> 47); 18 h (1P37)	2. 07 (coinc with 0.152 y) spect, β-y coinc (44RS2a); 2. 10 spect (86B49a); 2. 05 abs (24G47); others (26M48b, 99S39)	0.152 (70%, e _K /γ 0.05, K/L 0.42), 0.476 (1%), 0.638 (6%), 0.933 (8%), 1.3 (5%) spect, abs., spect (6852a); 0.15, 0.48, 0.64, 0.95, 1.40 spect (4852a); 0.16, 0.48, 0.64, 0.94, 1.43 spect (48046); 1.39 coinc abs (26M48b); 0.154 spect conv (10C48)		Re-n-y (8K35, 12A35, 1P37, 99539, 5F40a, 8840, 2547); Re-d-p (5F40a, 44C47, 66C50); spall ( (6cd50); spall Re (6cC50); daughter W ¹⁸⁸ (37L5), 37L51a)
Re 189	D chem (37L51, 33T51)		6 (37LS1, 33TS1)	150 d (37L51); 250-300 d (33T51)	0.2 abs (37L51, 33T51)	1.0 mbe (33T51)		W-a-p (33T51); Re-n-y (second order reaction) (37L51)
å	E chem (37L51)		p (37L51)	≥5 y (37£51)	0.75 abe (37 <u>L</u> 51)			Re-n-y (second order reaction) (?) (37L51)
281809,	B chem, genet (93550)		EC, no p ⁺ (93850)	24. 0 h (93S50)				Re-p-4n (93550); parent Re ¹⁸² (9356)
0.183	B chem, genet (93S50)	<b>q</b>	EC (93550)	12. 0 h (93S50)	conv: 0.15, 0.42 spect conv (93S50)	J. J. 1. 6 abs (93550)		Re-p-3n (93S50); parent Re ¹⁸³ (93S50)
81.80	B chem, cross bomb (24G47, 50K48)	(6N37a)	EC (L/K -0.35) (69M51a); no p* (2B50b)	97 d (50K48, 33T51); 95 d (24G47)		γ ₁ 0. 648, γ ₂ 0. 878 (γ ₁ /γ ₂ -6) spect, γ·γ coinc (2B50b); γ ₁ 0. 65, γ ₂ 0. 88 (γ ₁ /γ ₂ 6. 1) scint spect (69M51b); 0. 235, 0. 653 spect conγ (116552)	QEC -1.0 cate (69M51a)	Re-a-2n (24G47, 66C50); Re-p-n (93S50); Oe-n-y (50K48)
							15/2+) 15/2+)	
			_				(2B50b, 69M51b, HPS)	

Popula	Ches and	Percent	Type of	11.17.11	Energy of rad	Energy of radiation in Mev		Method of randuction and
V Z	identification	abundance	decay	rion-line	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
760e 186m	A genet (52M5la)		IT (52M5la)	8 x 10 = delay coinc (52M5la)		0.137 scint spect (52M51a)	see Re 186	daughter Re ¹⁸⁶ (52M5la)
98.00		1. 59 (6N37a)						
O. 187m(7)	E chem (66C50)			35 h (66C50)				daughter Ir ¹⁸⁷ (?) (66C50)
0.187		1. 64 (6N37a)						
981		13. 3 (6N37a)						
0.189		16.1 (6N37a)					Os 189, I = 1/2 (87M50)	
Og 190m(7)	E chem (66C50)			6 h (66C50)				daughter 12 d Ir   (?)
190m	D chem, genet (66C50)			9.5 m (66C50)				daughter 3 h Ir 190 (66C50)
06190		26. 4 (6N37a)						
m191m	A chem, genet (116S52)		II, no p. (11m 5%) (11m 5%)	14 h (116852)		0 . 0742 $(L_{\rm I}/L_{\rm II}/L_{\rm III}$ = 42/24/100) spect conv (116892)	(1/2-) Os 191m (1/2-) Os 191m (1/2-1) Os 191m (1/2-1) Os 191m	Os-n-y, Os-y-n, parent Os 191 (116552)
161 00	A n-capt (12240); cham, n-capt (1324b); cham, excit (23F48a, 116552)			16. 0 d (66C50); 16. 1 d (984a); 15. 0 d (50K40)	0.143 spect (38K5lb); 0.142 spect (9848lb); others (50K44, 1364lb, 37W47, 26M4@, 2B50b)	γ ₁ 0.0417 (L _{II} /L _{III} = 32/40, e/γ large), γ ₂ 0.129 (coinc with γ ₁ , K/L _I /L _{III} = 100/30/11/6) spect conv. conv-conv coinc (11652); γ ₁ (e _K /γ 1.36) (116552, calc from 39K3b); 0.042 (L/M 1.8), 0.128 (e _K /γ -0.5, K/L 2.1) spect conv. spect (21853b); 31855(c); 0.041, 0.128 spect conv. spect (21590b); 0.127 spect conv (9548a); 0.127 spect conv (9648a); 0.129 spect conv (10C47)	(9/1 (9/1 (9/1 (9/1 (9/1 (3/1 (3/1 (3/1 (3/1 (3/1 (3/1 (3/1 (3	Os-n-y (1354lb, 12Z40, 2847, 116852); Os-y-n (22F48s, 116S52); Os-y-n (22F48s, 116S52); ppall U (6O46); daughter Os ^{19Im} (116S52)
0° 192		41.0 (6N37a)						

Os.n.y (2547); Os.d.p (11-4.2p spall U (parent In not found not fo	-0.065 Os.n.y ( (371.50)	Re-a-2n. Os-d-3n	Re-a-n. (66C50) Os-d-2n,	Re-a-n, Os-d-n,	Re-a-n, Cs-d-n ( Ir-n-2n (		Ir-n-y (l	08 - d - 2n 1r - n - y (1 28.47); 1r - n - 2n (1 1r - d - p (1 1r - y - p (1)
Q, 117 (HPS)	(1/6 S 52)					Ir 191, I = 3/2 (99B50); Ir 191, I = 1/2 (94B49)		O 6 (50852)
with Ir 193m; 0 066 speet conv (116S52); 0.065 scint speet, β·γ delay coint (2MS0b); no γ (2BS0b); others (24G47, 26M48b)		-1. 3 abs (66C50)	-1. 8 abs (66C50)		0.2, 0.6 abs (66.050); 0.3 abs (24047)		0.057 spect conv (42C50); 0.056 spect conv (15H46a); $\gamma$ (continuum) scint spect (18M51); $\gamma$ ( $\epsilon_L/\gamma >400)$ ion ch (31K51)	γ ₁ 0.13633, γ ₂ 0.20131, γ ₃ 0.20574, O ₆ γ ₄ 0.29594, γ ₅ 0.10845, γ ₆ 0.1646, γ ₇ 0.46788, γ ₈ 0.4648, γ ₉ 0.5884, γ ₁₀ 0.66788, γ ₈ 0.4648, γ ₉ 0.5884, γ ₁₀ 0.6045, γ ₁₁ 0.6129, (rel abund γ ₁ 4, γ ₂ 10, γ ₃ 75, γ ₄ 380, γ ₅ 370, γ ₆ 990, γ ₇ 370, γ ₈ 11, γ ₉ 11, γ ₁₀ 41, γ ₁₁ 19, 14, γ ₁₁ 19, 14, γ ₁₁ 19, 14, γ ₁₁ 19, 16, γ ₁₁ 19, 16, 0.136, 0.136, 0.136, 0.136, 0.136, 0.136, 0.136, 0.136, 0.136, 0.136, 0.139, 0.139, 0.139, 0.139, 0.139, 0.400, 0.415, 0.445, 0.448, 0.589, 0.604, 0.611, φ ₁ 0.141, 0.438, 0.604, 0.611, φ ₁ 0.111, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.6511, 0.
10 spect (2850b); 05 scint spect (52M50b); . Is abs (66.550, 26M48b)		6. 2 2 spect (66C50); conv: 0.3, 1.2 spect conv (66C50)	β ⁺ : 2.0 spect (66C50); conv: 0.2, 0.9 spect conv (66C50)	p ⁺ : 1.7 spect (66C50); conv: 0.2, 0.8 spect conv (66C50)				0. 66 apect (88551a); 0. 65 apect (2.1.47); 0. 68 coinc abs (37W47); 0. 6 abs (26M48a, 24G47)
30.6 h (66C50); 1 31.9 h (24C47); 1 32.5 (13S4b); 1 30 h (12Z40)	-700 d (37 <u>1.51)</u>		41. 5 h (66C50)	3.2 h (66C50)	12.6 d (66C50); 10.7 d (24C47)		1.42 m (15H48a); 1.5 m (12M37)	74, 37 d (51K51); 74, 5 d (66C50)
p. (13541b)	[6] (37L50m) 700 d (37L51)	EC 99+%, 8 ⁺ 11.8 h (66C50) -0.2% (66C50)	EC 99+%, p+	6 (7)	EC (24G47)		IT (18G47a)	EC, B' (ICCSII); no b* (Imm 0, 008%) (41M51)
						38.5 (37536a)		
A n-capt (8K35, 12Z40); clem, n-capt (13S4b); chem, chem, chem, excit (23F48a, 116S52)	A chem, genet (37150a)	B chem, excit, sep isotopes (66C50)	B chem, excit, sep isotopes (66C50)	D chem, excit, sep isotopes (66C50)	B chem, excit (24G47); chem, excit, sep isotopes (66C50)		A n-capt (12M37); resonance neutron activation (18G47a)	A n-capt (12A36); mass spect (37846); chem (2W48a)

194

0.193

77lr |

1r 188

140 I

1,190

Ir 192m

161 21

14 192

	7	1	7 11 2		Freeze of rad	Freezes of radiation in Mey		Marked of sections
V Z	identification	abundance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
17 lr	B genet (52M50b)		IT (\$2M50b)	5.7 x 10 ⁻⁹ s delay coinc (52M50b)		0.065 scint spect, \$-y delay coinc (52M50b)	0,893	daughter Os ¹⁹³ (52M50b, 52M51)
							> 96%   Ir   193m     Ir   193m	
							(3/2+)	
1r 193		61. 5 (37536a)					Ir 193, I = 3/2 (99B50, 94E49)	
1 194 Ir	A n-capt (12A35); mass spect (37R46); chem (2W48a)		p ⁻ (12M37)	19. 0 h (24G47); 19. 5 h (53W41); 19 h (12A35, 12M37)	2.16 spect (\$3W41); 2.2 spect (24A36); 2.1 abs (53W41, 24G47); 0.5 β-γ coinc abs (26M48a)	γ ₁ 0.290, γ ₂ 0.326, γ ₃ 1.51 (γ ₁ /γ ₂ /γ ₃ = 1/5/1) spect (89B52); 0.328 spect conv (10C51f); 1. 7.2. 2 (0.145) Be. D·γ·n reaction (23 W50); onbers (BA9, 26M48s, 42C50, 33L5)		Ir-n-y (12435, IP37, 2547, 12447, 24438); Ir-d-p (24G47, 2W483); Pr-y-p, Pt-y-pn (25G52)
1r 195	D chem, excit (25C52)		p (25C52)	140 m (25C52, 65B52b)	1.8 abs (65B52b); -1 abs (25C52)	0.49, 0.84 scint spect (65B52b)		Pt -y-p (25C52); Pt-n-p (65B52b)
11 196	D chem, excit (65B52b)		p (65B52b)	9 d (65B52b)	-0.08 abs (65B52b)	y (65B52b)		Pt-n-p (65B52b)
1197	D chem, excit (25C52, 65B52b)		p ⁻ (65B52b)	7 m (25C52, 65B52b)	1.65, 0.6 abs (65B52b)	y (65B52b)		Pt-y-p (25C52); Pt-n-pn (65B52b)
1r 198	E excit (65B52b)		p^ (65B52b)	45 a (65B52b)	3.6 abs (65B52b)	0.78 scint spect (65B52b)		Pt-n-p (65B52b)
78Pt 190		0.012 (281.49a)						
161 A	B chem, excit (2W48a, 90M52)		EC (2W48a)	3.00 d (2W49c, 90M52)		0.083, 0.096, 0.173 spect (116552a); 0.6, 1.5 abs, abs corv (2W49c)		Ir-d-2n (2W48a, 2W49c); Pt-n-2n (2W48a, 2W49c); daughter Au ¹⁹¹ (2W48a,
Pt 192		0.78 (3147g)						75804
Pt 193m	B chem, excit (2W48a, 90M52)		IT (116552a); EC (2W48a)	4.33 d (2W49c) 4.6 d (90M52)		0.135 (K/L 0.28, L _I /L _{III} /L _{III} 1/0/2) spect conv (116552a); 0.2, 1.5 abs (2W49c)		Ir-d-2n (2W49c); Pr-n-y, Pt-n-2n, Pt-d-p (2W49c); Pt-y-n (11655.a);
¥61 K		32. 8 (3147g)					Pt ¹⁹⁴ , I = 0 (87M50)	daughter Au ¹⁷³ (2W49c, 90M52)

Pt-n-y (26M4Re, 79H52, 104S52, 12M37, 1937, 2547, 14H511, Pt-d-p (9K41b); Pt-y-n (4SC52); daughter Au ^{[45} (180 d) (104S52)			Pt-d-p (2854); Pt-n-2n (2854); Pt-y-n (60M4, 25C52); Hg-n-a (2854); Au-n-p (?) (286f)	Pt-n-y (IZM37, 28541, 2547, 79152); Pt-d-p (IOC36, 9K41b, 28541, 9K-42, 2W4R4); Pt-y-n (255-62, 25W4R); Pt-n-a (28541); Hg-n-a (28541)		Pt-n-y (12A35, 77M35b, 12M37, 28541, 2547, 50H51); Pt-d-p (28541, 9K41b, 10C36) Hg-n-a (28541)	Pt-n-y (10C50g)	epall Pt (42R52), Au (3T49, 42R52)	Ir-a-4n (2W49c); Pr-d-3n (2W49c); parent Pt ¹⁹ ! (2W48a, 2W49c, 90M52); daughter Hg ^{19!} (90M52)
(3/2-) P1995m 0.255 (3/2+) Au 95 (3/2-) EC (3/2-) (3/2-)	((72-) (104552) (104552) Pt 195, 1 = 1/2 (87M50)	-		10/2 -) P1/97 HS 197 (10/552) (10/2 -) P1/97 (10/552) (10/2 -) P1/97 (10/2 -) P1/	(268601)				
0.029 (e/y >7. 5), 0.097 (e/y 9.0, K/L 5.7), 0.126, 0.129 (e/y very large, K/L 0.26) spect, spect conv. y-conv colne. (0.052a); (0.052a); (0.052a); (0.15 (K/L 0.2)) spect conv. (15 (K			0.337 (e/y very large, K/L 1.3) spect conv (15H48a)	0 077, 0 191 (K/L 6.0) spect conv (10G52a); 0 191 spect, spect conv (10555z); others (4849)			0.6 abs (10C50g)		0.053, 0.064, 0.111, 0.123, 0.166, 0.250, 0.405 spect conv (90M52)
				0 670 spect (105552, 34451); 0. 7 abs (9K41b, 28541)		l. 8 abs (9K4lb, 28S4l)	0.5 abs (10C50g)	a: 5.07 ion ch (42R52)	
3.5 d (15H48a); 3.8 d (104552); 4. d d (79H52); 3.3 d (12M37)			78 m (15H48a); 80 m (28S41); 88 m (25C52)	18 h (12M37); 17.4 h (10C52a)		31 m (12M37)	82 d (10C50g)	4. 3 m (42R52)	18 h (90M52); -1 d (2W49c)
17 (104552)			IT (15H48a)	6 ⁻ (12M37)		p ⁻ (12M37)	p ⁻ (10C50g)	EC, p ⁺ , a -0.01% (3T49)	EC (2W49c)
	33.7 (3147g)	25. 4 (3147g)			7. 23 (3147g)				
B chem (12M37); chem, genet (104552)			B chem (28541); chem, excit, cross bomb (25C52)	A chem (10C36); chem, excit (12M37)		A n-capt (77M35b, 12A35); chem, n-capt, excit (28S41)	F n-capt (10C50g)	D chem, excit (3T49)	B chem, genet (2W49c, 90M52)
Pt ¹⁹⁵ m	Pt 195	P. 196	P. 197m	Pt 197	Pt 198	P. 199	ď.	183 -	161 nV

1	Clear and	Percent	Type of		Energy of rad	Energy of radiation in Mev		Method of penduction and
V Z	identification	abundance	decay	Half-life	Particles	Gamma-transitions	Distance ration energy and scheme	genetic relationships
26 nV 62	B chem, excit (2W49c); chem, genet (42T52,33F52)		EC, p [†] (2W49c)	5. 0 h (42T52); 4. 7 h (2W49c); 4. 1 h (33F52)	β ⁺ : -1.9 aos (2W49c); conv: -0.4 abs (2W49c)	2-3 abs (2W49c)		Ir-a-3n (2W49c); Pr-d-2n (2W49c); daughter Hg ¹⁹² (33F52, 42T52)
۳۷ مر	B chem, genet (2W49c, 90M52)		EC (2W49c)	15.8 h (2W49c, 90M52); 15.3 h (33F52)		0.051, 0.060, 0.084, 0.093, 0.109, 0.165, 0.177, 0.235 spect conv (90M52)		!r-a-2n (2W49c); Pt-d-n, Pt-d-3n (2W49c); parent Pt ¹⁹³ (2W49c, 90M52); daughter Hg ¹⁹³ (33F52, 90M52)
<b>7</b> 61 ¹³ ₹	B chem, excit (2W49c)		EC -97%, p ⁺ -3% (2W49c)	39. 5 h (2W49c) 39 h (82S49)	39. 5 h (2W49ck 1.8 abs (2W49c) 39 h (82549)	0.291 (e/y 0.054, K/L 2), 0.328 (e/y 0.19, K/L 2), 0.466 (weak), 1.48 (e/y 0.0026), 2.1 apect, apect conv (82549)		Ir-a-3n (2W49c); Pt-d-2n, Pt-d-3n (2W49c); Pt-p-n (82549)
Au 195m	B chem, genet (34H52a)		IT (34H524)	0.5 m (34H52a)		0.056, 0.259 spect conv (34H52a)		daughter Hg ^{195m} (34H52a)
Au 195	B chem, excit (2W49c); chem, genet (30D52)		EC (2W49c)	180 d (82549, 30D52); 185 d (2W49c)		0.0108, 0.0990, 0.130 spect conv (10D52), 0.29 (L/M 4.6), 0.097 (K/L.5.8), 0.26 spect, spect conv, y-conv coinc (10452); others (34H51, 82549)	aee pt195m	Ir-a-2n (2W49c); Pt-d-n, Pt-d-2n, Pt-d-3n (2W49c); Pt-p-n (82549); daughter Hg ^{195m} (30D52)
<b>V</b> n 196	B chem, excit (12M37)		EC or IT (2W49c)	14.0 h (2W49c); 13 h (12M37)			90	Au-n-2n (12M37, 2W49c); spall U (?) (6F51)
96 ₁ 78	A chem, excit (12M37)		EC -95%, p -5%, p -5%, p -5%, p -5%, p -20%, p -20%	5. 55 d (2W49ck 5. 60 d (82549)	p: . 0.27 spect (106552); 0.30 spect (82549); 0.34 abs (2W49c)	with EC: 0 312, 0 354 spect conv (106552); 0 310 (K/L 1. 7), 0 356 (K/L 1. 7) a pect conv (82549); 0 426 (a_/Y 0. 007, L/M+N 3. 5), no 0.175 y spect conv, \$conv coinc (106552); 0.75 spect conv (82549)	(E) Au 190 (C) Au	Pt-d-n (9K41b, 2W49c, 106552); Pt-p-n (82549); Au-n-Zh (12M3), 2W49c); Au-y-n (128W48); epail U (?) (6F51)
Au 197m	A excit (37W45a)		IT (37W45a)	7. 4 a (40F47); 7. 5 a (37W45a)		0.130 (e _K /y & 2.0, K/L/M = 1/7.5/ 3.6), 0.279 (e _K /y -0.3) spect conv (53M52c); 0.273 spect conv, conv-conv coinc 0.275 scint spect (24C52); 0.25 scint spect (24C52);	(04) 00652, 82552, HPS) (10,6552, 82552, HPS) (11,72-) Au 197m (11,72-) Au 197m (13,72+) 0.279 (33,72+) 0.279 (63,852c, HPS)	Au-y-y (37W45a); Au-n-n (37W45a,40F47); daughter 25 h Hg ¹⁹⁷ (40F47)
Au 197		100 (10354)					Au ¹⁹⁷ , 1 = 3/2 (87M50)	

V 198				Au 202,204
(12A35, 12M37)	A chem, genet (12M37)	B chem (28541); chem, sep inctopes, excit (65B52a)	B chem, excit, sep isotopes (65B50, 65B52s)	E excit (65B52a)
p (12M37); 0. EC (11m 0. 24) (38M42); 0. 44, 0. 44, 0. 003%; (41M51) (41M51)	ρ [*] (9K41b)	p (28541)	β (65B52a)	p or IT (65B52a)
2.69 d (57849, 9549b); 373 d (18851, 37046); 2.66 d (69C51)	3.15 d (8BS2b); 3.2 d (104552); 3.3 d (12M37)	48 m (65B52a. 28S41)	26 m (65B52a)	25 a (65B52a)
b, 0, 963 spect (average of 9548, 2149a, 10149, 82549, 107549, 62 4 £5); 62 0 Coinc with 0, 680 y) 62 y coinc spect (4851a); 63 1, 37 (0, 01%) spect (4E5)	0 460, 0 297 (coinc with 0 158 y), 0 250 (coinc with 0 207 y) 8-y aper (coinc (8824), -0.47 \$\tilde{p}\$ find coinc with \$\tilde{p}\$ for \$\tilde{p}\$ fo	2. 2 abs (65B52a); -2. 5 abs (28S41)	l. 5 abs (65B52a)	
10 - 4117 cryst spect (100M52, 34D81); 11 (c. 416 perct (29L51); 12 (c. 416 perct (29L51); 13 (c. 416 perct (29L51); 14 (c. 47 0 031, K/L 3 1, L/M 3 3); 15 (c. 47 0 031, K/L 3 1, L/M 3 3); 16 (c. 47 0 032, K/L 3 1, L/M 4 3); 16 (c. 47 0 029, K/L 2 1, L/M 4 3); 17 (c. 47 0 029, K/L 2 2, L/M 4 3); 18 perct conv (10S491); 19 (c. 47 0 0 03); K/L+M 2 3); 19 perct conv (10S491); 11 (c. 47 0 0 03); K/L+M 2 3); 11 (c. 47 0 0 03); K/L+M 2 3); 12 (c. 47 0 0 03); K/L+M 2 3); 13 perct conv (10S491); 14 (c. 47 0 0 03); K/L+M 2 3); 15 (c. 47 0 0 03); K/L+M 2 3); 16 (c. 51 3); 17 (c. 51 3); 18 (c. 57 3); 18 (c. 67 3); 18 (c.		1.13, 0.39 scint spect (65B52a)	0.55 acint spect (65B52a)	
(3-)-4(1PS) (3-)-4(1PS) (3-)-4(1PS) (0+)-(1PS) (1PS)	Gp 0.46 (HPS)  Gp 0.46 (HPS)  (32-) Au 199 (1324) Hq 199m2  (32-) Hq 199m   H 0.159  (32-) Hq 199m   H 0.159  (32-) Hq 199m   H 0.159  (172-) Hq 199m   H 0.159			
Au-n-y (12A35, 12M37, 1937, 16D41, 2547, 50H5)); Au-d-p (9441); Pr-p-n (#2544); Pr-p-n (#2548); ppall U (6O48)	Pt.d.n (9K4lb); Au.n.y (second order rescrion) (67150a); Hg.np (2854); daughter Pt.199 (12M37,86B49a, 37M49, 67150); parent Hg 19m1 (14C51a,8B52a)	Hg-n-p (28541, 3M42); Hg ²⁰¹ -y-p (65B52a); T1-n-a (3M42)	Hg-y-p (65B50); Hg ²⁰² -y-p (65B52a)	Hg-n-p (65B52a)

7.5	<b>'</b> . 1	1.2				2						REACTOR PHYSICS
Method of production and	genetic relationships	Hg-n-pn (65B52a); Hg ²⁰⁴ -y-p (65B52a)	spall Au (3T49)	spall Au (42T52)	opall Au (42T52)	spall Au, parent Au 191 (90M52)	epail Au (90M52, 33F52); parent Au ¹⁹² (33F52, 42T52)	Au-p-5n (33F52, 90M52); parent Au ¹⁹³ (33F52, 90M52)	Au-d-4n (34H52a); Au-p-3n (30D52, 33F52); parent Au ^{l95} (30D52); parent Au ^{l95m} (34H52a)	Au-p-3n (30D52)		P-a-n (2864); Au-d-n (16W4); 25F43); Hg-n-2n (12M37, 23F4); Hg-n-y (17356, 16W4), 23F43); Hg-a-y (17356, 16W4); Hg-a-p (9K40); parent (3%) Au ¹ 97m (40F50, 10452); parent Hg ^{197m} (20D50, 32M50c)
	Dannegration energy and waster											10.13.2 Hq 197m 10.13.3 Hq 197
Energy of radiation in Mev	Gamma-transitions	0. 69 acint apact (65B52a)		•			1.4 abs (33F52)		0.036, 0.056 (coinc with Au 195m), 0.122, 0.259 (coinc with Au 195m) apect conv (34452a); 0.037, 0.056, 0.122 (conv in Hg), 0.206, 0.261, 0.318, 0.558 apect conv (30D52)	0.061, 0.179, 0.600, 0.780 spect conv (90M52); 0.061, 0.179 spect conv (34H52a)		with II: 0.131 (4/4 0.5), K/L/M4N = 1.0/2.4/0.8), 0.164 (eg/4.6), K/L/M4N = 1.0/2.3/1.2) apect comy. yr coinc (60°F60.3491); 0.134 (KL/L col.), 0.165 (K/L 0.134 (LL/L)/L LIII = 0.05/1.1/1.0 0.165 (LL/L/L)/L LIII = 0.05/1.1/1.0 0.165 (LL/L/L)/L LIII = 0.05/1.1/1.0 0.191 (eg/y - 1.7, K/L - 6), 0.275 (weak, eg/y - 0.5, K/L - 5) apect comy (63M52c); with EC: 0.191 (eg/y - 1.7, K/L - 6), 0.275 (weak, eg/y - 0.5, K/L - 5) apect comy (63M52c); 0.191 (eg/y - 1.7, K/L - 6), 0.275 (weak, eg/y - 0.5, K/L - 5) apect comy (63M52c); 0.191 (eg/y - 1.7, K/L - 6), 0.275 (weak, eg/y - 0.5, K/L - 5) apect comy (63M52c);
Energy of ra	Particles	l. 9 abs (65B52a)	a: 5.60 ion ch (42R52)				l. 18 spect (33F52)					
	Half-life	55 e (65B52e)	0.7 m (42R52)	30 m (42T52)	90 m (42T52)	12.4 h (90M52)	5.7 h (33F52); 8.4 h (90M52)	10. 0 h (33F52); 14. 5 h (?), 29. 0 h (?) (90M52)	38 h (30D52); -31 h (33F52); 40 h (34H52a)	9.5 h (30D52, 34H52a)		23 h (23F43, 34H5)); 25 h (12M37)
Type of	decay	p [*] (65 <b>B</b> 52a)	a (3T49)			EC (90M52)	EC (90M52); p+ (33F52)	EC (33F52)	EC, 1T (30D52)	EC (30D52)		17 97%, EC 3% (104852)
Percent	abundance										0.146 (6N50a)	
7.0	identification	B chem, excit, aep isotopes (65B\$2a)	E chem (3T49)	D chem, excit (42T52)	D chem, excit (42T52)	D chem, excit (90M52)	D chem, excit (33F52,90M52)	B chem, excit (33F52, 90M52)	B chem, excit (30D52, 33F52)	B chem, excit (30D52)		A n-capt (17A36a); chem (12A37); chem, extit, cross bomb (16W41, 23F43)
1	Z V	79 <b>^u</b> 203	80 ^{Hg}	Hg 189	Hg 190	161 H	H <b>g</b> 192	H <b>g</b> 193	80 ^H g	195 Hg	961 BH	H 8 1979

daughter Hg	Au-d-2n (23F43, 16W41); Hg-n-y (23F43, 16W41); Hg-n-y (23F43, 16W41)	Pr-a-n (28541); Hg-n-c (12M3, 1P37, 6H37, 6F3949); Hg-n-123743, 16 W41, 67B49b); Hg-q-n (60448, 37W45a); Hg-y-n (16W41) daughter Au ¹⁹⁹ (14G51a,8B52a)	
(63M52c, .J4S52, HPS)		Hg ¹⁹⁸ , I = 0 (87M50)  see Au ¹⁹⁹ , TI ¹⁹⁹ (3A2-) Au ¹⁹⁹ (13A2-) Hg ¹⁹⁹ (3A2-) Hg ¹⁹⁹ (14A2-) (15A2-) (14A2-) (	Hg ¹⁹⁹ , I = 1/2 (87M50) Hg ²⁰⁰ , I = 0 (87M50) Hg ²⁰¹ , I = 3/2 (87M50) Hg ²⁰² , I = 0 (87M50)
0 13 scint spect (20050)	0.077 (e _L /y 2.5, L/M 3.6), 0.191 (e _K /y -1.7, K/L -6) spect conv, yy coinc (34H51, 40F50); 0.077 (L _I /L _I III = 1.0/0.45/ 0.34) spect conv (63M52c); 0.078 (L _I /M 4), 0.191 (K/L -9) spect conv (1052b); 0.077, 0.278 spect conv (30D52); others (2H42a, 40F47, 34H48a)	0.155 (e/y 0.25, K/L < 0.4), 0.368 (e/y 20, K/L 1.6) spect conv (15448a); 0.159 (L _{II} /L _{III} 1.6) spect conv (63462a); 0.16 y (coinc with 0.37 y) scint spect, y y coinc (1133); others (1547a, 37449) 0.158 spect conv, 6 y coinc (14GS1a, 8BS2a)	

Hg 197m1 A ge	Hg 197 A ch	Hg 198 Hg 99m2 A ch m m	Hg ^{199m} l A ge	199 H	Hg 200	Hg 201	Hg 202
genet (52M50c. 20D50)	chem, excit, cross bomb (16 W41, 23F43)	chem, excit (6437, 12M37); (67849b)	genet (14G51a)				
		10. 02 (6N5 0æ)		16. 84 (6N50 ₈ )	23.13 (6N50a)	13. 22 (6N50a)	29. 80 (6N50a)
IT (52M50c, 20D50)	EC (23F43)	IT (23F43)	IT (14G5la)				
7.0 x 10 ⁻⁹ a delay coinc (\$2.M\$50;); 8 x 10 ⁻⁹ a delay coinc (20D\$0)	65 h (34H51); 66 h (10C52b); 64 h (23F43)	44 m (15H47a, 60M48); 43 m (12M37, 6H37)	2.4 x 10 ⁻⁹ s delay coinc (8B52a)				

lactope Z	Class and identification	Percent	Type of decay	Half-life	Energy of rad	Energy of radiation in Mer	Disintegration energy and acheme	Method of production and
80 Hg 203	A excit (9K40); chem, excit, 2.3F43); mass spect (5S49a, 6TB49a)		p (23F43)	47.94 (10C52b); (30 94 (31 94); (31 54); (31 54); (35 48) (9548b)	0. 208 ft-y coinc spect (5549, 5549s); 0. 210 spect (13785ls); 0. 205 spect (554b); others (17W47)	0. 279 (e/y 0. 27, K/L 3) spect, spect conv, 6-y coinc (5549, 2549, 12450); 0. 278 (e/y 0. 19, K/L+M 3. 7) spect, spect conv (3) W51a); 0. 278 (K/L 0.) spect conv (10452); 0. 279 (K/L -10) spect conv (1052b); 0. 286 (e/y 0. 3, K/L 3) spect conv (1052b); 0. 286 (e/y 0. 3, K/L 3) spect conv (1052b); 0. 286 (e/y 0. 3, K/L 3) spect conv (1052b); 0. 286 (e/y 0. 3, K/L 3) spect conv (1052b); 0. 286 (e/y 0. 3, K/L 3) spect conv (1052b);	(1,24) (1,24) (1,24) (1,24) (1,24) (1,24) (1,24) (1,24) (1,24) (1,24)	Hg.n.y (23F43, 16W41, 3147h, 2547); Hg.n.c. n (6W41), 2864t, 23F43); Hg.d.p. (78L51a); Tl.n.p (3M42)
Hg 204		6.85 (6N50a)					Hg ²⁰⁴ , I = 0 (87M50)	
H ₈ 205	A n-capt, excit (9K40, 9K42); sep isotopes, n-capt (35L5ia)		6 (9K40)	5.5 m (3M42, 9K40); 5.6 m (35L5la)	1.8 abs (351.5]a); 1.6 abs (9K40)			Hg-d-p (9K40, 9K42); Hg-n-y (23F43, 16W41, 2547); Hg204-n-y (35L51a); TI-n-p (3M42); Pb-n-a (3M42)
81 T1198	B chem, excit (7049)		EC (7049)	1. 8 h (7049)	com: -0.4 abs (7049)	several y's, abs (7049)		Au-a-3n (7049); daughter Pb ¹⁹⁸ (4N50)
71199	A chem (9K40); chem, excit (7C44); genet (energy levels Hg199) (1153)		EC (7049); no p* (1151)	7 h (7049)		0.049, 0.078, 0.103, 0.157, 0.206, 0.245, 0.332, 0.454, 0.490 apect conv. Y-Y coinc (1151, 1153)	8.4\$1 T1 199	Au-a-2n (7049, 1151); Hg-d-2n (9K40); daughter Pb ¹⁹⁹ (4N50)
T1 200	A chem, excit (7049)		EC (7049); no p* (1151)	27 h (7049)		0.365, 0.577, 0.622, 0.829, 1.210, 1.360 spect conv (1151); -0.4, 1.6 abs (4N50)		Au-a-n (7049, 1151); Hg-d-2n (9K40); daughter Pb ²⁰⁰ (4N50)
T1 ²⁰¹	B chem, excit, crose bomb (4N50)		EC (4N50)	72 h (4N50)		0, 210 spect comv, abs (4N50)		Au-a-y (112551); Hg-d-2n (9K40); daughter Pb ²⁰¹ (4N50)
T1202	A chem, excit (9K40, 5F41)		EC (9K40, 3M42); EC (L/K-1), no p ⁺ or p ⁻ (2W50)	12. 5 d (80M52); 11. 5 d (2W50); 11. 8 d (5F41)		0, 435 spect conv, abs (2W50); 0, 431 scint spect (80M52)		Hgd-Zn (9K40, 2W50); Tl.nZn (9K40, 5F41, 3M42, B0M52)

NUCLEAR PHYSICS		CHAP. 1.2
	_	

NU	CLEAR PH	TY8IC						C	HAP.	1.2
	Tl-n-y (5F40, 2547); Tl-y-n (7H49); Tl-d-p (9K40, 5F41)		Ti.n.y (4P35, IP37, 6H37); T1205-n.y (4N50a); T1-d-p (5F40, 9K40); daughter Bi ²¹⁰ (RaE) (7B47); (4N50a)	Pb-n-p (6B40); Pb-y-p (10B46); natural source, daughter Bi (AcC)	natural source. daughter Bi212 (ThC)	daughter Bi ²¹³ parent Pb ²⁰⁹ (4H47, 11E47)	natural source, daughter Bi ²¹⁴ (RaC), pareni Pb ²¹⁰ (RaD)	T1-p-6n (7K51); parent T1 ¹⁹⁸ (7K51, 4N50); daughter Bi ¹⁹⁸ (4N50)	daughter B199, parent T1199 (4N50)	daughter Bi ²⁰⁰ , parent Ti ²⁰⁰ (4N50)
T1 ²⁰³ , I = 1/2 (87M50)	Q ₆ 0. 77 (13853)	T1 ²⁰⁵ , I = 1/2 (87M50)	O' 1. 51 (13A51)	Q ₆ 1.44 (13S53)	06 4 99 (13553)  71208  1208  (24)  (04)  (04)  (04)	Q 3. 92 calc (13553)	Q <b>p</b> 5.39 calc (13553)			
	no y (lim 0, 01%) (38MS2a); no y (lim 0, 5%) (6E50); no y (5F41); Hg K-x (33L52, 14MS2a)		no y (5£40, 7847, 13A51)	0.870 (-0.5%) (11541)	2. 62 (-100%, e'y-0 002), 0 889 (-15%, e'y-0 02), 0 582 (-80%, e'y-0 02), 0 582 (-80%, e'y-0 02), 0 582 (-80%, e'y-0 02), 0 510 (-25%, e'y-0 02), 0 277 (-10%, e'y-0 ) apect. (491.5); 2 6143 apect (491.5); 2 6143 apect (491.5); 2 6143 apect (491.5); 2 6154 apect (1085); 2 615 apect (1085); 2 615 apect (1085); 2 615 apect (1247); 2 62, 0 582, 0 510, 0 277 apect (-000% (87.3); 2 62, 0 582, 0 510, 0 572 apect (-000% (87.3); 2 62, 0 884, 0 581, 0 502 apect (-10.5); 0 512	0.12 scint spect (39W53)	no y >2. 8, D-y-p reaction (9850)			0.139, 0.320 spect conv (8O51)
	0. 765 apect (33L52); 0. 760 actin apect (38M52); 0. 78 apect (9543); 0. 77 apect (6P47); others (4H47a, 5F41, 6E50)		1. 51 spect (13.451); 1. 65 abs (5F41); 1. 8 abs (9K40); no conv (13.451)	1. 44 abs (6E50); 1. 47 abs (3S39a); 1. 6 abs (6L38)	1. 792 spect (6M48); 4. 795 spect (14H4); 1. 805 spect, f. y. coinc (4F48); 1. 72 spect (7547); 1. 82 abs (3533); f. 21, 792 (7) (4/%) spect (6M48)	1. 99 spect (39W53); 1. 8 abs (4H50)	l. 8 cl ch (6L38); 2. 0 abs (8D37)			
	3. 5 y (5F41); 2. 7 y (3V45)		4.19 m (3552); 4.23 m (5F40); 4.3 m (13A51)	4. 79 m (3552); 4. 77 m (5F40); 4. 76 m (1C31, 3S39)	3.1 m (IC31)	2. 2 m (4H50)	1, 32 m (1C31); 1, 5 m (9B50); -1, 3 m (8D37)	25 m (7K51)	-80 m (4N50)	18 h (4N50)
	6 - 98%, EC - 2% (33L52); 6 - 98.5%, EC - 1.5% (38M52)		p (5F40, 9K42)	<b>'</b> a	'a	p (4H50)	<b>'</b> &	EC (7KS1)	EC (4N50)	EC (4N50)
29. 50 (1B50)		70. 50 (1B50)								
	B chem, n-capt (5F40)		A n-capt (4P35); chem, genet (7B47); excit, sep isotopes (4N50a)	A chem, genet (IC31)	A chem, genet (IC31)	A chem, genet (4H50)	A chem, gener	B chem, genet (7K51)	B chem, genet (4N50)	A chem, genet (4N50)
T1203	T1 204	T1 205	T1206	T1 ²⁰⁷	T1 ²⁰⁸	T1209	T1 ²¹⁰	82Pb ¹⁹⁸	Pb 199	Pb 200

		Percent	Type of		Energy of rac	Energy of radiation in Mev		Method of production and
Z A	identification	abundance	decay	Half-life	Particles	Gamma-transitions	Distintegration energy and scheme	genetic relationships
82 Pb 201m	D chem, excit (89H52)		IT (89H52)	50 . (89H52)		0.25, 0.42, 0.67 scint spect (89H52)		T1-p-3n (89H52)
Pb 201	<b>a</b>		EC (4N50)	8 h (4N50)				T1-d-4n (5H46); daughter Bi ²⁰¹ , parent T1 ²⁰¹ (4N50)
Pb 202m	E excit (89H52)		IT (89H52)	5.6 • (89H52)		0. 89 scint spect (89H52)		T1-p-2n (89H52)
Pb 202		<4 x 10 ⁻⁴ (9D49)		>500 y genet, yield (2T47, 4N50)				T1-d (2T47)
Pb ²⁰³	B chem, excit (3M42): chem, excit, cross bomb (2T47)		EC (3M42, 8051)	52 h (5F40, 2T47); 54 h (9K40, 12D42)		0.153, 0.269, 0.422 spect conv (8051); 0.270, 0.420 abs conv (3M42); 0.270, -0.470 spect, spect conv (9L44)	*** Hg ²⁰³ Pp ²⁰³ EC	TI-d-2n (5F40, 9K40, 5F41, 2T47); TI-p-n (12D42); Pb-n-2n (3M42); Pb-204-n-2n (10B46)
							0153 07	
P6 ^{204m} 2	B chem (5F41); chem, excit, genet (2T47, 7K51)		IT (3M42)	68 m (3M42); 65 m (5F41)		0. 905 (e/y - 0.1, K/L.1.5), 0. 374 (with Pb. ^{204m1} , e/y - 0.05, K/L. 2. 1) spect conv., abs conv. abs (1450), 0. 9 abs conv. abs (574) 1. 1 abs conv., abs (574)	*** B ₁ Z04 (805)	11-d-n (5F41); 11-d-3n (2T41); Pb-n-n (7D39, 3M42); Pb-y-n (10B4), 2147, 14550, 445, (2T47);
							(2+) Pb ^{2O4m} , O.374	parent Pb************************************
рр 204ш	B genet (14850)		IT (14850)	3 x 10 ⁻⁷ a delay coinc (14S50)		0.374 (see y's of Pb ^{204m} 2)	(0+) 0 (18652)	daughter Pb ^{204m} 2 (14S50); daughter Bi ²⁰⁴ (14S5b)
Pb 204		1. 48 (6N38)					Pb ²⁰⁴ , I = 0 (87M50)	
Pb 206		23.6 (6N38)					Pb ²⁰⁶ , I = 0 (87M50)	

Pb.207.n.n (24U31); Pb.n.n (31L51); daughter Bi. ²⁰⁷ (23F52c); not daughter Po. ²¹¹ (11m 0.005%) (23F52a)			•	Pb-d-p (6737, 9840, 5F41, 5F41a, 9842, 3H50); Pb-n+y (3M42); Bi-d-2p (11555); Bi-n-p (3M42); daugher po 213 (4H47, 11E47, 11M49); daugher TI ²⁰⁹ (11E47, 4H47)	natural source, daughter T1210 (RaC''), daughter Po-214 (RaC'), parent Bi210 (RaE)	natural source, daughter Po ^{21‡} (AcA), parent Bl ²¹ ! (AcC)
113/2 +) Pb207m	(5/2-) (1/2-) (18652)	Pb ²⁰⁷ , I = 1/2 (87M50)	Pb ²⁰⁸ , I = 0 (87M50)	Op 0. 64 (13553)	Qp 0.065 (\$152) PD 210 PD 200	0p 1.4 (13553) PP 2!!
0.55, 1.05 acint spect (24C51); 0.5, 1.1 acint spect (23F52c)				no y, no conv (4W44, 47W52a); no y (19L44, 39W53)	γ ₁ 0. 0465, no other γ between 0.016 and 0.060 (lim - 2% of γ ₁ ) cryst spect (26252); γ ₁ 0.0467, no other γ (lim 5% of γ ₁ ) cryst spect (88852); 0.0467 (3.5%) spect conv. abs (2480, 8331, 19532, 6033); γ ₁ (ε/γ - 16. Lr/Lr/Lr/Lr/Lr/Lr/Lr/Lr/Lr/Lr/V-16. Lr/Lr/Lr/Lr/Lr/M = 1.0.0.09/0.019/0.29) spect conv (6550); γ ₁ (ε/γ - 17, using γ = 3.5%) spect conv (14851); γ ₁ (ε/γ - 17, using γ = 3.5%) spect conv (14851); 0.037, 0.0467 cryst spect (852); 0.037, 0.0467 cryst spect (852); 0.037 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.031 (0.2%), 0.	0.065, 0.083, 0.404, 0.425, 0.487, 0.764, 0.829 spect, spect conv. abs [11542]; 0.829 (5%) (54M44); 0.8 abs (5839a)
				0. 635 spect (47W52a); 0. 620 spect (39W53); 0. 68 spect (11R47); others (9K40, 5F4), 19L44)	0. 018 ion ch (5152); 0. 018 arist spect, \$\rho_T\$ coinc (67852a); 0. 017 (570%), 0. 056 (\$10%) ion ch (33152); others (\$1.39, 12546)	(3839a)
0.84 s (24C52); 0.82 s (51L51); 0.80 s (89H52)				44 3. 22 h (5F4)); 2. 75 h (9K40)	22 y (1C31)	36. 0 m (IC31)
IT (24C50)				p (9K40, 5F41)	'a	'a
		22. 6 (6N38)	52.3 (6N38)			
A excit, sep isotopes (24C51); chem, genet (23F52c)				A chem (6T37, 9K40); chem, eep isotopes (5F4la)	A chem, genet (1031)	A chem, genet (1C31)
Ph 207m		Pb 207	Pb 208	Pb 209	Pb210 (RaD)	Pb ²¹¹

Isotope	Class and	Percent	Type of	Half.life	Energy of radiation in Mer	ation in Mer	The state of the s	Method of production and
V Z	identification	abundance	decay		Particles	Gamma-transitions	District and Charles and Expense	genetic relationships
812 pp 212	A chem, genet (IC31)		'a	10. <b>6</b> h (IC31)	0.355, 0.569 spect, B-v coinc (1974, 0.569 (-12%) spect (2.340 spect (6624)) 0.340 spect (3533)	γ ₃ 0. 2386 spect conv (49151); γ ₁ 0. 112, γ ₂ 0. 176, γ ₃ 0. 128, γ ₄ 0. 249, γ ₅ 0. 299 spect conv (EE23); γ ₃ (1./L ₁ 1. 18, γ ₄ 0. 130 (-4%) γ ₃ (1./L ₁ 1. 18, γ ₄ (1. 1. 3) spect conv (11552); γ ₃ (1. 7. 1), γ ₅ (1. 7. 0. 3) (calc from 9739, 6448a, 6450); γ ₃ 0. 238 spect (7544)	G _p 0.58 (13553) Pp 2/2 P 2	natural source, daughter, parent Bi 212 (ThG), parent Bi 212 (ThG)
Pb.214	A cham, genet (IC31)		p. (3533, 7R346)	p* (15533, 7R36) &6. 8 m (1C31)	0. 65 spect (8C41)	γ 0. 05323, γ2 0. 24192, γ ₄ 0. 29522, γ ₅ 0. 35199 (γ ₂ /γ ₄ /γ ₅ = 0.2.05 55/1.0) (σ. γγε a speci (100M5.5); γ ₄ 0. 2410, γ ₃ 0. 2510, γ ₄ 0. 2528, γ ₄ 0. 2410, γ ₃ 0. 2528, γ ₄ 0. 4210, γ ₃ 0. 2529, γ ₄ 0. 3410, γ ₄ (K/L ₁ - 6. 7); γ ₄ (K/L ₁ - 6. 7); γ ₄ (K/L ₁ - 6. 7); γ ₅ (K/L ₁ - 6. 7); γ ₄ (K/L ₁ - 6. 7); γ ₅ (K/L ₁ - 6. 7); γ ₆ (K/L ₁ - 6. 7); γ ₇ (K/L ₁ -		natural source, daughter Po ²¹⁸ (RaA), parent Bi ²¹⁴ (RaC)
8.3Pi	E (2T48); chem (4N50)		a (2T48)	1.7 m (4N50)	6. 2 ion ch (4N50)			epail Pb (2T48, 4N50)
Bi 198	B chem (2T48); chem, genet (4N50)		EC 99+%, a 5 x 10 ⁻² % (4N50)	7 m genet (4N50)	5. 83 ion ch (4N50)			epail Pb (2T48, 4N50): parent Pb ¹⁹⁸ (4N50)
Bi 199	B chem (2T48); chem, genet (4N50)		EC 99+%, a 10-2% (4N50)	-25 m genet (4N50)	5.47 ion ch, abs mica (4N50)			spall Pb (4N50, 2T48); parent Pb ¹⁹⁹ (4N50)
Bi 200	B chem, genet (4N50)		EC (4N50)	35 m genet (4N50)				spall Pb. parent Pb 200 (4N50)
Bi ²⁰¹	B chem (2T48); chem, genet (4N50)		EC 99+%, a 3 x 10-3% (4N50)	62 m (4N50)	5. 15 ion ch (4N50)			spall Pb (2T48, 4N50); parent Pb ²⁰¹ (4N50)

NUCLEA	A Ph	15105			CHA
epail Pb, parent Pb ^{20]} (4NS0) daughter Po ²⁰² (7KS1)	epail Pb. parent Pb ²⁰³ (4N50); daughter Po ²⁰³ (7K51)	Pb 204 d . 2n (2T47); Pb-d-2n (14550); daughter Po 204 (7K51); Tl-a-3n, parent (-4%) Pb 204m 2 (2T47); parent Pb 204m1 (14552b)	daughter Po ²⁰⁵ (7K51). daughter At ²⁰⁹ (12B51)	T1-a-3n (2747); Pb-d-2n (5F41, 5F41a, 9K40, 13A51a); Pb 207-d-3n (2747); Pb 206-d-2n (5F41a); daughter pp 206 (2747a); dangher pp 206 (2747a);	
		Bi ²⁰⁴ (17.) Pb ^{204m} (18.) (18.) (18.) (18.) (18.)		 	18-207 (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2) (18-20-2)
		0. 217 spect conv (14550a)	0.431, 0 527, 0.550, 0.746, 1.84 spect conv (7K51)	0 182, 0 234, 0,260, 0 341, 0 196, 0 196, 0 196, 0 196, 0 889, 0 889, 1 1020, 1 097, 1 720 spect, spect conv. y-y-conc (13A51a); others (9K40, 5F41, 2T47a)	0.56, 1 1 (coinc with 0.56 y)  start spect, y-y coinc (7G51s); 0.66 or 0.137, 0.565, 1.063, 1.46, 2.05, 2.20, 2.33, 2.49  spect coinc (4N51); with pb.207m; 0.5, 1.1 start spect (23F52c)
	a: 4.85 range emuls (15D52a)	солу: -0.2, -0.8 (weak), abs, spect (2T41)			
-2 h genet (4N50) 95 m (7K51)	12 h genet (4N50)	12 h (2T47)	14. 5 d (7K51)	6. 4 d (9K40)	- 50 y genet (4N51)
EC (4N50)	EC (4N50); a -10-5% (15D52a)	EC, no p* (2147)	EC (7K51)	EC (9144); EC, no pt (13A51a)	EC (5G50,
B chem. genet (4N50) B chem. genet (7K51)	B chem, genet (4N50)	B chem, sep isotopes, cross bomb (ZT47)	B chem, genet, sep isotopes (7K51)	B chem. sep isotopes (5F41s, 2T47)	B chem. genet
B ₁ ²⁰¹ B ₁ ²⁰²	Bi 203	Bi 204	Bi ²⁰⁵	Bi 206	Bi 207

1	7	Berra	Twend		Energy of rad	Energy of radiation in Mey		Method of production and
Z V	identification	spandance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
83 Bi 208	F chem (4N51)		EC (4N51)	long (4N51)		no y (?) (4N51)	Qa 3. 2 calc (13S53)	Pb-d-2n (4N51)
Bi 209		100 (6N38b)					B; ²⁰⁹ , I = 9/2 (87M50) Q _a 3. 2 calc (13553)	
Bi 209	G a's not seen (91H52)		a (7F51)	>>10 ¹⁷ y ap act (91H52); 3 x 10 ¹⁷ y ap act (7F51)	-3.15 range emulsion (7F51)			
Bi 210	A chem, genet (IC31)		p ² 99+%, a 5 x 10 ⁻⁵ % (7847)	5 02 d (IIB52); 4 85 d (7547); 5 0 d (IC3); 5 1 d (15445a)	p': 1.17 spect (10137, 9F39s., 9N40, 2249, 10L49)	no y (19G36, 6L47, 10C51)	0 <mark>,</mark> 1.17, 0, 5 06 cale (13533)	natural source, daughter 19-70 (RaD), parent Po 210 (RaF); parent Ti 206 (TB47); Po -cy (LISS); Po -cy (LISS); Bi -cy (LIA40); Bi -cy (LIA40);
Bi 210	A chem, genet (4N50a); chem, mass spect (52L52)		a, p or IT (-0.3%) (52L52)	-10 ⁶ y yield (52L52)	4. 93 ion ch (52L52)		Q _a 5. 03 (52 <u>L</u> 52)	Bi-n-y, parent TI ²⁰⁶ (4N50a); parent Po ²¹⁰ (52L52)
Bi ²¹¹	A chem, genet (IC31)		a 99.68%, p-0.32% (IC31)	2. 16 m (1C31)	a: 6.618 (84%), 6.272 (16%) spect (9438, 1831); 6.621 (82.6%), 6.274 (17.4%) spect (13V52)	0.350 abs (3839a); -0.35 ( $\epsilon_K/\gamma=0.18,\ K/L.5.5$ ) (4732b, $10F52$ ); 0.354 abs ( $16H25$ )	Q _a 6. 746 (13853) Q _b 0. 61 cale (13853) Bl ² !!	natural source, daughter Pb ²¹¹ (AcB), parent Po ²¹¹ (AcC'), parent Ti ²⁰⁷ (AcC'')
							16% (1634, 9438)	
(ThC)	A chem, genet (IC33)		9, 66, 3%, a 33, 7% (6K38)	60.5 m (IC31)	a. 606 (27.2%), 6.047 (69.9%), 5.63 (1.7%), 5.62 (0.15%), 5.63 (1.1%), 5.44 (0.016%), spect (48.83), 6.042 (70%), 5.760 (1.8%), 5.618 (0.2%), 5.760 (1.8%), 5.618 (0.2%), 5.590 (1.1%) spect (11.34); 6.220 spect (6M48a); 2.250 spect, 6 y coinc (4F48); others (7C48,3S33)	0.000 (strong), 0.144, 0.164, 0.000 (ord. 0.000), 0.422, 0.452, 0.452, 0.452, 0.452, 0.452, 0.452, 0.452, 0.452, 0.452, 0.452, 0.452, 0.452, 0.452, 0.452, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0.454, 0	Q _{a.} 6. 203. Q _{p.} 2. 25 (13553)	natural source, daugher 12 Pb 312 (ThB), parent Po 212 (ThC') and T1206 (ThC')

4 Po 213	iter 218 er At ²¹⁸ . 51a)	iter At ²¹⁹ .	00	_			parent (7K51)	3, ²⁰⁵ .	3i 206	
daugher At ²¹³ , parent Po ²¹³ (4H47, 11E47, 4H50a); parent T1 ²⁰⁹ (4H50)	natural source, daughter Pb. ²¹⁴ (RaB), daughter At ²¹⁸ , parent Po. ²¹⁴ (RaC'), parent T1 ²¹⁰ (RaC''); descendent Fr ²²² (8H51a)	natural source, daughter At 219, parent Po ²¹⁵ (8H53)	Bi-p-10n, parent Bi 200 (7K51a)	Bi-p-9n, parent Bi (7K5la)	Bi-p-8n, Pb-a-spall, parent Bi ²⁰² (7K51)	Bi-p-7n, Pb-a-spall, parent Bi ²⁰³ (7K51)	Bi-p-6n, Pb-a-spall, parent Bi ²⁰⁴ , parent Pb ²⁰⁰ (7K51)	Pb ²⁰⁴ -a-3n, parent Bi ²⁰⁵ , parent Pb ²⁰¹ (7K51)	Pb ²⁰⁴ -a-2n, parent Bi ²⁰⁶ (2T47a)	Pb ²⁰⁶ -a-3n (2T47a)
Q ₆ 5. 97 (13553) Q ₆ 1.39 (199853) B ₁ 213 P ₁ 239853)	Q _a 5. 610 (13553) Q̄ _p 3. 17 (8C41)	Q 2. 01 est (60G53)			- <del>-</del>		- <del>-</del>		Q _a 5. 321 (HPS)	
0.434 spect conv. scint spect (19W53)	with 6: \( y_1 \) 6604 cryst spect (100M52); \( y_1 \) 6604 (K/L 5 · 6); \( y_2 \) 0.66, \( y_3 \) 0.933 \( y_4 \) 1.20 (K.6 · 7); \( y_5 \) 1.238 (K/L 5 · 9); \( y_6 \) 1.379, \( y_1 \) 1.520, \( y_6 \) 1.76 (K/L 6 · 7); \( y_1 \) 1.520, \( y_6 \) 1.76 (K/L 6 · 7); \( y_1 \) 1.520, \( y_6 \) 1.76 (K/L 6 · 7); \( y_1 \) 1.22 \( y_3 \) 1.42 (K/L 6 · 7); \( y_1 \) 1.22 \( y_3 \) 1.42 (K/L 9 \) 1.44 \( y_3 \) 1.42 (K/L 9 \) 1.94 \( y_6 \) 1.95 \( y_6 \) 1.12 \( y_6 \) 1.95 \( y_6 \) 1.12 \( y_6 \) 1.95 \(								0.8 abs (2T47a)	1.3 abs (2T47a)
f.: 1.39 (68%), 0.959 (32%) spect (39W53); -1.3 abs (4H47, IEE4); s.: 86 ion ch (IIE47); 6. 0 ion ch (4H47)	a.; 505 (45%), 5, 444 (55%) spect (11.34); 5, 33 (17%) spect (764%), 5, 33 (17%) spect (764%); 6; 3 17 (17%) spect (76.4%); 7; 8) spect (76.4%); 1, 65 (-77%) spect (66.4); 5,4%; 1, 55 (-77%) spect (18.4%); 15 spect, abs (18.33)		5.84 ion ch (7K5la)	5. 70 ion ch (7K5la)	5.59 ion ch (7K51)		5.37 ion ch (7K51)	5. 2 ion ch (7K51a)	5. 218, 5. 064 spect (4R52b); 5. 21 ion ch (7K5la)	5.10 ion ch (7K5la)
47 m (4H47); 46 m (IIE47)	19. 7 m (дс31)	8 m (8H53)	11 m (7K51a)	18 m (7K5la)	52 m genet (7K51)	47 m genet (7K51)	3.8 h (7K51)	1.5 h genet (7K51)	9 d (2T47a)	5.7 h (2T47a)
6 98%, a 2% (11E47, 4H50a, 39W53)	0.04%. a. (iC31)	p (8H53)	EC, a (7K51a)	EC, a (7K5la)	EC, a (7K51)	EC (7K51)	EC -99%, a -1% (7K51)	EC 99+%, a 0.074% (17H51a)	EC -90%, a -10% (2T47a)	EC 99+%, a -10-2% (2T47a)
A chem, genet (IIE47, 4H47)	A chem, genet (IC31)	A chem, genet	_	B chem, genet (7K5la)	B chem, genet, excit (7K51)	B chem, genet (7K51)	B chem, genet (7K51)	B chem, genet, sep isotopes, excit (7K51)	B chem, genet, sep isotopes (2T47a)	B chem, excit, sep isotopes (2T47a)
B ₁ ²¹³	(RaC)	Bi 215	84Po 200	Po 201	Po 202	Po 203	Po 204	Po 205	Po 206	Po ²⁰⁷

Class and identification	Percent	Type of decay	Half-life	Energy of rad Particles	Energy of radiation in Mev Gamma-transitions	Disintegration energy and scheme	Method of production and genetic relationships	CHA
A chem, excit, sep isotopes (2T47a)		a (2T47a)	2. 93 y (2T50)	5.108 apect (4A52b); 5.109 apect (4R52b); 5.10 ton ch (7K5ia)	no y (2 <b>147a,</b> 18H51)	<b>Q_a 5.208, Q_{EC} 1.3 calc</b> (13553)	Pb.206-a-2n (2T47a); Pb.207-a-3n (2T47a); Bi-d-3n (2T47a); Bi-p-2n (2T47); daughter Em. ²¹ 2, daughter 1. 7 h At. ²⁰⁸ (8H50); daughter T. oh At. ²⁰⁸ (12B51)	P. 1.2
chem, excit (10K49)		a >90%, EC <10% est (13P50)	-100 y yield (10K50)	4.87 spect (4A52b); 4.86 ion ch (7K51a)	0.87 (1%), 0.55 (0.5%), 0.2 (0.2%), 0.1 (0.07%) acint apect (18H51)	Qa 4. 972 (13S53)	Bi-d-2n (10K49)	
A chem, genet		a; stable (cons parts (cons (HPS)	a: 6 stable (cons 140 d (IC31) energy) (HPS)	5. 298 spect (9438, 1655); 5. 30 spect (7046); (10D52) (10D52)	y ₁ 0. 800 (e/γ - 0. 03, K/L 3.7) spect, spect conv (13.51a;) y ₁ 0. 804 scint spect (18P23); y ₁ 0. 773 spect (7527a;) y ₁ 1. 73 spect (7527a;) y ₁ 1. 13 spect (7527a;) y ₁ 0. 774 spect (7527a;) y ₂ 0. 77 (- 10.75;) y ₃ 0. 77 (- 10.75;) y ₄ 0. 77 (- 10.75;) y ₅ 0. 77 (- 10.	0a, 5. 401 (13553) 0a, 6.	natural source, daughter B. 10 (fa.B.); B. 20 (fa.B.); B. 20 (f. 1740. 10C.40); B. 20 (f. 100. 100. 100. 100. 100. 100. 100. 10	
A genet (1C31)		a; ß stable (cons energy) (HPS)	0. 52 . (131.51)	7. 434 spect (ILL34); 6. 88 (0.50%), 6. 56 (0.53%), no 6. 34 a (ltim 0.02%) spect 1749524; 6. 90 (0.6%), 6. 57 (0.5%), 6. 34 (0.1%) ion ch (4NS)		O _a 7 : 58 (1353)	(AcC); (AcC); daughter At ² II (IIC40, IIC40a); daughter Em ² I ⁵ (IIM52); not parent Pb ^{207m} (23F52a)	
D chem, excit, sep isotopes (114S51)		a (114S51)	25 s (114S51)	7.14 ion ch (114S51)			Pb ²⁰⁸ -a-n (114551)	
A genet (1C31)		ď	3. 04 x 10 ⁻⁷ s delay conc (4B49); 3. 0 x 10 ⁻⁷ s delay conc (1H48); cothers (3148, 4V49, 1ID39, 16B43)	8. 776 apect (15B36, 9H38); long range a *: 10.556 (0.017%), 10. 417 (0.02%, 10.489 (0.004%), spect (48R51)		O _a 8. 946 (13553)	natural source, daughter Bi ²¹² (ThC); daughter Em ²¹⁶ (IIM49)	
genet (4H47, IIE47)		a (4H47, IIE47)	4.2 x 10 ⁻⁶ s delay coinc (3J48)	8,336 ion ch (11E47,5C48); 8,34 ion ch (4H50a)		Qa 8.496 (13553)	daughter Bi ²¹³ , parent Pb ²⁰⁹ (4H47, 11E47); daughter Em ²¹⁷ (11M49)	RE
genet (1C31)		a; p stable (cons energy) (HPS)	1. 637 x 10 ⁻⁴ delay coinc delay coinc delay coinc delay coinc (11059, 6841, 5 W42, 4143, 14 L47, 4B48); 1, 4 x 10 ⁻⁴ a delay coinc (5847)	7.680 spect (15B36, 9H38); 7.683 spect (15B36); long range as: 9.099 (0.02%), others 8.280-10.509 spect		Q _{a. 7.} 826 (13553)	natural source, daughter Bidd (RaC), parent Db210 (RaD); daughter Em218 (4548)	ACTOR PHYSICS

natural source, daughter Em219 (An), parent Pb211 (AcB); parent At215 (5K44)	natural source, daughter Em ²²⁰ (Tn), parent Pb ²¹² (ThB); (ThB); (5K43) (?)	daughter Em ²²¹ (9M52b)	natural source, daughter  Em ²²² (Rn), parent Pb ²¹⁴ (RaB);  parent At ²¹⁸ (5K43a)	Bi-a-spall (12B51)	Bi-a-spall (12B51)	B1-a-10n (12B51); Au-C-6n (13H51, 4M50)	Bi-a-9n, parent Po ²⁰⁴ (12B51)	B1-a-8n, parent Po ²⁰⁵ (12B51); Au-C-4n (4M50, 13H51)	Bi-a-7n, parent Po ²⁰⁶ (12B51)	Bi-q-6n (2T48a, 12B51); parent Po ²⁰⁷ , parent Bi ²⁰³ (12B51)	Bi-a-5n, parent Po (12B51)	daughter Fr ²¹² , parent Po ²⁰⁸ (8H50, 9M52a)	Bi-a-4n, parent Po ²⁰⁹ , parent Bi ²⁰⁵ (12B51)	Bi-a-3n, parent Po ²¹⁰ (10K49, 12R51); parent Bi ²⁰⁰ (4N50b)
Qa 7. 505. Qp 0. 8 calc (13553)	Q _a 6. 902 (13553)	Qa 6. 7, Qg 1. 3 est (13553)	Q. 6. 110, Q. 0. 33 cale (13553)											
													0. 2, 0.8 scint spect (89M52)	0, 25, 1, 15, 1, 40 scint spect (74H52a); 1, 0 abs, abs conv (10K49)
7. 365 spect (111.34)	a: 6.774 spect (15B36, 9H38)	6. 5 ion ch (9M52b)	a: 5.998 spect (15B36, 9H38)	6. 50 ion ch (12B51)	6. 35 ion ch (12B51)	6. 10 ion ch (12B51)		5. 90 ion ch (12B51)		5. 75 ion ch (12B51)		5. 65 ion ch (8H50)	5.65 ion ch (12B51)	5. 519 (32%), 5. 437 (31%), 5. 355 (37%) spect (74H52a)
1 83 × 10 ⁻³ a delay coinc (5 W 4 2)	0. 158 a (5 W42)		3. 05 m (1C31)	43 . (12.851)	l. 7 m (12B51)	7 m (12B51, 13H51)	-25 m genet (12B51)	25 m (12 <b>B</b> 51, 13H51)	2.6 h genet (12B51)		6. 3 h genet (12B51)	1.7 h (8H50)	5.5 h (12B51)	8. 3 h (10K49)
5 x 10-4% (5K44,8A50)	a:	a (9M52b)	a 99+%, p 0.03% (5K43a)	a, EC (12B51)	a, EC (12B51)	a. EC (12B51)	EC (12851)	a, EC (12B51)	EC (12B51)	EC -90%, a -10% (2T48a, 12B51)	EC (12851)	EC 99+%, a 0.5%(8H50)	EC -95%, a -5% (12B51)	EC 99+%, a 0.17% (74H52a); EC 99+%, a 0.1%
Po ²¹⁵ A genet (IC31)	A genet (1C31)	C genet (9M52b)	A chem, genet	 D chem, excit (12B51)	D chem, excit (12851)	D chem, excit (12B51)	B chem, excit, genet (12B51)	B chem, excit, genet (12B51)	B chem, excit, genet (12B51)	B chem, excit, genet (2748a, 12B51)	B chem, excit, genet (12B51)	A chem, genet (8H50)	B chem, genet, excit (12851)	A chem, excit, genet (10K49)

					and an incitation by second	is New		
Y Z	Class and identification	sbundance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	Remod of production and genetic relationships
85 At 211	A chem, excit, genet (11C40, 10K49)		a 40.9%, EC 59.1% (4N51)	7. 5 h (11C40, 10K49); 7. 3 h (17H51)	5.862 spect (74H52a); 5.89 ion ch (2T48a, 12B51)		Qa 5.975, QEC 0.9 est (13553)	Bi-a-2n (11C40, 11C40a, 10K49, 12B51); spall Th, U (20B52, 13S47)
AL 212	E excit (7W48)		a (7W48)	0. 25 s (7W48)				Bi-a-n (7W48)
Ак 213	E genet, decay charac (57K51)		a (57K51)		9. 2 range emula (57K51)			descendent Pa ²²⁵ (57K51)
At 214	B genet (111649)		a (11M49)	-2 × 10 ⁻⁶ s	8.78 ion ch (IIM49, IIM51)		Qa 8. 95, QEC 1. 05 cale (13553)	daughter Fr 218 (11M49, 11M51)
At 215	A genet (5K44, 13G48)		a (5K44, 13G48)	-10-4 s delay coinc (13G48, llM51); short (5K44)	8. 00 ion ch (13G48, 11M51); 8. 4 ion ch (5K44)		Q _a 8.15, Q _p 0.0 calc (13553)	daughter Fr 219, parent Bill (AcC) (13C48, IMS1); natural source, daughter Po 215 (AcA), parent Bill (AcC) (5K44)
At 216	A genet (13G48)		a (5K43, 13G48)	-3 x 10-4 s delay coinc (11M49,11M51); short (<54 s) (5K43)	7. 79 ion ch (13G48, 11M51); 7. 64 ion ch (5K43)		O _{d.} 7.94, O _{p.} 2.03 calc, Q _{EC.} 0.46 calc (13553)	daughter Fr ²²⁰ parent Bi ²¹² (ThC) (13048, 11M5); natural source, parent Bi ²¹² (ThC) (5K4); daughter Po ²¹⁶ (ThA) (5K4); note Po ²¹⁶ 6 stable (HPS)
At 217	A genet (11E47, 4H47)		a (IIE47, 4H47)	0. 018 s delay coinc (4H47, 4H50a): 0. 021 s delay coinc (11E47)	7. 02 ion ch (\$C48); 7. 00 ion ch (4H47)		Q _a 7. 15, Q _p 0.65 calc (13553)	daughter Fr ²²¹ , parent Bi ²¹³ (11 <b>E</b> 47, 4H47, 4H50a)
At 218	E genet (5K43a)		a (5K43a); a 99+%, p 0.1% (3W48)	1. 5-2. 0 a (3W48): several sec (?) (5K43a)	a: 6.63 range (5K43a); 6.7 ion ch (3W48)		Qa 6.75, Qg 2.67 calc (13553)	natural source, daughter Polis (RaA), parent Bi ²¹⁴ (RaC) (5K43a, 3W48)
At 219	A chem, genet (8H53)		a -97%, p -3% (8H53)	0.9 m (8H53)	a: 6. 27 ion ch (8H53)		Q ₆ 6. 39, Q ² 1.45 est (13553)	natural source, daughter Fr ²²³ (AcK), parent Em ²¹⁹ (An), parent Bi ²¹⁵ (8H53)
86 Em 208	D cheni (9M52b)		EC -80%, 1 -20% (9M52b)	23 m (9MS2b)	6.138 spect (9M52)			epail Th (9M52b)
Em 209	B chem, genet (9M52a)		EC -80%, a -20% (9M52a)	30 m (9M52b)	6. 02 ion ch (9M52a)			Pb-C-spail, spail Th (9M52a); daughter Ra ²¹³ , parent At ²⁰⁹ (9M52a)
Em 210	B chem, genet (9M52a)		a >95%, EC <5% (9M52b)	2. 7 h (9M52a); 2. 1 h (13G49)	2. 7 h (9M52a); 6. 036 spect (9M52); 2. 1 h (13G49) 6. 02 ion ch (9M52a)		Q _a 6. 153 (13553)	epail Th (13G49, 9MS2a); Pb-C-spail (9MS2a); parent Po ²⁰⁶ (9MS2a)
Em 211	A chem, genet (9M52a)		EC 75%, a 25% (9M52a)	16 h (9M52a)	5.847 (33%), 5.778 (67%) spect (9M52); 5.82 ion ch (9M52a)			Pb-C-spall, parent At 211 (9M52a)
Em 212	A chem, genet (8H50, 13G49)		a (8H50)	23 m (13G49, 8H50, 9M52a)	3 m (13G49, 6, 262 spect (9M52); 8H50, 9M52a) 6, 23 ion ch (9M52a)		Q _a 6. 382 (13553)	spail Th (13G49); daughter Fr ²¹² , parent Po ²⁰⁸ (8H50, 9M52a)

										CHAP.	1.2
daughter Ra ²¹⁹ , parent Po ²¹¹ (AcC') (11M52) daughter Ra ²²⁰ , parent Po ²¹² (ThC') (11M49, 11M51)	daughter Ra ²²¹ , parent Po ²¹³ (11M49, 11M51)	daughter Ra 222, parent Po 214 (RaC') (4548)	natural source, daughter Ra ²²³ (AcX), parent Po ²¹⁵ (AcA). daughter At ²¹⁹ (8H53)			natural source, daughter Ra224 (ThX), parent Po216 (ThA)	Th-p-spall, parent Fr ²²¹ (9M52a); parent Po ²¹⁷ (9M52b)	natural source, daughter Ra ²²⁶ , parent Po ²¹⁸ (RaA)		spall Th (8H50); parent Em ²¹² (8H50, 9M52a)	descendent Pa ²²⁵ (57K51)
	Q 7. 89 (13553)	Q _a 7. 25 (13S53)	Q _a 6.951, Q _p 0.26 calc (1353)	44 / 1844 444 / 1844	6,397	(4R36, HPS) Q_6: 398 (13553)	Qa 6.0 cat, Qp 0.9 cat (13553)	Q 5. 587 (13553)			
			0.067, 0.124, 0.198 (strong), 0.267, 0.121, 0.199, 0.589 (weak) spect conv (1157); 0.123, 0.270, 0.590 cryst spect (8F40)								
8. 6 ion c† (11M52) 8. 01 ion ch (7050)	7.74 von ch (IIMSI)	7 '' ion ch (1J48)	6.824, 6.559, 6.414 spect(IILJ4); a ₀ (69%), a ₂₇₀ (15%), a ₃₉₇ (12%), a ₆₂₂ (4%) spect (4R36)			6. 282 spect (15B36, 9H38)		5. 486 spect (15B36, 9H38)		6.409 (37%), 6.387 (39%), 6.339 (24%) apect (8H52c); 6.36 son ch (8H51)	8.3 range emula (57K51)
-10-6 e est (11M5.2) -10-4 e est (11M5.1)	-10 ⁻³ delay coinc (11M51)	0.019 • delay coinc (45:8)	3.92 • (1C31)			54.5 • (1031)	25 m (9M52b)	3. 825 d (22T51, 1C31)		19. 3 m (8H50)	
a (11M52) a (11M49. i1M51); ß stable	(conserer gy) (HPS) a (IIMS1); b stable (conserer gy) (HPS)	a (4548); ß stable (consenergy) (HPS)	d			a: β stable (consenergy) (HPS)	p -80%, a -20% (9M52b)	a: no β ⁺ (lim 10 ⁻⁴ <del>%</del> ) (5K46)	•	EC 56%. a	a (57K51)
B genet (IIM52) A genet (IIM49, IIM51)	A genet (IIM49, IIM51)	A genet (4548)	A chem, genet			A chem, genet (IC31)	A chem, genet (9M52a)	A chem, genet (IC31)		A chem, genet (8H50); chem, mass spect (9M52a)	E genet, decay charac (57K51)
Em 215		Em 218	Em 219 (An)					Em ²²²		87Fr ²¹²	Fr 217

:												REA	TOR PHYSICS
Method of production and	genetic relationships	daughter Ac 222, parent At (11M49, 11M51)	daughter Ac ²²³ , parent At ²¹⁵ (13G48, 11M49, 11M51)	daughter Ac 224, parent At 216 (13G48, 11M49, 11M51)	daughter Ac 2.5, parent At 217 (11E47, 4H47, 5C48, 4H50a); daughter Em 221 (9M52a)	spall Th, parent Ra ²²² ancestor Bi ²¹⁴ (8H50a, 8H51a)	natural source, daughter Ac ²²⁷ , parent Ra ²²³ (AcX) (7P59, 7P59a, 7P59b, 7P4i, 7P46, 8G47, 6L50); parent At ²¹⁹ (8H53)	Pb-C-spall, spall Th, parent Em209 (9M52a)	daughter Th ²²³ , parent Em ²¹⁵ (11M52)	daughter Th ²²⁴ , parent Em ²¹⁶ (11M49, 11M51)	daughter Th ²²⁵ , parent Em ²¹⁷ (11M49, 11M51)	daughter Th ²²⁶ , parent Em ²¹⁸ (4548); daughter Fr ²²² (8H51a)	natural source, daughter TAZA (RdAc), daughter F7233 (AC); (An); (An); daughter Ac ²²³ (11M5); spail U (13547, 6047, 6F5)
	Disintegration energy and scheme	Qa 8.00, QEC 1.8 calc (13553)	Q, 7. 44 (13553)	$Q_{a}$ 6.81, $Q_{\beta}^{-}$ 1.27 calc, $Q_{EC}$ 0.87 calc (13553)	Q _a 6.42, Q _p 0.24 calc (13553)	Q _a 6. 00 est, Q _b 2. 04 est, Q _{EC} 0. 02 est (13553)	Q _a 5.60 est, Q _p 1.19 calc (13553)		Qa 8.1 (13553)	Q 7. 57 (13553)	Qa 6. 83 (13553)	Q _Q 6. 63 (13553)	Q _a 5. 855 (13853)
ation in Mev	Gamma-transitions				0.220 spect conv. scint spect (39W53)		0.09 abs (6L44, 7P46); -0.330 (6%) abs, 0.0486 (27%) crit abs (6L50)						0.144, 0.155, 0.180, 0.270, 0.026, 0.026, 0.026, 0.036, 0.034, 0.039, 0.136, 0.154, 0.180, 0.232, 0.280, 0.322, 0.348, 0.444 spect conv (1537)
Energy of radiation in Mev	Particles	7.85 ion ch (11M51)	7. 30 ion ch (IIMS1)	6. 69 ion ch (11M51)	6.30 ton ch (4H47, 5C48); 6.30 (-75%), 6.05 (-25%) ion ch (4H50a)		p: 1.2 cl ch (7P39a, 7P39b, 6L50)	m (9M52c) 6. 90 ion ch (9M52c)	8.0 ion ch (IIM52)	7.43 ion ch (7050)	6. 71 ion ch (11M51)	6. 51 ion ch (1J48)	5.860 (weak), 5.730 (95k), 5.704 (5.55), 5.506 (245), 5.506 (185), 5.506 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.606 (185), 5.6
:	Half-life	5 x 10 ⁻³ s cat (IIM51)	0.02 s delay coinc (11M51)	27.5 a (IIM51)	4.8 m (4H50a); 5 m (IIE47)	14.8 m (8H50a)	21 m (7P39)	2.7 m (9M52c)	-10 ⁻³ s est (IIM52)	3 x 10 ⁻² s est (11M51)	30 . (IIM51)	38 s (4548)	II. 2 d (IC31)
Type of	decay	a (IIMSI)	a (13G48); ß stable (consenergy) (HPS)	a (13G48)	a (11E47, 4H47)	6 99+%, a 0 01-0.1% (8H51a)	6 (7P39a, 8G47), a 4 x 10-3% (8H53)	a (9M52a)	a (IIM52)	a (IIMSI)	a (IIMSI)	a (4548); p stable (consenergy) (HPS)	a; 6 stable (consenergy) (HPS)
Percent	abundance												
Clear	identification	B genet (11M49, 11M51)	A genet (13G48)	A genet (13G48)	A chem, genet (4H47, 11E47)	A chem. genet (8H50a)	A chem, genet (7P39, 7P39b)	B chem, genet (9M52a)	B genet (IIM52)	A genet (11M49, 11M51)	A chem, genet (11M49, 11M51)	A chem, genet (4548)	A chem, genet (1C31)
Import	V 2	7Fr 218	Fr 219	Fr 220	Fr 221	Fr 222	Fr 223	88Ra 213	Ra 219	R. 220	Ra 221	Ra 222	Ra 223

NUCLEAR PHYS	IC8										(	CHAP. 1.2
natural source, daughter Th-228 (RdTh), parent Em-220 (Tn); spall U (13547, 6047, 6F51)	daughter Th ²²⁹ , parent Ac ²²⁵ (11E47, 4H47, 4H50a); epall U (6F51)	natural source, daughter Th ²³⁰ (lo), parent Em ²²² (Rn)	Ra-n-y, parent Ac 227 (8P49); spall U (6F50)	natural source, daughter Th ²³² , parent Ac ²²⁸ (MaTh ₂ )	[Ra ²²⁸ -n-y, parent Ac ²²⁹ ] (41D52)	spall Th, parent Ac 230 (5J52)	**	descendent Pa ⁴²³ (57K51)	daughter Pa 226, parent Fr 218 (11M49, 11M51)	daughter Pa ²²⁷ , parent Fr ²¹⁹ parent Ra ²²³ (AcX) (13G48, 11M49, 11M51)	daughter Pa ²²⁸ , parent Fr ²²⁰ , parent Ra ²²⁴ (ThX), (13G48, 11M49, 11M51)	daughter Ra 225, parent Fr 221 (4447,11E47,44150a); daughter Pa 229 (8449a); daughter Th 225 (11M49,11M51) apail Th (17H50), U (6O47)
Qa 5. 784 (1353) Ro224  A 664,  Qa494  O.495	(4R52, HPS)	Q _a 4.863 (4R52b) R _Q 226  G _a 3.7,94.3%	(4A52a, HPS)	Q ₆ -0.04 (13553)					Qa 7. 09, QEC 2. 26 calc (13553)	Qa 6. 76, QEC 0. 64 calc (13553)	Qa 6. 28, QEC 1.37 calc, Qg 0. 29 calc (13553)	Q _a 5. 90 (13553)
0. 241 (e _K /y 0.1) spect conv (4R52); no y (iM28, 4F49)		0.186 spect conv (10C51); -0.19 (+7,0.88, K/L -0.5) a-conv coinc aba (14/24, 78.36); (e/y -0.5) (5543)	0. 291, 0.498 scint spect (107B52)	-0.03 cl ch (6L48, 6L49)								
5. 681 (95%), 5. 448 (4. 6%), 5. 194 (0. 4%) spect (4844); 5. 681 spect (15536); 5. 66 ion ch (2C45)	-0.31 spect (3F\$2a); -0.2 abs (4H\$0a); <0.05 abs (11E47)	a ₀ 4.777 spect (4R52b); a ₀ (94.3%), a ₁₈₈ (5.7%) spect (4A52c); a ₀ (95.2%), a ₁₈₆ (4.8%) ion ch (7K5la); a ₀ (93.5%), a ₁₈₇ (6.5%) spect -(4R49a); others (109851)	l. 30 spect (107B52)	-0.012 (?) cl ch (6L48, 6L49a); 0.053 spect, abs (8L39)		1. 2 abs, spect (5J52)		7. 6 range emula (57K51)	6. 96 ion ch (IIM51)	6. 64 ion ch (IIM51)	6.17 ion ch (IIM51)	5. 80 ion ch (4H50a, 5C48)
3.64 d (IC31)	14.8 d (4H50a);	1622 y sp act (2K49a); (3K49a); (3C4) y sp act (3C46); (1590 y sp act (1C31)	41. 2 m (107B52)	6. 7 y (IC31)	[short] (41D52)	1 h (5J52)			5.5 e (IIM52)	2. 2 m (11M51)	2. 9 h (IIMSI)	10. 0 d (4H50a,
a: 6 stable (cons nnsrgy) (HPS)	6 (11E47, 4H47); no a (1im 0.1%) (9M52c)	• 6	6F50)	<b>'</b> a	[p ⁻ ](41D52)	6 (5352)		a (57K51)	a (111M51)	a 99%, EC 1% (11M51)	EC -90%, a -10% (ilMSi)	a (11E47, 4H47); ß stable (cons energy) (HPS)
A chem, genet	5 A chem, genet (11E47, 4H47)	A chem, genet	A n-capt, genet (8P49)	A chem, genet (1C31)	[B] n-capt, genet (41D52)			E genet, decay charac (57K51)	B genet (11M49, 11M51)	A genet (13G48)	A chem, genet (13G48)	(4H47, ILE47)
Ra 224 (ThX)	Ra 225	Ra 226	Ra 227	Ra ²²⁸ MeTh ₁ )	Ra 229	Ra 230	~	89Ac 22:	Vc 522	Ac 223	Ac 224	Ac 225

Inneres	Con sec	Percent	Two		Energy of radiation in Mev	sation in Mev		Meehod of remducation and
V 2	identification	abondance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
89 Ac 226	A chem, genet (6S48)		p. (6548)	29 h (6S50)	1.17 abs (17H50)		Qa 5. 44 est, QEC 0.6 est, Qb 1.07 est (13553)	apall U, daughter Pa.230, parent Th.28 (6548, 6550); spall Th (17450, 11M50); daughter Pa.230, parent Th.226 (11M50)
Ac 227	A chem, genet (IC31)		6 - 99% (7P3), 8P49a); a 1. 2% (2M14, 7P39, 7P46, 8P49a)	22.0 y (13H50a); 21.7 y (4C44); 13.5 y (1C31)	a; 4.942 spect (4B52b); 4.94 (100%) ion ch (13G48a); others (3G47) 6: 0.04 spect (3P50); c. 0.2 cl ch (7P46); c. 0.3 abs (6L44)	0.037 (weak) abs (6L4), 6L44, 7P46); (0.2%) (6L50)	Ac ²²⁷ , I = 3/2 (3655) Q _a 5. 03, Q _b -0. 08 cale (13553)	natural source, daughter 23.1, parent Th ²²⁷ (RdAc); parent Fr ²²³ (AcK) (TP39, TP46); daughter Ra ²²⁷ (8P49)
	A chem, genet (1G31)		<u>'a</u>	6. 13 h (IC31)	2.18 1054), 1.85 (955), 1.72 (75), 1.15 (355), 0.65 (655), 0.46 (1155) spect (825.5); 2.03, 1.74, 1.10 spect (535); others (47.36, 61.38, 51.39)	0. 058. 0 129, 0 184, 0.318, 0.452, 0.914, 0.969 spect conv (1.1324) 0. 133 0. 462, 0.913, 0.968 spect (0.633, 0.144, 0.186, 0.338, 0. 533, 0.590, 0.905 spect conv	Q. 4.66 est, Q. 2.18 (13553)	natural source, daughter Ra ²²⁸ (MsTh _j ), parent Th ²²⁸ (RdTh)
Ac 229	B chem, n-capt (41D52)		6 (41052)	66 m (41D52)			Q_ 1.0 est (13553)	daughter Ra ²²⁹ (41D52)
Ac 230	F genet (5352)		p ⁻ (5.35.2)	<  m genet (5.52)	-2. 2 abs, spect (5352)			daughter Ra ²³⁰ (5J52)
90Th ²²³	B genet (11M52)		a (IIM52)	-0.1 s est (IIM52)	7. 55 ion ch (11M52)		Q. 7.69 (13853)	daughter U ²²⁷ , parent Ra ²¹⁹ (IIMS2)
	A genet (11M49, 11M51)		a (liM51); ß stable (consenergy) (HPS)	-1 s est (IIM51)	7.13 ion ch (7050)		Q ₆ 7. 26 (13553)	daughter U ²²⁸   parent Ra ²²⁰   (11M49, 11M51)
	A chem, genet (11M49, 11M51)		a -90%, EC -10% (11M51)	8.0 m (IIMSI)	6. 57 ion ch (llM51)		Qa 6.69, QEC 0.55 calc (13553)	daughter U ²²⁹ , parent Ra ²²¹ , parent Ac ²²⁵ (11M49, 11M51)
Th 226	A chem, genet (4548)		a (4848); 6 stable (consenergy) (HPS)	30.9 m (4548)	a ₀ (78%), a ₁₁₇ (22%) spect (21852); 6. 30 ion ch (1348)		Qa 6. 41 (13553)	daughter U ²³⁰ , parent Ra ²²² (4548); daughter Ac ²²⁶ (6548, 6550)

NUCLEAR PHYSIC					CHAP. 1.2
natural source, daughter Ac 227, parent Ra 23 (Ac X); daughter Pa 227 (13G48, 11M51); spail U (6O47)	natural source, daughter Ac ²²⁸ (MaTh ₂ ), parem Ra ²²⁴ (ThX); daughter U ²³² (9G49); daughter Pa ²²⁸ (13G48b. llM51)	daughter U ²³³ , parent Ra ²²⁵ (11E47, 4H47, 4H50a)	natural source, daughter $U^{234}$ ( $U_{II}$ ), parent Ra 226 ; daughter Pa 230 (4548a)	natural source, daughter U ²³⁵ (AcU),parent Pa ²³¹ ; Th-n-2n (5N38, 13552)	natural source, parent Ra ²²¹ (MsTh ₁ )
Q ₆ 6.136 (13553)	Q 5. 520 (13553) The rest of t	(44495) 4436,445)	D _a 4. 765 (13553) Th230 a 2577 CHPS)	Q ₄ 4.19 cale (13533) Q ₅ 0.324 (3F52) Th ²³¹ B	(3F52) Q _a 4. 05 (13S53)
0.050, 0.057, 0.080, 0.101, 0.113, 0.129, 0.208, 0.240, 0.258 eryst speet (18740); 0.050 (13%), 0.120 (13%), 0.280 (15%), abs (1880); 0.050 (5%), 0.125 (10%), 0.270 (26%) abs (18845); 0.050 (-3%), 0.125 (23%) abs (9742)	0.0843 spect conv (4R52a); 0.083 (e/ 12) a-conv coinc abs (14V52); (e/y = 10) crit abs 0.083 (2.1%, e/y = 10) crit abs (1R53); others (IM28, IIS4la, 3R50, 103B51)		0.068, 0.228 (very weak) spect conv (485); 0.068 (0.85%), 0.140 (0.33%), 0.240 (0.05%) abs (4C48); 0.240 (0.05%) abs (4C48); 0.240 (0.05%) abs (4C48); 0.070 coinc with a 'v' +46, 0.06 (0.5%), 0.190 (0.3%) abs (1850); 0.07 (coinc with a), -0.2 (coinc with a) a-v, a-conv coinc abs (551); 0.07 (551); 0.0851);	γ ₁ 0. 022, γ ₂ 0. 059, γ ₃ 0. 063. γ ₄ 0. 065, γ ₅ 0. 107, γ ₆ 0. 122, γ ₇ 0. 167, γ ₈ 0. 208, γ ₉ 0. 230 γ ₂ γ ₃ γ ₄ γ ₄ γ ₆ γ ₄ γ ₄ γ ₆ γ ₇ γ ₈ γ ₉ = 0. 401, 0.00 0. 065, 0. 020, 0. 018, 0. 003, 0. 001) spect conv. scint spect (3F5.2); 0. 059, 0. 063, 0. 063, 0. 120 spect conv (10551); 0. 035, (280 γ ₆ ), 0. 210 abs (3K49)	-0.055 (coinc with 24% of a) a-conv coinc emula (1505.); -0.075 (coinc with -20% of a) a-conv coinc emula (5A52)
6.030 (19%), 6.001 (5%), 5.972 (13%), 5.92 (13%), 5.92 (13%), 5.92 (13%), 5.92 (13%), 5.706 (2%), 5.749 (17%), 5.728 (-2%), 5.706 (15%), 5.98 (15%), 5.96 (15%), 5.96 (15%), 5.96 (15%), 5.96 (15%), 5.96 (15%), 5.96 (15%), 5.92 (-1%), 5.96 (15%), 5.92 (-1%), 5.96 (15%), 5.92 (-1%), 5.96 (15%), 5.92 (-1%), 5.96 (15%), 5.92 (-1%), 5.96 (15%), 5.92 (-1%), 5.96 (15%), 5.92 (-1%), 5.96 (15%), 5.92 (-1%), 5.96 (15%), 5.96 (15%), 5.96 (15%), 5.97 (15%), 5.97 (15%)	(4R49b)	5,02 (-10%), 4.94 (-20%), 4.85 (-70%) ion ch (4H50a)	4.682 (-75%), 4.613 (-25%), 4.51(7) (weak) spect (4R48); 4.66 range air (1G22), ion ch (2C44, 2C45)	0.302 (44%), 0.216 (11%), 0.094 (45%) spect (15%2); 0.19 (-40%), 0.10 (-40%) spect (10S5); 0.2 abs (5E37, 1J51)	3.98 ion ch (2C45); 3.98 range emuls (7F5la); 4.20 ion ch (1537)
18. 6 d (8P49b);	1.90 y (1G31)	7340 y genet (4H50a); -10 ⁴ y genet (11E47)	8.0 x 10 ⁴ y sp. act (8H49b); 8.2 x 10 ⁴ y genet (1C30)	25.64 h (1351); 25.5 h (3649); 24.0 h (12G32); 24.0 h (12G32)	1. 39 x 10 ¹⁰ y sp act (6K38); spont fission: 1. 4 x 10 ¹⁸ y (24S52)
a: 6 stable (com 18.9 anergy (HPS)	a; p stable (consenergy) (HPS)	a; ß stable (consenergy) (HPS)	as stable (come one regy) (HPS)	'a	a; p stable (consenergy) (HPS)
					100 (1 <b>A35</b> , 1D36)
A chem, genet	A chem, genet (1C31)	A chem, genet (11E47, 4H47)	A chem, genet (IC31)	A chem, genet (IC31)	A chem, genet (IC31)
Th 227	Th ²²⁶ (RdTh)	Th.229	(10) (10)	(UY)	Th ²³²

	7	1	There are		Energy of rad	Energy of radiation in Mey		Marked of conduction
Y Z	identification	abundance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
90 ^{Th²³³}	A chem, n-capt (IM38)		p (13547a)	23. 3 m (2B50); 23. 5 m (13547a); 23. 6 m (31R52); 23 m (2G41)	1. 23 spect (2850, 31852); 1. 24 spect (3F53); 1. 2 abs (13552)	0.098 (0.25%), 0.172 (0.03%), 0.350 (0.004%), 0.448 (0.1%), 0.662 (0.05%) seint spect (3F3); no y (2B50, 31R52)	Qa 3. 79 est, Qg 1. 23 (13553)	Th·n·y (1M38, 13547a, 1354), 2G41); Th·d·p (9G49); parent Pa ²³³ (1M38)
Th ²³⁴ (UX ₁ )	A chem, genet		'a	24. 10 d (3K48); 24. 1 d (3S39); 24. 5 d (1C31)	0.205 (-80%), 0.111 (-20%) spect (16846); 0.195 (55%), 0.104 (44%) spect (19450); 0.190 spect (7346); 0.20, 0.1 abs (4F38a)	0.090 (e/y -0.2) spect conv (19450). 0.093 (-20%, e <u>L</u> /y -0.34), 0.180 (4.5%) spect conv, abs (16B46); 0.092 (1M23)	9, 0.20 (1353) Th.234	natural source, daughter $U^{238}$ parent $Pa^{234} (U\chi_2)$
Th 235	Th ²³⁵ [B] n-capt, genet		[6 ⁻ ] (20H50)	<<10 m genet (20H50)			(HPS)	[Th ²³⁴ -n-Y. parent Pa ²³⁵ ] (20H50)
91 Pa 225	E excit, decay charac (57K51)		a (57K51)	2.0 s (57K51)		•.		spall Th, ancestor Ac 221 Fr 217, At 213 (57K51)
Pa 226	B chem, genet (IIM49, IIM51)		a (IIM51)	1. 8 m (11M51)	6.81 ion ch (11M51)		Qa 6. 93, QEC 2.8 cale (13553)	<pre>spall Th, parent Ac (IIM49, IIM51, IIM52)</pre>
Pa 227	A chem, genet (13G48)	. ,-	a -85%, EC -15% (IIM51)	38. 3 m (11M51)	6.46 ion ch (IIMS1)		Q ₆ 6.58, Q _{EC} 1.08 calc (13553)	spall Th, parent Ac ²²³ , parent Th ²²⁷ (RdAc) (15G8, 1M31); daughter Np ²³ (13G48b); spall U (6O48)
Pa 228	A chem, genet (13G48)		EC -98%, a -2% (IIM51)	22 h (11 <b>M</b> 51)	6.09 (75%), 5.85 (25%) ion ch (IIMSI)		Qa 6. 20, QEC 2. 05 calc (13553)	spall Th. daughter U ²²⁸ , parent Ac ²²⁴ , parent Th ²²⁸ (RdTh) (13G48, 11M49, 11M51)
Pa 229	A chem, genet (8H49a)		EC 99+%, a 0. 25% (21S51); EC -99%, a -1% (11M51)	l. 5 d (6H48)	5. 69 ion ch (11M48); 5. 66 ion ch (8H48)		Qa 5. 79. GEC 0. 37 calc (13853)	Th ²³⁰ -d-3n, parent Ac ²²⁵ (8H49a); daughter U ²²⁹ (IIMSI)
Pa 230	A chem, genet, excit (4548)		EC -92%, 6' -8% (48-4); a -0.003% (11M50)	17. 7 d (5049); 17. 0 d (4548)	6 ⁻ : -0.43 abs (5049)	0. 94 abs (5049)	Q ₆ 5. 45 est, Q ₆ 0. 57 est, Q _{EC} 1. 28 est (1355)	Th-d-4n, Th-a-p5n, parent U230 (4548); Th230 (4548); Th230-d-2n (8149a); Pa-d-p2n, Pa-a-an (5049); U233-d-an (8149); parent Th230 (10), parent Ac226 (11M50)

natural source, daughter Th-21 (UY) parent Ac ²²⁷ ; Th-d-3n (4548); daughter U ²³¹ (14C50)	Th-d-2n (9649, 4848, 1J50), Th-c-phn (4548); Pa-d-p (5049); Pa-n-y (1J50); parent U ²³² (9649, 5049)	daughter Th ²³³ (IM38, 2C41, 11541, 11547a); parent U ²³³ (11547a); daughter Np ²³⁷ (4447); Th-d-n (4548, 9C49); Th-a-pān (4548, 9C49); Th-a-pān (4548), daughter Np ²³⁷ (15M47)	natural source, daughter Th ²³⁴ (UX _j ), parent U ²³⁴ (U _{II} )	natural source, parent $U^{234}$ $(U_{II})$ : $P_a^{233}$ -n- $\gamma$ (50K52)	U ²³⁸ -p-a, U ²³⁸ -d-an (IIM50); daughter Th ²³⁵ (20450)	Th-a-9n, parent Th ²²³ (11M52)	Th-a-8n, parent Th ²²⁴ , parent Pa ²²⁸ (IIM49, IIM51); daughter Pu ²³² (8J48)	
Pa ²³¹ 1 = 3/2 (87M50) Q _a 5, 131 (13533)	Qa 4. 70 est, Qg 1. 48, QEC 0.61 est (13553)	Q ₆ 4. 46 est. Q _p 0. 53 (13533)	Op 2. 32 (16B45)	Q 2. 2 (7) est (13553) Q 1. 95 (4F49)		Qa 7. 14 est (13553)	Qa 6. 79, QEC 0.30 calc (13553)	Qa 6.53, QEC 1.29 calc (13S53)
0.034, 0.038, 0.057, 0.064, 0.082, 0.102, 0.198, 0.259, 0.301, 0.31, 0.357, 0.383, 0.057, 0.284, 0.057, 0.284, 0.057, 0.284, 0.057, 0.32 apect conv (10428), 0.057, 0.087, 0.100, 0.30 (4%), abs. crit abs. 3187823); 0.044, 0.066 ci ch (41751); others (4546, 4149)	-0.23 (-30%), 1.05 (-100%) abs (1348b); 0.21, 1.0 abs (5049)	0 029, 0.041, 0.058, 0.076, 0.087, 0.105, 0.273, 0.302, 0.312, 0.302, 0.313, 0.342, 0.377, 0.400, 0.028, 0.046, 0.058, 0.046, 0.058, 0.047, 0.0405, 0.0754, 0.048, 0.048, 0.0754, 0.087, 0.088, 0.0754, 0.087, 0.088, 0.309, 0.337 spect conv (21.47); conv (2	0.817 (eg/y 0.04) apect conv (19H50); 0.394 (with IT, 0.15%, e/y -1), -0.9 (-2%), -1.5 (-0.2%) apect, apect conv (16B43), 0.782 (weak, e/y large) apect conv (16B43a)	0.85 (two y's) abs. β-y coinc (16B45); -0.7 (two y's) abs. y-y coinc (4F38a, 4F38b)	no y. abs (11M50)			
5.042 (11%), 5.002 (47%), 4.938 (25%), 4.838 (3%), 4.720 (11%), 4.660 (1-3%) spect (4R49c, 13C51), -4.7 (15%) ion ch (2C44, 9746a, 13C48a)	0.99 (-30%), 0.64 (-10%), 0.28 (-60%) spect (35P52), -0.28 abs (1J48b)	0.530, 0.430 spect (3F51); 0.5 abs (1355); 0.2 aps (1355); 11K50); 11K50); -0.7 spect (11F44)	2.32 (80%), 1.50 (13%), 0.60 (7) (-7%) spect (19H50); 2.32 (98%) spect (16B45)	-1. 2 (10%), 0. 45 (90%) apect (16845); 1. 6, 0. 6 abs (4F38a)	1. 4 abs (IIM50)	6. 8 ion ch (11M52)	6. 67 ion ch (7050)	6. 42 ion ch (IIM51)
3, 43 x 10 ⁴ y ap act (8W49); 3, 2 x 10 ⁴ y ap act (2G30)	1. 32 d (1/50); 1. 4 d (5049); 1. 6 d (9G49)	27.4 d (2G41)	1.175 m (112851); 1.14 m (IC31)	6.7 h (1C31)	23.7 m (IIM50); 23 m (20H50)	1. 3 m (IIM52)	9.3 m (IIM51)	58 m (IIMSI)
a: B stable (consenergy) (HPS)	6 (9G49); no EC (lim 2%) (88B52a)	p* (1M38,	B 99+%, IT 0.15% (4F38a, 16B45)	<b>'a</b>	p. (IIMSo, 20H5o)	a (IIM52)	a-80%, EC-20% (11M51)	EC -80%. a -20% (IIMSI)
A chem, genet (IC31)	A chem, genet (9G49)	A chem, genet (IM38, 2G4), 1354))	A chem, genet (IC31)	A chem, genet (1C31)	B chem, excit, sep isotopes (IIM50), genet (20H50)	B chem, genet (11M52)	A chem, genet (11M49, 11M51)	A chem, genet (11M49, 11M51)
Pa ²³¹	Pa 232	P. 233	Pa ²³⁴ (UX ₂ )	Pa ²³⁴ (UZ)	Pa 235	92 ^{U227}	U ²²⁸	0,229

		9	7		Energy of radiation in Mey	acion in Mev		Method of production and
Y Z	identification	abundance	decay	Half-life	Particles	Gamma-transitions	Disintegration energy and scheme	genetic relationships
92 ^{U²³⁰}	A chem, genet (4548)		a (4548); 6 stable (consenergy) (HPS)	20. 8 d (4548)	5. 85 ion ch (1J48); a ₀ (77%), a ₇₀ (23%) spect (21552)		Q_ 5. 99 (13553)	daughter Pa 230 parent Th 226 Th-a-en (4844); daughter Pa 230 Pa-d-3n, Pa-a-pen (5049); adaughter Pu 244 (13P49); spall U (6047)
U ²³¹	A chem, sep isotopes, excit (5049); genet (14C50)		EC 99+%, a 5.5 x 10-3 % (14C50)	4. 3 d (14C50); 4. 2 d (5O49)	5. 45 ion c <u>h</u> (14C50)	(8050)	Qa 5. 55, QEC 0.34 calc (13853)	Pa ²³¹ -d-2n, Pa ²³¹ -a-p3n (5049); Th-a-5n (14C50, 8050); parent Th ²²⁷ , parent Pa ²³¹ (14C50)
U.232	A chem, genet (9C49)		e (9G49); p stable (consenergy) (HPS)	70 y yield (8.149): -30 y yield (9.049)	5. 31 range A1 (1348a); 5. 27 range air (12444); a ₀ (69%), a ₅₈ (31%) spect (21852)	a.copy coinc emule (15D52)	Q _a 5. 40 (1353)) U232	daughter p. 234. parent Th 228 (RATh) (9504). daughter p. 256 (8349); daughter p. 232. p. 231.d-n, p. 231.d-p. 2n (5049); Th. d. daughter p. 232. p. 231.d-n,
U ²³³	A chem, genet (13547a, 13552)		a (13552); ß stable (cons energy) (HPS)	1. 62 x 10 ⁵ y ep act + mass spect (BHS24); 1. 63 x 10 ⁵ y ep act + mass spect (151.45); 1. 2 x 10 ⁵ y yield (1352)	4. 823 ion ch (5C48); o _Q (828); e _Q (828); e _Q (828); 4. 80 abs air (15C47); others (11E47)	0. 0428 (0.05%), 0.0561 (0.01%) inn eft (12.9%), 0.041, 0.056, 0.094, 0.090 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.081 (0.1%), 0.	Q _a 4.91 (13833) (14F3) (1233 (14F3) (1233 (14F2) (14F2) (14F2) (14F2)	daughter pa ²³³ (13547a); parent Th ²²⁹ (11 <u>5</u> 47, 4H47)
U234	A chem, genet, mass spect (IC31)	(1850)	o simple Coma and Ty) (HPS)	2. 48 × 10 ⁵ y 1(2F 5); 25 × 10 ⁵ y 25 × 10 ⁵ y 27 × 10 ⁵ y 28 × 10 ⁵ y 28 × 10 ⁵ y 28 × 10 ⁵ y 28 × 10 ⁵ y 29 × 10 ⁵ y 27 × 10 ⁵ y 28 × 10 ⁵ y 28 × 10 ⁵ y 29 × 10 ⁵ y 20 × 10 ⁵ y 20 × 10 ⁵ y 20 × 10 ⁵ y 21 × 10 ⁵ y 22 × 10 ⁵ y 23 × 10 ⁵ y 24 × 10 ⁵ y 25 × 10 ⁵ y 27 × 10 ⁵ y 28 × 10 ⁵ y 28 × 10 ⁵ y 29 × 10 ⁵ y	4.763 ion ch (2C44); 00 (745); 04 (745); 4.76 ion ch (1839, 1955); 4.76 ion ch (1839, 1955); (3A47)	0.050, 0.117 scint spect (1783h); 11, 0.053, 12, 0.053, 13, 0.18 12, 12, 12, 0.2, 0.4) scint spect (11824); 0.054 (coinc with a. e/y large) 0.054 (coinc with a. e/y large)	C 1384)	natural source, daughter Pa ²³⁴ (UX, and UZ), parent Th ²³⁰ (io)
U ²³⁵	A chem, mass spect (IC31)	0. 715 (IB50)	o; 6 stable (cons ensf gy) (HPS)	7.13 x 10.8 y ap act (12F52); 7.07 x 108 y radiogenic Pb ratios (6N39); spont fission: 1.9 x 1017 y (24552)	4.58 (10%), 4.47 (?) (~3%), 4.40 (18%), 4.20 (4%) ion ch (1051); 4.39 ion ch (15V52)	Y, 0.094, Y ₂ 0.143, Y ₃ 0.184, Y ₄ 0.289, Y ₅ 0.386 (Y ₁ /Y ₂ /Y ₃	O _{G.} 4. 66 (13833) U ²³⁵ , I = \$/2 (102850)	(UV)

		•						OIMP.
	U 235.av (9W45, 19G5la, 135la)	U-n-2n (12M40, SN40, 1W48, 2A44); paren Np ²³⁷ (1W48); daughter Pp. ²⁴ (2K45, 13549); U-a-en (8J49)	natur al source (18B96), parent Th ²³⁴ (UX ₁ )	U-n-v (1M37, 2139, 12M39, 22842); parent Np 239 (12M40a, 22842); U-d-p (13849a)	U-n-v (second order reaction) (4349a); parent Np240 (8H48b)	U ²³⁶ -d-9n, U ²³³ -d-4n, U ²³⁵ -d-6n, parent Pa ²²⁷ (15M50)	U ²³³ -d-3n (15M50)	U ²³³ -d-2n, U ²³⁵ -d-4n (15M50); U ²³³ -p-n (7051)
-	Q _a 4. 56 (13553) U236 * 3774 (MPS)	Qp 0.514 (3F53)	Q. 4. 25 (13853) 236 226 226 000000000000000000000000000	Q _p 1. 28 (3F3) Q _q 4. 12 est (13S3)		Qa 6. 39, QEC l. 92 calc (13553)	Q. 6.04 est, QEC 2.7 est (13553)	Qa 5.63, QEC 1.09 cale (13853)
	-0.030 (coinc with 27% of a) a-coav coinc emula (15D52)	$Y_1$ 0. 027, $Y_2$ 0. 043, $Y_3$ 0. 059, $Y_4$ 0. 165, $Y_5$ 0. 207 (aK/Y 1.6, K/L 5.0), $Y_6$ 0. 269, $Y_7$ 0. 334, $Y_8$ 0. 370, $Y_9$ 0. 430 ( $Y_3/Y_2/Y_7$ 27/212, 5) acins apact, apact corr (1873); 0. 039 c. 7918 apact (aBB52a); 0. 032, 0. 037, 0. 204, 0. 260 aba, apact corre (13M48); 0. 14, 0. 23, 0. 53 aba (17243)	-0.045 (coinc with 22% of a) a-conv coinc emula (15052); 0.046 (coinc with 23% of a) a- conv coinc emula (1252); -0.050 (coinc with 24% of a) a-conv coinc emula (5.452a)	0.0736 spect conv. scint spect (3F53); 0.073 spect conv. abs (5847); 0.076, >0.3 (410%) abs (4F47.			bard y (15M50)	
	4. 499 ion ch (13Gh); 4. 5 ion ch (13Ghb)	0.245, other & (weak) spect (3F53); -0.23 spect (13M48)	4. 21 range (1839)	1. 21 spect (3F53); 1. 20 abs (4F47, 4F47a); 1. 2 abs (W42, 14M42); 1. 12 spect (5647)		6. 28 ion ch (15M50)		5. 53 ion ch (15M50); conv: -0. 3 (15M50)
	2.39 x 10 ⁷ y (12F32); (12F32); 2.46 x 10 ⁷ y 9.5 act (135la)	6. 53 d (31452); 6. 53 d (33448); 6. 8 d (3W48)	4.49 x 10 y ap act 4.51 x 109 y sp act (6N39); acnt fission; 8.0 x 10 ¹⁵ y (2455, 17546)	23. 54 m (14M43); 23. 5 m (4F47, 13M47)	18 h genet (4849a)	-50 m (15M50)	-13 m (15MS0)	35 m (15MS0)
_	c (13G5la); g etable (cons energy) (HPS)	6 (5N40, 12M40)	a; p stable (consenergy) (HPS)	p (12M39)	p_ (4549a)	a (15M50)	EC (15MS0)	EC 99+%, a -10 ⁻³ % (15M50)
			99. 28 (IB50)					
	A chem, n-capt, mass spect (9 W45, 13G3ta)	A chem, excit (5N40 12M40)	A chem, genet, mass spect (IC31)	A n-capt (1M37)	A chem, n-capt (4549a)	A chem, genet, excit, sep isotopes (ISM50)	D chem (15M50)	A chem, excit, sep isotopes (15M50, 7051)
-	or or	U ²³⁷	(U _I )	U239	U ²⁴⁰	13 Np 231	Np 232	Np 233

	77.75		2		Reserv of radiation in Mev	isoloo in Mey		Marked of section 2
Z Z	identification	abundance	decay	Hell-life	Particles	Gamma-transitions	Distangration energy and scheme	genetic relationships
93 Np 234	A chem, excit, genet, sep isotopes (5.149)		EC (L/K-1) (705la); no e (lim 0.01%) (8H49); no p* (8H49)	4. 40 d (8H49); 4. 4 d (5O49)		0.177, 0.442, 0.803, 1.42 spect coav (7051a); 1.9 abs (8H49, 5049)	Qa 5.39 est, QEC 1.8 est	U235_d-3n, U ²³⁵ _a-p4n (83-6); (83-6); U235_a-p-2n (10-64); U233_a-p.n (8449); Pa. ²³³ _a-n (50-49); Pa. ^{233_a} -n (50-49);
	A chem, excit, sep isotopes (8J49)		EC (L/K >9) (8J52); a -5 x 10-3,g (8J52)	410 d (8J52)	5. 06 ion ch (8352)		Q. 5.15, QEC 0.17 calc (13853)	U235-d-2n (8149, 8152); U233-a-pn (8H49)
Np 236	A chem, genet, sep inotopes, excit (8.149)		6 -33%, EC -67% (L/K -2) (7051b)	22 b (8349)	0. 51 (-60%), 0. 36 (-40%) spect (705lb)	0.150 (e/y large) spect conv (705lb)	Q _E 5. 00 est, Q _F 0. 63 est, Q _E C 1. 03 est (13853)	U235-d-n, U235-e-p2n, U-d-4n (8149); Np ²³⁷ -d-p2n (8149); U233-q-p (8149);
							EC	Np="-1 = 25 (1364), 13F50); parent Pu ²²⁶ (8149, 8349a, 8H49, 13G52)
Мр 237m	A genet (103B52)		IT (103B52)	6.3 x 10 ⁻⁸ s delay coinc (103B52)		0.060 scint spect (103B52)	*** Am241 (7051b)	daughter Am ²⁴¹ (103B52)
Np 237	A chem, genet, excit (1W48)		a (1W48); p stable (consenergy) (HPS)	2. 20 × 10 ⁶ y sp act (15M48)	4.77 ion ch (13G48c)	soft y's (coinc with 80% of a) a-conv coinc emuls (15D52); soft y, spect conv (15M45)	Np 237 1 = 5/2 (87M50) Q ₆ 4.97 est (13S53)	daughter U ²³⁷ (1W48); parent Pa ²³³ (15M47)
Z 23	A chem, genet, increast, esp is creast, esp is creast and its contract (13646)		135492)	2. 0 d (13649a);	1, 272 (47%), 0, 258 (53%) spect, spect coinc (3F50a); 1, 39, 0, 22 abs (1J49)	0.043, 0.047, 0.103 (L/M 1.6), 0.983, 1.03 (1.03 γ/0.98 γ = 1) spact, spact conv. β-γ. β-π coinc (13790.); no 0.047 (6)M522, 4A52a); 1.1 abs (1359a); 0.075, 1.2 abs, abs conv (1349)	4. 83 est, Q _p 1. 42, Q _E C 0. 3 est (1353)  est (1353)  No 236  A775  A775  A775  (44686)	U-d-2n (13846, 13849a, 14K49); U ²³⁸ -d-2n (14K49); parent Pu ²³⁸ (13846, 14K49, 1349, 5149); daughter Am ²⁴² (13849, 6850a); Mp ²³⁷ -n-y (1349); Np ²³⁷ -d-p (8349a)

daughter U ²³⁹ (12440a, 22542); parent Pu ²³⁹ (12446, 13549a); U-a-p. (1346, 13549, 1349); U-a-p. (1349, 1349); daughter Am ²⁴³ (6550a)	daughter U ²⁴⁰ (8H48b)	U ²³⁸ -a-p (705ia)	U ²³⁵ -a-7n, U ²³³ -a-5n, parent U ²²⁸ (7051a)		* D	U235-a-3n, U236-a-6n (8J49); Np237-d-3n (8J49a); U233-a-n (8H49, 13P49); daughter Cm240 (13S49b); daughter Np256 (8J49a, 8J49a,	U ²³⁵ -e-2n, U-e-5n (8J49); Np ²³⁷ -d-2n (8J49a)
C 0 . 715 (3773), 14051)	(4A52e)		Qa 6. 70, QEC 0. 96 est (13553)	Q 6. 30, Q _{EC} 0. 21 est (13553)	Q. 5.95, Q.E.C 1.14 calc (13853)	Q _a 5. 85 (13853) P ₂ 236	Qu 5. 72 est, QEC 0. 21 est
(coinc with 0.210 y), 0.210, 0.210, 0.221, 0.276   task 0.276 y are coinc with 0.435 \$\vec{p}\), 0.276 y are coinc with 0.435 \$\vec{p}\), 0.276 y are coinc with 0.435 \$\vec{p}\), 0.276 y are coinc with 0.437 \$\vec{p}\), 0.276 y are coinc (14631); 0.64, 0.049, 0.037, 0.081, 0.067, 0.077, 0.105, 0.209, 0.228, 0.277, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.049, 0.057, 0.061, 0.049, 0.079, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.289, 0.287, 0.049, 0.057, 0.061, 0.057, 0.061, 0.057, 0.057, 0.061, 0.057, 0.057, 0.061, 0.057, 0.057, 0.061, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0.057, 0		0.15, 0.20, 0.26, 0.56 spect conv (705la); -0.7 abs (705la)				-0.045 (coinc with 20% of a) a-conv coinc emula (15052)	К, L-ж, во ү (8.349)
0. 715, 0. 654, 0. 44, 0. 33 spect (773); 0. 78 (4. 5%), 0. 655 (1. 7%), 0. 78 (4. 13%), 0. 350 (10%), 0. 355 (2. %) spect (375.) spect (3547); 0. 676, 0. 403, 0. 288 spect (3547); 0. 676, 0. 403, 0. 288 spect others (22H45, 11749)	-1. 3 abs (8H48a)	0. 89 spect (705ia)	6. 58 ion ch (705ia)	6. 19 ion ch (7051a); 6. 2 ion ch (13P49)	5. 85 ion ch (705la)	5. 75 range sir (8349); 5. 75 ion ch (13G53)	
2. 33 d (1942); 2. 34 (3946)	7.3 m (8H48b)	60 m (705ia)	36 m (7051a)	9.0 b (705la); 8.5 h (13P49)	26 m (705la)	2.7 y (8149); spont fission: 3.5 = 10 ⁹ y (13G52)	-40 d (8349)
p. (122440a)	6 (8H48b)	p (705ia)	6 > 2 %, EC 698% (705la)	a -4%, EC -96% (7051a, 23H52a)	EC 99+%, e -0.002% (7051a)	a (8J49); p stable (cons energy) (HPS)	EC (8349)
Mp 239 A chem, n-capt, genet, excit (12M39, 12M40a)	Np ²⁴⁰ A chem, genet (8H46b)	Np 241 B chem, cross bomb (705la)	94Pu ²³² B chem, sep isotopes, excit, sent (705ls)	Pu ²³⁴ A chem, genet, sep lactopes, excit (8H49, 13P49)	Pu ²³⁵ B chem, excit, exp isotopes (7051a)	Pu ²³⁶ A chem, excit, sep isotopes, cross bomb, genet (8149)	Pu ²³⁷ B chem, sep isotopes, cross bomb (8149)

1	Page 440	Person	Trans		Recent of radiation in Mev	edos is Mev		Method of sendantine and	• •
Z Z	identification		decay	Helf-life	Particles	Genera-transitions	Disintegration energy and scheme	generic relationships	
94 Pu 236	A chem. sep laotopes axcit (13846, 13846s, 13849s)		a (13946); f stable (cons ens (N) (HPS)	89. 6 y (1356); 92. y genet (13549b); 77 y genet (1149); sport fission; 3. 8 x 10 ¹⁰ y (2455)	5, 492 (16%), 5, 450 (24%) spect (4A52a); (4A52a); 5, 47 range air (8749); 5, 51 range air (15C47)	0. 045 spect come (BOS1); -0. 040 (colac with 23% of a) a-cone colac smuls (15%); -0. 04 (a/y -700) a-y coinc, scint spect (4A52d)	Ca 5. 586 (13553) Pu238 244, 244, 244, 484	U238-d-fn (13846, 13849a, 14K49, 7E42, 8149); U296-a-da, U259-a-n (8149); daughter Np 218 (8149, 1149, 13846a, 14K49); daughter Cm ²⁴² (13849b)	
Pu 239m	A genet (14G51)		IT (14051)	1.1 x 10 ⁻⁹ s delay coisc (14G51)		0.049, 0.067, 0.210, 0.227, 0.276 spect comy, coinc (i4G5))	÷ 5 4	daughter Np ²³⁹ , parent Pu ²³⁹ (14G31)	
P. 239	A chem. genet, mass spect (146(46)		a (14K46); f stable (cons anns (17) (HPS)	7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	5. 150 (69%), 5.137 (20%), 5. 099 (11%) spect (44.52a); 5. 147 (-70%), 5. 097 (-10%) spect (44.80); 5. 14 one ch (10.74); 5. 15 one ch (10.74); 5. 13 one ch (17.73); 5. 13 one ch (17.73); 5. 13 cone and (17.73); cone: -0.10 (week) a-conv coinc emula (15.05; 5.451)	10.039, γ ₂ 0.0531, γ ₃ 0.100, γ ₄ 0.124, γ ₅ 0.34 (γ ₁ /γ ₂ /γ ₃ /γ ₄ /γ ₅ γ ₅ π 0.4/1.4/1.1/0.5/0.3 spect core, scine spect (3F52b); 0.0385 (2 π 10 ⁻³ %), 0.0520 (7 π 10 ⁻³ %) son π (18 W5), 12 W521; (18 D53), 0.05 π - core coinc smule (18 D52); 0.05 π - core coinc smule 0.05 π - core coinc smule	Q_ 5. 238 (13853) Q_ 5. 238 (13853) Pure (14651) Q_ 60091	daugker Np 239 (14K46, 13549a); U ²³⁸ aa-3n (8349); Pu ²³⁸ -n-y (9K48, 19B48)	
Pu 240	A chem, n-capt, mars spect (15C4, 14746, 21844)		a (8349); 6 stable (cone energy) (NFB)	(24852) 6580 y genet (1131); (2300 y sp act (11951); (5760 y sp act	5.162 (76%), 5.118 (24%) spect (4A52e)	0.0496 spect conv. scint spect (3F52b)	(4A520,HPS) (4A520,HPS) 0 ₆ 5. 250 (4A52a) p ₁₂ 840 6 7854	Pu ²³⁹ -a-y (15C44, 14F46, 21B44): U ²³⁶ -a-2n (6349)	TONC I
P. 241	A cham, n-capt, mae a spect, extit, genet (13549, 13549b, 13650)		6 99+#, a -10-3# (13849, 3T50e)	14 y genet (3T50a)	a; 4.91 ton ch (3750e); f): 0.021 spect (3752b); -0.02 abs (13549)	ν ₁ 0.100, γ ₂ 0.145 (γ ₁ /γ ₂ = 5) scint spect (3F52b)	Q _a 5.15, Q _b 0.021 (13553)	Pu ²⁴⁰ -n-y (13G50, 3750e); U ²³⁸ -a-n (13649); parent Am ²⁴¹ (13849, 16C49a); parent U ²³⁷ (2K45, 13849)	ON PHIORO

Pu ²⁴¹ .n-y (3T50a, 3149); daughter Am ^{242m} (8050a)	Pu ²⁴² -n-y (2885), 3751); parent Am ²⁴³ (3751)	Pu ²³⁹ -d-4n, Pu ²³⁹ -p-3n (23H52a)	Pu ²³⁹ -d-3n (6550a, 23H52a)	Np 237 -a-2n (13849); Pu239 -p-n (6850a); Pu239 -d-2n (13849, 23H52a); Pu239 -a-p3n (23H52a)	Np 237-a-n (13649); Pu 239-d-n (13649, 6850a, 23H52a); Pu 239-a-p2n (23H52a)	daughter Pu ²⁴¹ (13549,16C49a); parent Np ^{237m} (103B52)
Q. 4. 96 (13853)	O. 4. 82 est, O. 67 est (13853)	Q. 6. 20 est, QEC 1.6 est (13853) Pu.239-d-4n, Pu.239-p-3n	Q _{a.} 5.99 est, Q _{EC} 2.22 est (1353)	Qa 5.85, QEC 0.78 calc (13553)	Q _a 5. 76 est, Q _b 0.02 est, Q _{EC} 1. 54 est (13553)	Am 241 1 = 5/2 (138752) Qu 5. 639 (13853) Am 241  Left (0.170 04%  Am 241  Am
	0.095, 0.12 spect conv (3751)			0. 3 (10%) scint spect (23H52a); 0. 3 abs conv (13849)	no y >0. 7 (23H52a)	γ ₁ 0.0597 (40%, e/γ ¢l. 5, with Np 217m), γ ₂ 0.0263 (2.6%, e/γ ¢20), γ ₃ 0.0269, γ ₄ 0.0173, γ ₅ 0.035 (γ ₁ /γ ₁ /γ ₂ /γ ₃ /γ ₄ /γ ₅ = 1/0.069/0.155/0.36/0.32) ion ch, a-γ delay coinc (103B5.); γ ₁ 0.0598, γ ₂ 0.0264 (γ ₁ /γ ₂ /γ ₃ /γ ₄ = 1/0.0598, γ ₂ 0.0264 (γ ₁ /γ ₂ /γ ₃ /γ ₄ = 1/0.0598, γ ₂ 0.0264 (γ ₁ /γ ₂ /γ ₃ /γ ₄ = 1/0.0590, 0.0414, 0.0264 spect conv., scint spect (3F5.E); others (13849, BOS1, 3F9.1, 15D5.2)
-5 x 10 ⁵ y genet (3T50e)	0.39 spect (3TSI); -0.45 abs (25851)	-1. 3 h (23H52a) 6. 01 ion ch (23H52a)	conv (6550a)	5. 75 ion ch (23H52a)		5. 546 (0. 23%), 5. 535 (0. 34%), 5. 503 (0. 24%), 5. 476 (84. 2%), 5. 476 (84. 2%), 5. 579 (1. 4%), 5. 58 ion ch (13G48c); 5. 47 range air (8T49)
-5 x 10 ⁵ y genet (3T50e)	4.98 b (81H52a); 5.0 b (2585), 3T51)	-1. 3 h (23H52a)	2.1 h (23H52a) conv (6550a)	12 h (13549)	50 h (13 <b>54</b> 9); 53 h (23H52a)	470 y sp. act (20452a); 473 y sp. act (16C50)
4 (3750e); p stable (cons energy) (HPS)	ه ( (2585)	EC 99+%. a 0.005% (23H52a)	EC (6850a); no a (lim 3 x 10-4 g; (23H52a)	EC 99+%, a 0.003% (23H52a)	EC (13849); no a (lim 0.2%) (23H52a)	e (13849); p stable (consensity) (HPS)

A chem, mass spect, n-capt, genet (3T50s)	B chem, n-capt, cross bomb (25851)	B chem, excit (23H52a)	B chem, excit (6850a)	B chem, excit (13849)	B chem, excit (13849); chem, excit, cross bomb (6550s)	A chem, n-capt, excit, mass spect (13549)	
Pu 242	P. 243	95Am ²³⁷	Am 238	Am ²³⁹	Am 240	Am 241	

0. 623 abs (15G20) 0. 63 abs (13G40) 0. 64 abs (13G40) 0. 65 acint apsect (49M52a) 0. 65 acint apsect (89M52a) 0. 65 acint apsect (89M52a)	16.01 h	16. 01 h (44K52) 15. 74 15. 74 15. 74 16 h (16M49) (6850a) (6850a) (6850a)  2. 5 h (68
(-10%) spect		2 -
	92 (q	
	3	2 0
		252)
		_
	<u> </u>	26. 8 d (13549b); 6. 25 ton ch (23H52); 9pont fission: 6. 3 range air (13549b) 7. 9 x 10 ⁵ y (13G52)
	<u> </u>	35 d (23H52) 5.90 ion ch (23H52a)
(26.3%), 0.043 spect conv (8031); -0.04 (6/4 - 600) a-v coinc, scint spect (4532); -0.045 (coinc with 23% of a) -0.045 (coinc with 23% of a) -0.045 (coinc with a) aconv coinc (5P91)	950; 920; 950;	162.5 d (24850), 6. 110 (73.7%), 6. 066 (26.3%), 5. 066 (20.3%), 5. 065 (0.03%) spect (4452, 162 d (13484)), 6. 118 ion ch (13G48c) (24851)

Cm ²⁴² .n.v (10R50); daughter Bk ²⁴³ (3T50b)	daughter Am ²⁴⁴ . Cm ²⁴³ -n-y (10R50)	daughter Bk ²⁴⁵ (25H51)	Am ²⁴¹ -a-2n (3T50, 3T50b); Cm ²⁴² -d-n (25H51); parent Cm ²⁴³ (3T50b)	Am ²⁴¹ -a-n (3T52)	Am ²⁴³ -a-2n (3T52); Cm ²⁴⁴ -d-n, Cm ²⁴² -a-p (2H51); parent Cm ²⁴⁵ (25H51)	U-C-6n (13G3ic);	U-C-4n (13G51c); Cm ²⁴³ -an, Cm ²⁴⁴ -a-2n (25H51); parent Cm ²⁴² (25H51)
GE 6. 15 (4A52a) GEC 0. 00 calc (1353) eee Np239, Pu239m GE 60.594	Q 5. 895 (13853) Q 5. 895 (13853) Q 643 Q 643 Q 643 Q 643 Q 643 Q 643 Q 643		Qa 6. 83, QEC 1. 46 calc (13553)	Q _{a.} 6. 63 est, Q _{EC} 2. 27 est (13553)	Q. 6. 44, QEC 0. 67 est (13553)	Q. 7.27, QEC 0.7 est (13553)	Q, 6. 86 (13553)
0. 226, 0. 277 (both y's coinc with 5. 777 a) scint spect (4A52d)							
5.985 (6. 4%), 5.777 (80.5%), 5.732 (13.1%) spect (4652d); 5.89 (15%), 5.79 (85%) ion ch (3T50b)	6.798 (75%), 5.755 (25%) spect (4.828d)	-5.6 ion ch (25H51)	6.72 (30%), 6.55 (53%), 6.20 (17%) ion ch (3T50b)		6.33 (18%), 6.15 (48%), 5.90 (34%) ion ch (25H51)	7. 15 ion ch (3T50d)	6. 75 ion ch (13G51c)
(3150b)	19 y (1752); epont fireion: 1. 4 x 10 ⁷ y (13G52)	>500 y (25H51)	4.6 b (3T50b)	-5 h (3T52)	4. 95 d (25H51)	45 m (3T50d)	2000 y (a pontane ous fission) (25H53)
• (10R50)	a (10R50); B stable (cons energy) (HPS)	a (25H51)	EC 99+%, a -0.1% (3T50b)	EC (3T52)	EC 99+%, a - 0.1% (25H51)	a. EC (7)	a (13GS1c); ß stable (cons energy) (HPS)
A chem, mass spect, genet (10R50)	A chem, mass spect (10K50)	5 B chem, decay charac, genet (25H51)	<	D chem, decay charac (3T52)	S B chem, excit, decay charac (25H51)	M chem, excit,	(3750c) A chem, genet (13G51c)
Cm 243	**************************************	Cm 245	97Bk ²⁴³	Bk 244	Bk ²⁴⁵	98 ^{Cf.244}	2 ⁵ 46

## RAPID METHOD FOR CALCULATING LOG (ft) VALUES

from S. A. Moszkowski, Phys. Rev. 82, 35 (1951)

The following figures permit the rapid calculation of log (ft) for a given type of decay, given energy, half-life, etc. The notation is:  $E_0$  for  $\beta^{\pm}$  emission is the maximum kinetic energy of the particles in Mev;  $E_0$  for K electron capture is the disintegration energy in Mev. When a  $\beta^{+}$  emission and K electron capture go from and to the same level,  $E_0$  for K capture =  $E_0$  for  $\beta^{+}$  emission + 1.02 Mev. Z is the atomic number of the initial nucleus, t is the total half-life, and p is the percentage of decay occurring in the mode under consideration. When no branching occurs, p = 100.

## Procedure for obtaining log (ft)

- (1) First obtain  $\log (f_0 t)$ , using Fig. 1.  $E_0$  is read off the left-hand side of the  $E_0$  column for K electron capture, and off the right-hand side for  $\beta^{\pm}$  emission. Put a straight edge over the given values of  $E_0$  and t and note where it crosses the column of  $\log (f_0 t)$  values.
- (2) Then read off log (C) from Figs. 2, 3, and 4 for β⁻, β⁺, and K electron capture, respectively.
- (3) Get  $\triangle \log$  (ft) from Fig. 5 if p <100. When p = 100,  $\triangle \log$  (ft) = 0.
- (4) Log (ft) =  $\log (f_0 t) + \log (C) + \Delta \log (ft)$ .

These graphs have been reproduced with the kind permission of Dr. Moszkowski. For details concerning their construction, significance, and range of usefulness, reference should be made to the original paper.

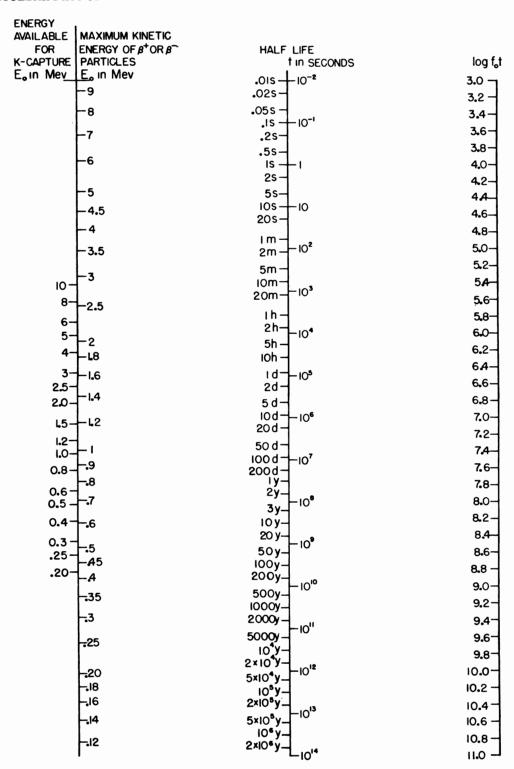


Fig. I. Log ( $f_0$ t) as a function of  $E_0$  and t.

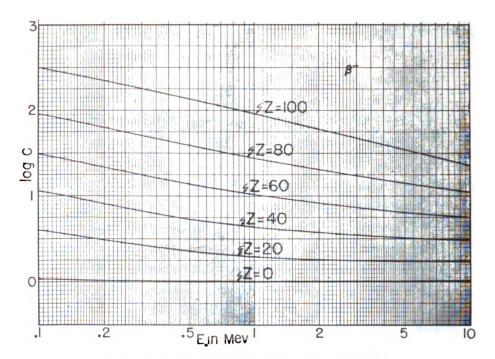


Fig. 2. Log (C) as a function of  $E_0$  and Z for  $\beta$  emission.

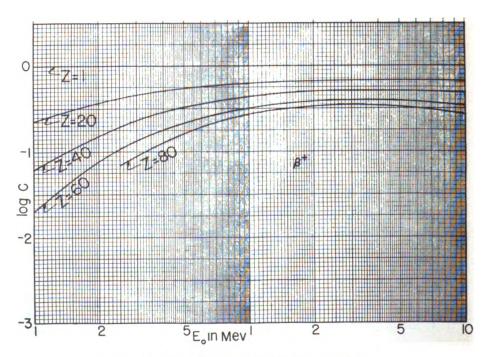


Fig. 3. Log (C) as a function of  $E_0$  and Z for  $\beta^+$  emission.

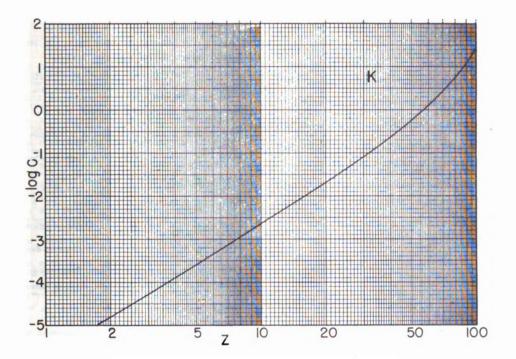


Fig. 4. Log (C) as a function of Z for K electron capture.

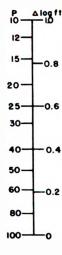


Fig. 5.  $\triangle \log (ft)$  as a function of p.

1A20	F. W. Aston, Phil. Mag. 40, 628 (1920)	13A52b	D. E. Alburger, Phys. Rev. (to be published) (1952)
1A35	F. W. Aston, Proc. Roy. Soc. (London) <u>149A</u> , 396 (1935)	14A48	H. R. Allan and C. A. Wilkinson, Proc. Roy. Soc. (London) 194A, 131 (1948)
2A44	M. B. Allen, University of California Radiation Laboratory Classified Report RL-4.6. 270 (July 1944)	15A40	W. D. Allen and C. Hurst, Proc. Phys. Soc. (London) 52, 501 (1940)
3'A47	F. Alder, P. Huber, and F. Metsger, Helv. Phys. Acta 20, 234 (1947)	16A50	H. M. Agnew, Phys. Rev. 77, 655 (1950)
3A51	F. Alder and F. C. Yu, Phys. Rev. 81, 1067 (1951)	17A36	E. B. Andersen, Z. physik. Chem. 32B, 237 (1936)
3A51a	F. Alder and F. C. Yu, Phys. Rev. 82, 105 (1951)	17A36a	E. B. Anderson, Nature 137, 457 (1936)
4A52	F. Asaro, F. L. Reynolds, and I. Perlman, Phys.	18A48	R. D. Albert and C. S. Wu, Phys. Rev. 74, 847 (1948)
4A52a	Rev. 87, 277 (1952)  F. Asaro and I. Perlman, private communication	19.41	H. Akabori, et al., Proc. PhysMath. Soc. Japan 23, 599 (1941)
	(Nov. 1952)  F. Asaro and W. J. Heiman, private communication  (Nov. 1952)	20A48	L. H. Ahrens and R. D. Evans, Phys. Rev. <u>74</u> , 279 (1948)
4A52b	(Aug. 1952)	21A41	J. S. V. Allen, M. L. Pool, J. D. Kurbatov, and L. L. Quill, Phys. Rev. 60, 425 (1941)
4A52c	F. Asaro and I. Perlman, Phys. Rev. 88, 129 (1952)	22A40	T. Amaki, T. limori, and A. Sugimoto, Phys. Rev.
4A52d	F. Asaro, S. G. Thompson, and I. Perlman, private communication (Nov. 1952)		57, 751 (1940)
4A52e	F. Asaro and I. Perlman, Phys. Rev. 88, 828 (1952)	23A47	J. R. Arnold and N. Sugarman, J. Chem. Phys. <u>15,</u> 703 (1947)
5.A51	G. Albouy and J. Teillac, Compt. rend. 232, 326 (1951)	24A36	A. I. Alichanian, A. I. Alichanov, and B. S. Dehelepov, Physik. Z. Sowjetunion 10, 78 (1936)
5A52	G. Albouy, J. phys. et radium 13, 309 (1952)	25A39	A. H. W. Aten, Jr., C. J. Bakker, and F. A. Heyn, Nature 143, 679 (1939)
5A52a	G. Albouy and J. Teillac, Compt. rend. <u>234</u> , 829 (1952)	25A52	A. H. W. Aten, Jr. and M. Boelhouwer, Physica 18, 651 (1952)
6A38	L. W. Alvares, Phys. Rev. 54, 486 (1938)	26A51	R. M. Adams and H. Finston, NNES-PPR 9, 1791 (1951)
6A39	L. W. Alvares and R. Cornog, Phys. Rev. <u>56</u> , 613 (1939)	27A39	_
6A40	L. W. Alvares, A. C. Helmhols, and E. Nelson, Phys. Rev. <u>57</u> , 660 (1940)		H. L. Anderson, E. Fermi, and H. B. Hanstein, Phys. Rev. 55, 797 (1939)
		28A43	M. Ageno, Nuovo cimento 1, 33 (1943)
6A40a	L. W. Alvares and R. Cornog, Phys. Rev. <u>57</u> , 248 (1940)(A)	28A43a	M. Ageno, Nuovo cimento 1, 415 (1943)
6A49	L. W. Alvarez, Phys. Rev. 75, 1815 (1949)	29A52	P. Axel and R. B. Duffield, private communication (Oct. 1952)
6A49a	L. W. Alvares, Phys. Rev. 75, 1127 (1949)	30A38	K. Alexeeva, Compt. rend. U. R. S. S. 18, 553 (1938)
6A50 7A46	L. W. Alvaren, Phys. Rev. <u>80</u> , 519 (1950)  L. T. Aldrich and A. O. Nier, Phys. Rev. <u>70</u> , 983	31A50	N. M. Anton eva, A. A. Bashilov, B. S. Dzhelepov, and A. V. Zolotavin, Doklady Akad. Nauk, S. S. S. R. 70, 397 (1950)
1240	(1946)	31.A50a	<del></del>
8A50	P. Avignon, J. phys. et radium 11, 521 (1950)		N. M. Anton'eva, A. A. Bashilov, B. S. Dahelepov, and A. V. Zolotavin, Doklady Akad. Nauk, S. S. S. R. 70, 597 (1950); Isv. Akad. Nauk, S. S. S. R. 14, 299
9A50	R. Ashapa and G. Grimm, reported in Columbia University Document CUD-53 (June 1950)		(1950)
10A49	J. Angus, A. L. Cockroft, and S. C. Curran, Phil. Mag. <u>40</u> , 522 (1949)	31A51	N. M. Anton'eva, A. A. Bashilov, and B. S. Dahelepov, Doklady Akad. Nauk, S.S.S.R. 77, 41 (1951)
11A50	R. E. Adamson, Jr., W. W. Buechner, W. M.	32A39	P. Abelson, Phys. Rev. <u>56</u> , 1 (1939)
	Preston, C. Goodman, and D. M. Van Patter, Phys. Rev. 80, 985 (1950)	33A50	D. L. Anderson and M. L. Pool, Phys. Rev. <u>77,</u> 142 (1950)
12A35	E. Amaldi, O. D'Agostino, E. Fermi, B. Pontecorvo, R. Rasetti, and E. Segre, Proc. Roy. Soc. (London) 149A, 522 (1935)	34A45	H. Atterling, E. Bohr, and T. Sigurgeirsson, Arkiv Mat., Astron. Fysik 32A, No. 2 (1945)
12A36	E. Amaldi and E. Fermi, Ricerca sci. 7, Part I, 56 (1936)	35A50	K. Artemov and B. Dshelepov, Uspekhi Fis. Nauk 41, 189 (1950)
13A49	D. E. Alburger, Phys. Rev. 76, 435 (1949)	36A51	H. Aeppli, A. S. Bishop, H. Frauenfelder, M. Walter and W. Zunti, Phys. Rev. 82, 550 (1951); Helv. Phys.
13 <b>A</b> 50	D. E. Alburger, C. Eggler, and D. J. Hughes, Phys. Rev. 77, 726 (1950)	36A51a	Acta 24, 355 (1951)  H. Aeppli, H. Albers-Schönberg, A. S. Bishop, H. Frauenfelder, and E. Heer, Phys. Rev. 84, 370
13A50a	D. E. Alburger, Phys. Rev. 78, 629 (1950)		H. Frauenfelder, and E. Heer, Phys. Rev. 84, 370 (1951)
13A50b	D. E. Alburger, E. der Mateosian, G. Friedlander, M. Goldhaber, J. W. Mihelich, G. Scharff-Goldhaber, and A. W. Sunyar, reported in Brookhaven National	36A52	H. Aeppli, H. Frauenfelder, E. Heer, and R. Ruetschi, Phys. Rev. 87, 379 (1952)
	Laboratory Unclassified Report BNL-82 (Nov. 1950)	36A52a	H. Aeppli, H. Albers-Schoenberg, H. Frauenfelder, and P. Scherrer, Helv. Phys. Acta 25, 339 (1952)
13 <b>A</b> 50c	D. E. Alburger, E. der Mateosian, and M. Goldhaber, reported in Brookhaven National Laboratory Unclassified Report BNL-64 (July 1950)	37A52	C. J. Avery, K. C. Kaericher, and M. L. Pool, Phys. Rev. 87, 216 (1952)(A)
13A51	D. E. Alburger and G. Friedlander, Phys. Rev. 82, 977 (1951)	38A52	C. E. Anderson, G. W. Wheeler, and W. W. Watson, Phys. Rev. 87, 668 (1952)
13A5la	D. E. Alburger and G. Friedlander, Phys. Rev. <u>81</u> , 523 (1951)	39A52	G. B. Arfken, E. D. Klema, and F. K. McGowan, Phys. Rev. 86, 413 (1952)
13A52	D. E. Alburger, Phys. Rev. 88, 339 (1952)	40A52	D. P. Ames, M. E. Bunker, and L. M. Langer,
13A52a	D. E. Alburger and J. Kraushaar, Phys. Rev. 87,		Phys. Rev. (in press) (1952)

13A52a D. E. Alburger and J. Kraushaar, Phys. Rev. 87, 448 (1952)

- 40A52a D. P. Ames, M. E. Bunker, and J. W. Starner, reported in Los Alamos Scientific Laboratory Classified Report WASH-75 (Jan. 1952)
- 40A52b D. P. Ames, M. E. Bunker, and B. M. Sorensen, reported in Los Alamos Scientific Laboratory Classified Report WASH-66 (March 1952)
- 1B50 K. T. Bainbridge and A. O. Nier, National Research Council Nuclear Energy Series, Preliminary Report No. 9 (Dec. 1950)
- 1B52 K. T. Bainbridge, M. Goldhaber, and E. Wilson, private communication (Oct. 1952)
- 2B50 M. E. Bunker, L. M. Langer, and R. J. D. Moffat, Phys. Rev. 80, 468 (1950)
- 2B50a M. E. Bunker and R. Canada, Phys. Rev. <u>80</u>, 961 (1950)
- 2B50b M. E. Bunker, R. Canada, and A. C. G. Mitchell, Phys. Rev. 79, 610 (1950)
- 2B51 M. E. Bunker, L. M. Langer, and R. J. D. Moffat, Phys. Rev. <u>81</u>, 30 (1951)
- 2B52 M. E. Bunker and J. W. Starner, reported in Los Alamos Scientific Laboratory Classified Report WASH-76 (May 1952)
- 3B44 M. Bachelet and P. Savel, Cahiers phys. No. 19, 51 (1944)
- 4B48 D. E. Bunyan, A. Lundby, A. H. Ward, and D. Walker, Proc. Phys. Soc. (London) 61, 300 (1948)
- 4B49 D. E. Bunyan, A. Lundby, and D. Walker, Proc. Phys. Soc. (London) 62A, 253 (1949)
- 5B49 W. H. Beamer and W. E. Easton, J. Chem. Phys. 17, 1298 (1949)
- 6B39 E. Bretecher and L. G. Cook, Nature 143, 559 (1939)
- 6B40 E. Bretscher and L. G. Cook, Nature 146, 430 (1940)
- 7B47 E. Broda and N. Feather, Proc. Roy. Soc. (London) 190A, 20 (1947)
- 8B48 R. E. Bell and L. G. Elliott, Can. J. Research 26A, 379 (1948)
- 8B49 R. E. Bell and H. E. Petch, Phys. Rev. <u>76</u>, 1409 (1949)
- 8B50 R. E. Bell and R. L. Graham, Phys. Rc 78, 490 (1950)
- 8B52 R. E. Bell and R. L. Graham, Phys. Rev. <u>86</u>, 212 (1952)
- 8B52a R. E. Bell, R. L. Graham, and H. E. Petch, Can. J. Phys. 30, 35 (1952)
- 8B52b R. E. Bell, R. L. Graham, and L. Yaffe, Can. J. Phys. (in press) (1952)
- 9B50 G. R. Bishop, R. Wilson, and H. Halban, Phys. Rev. 77, 416 (1950)
- 10B46 G. C. Baldwin and G. S. Klaiber, Phys. Rev. <u>70</u>, 259 (1946)
- 10B49 G. C. Baldwin, Phys. Rev. 76, 182 (1949)(A)
- 11B49 P. R. Bell, B. H. Ketelle, and J. M. Cassidy, Phys. Rev. <u>76</u>, 574 (1949)
- llB49a P. R. Bell and J. M. Cassidy, reported in Oak Ridge National Laboratory Unclassified Report ORNL-481 (Dec. 1949)
- 11B50 P. R. Bell, Science 112, 7 (1950)
- 11B50a P. R. Bell and J. M. Cassidy, Phys. Rev. <u>77</u>, '301 (1950)
- 11B50b P. R. Bell and J. M. Cassidy, Phys. Rev. <u>79</u>, 173 (1950)
- llB50c P. R. Bell, B. Weaver, and J. M. Cassidy, Phys. Rev. <u>77</u>, 399 (1950)
- P. R. Bell, J. M. Cassidy, W. H. Jordan, and R. C. Davis, Oak Ridge National Laboratory Classified Report ORNL-782 (Oct. 1950)

- 11B50e P. R. Bell, J. M. Cassidy, and R. C. Davis reported in Oak Ridge National Laboratory Unclassified Report ORNL-694 (June 1950)
- 11B50f P. R. Bell, J. M. Cassidy, W. H. Jordan, and R. C. Davis, reported in Oak Ridge National Laboratory Unclassified Report ORNL-782 (Oct. 1950)
- 11B51 P. R. Bell, J. M. Cassidy, and G. G. Kelley, Phys. Rev. 82, 103 (1951)
- 11B52 P. R. Bell, R. C. Davis, J. E. Francis, and J. Cassidy, reported in Oak Ridge National Laboratory Unclassified Report ORNL-1092 (Jan. 1952)
- IIB52a P. R. Bell, R. C. Davis, J. E. Francis, and J. M. Cassidy, reported in Oak Ridge National Laboratory Unclassified Report ORNL-1164 (April 1952)
- 12B51 G. W. Barton, Jr., A. Ghiorso, and I. Perlman, Phys. Rev. 82, 13 (1951)
- 13B24 D. H. Black, Proc. Roy. Soc. (London) 106A, 632
- 14B49 D. K. Butt, unpublished data quoted in (4F49)
- 14B51 D. K. Butt and W. D. Brodie, Proc. Phys. Soc. (London) 64A, 791 (1951)
- 15B36 G. H. Briggs, Proc. Roy. Soc. (London) <u>157A</u>, 183 (1936)
- 16B43 H. Bradt and P. Scherrer, Helv. Phys. Acta 16, 259 (1943)
- 16B43a H. Bradt, H.-G. Heine, and P. Scherrer, Helv. Phys. Acta 16, 455 (1943)
- 16B45 H. Bradt and P. Scherrer, Helv. Phys. Acta 18, 405 (1945); and private communication to R. W. Stoughton (Feb. 1947)
- 16B45a H. Bradt, P. C. Gugelot, O. Huber, H. Medicus, P. Preiswerk, and P. Scherrer, Helv. Phys. Acta 18, 259 (1945)
- 16B45b H. Bradt, P. C. Gugelot, O. Huber, H. Medicus, P. Preiswerk, and P. Scherrer, Helv. Phys. Acta 18, 252 (1945)
- 16B45c H Bradt, P. C. Gugelot, O. Huber, H. Medicus, P. Preiswerk, and P. Scherrer, Helv. Phys. Acta 18, 256 (1945)
- 16B45d H. Bradt, P. C. Gugelot, O. Huber, H. Medicus, P. Preiswerk, and P. Scherrer, Phys. Rev. 68, 57 (1945)
- 16B45e H. Bradt, P. C. Gugelot, O. Huber, H. Medicus, P. Preiswerk, and P. Scherrer, Helv. Phys. Acta 18, 351 (1945)
- 16B46 H. Bradt and P. Scherrer, Helv. Phys. Acta 19, 307 (1946); Phys. Rev. 71, 141 (1947) (A)
- 16B46a H. Bradt, P. C. Gugelot, O. Huber, H. Medicus, P. Preiswerk, P. Scherrer, and R. Steffen, Helv. Phys. Acta 19, 219 (1946)
- 16B46b H. Bradt, P. C. Gugelot, O. Huber, H. Medicus, P. Preiswerk, P. Scherrer, and R. Steffen, Helv. Phys. Acta 19, 222 (1946)
- 16B46c H. Bradt, P. C. Gugelot, O. Huber, H. Medicus, P. Preiswerk, P. Scherrer, and R. Steffen, Helv. Phys. Acta 19, 218 (1946)
- 16B47 H. Bradt, P. C. Gugelot, O. Huber, H. Medicus, P. Preiswerk, P. Scherrer, and R. Steffen, Helv. Phys. Acta 20, 153 (1947)
- 16B47a H. L. Bradt and D. J. Tendam, Phys. Rev. <u>72</u>, 1117 (1947)
- 17B43 E. L. Brady and W. Rubinson, reported in Metallurgical Laboratory Classified Report CC-724 (June 1943)
- 17B50 E. L. Brady and M. Deutsch, Phys. Rev. 78, 558 (1950)
- 17B51 E. L. Brady and N. Sugarman, NNES-PPR 9, 613 (1950)
- 17B5la E. L. Brady, D. W. Engelkemeir, and E. P. Steinberg, NNES-PPR 9, 711 (1951)
- 18B96 H. Becquerel, Compt. rend. 122, 420, 501, 559, 609, 762, 1086 (1896)
- 19B48 R. J. Bruehlman, W. C. Bentley, and E. K. Hyde, reported in Argonne National Laboratory Classified Report ANL-4215 (Oct. 1948)

20B52	Berkeley Chemistry Group, unpublished results (1947-1952)	36B50a	H. Brown and V. Peres-Mendes, Phys. Rev. 78, 812 (1950)
21B44	A. A. Bartlett, D. F. Swinehart, and R. W. Thompson, Los Alamos Scientific Laboratory Classified Reports LA-168 (Nov. 1944); LA-327 (July 1945); LA-561	37B37 37B37a	W. Bothe and W. Gentner, Z. Physik 106, 236 (1937) W. Bothe and W. Gentner, Naturwiss. 25, 90, 126,
225.40	(May 1946)	170.10	191 (1937)
22B49	W. J. Byatt, F. T. Roger, Jr., and A. Waltner, Phys. Rev. 75, 909 (1949)	37B39 37B41	W. Bothe and W. Gentner, Z. Physik 112, 45 (1939)  W. Bothe and A. Flammersfeld, Naturwiss. 29,
23B36	T. Bjerge, Nature 137, 865 (1936)	J.2	194 (1941)
23B36a	T. Bjerge, Nature 138, 400 (1936)	37B43	W Bothe, Naturwiss. 31, 551 (1943)
23B36b	T. Bjerge and K. J. Broström, Nature 138, 400 (1936)	37B46	W. Bothe, Z. Naturforsch. 1, 179 (1946)
23B37	T. Bjerge, Nature 139, 757 (1937)	37B46a	W. Bothe, Z. Naturforsch. 1, 173 (1946)
24B 30	S. Bramson, Z. Physik <u>66</u> , 721 (1930)	38B40	J. C. Bower and W. E. Burcham, Proc. Roy. Soc. (London) 173A, 379 (1940)
25B39	R. A. Becker and E. R. Gaerttner, Phys. Rev. <u>56</u> , 854 (1939) (A)  R. A. Becker, A. O. Hanson, and B. C. Diven,	39B48	H. Bradner and J. D. Gow, Phys. Rev. 74, 1559 (1948) (A)
25B47	Phys. Rev. 71 466 (1947) (A)	40B39	K. J. Broström, J. Koch, and T. Lauritsen, Nature 144, 830 (1939)
25B49	R. A. Becker, F. S. Kirn, and W. L. Buck, Phys. Rev. 76, 1406 (1949)	40B47	K. J. Broström, T. Huus, and J. Koch, Nature 160, 498 (1947)
26B37	D. S. Bayley and H. R. Crane, Phys. Rev. <u>52</u> , 604 (1937)	41B46	D. S. Ballantine, reported in Oak Ridge National Laboratory Classified Report Mon N-150 (Aug. 1946)
27B48	T. W. Bonner, J. E. Evans, C. W. Malich, and J. R. Risser, Phys. Rev. 73, 885 (1948)	42B51	R. E. Batsel and G. T. Seaborg, Phys. Rev. 82, 607 (1951)
28B48	J. C. Bowe, M. Goldhaber, R. D. Hill, W. E. Meyerhof, and O. Sala, Phys. Rev. 73, 1219 (1948) (A)	42B5la	R. E. Batsel, D. R. Miller, and G. T. Seaborg, Phys. Rev. 84, 671 (1951)
28B49	J. C. Bowe and G. Scharff-Goldhaber, Phys. Rev. 76, 437 (1949)	43B48	J. Benes, A. Hedgran, and N. Hole, Arkiv Mat., Astron. Fysik 35A, No. 12 (1948)
28B51 28B52	<ul> <li>J. C. Bowe and P. Axel, Phys. Rev. <u>84</u>, 939 (1951)</li> <li>J. C. Bowe and P. Axel, Phys. Rev. 85, 858 (1952)</li> </ul>	43B48a	J. Benes, A. Ghosh, A. Hedgran, and N. Hole, Nature 162, 261 (1948); Arkiv Mat., Astron. Fysik
29B49	J. F. Bonner, Jr., U. S. Atomic Energy Commission	44B38	35A, No. 33 (1948) H. Brandt, Z. Physik 108, 726 (1938)
30B51	Unclassified Document AECU-107 (Feb. 1949)  J. E. Brolley, Jr., D. H. Cooper, W. S. Hall,	45B50	J. G. Bayly, Can. J. Research 28A, 520 (1950)
30531	M. S. Livingston, and L. K. Schlacks, Phys. Rev. 83, 990 (1951)	46B48	J. L. Berggren and R. K. Osborne, Phys. Rev. 74,
30B52	J. E. Brolley, Jr., J. L. Fowler, and L. K. Schlacks, Phys. Rev. 88, 618 (1952)	47B49	1240 (1948) (A)  J. P. Blaser, F. Boehm, and P. Marmier, Phys. Rev. 75, 1953 (1949)
31B38	W. E. Burcham, M. Goldhaber, and R. D. Hill, Nature 141, 510 (1938)	47B50	J. P. Blaser, F. Boshm, and P. Marmier, Helv. Phys. Acta 23, 623 (1950)
32B39	H. A. Bethe and W. J. Henderson, Phys. Rev. <u>56</u> , 1060 (1939)	47B51	J. P. Blaser, F. Boehm, P. Marmier, and H. Wäffler, Helv. Phys. Acta 24, 245 (1951)
33B39	W. H. Barkas, Phys. Rev. 56, 287 (1939)	47B5la	J. P. Blaser, F. Boehm, P. Marmier, and
33B40	W. H. Barkas, E. C. Creutz, L. A. Delsasso, R. A. Sutton, and M. G. White, Phys. Rev. 58, 383 (1940)	47B51b	P. Scherrer, Helv. Phys. Acta 24, 465 (1951)  J. P. Blaser, F. Boehm, P. Marmier, and
33B40a	W. H. Barkas, E. C. Creutz, L. A. Delsasso, and		D. C. Peaslee, Helv. Phys. Acta 24, 3 (1951)
	R. A. Sutton, Phys. Rev. <u>57</u> , 1087 (1940) (A)	48B46	A. R. Brosi, private communication (June 1946)
33B52	W. H. Barkas, R. W. Deutsch, and H. Tyren, private communication (Sept. 1952)	48B46a	A. R. Brosi, reported in Oak Ridge National Laboratory Claesified Reports Mon N-150 (Aug. 1946); Mon N-229 (Jan. 1947)
34B42	L. B. Borst, Phys. Rev. <u>61</u> , 106 (1942) (A)	48B49	A. R. Brosi, T. W. DeWitt, and H. Zeldes, Phys.
35B46	E. Bleuler, P. Scherrer, M. Walter, and W. Zunti, Helv. Phys. Acta 19, 421 (1946)		Rev. 75, 1615 (1949)
35B46a	E. Bleuler and W. Zunti, Helv. Phys. Acta 19, 375 (1946)	488498	A. R. Brosi and P. M. Gross, Jr., reported in Oak Ridge National Laboratory Classified Report ORNL-499 (Dec. 1949)
35B46b	E. Bleuler and W. Zunti, Helv. Phys. Acta 19, 137 (1946)	48B50	A. R. Brosi, H. Zeldes, and B. H. Ketelle, Phys. Rev. <u>79</u> , 902 (1950)
35B46c	E. Bleuler, W. Bollman, and W. Zunti, Helv. Phys. Acta 19, 419 (1946)	48B51	A. R. Brosi, C. J. Borkowski, E. E. Conn, and J. C. Griess, Jr., Phys. Rev. 81, 391 (1951)
35B47	E. Bleuler, P. Scherrer, M. Walter, and W. Zünti, Helv. Phys. Acta <u>20</u> , 96 (1947)	48B5la	A. R. Brosi, B. H. Ketelle, H. Zeldes, and E. Fairstein, Phys. Rev. 84, 586 (1951)
35B47a	E. Bleuler and W. Zunti, Helv. Phys. Acta 20, 195 (1947)	48B52	A. R. Brosi, B. H. Ketelle, and H. Zeldes, reported in Oak Ridge National Laboratory Classified Report ORNL-1116 (Feb. 1952)
35B51	E. Bleuler, J. W. Blue, and A. C. Johnson, Phys. Rev 82, 333 (1951) (A)	48B53	A. R. Brosi, B. H. Ketelle, H. Zeldes, and F. M. Porter, Phys. Rev. (to be published) (1953)
35B52	E. Bleuler, A. K. Stebbins, and D. J. Tendam, reported in Purdue University Progress Report II (June 1952)	49B50	J. A. Bruner and L. M. Langer, Phys. Rev. 79, 606 (1950)
36 B 49	H. Brown and V. Perez-Mendes, Phys. Rev. <u>75</u> , 1276 (1949)	49B50a	J. Bruner, L. M. Langer, and R. D. Moffat, Phys. Rev. <u>77</u> , 747 (1950) (A)
36B50	H. Brown and V. Perez-Mendez, Phys. Rev. 28, 649 (1950)		_



50B50	W. H. Burgue and J. W. Kennedy, J. Chem. Phys. 18, 97 (1950)	65B52	F. D. S. Butement, Proc. Phys. Soc. (London) 65A, 254 (1952)
50B50a	W. H. Burgus, J. D. Knight, and R. J. Prestwood, Phys. Rev. 79, 104 (1950)	65B52a	F. D. S. Butement and R. Shillito, Proc. Phys. Soc. (London) (in press)(1952)
50B51	W. H. Burgus and N. E. Ballou, NNES-PPR 9, 1184 (1951)	65B52b	F. D. S. Butement and A. J. Poe, unpublished data (Oct. 1952)
50B5la	W. H. Burgus, L. Winsberg, J. A. Seiler, and W. Rubinson, NNES-PPR 9, 1195 (1951)	65 <b>B</b> 52c	F. D. S. Butement, private communication (Oct. 1952)
50B52	W. H. Burgue, Phys. Rev. 88, 1129 (1952)	66B51	W. Biller, reported in University of California
51B50	F. O. Bartell, A. C. Helmholz, S. D. Softky, and D. B. Stewart, Phys. Rev. 80, 1006 (1950)		Radiation Laboratory Classified Report UCRL-1507 (Oct. 1951)
52B51	F. I. Boley and L. J. Laslett, Phys. Rev. 83, 215 (1951) (A)	67B49	I. Bergström and S. Thulin, Phys. Rev. <u>76</u> , 1718 (1949)
52B5la	F. I. Boley and D. J. Zaffarano, Phys. Rev. <u>84</u> , 1059 (1951)	67B49a	I. Bergström, S. Thulin, N. Svartholm, and K. Siegbahn, Arkiv Fysik <u>I</u> , 281 (1949)
52B51b	F. I. Boley and D. J. Zaffarano, lowa State College Unclassified Report ISC-154 (July 1951)	67B49b	<ol> <li>Bergström and S. Thulin, Phys. Rev. 76, 313 (1949)</li> </ol>
53B50	G. L. Brownell and C. J. Maletskos, Phys. Rev. 80, 1102 (1950)	67B50	I. Bergetröm, S. Thulin, and G. Andersson, Phys. Rev. <u>77</u> , 851 (1950)
54B39	G. Barresi and B. N. Cacciapuoti, Ricerca sci.	67B50a	<ol> <li>Bergström and S. Thulin, Phys. Rev. <u>79</u>, 537 (1950)</li> </ol>
55B47	10, 464 (1939)  R. Bouches, R. Daudel, P. Daudel, and R. Muzart,	67B50b	I. Bergström, Phys. Rev. 80, 114 (1950)
	J. phys. et radium 8, 336 (1947)	67B50c	I. Bergström and S. Thulin, Phys. Rev. <u>79</u> , 538 (1950)
55B49	R. Bouches and G. Kayas, J. phys. et radium <u>10,</u> 110 (1949)	67B51	I. Bergström, Phys. Rev. 82, 112 (1951)
55B50	R. Bouchez, S. R. de Groot, R. Nataf, and H. A. Tolhoek, J. phys. et radium 11, 105 (1950)	67B5la	I. Bergström, Phys. Rev. <u>81</u> , 638 (1951)
56B49	F. Boehm, O. Huber, P. Marmier, P. Preiswerk,	67B51b	I. Bergström, Phys. Rev. 82, 111 (1951)
***	and R. Steffen, Helv. Phys. Acta 22, 69 (1949)	67B51c	I. Bergström, Nature <u>167</u> , 634 (1951)
56B49a	F. Boehm and P. Preiswerk, Helv. Phys. Acta 22, 331 (1949)	67B51d	I. Bergström, reported in M. Siegbahn Commemorative Volume, p 307 (Uppsala 1951); Arkiv Fysik <u>5</u> , 191 (1952)
56B50	F. Boehm, J. P. Blaser, P. Marmier, and P. Preiswerk, Phys. Rev. <u>77</u> , 295 (1950)	68B50	E. Berne, Phys. Rev. 77, 568 (1950)
57B47	H. S. Brown and M. G. Inghram, Phys. Rev. 72, 347 (1947)	69B44	A. Berthelot, Ann. phys. 19, 219 (1944)
58B38	S. W. Barnes and G. Valley, Phys. Rev. <u>53</u> , 946 (1938) (A)	70B43	H. J. Born and W. Seelmann-Eggebert, Naturwiss. 31, 86 (1943)
58B 39	S. W. Barnes, Phys. Rev. 56, 414 (1939)	70B43a	H. J. Born and W. Seelmann-Eggebert, Naturwiss. 31, 201 (1943)
58B39a	S. W. Barnes and P. W. Aradine, Phys. Rev. <u>55</u> , 50 (1939)	70B43b	H. J. Born and W. Seelmann-Eggebert, Naturwiss.
59B38	J. H. Buck, Phys. Rev. <u>54</u> , 1025 (1938)	71B46	M. Burgy, L. A. Pardue, H. B. Willard, and
60B51	F. Brown, G. C. Hanna, and L. Yaffe, Phys. Rev. 84, 1243 (1951)	•	E. O. Wollan, U. S. Atomic Energy Commission Declassified Document MDDC-16 (June 1946)
60B52	F. Brown and L. Yaffe, Can. J. Chem. (in press) (1952)	72B46	N. E. Ballou, reported in J. Am. Chem. Soc. <u>68</u> , 2411 (1946)
60B52a	F. Brown, G. C. Hanna, and L. Yaffe, private	72B48	N. E. Ballou, Phys. Rev. 73, 630 (1948)
61B47	communication (Sept. 1952)  E. C. Barker, reported in Oak Ridge National	72B51	N. E. Ballou, W. H. Burgue, J. B. Dial, L. E. Glendenin, H. Finston, M. F. Ravely, B. Schloss, and N. Sugarman, NNES-PPR 9, 1410 (1951)
62B51	Laboratory Classified Report Mon P-269 (March 1947)  J. K. Bair and F. Maienschein, Phys. Rev. 81, 463	72B51a	N. E. Ballou, T. B. Novey, D. E. Engelkemeir, E. L. Brady, and J. A. Seiler, NNES-PPR 9, 675
	(1951)		(1951)
63B47	W. C. Barber, Phys. Rev. 72, 1156 (1947)	72B51b	N. E. Ballou, NNES-PPR 9, 695 (1951)
63B50	W. C. Barber, Phys. Rev. 80, 332 (1950)	72B51d	N. E. Ballou, W. Rubinson, and L. E. Glendenin, NNES-PPR 9, 1115 (1951)
63B52	W. C. Barber and R. H. Helm, Phys. Rev. <u>86</u> , 275 (1952)	72B5le	N. E. Ballou and W. H. Burgus, NNES-PPR 9, 1168 (1951)
64B51	R. A. Brightsen, K. Shure, C. Fisher, and C. D. Coryell, Phys. Rev. 81, 298 (1951) (A)	72B51f	N. E. Ballou, NNES-PPR 9, 1151 (1951)
65B49	F. D. S. Butement, Phys. Rev. <u>75</u> , 1276 (1949)	72B51g	N. E. Ballou, NNES-PPR 9, 1176 (1951)
65B50	F. D. S. Butement, Nature 165, 149 (1950); Proc. Phys. Soc. (London) 64A, 395 (1951)	72B51h	N. E. Ballou, W. H. Burgus, and J. A. Marinsky, NNES-PPR 9, 1181 (1951)
65B50a	F. D. S. Butement, Proc. Phys. Soc (London) <u>63A,</u> 532 (1950)	72B5li	N. E. Ballou, NNES-PPR 9, 1220 (1951)
65B50b	F. D. S. Butement, Proc. Phys. Soc (London) <u>63A</u> , 775 (1950)	73B50	C. Beckham and M. L. Pool, Phys. Rev. <u>80</u> , 125 (1950) (A)
65B51	F. D. S. Butement, Nature <u>167</u> , 400 (1951)	74B49	C. H. Braden, L. Slack, and F. B. Shull, Phys. Rev. 75, 1964 (1949)
45861-	F D S Butement Proc Phys. Soc. (London) 644	75R49	I. I Brown and S. Katcoff 1 Chem. Phys. 17

75B49

F. D. S. Butement, Nature 167, 400 (1951) 65B5ia F. D. S. Butement, Proc. Phys. Soc. (London) <u>64A</u>, 428 (1951)

L. J. Brown and S. Katcoff, J. Chem. Phys. <u>17</u>, 497 (1949)

76B47	G. E. Boyd and Q. V. Larson, reported in Oak Ridge National Laboratory Classified Report Mon N-229 (Jan. 1947)	87B51	R. C. Bannerman, G. M. Lewis, and S. C. Curran, Phil Mag. 42, 1097 (1951)
76B49	G. E. Boyd and O. V. Larson, reported in Oak	87B52	R. C. Bannerman, Proc. Phys. Soc. (London) 65A, 565 (1952)
	Ridge National Laboratory Classified Report ORNL- 499 (Dec. 1949)	87B52a	R. C. Bannerman and S. C. Curran, Phys. Rev. <u>85,</u> 134 (1952)
76B49a	G. E. Boyd and Q. V. Larson, reported in Oak Ridge National Laboratory Classified Report ORNL-286 (Sept. 1949)	88B52	C. I. Browne, J. O. Rasmussen, J. P. Suris, and D. F. Martin, Phys. Rev. 85, 146 (1952)
76B49b	G. E. Boyd, reported in Oak Ridge National Laboratory	88B52a	C. I. Browne and I. Perlman, unpublished data (1952)
	Classified Report ORNL-229 (Feb. 1949)	89B52	D. T. Baker, E. Bleuler, and R. M. Steffen,
76B50	G. E. Boyd and Q. V. Larson, reported in Oak Ridge National Laboratory Classified Report ORNL-685 (June 1950)		reported in Purdue University Progress Report II (June 1952)
76B50a	G. E. Boyd and Q. V. Larson, reported in Oak Ridge	90B52	D. A. Bromley and L. M. Goldman, Phys. Rev. 86, 790 (1952)
	National Laboratory Classified Report ORNL-607 (March 1950)	90B52a	D. A. Bromley, Phys. Rev. 88, 565 (1952)
76B51	G. E. Boyd and B. H. Ketelle, reported in Oak Ridge	91B52	P. T. Barrett, Proc. Phys. Soc. (London) 65A, 450
	National Laboratory Classified Report ORNL-870	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	(1952)
	(March 1951)	92B49	E. Bestenreiner and E. Broda, Nature 164, 658 (1949)
76B51a	G. E. Boyd and B. H. Ketelle, Phys. Rev. 83, 216 (1951) (A)	93B52	D. Brower, G. Hinman, G. Lang, R. Leamer, and
76B51b	G. E. Boyd, Record Chem. Progress (Kresge-		D. Rose, Phys. Rev. <u>86</u> , 1054 (1952)
	Hooker Sci. Lib.) 12, 67 (1951)	94B49	G. J. Bene, P. M. Denis, and R. C. Extermann, Helv. Phys. Acta 22, 606 (1949)
76B51c	G. E. Boyd, reported in Oak Ridge National Laboratory Classified Report ORNL-870 (March 1951)	95B51	H. N. Brown, W. L. Bendel, F. J. Shore, and
7( 0 () )		75251	R. A. Becker, Phys. Rev. 84, 292 (1951)
76B51d	G. E. Boyd and B. H. Ketelle, reported in Oak Ridge National Laboratory Classified Report ORNL-1053	96B49	J. W. Burkig and J. R. Richardson, Phys. Rev. 76,
	(Oct . 1951)		586 (1949) (A)
76B52	G. E. Boyd, Q. V. Larson, and G. W. Parker, Phys. Rev. 86, 1051 (1952)	97B50	B. Bleaney and H. E. D. Scovil, Proc. Phys. Soc. (London) 63A, 1369 (1950)
76B52a	G. E. Boyd, Phys. Rev. 86, 578 (1952)	97B51	B. Bleaney and K. D. Bowers, Proc. Phys. Soc.
	<del>-</del>	,,,,,,,	(London) 64A, 1135 (1951)
76B52b	G. E. Boyd and R. A. Charpie, Phys. Rev. 88, 681 (1952)	97B5la	B. Bleaney and D. J. E. Ingram, Proc. Roy. Soc.
76B52c	G. E. Boyd, private communication (Nov. 1952)		(London) <u>205A</u> , 336 (1951)
77B45	E Bohr and N. Hole, Arkiv Mat., Astron. Fysik	97B5lb	B. Bleaney and H. E. D. Scovil, Proc. Phys. Soc. (London) 64A, 204 (1951)
	32A, No. 15 (1945)	97B51c	B. Bleaney, D. J. E. Ingram, and H. E. D. Scovil,
78B48	J. Beydon, Compt. rend. <u>227</u> , 1159 (1948)		Proc. Phys. Soc. (London) 64A, 601 (1951)
79B51	W. L. Bendel, F. J. Shore, and R. A. Becker, Phys. Rev. <u>83</u> , 677 (1951)	97B51d	B. Bleaney and D. J. E. Ingram, Proc. Roy. Soc. (London) 208A, 143 (1951)
79B52	W. L. Bendel, F. J. Shore, H. N. Brown, and R. A. Becker, Phys. Rev. 87, 195 (1952) (A)	98B51	E. H. Bellamy, Nature 168, 556 (1951)
80B51	J. W. Barnes and A. J. Freedman, Phys. Rev. 84, 365 (1951)	99B50	P. Brix, H. Kopfermann, and W. v. Siemans, Naturwiss. 37, 397 (1950)
80063		99B51	P. Brix and A. Stendel, Naturwiss. 38, 431 (1951)
80B52	J. W. Barnes, private communication (May 1952)	100B50	D. Binder, Phys. Rev. 77, 291 (1950)
81B46	P. T. Bittencourt and M. Goldhaber, Phys. Rev. 70, 780 (1946)	101B51	L. E. Beghian, G. R. Bishop, and H. Halban, Phys. Rev. 83, 186 (1951)
82B46	S. B. Burson, P. T. Bittencourt, R. B. Duffield, and M. Goldhaber, Phys. Rev. 70, 566 (1946)	102B52	A. C. Birge, Phys. Rev. 85, 753 (1952) (A)
82B48	S. B. Burson and C. O. Muchlhause, Phys. Rev.	102B52a	A. C. Birge, private communication (Oct. 1952)
82B50	74, 1264 (1948) (A) S. B. Burson, K. W. Blair, and D. Saxon, Phys. Rev.	103B51	J. K. Beling, B. T. Feld, and I. Halpern, Phys. Rev. 84, 155 (1951)
82B51	77, 403 (1950)  S. B. Burson, K. W. Blair, H. B. Keller, and S. Waylon, Phys. 82, 42 (1951)	103B52	J. K. Beling, J. O. Newton, and B. Rose, Phys. Rev. 87, 670 (1952); <u>86</u> , 797 (1952)
82B52	Wexler, Phys. Rev. <u>83</u> , 62 (1951)  S. B. Burson and W. C. Rutledge, Phys. Rev. <u>86</u> , (22)	104B52	D. F. Bracher and A. R. Crathorn, Nature 169, 364 (1952)
	633 (1952) (A)	105B52	G. S. Bogle and H. E. D. Scovil, Proc. Phys. Soc.
83B50	C. J. Borkowski and A. R. Brosi, reported in Oak Ridge National Laboratory Classified Report ORNL- 607 (March 1950)	106B52	(London) 65A, 360 (1952)  R. M. Bartholomew, F. Brown, R. C. Hawkings,
84B51	H. Behrens, Z. Naturforsch. 6a, 249 (1951)		W. F. Merritt, and L. Yaffe, Can. J. Chem. (in press) (1952)
85B50	J. R. Beyster and M. L. Wiedenbeck, Phys. Rev.	106B52a	R. M. Bartholomew, R. C. Hawkings, W. F. Merritt,
85B50a	79, 411 (1950)  J. R. Beyster and M. L. Wiedenbeck, Phys. Rev.	106B52b	and L. Yaffe, Can. J. Chem. (in press) (1952)  R. M. Bartholomew, F. Brown, W. D. Howell,
86B49	79, 728 (1950)  L. A. Beach, C. L. Peacock, and R. G. Wilkinson,	107B52	<ul><li>W. Shorey, and L. Yaffe, Can. J. Phys. (in press) (1952)</li><li>J. P. Butler and B. G. Harvey, private communication</li></ul>
00517	Phys. Rev. 76, 1624 (1949)		(Oct. 1952)
86B49a	L. A. Beach, C. L. Peacock, and R. G. Wilkinson, Phys. Rev. <u>76</u> , 1585 (1949)	108852	S D. Bloom, Phys. Rev. <u>88</u> , 312 (1952)
86B49b	L. A. Beach, C. L. Peacock, and R. G. Wilkinson, Phys. Rev. 75, 211 (1949)	109B51	G. Bastin-Scoffier, Compt. rend. 233, 945 (1981)



110B51	W. L. Brown, Phys. Rev. 83, 271 (1951)	10C48	J. M. Cork, R. G. Shreffler, and C. M. Fowler,
111852	F. Begemann and F. G. Houtermans, Z. Naturforsch. 7a, 143 (1952)	10C48a	Phys. Rev. 74, 1657 (1948)  J. M. Cork, R. G. Shreffler, and C. M. Fowler,
112851	F. Barendregt and Sj. Tom, Physica 17, 817 (1951)		Phys. Rev. 73, 1220 (1948) (A)
113852	K. Maack Bisg ^g rd, Proc. Phys. Soc. (London) 65A, 677 (1952)	10С48Ъ	J. M. Cork, R. G. Shreffler, and C. M. Fowler, Phys. Rev. 74, 240 (1948)
		10C49	J. M. Cork, H. B. Keller, and A. E. Stoddard, Phys. Rev. <u>76</u> , 575 (1949)
		10C49a	J. M. Cork, H. B. Keller, and A. E. Stoddard, Phys. Rev. <u>76</u> , 986 (1949)
1C30	M. Curie and S. Cotelle, Compt rend. 190, 1289 (1930)	10C49b	J. M. Cork, H. B. Keller, J. Sazynski, W. C. Rutledge, and A. E. Stoddard, Phys. Rev. 75, 1778 (1949)
1C31	M. Curie, A. Debierne, A. S. Eve, H. Geiger, O. Hahn, S. C. Lind, St. Meyer, E. Rutherford, and E. Schweidler, Revs. Modern Phys. 3, 427 (1931). Summarises results of various investigators.	10C50	J. M. Cork, W. C. Rutledge, C. E. Branyan, A. E. Stoddard, and J. M. LeBlanc, Phys. Rev. 79, 889 (1950)
2044	F. L. Clark, H. J. Spencer-Palmer, and R. N. Woodward, British Declassified Report BR-522 (Oct. 1944)	10C50a	J. M. Cork, W. C. Rutledge, C. E. Branyan, A. E. Stoddard, W. J. Childs, and J. M. LeBlanc, Phys. Rev. 80, 286 (1950)
2C45	F. L. Clark, H. J. Spencer-Palmer, and R. N. Woodward, British Unclassified Report BR-584 (March 1945)	10С50Ь	J. M. Cork, W. C. Rutledge, A. E. Stoddard, C. E. Branyan, and J. M. LeBlanc, Phys. Rev. 79, 938 (1950)
3C46	L. F. Curtiss, private communication (July 1946);	10C50c	J. M. Cork, H. B. Keller, W. C. Rutledge, and A. E. Stoddard, Phys. Rev. 77, 848 (1950)
	value derived from average of values given in following references: Ward, Wynn-Williams, and Cave, Proc. Roy. Soc. (London) 125, 713 (1929); Jedrsejowski, Ann. phys. 9, 128 (1928); Braddick	10C50d	J. M. Cork, C. E. Branyan, W. C. Rutledge, A. E. Stoddard, and J. M. LeBlanc, Phys. Rev. 78, 304 (1950)
	and Cave, Proc. Roy. Soc (London) 121, 367 (1928); Gregoire, Ann. phys. 2, 161 (1934); Gleditsch and Föyn, Am. J. Sci. <u>29</u> , 253 (1935)	10C50e	J. M. Cork, H. B. Keller, W. C. Rutledge, and A. E. Stoddard, Phys. Rev. 78, 95 (1950)
4C34	I. Curie and F. Joliot, Compt. rend. 198, 254 (1934)	10C50f	J. M. Cork, A. E. Stoddard, W. C. Rutledge, C. E. Branyan, and J. LeBlanc, Phys. Rev. 78,
4C34a	<ol> <li>Curie and F. Joliot, J. phys. et radium <u>5</u>, 153 (1934)</li> </ol>	10050-	299 (1950)
4C34b	I. Curie, F. Joliot, and P. Preiswerk, Compt. rend. 198, 2089 (1934)	10C50g	J. M. Cork, A. E. Stoddard, W. C. Rutledge, C. E. Branyan, and J. M. LeBlanc, Phys. Rev. 27, 843 (1950)
4C39	I. Curie and P. Savitch, Compt. rend. 208, 343 (1939)	10C51	J. M. Cork, C. E. Branyan, A. E. Stoddard, H. B. Keller, J. M. LeBlanc, and W. J. Childs,
4C44	<ol> <li>Curie and G. Bouissières, Cahiers phys. No. 26, 1 (1944)</li> </ol>		Phys. Rev. 83, 681 (1951)
4C48	I. Curie, Compt. rend. <u>227</u> , 1225 (1948); J. phys. et radium <u>10</u> , 381 (1949)	10C51a	J. M. Cork, A. E. Stoddard, C. E. Branyan, W. J. Childa, D. W. Martin, and J. M. LeBlanc, Phys. Rev. <u>84</u> , 596 (1951)
5C48	T. E. Cranshaw and J. A. Harvey, Can. J. Research <u>26A</u> , 243 (1948)	10C51b	J. M. Cork, W. C. Rutledge, A. E. Stoddard, C. E. Branyan, and W. J. Childs, Phys. Rev. 81, 482 (1951)
6C50	L. Cranberg, Phys. Rev. <u>77</u> , 155 (1950)	10C51c	J. M. Cork, J. M. LeBlanc, A. E. Stoddard,
7C37	W. Y. Chang, M. Goldhaber, and R. Sagane, Nature 139, 962 (1937)		D. W. Martin, C. E. Branyan, and W. J. Childs, Phys. Rev. 83, 856 (1951)
7C46	W. Y. Chang, Phys. Rev. <u>69</u> , 60 (1946)	10C51d	J. M. Cork, A. E. Stoddard, J. M. LeBlanc, C. E. Branyan, D. W. Martin, and W. J. Childs,
7C48	W. Y. Chang and T. Coor, Phys. Rev. 74, 1196 (1948) W. Y. Chang, Phys. Rev. 74, 1195 (1948)	10061-	Phys. Rev. 83, 856 (1951)
7C48a 8C41	A. A. Constantinov and G. D. Latyshev, J. Phys.	10C5le	J. M. Cork, W. J. Childs, C. E. Branyan, W. C. Rutledge, and A. E. Stoddard, Phys. Rev. 81, 642 (1951)
9C38	(U.S. S. R.) 5, 239 (1941)  S. P. Choong and J. Surugue, J. phys. et radium 9, 437 (1938)	10C5H	J. M. Cork, J. M. LeBlanc, A. E. Stoddard, W. J. Childs, C. E. Branyan, and D. W. Martin, Phys. Rev. 82, 258 (1951)
10C36	J. M. Cork and E. O. Lawrence, Phys. Rev. <u>49</u> , 788 (1936)	10C52	J. M. Cork, J. M. LeBlanc, F. B. Stumpf, and W. H. Nester, Phys. Rev. 86, 575 (1952)
10C37	J. M. Cork and R. L. Thornton, Phys. Rev. <u>51</u> , 608 (1937)	10C52a	J. M. Cork, J. M. LeBlanc, F. B. Stumpf, and W. H. Nester, Phys. Rev. 86, 415 (1952)
10C38	J. M. Cork and R. L. Thornton, Phys. Rev. <u>53</u> , 866 (1938)	10C52b	J. M. Cork, D. W. Martin, J. M. LeBlanc, and C. E. Branyan, Phys. Rev. 85, 386 (1952)
10C39	J. M. Cork and J. L. Lawson, Phys. Rev. <u>56</u> , 291 (1939)	10C52c	J. M. Cork, J. M. LeBlanc, W. H. Nester, and F. B. Stumpf, Phys. Rev. 88, 685 (1952)
10C40	J. M. Cork, J. Halpern, and H. Tatel, Phys. Rev. <u>57</u> , 371 (1940)	11C40	D. R. Corson, K. R. MacKenzie, and E. Segrè, Phys. Rev. 57, 459, 1087 (1940)
10C40a	J. M. Cork and W. Middleton, Phys. Rev. 58, 474 (1940)	11C40a	D. R. Corson, K. R. MacKenzie, and E. Segrê, Phys. Rev. 58, 672 (1940)
10C41	J. M. Cork and G. P. Smith, Phys. Rev. <u>60</u> , 480 (1941)	12C37	B. N. Cacciapuoti and E. Segré, Phys. Rev. 52, 1252 (1937)
10C42	J. M. Cork, L. N. Hadley, Jr., and C. V. Kent, Phys. Rev. 61, 388 (1942) (A)	12C38	B. N. Cacciapuoti, Nuovo Cimento 15, 213 (1938)
10C47	J. M. Cork, R. G. Shreffler, and C. M. Fowler,	12C39	B. N. Cacciapuoti, Phys Rev. <u>55</u> , 110 (1939)
	Phys. Rev. <u>72</u> , 1209 (1947)	13C51	E. Cotton, Ann. phys. 6, 481 (1951)

14C50	w. w.	T.	Crane	and	I.	Perlman,	unpublished of	iata
	(1950)							

- Chamberlain, G. W. Farwell, and E. Segré, Lqs Alamos Scientific Laboratory Classified Report LAMS-131 (Sept. 1944)
- 15C46 O. Chamberlain, D. Williams, and P. Yuster, Phys. Rev. <u>70</u>, 580 (1946)
- O. Chamberlain, J. W. Gofman, E. Segré, and A. C. Wahl, Phys. Rev. 71, 529 (1947)
- 16C47 B. B. Cunningham and H. H. Hopkins, Jr., unpublished work (Feb. 1947)
- 16C49 B. B. Cunningham and L. B. Werner, J. Am. Chem. Soc. 71, 1521 (1949); NNES-PPR 14B, 51 (1949)
- 16C49a B. B. Cunningham, NNES-PPR 14B, 1363 (1949)
- 16C50 B. B. Cunningham, S. G. Thompson, and H. R. Lohr, unpublished data (1950)
- 17C51 M. Conjeaud and V. Naggiar, Compt. rend. 232, 499 (1951)
- 18C32 J. Chadwick, Proc. Roy. Soc. (London) <u>136A</u>, 692 (1932)
- 18C35 J. Chadwick and M. Goldhaber, Proc. Roy. Soc. (London) <u>151A</u>, 479 (1935)
- 19C48 J. H. Coon, M. Goldblatt, R. Nobles, and C. F. Robinson, U. S. Atomic Energy Commission Declassified Document AECD-2190 (July 1948)
- 19C49 J. H. Coon, Phys. Rev. 75, 1355 (1949)
- 20C41 R. Cornog and W. F. Libby, Phys. Rev. 59, 1046 (1941)
- 21C39 S. C. Curran and J. E. Strothers, Proc. Roy. Soc. (London) 172A, 72 (1939)
- 21C40 S. C. Curran and J. E. Strothers, Proc. Cambridge Phil. Soc. 36, 252 (1940)
- 21C40a S. C. Curran, P. I. Dee, J. E. Strothers, Proc. Roy. Soc. (London) <u>174A'</u>, 546 (1940)
- 21C48 S. C. Curran, J. Angus, and A. L. Cockroft, Nature 162, 302 (1948)
- 21C49 S. C. Curran, J. Angus, and A. L. Cockroft, Phys. Rev. <u>76</u>, 853 (1949)
- 21C51 S. C. Curran, D. Dixon, and H. W. Wilson, Phys. Rev. 84, 151 (1951); Phil. Mag. 43, 82 (1952)
- 21C52 S. C. Curran, D. Dixon, and H. W. Wilson, private communication (Sept. 1952)
- 22C34 H. R. Crane and C. G. Lauritsen, Phys. Rev. <u>45</u>, 430 (1934)
- 22C34a H. R. Crane and C. C. Lauritsen, Phys. Rev. 45, 497 (1934)
- 22C35 H. R. Crane, L. A. Delsasso, W. A. Fowler, and C. C. Lauritsen, Phys. Rev. 47, 971 (1935)
- 22C35a H. R. Crane, L. A. Delsasso, W. A. Fowler, and C. C. Lauritsen, Phys. Rev. 47, 887 (1935)
- 23C50 J. Crussard, Compt. rend. 231, 141 (1950)
- 24C49 E. C. Campbell and W. M. Good, Phys. Rev. 76, 195 (1949) (A)
- 24C50 E. C. Campbell and M. Goodrich, Phys. Rev. 78, 640 (1950) (A)
- 24C51 E. C. Campbell and M. Goodrich, private communication (Oct. 1951)
- 24C51a E. C. Campbell, J. H. Kahn, and M. Goodrich, reported in Oak Ridge National Laboratory Unclassified Report ORNL-1164 (April 1951)
- 24C52 E. C. Campbell, private communication (Oct. 1952)
- 24C52a E. C. Campbell and M. Goodrich, private communication (Oct. 1952)
- 25C50 D. Christian and D. S. Martin, Jr., Phys. Rev. <u>80</u>, 1110 (1950)
- 25C52 D. Christian, R. F. Mitchell, and D. S. Martin, Jr., Phys. Rev. 86, 946 (1952)
- 26C35 J. D. Cockcroft, C. W. Gilbert, and E. T. S. Walton, Proc. Roy. Soc. (London) 148A, 225 (1935)

- 27C47 W. W. Chupp and E. M. McMillan, Phys. Rev. 72, 873 (1947)
- 27C48 W. W. Chupp and E. M. McMillan, Phys. Rev. 74, 1217 (1948) (A)
- 28C42 C. S. Cook and P. W. McDaniel, Phys. Rev. 62, 412 (1942)
- 28C46 C. S. Cook, E. T. Jurney, and L. M. Langer, Phys. Rev. 70, 985 (1946)
- 28C48 C. S. Cook, L. M. Langer, and H. C. Price, Jr., Phys. Rev. 74, 548 (1948)
- 28C48a C. S. Cook, L. M. Langer, H. C. Price, Jr., and M. B. Sampson, Phys. Rev. 74,502 (1948)
- 28C48b C. S. Cook and L. M. Langer, Phys. Rev. 74, 227 (1948)
- 28C48c C. S. Cook and L. M. Langer, Phys. Rev. 73, 601 (1948)
- 28C48d C. S. Cook and L. M. Langer, Phys. Rev. 73, 1149 (1948)
- 28C51 C. S. Cook, Phys. Rev. 83, 462 (1951)
- 29C40 E. C. Creuts, W. H. Barkas, and N. H. Furman, Phys. Rev. 58, 1008 (1940)
- 29C40a E. C. Creutz, J. G. Fox, and R. Sutton, Phys. Rev. <u>57</u>, 567 (1940) (A)
- 29C40b E. C. Creuts, L. A. Delsasso, R. B. Sutton, M. G. White, and W. H. Barkas, Phys. Rev. <u>58</u>, 481 (1940)
- 30C44 E. T. Clarke and J. W. Irvine, Jr., Phys. Rev. 66, 231 (1944)
- 30C46 E. T. Clarke and J. W. Irvine, Jr., Phys. Rev. 69, 680 (1946) (A)
- 30C47 E. T. Clarke, Phys. Rev. 71, 187 (1947)
- 31C50 J. W. Cobble and R. W. Atterbury, Phys. Rev. <u>80</u>, 917 (1950)
- 32C39 E. C. Crittenden, Jr., Phys. Rev. 56, 709 (1939)
- 33C38 J. Cichocki and A. Soltan, Compt. rend. 207, 423 (1938)
- 34C39 R. A. Cooley, D. M. Yost, and E. M. McMillan, J. Am. Chem. Soc. <u>61</u>, 2970 (1939)
- 5C52 H. Craig, Phys. Rev. 85, 688 (1952)
- 36C50 M. Ceccarelli, G. Quareni, and A. Rostagni, Phys. Rev. 80, 909 (1950)
- 37C51 S. A. Colgate, Phys. Rev. 81, 1063 (1951)
- 38C48 W. O. Caster and T. P. Kohman, private communication (1948)
- 39C50 W. H. Cuffey, Phys. Rev. 79, 180 (1950)
- 39C51 W. Y. Cuffey, Phys. Rev. 82, 461 (1951)
- 39C5la W. H. Cuffey and R. Canada, Phys. Rev. 83, 654 (1951)
- 40C51 D. O. Caldwell and H. F. Stoddart, Phys. Rev. 81, 660 (1951) (A)
- 41C51 R. R. Carlson, Phys. Rev. 84, 749 (1951)
- 42C50 R. L. Caldwell, Phys. Rev. 78, 407 (1950)
- 43C51 R. Canada and A. C. G. Mitchell, Phys. Rev. 83, 955 (1951)
- 43C5la R. Canada and A. C. G. Mitchell, Phys. Rev. 81, 485 (1951)
- 43C5lb R. Canada, W. H. Cuffey, A. E. Lessor, and A., C. G. Mitchell, Phys. Rev. 82, 750 (1951)
- 43C51c R. Canada and A. C. G. Mitchell, Phys. Rev. 83, 76 (1951)
- 44C44 M. Camac, Metallurgical Laboratory Declassified Report CC-2409 (Dec. 1944)
- 44C45 M. Camac and L. Brown, Metallurgical Laboratory Classified Report CP-2407 (Feb. 1945)
- 45C46 E. E. Conn, A. R. Brosi, J. A. Swartout, A. E. Cameron, R. L. Carter, and D. G. Hill, Phys. Rev. <u>70</u>, 768 (1946)

			0.2
46C50	A. G. W. Cameron and L. Kats, Phys. Rev. <u>80,</u> 904 (1950)	69C52a	P. E. Cavanagh, Phil. Mag. 43, 648 (1952)
47C50	R. A. Cohn and J. D. Kurbatov, Phys. Rev. <u>78,</u> 318 (1950) (A)	70C5 <b>0</b>	L. S. Cheng and J. D. Kurbatov, Phys. Rev. 78, 319 (1950) (A)
48C38	B. R. Curtis and J. M. Cork, Phys. Rev. <u>53</u> , 681 (1938) (A)	70C52	L. S. Cheng, G. John, and J. D. Kurbatov, Phys. Rev. <u>86</u> , 632 (1952) (A); <u>85</u> , 487 (1952)
48C40	B. R. Curtis and J. R. Richardson, Phys. Rev. 57, 1121 (1940)	71C49	K. Y. Chu and M. L. Wiedenbeck, Phys. Rev. <u>75,</u> 226 (1949)
49C48	W. S. Cowart, M. L. Pool, D. A. McCown, and	72C42	A. F. Clark, Phys. Rev. 61, 242 (1942)
50C48	L. L. Woodward, Phys. Rev. 73, 1454 (1948)  S. D. Chatterjee and N. K. Saha, Indian J. Phys.	73C48	J. B. Chubbuck and I. Perlman, Phys. Rev. 74, 982 (1951)
51C51	22, 515 (1948)  C. D. Coryell, unpublished data quoted in NNES-PPR	74C46 75C52	P. Cuer and C. M. G. Lattee, Nature 158, 197 (1946)  R. J. Carr and G. H. Higgins, private communication
51C52	9, 2013 (Appendix 3) (1951) C. D. Coryell, private communication (Oct. 1952)	76C51	(Aug. 1952)  J. M. Cassels, T. C. Randle, T. G. Pickavance,
51C52a	C. D. Coryell, P. Levêque, and H. G. Richter, unpublished data (Oct. 1952)	77C52	and A. E. Taylor, Phil. Mag. 42, 215 (1951)  R. S. Caswell, Phys. Rev. 86, 82 (1952)
52C41	E. P. Clancy, Phys. Rev. <u>60</u> , 87 (1941)	78C52	A. A. Caretto and E. O. Wiig, J. Am. Chem. Soc.
53C50	S. V. Castner, M.S. Thesis, University of California Radiation Laboratory Unclassified Report	78C52a	74, 5235 (1952)  A. A. Caretto and S. Katcoff, private communication
53C51	UCRL-942 (Oct. 1950); Phys. Rev. 88, 1126 (1952)  S. V. Castmer, University of California Radiation	79C52	(Sept. 1952)  R. S. Caird and A. C. G. Mitchell, Phys. Rev.
	Laboratory Unclassified Report UCRL-1099 (Jan. 1951)	80C52	(in press) (1952)  P. G. Cobb, reported in Purdue University Progress
54C06	N. R. Campbell and A. Wood, Proc. Cambridge Phil. Soc. 14, 15 (1906); N. R. Campbell, Proc. Cambridge Phil. Soc 14, 211 (1907); 557 (1908)	81C43	Report II (June 1952)
55C50	G. Charpak and F. Susor, J. phys. et radium ll,	82C52	K. L. Cook, Phys. Rev. 64, 278 (1943) C. G. Campbell, W. J. Henderson, and J. Kyles,
55C51	633 (1950) — G. Charpak and F. Susor, Compt. rend. 233, 1356		Phil. Mag. 43, 126 (1952); private communication (Oct. 1952)
56C49	(1951)  A. L. Cockroft and G. M. Insch, Phil. Mag. 40,	83C49	R. A. Charpie, K. H. Sun, B. Jennings, and J. F. Nechaj, Phys. Rev. <u>76</u> , 1255 (1949)
57C43	1014 (1949)  A. A. Cohen, Phys. Rev. 63, 219 (1943) (A)		
58C47	P. Chudom and C. O. Muchlhause, reported in		
	Argonne National Laboratory Classified Report CP-3801 (May 1947)	1D35	A. J. Dempster, Nature 135, 993 (1935)
59C51	J. M. Cassidy, Phys. Rev. 83, 483 (1951) (A)	1D35a	A. J. Dempeter, Nature 136, 65 (1935)
60C50	W. L. Carse, J. R. Gum, and M. L. Pool, Phys.	1D36	A. J. Dempeter, Nature 138, 120 (1936)
	Rev. <u>80</u> , 1028 (1950)	1D39	A. J. Dempeter, Phys. Rev. 55, 794 (1939)
61C49	S. A. Chowdary, reported in Purdue University Unclassified Report NP-943 (June 1949)	1D48	A. J. Dempeter, Phys. Rev. 73, 1125 (1948)
62C52	T. B. Cook, Jr. and S. K. Haynes, Phys. Rev. <u>86,</u> 190 (1952)	2D38	L. A. Dubridge, S. W. Barnes, J. H. Buck, and C. V. Strain, Phys. Rev. <u>53</u> , 447 (1938)
63C48	S. G. Cohen, Nature 161, 475 (1948)	2D39	L. A. Dubridge and J. Marshall, Phys. Rev. <u>56</u> , 706 (1939)
63C51	S. G. Cohen, Nature 167, 779 (1951)	2D40	L A. Dubridge, private communication to G. T.
63C52	S. G. Cohen and A. A. Jaffe, Phys. Rev. <u>86,</u> 800 (1952)		Seaborg (1940); includes work of entire Rochester group
64C39	G. B. Collins, B. Waldman, E. M. Stubblefield, and M. Goldhaber, Phys. Rev. <u>55</u> , 507 (1939)	2D40a	L. A. Dubridge and J. Marshall, Phys. Rev. 58, 7 (1940)
64C40	G. B. Collins and B. Waldman, Phys. Rev. <u>57,</u> 1088 (1940) (A)	2D406	L. A. Dubridge and J. Marshall, Phys. Rev. <u>57</u> , 348 (1940) (A)
65C47	K. D. Coleman and M. L. Pool, Phys. Rev. 72, 1070 (1947)	3D40	W. L. Davidson, Jr., Phys. Rev. <u>57</u> , 1086 (1940) (A)
65C47a	K. D. Coleman, R. Nudenberg, and M. L. Pool, Phys. Rev. 72, 164 (1947) (A)	3D40a 4D50	W. L. Davidson, private communication (1940)  J. M. Dickson and T. C. Randle, Nature 166, 235
66C50	T. C. Chu, Phys. Rev. 79, 582 (1950)		(1950)
67C51	G. W. Campbell, N. R. Sleight, and W. H Sullivan, NNES-PPR 9, 931 (1951)	4D51	J. M. Dickson and T. C. Randle, Proc. Phys. Soc. (London) 64A, 902 (1951)
<b>68</b> C51	G. B. Cook, British Atomic Energy Report AERE C/R-729 (June 1951)	5D35	L. A. Delsasso, W. A. Fowler, and C. C. Lauritsen, Phys. Rev. 48, 848 (1935)
68C51a	G. B. Cook, reported in British Classified Report AERE-PR-20 (April 1951)	5D39	L. A. Deleasso, L. N. Ridenour, R. Sherr, and M. G. White, Phys. Rev. <u>55</u> , 113 (1939)
69C51	P. E. Cavanagh, J. F. Turner, D. V. Booker, and H. J. Dunster, Proc. Phys. Soc. (London) 64A, 13	5D40	L. A. Delsasso, M. G. White, W. Barkas, and E. C. Creuts, Phys. Rev. <u>58</u> , 586 (1940)
	(1951)	6D33	G. von Droste, Z. Physik 34, 17 (1933)
69C5la	P. E. Cavanagh, Phys. Rev. 82, 791 (1951)	7D38	H. DeVries and J. Veldkamp, Physica 5, 249 (1938)
69C52	P. E. Cavanagh, Phil. Mag. 43, 221 (1952)	7D39	H. DeVrice and G. Diemer, Physica 6, 599 (1939)

8D37	S. Devons and G. J. Neary, Proc. Cambridge Phil. Soc. 33, 154 (1937)	21D40	D. DeVault and W. F. Libby, Phys. Rev. <u>58</u> , 688 (1940)
9D49	H. E. Duckworth, R. F. Black, and R. F. Woodcock, Fhys. Rev. <u>75</u> , 1616 (1949)	22D39	R. W. Dodson and R. D. Fowler, .'hys. Rev. <u>55</u> , 880 (1939)
10D47	S. DeBenedetti and E. H. Kerner, Phys. Rev. <u>71,</u> 122 (1947)	22D40	R. W. Dodson and R. D. Fowler, Phys. Rev. <u>57</u> , 966 (1940)
10D48	S. DeBenedetti and F. K. McGowan, Phys. Rev. 74, 728 (1948)	23D48	R. B. Duffield and J. D. Knight, private communication (Oct. 1948)
10D52	S. DeBenedetti and G. H. Minton, Phys. Rev. 85, 944 (1952)	23D49	R. B. Duffield and J. D. Knight, Phys. Rev. <u>76</u> , 573 (1949)
11D39	J. V. Dunworth, Nature 144, 152 (1939)	23D49a	R. B. Duffield and J. D. Knight, Phys. Rev. 75,
11D47	J. V. Dunworth and B. Pontecorvo, Proc. Cambridge Phil. Soc. 43, 123 (1947)	23D49b	1613 (1949)  R. B. Duffield and J. D. Knight, Phys. Rev. 75, 1057 (1949)
11D47a	J. V. Dunworth and B. Pontecorvo, Proc. Cambridge Phil. Soc. 43, 429 (1947)	23D49c	1967 (1949)  R. B. Duffield and L. M. Langer, Phys. Rev. <u>76</u> , 1272 (1949)
12D42	G. Dessauer, private communication (May 1942)	23D50	R. B. Duffield, L. Hsiao, and E. N. Sloth, Phys. Rev.
13D50	G. von Dardel, Phys. Rev. 79, 734 (1950)	2,2,0	79, 1011 (1950)
14D41	R. L. Doran and W. J. Henderson, Phys. Rev. <u>60,</u> 411 (1941)	23D50a	R. B. Duffield and L. M. Langer, Phys. Rev. <u>??,</u> 743 (1950) (A)
14D48	R. L. Doran and W. J. Henderson, private communication from K. Lark-Horowitz (1948)	23D51	R. B. Duffield and L. M. Langer, Phys. Rev. 81, 203 (1951)
15D52	D. C. Dunlavey and G. T. Seaborg, Phys. Rev. <u>87,</u> 165 (1952)	23D5la	R. B. Duffield, reported in U. S. Atomic Energy Commission Classified Report WASH-62 (Dec. 1951)
15D52a	D. C. Dunlavey and G. T. Seaborg, Phys. Rev. 85, 757 (1952) (A)	23D51b	R. B. Duffield and L. M. Langer, Phys. Rev. 84, 1065 (1951)
16D41	B. S. Dahelepov and A. A. Konstantinov, Compt. rend. U.S.S.R. 30, 701 (1941)	23D52	R. B. Duffield and L. M. Langer, Phys. Rev. (to be published) (1952)
16D46	B. Dahelepov, M. Kopjova, and E. Vorbjov, Phys. Rev. 69, 538 (1946)	24D51	C. R. Dillard, R. M. Adams, H. Finston, and A. Turkevich, NNES-PPR 9, 624 (1951)
16D49	B. S. Dzhelepov, N. M. Anton'eva, and S. A. Shestopalova, Dokiady Akad. Nauk, S.S.S. R. 64,	24D5la	C. R. Dillard, R. M. Adams, H. Finston, and A. Turkevich, NNES-PPR 9, 616 (1951)
16D51	309 (1949)  B. Dahelepov, N. Zhukovskii, and Yu. Kholnov,	24D5Tb	C. R. Dillard, R. M. Adams, H. Finston, and A. Turkevich, NNES-PPR 9, 692 (1951)
14062	Doklady Akad. Nauk, S.S.S.R. 77, 233 (1951)	24D5lc	C. R. Dillard, H. Finston, and R. M. Adams,
16D52	B. Dzhelepov and A. Silantov, Doklady Akad. Nauk, S.S. S. R. 85, 533 (1952)	25D41	J. R. Downing, M. Deutsch, and A. Roberts,
17D51	C. F. G. Delaney, Phys. Rev. 81, 158 (1951)	25042	Phys. Rev. 60, 470 (1941)
17D5la	C. F. G. Delaney, Sci. Proc. Roy. Dublin Soc. 25, 251 (1951)	25D42	J. R. Downing, M. Deutsch, and A. Roberts, Phys. Rev. 61, 686 (1942)
18D40	G. Dickson, P. W. McDaniel, and E. J. Konopinski, Phys. Rev. <u>57</u> , 351 (1940) (A)	26D51	B. Dreyfus, J. K. Major, and P. Radvanyi, Compt. rend. 232, 617 (1951)
19D37	B. T. Darling, B. R. Curtis, and J. M. Cork, Phys. Rev. <u>51</u> , 1010 (1937) (A)	27D38	M. Dode and B. Pontecorvo, Compt. rend. 207, 287 (1938)
20D41	M. Deutsch and A. Roberts, Phys. Rev. <u>60</u> , 362 (1941)	28D50	E. B. Dale and J. D. Kurbatov, Phys. Rev. <u>80,</u> 126 (1950) (A)
20 D42	M. Deutsch, J. R. Downing, L. G. Elliott, J. W. Irvine, Jr., and A. Roberts, Phys. Rev. <u>62</u> , 3 (1942)	28D50a	E. B. Dale, E. D. Richert, T. A. Redfield, and J. D. Kurbatov, Phys. Rev. <u>80</u> , 763 (1950)
20D42a	M. Deutsch and L. G. Elliott, Phys. Rev. <u>62</u> , 558 (1942) (A)	29D42	J. W. DeWire, M. L. Pool, and J. D. Kurbatov, Phys. Rev. <u>61</u> , 564 (1942)
20D42b	M. Deutsch, Phys. Rev. <u>61</u> , 672 (1942)	30D49	D. G. Douglas, Phys. Rev. <u>75</u> , 1960 (1949)
20D42c	M. Deutsch, A. Roberts, and L. G. Elliott, Phys. Rev. <u>61</u> , 389 (1942) (A)	30D52	D. G. Douglas, J. S. Foster, and A. L. Thompson, private communication (Oct. 1952)
20D44	M. Deutsch and L. G. Elliott, Phys. Rev. <u>65</u> , 211 (1944)	31D50	T. Dybvig and M. L. Pool, Phys. Rev. <u>80</u> , 126 (1950) (A)
20D45	M. Deutsch, L. G. Elliott, and A. Roberts, Phys. Rev. 68, 193 (1945)	32D51	S. P. Davis and F. A. Jenkins, Phys. Rev. <u>83</u> , 1269 (1951)
20D47	M. Deutsch, Phys. Rev 72, 729 (1947)	33D46	G. Diemer and H. Groendijk, Physica <u>II</u> , 396 (1946)
20D47a	M. Deutsch, Phys. Rev. 72, 527 (1947) (A)	34D48	J. W. M. DuMond, D. A. Lind, and B. B. Watson, Phys., Rev. 73, 1392 (1948)
20D49	M. Deutsch and A. Hedgran, Phys. Rev. <u>75</u> , 1443 (1949)	35D51	D. B. Duncan and J. E. Perry, Phys. Rev. 82, 809 (1951)
20D49a	M. Deutsch and D. T. Stevenson, Phys. Rev. <u>76,</u> 184 (1949) (A)	36D52	J. T. Dewan, T. P. Pepper, K. W. Allen, and E. Almqvist, Phys. Rev. 86, 416 (1952)
20D50	M. Deutsch and W. E. Wright, Phys. Rev. 77, 139 (1950)	37D51	S. Das and S. K. Sen, Indian J. Phys. 25, 451 (1951)
20D50a	M. Deutsch and A. Hedgran, Phys. Rev. 79, 400 (1950)	38D52	S. S. Dharmatti and H. E. Weaver, Jr., Phys. Rev.
20D51	M. Deutsch and G. Scharff-Goldhaber, Phys. Rev.		85, 927 (1952)
	83, 1059 (1951)	39 <b>D</b> 51	E. K. Darby and W. Opechowski, Phys. Rev. 83, 676 (1951)



39D5la	E. K. Darby, Can. J. Phys. 29, 569 (1951)	8E36	C. D. Ellis and W. J. Henderson, Proc. Roy. Soc. (London) 156A, 358 (1936)
10D52	B. Droposky and E. O. Wilg, Phys. Rev. 58, 683 (1952)	9E48	C. Eggler, D. J. Hughes, and C. Huddleston, Phys. Rev. 74, 1239 (1948) (A)
41D52	F. Depocas and B. G. Harvey, Phys. Rev. <u>85</u> , 499 (1952)	10E41	S. Eklund, Arkiv Mat., Astron. Fysik 28A, No. 3 (1941)
42D52	D. Dimon, McMair, and S. G. Curran, Physica (in press) (1952)	10E43	S. Eklund and N. Hole, Arkiv Mat., Astron. Fysik 29A, No. 26 (1943)
43D52	R. M. Diamond, private communication (Nov. 1952)	10E46	5. Eklund, Arkiv Mat., Astron. Fysik 33A, No. 14
44D52	C. Dahlstrom, J. S. Feeter, and A. L. Thompson, private communication (Oct. 1952)	11 <b>E4</b> 7	(1946) A. C. English, T. E. Cranshaw, P. Demers, J. A.
			Harvey, E. P. Hincks, J. V. Jelley, and A. N. May, Phys. Rev. <u>72</u> , 253 (1947)
		12E41	D. R. Elliott and L. D. P. King, Phys. Rev. <u>60</u> , 489 (1941)
1E46	D. T. Eggen and M. L. Pool, Phys. Rev. 74, 57 (1948)	12E4la	D. R. Elliott and L. D. P. King, Phys. Rev. <u>59</u> , 403 (1941)
1 <b>E49</b>	D. T. Eggen and M. L. Pool, Phys. Rev. <u>75</u> , 1464 (1949) (A)	13 <b>E46</b>	D. W. Engelkemeir and E. L. Brady, reported in J. Am. Chem. Soc. <u>68</u> , 2411 (1946)
2549	W. S. Emmerich and J. D. Kurbatov, Phys. Rev. <u>75,</u> 1446 (1949)	13 <b>E48</b>	D. W. Engelkemeir, U. S. Atomic Energy Commission Declassified Document AECD-2125 (July 1948)
2251	W. S. Emmerich, G. John, and J. D. Kurbatov, Phys. Rev. <u>82</u> , 968 (1951)	13 <b>E</b> 50	D. W. Engelkemeir, M. S. Freedman, and J. May,
225la	W. S. Emmerich and J. D. Karbatov, Phys. Rev. 83, 40 (1951)		Argonne National Laboratory Unclassified Report ANL-4473 (June 1950)
2852	W. S. Emmerich and J. D. Karbatov, Phys. Rev. 85, 149 (1952)	13 <b>E</b> 51	D. W. Engelkemeir, J. A. Seiler, E. P. Steinberg, and L. Winsberg, NNES-PPR 9, 1354 (1951)
3E50	A. G. Engelkemeir and W. F. Libby, Rev. Sci. Instr. 21, 550 (1950)	13 <b>E5la</b>	D. W. Engelkemeir and E. L. Brady, NNES-PPR 9, 746 (1951)
4E43	L. G. Elliott, M. Deutsch, and A. Roberts, Phys. Rev. 63, 336 (1943)	13 <b>E</b> 5Ib	D. W. Engelkemeir, E. L. Brady, and E. P. Steinberg, NNES-PPR <u>9</u> , 722 (1951)
4E43a	L. G. Elliott and M. Doutsch, Phys. Rev. 64, 321	13E51c	D. W. Engelkemeir, Phys. Rev. <u>82</u> , 552 (1951)
	(1943)	13E514	D. W. Engelkemeir, reported in Argonne National Laboratory Classified Report ANL-4526 (Jan. 1951)
4E436	L. G. Elliott and M. Doutsch, Phys. Rev. 63, 457 (1943) (A)	13 <b>E</b> 5le	D. W. Engelkemeir and N. Sugarman, NNES-PPR 9, 1052 (1951)
4E47	L. G. Elliott and R. E. Bell, Phys. Rev. <u>72</u> , 979 (1947)	13E5H	D. W. Engelkemeir, M. S. Freedman, L. E.
4E48	L. G. Elliott and R. E. Bell, Phys. Rev. 74, 1869 (1948)		Glendenin, and R. P. Metcalf, NNES-PPR 9, 1104 (1951)
4E49	L. G. Elliott and R. E. Bell, Phys. Rev. 76, 168	13E51g	D. W. Engelkemeir, NNES-PPR 9, 1106 (1951)
	(j949) (A) and private communication from N. L. Graham (Sept. 1952)	13E52	D. W. Engelkemeir, reported in Argonne National Laboratory Classified Report ANL-4717 (April 1952)
4E50	L. G. Elliott, R. E. Bell, et al., reported in Chalk River Laboratory Classified Report PR-P-7 (Aug. 1950)	14 <b>E46</b>	J. E. Edwards and M. L. Pool, Phys. Rev. <u>69</u> , 253 (1946) (A)
4 <b>250</b> a	L. G. Elliott et al., reported in Chalk River Laboratory Classified Report PR-P-8 (Nov. 1950)	14 <b>E46a</b>	J. E. Edwards and M. L. Pool, Phys. Rev. <u>69</u> , 140 (1946)
4 <b>251</b>	L. G. Elliott and J. L. Wolfson, Phys. Rev. <u>82</u> , 333 (1951) (A)	14E47	J. E. Edwards and M. L. Pool, Phys. Rev. 72, 384 (1947)
4ESla	L. G. Elliott et al., reported in Chalk River Laboratory Classified Reports PR-P-12 (Nov. 1951) and PR-P-13 (Feb. 1952)	15 <b>E39</b>	D. Ewing, T. Perry, and R. McGreary, Phys. Rev. 55, 1136 (1939) (A)
4E52	L. G. Elliott, Phys. Rev. 85, 942 (1952)	16E43	H. Ewald, private communication to S. Flugge and J. Mattauch, Ber. deet. chem. Ges. 76A, 1 (1943);
3E37	Z. V. Erchovn, J. phys. et radium 8, 501 (1937)		Z. physik 122, 487 (1944)
6E50	H. D. Evans, Proc. Phys. Soc. (London) 63A, 575 (1950)	17E39 18E51	T. Ems., Phys. Rev. <u>56</u> , 872 (1939)  N. Elliott, NNES-PPR 9, 1047 (1951)
TEAZ	S. G. English and R. A. James, reported in	19E51	H. B. Evans, L. E. Glendenin, and R. P. Metcalf,
	Metallurgical Laboratory Classified Report CN-261 (Sept. 1942)		NNES-PPR 9, 1061 (1951)
8E30	C. D. Ellis and G. H. Aston, Proc. Roy. Soc. (London) 129A, 180 (1930)	20E51	R. R. Edwards, H. Cost, and T. H. Davies, HNES-PPR 9, 237 (1951)
8E32	C. D. Ellis, Proc. Roy. Soc. (London) 138A, 318 (1932)	21 <b>E</b> 52	G. G. Eichhols and L. A. Ficko, Phys. Rev. <u>86</u> , 794 (1952)
8E33	C. D. Ellis and N. F. Mott, Proc. Roy. Soc. (London) <u>141A</u> , 502 (1933)	22E52	L: S. Edwards and F. A. MacMillan, Phys. Rev. 87, 377 (1952)
8E34	C. D. Ellis, Proc. Roy. Soc. (London) 143A, 350 (1934)	23252	V. O. Erikson, G. Jensson, and A. Sundo, Physica 18, 91 (1952)
8E34a	C. D. Ellis and W. J. Honderson, Proc. Roy. Soc. (London) 146A, 206 (1934)	24E51	E. W. Emery, Phys. Rev. 83, 679 (1951)
8E35	(London) 146A, 200 (1734)  G. D. Ellis and W. J. Henderson, Nature 135, 429	25E52	M. W. Elliott, L. S. Cheng, J. R. Haskins, and J. D. Kurbatov, Phys. Rev. 88, 263 (1952)
	(1935)	26E52	G. T. Ewan and M. A. S. Ross, Nature <u>170</u> , 760 (1952)

			1,2101001
1F 36	W. A. Fowler, L. A. Delsasso, and C. C. Lauritsen, Phys. Rev. 49, 561 (1936)	9F39a	A. Flammersfeld, Z. Physik 112, 727 (1939)
1F37	W. A. Fowler and C. C. Lauritsen, Phys. Rev. <u>51</u> , 1103 (1937)	9F43	A. Flammersfeld and J. Mattauch, Naturwiss. 31, 66 (1943)
2F51	M. H. Feldman, L. E. Glendenin, and R. R. Edwards,	9F44	A. Flammersfeld, Naturwiss. 32, 36 (1944)
1861-	NNES-PPR 9, 598 (1951)	9F44a	A. Flammersfeld and O. Bruna, Naturwiss. 32, 70 (1944)
2F5la	M. H. Feldman and L. E. Glendenin, NNES-PPR 9, 654 (1951)	9F44b	A. Flammersfeld, Naturwiss 32, 68 (1944)
3F50	M. Freedman, J. May, R. Pairs, W. Ramler, and M. Rusnak, reported in Argonne National Laboratory	9F46	A. Flammersfeld, Z. Naturforsch. 1, 190 (1946)
•	Classified Report ANL-4380 (March 1950)	9F47	A. Flammersfeld and O. Bruna, Z. Naturforsch. 2a, 241 (1947)
3F50a	M. S. Freedman, A. H. Jaffey, and F. Wagner, Jr., Phys. Rev. 79, 410 (1950)	9F47a	A. Flammersfeld, Z. Naturforsch. 2a, 86 (1947)
3F50b	M. S. Freedman and E. P. Steinberg, reported in Argonne National Laboratory Classified Report ANL-4427 (July 1950)	9F50	A. Flammersfeld and C. Ythier, Z. Naturforsch. 5a, 401 (1950)
3F50c	M. S. Freedman and D. W. Engelkemeir, Phys. Rev.	9F50a	A. Flammersfeld, Z. Naturforsch. 5a, 687 (1950)
	79, 897 (1950)	9F50b	A. Flammersfeld and W. Herr, Z. Naturforsch. 5a, 569 (1950)
3F51	M. Freedman and F. Wagner, Jr., reported in Argonne National Laboratory Classified Report ANL-4526 (Jan. 1951)	9F51	A. Flammersfeld, Z. Naturforsch. 6a, 559 (1951)
3F52	M. S. Freedman, F. Wagner, Jr., A. H. Jaffey,	9F52	A. Flammersfeld, Z. Naturforsch. 7a, 295 (1952)
	and J. May, Phys. Rev. (in press) (1952)	9F52a	A. Flammersfeld, Z. Naturforsch. 7a, 296 (1952)
3F52a	M. Freedman, J. May, M. Rusnak, and F. Wagner, Jr., reported in Argonne National Laboratory Classified Report ANL-4717 (April 1952)	10F51	P. Falk-Vairant and J. Teillac, J. phys. et radium 12, 659 (1951)
3F52b	M. S. Freedman, F. Wagner, Jr., and D. W. Engelkemeir, Phys. Rev. 88, 1155 (1952)	10F52	P. Falk-Vairant, J. Teillac, and C. Victor, J. phys. et radium 13, 313 (1952)
3F53		10F52a	P. Falk-Vairant, Compt. rend. 235, 796 (1952)
32 33	M. S. Freedman, F. Wagner, Jr., D. W. Engelkemeir, J. R. Huizenga, and L. B. Magnusson, Phys. Rev. (to be published) (1953)	11F44	H. W. Fulbright, reported in Metallurgical Laboratory Classified Report CP-1954 (Aug. 1944)
4F32	N. Feather, Proc. Roy. Soc. (London) 136, 709 (1932); 142, 689 (1933)	IIF44a	H. W. Fulbright, W. Bents, K. Booth, R. G. Gilbert, H. Huth, A. Knudson, H. Meier, H. Plew, C. A. Potter, W. Rall, A. A. Schulke, and M. Waldner,
4F38	N. Feather, Proc. Cambridge Phil. Soc. 34, 115 (1938)		Metallurgical Laboratory Classified Report CP-1357 (Feb. 1944)
4F38a	N. Feather and E. Bretscher, Proc. Roy. Soc. (London) 165A, 530 (1938)	11F49	H. W. Fulbright, NNES-PPR 14B, 1011 (1949)
4F38b	N. Feather and J. V. Dunworth, Proc. Roy. Soc. (London) 168A, 566 (1938)	11F49a	H. W. Fulbright and J. G. D. Milton, Phys. Rev. <u>76</u> , 1271 (1949)
4F42	N. Feather, British Classified Report CPB-83 (1942)	12F52	E. H. Fleming, Jr., A. Ghiorso, and B. B. Cunningham, Phys. Rev. 88, 642 (1952)
4F44	N. Feather and J. Dainty, Proc. Cambridge Phil. Soc. 40, 57 (1944)	13F50	P. R. Fields, G. L. Pyle, and J. F. Mech, reported in Argonne National Laboratory Classified
4F47	N. Feather and R. S. Krishnan, Proc. Cambridge Phil. Soc. 43, 267 (1947)		Report ANL-4469 (June 1950)
4F47a	N. Feather, Nature 160, 749 (1947)	14F45	G. W. Farwell, J. E. Roberts, A. Spane, and A. C. Wahl, Los Alamos Scientific Laboratory Classified Report LAMS-293 (Oct. 1945)
4F48	N. Feather, J. Kyles, and R. W. Pringle, Proc. Phys. Soc. (London) <u>61</u> , 466 (1948)	14F46	G. W. Farwell, E. Segré, A. Spane, and C. E. Wiegand, Los Alamos Scientific Laboratory
4F49	N. Feather, Nucleonics 5, No. 1, 22 (1949)		Classified Report LA-490 (April 1946)
5F39	K. Fajans and D. W. Stewart, Phys. Rev. <u>56</u> , 625 (1939)	15F49	L. Feldman and C. S. Wu, 'Phys. Rev. <u>75</u> , 1286 (1949) (A)
5F40	K. Fajans and A. F. Voigt, Phys. Rev. <u>58</u> , 177 (1940)	15F49a	L. Feldman, L. Lidofsky, P. Macklin, and C. S. Wu, Phys. Rev. 76, 1888 (1949)
5F40a	K. Fajans and W. H Sullivan, Phys. Rev. 58, 276 (1940)	15F52	L. Feldman and C. S. Wu, Phys. Rev. <u>87</u> , 1091 (1952)
5F41	K. Fajans and A. F. Voigt, Phys. Rev. 60, 619 (1941)	16F34	E. Fermi, E. Amaldi, O. d'Agnostino, F. Rasetti,
5F4la	K. Fajans and A. F. Voigt, Phys. Rev. <u>60</u> , 626 (1941)		and E. Segré, Proc. Roy. Soc. (London) 146A, 483 (1934)
5F4lb 6F50	K. Fajans and A. F. Voigt, Phys. Rev. <u>60</u> , 533 (1941)  R. L. Folger, University of California Radiation	16F41	E. Fermi and E. Segre, Phys. Rev. 59, 680 (1941)
02 30	Laboratory Declassified Report UCRL-937 (Oct. 1950)	17F34	O. R. Frisch, Nature 133, 721 (1934)
6F51	R. L. Folger, P. C. Stevenson, and G. T. Seaborg, University of California Radiation Laboratory	17F35	O. R. Frisch, Nature 136, 220 (1935)
	Classified Report UCRL-1195 Revised (May 1951)	18F35	H. Fahlenbrach, Z. Physik <u>96</u> , 503 (1935)
7F51	H. Faraggi and A. Berthelot, Compt. rend. 232, 2093 (1951)	19F50	W. R. Faust, Phys. Rev. 78, 624 (1950)
7F5la	H. Faraggi, Ann. phys. 6, 325 (1951)	20F49	J. J. Floyd and L. B. Borst, Phys. Rev. <u>75</u> , 1106 (1949)
8F40	M. Frilley, J. phys. et radium 1, 34 (1940)	21F43	B. T. Feld, reported in Metallurgical Laboratory
8F52	M. Frilley, B. G. Gokhale, and M. Valadares, Compt. rend. 232, 50 (1952)	22F47	Classified Report CP-1016 (Oct. 1943)  I. Feister and L. F. Curtiss, J. Research Natl. Bur. Standards 38, 411 (1947)
9F39	A. Flammersfeld, Z. Physik 114, 227 (1939)	22F50	I. Feister and L. F. Curtiss, Phys. Rev. 78, 179
			(1950)

23F40	G. Friedlander, private communication (1940)	37F36	V. Fornin and F. G. Houtermans, Physik Z. Sowjetunion 9, 273 (1936)
23F43	G. Friedlander and C. S. Wu, Phys. Rev. <u>63</u> , 227 (1943)	38F52	M. S. Fred and F. S. Tompkins, Phys. Rev. (in press) (1952)
23F48	G. Friedlander, M. Goldhaber, and G. Scharff-Goldhaber, Phys. Rev. 74, 981 (1948)	39F52	S. C. Fung and I. Perlman, Phys. Rev. <u>87</u> , 623 (1952)
23F48a	G. Friedlander and M. L. Perlman, private communication (Sept. 1948)	40F47	H. Frauenfelder, P. C. Gugelot, O. Huber, H. Medicus, P. Preiswerk, P. Scherrer, and R.
23F49	G. Friedlander, reported in Brookhaven National Laboratory Unclassified Report BNL-AS-2 (June 1949)		Steffen, Helv. Phys. Acta 20, 238 (1947)
23F 50	G. Friedlander, M. L. Perlman, D. Alburger, and A. W. Sunyar, Phys. Rev. 80, 30 (1950)	40F50	H. Frauenfelder, O. Huber, A. de Shalit, and W. Zunti, Phys. Rev. 79, 1029 (1950)
23F50a	G. Friedlander, M. L. Perlman, and G. Scharff- Goldhaber, Phys. Rev. 80, 1103 (1950)	40F50a	H Frauenfelder, M. Walter, and W. Zünti, Phys. Rev. 77, 557 (1950)
23F51	G. Friedlander and J. M. Miller, Phys. Rev. 84, 588 (1951)	41F52	A. J. Ferguson and J. H. Montague, Phys. Rev. 87, 215 (1952) (A)
23F51a	G. Friedlander and D. E. Alburger, Phys. Rev. <u>84</u> , 231 (1951)	42F52	A. W. Fairhall, private communication (Dec. 1952)
23F51b	G. Friedlander and W. C. Orr, Phys. Rev. <u>84</u> , 484 (1951)		
23F52	G. Friedlander and M. L. Perlman, private communication (Aug. 1952)	1G22	H. Geiger, Z. Physik 8, 45 (1922)
23F52a	G. Friedlander, A. Ghiorso, and I. Perlman, unpublished data (Sept. 1952)	2G30	A. V. Grosse, J. Am. Chem. Soc. 52, 1742 (1930); Naturwiss. 20, 505 (1932)
23F52b	G. Friedlander and J. M. Miller, private communication (Oct. 1952)	2G39	A. V. Grosse, E. T. Booth, and J. R. Dunning, Phys. Rev. 56, 382 (1939)
23F52c	G. Friedlander, private communication (Dec. 1952)	2G40	A. V. Grosse and E. T. Booth, Phys. Rev. 57, 664
24F51	S. E. Furberg, Nature 168, 1005 (1951)		(1940)
25F5I	S C. Fultz and M. L. Pool, Phys. Rev. 83, 875 (1951) (A)	2G41	A. V. Grosse, E. T. Booth, and J. R. Dunning, Phys. Rev. <u>59</u> , 322 (1941)
25 <b>F52</b>	S. C. Fultz and M. L. Pool, Phys. Rev. <u>86</u> , 347 (1952)	2G48	A. V. Grosse and E. T. Booth, J. Am. Chem. Soc. 70, 465 (1948)
26F47	H. N. Friedlander, L. Seren, and S. H. Turkel, Phys. Rev. 72, 23 (1947)	3G47	R. G. Grégoire and M. Perey, Compt. rend. <u>225,</u> 733 (1947)
27F50	E. W. Fuller, Proc. Phys. Soc. (London) 63A, 1044 (1950)	4G49	C. H. Goddard and C. S. Cook, Phys. Rev. <u>76</u> , 1419 (1949)
		5G50	L. S. Germain, Phys. Rev. 80, 937 (1950)
27F50a	E. W. Fuller, Proc. Phys. Soc. (London) 63A, 1348 (1950)	6G49	L. V. Groshev and L. Y. Shavtvalov, Doklady Akad. Nauk S.S.S.R. <u>68</u> , 257 (1949)
28F47	B. J. Finkle, Phys. Rev. 72, 1260 (1947)	7G51	M. A. Grace, R. A. Allen, D. West, and H. Halban,
28F 51	B. Finkle, E. J. Hoagland, S. Katcoff, and N. Sugarman, NNES-PPR 9, 1368 (1951)	7G5la	Proc. Phys. Soc. (London) <u>64A</u> , 493 (1951)  M. A. Grace and J. R. Prescott, Phys. Rev. 84,
28F 51a	B. Finkle, S. Katcoff, and N. Sugarman, NNES-PPR 9, 663 (1951)	8G47	1059 (1951)
28F 51b	B. Finkle, D. W. Engelkemeir, and N. Sugarman, NNES-PPR 9, 1083 (1951)		M. Guillot and M. Perey, Compt. rend. 225, 330 (1947)
28F51c	B. Finkle and N. Sugarman, NNES-PPR 9, 1121 (1951)	9G49	J. W. Gofman and G. T. Seaborg, NNES-PPR 14B, 1427 (1949)
29F 5Z	C. Y. Fan, Phys. Rev. 87, 252 (1952)	10G49	A. S. Goldin, G. B. Knight, P. A. Macklin, and R. L. Macklin, Phys. Rev. 76, 336 (1949)
30F51	S. Fried, A. H. Jaffey, N. F. Hall, and L. E. Glendenin, Phys. Rev. <u>81</u> , 741 (1951)	11G46	R. H. Goeckermann, P. R. O'Connor, and W. J. Knox, private communication (1946)
31F41	J. R. Feldmeier and G. B. Collins, Phys. Rev. <u>59,</u> 937 (1941)	11G49 ·	R. H. Goeckermann and I. Perlman, Phys. Rev. 76, 628 (1949)
32F52	E. L. Fireman and D. Schwarser, Phys. Rev. <u>86,</u> 451 (1952)	12G32	O. Gratias and C. H. Collie, Proc. Roy. Soc. (London) 135A, 299 (1932)
33F50	R. W. Fink, F. L. Reynolds, and D. H. Templeton, Phys. Rev. 77, 614 (1950)	13G44	A. Ghiorso, reported in Metallurgical Laboratory Classified Reports CK-1511 (April 1944); CS-1657
33F50a	R. W. Fink and D. H. Templeton, J. Am. Chem. Soc. 72, 2818 (1950)	13G45	(May 1944)
33F51	R. W. Fink and E. O. Wiig, J. Am. Chem. Soc. 73, 2365 (1951)	13G48	A. Ghiorso, unpublished data (1945)  A. Ghiorso, W. W. Meinke, and G. T. Seaborg,
33F52	R. W. Fink and E. O. Wiig, J. Am. Chem. Soc. 74, 2457 (1952)	13G48a	Phys. Rev. 74, 695 (1948)  A. Ghiorso, J. M. Hollander, and I. Perlman,
34F52	V. Kistiakowsky Fischer, Ph. D. Thesis, University of California Radiation Laboratory Unclassified	120.00	U. S. Atomic Energy Commission Declassified Document AECD-2232 (July 1948)
	Report UCRL-1629 (Jan. 1952); Phys. Rev. 87, 859 (1952)	13G48b	A. Ghiorso, L. B. Magnusson, and G. T. Seaborg, unpublished data (July 1948)
35F50	C. M. Fowler and R. G. Shreffler, Rev. Sci. Instr. 21, 740 (1950)	13G48c	A. Ghiorso, unpublished data (1948)
3 <b>6</b> F49	J. S. Fraser, Phys. Rev. <u>76</u> , 1540 (1949)	13G49	A. Ghiorso, W. W. Meinke, and G. T. Seaborg, Phys. Rev. <u>76</u> , 1414 (1949)

13G50	A. Ghiorso, R. A. James, L. O. Morgan, and G. T. Seaborg, Phys. Rev. 78, 472 (1950)	22G50a	P. J. Grant, Nature 165, 1018 (1950)
13G51	A. Ghiorso, Phys. Rev. 82, 979 (1951)	23G50	L. Gross and D. R. Hamilton, Phys. Rev. 80, 484 (1950)
13G51a	A. Ghiorso, J. W. Brittain, W. M. Manning, and G. T. Seaborg, Phys. Rev. <u>82</u> , 558 (1951)	24G47	L. J. Goodman and M. L. Pool, Phys. Rev. <u>71</u> , 288 (1947)
13G51b	A. Ghiorso, unpublished data (1951)	25G51	M. L. Good, Phys. Rev. 83, 1054 (1951)
13G5lc	A. Ghiorso, S. G. Thompson, K. Street, Jr., and G. T. Seaborg, Phys. Rev. 81, 154 (1951)	25G51a	M. L. Good, Phys. Rev. 81, 891 (1951)
13G52	A. Ghiorso, G. H. Higgins, A. E. Larsh, G. T.	25G51b	M. L. Good, Phys. Rev. 81, 1058 (1951)
1,0,2	Seaborg, and S. G. Thompson, Phys. Rev. 87, 163 (1952) and private communication (Nov. 1952)	26G47	E. Gleditsch and T. Graf, Phys. Rev. 72, 640 (1947)
13G53	A. Ghiorso, unpublished rumor (1953)	27G48	T. Graf, Phys. Rev 74, 831 (1948)
14G49	R. L. Graham and D. H. Tomlin, Nature 164, 278	27G50	T. Graf, Phys. Rev. 79, 1014 (1950)
14651	(1949)	27G51	T. Graf, Arkiv Fysik 3, 171 (1951)
14G51	R. L. Graham and R. E. Bell, Phys. Rev. 83, 222 (1951) (A)	28G41 28G48	A. Guthrie, Phys. Rev. 60, 746 (1941)
14G51a	R. L. Graham and R. E. Bell, Phys. Rev. <u>84</u> , 380 (1951)		A. Guthrie, private communication from K. Lark-Horowitz (1948)
14G52	R. L. Graham, J. L. Wolfson, and R. E. Bell, Can. J. Phys. <u>30</u> , 459 (1952)	29G43	J. Govaerts, Bull. Soc. Roy. Sci. Liege 12, 555 (1943); Chem. Zentr. I, 634 (1944)
14G53	R. L. Graham and R. E. Bell, Can. J. Phys.	30G51	G. M. Griffiths, Phys. Rev. 83, 852 (1951)
	(to be published) (1953)	31G38	D. C. Grahame and G. T. Seaborg, Phys. Rev. <u>54</u> , 240 (1938) (A)
15G50	J. M. Grunlund, B. G. Harvey, N. Moss, and L. Yaffe, Phys. Rev. 78, 69 (1950)	31G41	D. C. Grahame and H. J. Walke, Phys. Rev. <u>60</u> , 909 (1941)
16G47	M. Goldblatt, E. S. Robinson, and R. W. Spence, Phys. Rev. 72, 973 (1947)	32G49	D. N. Gideon, W. C. Miller, and B. Waldman, Phys. Rev. 75, 329 (1949) (A)
17G49	E. R. Graves and D. I. Meyer, Phys. Rev. <u>76,</u> 183 (1949) (A)	33G46	L. E. Glendenin, reported in J. Am. Chem. Soc. 68, 2411 (1946)
18G38	M. Goldhaber, R. D. Hill, and L. Szilard, Phys. Rev. 55, 47 (1939); Nature 142, 521 (1938)	33G46a	L. E. Glendenin and E. P. Steinberg, reported in J. Am. Chem. Soc. 68, 2411 (1946)
18G46	M. Goldhaber and R. D. O'Neal, private communication (Dec. 1946)	33G47	L. E. Glendenin and R. R. Edwards, Phys. Rev. 71, 742 (1947)
18G46a	M. Goldhaber and W. J. Sturm, Phys. Rev. 70, III (1946) (A)	33G49	L. E. Glendenin, Ph. D. Thesis, Massachusetts
18G46b	M. Goldhaber, C. O. Muehlhause, and W. J. Sturm, reported in Metallurgical Laboratory Classified		Institute of Technology Unclassified Report NP-1242 (Dec. 1949)
18G46c	Report CF-3574 (Oct. 1946)	33G51	L. E. Glendenin, NNES-PPR 9, 596 (1951)
18G46d	M. Goldhaber, Phys. Rev. 70, 89 (1946)  M. Goldhaber, L. Jacobs, and D. J. Williams,	33G5la	L. E. Glendenin, NNES-PPR 9, 592 (Editor's note) (1951)
	reported in Argonne National Laboratory Classified Report CP-3647 (Nov. 1946)	33G51b	L. E. Glendenin, NNES-PPR 9, 590 (Editor's note) (1951)
18G47	M. Goldhaber and C. O. Muchlhause, reported in Argonne National Laboratory Classified Report ANL-4010 (Sept. 1947)	33G51c	L. E. Glendenin and C. D. Coryell, NNES-PPR 9, 687 (1951)
18G47a	M Goldhaber, C. O. Muehlhause, and S. H. Turkel,	33G51e	L. E. Glendenin, NNES-PPR 9, 773 (1951)
	Phys. Rev. 71, 372 (1947)	33G5H	L. E. Glendenin and E. P. Steinberg, NNES-PPR 9, 793 (1951)
18G48	M. Goldhaber and C. O. Muehlhause, Phys. Rev. 74, 1877 (1948)	33G51g	L. E. Glendenin, NNES-PPR 9, 849 (1951)
18G48a	M. Goldhaber and C. O. Muehlhause, Phys. Rev. 74, 1248 (1948) (A)	33G51h	L. E. Glendenin, NNES-PPR 9, 895 (1951)
18G50	M. Goldhaber, private communication listed in Natl. Bur. Standards Circular No. 499 (Sept. 1950)	33G51i	L. E. Glendenin, NNES-PPR 9, 979 (Editor's note) (1951)
18G51	M. Goldhaber, E. der Mateosian, G. Scharff- Goldhaber, A. W. Sunyar, M. Deutsch, and N. S.	33G51j	L. E. Glendenin and R. P. Metcalf, NNES-PPR 9, 992 (1951)
18G52	Wall, Phys. Rev. 83, 661 (1951)  M. Goldhaber and R. D. Hill, Revs. Modern Phys.	33G51k	L. E. Glendenin and J. D. Knight, NNES-PPR 9, 1074 (1951)
18032	24, 179 (1952)	33G51#	L. E. Glendenin, NNES-PPR 9, 1931 (1951)
19G38	J. A. Gray, Nature 130, 738 (1932)	33G51m	L. E. Glendenin, NNES-PPR 9, 1092 (1951)
19G36	J. A. Gray and J. F. Hinds, Phys. Rev. <u>49</u> , 477 (1936)	33G51n	L. E. Glendenin and R. P. Metcalf, NNES-PPR 9, 1067 (1951)
20G51	W. L. Gardner, N. Knable, and B. J. Moyer, Phys. Rev. <u>83</u> , 1054 (1951)	33G53	L. E. Glendenin and E. P. Steinberg, Phys. Rev. (to be published) (1953)
21G46	W. M. Good, D. Peaslee, and M. Deutsch, Phys. Rev. <u>69</u> , 313 (1946)	34G46	N. Goldstein and W. Spats, reported in Metallurgical Laboratory Classified Report CF-3574 (Oct. 1946)
21G46a	W. M. Good and W. C. Peacock, Phys. Rev. <u>69</u> , 680 (1946) (A)	35G40	A. P. Grinberg and L. I. Roussinow, Phys. Rev. 58, 181 (1940)
22G49	P. J. Grant and J. M. Hill, Nature 163, 524 (1949)	36G40	G. N. Glasoe and J. Steigman, Phys. Rev. 58, 1
22G49a	P. J. Grant and R. Richmond, Nature 163, 840 (1949); Pruc. Phys. Soc. (London) 62A, 573 (1949)	37G51	(1940)  K. Geiger, Ann. Physik 9, 293 (1951); Z. Naturforsch.
22G50	P. J. Grant, Proc. Phys. Soc. (London) 63A, 1298		6a, 54 (1951)



P. J. Grant, Proc. Phys. Soc. (London) 63A, 1298 (1950)

37G52	K. Geiger, Z. Naturforsch. 7a, 579 (1952)	59G52	G. A. Graves, L. M. Langer, and R. D. Moffat, Phys. Rev. 88, 344 (1952)
38G46	W. E. Grummitt and G. Wilkinson, Nature 158, 163 (1946)		<u> </u>
38G47	W. E. Grummitt, J. Gueron, G. Wilkinson, and L. Yaffe, Can. J. Research <u>25B</u> , 357, 364 (1947)		
38G48	W. E. Grummitt and G. Wilkinson, Nature 161, 520 (1948)	1H48	W. F. Hornyak, C. B. Dougherty, and T. Lauritsen,
3 <b>8</b> G51	W. E. Grummitt and G. Wilkinson, Chalk River Laboratory Declassified Report CRC-470 (March 1951)	1H49	Phys. Rev. <u>74</u> , 1727 (1948)  W. F. Hornyak, T. Lauritsen, and V. K.
39G43	B. L. Goldschmidt and F. Morgan, National Research Council of Canada, Atomic Energy Project Report MG-11 (Aug. 1943)	1H50	Rasmussen, Phys. Rev. <u>76</u> , 731 (1949)  W. F. Hornyak and T. Lauritsen, Phys. Rev. <u>77</u> , 160 (1950)
39G46	B. L. Goldschmidt and I. Perlman, reported in J. Am. Chem. Soc. 68, 2411 (1946)	2H41	A. C. Helmholz, Phys. Rev. <u>60</u> , 415 (1941)
39G51	B. L. Goldechmidt and I. Periman, NNES-PPR 9, 709 (1951)	2H4la	A. C. Helmhols, C. Pecher, and P. R. Stout, Phys. Rev. <u>59</u> , 902 (1941)
39G51a	B. L. Goldschmidt and I. Perlman, NNES-PPR 9,	2H41b 2H42	A. C. Helmholz, Phys. Rev. <u>60</u> , 160 (1941) (A)
	790 (1951)		A. C. Helmholz, Phys. Rev. 62, 301 (1942) (A)
<b>40</b> G40	H. Götte, Naturwiss. 28, 449 (1940)	2H42a	A. C. Helmhols, Phys. Rev. 61, 204 (1942) (A)
40G41	H. Götte, Naturwiss. 29, 496 (1941)	2H46	A. C. Helmhols, Phys. Rev. 70, 982 (1946)
40G42	H. Götte, Naturwise. 30, 108 (1942)	2H48	A. C. Helmhols and C. L. McGinnis, Phys. Rev. <u>74</u> , 1559 (1948) (A)
40G43 40G46	H. Götte, reported in (16H43b)  H. Götte, Z. Naturforsch. 1, 377 (1946)	3H50	J. A. Harvey, reported in Massachusetts Institute of
41G44	G. R. Gamertsfelder, Phys. Rev. 66, 288 (1944)	4H47	Technology Progress Report NP-1586 (April 1950)  F. Hagemann, L. I. Katsin, M. H. Studier, A. Ghiorso,
	P. C. Gugelot, O. Huber, H. Medicus, P. Preiswerk,	41141	and G. T. Seaborg, Phys. Rev. 72, 252 (1947)
42G47	P. Scherrer, and R. Steffen, Helv. Phys. Acta 19, 418 (1947); 20, 240 (1947)	4H47a	F. Hagemann, reported in Argonne National Laboratory Classified Report CC-3780 (March 1947)
43G48	H. F. Gunlock and M. L. Pool, Phys. Rev. 74, 1264 (1948)	4H50	F. Hagemann, Phys. Rev. <u>79</u> , 534 (1950)
44049	J. R. Gum, L. E. Thompson, and M. L. Pool, Phys. Rev. 76, 184 (1949) (A)	4H50a	F. Hagemann, L. I. Katzin, M. H. Studier, G. T. Seaborg, and A. Ghiorso, Phys. Rev. 79, 435 (1950)
44G50	J. R. Gum and M. L. Pool, Phys. Rev. 80, 315 (1950)	5H46	J. J. Howland, D. H. Templeton, and I. Perlman, University of California Radiation Laboratory Declassified Report BC-31 (Nov. 1946)
45G50	M. Goodrich and E. C. Campbell, Phys. Rev. 79,	6н36	F. A. Heyn, Nature 138, 723 (1936)
	418 (1950) (A)	6н37	F. A. Heyn, Nature 139, 842 (1937)
45G51	M. Goodrich, reported in Oak Ridge National Laboratory Unclassified Report ORNL-940 (March	6H37a	F. A. Heyn, Physica 4, 160 (1937)
	1951)	6н37ъ	F. A. Heyn, Physica 4, 1224 (1937)
45G5la	M. Goodrich, Phys. Rev. 82, 759 (1951)	6Н39	F. A. Heyn, A. H. W. Aten, Jr., and C. J. Bakker,
45G52 46G36	M. Goodrich and E. C. Campbell, Phys. Rev. 85, 762 (1952) (A) and private communication (Nov. 1952)  E. R. Gaerttner, J. J. Turin, and H. R. Crane,	7H49	Nature 143, 516 (1939)  A. O. Hanson, R. B. Duffield, J. D. Knight, B. C. Diven, and H. Palevsky, Phys. Rev. 76,
	Phys. Rev. <u>49</u> , 793 (1936)	8H48	578 (1949)  E. K. Hyde, M. H. Studier, and R. J. Bruehlman,
47G50	P. S. Gill, C. E. Mandeville, and E. Shapiro, Phys. Rev. 80, 284 (1950); Indian J. Phys. 33, 566 (1950)	0140	reported in Argonne National Laboratory Classified Report ANL-4112 (March 1948)
48G48	S. N. Ghoshal, Phys. Rev. 73, 417 (1948)	8H48a	E. K. Hyde and M. H. Studier, reported in Argonne National Laboratory Memorandum ANL-WMM-445
48G50	S. N. Ghoshal, Phys. Rev. 80, 939 (1950)		(Dec. 1948)
49G50	G. J. Goldsmith and E. Bleuler, J. Phys. Colloid Chem. <u>54</u> , 717 (1950)	8Н48Ъ	E. K. Hyde and M. H. Studier, Argonne National Laboratory Classified Report ANL-4182 (Aug. 1948)
50G47	A. C. Graves and R. L. Walker, Phys. Rev. 71, 1 (1947)	8H49	E. K. Hyde, M. H. Studier, and A. Ghioreo, NNES-PPR 14B, 1622 (1949)
51G52	M. J. Glaubman and F. R. Metzger, Phys. Rev. <u>87</u> , 203 (1952) (A)	8H49a	E. K. Hyde, M. H. Studier, H. H. Hopkins, Jr., and A. Ghiorso, NNES-PPR <u>14B</u> , 1439 (1949)
52G51	A. Goldstein, NNES-PPR 9, 1096 (1951)	8Н49Ъ	E. K. Hyde, NNES-PPR 14B, 1435 (1949)
52G51a	A. Goldstein, R. P. Schuman, and W. Rubinson, NNES-PPR 9, 1188 (1951)	8H50	E. K. Hyde, A. Ghiorso, and G. T. Seaborg, Phys. Rev. <u>77</u> , 765 (1950)
53G51	M. M. Gransden and W. S. Boyle, Phys. Rev. <u>82</u> , 447 (1951)	8H50a	E. K. Hyde and A. Ghiorso, University of Califor a Radiation Laboratory Unclassified Report UCRL-593 (Feb. 1950)
54G51	H. Gest and R. R. Edwards, NNES-PPR 9, 1144 (1951)	8H51	E. K. Hyde, A. Ghiorso, and G. T. Seaburg,
55G50	S. Geschwind, H. Minden, and C. H. Townes, Phys. Rev. 78, 174 (1950)		unpublished results (Aug. 1951)
56G49	R. L. Garwin, Phys. Rev. <u>76</u> , 1876 (1949)	8H5 La	E. K. Hyde and A. Ghiorso, unpublished data (May 1951)
57G51	D. H. Greenberg and J. M. Miller, Phys. Rev. <u>84,</u> 845 (1951)	8Н51Ь	E. K. Hyde and G. D. O'Kelley, Phys. Rev. <u>82,</u> 944 (1951)
58G51	D. Green and J. R. Richardson, Phys. Rev. <u>83</u> , 891 (1951) (A)	8H52	E. K. Hyde, private communication (May 1952)

8Н52Ъ	E. K. Hyde and H. B. Mathur, private communic (June 1952)	ation

E. K. Hyde, NNES-PPR 17B, 46 (1952) (classified)

8H52c E. K. Hyde and F. Asaro, private communication (Dec. 1952)

8H52a

- 8H53 E. K. Hyde and A. Ghiorso, Phys. Rev. (to be published) (1953); University of California Radiation Laboratory Unclassified Report UCRL-2019 (Nov. 1952)
- 9H38 M. G. Holloway and M. S. Livingston, Phys. Rev 54, 18 (1938). Summarises results of various investigators.
- 10H51 C. M. Huddleston and A. B. Smith, Phys. Rev. 84, 289 (1951)
- 10H52 C. M. Huddleston and A. C. G. Mitchell, Phys. Rev. (in press) (1952)
- llH48 J. M. Hill, Proc Cambridge Phil Soc. 44, 440 (1948)
- IIH50 J. M. Hill and L. R. Shepherd, Proc. Phys. Soc. (London) 63A, 126 (1950)
- 12H50 A. Hedgran, K. Siegbahn, and N. Svartholm, Proc. Phys. Soc. (London) 63A, 960 (1950)
- 12H51 A. Hedgran, Phys. Rev. 82, 128 (1951)
- 12H5la A. Hedgran and S. Thulin, Phys. Rev. 81, 1072 (1951)
- 12H52 A. Hedgran and D. Lind, Arkiv Fysik 5, 177 (1952)
- 13H50 J. M. Hollander, A. Ghiorso, and I. Perlman, reported in University of California Radiation Laboratory Classified Report UCRL-923 (Sept. 1950)
- 13H50a J. M. Hollander and R. F. Leininger, Phys. Rev. 80, 915 (1950)
- 13H51 J. M. Hollander, Ph. D. Thesis, University of Galifornia Radiation Laboratory Unclassified Report UCRL-1396 (July 1951)
- 14H34 W. J. Henderson, Proc. Roy. Soc (London) 147A, 572 (1934)
- 14H37 W. J. Henderson, L. N. Ridenour, M. G. White, and M. C. Henderson, Phys. Rev. <u>51</u>, 1107 (1937)
- l4H37a W. J. Henderson and L. N. Ridenour, Phys Rev. <u>52,</u> 40 (1937)
- 14H39 W. J. Henderson and R. L. Doran, Phys. Rev. <u>56,</u> 123 (1939)
- 15H45 N. Hole, Arkiv Mat., Astron. Fysik 32A, No. 3 (1945)
- 15H45a N. Hole, Arkiv Mat., Astron. Fysik 31B, No. 9 (1945)
- 15H46 N. Hole and K. Siegbahn, Arkiv Mat., Astron. Fysik 33A, No. 9 (1946)
- 15H47 N. Hole, Arkiv Mat., Astron. Fysik 34B, No. 5 (1947)
- 15H47a N. Hole, Arkiv Mat., Astron. Fysik 34B, No. 19 (1947)
- 15H48 N. Hole, Arkiv Mat., Astron. Fysik 36A, No. 2 (1948)
- 15H48a N. Hole, Arkiv Mat., Astron. Fysik 36A, No. 9 (1948)
- 15H48b N. Hole, J. Benes, and A. Hedgran, Arkiv Mat., Astron. Fysik 35A, No. 35 (1948)
- 16H24 O. Hahn and L. Meitner, Z. Physik 26, 161 (1924)
- 16H25 O. Hahn and L. Meitner, Z. Physik 34, 795 (1925)
- 16H37a O. Hahn, F. Strassmann, and E. Walling, Naturwiss. 25, 189 (1937)
- 16H39 O. Hahn and F. Strassmann, Naturwiss. 27, 11 (1939)
- 16H39a O. Hahn and F. Strassmann, Naturwiss. 27, 529 (1939)
- 16H39b O. Hahn and F. Strassmann, Physik Z. 40, 673 (1939)
- 16H39c O. Hahn and F. Strassmann, Naturwiss. 27, 89 (1939)
- 16H39d O. Hahn, F. Strassmann, and S. Flügge, Naturwiss. 27, 544 (1939)
- 16H39e O. Hahn and F. Strassmann, Naturwiss. 27, 451 (1939)
- 16H40 O. Hahn and F. Strassmann, Naturwiss. 28, 61 (1940)
- 16H40a O. Hahn and F. Strassmann, Naturwiss. 28, 54 (1940)
- 16H40b O. Hahn and F. Strassmann, Naturwiss. 28, 455 (1940)

- 16H40c O. Hahn and F. Strassmann, Naturwiss. 28, 543 (1940)
- 16H41 O. Hahn and F. Strassmann, Naturwiss. 29, 369 (1941)
- 16H4la O. Hahn and F. Strassmann, Naturwiss. 29, 285 (1941)
- 16H4lb O. Hahn and F. Strassmann, Z. Physik 117, 789 (1941)
- 16H42 O. Hahn, F. Strassmann, and H. Götte, Abhandl. preuss. Akad. Wiss. Math.-naturw. Klasse, No. 3 (1942)
- 16H42a O. Hahn and F. Strassmann, Naturwiss. 30, 324 (1942)
- 16H43 O. Hahn and F. Strassmann, Naturwiss 31, 249 (1943)
- 161143a O. Hahn and F. Strassmann, Z. Physik 121, 729 (1943)
- 16H43b O. Hahn and F. Strassmann, Naturwiss. 31, 499 (1943)
- 17H50 K. L. Hall and D. H. Templeton, University of California Radiation Laboratory Unclassified Report UCRL-957 (Oct. 1950)
- 17H51 K. L. Hall and D. H. Templeton, unpublished data (Aug. 1951)
- 17H5la K. L. Hall, University of California Radiation Laboratory Unclassified Report UCRL-1460 (Aug. 1951)
- 18H50 W. J. Heiman and A. Voigt, Iowa State College Unclassified Report ISC-89 (June 1950)
- 18H51 W. J. Heiman and D. F. Martin, unpublished data (Aug. 1951)
- 19H50 M. Heerschap, O. P. Hok, and G. J. Sizoo, Physica 16, 767 (1950)
- 20H49a B. G. Harvey and N. Moss, reported in Chalk River Laboratory Report CRR-427 (Dec. 1949)
- 20H50 B. G. Harvey and B. I. Parsons, Phys. Rev. <u>80</u>, 1098 (1950)
- 20H52 B. G. Harvey, private communication to S. G. Thompson (Feb. 1952)
- 20H52a B. G. Harvey, Phys. Rev. 85, 482 (1952)
- 21H41 E. Haggstrom, Phys. Rev. 59, 322 (1941)
- 22H45 J. Halperin and D. E. Koshland, Jr., Clinton Laboratory Classified Report CN-3422x (June 1945)
- 23H52 G. H. Higgins and K. Street, Jr., Phys. Rev. <u>86</u>, 252 (1952)
- 23H52a G. H. Higgins, Ph.D. Thesis, University of California Radiation Laboratory Unclassified Report UCRL-1796 (June 1952)
- 24H49 G. C. Hanna and B. Pontecorvo, Phys. Rev 75, 983 (1949)
- 24H50 G. C. Hanna, B. G. Harvey, and N. Moss, Phys. Rev. 78, 617 (1950)
- 24H51 G. C. Hanna, B. G. Harvey, N. Mose, and P. R. Tunnicliffe, Phys. Rev. 81, 466 (1951)
- 25H51 E. K. Hulet, S. G. Thompson, A. Ghiorso, and K. Street, Jr., Phys. Rev. 84, 366 (1951)
- 25H53 E.K. Hulet, S. G. Thompson, and A. Ghiorso, Phys. Rev. (to be published) (1953)
- 26H51 D. R. Hamilton, W. P. Alford, and L. Gross, Phys. Rev. 83, 215 (1951) (A)
- 27H49 J. E. R. Holmes, Proc. Phys. Soc. (London) 62A, 293 (1949)
- 28H46 D. J. Hughes and C. Eggler, private communication (Oct. 1946)
- 28H46a D. J. Hughes and W. D. B. Spats, private communication (Oct. 1946)
- 28H46b D. J. Hughes, J. Wallace, E. Goldfarb, C. Eggler, H. Murdock, and N. Goldstein, reported in Argonne National Laboratory Classified Reports CP-3647 (Nov. 1946); CF-3574 (Oct. 1946)
- 28H47 D. J. Hughes, D. Hall, C. Eggler, and E. Goldfarb, Phys. Rev. 72, 646 (1947)
- 28H47a D. J. Hughes, C. Eggler, and C. M. Huddleston, Phys. Rev. 71, 269 (1947)
- 28H47b D. J. Hughes, C. Eggler, and N. Goldstein, reported in Argonne National Laboratory Classified Report CP-3801 (May 1947)
- 28H48 D. J. Hughes and C. Eggler, Phys. Rev. 73, 809 (1948)

28H48a	D. J. Hughes, J. Dabbs, A. Cahn, and D. Hall,	40H49	A. Hemmendinger, Phys. Rev. 75, 1267 (1949)
28H49	Phys. Rev. 73, III (1948)  D. J. Hughes, C. Eggler, and C. M. Huddleston,	41H49	S. G. Hughes and W. E. Stephens, Phys. Rev. 75, 1286 (1949) (A)
29H50	Phys. Rev. <u>75</u> , 515 (1949)  T. H. Handley, reported in Oak Ridge National	42H46	O. Hirzel and H. Waffler, Helv. Phys. Acta 19, 216 (1946)
30H48	Laboratory Classified Report ORNL-867 (Dec. 1950)  F. L. Hereford, Phys. Rev. 74, 574 (1948)	42H46a	O. Hirsel and H. Waffler, Helv. Phys. Acta 19, 214 (1946)
31H48	R. C. Hawkings, R. F. Hunter, W. B. Mann, and W. H. Stevens, Phys. Rev. 74, 696 (1948)	42H47	O. Hirsel and H. Waffler, Helv. Phys. Acta <u>20,</u> 373 (1947)
31H49	R. C. Hawkings, R. F. Hunter, W. B. Mann, and W. H. Stevens, Can. J. Research 27B, 545 (1949)	42H47a	O. Hirsel, P. Stoll, and H. Wäffler, Helv. Phys. Acta 20, 241 (1947)
32H50	E. L. Hudspeth, C. P. Swann, and N. P.	42H48	O. Hirsel and H. Wäffler, Phys. Rev. 74, 1553 (1948)
32H50a	Heydenburg, Phys. Rev. 77, 736 (1950)  E. L. Hudepeth, C. P. Swann, and N. P.	43H47	D. C. Hess, Jr., R. J. Hayden, and M. G. Inghram, Phys. Rev. <u>72</u> , 730 (1947)
23177.05	Heydenburg, Phys. Rev. 80, 643 (1950)	43H48	D. C. Hess, Jr., Phys. Rev. 74, 773 (1948)
32H50b	E. L. Hudspeth and C. P. Swann, Phys. Rev. 78, 337 (1950) (A)	43H49	D. C. Hess, Jr. and M. G. Inghram, Phys. Rev. 76, 1717 (1949)
32H52	E. L. Hudepeth, W. B. Rose, and N. P. Heydenburg, Phys. Rev. <u>85</u> , 742 (1952) (A)	44H43	R. H. Hendricks, L. C. Bryner, M. D. Thomas, and J. O. Ivie, J. Phys. Chem. 47, 469 (1943)
33H35	L. R. Hafstad and M. A. Tuve, Phys. Rev. 48, 306 (1935)	45H51	R. B. Heller, E. F. Sturcken, and A. H. Weber, Phys. Rev. 83, 848 (1951)
34H41	O. Huber, O. Lienhard, P. Scherrer, and H. Wäffler, Phys. Rev. 60, 910 (1941)	46H40	J. B. Hoag, Phys. Rev. <u>57</u> , 937 (1940)
34H42	O. Huber, O. Lienhard, P. Scherrer, and H.	47H37	D. G. Hurst and H. Walke, Phys. Rev. 51, 1033 (1937)
34H43	Wäffler, Helv. Phys. Acta 15, 312 (1942) O. Huber, O. Lienhard, P. Scherrer, and H.	47H40	D. G. Hurst, R. Latham, and W. B. Lewis, Proc. Roy. Soc. (London) <u>174A</u> , 126 (1940)
34H43a	Wäffler, Helv. Phys. Acta 16, 33 (1943)  O. Huber, O. Lienhard, P. Scherrer, and H.	48H48	H. H. Hopkins, Jr. and B. B. Cunningham, private communication (Aug. 1948)
34H43b	Wäffler, Helv. Phys. Acta 16, 431 (1943)  O. Huber, O. Lienhard, and H. Wäffler, Helv.	48H48a	H. H. Hopkins, Jr. and B. B. Cunningham, Phys. Rev. 73, 1406 (1948)
34H44	Phys. Acta 16, 226 (1943)  O. Huber, O. Lienhard, and H. Wälfler, Helv. Phys. Acta 17, 195 (1944)	<b>48</b> H49	H. H. Hopkins, Jr., Ph. D. Thesis, University of California Radiation Laboratory Report UCRL-312 (March 1949)
34H44a	O. Huber, O. Lienhard, P. Scherrer, and H. Wäffler, Helv. Phys. Acta 17, 139 (1944)	48H50	H. H. Hopkins, Jr., Phys. Rev. <u>77</u> , 717 (1950)
34H45	O. Huber, O. Lienhard, P. Scherrer, and H. Wäffler,	49H49	R. N. H. Haslam, L. Kata, H. E. Johns, and H. J. Moody, Phys. Rev. 76, 704 (1949)
34H47	Helv. Phys. Acta 18, 221 (1945)  O. Huber, H. Medicus, P. Preiswerk, and R. Steffen,	49H50	R. N. H. Haslam, L. Katz, H. J. Moody, and H. M. Skarsgard, Phys. Rev. 80, 318 (1950)
34H48	Helv. Phys. Acta <u>20</u> , 495 (1947)  O. Haber, P. Marmier, H. Medicus, P. Preiswerk,	49H5I	R. N. H. Haslam, L. A. Smith, and J. G. V. Taylor, Phys. Rev. 84, 840 (1951)
	and R. Steffen, Phys. Rev. 73, 1208 (1948)	49H5la	R. N. H. Haslam and H. M. Skarsgard, Phys. Rev.
34H48a	O. Huber, R. Steffen, and F. Humbel, Helv. Phys. Acta 21, 192 (1948)	50H51	81, 479 (1951)  V. Hummel and B. Hammermesh, Phys. Rev. 82,
34H49	O. Huber, R. Rüetschi, and P. Scherrer, Helv. Phys. Acta 22, 375 (1949)	£11143	67 (1951)
34H51	O. Huber, F. Humbel, H. Schneider, and A. de Shalit, Helv. Phys. Acta 24, 127, 629 (1951)	51H43	J. G. Hamilton, reported in Metallurgical Project Classified Report (work performed at Berkeley) CH-843 (Aug. 1943)
34H52	O. Huber, F. Humbel, H. Schneider, and A. de Shalit, Helv. Phys. Acta 25, 3 (1952)	51H48	J. G. Hamilton, private communication (Sept. 1948)
34H52a	O. Huber, R. Joly, P. Scherrer, and N. F. Verster,	52H38	M. Heyden and W. Wefelmeier, Naturwiss. <u>26,</u> 612 (1938)
	Helv. Phys. Acta 25, 621 (1952) and private communication (Sept. 1952)	53H43	C. T. Hibdon, M. L. Pool, and J. D. Kurbatov, Phys. Rev. 63, 462 (1943) (A)
35H34	M. C. Henderson, M. S. Livingston, and E. O. Lawrence, Phys. Rev. 45, 428 (1934)	53H44	C. T. Hibdon, M. L. Pool, and J. D. Kurbatov, Phys. Rev. <u>65</u> , 351 (1944) (A)
35H35	M. C. Henderson, Phys. Rev. 48, 855 (1935)	53H45	C. T. Hibdon, M. L. Pool, and J. D. Kurbatov,
36H49 37H35	E. Hayward, Phys. Rev. <u>75</u> , 917 (1949)  O. Haxel, Z. Physik 93, 400 (1935)	53H45a	Phys. Rev. <u>67</u> , 289 (1945)  C. T. Hibdon and M. L. Pool, Phys. Rev. 67,
37H48	O. Hazel, F. G. Houtermans, and M. Kemmerich,	3311436	313 (1945)
	Phys. Rev. 74, 1886 (1948)	54H43	E. B. Hales and E. B. Jordan, Phys. Rev. <u>64</u> , 202 (1943)
37H48a	O. Hazel and F. G. Houtermans, Z. Physik 124, 705 (1948)	55H50	R. Hofstadter and J. A. McIntyre, Phys. Rev. 80, 631 (1950)
38H46	Zah-Wei Ho, Phys. Rev. 70, 782 (1946)	56H48	S. K. Haynes, Phys. Rev. 74, 423 (1948)
38H48	Zah-Wei Ho, Compt. rend. 226, 1187 (1948)	57H51	P. Hubert, J. phys. et radium 12, 823 (1951)
39H39	J. E. Hill and G. E. Valley, Phys. Rev. <u>55</u> , 678 (1939) (A)	57H5la	P. Hubert and J. Laberrigue-Frolow, Compt. rend. 232, 2420 (1951)
39H40	J. E. Hill, Phys. Rev. <u>57</u> , 567 (1940) (A)	57H51b	P. Hubert, Compt. rend. 232, 2201 (1951)
40H37	A. Hemmendinger and W. R. Smythe, Phys. Rev. 51, 1052 (1937)	58H51	E. J. Hoagland and N. Sugarman, NNES-PPR 9,
401140	A. Hemmendinger, Phys. Rev. <u>58</u> , 929 (1940)		642 (1951)

58H5la	E. J.	Hoagland	and N,	Sugarman,	NNES-PPR	9,	635
	(1951)					_	

- 58H5lb E. J. Hoagland and S. Katcoff, NNES-PPR 9, 660 (1951)
- 58H5lc E. J. Hoagland and N. Sugarman, NNES-PPR 9, 1031 (1951)
- 59H40 J. O. Hancock and J. C. Butler, Phys. Rev. <u>57</u>, 1088 (1940) (A)
- 60H46 R. J. Hayden and M. G. Inghram, Phys. Rev. <u>70</u>, 89 (1946)
- 60H46a R. J. Hayden and L. G. Lewis, Phys. Rev. 70, 111 (1946) (A)
- 60H48 R. J. Hayden, Phys. Rev. 74, 650 (1948)
- 60H49 R. J. Hayden, J. H. Reynolds, and M. G. Inghram, Phys. Rev. 75, 1500 (1949)
- 60H50 R. J. Hayden, D. C. Hess, Jr., and M. G. Inghram, Phys. Rev. <u>77</u>, 299 (1950)
- 61H49 R. W. Hayward and A. C. Helmholz, Phys. Rev. 75, 1469 (1949) (A)
- 61H50 R. W. Hayward, Phys. Rev. 79, 541 (1950)
- 61H50a R. W. Hayward, Phys. Rev. 79, 542 (1950)
- 61H50b R. W. Hayward, Phys. Rev. 79, 409 (1950)
- 61H52 R. W. Hayward, Phys. Rev. 85, 760 (1952) (A) and private communication (Oct. 1952)
- 61H52a R. W. Hayward, Phys. Rev. 87, 202 (1952) (A) and private communication (Oct. 1952)
- 62H49 J. E. Hudgens, Jr. and W. S. Lyon, Phys. Rev. 75, 206 (1949)
- 63H48 R. E. Hein and A. F. Voigt, Phys. Rev. 74, 1265 (1948) (A)
- 63H50 R. E. Hein and A. F. Voigt, Phys. Rev. 79, 783
- 63H52 R. E. Hein, C. M. Fowler, and R. H. McFarland, Phys. Rev. 85, 138 (1952)
- 64H52 R. A. House, R. L. Colligan, D. N. Kundu, and M. L. Pool, Phys. Rev. 86, 654 (1952) (A)
- 65H44 L. K. Hurst and M. L. Pool, Phys. Rev. <u>65</u>, 60 (1944) (A)
- 65H44a L. K. Hurst and M. L. Pool, Phys. Rev. 65, 351 (1944) (A)
- 66H49 R. A. Hinshaw and M. L. Pool, Phys. Rev. 76, 358 (1949)
- 67H48 R. D. Hill and J. W. Mihelich, Phys. Rev. 74, 1874 (1948)
- 67H48a R. D. Hill, Phys. Rev. 74, 78 (1948)
- 67H48b R. D. Hill and W. E. Meyerhof, Phys. Rev. 73, 812 (1948)
- 67H49 R. D. Hill, Phys. Rev. 76, 333 (1949)
- 67H49a R. D. Hill, G. Scharff-Goldhaber, and G. Friedlander, Phys. Rev. 75, 324 (1949)
- 67H50 R. D. Hill, Phys. Rev. 79, 413 (1950)
- 67H50a R. D. Hill and J. W. Mihelich, Phys. Rev. 79, 275 (1950)
- 67H51 R. D. Hill, Phys. Rev. 83, 865 (1951)
- 67H5la R. D. Hill and F. R. Metzger, Phys. Rev. 83, 455 (1951)
- 67H5lb R. D. Hill, G. Scharff-Goldhaber, and M. McKeown, Phys. Rev. 84, 382 (1951)
- 67H5lc R. D. Hill, Phys. Rev. 82, 449 (1951)
- 67H5ld R. D. Hill, Phys. Rev. 81, 470 (1951)
- 67H52 R. D. Hill, P. Axel, and A. W. Sunyar, private communication (Sept. 1952)
- 67H53 R. D. Hill and J. W. Mihelich, Phys. Rev. (to be published) (1953)
- 68H51 B. Hammermesh and V. Hummel, Phys. Rev. <u>84</u>, 381 (1951)

- 68H52 B Hammermesh, V Hummel, L. Goodman, and D. Engelkemeir, Phys. Rev. 87, 528 (1952)
- 69H41 D. E. Hull and H. Seelig, Phys. Rev 60, 553 (1941)
- 70H52 B. G. Hogg and H. E. Duckworth, Phys. Rev. 86, 567 (1952)
- 71H32 G. Hevesy and M. Pahl, Nature 130, 846 (1932)
- 71H35 G. Hevesy and H. Levi, Nature 135, 580 (1935)
- 71H36 G. Hevesy and H. Levi, Kgl. Danske Videnskab Selskab, Mat.-fys. Medd. 14, No. 5 (1936); Nature 137, 185 (1936)
- 71H38 G. Hevesy and H. Levi, Kgl. Danske Videnskab. Selskab, Mat.-fys. Medd. 15, No. 11 (1938)
- 72H35 R. Hosemann, Z. Physik 99, 405 (1935)
- 73H49 C. Haenny, M. Najar, and M. Gailloud, Helv Phys Acta 22, 611 (1949)
- 74H51 R. W. Hoff, J. O. Rasmussen, and S. G. Thompson, Phys. Rev. 83, 1068 (1951)
- 74H52 R. W. Hoff, unpublished data (July 1952)
- 74H52a R. W. Hoff and F. Asaro, private communication (Aug. 1952)
- 75H49 R. F. Hibbs, U. S. Atomic Energy Commission Unclassified Report AECU-556 (Aug. 1949)
- 76H40 F. G. Houtermans, Naturwiss. 28, 578 (1940)
- 76H50 F. G. Houtermans, O. Haxel, and J. Heintze, Z. Physik 128, 657 (1950)
- 77H51 J. Hatton, B. V. Rollin, and E. F. W. Seymour, Phys. Rev. 83, 672 (1951)
- 78H52 R. B. Holt, R. N. Thorn, and R. W. Wanick, Phys. Rev. <u>87</u>, 378 (1952)
- 79H52 B. C. Haldar, Phys. Rev. <u>87</u>, 158 (1952)
- 80H52 R. L. Heath and P. R. Bell, Phys. Rev. 87, 176 (1952) (A)
- 80H52a R. L. Heath, Phys. Rev. 87, 1132 (1952)
- 81H52 J. R. Huizenga and K. F. Flynn, private communication (June 1952)
- 81H52a J. R. Huixenga, D. W. Engelkemeir, and P. R. Fields, private communication (June 1952)
- 82H52 N. M. Hintz, Phys. Rev. 86, 1042 (1952)
- 83H52 W. A. Hardy, G. Silvey, and C. H. Townes, Phys. Rev. 85, 494 (1952)
- 84H51 H. R. Haymond, W. R. Garrison, and J. G. Hamilton, J. Chem. Phys. 19, 382 (1951)
- 85H52 R. B. Holtzman and N. Sugarman, Phys. Rev. <u>87</u>, 633 (1952)
- 86H52 R. J. Horsley, R. N. H. Haslam, and H. E. Johns, Phys. Rev. <u>87</u>, 756 (1952)
- 87H33 W. D. Harkins, D. M. Gans, and H. W. Newson, Phys. Rev. 44, 529 (1933)
- 88H52 L. Hsiao and R. B. Duffield, private communication (Oct. 1952)
- 89H52 N. J. Hopkins, Phys. Rev. <u>88,</u> 680 (1952)
- 91H52 E. P. Hincks and C. H. Millar, Abstract 106, June Meeting, Roy. Soc. Canada (1952)
- 92H39 H. v. Halban, Jr., F. Joliot, and L. Kowarski, Nature <u>143</u>, 470, 680 (1939)
- 93H52 J. R. Haskins, J. E. Duval, L. S. Cheng, and J. D. Kurbatov, Phys. Rev. 88, 876 (1952)
- 93H52a J. R. Haskins and J. D. Kurbatov, Phys. Rev. 88, 884 (1952)
- 94H52 D. R. Hutchinson and M. L. Wiedenbeck, Phys. Rev. 88, 699 (1952)

1151	H. I. Israel and R. G. Wilkinson, Phys. Rev. 83, 1051 (1951)	1J48	A. H. Jaffey, quoted by M. H. Studier and E. K.
1152	H. 1. Israel, Phys. Rev. 88, 682 (1952)	1.740	Hyde, Phys. Rev. 74, 591 (1948)
1153	H. I. Israel, C. H. Pruett, and R. G. Wilkinson, Phys. Rev. (to be published) (1953)	1J48a 1J48b	A. H. Jaffey, unpublished data (1948)  A. H. Jaffey and Q. Van Winkle, Argonne National
2139	J. W. Irvine, Jr., Phys. Rev. 55, 1105 (1939)		Laboratory Classified Report ANL-4193 (Oct. 1948); NNES-PPR 17B, 729 (1952) (classified)
2142	J. W. Irvine, Jr., J. Phys. Chem. 46, 910 (1942)	1J49	A. H. Jaffey and L. B. Magnusson, NNES-PPR 14B, 978 (1949)
2146	J. W. Irvine, Jr., Oak Ridge National Laboratory Classified Report Mon C-142 (Sept. 1946)	1350	A. H. Jaffey and E. K. Hyde, Phys. Rev. 79, 280
3146	M. G. Inghram and R. J. Hayden, U. S. Atomic		(1950)
	Energy Commission Declassified Document MDDC-525 (Dec. 1946)	1J50a	A. H. Jaffey and J. Lerner, reported in Argonne National Laboratory Classified Report ANL-4411 (Feb. 1950)
3147	M. G. Inghram, D. C. Hess, Jr., and R. J. Hayden, Phys. Rev. 72, 1269 (1947)	1351	A. H. Jaffey, J. Lerner, and S. Warshaw, Phys. Rev. 82, 498 (1951)
3147a	M. G. Inghram, R. J. Hayden, and D. G. Hess, Jr., Phys. Rev. <u>72</u> , 349, 967 (1947)	1 <b>J5la</b>	A. H. Jaffey, H. Diamond, A. Hirsch, and J. Mech, Phys. Rev. 84, 785 (1951)
3147b	M. G. Inghram, D. C. Hess, Jr., R. J. Hayden, and G. W. Parker, Phys. Rev. <u>71</u> , 743 (1947)	2J47	A. Johansson, Arkiv Mat., Astron. Fysik 34A, No. 9 (1947)
3147c	M. G. Inghram, R. J. Hayden, and D. C. Hess, Jr., Phys. Rev. 71, 643 (1947)	3J48	J. V. Jelley, Can. J. Research <u>26A</u> , 255 (1948)
3147d	M. G. Inghram and R. J. Hayden, Phys. Rev. 71, 130 (1947)	3J48a	J. V. Jelley and E. B. Paul, Proc. Cambridge Phil. Soc. 44, 133 (1948)
3147e	M. G. Inghram, A. E. Shaw, D. C. Hess, Jr., and R. J. Hayden, Phys. Rev. <u>72</u> , 515 (1947)	3J50	J. V. Jelley, Proc. Phys. Soc. (London) 63A, 538 (1950); Phil. Mag. 41, 1199 (1950)
3147f	M. G. Inghram, R. J. Hayden, and D. C. Hess, Jr., Phys. Rev. 71, 270 (1947)	4J43	J. C. Jacobsen and T. Sigurgeirsson, Det. Kgl. Danske Vid. Sels. 20, No. II (1943)
3147g	M. G. Inghram, D. C. Hess, Jr., and R. J. Hayden, reported in Argonne National Laboratory Classified	4J48	J. C. Jacobsen and O. Kofoed-Hansen, Phys. Rev. 73, 675 (1948)
3147h	Report ANL-4012 (Aug. 1947)  M. G. Inghram, D. C. Hess, Jr., and R. J. Hayden,	5,51	W. A. Jenkins and G. D. O'Kelley, unpublished data (April 1951)
3148	Phys. Rev. <u>71</u> , 561 (1947)  M. G. Inghram, D. C. Hess, Jr., H. S. Brown, and	5J52	W. A. Jenkins and G. T. Seaborg, Phys. Rev. 85, 758 (1952) (A)
3148a	E. Goldberg, Phys. Rev. 74, 343 (1948)  M. G. Inghram, D. C. Hess, Jr., and R. J. Hayden,	6,51	C. J. D. Jarvis and M. A. S. Ross, Proc. Phys. Soc. (London) 64A, 535 (1951)
J1104	reported in Argonne National Laboratory Classified Report ANL-4082 (Jan. 1948)	7J46	S. Jnanananda, Phys. Rev. 69, 570 (1946)
3148ъ	M. G. Inghram and D. C. Hess, Jr., Phys. Rev. 74,	7J47	S. Jnanananda, Phys. Rev. 72, 1124 (1947)
3148c	627 (1948)  M. G. Inghram, D. C. Hess, Jr., and R. J. Hayden,	7,149	S. Jnanananda, J. Sci. Ind. Research (India) 8B, No. 9, 147 (1949)
3148d	Phys. Rev. <u>74</u> , 98 (1948)  M. G. Inghram, D. C. Hess, Jr., and R. J. Hayden,	8J48	R. A. James, D. A. Orth, and G. T. Seaborg, unpublished data (July 1948)
31400	Phys. Rev. 73, 180 (1948)	8 J48a	R. A. James, reported in University of California
3149	M. G. Inghram and D. C. Hess, Jr., reported in Argonne National Laboratory Classified Report ANL-4355 (Oct. 1949)		Radiation Laboratory Memorandum MB-IP-247 (Jan. 1948)
3149a	M. G. Inghram, D. C. Hess, Jr., and J. H. Reynolds, Phys. Rev. 76, 1717 (1949)	8J <b>4</b> 9	R. A. James, A. E. Florin, H. H. Hopkins, Jr., and A. Ghiorso, NNES-PPR 14B, 1604 (1949)
3149b	M. G. Inghram, R. J. Hayden, and D. C. Hess, Jr., Phys. Rev. 75, 693 (1949); 74, 1724 (1948)	8J49a	R. A. James, S. G. Thompson, and H. H. Hopkins, Jr., NNES-PPR 14B, 1634 (1949)
3150	M. G. Inghram, H. S. Brown, C. Patterson, and	8J52	R. A. James, A. Ghiorso, and D. A. Orth, Phys. Rev. <u>85</u> , 369 (1952)
3150a	D. C. Hess, Phys. Rev. <u>80</u> , 916 (1950)  M. G. Inghram, R. J. Hayden, and D. C. Hess, Jr.,	8J52a	R. A. James, private communication (Oct. 1952)
,,,,,,	Phys. Rev. 79, 271 (1950)	9,51	J. Jacquesson and A. Lataste, Compt. rend. <u>232,</u> 1822 (1951)
3150Ъ	M. G. Inghram and J. H. Reynolds, Phys. Rev. 78, 822 (1950)	10J <b>4</b> 8	W. P. Jesse and H. Forstat, Phys. Rev. <u>73</u> , 926 (1948)
3151	M. G. Inghram, D. C. Hess, P. R. Fields, and G. L. Pyle, Phys. Rev. <u>83</u> , 1250 (1951)	10L50	W. P. Jesse and J. Sadanskis, Phys. Rev. <u>78</u> , 1 (1950)
4141	J. Itoh, Proc. PhysMath. Soc. Japan 23, 605 (1941)	11 J49	W. M. Jones, Phys. Rev. 76, 885 (1949)
5151	G. M. Insch and S. C. Curran, Phil. Mag. 42, 892 (1951)	11,751	W. M. Jones, Phys. Rev. 83, 537 (1951)
5152	G. M. Insch, J. G. Balfour, and S. C. Curran, Phys. Rev. 85, 805 (1952)	12J49	G. H. Jenks, J. A. Ghormley, and F. H. Sweeton, Phys. Rev. 75, 701 (1949)
		12J50	G. H. Jenks, F. H. Sweeton, and J. A. Ghormley, Phys. Rev. 80, 990 (1950)
		12,52	G. H. Jenks and F. H. Sweeton, Phys. Rev. <u>86,</u> 803 (1952)
		13J49	E. N. Jensen, L. J. Laslett, and W. W. Pratt, Phys. Rev. 76, 430 (1949)
		13J49a	E. N. Jensen, Phys. Rev. 76, 958 (1949)

13 Ј49Ь	E. N. Jensen, reported in Iowa State College Unclassified Report ISC-46 (July 1949)	2K45	T. P. Kohman, J. A. Swartout, and W. H Sullivan, Hanford Engineer Works Report (H)CN-3212 (Oct. 1945)
13J50	E. N. Jensen, L. J. Laslett, and D. J. Zaffarano, Phys. Rev. 80, 862 (1950)	2K49	T. P Kohman, private communication (1949)
13.J51	E. N. Jensen, R. T. Nichols, and J. Clement, Phys. Rev. 81, 143 (1951)	2K49a	T. P. Kohman, D. P. Ames, and J. Sedlet, NNES-PPR 14B, 1675 (1949)
13J52	E. N. Jensen, L. J. Laslett, and D. J. Zaffarano, Phys. Rev. 86, 1047 (1952)	3K48	G. B. Knight and R. L. Macklin, Phys. Rev. 74, 1540 (1948)
13J5Za	E. N. Jensen, L. J. Laslett, D. S. Martin, Jr., F. J. Hughes, and W. W. Pratt, Phys. Rev	3K49	G. B. Knight and R. L. Macklin, Phys. Rev. 75, 34 (1949)
13J5 <i>2</i> b	(to be published)(1952)  E. N. Jensen, R. T. Nichols, J. Clement, and A. Pohm, Phys. Rev. 85, 112 (1952)	4K42	C. V. Kent, J. M. Cork, and W. G. Wadey, Phys. Rev. 61, 389 (1942) (A)
14J49	F. Johnston and J. E. Willard, Phys. Rev. 75,	4K4Za	C. V. Kent and J. M. Cork, Phys. Rev. <u>62</u> , 297 (1942) (A)
15J48	528 (1949)  E. T. Jurney, Phys. Rev. 74, 1049 (1948)	5K43	B. Karlik and T. Bernert, Naturwiss. 31, 492 (1943)
15349	E. T. Jurney, Phys. Rev. 76, 290 (1949)	5K43a	B. Karlik and T. Bernert, Naturwiss. 31, 298 (1943); Z. Physik 123, 51 (1944)
16J41	A. S. Jensen, Phys. Rev. 60, 430 (1941)	5K44	B. Karlik and T. Bernert, Naturwiss. 32, 44 (1944)
17J50	S. Johansson, Phys. Rev. 79, 896 (1950)	5K46	B. Karlik and T. Bernert, Naturwiss. 33, 23 (1946)
17351	.S. Johansson, Y. Cauchois, and K. Siegbahn, Phys. Rev. 82, 275 (1951)	6K38	A. F. Kovarik and N. I. Adams, Jr., Phys. Rev. 54, 413 (1938)
17J51a	S. Johansson, reported in M. Siegbahn Commemorative Volume, p 183 (Uppsala, 1951)	6K41	A. F. Kovarik and N. I. Adams, Jr., J. Appl. Phys. 12, 296 (1941) (A)
17J52	S. Johansson, Arkiv Fysik 4, 273 (1952)	7K49	D. G. Karraker, F. L. Reynolds, and D. H. Templeton, University of California Radiation
17J52a	S. Johansson, Arkiv Fysik 3, 533 (1952)		Laboratory Unclassified Report UCRL-285 (Feb. 1949)
18J45	S. Jashemski and N. Goldstein, reported in Metallurgical Laboratory Classified Report CP-2984 (May 1945)	7K50	D. G. Karraker and D. H. Templeton, Phys. Rev. <u>80</u> , 646 (1950)
19J44	F. Joliot, Compt. rend. 218, 733 (1944)	7K51	D. G. Karraker and D. H. Templeton, Phys. Rev. 81, 510 (1951)
20J51	L. Jacobson and R. Overstreet, NNES-PPR 9, 735 (1951)	7K5la	D. G. Karraker, A. Ghiorso, and D. H. Templeton, Phys. Rev. 83, 390 (1951)
21J44	P. Jensen, Z. Physik 122, 387 (1944)	7K5lb	D. G. Karraker, unpublished data (May 1951)
22J50	H. E. Johns, L. Kats, R. A. Douglas, and R. N. H. Haslam, Phys. Rev. 80, 1062 (1950)	7K52	D. G. Karraker, R. J. Hayden, and M. G. Inghram, Phys. Rev. <u>87</u> , 901 (1952)
23J52	W. H. Johnson, Jr., Phys. Rev. 87, 166 (1952)	8K35	I. V. Kurtchatov, G. D. Latyshev, L. M. Nemenov, and I. P. Selinov, Physik Z. Sowjetunion 8, 589
24J38	R. Jaeckel, Z. Physik <u>110</u> , 330 (1938)		(1935)
25J52	M. W. Johns, C. D. Cox, R. J. Donnelly, and C. C. McMullen, Phys. Rev. <u>87</u> , 1134 (1952)	9K39	R. S. Krishnan and D. H. T. Gant, Nature 144, 547 (1939)
26J52	H. Jaffe and I. Perlman, unpublished data (Aug. 1952)	9K40	R. S. Krishnan and E. A. Nahum, Proc. Cambridge Phil. Soc. 36, 490 (1940)
27J51	C. M. Johnson and W. Gordy, Phys. Rev. <u>83</u> , 1249 (1951)	9K40a	R. S. Krishnan and T. E. Banks, Nature 145, 777 (1940)
28J52	J. W. Jones and T. P. Kohman, Phys. Rev. <u>85,</u> 941 (1952)	9K40b	R. S. Krishnan, Proc. Cambridge Phil. Soc. <u>36</u> , 500 (1940)
29J52	C. D. Jeffries, H. Loeliger, and H. H. Staub, Phys. Rev. 85, 478 (1952)	9K41	R. S. Krishnan, Nature 148, 407 (1941)
30J52	V. Jaccarino, B. Bederson, and H. H. Stroke, Phys. Rev. 87, 676 (1952)	9K4la	R. S. Krishnan and T. E. Banks, Proc. Cambridge Phil. Soc. 37, 317 (1941)
31J52	D. R. Jones, S. C. Fults, and M. L. Pool, Phys. Rev. 86, 654 (1952) (A)	9K41b	R. S. Krishnan and E. A. Nahum, Proc. Cambridge Phil. Soc 37, 422 (1941)
32J52	F. A. Johnson, Abstract 76, June Meeting, Roy. Soc. Canada (1952) and private communication (Oct. 1952)	9K4lc	R. S. Krishnan, Proc. Cambridge Phil. Soc. 37, 186 (1941)
33J52	A. A. Jaffe and S. G. Cohen, Phys. Rev. <u>86,</u> 1041 (1952)	9K42	R. S. Krishnan and E. A. Nahum, Proc. Roy. Soc. (London) <u>18CA</u> , 321, 333 (1942)
34J52	P. S. Jastram and C. E. Whittle, Phys. Rev. <u>87,</u> 1133 (1952)	10K49	E. L. Kelly and E. Segré, Phys. Rev. <u>75</u> , 999 (1949)
		10K50	E. L. Kelly, Ph. D. Thesis, University of California Classified Report UCRL-1044 (Dec. 1950)
		11K50	H. B. Keller and J. M. Cork, Phys. Rev. 79, 1030 (1950)
1K40	M. D. Kamen and S. Ruben, Phys. Rev. <u>58</u> , 194 (1940) (A)	IIK50a	H. B. Keller, reported in Argonne National Laboratory Classified Report ANL-4437 (April 1950)
1K41	M. D. Kamen, Phys. Rev. 60, 537 (1941)	11K51	H. B. Keller and J. M. Cork, Phys. Rev. <u>84</u> , 1079 (1951)
1K42	M. D. Kamen, Phys. Rev. 62, 303 (1942) (A)	12K44	M. Kahn and G. A. Linenberger, reported in Los Alamos Scientific Laboratory Classified Report
1K46	M. D. Kamen, Bull. Am. Museum Nat. Hist. <u>87,</u> 103 (1946)		Low Alamos Scientific Laboratory Classified Report LAMS-151 (Oct. 1944)

'3K49	C. A. Kienberger, Phys. Rev. 76, 1561 (1949)	24K50	B. H. Ketelle, Phys. Rev. <u>80</u> , 758 (1950)
13K52	C. A. Kienberger, Phys. Rev. <u>87</u> , 520 (1952)	24K50a	B. H. Ketelle and J. W. Ruch, Phys. Rev. <u>77</u> , 565 (1950)
14K39	J W Kennedy, G T. Seaborg, and E Segrè, Phys. Rev. <u>56</u> , 1095 (1939)	24K50b	B. H. Ketelle, C. M. Nelson, and G. E. Boyd, Phys. Rev. 79, 242 (1950) (A)
14K40	J. W. Kennedy and G. T. Seaborg, Phys. Rev. <u>57</u> , 843 (1940)	24K50c	B. H. Ketelle, A. R. Bross, and H. Zeldes,
14K46	J. W. Kennedy, G. T. Seaborg, E. Segrè, and A. C. Wahl, Phys. Rev. <u>70</u> , 555 (1946); NNES-PPR 14B, 5 (1949)	24K50d	Phys Rev 80, 485 (1950)  B. H. Ketelle, reported in Oak Ridge National Laboratory Classified Report ORNL-607 (March 1950)
14K49	J. W. Kennedy, M. L. Perlman, E. Segrè, and A. C. Wahl, NNES-PPR 14B, 79 (1949)	24K51	B. H. Ketelle, H. Zeldes, A. R. Brosi, and R. A. Dandl, Phys. Rev. 84, 585 (1951); H. Zeldes,
15K36	K. S. Knol and J. Veldkamf, Physica 3, 145 (1936)		A. R. Brosi, and B. H. Ketelle, Phys. Rev. 81, 642 (1951)
16K47	W. J. Knox, Phys. Rev. 72, 1254 (1947)	24K5la	B. H. Ketelle, A. R. Brosi, and H. Zeldes, reported in Oak Ridge National Laboratory Classified
16K48	W. J. Knox, Phys. Rev. <u>74</u> , 1192 (1948)		Report ORNL-870 (March 1951)
17K 36	F. N. D. Kurie, J. R. Richardson, and H. C. Paxton, Phys. Rev. 49, 368 (1936)	24K52	B. H. Ketelle and A. R. Brosi, private communication (Oct. 1952)
17K48	F. N. D. Kurte and M. Ter-Pogossian, Phys. Rev. 74, 677 (1948)	25K46	J. X. Khym, Oak Ridge National Laboratory Classified Report Mon C-61 (Feb. 1946)
17K51	F. N. D. Kurie, unpublished data quoted in (39551a)	26K48	N. L. Krisberg, M. L. Pool, and C. T. Hibdon, Phys. Rev. 74, 44 (1948)
18K48	K. Knable, E. O. Lawrence, C. E. Leith, P. J. Moyer, and R. L. Thornton, Phys. Rev. 74, 1217 (1948) (A)	26K49	N. L. Krisberg and M. L. Pool, Phys. Rev. <u>75,</u> 1693 (1949)
19K39	L. D. P. King, W. J. Henderson, and J. R. Risser, Phys. Rev. 55, 1118 (1939) (A)	27K50	H. E. Kubitschek, Phys. Rev. 79, 23 (1950)
19K39a	L. D. P. King and W. J. Henderson, Phys. Rev. 56,	28K48	B. D. Kern, D. J. Zaffarano, and A. C. G. Mitchell, Phys. Rev. 73, 1142 (1948)
19849	L. D. P. King and D. R. Elliott, Phys. Rev. 58,	28K49	B. D. Kern, A. C. G. Mitchell, and D. J. Zaffarano, Phys. Rev. 76, 94 (1949)
20K45	J. D. Knight, T. B. Novey, C. V. Cannon, and	29K46	D. N. Kundu and M. L. Pool, Phys. Rev. 70, 111 (1946) (A)
	A. Turkevich, Metallurgical Laboratory Classified Report CC-2605 (April 1945)	29K47	D. N. Kundu and M. L. Pool, Phys. Rev. <u>71</u> , 140 (1947) (A)
20K49	J. D. Knight, W. H. Burgus, and R. J. Prestwood, private communication listed in NNES-PPR 9, 2063 (1951) (ref. Kl4)	29K47a	D. N. Kundu and M. L. Pool, Phys. Rev. 72, 101 (1947)
20K51	J. D. Knight and G. A. Cowan, reported in Los Alamos Scientific Laboratory Classified Report	29K48	D. N. Kundu and M. L. Pool, Phys. Rev 73, 22 (1948)
	WASH-58 (March 1951) and private communication (Oct. 1952)	29K48a	D. N. Kundu and M. L. Pool, Phys. Rev. <u>74</u> , 1775 (1948)
20K51a	J. D. Knight and D. P. Ames, reported in Los Alamos Scientific Laboratory Classified Report WASH-62 (Dec. 1951)	29K49	D. N. Kundu and M. L. Pool, Phys. Rev. 76, 183 (1949) (A)
20K52	J. D. Knight and L. Baggett, private communication (April 1952)	29K49a	D. N. Kundu and M. L. Pool, Phys. Rev. <u>75</u> , 1690 (1949)
21K47	B. B. Kinsey, Phys. Rev. 72, 526 (1947) (A)	29K50	D. N. Kundu and M. L. Pool, Phys. Rev. 78, 488 (1950)
21K50	B. B. Kinsey, G. A. Bartholomew, and W. H. Walker, Phys. Rev. 78, 481 (1950)	29K50a	D. N. Kundu, J. L. Hult, and M. L. Pool, Phys. Rev. 77, 71 (1950)
21K50a	B. B. Kinsey, et al., reported in Chalk River Laboratory Classified Report PR-P-6 (March 1950)	29K51	D. N. Kundu and M. L. Pool, Phys. Rev. 84, 481 (1951)
22K39	G. Kuerti and S. N. Van Voorhis, Phys. Rev. <u>56,</u> 614 (1939)	29K52	D. N. Kundu, J. D. Service, and M. L. Pool,
23K48	E. D. Klema and A. O. Hanson, Phys. Rev. 73, 106 (1948)	30K50	Phys. Rev. 87, 203 (1952) (A)  L. Katz, A. S. Penfold, H. J. Moody, R. N. H.
23K52	E. D. Klema and F. K. McGowan, Phys. Rev. <u>87,</u> 524 (1952)		Haslam, and H. E. Johns, Phys. Rev. 77, 289 (1950)
24K48	B. H. Ketelle and W. C. Peacock, Phys. Rev. <u>73</u> , 1269 (1948) (A)	30K51	L. Katz and A. G. W. Cameron, Phys. Rev. 84, 1115 (1951)
24K48a	B. H. Ketelle and G. E. Boyd, reported in Oak Ridge National Laboratory Classified Report	30K5la	L. Katz and A. G. W. Cameron, Can. J. Phys. 29, 518 (1951)
24K49	ORNL-65 (July 1948)  B. H. Ketelle, reported in Oak Ridge National	31K51	J. H. Kahn, Oak Ridge National Laboratory Unclassified Report ORNL-1089 (Nov. 1951)
24K49a	Laboratory Classified Report ORNL-286 (Sept. 1949)  B. H. Ketelle, reported in Oak Ridge National	31K52	J. H. Kahn and E. C. Campbell, private communication (Oct. 1952)
24K49b	Laboratory Classified Report ORNL-336 (May 1949)  B. H. Ketelle, reported in Oak Ridge National	32K46	S. Katcoff and A. Goldstein, U. S. Atomic Energy Commission Declassified Document MDDC-293 (April 1946)
34975	Laboratory Classified Report ORNL-229 (Feb. 1949)	32K47	S. Katcoff, Phys. Rev. 71, 826 (1947)
24K49c	B. H. Ketelle, reported in Brookhaven National Laboratory Unclassified Report BNL-C-9 (Aug. 1949)	32K47a	S. Katcoff, Phys. Rev. 72, 1160 (1947)
24K49d	B. H. Ketelle, Phys. Rev. 76, 1256 (1949)	32K48	S. Katcoff, J. A. Miskel, and C. W. Stanley, Phys. Rev. 74, 631 (1948)
24K49e	B. H. Ketelle and G. W. Parker, Phys. Rev. <u>76,</u> 1416 (1949)		

32K49	S. Katcoff, J. A. Leary, K. A. Walsh, R. A. Elmer, S. S. Goldsmith, L. D. Hall, E. G. Newbury,	45K40	D. C. Kalbfell and R. A. Cooley, Phys. Rev. <u>58,</u> 91 (1940)
	J. J. Povelites, and J. S. Waddell, J. Chem. Phys. 17, 421 (1949)	46K52	A. W. Knudsen, Phys. Rev. 86, 571 (1952)
32K50	S. Katcoff, reported in Brookhaven National Laboratory Unclassified Report BNL-39 (Jan. 1950)	47K42	J D Kurbatov, D C MacDonald, M. L. Pool, and L. L. Quill, Phys. Rev. <u>61</u> , 106 (1942) (A)
32K51	S. Katcoff, B. Finkle, and N. Sugarman, NNES-PPR 9, 587 (1951)	47K43	J. D. Kurbatov and M. L. Pool, Phys. Rev. <u>63</u> , 463 (1943) (A)
32K5la	S. Katcoff and E. J. Hoagland, NNES-PPR 9, 659 (1951)	48K51	K. G. Kessler and W. F. Meggers, Phys. Rev. 80, 905 (1951)
32K5Ib	S. Katcoff and B. Finkle, NNES-PPR 9, 705 (1951)	49K50	H. Kuhn and K. G. Woodgate, Nature 166, 906 (1950);
32K5lc	S. Katcoff, NNES-PPR 9, 765 (1951)		Proc. Phys. Soc. (London) 64A, 1090 (1951)
32K5Id	S. Katcoff, NNES-PPR 9, 980 (1951)	50K48	L. I. Katzin and M. Pobereskin, Phys. Rev. 74, 264 (1948)
32K5le	S. Katcoff, C. R. Dillard, H. Finston, B. Finkle, J. A. Seiler, and N. Sugarman, NNES-PPR 9.	50K52	L. I. Katzin and F. Hagemann, NNES-PPR <u>17B.</u> 582 (1952) (classified)
	1005 (1951)	51K51	J. Kastner, Can. J. Phys. 29, 480 (1951)
32K5If	S. Katcoff, O. A. Schaeffer, and J. M. Hastings, Phys. Rev. 82, 688 (1951)	52K51	I. Kirshenbaum, J. Graff, and H. Forstat, NNES Div. III, 4A, 393 (1951)
32K51g	S. Katcoff, B. Finkle, N. Sugarman, L. E. Glendenin, and L. Winaberg, NNES-PPR 9, 1017 (1951)	53K43	S. Kikuchi, et al., Proc. PhysMath. Soc. Japan 25, 502 (1943)
32K51h	S. Katcoff, B. Finkle, E. J. Hoagland, N. Sugarman, L. E. Glendenin, and R. P. Metcalf, NNES-PPR 9, 982 (1951)	54K52	P. Kofstad and G. T. Seaborg, reported in University of California Radiation Laboratory Classified Report UCRL-1770 (April 1952)
32K51i	S. Katcoff, B. Finkle, and N. Sugarman, NNES-PPR 9, 1097 (1951)	55K52	V. E. Krohn, Jr. and E. F. Shrader, Phys. Rev. 87, 685 (1952)
32K51j	S. Katcoff, NNES-PPR 9, 1147 (1951)	56K52	C. Kikuchi, M. H. Sirvetz, and V. W. Cohen,
32K51k	S. Katcoff, NNES-PPR 9, 1400 (1951)		Phys. Rev. 88, 142 (1952)
32K52	S. Katcoff, Phys. Rev. <u>87</u> , 886 (1952)	57K51	J. D. Keys, Ph. D. Thesis, McGill University (1951)
32K52a	S. Katcoff, reported in Brookhaven National Laboratory Unclassified Report BNL-149 (March 1952)	58K52	J. Kraushaar, E. Wilson, and K. T. Bainbridge, private communication (Oct. 1952)
33K35	B. Kurtchatov, I. Kurtchatov, L. Myssowsky, and L. Roussinov, Compt. rend. 200, 1201 (1935)	59K51	S. Kageyama, J. Phys. Soc. Japan <u>6</u> , 285 (1951)
34K49	J Koch, O. Kofoed-Hansen, P Kristensen, and	59K52	S. Kageyama, J. Phys. Soc. Japan 7, 93 (1952)
	W Drost-Hansen, Phys. Rev. <u>76</u> , 279 (1949)	60K52	L. Koester, H. Maier-Leibnitz, T. Mayer-Kuckuk, K. Schmeiser, and G. Schulze-Pillot, Z. Physik
35K5I	O. Kofoed-Hansen and P. Kristensen, Phys. Rev. 82, 96 (1951)	61K52	133, 319 (1952)
35K5la	O. Kofoed-Hansen and K. O. Nielsen, Phys. Rev. 82, 96 (1951); Kgl. Danske Videnskab. Selskab, Mat. fys. Medd. <u>26</u> , No. 7 (1951)	26710	R. M. Kloepper, E. S. Lennox, and M. L. Wiedenbeck, Phys. Rev. 88, 695 (1952)
35К51Ь	O. Kofoed-Hansen, Phil. Mag. 42, 1448 (1951)		
36K 35	O. Klemperer, Proc. Roy. Soc. (London) 148A, 638 (1935)		
37K49	M. Kemmerich, Z. Physik 126, 399 (1949)	1L35	E. O. Lawrence, Phys. Rev. <u>47</u> , 17 (1935)
38K50	E. Kondaiah, Phys. Rev. 79, 891 (1950)	21.47	P. W. Levy, Phys. Rev. 72, 352 (1947)
38K50a	E. Kondaiah, Arkiv Fysik 2, 295 (1950)	2L47a	P. W. Levy, Phys. Rev. 72, 248 (1947)
38K51	E. Kondaiah, Phys. Rev. 83, 471 (1951)	2L48	P. W. Levy and E. Greuling, Phys. Rev. 73, 83 (1948)
38K51a	E. Kondaiah, Phys. Rev. 81, 1056 (1951)	2L49	P. W. Levy, reported in Oak Ridge National
38K5lb	E. Kondaiah, Arkiv Fysik 3, 47 (1951)		Laboratory Unclassified Report ORNL-312 (March 1949); U. S. Atomic Energy Commission
38K5lc	E. Kondaiah, reported in M. Siegbahn Commemorative Volume, p 411 (Uppsala, 1951)	2L49a	Unclassified Document AECU-173 (March 1949)  P. W. Levy and E. Greuling, Phys. Rev. 75,
38K5ld	E. Kondaiah, Arkiv Fysik 2, 295 (1951)		819 (1949)
39K 37	J. D. Kraus and J. M. Cork, Phys. Rev. <u>52,</u> 763 (1937)	3L33	W. F. Libby and W. M. Latimer, J. Am. Chem. Soc. <u>55</u> , 433 (1933)
40K52	W. C. Kelly, Phys. Rev. 85, 101 (1952)	3L34	W. F. Libby, Phys. Rev. 45, 845 (1934)
41K52	M. I. Kalkstein and W. F. Libby, Phys. Rev. 85, 368 (1952)	3L39	W. F. Libby and D. D. Lee, Phys. Rev. <u>55</u> , 245 (1939)
42K45	P. G. Kruger and W. E. Ogle, Phys. Rev. 67,	3L39a	W. F. Libby, Phys. Rev. <u>56,</u> 21 (1939)
	273 (1945)	3 L 51	W. F. Libby, private communication (Oct. 1951)
42K52	P. Kruger and C. D. Coryell, private communication (Oct. 1952)	4L47	E. J. Lofgren, reported by (2T47a)
43K50	R. Katz, R. D. Hill, and M. Goldhaber, Phys. Rev.	5L47	G. D. Latyshev, Revs. Modern Phys. 19, 132 (1947)
	<u>78,</u> 9 (1950)	6L38	M. Lecoin, J. phys. et radium 9, 81 (1938)
43K52	R. Katz and M. R. Lee, Phys. Rev. 85, 1038 (1952)	6L43	M. Lecoin, M. Perey, and San-Tsiang Tsien, Compt. rend. 217, 146 (1943)
44K52	T. K. Keenan, R. A. Penneman, and B. B. McInteer, Phys. Rev. 87, 204 (1952) (A)	6L44	M. Lecoin, M. Perey, and San-Tsiang Tsien, Cahiers phys. No. 26, 10 (1944)



- 6L47 M. Lecoin, Compt. rend. 224, 912 (1947)
  6L48 M. Lecoin, M. Perey, and J. Teillac, Compt. rend. 227, 121 (1948)
  6L49 M. Lecoin, M. Perey, and M. Riou, J. phys. et radium 10, 390 (1949)
  6L49a M. Lecoin, M. Perey, and J. Teillac, J. phys. et radium 10, 33 (1949)
- 6L50 M. Lecoin, M. Perey, M. Riou, and J. Teillac, J. phys. et radium 11, 227 (1950)
- 7L50 C. R. Lagergren and M. E. Kettner, Phys. Rev. 80, 102 (1950)
- 8L39 D. D. Lee and W. F. Libby, Phys. Rev. <u>55</u>, 252 (1939)
- 9L44 A. L. Lutz, M. L. Pool, and J. D. Kurbatov, Phys. Rev. <u>65</u>, 61 (1944) (A)
- 10L37 L. M. Langer and M. D. Whitaker, Phys. Rev. <u>51</u>, 713 (1937)
- 10L47 L. M. Langer, C. S. Cook, and M. B. Sampson, Phys. Rev. <u>71</u>, 906 (1947)
- 10L49 L. M. Langer and H. C. Price, Jr., Phys. Rev. 76, 641 (1949)
- 10L49a L. M. Langer and H. C. Price, Jr., reported by (53M49)
- 10L50 L. M. Langer, Phys. Rev. 77, 50 (1950)
- 10L50a L. M. Langer and R. D. Moffat, Phys. Rev. 80, 651 (1950)
- 10L50b L. M. Langer, R. D. Moffat, and H. C. Price, Jr., Phys. Rev. 79, 808 (1950)
- 10L50c L. M. Langer, J. W. Motz, and H. C. Price, Jr., Phys. Rev. 77, 798 (1950)
- 10L50d L. M. Langer and R. D. Moffat, Phys. Rev. 78, 74 (1950)
- 10L51 L. M. Langer and R. D. Moffat, Phys. Rev. 82, 635 (1951)
- 10L51a L. M. Langer and G. Ford, reported in U. S. Atomic Energy Commission Classified Report WASH-62 (Dec. 1951)
- 10L52 L. M. Langer, R. D. Moffat, and G. A. Graves, Phys. Rev. 86, 632 (1952) (A)
- 10L52a L. M. Langer, R. B. Duffield, and C. W. Stanley, private communication (Sept. 1952)
- 10L52b L. M. Langer and R. J. D. Moffat, Phys. Rev. 88, 689 (1952)
- 10L52c L. M. Langer, private communication (Oct. 1952)
- 10L52d L. M. Langer and R. B. Duffield, private communication (Oct. 1952)
- IlL34 W. B. Lewis and B. V. Bowden, Proc. Roy. Soc. (London) 145A, 235 (1934). Summarizes the results of various investigators. Values recalculated according to (9H38)
- 11L37 W. B. Lewis, W. E. Burcham, and W. Y. Chang, Nature 139, 24 (1937)
- 12L36 J. J. Livingood, Phys. Rev. 50, 425 (1936)
- 12L37 J. Livingood, F. Fairbrother, and G. T. Seaborg, Phys. Rev. <u>52</u>, 135 (1937)
- 12L37a J. Livingood and G. T. Seaborg, Phys. Rev. <u>52</u>, 135 (1937)
- 12L38 J. J. Livingood and G. T. Seaborg, Phys. Rev. <u>54</u>, 391 (1938)
- 12L38a J. J. Livingood and G. T. Seaborg, Phys. Rev. <u>54</u>, 51 (1938)
- 12L38b J. J. Livingood and G. T. Seaborg, Phys. Rev. <u>53</u>, 847 (1938)
- 12L38c J. J. Livingood and G. T. Seaborg, Phys. Rev. <u>53</u>, 765 (1938)
- 12L38d J. J. Livingood and G. T. Seaborg, Phys. Rev. <u>54</u>, 88 (1938)

- 12L38e J. J. Livingood and G. T. Seaborg, Phys. Rev. 54, 775 (1938)
- 12L39 J. J. Livingood and G. T. Seaborg, Phys. Rev. <u>55</u>, 457 (1939)
- 12L39a J. J. Livingood and G. T. Seaborg, Phys. Rev. <u>55</u>, 1268 (1939)
- 12L39b J. J. Livingood and G. T. Seaborg, unpublished data (1939)
- 12L39c J. J. Livingood and G. T. Seaborg, Phys. Rev. <u>55</u>, 667 (1939)
- 12L39d J. J. Livingood and G. T. Seaborg, Phys. Rev. <u>55</u>, 414 (1939)
- 12L41 J. J. Livingood and G. T. Seaborg, Phys. Rev. 60, 913 (1941)
- 13L51 R. F. Leininger, E. Segrè, and F. N. Spiess, Phys. Rev. 82, 334 (1951) (A)
- 14L47 A. Lundby, Forsvarets Forskning Institutt, Arbok (1947), 13
- 14L49 A. Lundby, Phys. Rev. 76, 1809 (1949)
- 15L45 G. A. Linenberger, reported in Los Alamos Scientific Laboratory Classified Report LAMS-256 (May 1945)
- 16L51 C. W. Li, W. Whaling, W. A. Fowler, and G. C. Lauritsen, Phys. Rev. 83, 512 (1951)
- 17L38 H. Lu, Phys. Rev. 53, 845 (1938)
- 18L39 A. M. Lawrance, Proc. Cambridge Phil. Soc. 35, 304 (1939)
- 19L44 J. S. Levinger, Metallurgical Laboratory Declassified Report CP-2267 (Oct. 1944)
- 19L47 J. Levinger and E. Meiners, Phys. Rev. <u>71</u>, 586 (1947)
- 19L51 J. S. Levinger, NNES-PPR 9, 757 (1951)
- 19L51a J. S. Levinger, E. P. Meiners, M. B. Sampson, A. H. Snell, and R. G. Wilkinson, NNES-PPR 9, 603 (1951)
- 20L39 A. Langedorf, Jr., Phys. Rev. <u>56</u>, 205 (1939)
- 20L40 A. Langsdorf, Jr. and E. Segrè, Phys. Rev. <u>57</u>, 105 (1940)
- 20L45 A. S. Langsdorf, Jr. and R. L. Purbrick, Metallurgical Laboratory Classified Report CP-3272 (Oct. 1945)
- 21L37 E. M. Lyman, Phys. Rev. <u>51</u>, 1 (1937)
- 21L39 E. M. Lyman, Phys. Rev. 55, 1123 (1939) (A)
- 22L34 M. S. Livingston, M. C. Henderson, and E. O. Lawrence, Phys. Rev. 46, 325 (1934) (A)
- 22L34a M. S. Livingston and E. M. McMillan, Phys. Rev. 46, 437 (1934)
- 23L37 L. J. Laslett, Phys. Rev. <u>52</u>, 529 (1937)
- 23L49 L. J. Laslett, Phys. Rev. <u>76</u>, 858 (1949)
- 23L50 L. J. Laslett, E. N. Jensen, and A. Paskin, Phys. Rev. 79, 412 (1950)
- 24L37 J. L. Lawson and J. M. Cork, Phys. Rev. 52, 531 (1937)
- 24L39 J. L. Lawson, Phys. Rev. <u>56</u>, 131 (1939)
- 24L40 J. L. Lawson and J. M. Cork, Phys. Rev. <u>57</u>, 982 (1940)
- 25L46 D. C. Lincoln and W. H Sullivan, reported in J. Am. Chem. Soc. <u>68</u>, 2411 (1946)
- 25L51 D. C. Lincoln and W. H Sullivan, NNES-PPR 9, 778 (1951)
- 26L40 H. Levi, Nature 145, 588 (1940)
- 27L48 R. V. Langmuir, Phys. Rev. 74, 1559 (1948) (A)
- 28L48 W. T. Leland and A. O. Nier, Phys. Rev. 73, 1206 (1948)
- 28L49 W. T. Leland, Phys. Rev. 76, 1722 (1949)

28L49a	W. T. Leland, Phys. Rev. 76, 992 (1949)	42L40	A. Langer and W. E. Stephens, Phys. Rev. <u>58,</u> 759 (1940)
28L50	W. T. Leland, Phys Rev. <u>77</u> , 634 (1950)	43L52	J. K. Long and M. L. Pool, Phys. Rev. 85, 137
29L49	D. A. Lind, J. R. Brown, and J. W. M. DuMond, Phys. Rev. <u>76</u> , 591 (1949) (A)	43L52a	(1952)
29L49a	D. A. Lind, J. Brown, D. Klein, D. Muller, and J. DuMond, Phys. Rev. 75, 1544 (1949)		Phys. Rev. 88, 171 (1952) (A)
29L51	D. Lind and A. Hedgran, reported in M. Siegbahn Commemorative Volume, p 283 (Uppsala, 1951)	44 L41	H. B. Law, M. L. Pool, J. D. Kurbatov, and L. L. Quill, Phys. Rev. <u>59</u> , 936 (1941) (A)
30L47	C. E. Leith, A. Bratenahl, and B. J. Moyer, Phys. Rev. 72, 732 (1947)	45L47	C. M. G. Lattes, E. G. Samuel, and P. Cuer, Anais acad. brasil. cienc. 19, 1 (1947)
31L40	R. S. Livingston and B. T. Wright, Phys. Rev. 58, 656 (1940)	46L51	M. J. W. Laubenstein, R. A. Laubenstein, L. J. Koester, and R. C. Mobley, Phys. Rev. 81, 654 (1951) (A)
32L47	H. A. Levy and M. H. Feldman, reported in	47L50	R. M. Littauer, Phil. Mag. 41, 1214 (1950)
	Oak Ridge National Laboratory Classified Report Mon N-432 (Dec. 1947)	48L50	E. Luscher, R. Ricamo, P. Scherrer, and W. Zunti, Helv. Phys. Acta 23, 561 (1950)
32L48	H. A. Levy and B. Zemel, reported in Oak Ridge National Laboratory Classified Report ORNL-176 (Nov. 1948)	49L51	G. Lindström, Arkiv Fysik 4, 1 (1951); Phys. Rev. 83, 465 (1951)
32L49	H. A. Levy and M. H. Feldman, reported in Oak	49L52	G. Lindström, Phys. Rev. 87, 678 (1952)
	Ridge National Laboratory Classified Report ORNL-286 (Sept. 1949)	50L52	G. M. Lewis, Phil. Mag. 43, 1070 (1952)
33L49	L. Lidofsky, P. Macklin, and C. S. Wu, Phys. Rev. 76, 1888 (1949)	51L51	J. Lascoux and G. Vendryes, Compt. rend. 233, 858 (1951)
33L50	L. J. Lidofsky, P. A. Macklin, and C. S. Wu, Phys. Rev. 78, 318 (1950) (A)	52L52	H. B. Levy and I. Perlman, Phys. Rev. <u>85</u> , 758 (1952) (A); unpublished data (Nov. 1952)
33L51	L. Lidofsky, P. Macklin, and C. S. Wu, reported in Columbia University Report CU-97 (Nov. 1951)	53L52	D. L. Livesey and C. L. Smith, Proc. Phys. Soc. (London) 65A, 758 (1952)
33L52	L. Lidofsky, P. Macklin, and C. S. Wu, Phys. Rev. 87, 391 (1952)	54L52	L. M. Litz, S. A. Ring, and W. R. Balkwell, private communication (Nov. 1952)
34L51	J. Laberrigue-Frolow, Compt. rend. 232, 1201 (1951)		
34L52	J. Laberrigue-Free, Compt. rend. 234, 2599 (1952)		
35L49	W. S. Lyon, reported in Oak Ridge National Laboratory Classified Report ORNL-286 (Sept. 1949)		
35L51	W. S. Lyon and D. J. Coombe, reported in Oak	1M23	L. Meitner, Z. Physik 17, 54 (1923)
	Ridge National Laboratory Classified Report ORNL-1088 (Oct. 1951)	1M28	L. Meitner, Z. Physik 52, 637, 645 (1928)
35L51a	W. S. Lyon, Phys. Rev. 82, 276 (1951)	1M 28a	L. Meitner, Z. Physik <u>50</u> , 15 (1928)
35L52	W. S. Lyon, Phys. Rev. 87, 1126 (1952)	1 <b>M</b> 37	L. Meitner, O. Hahn, and F. Strassmann, Z. Strassmann, Z. Physik 106, 249 (1937)
35L52a	W. S. Lyon and B. Kahn, reported in Oak Ridge National Laboratory Classified Report ORNL-1276	1M38	L. Meitner, F. Strassmann, and O. Hahn, Z. Physik <u>109</u> , 538 (1938)
36L39	(Oct. 1952)  C. Lieber, Naturwiss. 27, 421 (1939)	1M40	L. Meitner, Arkiv Mat., Astron. Fysik 27A, No. 17 (1940)
37L48	M. Lindner and I. Perlman, Phys. Rev. 73, 1202	1M48	L. Meitner, Ann. Physik 3, 115 (1948)
37L48a	(1948)  M. Lindner and I. Perlman, Phys. Rev. 73, 1124 (1948)	2M14	S. Meyer, V. F. Hess, and F. Paneth, Wien. Ber. 123, 1459 (1914)
37L48b	M. Lindner and I. Perlman, unpublished data (May 1948)	3M41	W. Maurer and W. Ramm, Naturwiss. 29, 368 (1941); Z. Physik 119, 334 (1942)
37L50	M. Lindner and I. Perlman, Phys. Rev. 78, 499 (1950)	3M42	W. Maurer and W. Ramm, Z. Physik 119, 602 (1942)
37L50a	M. Lindner and J. S. Coleman, Phys. Rev. 78, 67	3M47	W. Maurer, Z. Naturforsch. 2a, 586 (1947)
	(1950)	3M49	W. Maurer, Z. Naturforsch. 4a, 150 (1949)
37L51	M. Lindner, Phys. Rev. 84, 240 (1951)	4M50	J. F. Miller, J. G. Hamilton, T. M. Putnam,
37L51a	M. Lindner and J. S. Coleman, J. Am. Chem. Soc. 73, 1610 (1951)		H. R. Haymond, and G. B. Rossi, Phys. Rev. 80, 486 (1950)
37L52	M. Lindner and R. Osborne, private communication (July 1952)	5M50	M. Miwa and S. Kageyama, J. Phys. Soc. Japan 5, 416 (1950)
37L53	M. Lindner, Phys. Rev. (to be published) (1953)	6M48	D. G. E. Martin, H. O. W. Richardson, and Yun-Kuei Hsü, Proc. Phys. Soc. (London) 60,
38L39	K. Lark-Horowitz, J. R. Risser, and R. N. Smith, Phys. Rev. 55, 878 (1939)		466 (1948)
39L49	J. C. Lee and M. L. Pool, Phys. Rev. 76, 606 (1949)	6M48a	D. G. E. Martin and H. O. W. Richardson, Proc. Roy. Soc. (London) 195A, 287 (1948)
40L46	G. R. Leader, reported in J. Am. Chem. Soc. <u>68</u> , 2411 (1946)	6M50	D. G. E. Martin and H. O. W. Richardson, Proc. Phys. Soc. (London) 63A, 223 (1950)
40L51	G. R. Leader, NNES-PPR 9, 919 (1951)	7M48	K. R. MacKensie, private communication (1948)
40L51a	G. R. Leader and W. H Sullivan, NNES-PPR 9,	8M37	J. Mattauch, Naturwiss. 25, 189 (1937)
411.51	934 (1951)  J. S. Lawson, Phys. Rev. 81, 299 (1951) (A)	8M39	J. Mattauch and H. Lichtblau, Z. Physik III, 514 (1939)
41L51	J. S. Mawson, Phys. Rev. of, 277 (1791) [K]		

MOCL	EAR FII ISIOS		Chap. 1.2
9M52	F. F. Momyer, F. Asaro, and E. K. Hyde, private communication (Aug. 1952)	14M49a	A. C. G. Mitchell and C. L. Peacock, Phys. Rev. 75, 197 (1949)
9M52a	F. F. Momyer, E. K. Hyde, A. Ghiorso, and W. E. Glenn, Phys. Rev. <u>86</u> , 805 (1952)	14M51	A. C. G. Mitchell and L. J. Brown, NNES-PPR 9, 717 (1951)
9M52b	F. F. Momyer, A. Ghiorso, and E. K. Hyde, private communication (Aug. 1952)	14M52	A. C. G. Mitchell and A. B. Smith, Phys. Rev. 85, 153 (1952)
9M52c	F. F. Momyer and E. K. Hyde, unpublished data (Dec. 1952)	14M52a	A. C. G. Mitchell and R. S. Caird, Phys. Rev. 87, 388 (1952)
10 <b>M47</b>	R. L. Macklin and G. B. Knight, Phys. Rev. <u>72</u> , 435 (1947)	15M45	L. B. Magnusson and A. Ghiorso, unpublished data (1945)
10M49	R. L. Macklin, Phys. Rev. 76, 595 (1949)	15M47	L. B. Magnusson and T. J. LaChapelle, unpublished
11M48	W. W. Meinke, A. Ghiorso, and G. T. Seaborg, unpublished data (July 1948)	15M48	data (1947)  L. B. Magnusson and T. J. LaChapelle, J. Am.
11M49	W. W. Meinke, A. Ghiorso, and G. T. Seaborg, Phys. Rev. 75, 314 (1949)		Chem. Soc. 70, 3534 (1948); NNES-PPR 14B, 39 (1949)
11M50	W. W. Meinke and G. T. Seaborg, Phys. Rev. <u>78</u> , 475 (1950)	15M50	L. B. Magnusson, S. G. Thompson, and G. T. Seaborg, Phys. Rev. 78, 363 (1950)
11M51	W. W. Meinke, A. Ghiorso, and G. T. Seaborg, Phys. Rev. 81, 782 (1951)	16 <b>M49</b>	W. M. Manning and L. B. Asprey, NNES-PPR 14B, 1595 (1949)
11M52	W. W. Meinke, A. Ghiorso, and G. T. Seaborg,	17M 39	H. Maier-Leibnitz, Naturwiss. 26, 614 (1939)
11M52a	Phys. Rev. <u>85</u> , 429 (1952)  W. W. Meinke and K. L. Hall, private	18M51	C. H. Millar and A. G. W. Cameron, Phys. Rev. 81, 316 (1951) (A)
	w. w. meinke and t. D. Hall, private communication (Oct. 1952)  W. W. Meinke, Phys. Rev. (to be published) (1953)	18M51a	C. H. Millar, G. A. Bartholomew, and B. B. Kinsey, Phys. Rev. 81, 150 (1951)
11M53 12M35	E. M. McMillan and M. S. Livingston, Phys. Rev.	18M52	C. H. Millar and A. G. W. Cameron, private communication (Oct. 1952)
12M 35a	47, 452 (1935)  E. M. McMillan and E. O. Lawrence, Phys. Rev.	18M52a	C. H. Millar, G. A. Bartholomew, and B. B. Kinaey, private communication (Oct. 1952)
12M37	47, 343 (1935)  E. M. McMillan, M. Kamen, and S. Ruben, Phys. pp. 43 375 (1037)	19M47	A. N. May and E. P. Hincks, Can. J. Research 25A, 77 (1947)
12M39	Rev. <u>52</u> , 375 (1937)  E. M. McMillan, Phys. Rev. 55, 510 (1939)	20M51	G. G. Manov and L. F. Curtiss, J. Research Natl. Bur. Standards 46, 328 (1951)
12M40	E. M. McMillan, Phys. Rev. 58, 178 (1940)	21M50	W. W. Miller, R. Ballentine, W. Bernstein,
12M40a	E. M. McMillan and P. H. Abelson, Phys. Rev. <u>57</u> , 1185 (1940)		L. Friedman, A. O. Nier, and R. D. Evans, Phys. Rev. 77, 714 (1950)
12M46	E. M. McMillan, private communication (June 1946)	22M43	J. Marshall, reported in Metallurgical Laboratory Classified Report CP-718 (June 1943)
12 <b>M46a</b>	E. M. McMillan and S. Ruben, Phys. Rev. <u>70,</u> 123 (1946)	23M50	P. A. Macklin, L. J. Lidofsky, and C. S. Wu, Phys. Rev. 78, 318 (1950) (A)
12M46b	E. M. McMillan and T. M. Putnam, private communication (July 1946)	23M50a	P. A. Macklin, L. Feldman, L. Lidofsky, and C. S. Wu, Phys. Rev. 77, 137 (1950)
12M46c	E. M. McMillan, W. J. Knox, and R. H. Goeckermann, private communication (June 1946)	23M51	P. A. Macklin, L. I. Lidofsky, and C. S. Wu, Phys. Rev. 82, 334 (1951) (A)
12M47	E. M. McMillan, Phys. Rev. 72, 591 (1947)	23M5la	P. Macklin, L. Lidofsky, and C. S. Wu, reported
12M47a	E. M. McMillan, private communication (Jan. 1947)		in Columbia University Unclassified Report CU-96 (June 1951)
13M47	L. Melander, Acta Chem. Scan. 1, 169 (1947)	24M37	C. Magnan, Compt. rend. 205, 1147 (1937)
13 <b>M48</b>	L. Melander and H. Slätis, Phys. Rev. 74, 709 (1948); Arkiv Mat., Astron. Fysik 36A, No. 15 (1949)	24M4I	C. Magnan, Ann. phys. 15, 5 (1941)
14M37	A. C. G. Mitchell, Phys. Rev. <u>51</u> , 995 (1937)	25M49	K. H. Morganstern and K. P. W. Wolf, Phys. Rev. 76, 1261 (1949)
14M38	A. C. G. Mitchell, Phys. Rev. 53, 269 (1938)	26M42	C. E. Mandeville, Phys. Rev. <u>62</u> , 555 (1942)
14M38a	A. C. G. Mitchell and L. M. Langer, Phys. Rev.	26M43	C. E. Mandeville, Phys. Rev. <u>63</u> , 387 (1943)
14M40	53, 505 (1938)  A. C. G. Mitchell, L. M. Langer, and P. W. McDaniel,	26 M 4 3 a	C. E. Mandeville, Phys. Rev. 64, 147 (1943)
14M42	Phys. Rev. 57, 1107 (1940)  A. C. G. Mitchell, L. M. Langer, and L. J. Brown,	26M48	C. E. Mandeville and M. V. Scherb, Phys. Rev. 73, 141 (1948)
	Metallurgical Project Classified Report (work performed at Indiana University) CN-409 (Dec. 1942)	26M48a	C. E. Mandeville and M. V. Scherb, Phys. Rev. 73, 1434 (1948)
14M43	A. C. G. Mitchell, L. Slotin, J. Marshall, V. A. Nedsel, L. J. Brown, and J. R. Pruett, Metallurgical Laboratory Classified Report CP-597	26M48b	C. E. Mandeville, M. V. Scherb, and W. B. Keighton, Phys. Rev. 74, 888 (1948)
14M47	(April 1943)  A. C. G. Mitchell, E. T. Jurney, and M. Ramsey,	26M48c	C. E. Mandeville and M. V. Scherb, Phys. Rev. 73, 848 (1948)
14M48	Phys. Rev. 71, 825 (1947)  A. C. G. Mitchell, D. J. Zaffarano, and B. D. Kern,	26M48d	C. E. Mandeville and M. V. Scherb, Phys. Rev. 73, 340 (1948)
14M49	Phys. Rev. 73, 1424 (1948)  A. C. G. Mitchell, J. Y. Mei, F. C. Maienschein,	26M48e	C. E. Mandeville, M. V. Scherb, and W. B. Keighton, Phys. Rev. 74, 601 (1948)
144637	and C. L. Peacock, Phys. Rev. <u>76</u> , 1450 (1949)	26M49	C. E. Mandeville, Y. H. Woo, M. V. Scherb, W. B. Keighton, and E. Shapiro, Phys. Rev. 75, 1528 (1949)

- 26M49a C. E. Mandeville, M. V. Scherb, and W. B. Keighton, Phys. Rev. 75, 221, 329 (1949)
- 26M49b C. E. Mandeville and E. Shapiro, Phys. Rev. 75, 897 (1949)
- 26M49c C. E. Mandeville and E. Shapiro, Phys. Rev. 76, 718 (1949)
- 26M49d C. E. Mandeville, Phys. Rev. 75, 1017 (1949)
- 26M49e C. E. Mandeville and E. Shapiro, Phys. Rev. 75, 1834 (1949)
- 26M49f C. E. Mandeville and M. V. Scherb, Phys. Rev. 76, 186 (1949) (A)
- 26M50 C. E. Mandeville and E. Shapiro, Phys. Rev. 77. 439 (1950)
- 26M50a C. E. Mandeville and E. Shapiro, Phys. Rev. 79, 243 (1950) (A)
- 26M50b C. E. Mandeville and E. Shapiro, Phys. Rev. <u>79</u>, 391 (1950)
- 26M51 C. E. Mandeville and E. Shapiro, Phys. Rev. 82, 953 (1951); J. Franklin Inst. 253, 145 (1952)
- 26M52 C. E. Mandeville, E. Shapiro, R. I. Mendenhall, E. R. Zucker, and G. L. Conklin, Phys. Rev. 86, 813 (1952)
- 26M52a C. E. Mandeville E. Shapiro, R. I. Mendenhall, E. R. Zucker, and G. L. Conklin, Phys. Rev. 88, 554 (1952)
- 27M49 J. McElhinney, A. O. Hanson, R. A. Becker, R. B. Duffield, and B. G. Diven, Phys. Rev. <u>75</u>, 542 (1949)
- 28M40 B. L. Moore, Phys. Rev. 57, 355 (1940) (A)
- 29M52 H. T. Motz and D. E. Alburger, Phys. Rev. 86, 165 (1952)
- 29M52a H. T. Motz, Phys. Rev. 85, 501 (1952)
- 30M40 R. L. McCreary, G. Kuerti, and S. N. Van Voorhis, Phys. Rev. <u>57</u>, 351 (1940) (A)
- 31M40 D. Mulder, G. W. Hoeksema, and G. J. Sizoo, Physica 7, 849 (1940)
- 32M48 D. R. Miller, R. C. Thompson, and B. B Gunningham, Phys. Rev. <u>74</u>, 347 (1948)
- 32M48a D. R. Miller, Ph. D. Thesis, University of California Radiation Laboratory Declassified Report UCRL-142 (July 1948)
- 32M50 D. R. Miller, Phys. Rev. 78, 808 (1950)
- 33M49 V. Myers and A. Wattenberg, Phys. Rev. <u>75</u>, 992 (1949)
- 34M47 H. A. Meyer, G. Schwachheim, and M. D. de Souza Santos, Phys. Rev. <u>71</u>, 908 (1947)
- 35M51 P. Morrison, Phys. Rev. 82, 209 (1951)
- 36M47 D. E. Matthews and M. L. Pool, Phys. Rev. 72, 163 (1947) (A)
- 37M49 J. L. Meem, Jr. and F. Maienachein, Phys. Rev. 76, 328 (1949)
- 38M47 E. der Mateosian, M. Goldhaber, C. O. Muehlhause, and M. McKeown, Phys. Rev. 72, 1271 (1947)
- 38M49 E. der Mateosian, M. Goldhaber, and A. Smith, reported in Argonne National Laboratory Classified Report ANL-4237 (Jan. 1949)
- 38M49a E. der Mateosian and M. Goldhaber, Phys. Rev. <u>76</u>, 187 (1949) (A)
- 38M50 E. der Mateosian and M. Goldhaber, Phys. Rev. 79, 192 (1950)
- 38M50a E. der Mateosian, M. Goldhaber, and D. E. Alburger, reported in Brookhaven National Laboratory Unclassified Report BNL-39 (Jan. 1950)
- 38M51 E. der Mateosian and M. Goldhaber, Phys. Rev. 82, 115 (1951)
- 38M5la E. der Mateosian, Phys. Rev. 83, 223 (1951) (A)
- 38M5lb E. der Mateosian and M. Goldhaber, Phys. Rev.  $\underline{83}$ , 843 (1951)

- 38M51c E. der Mateosian and M. Goldhaber, unpublished data quoted in (18G52)
- 38M52 E. der Mateosian, private communication (Oct. 1952)
- 38M52a E. der Mateosian, G. Friedlander, M. Goldhaber, and A. W. Sunyar, quoted in (18G52)
- 39M50 M. L. Moon, M. A. Waggoner, and A. Roberts, Phys. Rev. <u>79</u>, 905 (1950)
- 40M47 A. E. Miller and M. Deutsch, Phys. Rev. 72, 527 (1947) (A)
- 41M50 W. Mims, H. Halban, and R. Wilson, Nature 166, 1027 (1950)
- 41M51 W. Mims and H. Halban, Proc. Phys. Soc. (London) 64A, 311 (1951)
- 41M5la W. B. Mims and H. Halban, Proc. Phys. Soc. (London) 64A, 753 (1951)
- 42M47 J. Martelly, Ann. phys. 2, 555 (1947)
- 43M46 L. C. Miller and L. F. Curtiss, Phys. Rev. 70, 983 (1946)
- 43M47 L. C. Miller and L. F. Curtiss, J. Research Natl. Bur. Standards 38, 359 (1947)
- 44M48 F. Metzger and M. Deutsch, Phys. Rev. 74, 1640 (1948)
- 44M50 F. Metzger, Phys. Rev. 79, 398 (1950)
- 44M50a F. Metzger and M. Deutsch, Phys. Rev. <u>78</u>, 551 (1950)
- 44M51 F. R. Metzger and R. D. Hill, Phys. Rev. 82, 646 (1951)
  - 14M52 F. R. Metzger, Phys. Rev. 85, 727 (1952) (A)
- 44M52a F. R. Metzger, Phys. Rev. 86, 435 (1952)
- 44M52b F. R. Metsger and H. C. Amacher, Phys. Rev. 88, 147 (1952)
- 45M4l J. J. Mitchell, H. S. Brown, and R. D. Fowler, Phys. Rev. <u>60</u>, 359 (1941)
- 46M49 F. Maienschein and J. L. Meem, Jr., Phys. Rev. 76, 899 (1949)
- 46M51 F. C. Maienschein, J. K. Bair, and W. B. Baker, Phys. Rev. <u>83</u>, 477 (1951)
- 47M47 W. E. Meyerhof and G. Scharff-Goldhaber, Phys. Rev. 72, 273 (1947)
- 47M48 W. E. Meyerhof and M. Goldhaber, Phys. Rev. 74, 348 (1948)
- 47M48a W. E. Meyerhof, Phys. Rev. 74, 621 (1948)
- 47M52 W. E. Meyerhof, L. G. Mann, and H. I. West, Jr., private communication (Oct. 1952)
- 48M49 K. C. Mann, D. Rankin, and P. N. Daykin, Phys. Rev. <u>76</u>, 1719 (1949)
- 48M51 K. C. Mann and G. H. Hanson, Phys. Rev. 83, 893 (1951) (A)
- 49M50 A. Mukerji and P. Preiswerk, Helv. Phys. Acta 23, 516 (1950)
- 49M52 A. Mukerji and P. Preiswerk, Helv. Phys. Acta 25, 387 (1952)
- 50M37 W. B. Mann, Phys. Rev. 52, 405 (1937)
- 50M38 W. B. Mann, Phys. Rev. 54, 649 (1938)
- 50M38a W. B. Mann, Phys. Rev. 53, 212 (1938) (A)
- 51M48 D. A. McCown, L. L. Woodward, and M. L. Pool, Phys. Rev. <u>74</u>, 1311 (1948)
- 51M48a D. A. McCown, L. L. Woodward, and M. L. Pool, Phys. Rev. <u>74</u>, 1315 (1948)
- 52M49 F. K. McGowan, Phys. Rev. 76, 1730 (1949)
- 52M50 F. K. McGowan, Phys. Rev. <u>80</u>, 482 (1950)
- 52M50a F. K. McGowan, Phys. Rev. 80, 923 (1950)
- 52M50b F. K. McGowan, Phys. Rev. 79, 404 (1950)

	F. K. McGowan, Phys. Rev. <u>77</u> , 138 (1950)	62M52	H. Medicus and H. T. Easterday, Phys. Rev. <u>85,</u> 735 (1952) (A)
52M51	F. K. McGowan, Oak Ridge National Laboratory Unclassified Report ORNL-952 (March 1951)	63M50	J. W. Mihelich and R. D. Hill, Phys. Rev. 79, 781 (1950)
52M51a 52M52	F. K. McGowan, Phys. Rev. <u>81</u> , 1066 (1951)  F. K. McGowan, Phys. Rev. <u>85</u> , 142 (1952)	63M51	J. W. Mihelich, M. Goldhaber, and E. Wilson, Phys. Rev. 82, 972 (1951)
52M52a	F. K. McGowan, Phys. Rev. 85, 151 (1952)	63M51a	J. W. Mihelich, reported in Brookhaven National Laboratory Unclassified Report BNL-93 (March 1951)
52M52b	F. K. McGowan and E. D. Klema, reported in Oak Ridge National Laboratory Unclassified	63M52	J. W. Mihelich and E. L. Church, Phys. Rev. 85,
52M52c	Report ORNL-1164 (April 1952)  F. K. McGowan, Phys. Rev. 87, 542 (1952)	63M52a	690 (1952)  J. W. Mihelich, Phys. Rev. 87, 646 (1952)
52M52d	F. K. McGowan, E. D. Klema, and P. R. Bell,	63M52b	J. W. Mihelich, private communication (Oct. 1952)
JEM JEG	Phys. Rev. 85, 152 (1952)	63M52c	J. W. Mihelich and A. de Shalit, private
52M52e	F. K. McGowan, private communication (Oct. 1952)		communication (Nov. 1952)
53M49	J. Y. Mei, A. C. G. Mitchell, and D. J. Zaffarano, Phys. Rev. <u>76</u> , 1883 (1949)	63M52d	J. W. Mihelich, Bull. A. P. S. <u>27</u> , No. 5, Abstract V3 (1952)
53M50	J. Y. Mei, A. C. G. Mitchell, and C. M. Huddleston, Phys. Rev. 79, 19 (1950)	64M40	O. Minakawa, Phys. Rev. <u>57</u> , 1189 (1940)
53M50a	J. Y. Mei, C. M. Huddleston, and A. C. G.	64M41	O. Minakawa, Phys. Rev. 60, 689 (1941)
	Mitchell, Phys. Rev. 79, 429 (1950)	65M52	A. K. Mousuf, Phys. Rev. 88, 150 (1952)
53M50b	J. Y. Mei, C. M. Huddleston, and A. C. G. Mitchell, Phys. Rev. <u>79</u> , 1010 (1950)	66M5I	C. L. McGinnis, Phys. Rev. 81, 734 (1951)
54M44	N. Marty, J. phys. et radium 5, 276 (1944)	66M51a	C. L. McGinnis, Phys. Rev. 83, 686 (1951)
5÷M49	N. Marty, J. Labeyrigue, and H. Langevin, Compt. rend. 228, 1722 (1949)	/5M52	C. L. McGinnis, Phys. Rev. 87, 202 (1952) (A) and private communication (Oct. 1952)
54M51	N. Marty-Wollman, Ann. phys. 6, 662 (1951)	67M51	R. P. Metcalf, NNES-PPR 9, 891 (1951)
55M50	H. R. Muether and S. L. Ridgway, Phys. Rev. 80,	67M51a	R. P. Metcalf, NNES-PPR 9, 898 (1951)
	750 (1950)	67M51b	R. P. Metcalf, NNES-PPR 9, 905 (1951)
56M50	J. Miskel, Phys. Rev. 79, 403 (1950)	68M49	E. C. Mallary and M. L. Pool, Phys. Rev. 76, 1454 (1949)
56M50a	J. Miskel and G. Friedlander, reported in Brookhaven National Laboratory Unclassified Report BNL-39 (Jan. 1950)	68M50	E. C. Mallary and M. L. Pool, Phys. Rev. 77, 75 (1950)
56M51	J. A. Miskel and A. C. Wahl, Phys. Rev. <u>84</u> , 700 (1951)	69M51	M. M. Miller, C. H. Pruett, and R. G. Wilkinson, Phys. Rev. <u>84</u> , 849 (1951)
56M52	J. A. Miskel and M. L. Perlman, Phys. Rev. <u>87,</u> 543 (1952)	69M51a	M. M. Miller and R. G. Wilkinson, Phys. Rev. <u>83,</u> 1050 (1951)
57 <b>M4</b> 1	A. Moussa and L. Goldstein, Phys. Rev. <u>60</u> , 534 (1941); Compt. rend. <u>212</u> , 986 (1941)	69M51b	M. M. Miller and R. G. Wilkinson, Phys. Rev. <u>82</u> , 981 (1951)
58M50	L. G. Mann and P. Axel, Phys. Rev. 80, 759 (1950)	69M52	M. M. Miller, Phys. Rev. 88, 516 (1952)
58M51	L. G. Mann and P. Axel, Phys. Rev. 84, 221 (1951)	70M49	W. C. Miller and B. Waldman, Phys. Rev. <u>75,</u> 425 (1949)
58M52	L. G. Mann and W. E. Meyerhof, Phys. Rev. 87, 202 (1952) (A) and private communication with H. I. West, Jr. (Oct. 1952)	71M50	E. A. Martell and W. F. Libby, Phys. Rev. <u>80</u> , 977 (1950)
59M44	W. N. Moquin and M. L. Pool, Phys. Rev. 65,	72M52	J. A. McCarthy, Phys. Rev. 87, 194 (1952) (A)
60M48	60 (1944) (A)  D. L. Mock, R. C. Waddel, L. W. Fagg, and	73M52	H. B. Mathur, M. Michel, T. O. Passell, and E. K. Hyde, private communication (Dec. 1952)
61M47	R. A. Tobin, Phys. Rev. <u>74</u> , 1536 (1948)  E. E. Motta, Q. V. Larson, and G. E. Boyd, Phys. Rev. 72, 1270 (1947)	74M50	L. Marquez and I. Perlman, Phys. Rev. 78, 189 (1950)
61M47a	E. E. Motta, Q. V. Larson, and G. E. Boyd, reported in Oak Ridge National Laboratory Classified	74M5I	L. Marques and I. Perlman, Phys. Rev. <u>81</u> , 953 (1951)
	Report Mon N-432 (Dec. 1947)	74M52	L. Marquez, Phys. Rev. 88, 225 (1952)
61М47Ъ	E. E. Motta, G. E. Boyd, and A. R. Brosi, Phys. Rev. 71, 210 (1947)	74M52a	L. Marques, Phys. Rev. <u>86</u> , 406 (1952)
61M48	E. E. Motta and G. E. Boyd, Phys. Rev. 73, 1470 (1948)	75M51	D. S. Martin, Jr. and F. J. Hughes, reported in lowa State College Classified Report ISC-137 (May 1951)
61M48a	E. E. Motta and G. E. Boyd, Phys. Rev. 74, 220 (1948)	75M5la	D. S. Martin, Jr., E. N. Jensen, F. J. Hughes, and R. T. Nichols, Phys. Rev. 82, 579 (1951)
61M48b	E. E. Motta and G. E. Boyd, Phys. Rev. <u>74</u> , 344 (1948)	76M50	J. Macnamara, C. B. Collins, and H. G. Thode, Phys. Rev. <u>78</u> , 129 (1950)
62M49	H. Medicus, D. Maeder, and H. Schneider, Helv. Phys. Acta 22, 603 (1949)	76M50a	J. Macnamara and H. G. Thode, Phys. Rev. 78, 307 (1950)
62M50	H. Medicus, P. Preiswerk, and P. Scherrer, Helv. Phys. Acta 23, 299 (1950)	77M35	J. C. McLennan, L. G. Grimr tt, and J. Read, Nature <u>135</u> , 505 (1935)
62M50a	H. Medicus and P. Preiswerk, Phys. Rev. <u>80,</u> 1101 (1950)	77M35a	J. C. McLennan and W. H. Rann, Nature 136, 831 (1935)

H. Medicus, D. Maeder, and H. Schneider, Helv. Phys. Acta <u>24</u>, 72 (1951); Phys. Rev. <u>81</u>, 652 (1951) (A)

62**M**51

77M35b	J. C. McLennan, L. G. Grimmett, and J. Read, Nature 135, 147 (1935)	99M52	M. McKeown and S. Katcoff, private communication (Oct. 1952)
78M41	M. Melhase, unpublished data, University of California, Berkeley (Sept. 1941)	100M52	D. E. Muller, H. C. Hoyt, D. J. Klein, and J. W. M. DuMond, Phys. Rev. 88, 775 (1952)
79M52	M. H. MacGregor and M. L. Wiedenbeck, Phys. Rev. 86, 420 (1952)		_
80M52	H. C. Martin and B. C. Diven, Phys. Rev. 86, 565 (1952)		
81M42	K. E. Mounce, M. L. Pool, and J. D. Kurbatov, Phys. Rev. 61, 389 (1942) (A)	IN50	T. B. Novey, reported in Argonne National Laboratory Classified Report ANL-4427 (July 1950)
82M35	J. K. Marsh and S. Sugden, Nature 136, 102 (1935)	IN50a	T. B. Novey, Phys. Rev. 78, 66 (1950)
83M50	A. J. Moses and D. S. Martin, Jr., Phys. Rev. 79, 467 (1950)	IN51	T. B. Novey, D. W. Engelkeimeir, E. L. Brady, and L. E. Glendenin, NNES-PPR 9, 678 (1951)
83M51	A. J. Moses and D. S. Martin, Jr., Phys. Rev.	IN51a	T. B. Novey, NNES-PPR 9, 976 (1951)
84M47	84, 366 (1951)  J. A. Marinsky, L. E. Glendenin, and C. D. Coryell, J. Am. Chem. Soc. 69, 2781 (1947)	1N51b	T. B. Novey, W. H. Sullivan, C. D. Coryell, A. S. Newton, N. R. Sleight, and O. Johnson, NNES-PPR 9, 958 (1951)
84M49	J. A. Marinsky, reported in Massachusetts Institute of Technology Unclassified Report NP-1272 (July 1949)	1N51c	T. B. Novey and J. D. Knight, NNES-PPR 9, 1043 (1951)
84M49a	J. A. Marinsky, L. E. Glendenin, and F. Metsger, reported in Massachusetts Institute of Technology	2N36	R. Naidu and R. E. Siday, Proc. Phys. Soc. (London) 48, 332 (1936)
84M51	Unclassified Report NP-1727 (July 1949)  J. A. Marinsky and L. E. Glendenin, NNES-PPR 9,	3N36	M. E. Nahmiae and R. J. Walen, Compt. rend. 203, 71 (1936)
	1229 (1951)	4N50	H. M. Neumann and I. Perlman, Phys. Rev. <u>78,</u> 191 (1950)
84M5la 84M5lb	J. A. Marinsky and L. E. Glendenin, NNES-PPR 9, 1243 (1951)	4N5 0a	H. M. Neumann, J. J. Howland, Jr., and I. Perlman, Phys. Rev. <u>77</u> , 720 (1950)
	J. A. Marinsky and L. E. Glendenin, NNES-PPR 9, 1264 (1951)	4 N5 0b	H. M. Neumann, A. Ghiorso, and I. Perlman, unpublished data (1950)
84M51c	J. A. Marinsky and L. E. Glendenin, NNES-PPR 9, 1254 (1951)	4N51	H. M. Neumann and I. Perlman, Phys. Rev. <u>81,</u> 958 (1951)
84M51d	J. A. Marinsky and L. E. Glendenin, NNES-PPR <u>9</u> , 1969 (1951)	5N38	Y. Nishina, T. Yasaki, K. Kimura, and M. Bawa, Nature 142, 874 (1938)
85M52	G. I. Mulholland and T. P. Kohman, Phys. Rev. 85, 144 (1952)	5N40	Y. Nishina, T. Yasaki, H. Esoe, K. Kimura, and M. Ikawa, Phys. Rev. 57, 1182 (1940)
85M52a	G. I. Mulholland and T. P. Kohman, Phys. Rev. 87, 681 (1952)	5N40a	Y. Nishina, T. Yasaki, K. Kimura, and M. Ikawa, Phys. Rev. 58, 660 (1940)
86M52	R. C. Mack, D. I. Prickett, and M. L. Pool, Phys. Rev. <u>86</u> , 633 (1952) (A)	5N40b	Y. Nishina, T. Yasaki, H. Ezoe, K. Kimura, and M. Ikawa, Nature 146, 24 (1940)
87M50	J. E. Mack, Revs. Modern Phys. 22, 64 (1950)	5N41	Y. Nishina, T. Yasaki, K. Kimura, and M. Ikawa,
88M51	K. Murakawa and J. S. Ross, Phys. Rev. 82, 967 (1951)	5N42	Phys. Rev. 59, 677 (1941)  Y. Nishina, K. Kimura, T. Yasaki, and M. Ikawa,
89M52	D. F. Martin, unpublished data (Aug. 1952)	3.112	Z. Physik 119, 195 (1942)
89M52a	D. F. Martin, R. W. Hoff, G. H. Higgins, and S. G. Thompson, reported in University of California Radiation Laboratory Classified Report	6N36	A. O. Nier and E. E. Hanson, Phys. Rev. <u>50</u> , 722 (1936)
	UCRL-1770 (April 1952)	6N37	A. O. Nier, Phys. Rev. 52, 933 (1937)
90M52	J. H. Moon and A. L. Thompson, Phys. Rev. 83, 892 (1951) (A) and private communication (Oct. 1952)	6N37a	A. O. Nier, Phys. Rev. 52, 885 (1937)
91M51	S. L. Miller, A. Javan, and C. H. Townes,	6N38	A. O. Nier, J. Am. Chem. Soc. 60, 1571 (1938)
, ,	Phys. Rev. 82, 454 (1951)	6N38a	A. O. Nier, Phys. Rev. 53, 282 (1938)
92M51	J. W. Meadows and R. B. Holt, Phys. Rev. <u>83,</u> 1257 (1951)	6N38b	A. O. Nier, Phys. Rev. 54, 275 (1938)
93M51	J. M. Miller and G. Friedlander, Phys. Rev. 84, 589 (1951)	6N39	A. O. Nier, Phys. Rev. 55, 150 (1939), Values recalculated according to (6K41)
94M51	D. Maeder and P. Preiswerk, Phys. Rev. 84,	6N50	A. O. Nier, Phys. Rev. 77, 789 (1950)
	595 (1951)	6N50a	A. O. Nier, Phys. Rev. 79, 450 (1950)
94M51a	D. Maeder and P. Preiswerk, Helv. Phys. Acta 24, 625 (1951)	7N49	A. S. Newton, Phys. Rev. <u>75</u> , 209 (1949)
95M52	J. K. Major, Compt. rend. 234, 2276 (1952); Phys. Rev. 86, 631 (1952) (A)	7N49a 7N49b	A. S. Newton, Phys. Rev. 75, 17 (1949)  A. S. Newton and W. R. McDonell, University of
96M52	J. Moreau and J. Perex y Jorba, Compt. rend. 235, 38 (1952)		California Radiation Laboratory Unclassified Report UCRL-395 (July 1949)
97M52	K. C. Maclure, Ph. D. Thesis, McGill University (Sept. 1952)	7 <b>N</b> 51	A. S. Newton, W. H Sullivan, O. Johnson, and R. Nottorf, NNES-PPR 9, 1028 (1951)
98M51	W. M. Martin, Ph.D. Thesis, McGill University (1951)	7N51a	A. S. Newton, A. Kant, and R. E. Hein, NNES- PPR 9, 1200 (1951)

8N47 A. Novick, Phys. Rev. 72, 972 (1947)

W. M. Martin and S. W. Breckon, Can. J. Phys. (to be published) (1952)

9 N40	G. J. Neary, Proc. Roy. Soc. (London) 175A, 71 (1940)	6048	P. R. O'Connor and G. T. Seaborg, Phys. Rev. 74, 1189 (1948)
10N48	L. D. Norris and M. G. Inghram, Phys. Rev. 73, 350 (1948)	7049	D. A. Orth, L. Marquez, W. J. Heiman, and D. H. Templeton, Phys. Rev. <u>75</u> , 1100 (1949)
11N37	S. Nishida, Proc. Phys Math. Soc. Japan 19, 809 (1937)	7050	D. A. Orth, A. Ghiorso, and G. T. Seaborg, unpublished data (April 1950)
12N35	H. W. Newson, Phys. Rev. 48, 790 (1935)	7051	D. A. Orth and R. A. Glass, unpublished data (March 1951)
12N35a	H. W. Newson, Phys. Rev. 48, 482 (1935) (A)	7051a	D. A. Orth and K. Street, Jr., unpublished data
12N37 13N50	H. W. Newson, Phys. Rev. <u>51</u> , 624 (1937)	7051b	(1951)
13030	Y. A. Nemilov and L. I. Gedeonov, Doklady Akad. Nauk S. S. S. R. 70, 219 (1950)	70518	D. A. Orth and G. D. O'Kelley, Phys. Rev. 82, 758 (1951)
14 <b>N</b> 50	B. D. Nag, S. Sen, and S. Chatterjee, Indian J. Phys. <u>24</u> , 479 (1950)	8050	G. D. O'Kelley and F. L. Reynolds, reported in University of California Radiation Laboratory Classified Report UCRL-550 (Jan. 1950)
15 <b>N4</b> 2	M. E. Nelson, M. L. Pool, and J. D. Kurbatov, Phys. Rev. <u>62</u> , 1 (1942)	8050a	G. D. O'Kelley, G. W. Barton, Jr., W. W. T. Crane, and I. Perlman, Phys. Rev. 80, 293 (1950)
15N42a	M. E. Nelson, M. L. Pool, and J. D. Kurbatov, Phys. Rev. <u>61</u> , 428 (1942)	8051	G. D. O'Kelley, Ph. D. Thesis, University of
15 <b>N</b> 50	M. E. Nelson and M. L. Pool, Phys. Rev. 77, 682 (1950)		California Radiation Laboratory Unclassified Report UCRL-1243 (May 1951)
16N44	B. D. Nag-Chowdhury, Proc. Nat. Inst. Sci. India 10, 317 (1944); Chem. Abs. 42, 4452b (1948)	9049	A. Orsini, Anais faculdade farm. odontol., Univ. São Paulo <u>7</u> , 9 (1949)
17N44	V. A. Nedzel and E. C. Barker, reported in Metallurgical Laboratory Classified Report	10046	R. T. Overman, U. S. Atomic Energy Commission Declassified Document MDDC-354 (Sept. 1946)
100.001	CP-1728 (June 1944)	10047	R. T. Overman, U. S. Atomic Energy Commission Declassified Document AECD-857 (April 1947)
17N51 17N51a	V. A. Nedsel, NNES-PPR 9, 719 (1951)  V. A. Nedsel, NNES-PPR 9, 732 (1951)	11042	R. Overstreet, L. Jacobson, K. Scott, and J. G. Hamilton, Metallurgical Project Declassified Report
17N51b	V. A. Nedsel, NNES-PPR 9, 1213 (1951)		(work performed at Berkeley) CH-379 (Dec. 1942)
18N51	R. W. Nottorf, NNES-PPR 9, 682 (1951)	11043	R. Overstreet and L. Jacobson, reported in Metallurgical Project Classified Report (work performed at Berkeley) CH-498 (Feb. 1943)
19 <b>N</b> 50	C. M. Nelson, B. H. Ketelle, and G. E. Boyd, Oak Ridge National Laboratory Unclassified Report ORNL-828 (Nov. 1950)	11049	R. Overstreet, L. Jacobson, and P. R. Stout, Phys. Rev. 75, 231 (1949)
20N51	G. J. Nijgh, N. F. Verster, R. H. Nussbaum, R. Van Lieshout, and C. J. Bakker, Physica 17, 658 (1951)	11051	R. Overstreet and L. Jacobson, NNES-PPR 9, 621 (1951)
21N50	R. A. Naumann, F. L. Reynolds, and I. Periman, Phys. Rev. 77, 398 (1950)	12042	J. J. O'Connor, M. L. Pool, and J. D. Kurbatov, Phys. Rev. <u>62</u> , 413 (1942)
22N52	W. E. Nervik, reported in University of California Radiation Laboratory Classified Report UCRL-1632	13048	G. E. Owen, D. Moe, and C. S. Cook, Phys. Rev. 74, 1879 (1948); 75, 1270 (1949)
	(Jan. 1952)	13049	G. E. Owen and C. S. Cook, Phys. Rev. <u>76</u> , 1726 (1949)
23N35	E. Neuninger and E. Rona, Anz. Akad. Wiss. Wien, Mathnaturw. Klasse 72, 275 (1935)	13050	G. E. Owen, C. S. Cook, and P. H. Owen, Phys. Rev. 78, 686 (1950)
23N36	E. Neuninger and E. Rona, Ans. Akad. Wiss. Wien, Mathnaturw. Klasse 73, 159 (1936)	14040	Z. Ollano, Ricerca sci. 11, 568 (1940)
24N47	H. Neuert, Z. Naturforsch. 2a, 432 (1947)	14041	Z. Ollano, Nuovo cimento 18, 11 (1941)
25N48	S. N. Naldrett and W. F. Libby, Phys. Rev. <u>73,</u> 487 (1948)	15049	J. S. Osoba, Phys. Rev. 76, 345 (1949)
		16051	J. Ovadia and P. Axel, Phys. Rev. 82, 332 (1951) (A)
		17038	O. Oldenberg, Phys. Rev. <u>53</u> , 35 (1938)
		18050	F. E. O'Meara, Phys. Rev. 79, 1032 (1950)
1046	R. K. Osborne and W. C. Peacock, Phys. Rev. <u>69</u> , 679 (1946) (A)	19052	J. Orring, Arkiv Fysik 4, 469 (1952); reported in M. Siegbahn Commemorative Volume, p 197 (Uppsala, 1951)
1047	R. K. Osborne and M. Deutsch, Phys. Rev. <u>71</u> , 467 (1947) (A)	20052	J. Owen and J. H. E. Griffiths, (to be published) (1952)
2039	F. Oppenheimer and E. P. Tomlinson, Phys. Rev. 56, 858 (1939) (A)		
3047	W. Ogle, L. Brown, and R. Conklin, Phys. Rev. 71, 378 (1947)		
3050	W. E. Ogle, L. J. Brown, and A. N. Carson, Phys. Rev. 78, 63 (1950)	1P37	M. L. Pool, J. M. Cork, and R. L. Thornton, Phys. Rev. <u>52</u> , 239 (1937)
4040	R. D. O'Neal and M. Goldhaber, Phys. Rev. <u>58</u> 574 (1940)	1P37a	M. L. Pool and J. M. Cork, Phys. Rev. <u>51</u> , 1010 (1937) (A)
4040a	R. D. O'Neal and M. Goldhaber, Phys. Rev. <u>57</u> , 1086 (1940) (A)	1P38	M. L. Pool, Phys. Rev. <u>53</u> , 116 (1938)
4041	R. D. O'Neal, Phys. Rev. 60, 359 (1941)	1P38a	M. L. Pool and L. L. Quill, Phys. Rev. <u>53</u> , 437 (1938)
5049	D. W. Osborne, R. C. Thompson, and Q. Van Winkle, NNES-PPR <u>14B</u> , 1397 (1949)	1P43	M. L. Pool and J. D. Kurbatov, Phys. Rev. <u>63</u> , 463 (1943) (A)
6047	P. R. O'Commor and G. T. Seaborg, unpublished data (1947)	1P45	M. L. Pool and J. E. Edwards, Phys. Rev. <u>67,</u> 60 (1945) (A)

IP48	M. L. Pool and N. L. Krisberg, Phys. Rev. <u>73</u> , 1035 (1948)	12P49	M. L. Perlman, Phys. Rev. 75, 988 (1949)
1P52	M. L. Pool and D. N. Kundu, private communication (Nov. 1952)	12P51	M. L. Perlman and G. Friedlander, Phys. Rev. 82, 449 (1951)
2P49	V. Perez-Mendes and H. Brown, Phys. Rev. 76,	12P52	M. L. Perlman and R. Schwarts, private communication (Oct. 1952)
2P50	689 (1949)  V. Perez-Mendez and H. Brown, Phys. Rev. 77.	13P47	I. Periman, R. H. Goeckermann, D. H. Templeton, and J. J. Howland, Jr., Phys. Rev. 72, 352 (1947)
2P50a	404 (1950)  V. Perez-Mendez and H. Brown, Phys. Rev. 78,	13P47a	I. Periman, J. J. Howland, Jr., and D. H. Templeton, unpublished data (1947)
2P50b	812 (1950)  V. Perez-Mendez and P. Lindenfeld, reported in	13P49	I. Perlman, P. R. O'Connor, and L. O. Morgan, NNES-PPR 14B, 1651 (1949)
21 700	Columbia University Unclassified Document CUD-56 (Aug. 1950)	13P50	I. Perlman, A. Ghiorso, and G. T. Seaborg, Phys. Rev. 77, 26 (1950)
2P50c	V. Perez-Mendes and P. Lindenfeld, Phys. Rev. 80, 1097 (1950)	14P40	E. Pollard and W. W. Watson, Phys. Rev. 58,
2P51	V. Perez-Mendez and P. Lindenfeld, Phys. Rev. 83. 864 (1951)	15P49	12 (1940)  D. D. Phillips, U. S. Atomic Energy Commission
3P46	K. Philipp and J. Riedhammer, Z. Naturforsch. 1, 372 (1946)	16P52	Unclassified Report AECU-404 (June 1949)  M. Paganelli and G. Quareni, Phys. Rev. 86,
3P48	K. Philipp and F. Rehbein, Z. Physik 124, 225 (1948)		423 (1952); Nuovo cimento <u>9,</u> 324 (1952)
4P35	P. Preiswerk and H. von Halban, Compt. rend. 201,	17P38	B. Pontecorvo, Phys. Rev. <u>54</u> , 542 (1938)
	722 (1935)	17P 38a	B. Pontecorvo and A. Lasard, Compt. rend. 208, 99 (1938)
4P51	P. Preiswerk and P. Stähelin, Helv. Phys. Acta 24, 300 (1951)	17P49	B. Pontecorvo, D. H. W. Kirkwood, and G. C. Hanna, Phys. Rev. 75, 982 (1949)
5P5I	C. A. Prohaska, Ph.D. Thesis, University of California Radiation Laboratory Unclassified Report UCRL-1395 (Aug. 1951)	18P50	R. W. Pringle, S. Standil, and K. I. Rouleton, Phys. Rev. 77, 841 (1950)
6P46	W. C. Peacock and M. Deutsch, Phys. Rev. <u>69</u> , 306 (1946)	18P50a	R. W. Pringle and S. Standil, Phys. Rev. <u>80</u> , 762 (1950)
6P46a	W. C. Peacock, R. D. Evans, J. W. Irvine, W. M. Good, A. F. Kip, S. Weiss, and J. G. Gibson, J. Clin. Invest. 25, 605 (1946)	18P51	R. W. Pringle, S. Standil, H. W. Taylor, and G. Fryer, Phys. Rev. 84, 1066 (1951)
6P47	W. C. Peacock, J. W. Jones, and R. T. Overman,	18P52	R. W. Pringle, H. W. Taylor, and S. Standil, Phys. Rev. 87, 384 (1952)
	reported in Oak Ridge National Laboratory Classified Report Mon N-432 (Dec. 1947)	19P51	F. T. Porter and C. S. Cook, Phys. Rev. 81, 640 (1951)
6P47a	W. C. Peacock, Phys. Rev. 72, 1049 (1947)	19P51a	F. T. Porter and C. S. Cook, Phys. Rev. 81,
6P47b	W. C. Peacock, A. R. Brosi, and A. D. Bogard, reported in Oak Ridge National Laboratory Classified Reports Mon N-432 (Dec. 1947); ORNL-65	19P52	298 (1951) (A) — — — — — — — — — — — — — — — — — — —
	(July 1948), ORNL-176 (Nov. 1948)		464 (1952)
6P48	W. C. Peacock and J. W. Jones, U. S. Atomic Energy Commission Declassified Document AECD-1812 (March 1948)	20P48	C. L. Peacock and R. G. Wilkinson, Phys. Rev. 74, 297 (1948)
7P39	M. Perey, Compt. rend. 208, 97 (1939); J. phys. et radium 10, 435 (1939)	20P49	C. L. Peacock and A. C. G. Mitchell, Phys. Rev. 75, 1272 (1949)
7P39a	M. Perey and M. Lecoin, J. phys. et radium 10, 439 (1939)	20P51	C. L. Peacock and J. L. Braud, Phys. Rev. <u>83</u> , 484 (1951) (A)
7P39b	M. Perey and M. Lecoin, Nature 144, 326 (1939)	21P42	E. H. Plesset, Phys. Rev. 62, 181 (1942)
7P41	M. Perey and M. Lecoin, Compt. rend. 212, 893 (1941)	22P37	C. Perrier and E. Segré, J. Chem. Phys. <u>5.</u> 713 (1937); <u>7</u> , 155 (1939)
7P46	M. Perey, J. chim. phys. <u>43</u> , 155, 269 (1946)	22P38	C. Perrier, M. Santangelo, and E. Segré, Phys. Rev. 53, 104 (1938)
8P49	S. Peterson, NNES-PPR 14B, 1393 (1949)	23P47	T. J. Parmley and B. J. Moyer Phys. Rev. 72, 82 (1947)
8P49a	S. Peterson and A. Chiorso, NNES-PPR 14B, 1395 (1949)	23P49	T. J. Parmley, B. J. Moyer, and R. C. Lilly.
8P49b	S. Peterson and A. Ghiorso, NNES-PPR 14B, 1424 (1949)	24P51	Phys. Rev. 75, 619 (1949)  E. Plassmann and F. R. Scott, Phys. Rev. 84,
9P37	A. Polessitsky, Physik Z. Sowjetunion 12, 339 (1937)	14041	156 (1951)
9P40	A. Polessitsky and N. Nemerovsky, Compt. rend. U. R.S.S. <u>28</u> , 217 (1940)	25P52	R. M. Pearce and E. K. Darby, Phys. Rev. <u>86</u> , 1049 (1952)
9P40a	A. Polessitsky and M. Orbeli, Compt. rend. U.R.S.S. 28, 215 (1940)	26P47	G. W. Parker, P. M. Lants, M. G. Inghram, D. C. Hess, Jr., and R. J. Hayden, Phys. Rev. 72, 85 (1947)
9P41	A. Polessitsky, N. Nemerovsky, M. Orbeli, and N. Baronckik, J. Phys. (U.S.S.R.) <u>IV.</u> 284 (1941)	26P49	G. W. Parker, G. E. Creek, G. M. Hebert, P. M. Lantz, and W. J. Martin, reported in Oak Ridge National Laboratory Classified Report
10P46	M. J. Poole and E. B. Paul, Nature 158, 482 (1946)		ORNL-499 (Dec. 1949)
11P46	A. K. Pierce and F. W. Brown, III, Phys. Rev. 70, 779 (1946)	26P49a	G. W. Parker, G. E. Creek, G. M. Hebert, and P. M. Lants, reported in Oak Ridge National Laboratory Classified Report ORNL-336 (May 1949)
12P48	M. L. Perlman and G. Friedlander, Phys. Rev. <u>74</u> , 442 (1948)		May 1949)

24749b	G. W. Parker, G. E. Creek, G. M. Hebert, P. M. Lants, and W. J. Martin, reported in Oak	5R47	S. Rowlands, Nature 160, 191 (1947)
	Ridge National Laboratory Classified Report ORNL- 286 (Sept. 1949)	6R35	J. Rotblat, Nature 136, 515 (1936)
26*51	G. W. Parker, reported in Oak Ridge National	6R41	J. Rotblat, Proc. Roy. Soc. (London) 177A, 260 (1941)
	Laboratory Classified Report ORNL-870 (March 1951)	6R4la	J. Rotblat, Nature 148, 371 (1941)
26P52	G. W. Parker and W. J. Martin, private communication (Oct. 1952)	7R36	F. Rasetti, "Elements of Nuclear Physics," Prentice-Hall, Inc., New York (1936)
27P51	J. P. Palmer and L. J. Laslett, U. S. Atomic Energy Commission Unclassified Report AECU-1220 (March 1951)	8R40	R. Ringo, Phys. Rev. 58, 942 (1940); 59, 107 (1941). Values recalculated according to (9H38)
27P51a	J. P. Palmer, Phys. Rev. 82, 772 (1951) (A)	9R48	G. Reed, Jr., W. M. Manning, and W. Bentley, reported in Argonne National Laboratory Classified Report ANL-4112 (March 1948)
28P50	R. I. Powers and A. F. Voigt, Phys. Rev. <u>79,</u> 175 (1950)	10R49	F. L. Reynolds, D. G. Karraker, and D. H. Templeton, Phys. Rev. 75, 313 (1949)
29P40	C. Pecher, Phys. Rev. <u>58</u> , 843 (1940)	10R50	F. L. Reynolds, E. K. Hulet, and K. Street, Jr.,
30P51	A. C. Pappas, Phys. Rev. 81, 299 (1951) (A)		Phys. Rev. 80, 467 (1950)
30P51a	A. C. Pappas and C. D. Coryell, Phys. Rev. 81, 329 (1951) (A)	11R47	W. Rall and R. G. Wilkinson, Phys. Rev. <u>71</u> , 321 (1947)
30P52	A. C. Pappas, Phys. Rev. 87, 162 (1952)	11R51	W. Rall and K. G. McNeill, Phys. Rev. 83, 1244 (1951)
30P52a	A. C. Pappas, private communication (Oct. 1952)	12R52	P. Radvanyi, Compt. rend. 234, 1275 (1952)
31P49	E. Picciotti, Compt. rend. 229, 117 (1949)	12R52a	P. Radvanyi, Compt. rend. 235, 289 (1952)
32P50	W. W. Pratt, Phys. Rev. 80, 289 (1950)	12R52b	P. Radvanyi, Compt. rend. 235, 428 (1952)
33P52	W. K. H. Panofsky and D. Reagan, Phys. Rev. <u>87,</u> 543 (1952)	13R37	L. H. Rumbaugh, R. B. Roberts, and L. R. Hafstad, Phys. Rev. 51, 1106 (1937)
34P52	I. Pullman and P. Axel, private communication (Oct. 1952)	13R38	L. H. Rumbaugh, R. B. Roberts, and L. R. Hafstad, Phys. Rev. 54, 657 (1938)
35P52	T. Passel, W. A. Jenkins, and W. W. T. Crane, reported in University of California Radiation Laboratory Classified Report UCRL-1770 (April 1952)	14R38	R. B. Roberts and N. P. Heydenburg, Phys. Rev. 53, 929 (1938) (A)
		14R38a	R. B. Roberts, N. P. Heydenburg, and G. L. Locher, Phys. Rev. 53, 1016 (1938)
		15R46	S. Rubin, Phys. Rev. 69, 134 (1946) (A)
		16R40	S. Ruben and M. D. Kamen, Phys. Rev. 57, 549
1R31	E. Rutherford, C. E. Wynn-Williams, and W. B. Lewis, Proc. Roy. Soc. (London) 133A, 351 (1931)	16R41	(1940)  S. Ruben and M. D. Kamen, Phys. Rev. 59, 349
2R50	J. M. Robson, Phys. Rev. <u>78</u> , 311 (1950)		(1941)
2R51	J. M. Robeon, Phys. Rev. 83, 349 (1951)	17R46	A. F. Reid, J. R. Dunning, S. Weinhouse, and A. V. Grosse, Phys. Rev. 70, 431 (1946)
3R50	M. Riou, J. phys. et radium 11, 185 (1950); Compt. rend. 228, 678 (1949)	17R46a	A. F. Reid and A. S. Keston, Phys. Rev. <u>70,</u> 987 (1946)
3R52	M. Riou, J. phys. et radium 13, 244 (1952)	18R37	L. N. Ridenour and W. J. Henderson, Phys. Rev.
3R52a	M. Riou, Compt. rend. <u>234</u> , 1157 (1952)		<u>52</u> , 889 (1937)
3R53 4R36	M. Riou, Ann. phys. (to be published) (1953)  S. Rosenblum, M. Guillot, and M. Perey, Compt.	18R 37a	L. N. Ridemour and W. J. Henderson, Phys. Rev. 51, 1102 (1937)
4R37	rend. 202, 1274 (1936)  S. Rosenblum, M. Guillot, and M. Perey, Compt.	19R51	L. Ruby and J. R. Richardson, Phys. Rev. <u>83</u> , 698 (1951)
4R48	rend. 204, 175 (1937)  S. Rosenblum, M. Valadares, and J. Vial, Compt.	20R49	J. E. Robinson, M. Ter-Pogossian, and C. S. Cook, Phys. Rev. 75, 1099 (1949)
7840	rend. 227, 1088 (1948)	21R43	W. Riesler, Naturwiss. 31, 326 (1943)
4R49	S. Rosenblum, M. Valadares, M. Perey, and J. Vial, Compt. rend. 229, 1009 (1949)	21R44	W. Riesler, Physik Z. 45, 191 (1944)
4R49a	S. Rosenblum, M. Guillot, and G. Bastin-Scoffier,	21R46	W. Riesler, Naturwies. 33, 53 (1946)
4R49b	Compt. rand. 229, 191 (1949)  S. Rosenblum, M. Valadarce, and M. Perey,	22R49	S. A. Reynolds, reported in Oak Ridge National Laboratory Classified Report ORNL-286 (Sept. 1949)
4R49c	Compt. rend. 228, 385 (1949)  S. Rosenblum, E. Cotton, and G. Bouissières,	22R50	S. A. Reynolds, reported in Oak Ridge National Laboratory Classified Report ORNL-867 (Dec. 1950)
4R50	Compt. rend. 229, 825 (1949)  S. Rosenblum, M. Valadares, and B. Goldechmidt,	23R36	J. R. Richardson and F. N. D. Kurie, Phys. Rev. 50, 999 (1936)
	Compt. rend. 230, 638 (1950)	23R39	J. R. Richardson, Phys. Rev. <u>55</u> , 609 (1939)
4R51	S. Rosenblum and M. Valadares, Compt. rend. 232, 501 (1951)	23R46	J. R. Richardson and B. T. Wright, Phys. Rev. 70, 445 (1946) (A)
4R52	S. Rosenblum, M. Valadares, and M. Guillot, Compt. rend. <u>234</u> , 1767 (1952)	24R47	M. M. Ramsey, J. L. Meem, Jr., and A. C. G. Mitchell, Phys. Rev. <u>72</u> , 639 (1947)
4R52a	S. Rosenblum, M. Valadares, and M. Guillot, Compt. rend. <u>235</u> , 238 (1952)	25R48	G. A. Renard, Compt. rend. 226, 1269 (1948)
4R52b	S. Rosenblum, M. Perey, M. Valadares, and M.	25R49	G. A. Renard, Compt. rend. 228, 387 (1949)
	Gaillot, private communication (Oct. 1952)	25R50	G. A. Renard, Ann. phys. <u>5</u> , 385 (1950)

26R50	T. R. Roberts and A. O. Nier, Phys. Rev. 79, 198 (1950) (A)	47R52	H. N. Ritland and F. H. Schmidt, private communication (Oct. 1952)
27R37	J. R. Risser, Phys. Rev. 52, 768 (1937)	48R51	A. Rytz, Compt. rend. 233, 790 (1951)
27R40	J. R. Risser, K. Lark-Horowits, and R. N. Smith, Phys. Rev. <u>57</u> , 355 (1940) (A)	49R52	W. Rubinson and W. Bernstein, Phys. Rev. 86, 545 (1952)
27R48	J. R. Risser and R. N. Smith, private communication from K. Lark-Horowitz (1948)	50R52	K. I. Roulston and R. W. Pringle, Phys. Rev. <u>87</u> , 930 (1952)
28R50	J. H. Reynolds, Phys. Rev. 79, 789 (1950)	51R50	H. T. Richards, R. V. Smith, and C. P. Browne,
28R 50a	J. H. Reynolds, Phys. Rev. 79, 886 (1950)	51R51	Phys. Rev. <u>80</u> , 524 (1950)  H. T. Richards, Phys. Rev. 83, 694 (1951)
28R50b	J. H. Reynolds, reported in Argonne National Laboratory Classified Report ANL-4515 (Oct. 1950)	52R52	H. Rose, Phil. Mag. 43, 1146 (1952)
29R50	E. Rabinowicz, Proc. Phys. Soc. (London) <u>63A</u> , 1040 (1950)		
30R51	H. Roderick, W. E. Meyerhof, and L. G. Mann, Phys. Rev. <u>84</u> , 887 (1951)		
30R52	H. Roderick, O. Lonsjo, and W. E. Meyerhof, private communication (Oct. 1952)	1537	J. Schintlmeister, Sitzber. Akad. Wiss. Wien. Abt. IIa, <u>146</u> , 371 (1937)
31R52	W. C. Rutledge, J. M. Cork, and S. B. Burson, Phys. Rev. <u>86</u> , 775 (1952)	1539	J. Schintlmeister and K. Lintner, Sitsber, Akad. Wiss, Wien, Abt. IIa, <u>148</u> , 279 (1939)
32R50	P. Rothwell and D. West, Proc. Phys. Soc. (London) 63A, 539 (1950)	2546	L. Seren, W. E. Moyer, and W. Sturm, Phys. Rev. 70, 561 (1946)
33R4I	A. Roberts, J. R. Downing, and M. Deutsch, Phys. Rev. <u>60</u> , 544 (1941)	2547	L. Seren, H. N. Friedlander, and S. H. Turkel, Phys. Rev. <u>72</u> , 888 (1947)
33R4la	A. Roberts and J. W. Irvine, Jr., Phys. Rev. <u>59</u> , 936 (1941)	2547a	L. Seren, H. N. Friedlander, and S. H. Turkel, Phys. Rev. <u>71</u> , 454 (1947)
33R43	A. Roberts, L. G. Elliott, J. R. Downing, W. C. Peacock, and M. Deutsch, Phys. Rev. 64, 268 (1943)	2547ъ	L. Seren, D. Engelkemeir, W. Sturm, H. N. Friedlander, and S. Turkel, Phys. Rev. <u>71</u> , 409 (1947)
34R47	W. C. Redman and D. Saxon, Phys. Rev. <u>72,</u> 570 (1947)	3533	B. W. Sargent, Proc. Roy. Soc. (London) 139A, 659 (1933). Summarizes the results of various investigators.
35R38	H. Reddemann and F. Strassmann, Naturwiss. 26, 187 (1938)	3539	B. W. Sargent, Can. J. Research 17A, 103 (1939)
35R40	H. Reddemann, Naturwiss. 28, 110 (1940)	3539a	B. W. Sargent, Can. J. Research 17A, 82 (1939);
35R40a	H. Reddemann, Z. Physik 116, 137 (1940)		Phys. Rev. <u>54</u> , 232 (1938)
36R49	B. E. Robertson, W. E. Scott, and M. L. Pool, Phys. Rev. 76, 1649 (1949)	3552	B. W. Sargent, L. Yaffe, and A. P. Gray, Can. J. Phys. (in press) (1952)
36R50	B. E. Robertson, W. E. Scott, and M. L. Pool, Phys. Rev. 78, 318 (1950) (A)	4546	M. H. Studier, Argonne National Laboratory Classified Report CP-3642 (Dec. 1946); NNES-PPR 17B, 634 (1952) (classified)
36R 50a	B. E. Robertson, W. L. Carss, and M. L. Pool, Phys. Rev. 77, 747 (1950) (A)	4548	M. H. Studier and E. K. Hyde, Phys. Rev. 74, 591 (1948)
37R46	Wilfrid Rall, Phys. Rev. 70, 112 (1946) (A)	4548a	M. H. Studier and R. J. Bruehlman, private
38R50	B. Russell and A. Wattenberg, U. S. Atomic Energy Commission Declassified Document AECD-2926 (Dec. 1950)	4549	communication (Oct. 1948)  M. H. Studier and R. J. Bruehlman, reported in Argonne National Laboratory Classified Report
39R51	B. L. Robinson and L. Madansky, Phys. Rev. 84, 604 (1951)	4549a	ANL-4252 (Feb. 1949)  M. H. Studier and E. K. Hyde, unpublished data
39R5la	B. L. Robinson and L. Madansky, Phys. Rev. 84,		(Feb. 1949)
	1067 (1951)	4552	M. H. Studier, NNES-PPR 17B, 50 (1952) (classified)
40R52	D. Rose, G. Hinman, and L. G. Lang, Phys. Rev. 86, 863 (1952)	5545	H. Slätis, Arkiv Mat., Astron. Fysik 32A, No. 16 (1945)
41R50	E. R. Rae, Proc. Phys. Soc. (London) 63A, 292 (1950)	5546	H. Slätis, Arkiv Mat., Astron. Fysik 33A, No. 17 (1946)
42R50	J. O. Rasmussen, F. L. Reymolds, S. G. Thompson, and A. Ghiorso, Phys. Rev. 80, 475 (1950)	5547	H. Slätis, Nature 160, 579 (1947); Arkiv Mat., Astron. Fysik 35A, No. 3 (1948)
42R52	J. O. Rasmussen, Jr., S. G. Thompson, and A. Ghiorso, Phys. Rev. (to be published) (1952)	5549	H. Slätis and K. Siegbahn, Arkiv Mat., Astron. Fysik 36A, No. 21 (1949)
43R52	P. L. Roggenkamp, C. H. Pruett, and R. G. Wilkinson, Phys. Rev. (in press) (1952)	5549a	H. Slätis and K. Siegbahn, Phys. Rev. 75, 318 (1949)
43R53	P. L. Roggenkamp, C. H. Pruett, and R. G. Wilkinson, Phys. Rev. (to be published) (1953)	5850	H. Slätis, S. J. du Toit, and K. Siegbahn, Phys. Rev. 78, 498 (1950); Arkiv Fysik 2, 321 (1950)
44R52	R. Richmond and H. Rose, Phil. Mag. 43, 367 (1952)	5551	H. Slätis and K. Siegbahn, reported in M. Siegbahn Commemorative Volume, p 153 (Uppsala, 1951)
44R52a	R. Richmond, P. J. Grant, and H. Rose, Proc.	5652	H. Slätis and L. Zappa, Arkiv Fysik 5, 26 (1952)
45R52	Phys. Soc. (London) 65A, 484 (1952)  G. Rudstam, P. C. Stevenson, and R. L. Folger,	6548	K. Street, Jr., R. A. James, and G. T. Seaborg, unpublished data (July 1948)
46.043	Phys. Rev. 87, 358 (1952)	6548a	K. Street, Jr., A. Ghiorso, D. A. Orth, and
46R52	G. W. Rodeback and J. S. Allen, Phys. Rev. 86, 446 (1952)		G. T. Seaborg, unpublished data (Oct. 1948)



6550	K. Street, Jr., unpublished data quoted in Phys. Rev. 78, 475 (1950)	9549c	D. Saxon, reported in Argonne National Laboratory Classified Report ANL-4237 (Jan. 1949)
6550a	K. Street, Jr., A. Chiorso, and G. T. Seaborg, Phys. Rev. <u>79</u> , 530 (1950)	10551	P. H. Stoker, O. P. Hok, and G. J. Sizoo, Physica 17, 164 (1951)
7544	K. Siegbahn, Arkiv Mat., Astron. Fysik 30A, No. 20 (1944)	11537	J. Surugue, Ann. phys. <u>8</u> , 484 (1937)
7544a	K. Siegbahn and E. Bohr, Arkiv Mat., Astron. Fysik	11538	J. Surugue, J. phys. et radium <u>9</u> , 438 (1938)
	30B, No. 3 (1944)	11541	J. Surugue, Compt. rend. 212, 337 (1941)
7S45	K. Siegbahn and H. Slätis, Arkiv Mat., Astron. Fysik <u>32A</u> , No. 9 (1945)	115 <b>4</b> 1a	J. Surugue and San-Tsiang Tsien, Compt. rend. 213, 172 (1941)
7546	K. Siegbahn and N. Hole, Phys. Rev. 70, 133 (1946)	11542	J. Surugue, J. phys. et radium 4, 71 (1942)
7546a	K. Siegbahn and S. E. Petersson, Arkiv Mat., Astron. Fysik 32B, No. 5 (1946)	11546	J. Surugue, J. phys. et radium 7, 145 (1946)
7S46b	K. Siegbahn, Phys. Rev. 70, 127 (1946)	12546	A. K. Saha, Proc. Nat. Inst. Sci. India 12, No. 3, 159 (1946)
7546c	K. Siegbahn, Arkiv Mat., Astron. Fysik 33A, No. 10 (1946)	13539	G. T. Seaborg and E. Segrè, Phys. Rev. <u>55</u> , 808 (1939)
7 <b>S47</b>	K. Siegbahn and A. Johansson, Arkiv Mat., Astron. Fysik 34A, No. 10 (1947)	13540	G. T. Scaborg, J. J. Livingood, and J. W. Kennedy, Phys. Rev. <u>57</u> , 363 (1940)
7547a	K. Siegbahn and H. Slatis, Nature 159, 471 (1947); Arkiv Mat., Astron. Fysik <u>34A</u> , No. 15 (1947)	13541	G. T. Seaborg, J. W. Gofman, and J. W. Kennedy, Phys. Rev. <u>59</u> , 321 (1941)
7547Ь	K. Siegbahn, Arkiv Mat., Astron. Fysik 34E, No. 6 (1947)	1354 la	G. T. Seaborg, J. J. Livingood, and G. Friedlander, Phys. Rev. 59, 320 (1941)
7547c	K. Siegbahn, Arkiv Mat., Astron. Fysik 34B, No. 4 (1947)	135416	G. T. Seaborg and G. Friedlander, Phys. Rev. <u>59</u> , 400 (1941)
7 <b>54</b> 7d	K. Siegbahn, Arkiv Mat., Astron. Fysik 34A, No. 7 (1947)	13546	G. T. Seaborg, E. M. McMillan, J. W. Kennedy, and A. C. Wahl, Phys. Rev. <u>69</u> , 366 (1946); NNES-PPR 14B, I (1949)
75 <b>4</b> 7e	K. Siegbahn and M. Deutsch, Phys. Rev. 71, 483 (1947) (A)	13546a	G. T. Seaborg, A. C. Wahl, and J. W. Kennedy, Phys. Rev. 69, 367 (1946); NNES-PPR 14B, 3 (1949)
7547f	K. Siegbahn and H. Slätis, Arkiv Mat., Astron. Fysik 34A, No. 6 (1947)	13547	G. T. Seaborg, B. B. Cunningham, H. H. Hopkins, Jr., M. Lindner, D. R. Miller, P. R. O'Connor,
7547g	K. Siegbahn, Proc. Roy. Soc. (London) 189A, 527 (1947)	12547-	I. Perlman, and R. C. Thompson, Phys. Rev. 72, 740 (1947) (A)
7548	K. Siegbahn and M. Deutsch, Phys. Rev. 73, 410 (1948); A. Hedgran, K. Siegbahn, and N. Svartholm, Proc. Phys. Soc. (London) <u>63A</u> , 960 (1950)	13547a	G. T. Seaborg, J. W. Gofman, and R. W. Stoughton, Phys. Rev. 71, 378 (1947)
7549	K. Siegbahn and A. Ghosh, Phys. Rev. 76, 307 (1949); Arkiv Mat., Astron. Fysik 36A, No. 19 (1949)	13347	G. T. Seaborg, R. A. James, and L. O. Morgan, NNES-PPR 14B, 1525 (1949)
7549a	K. Siegbahn, A. Hedgran, and M. Deutsch, Phys. Rev. 76, 1263 (1949)	135 <b>49a</b>	G. T. Seaborg, A. C. Wahl, and J. W. Kennedy, NNES-PPR 14B, 13 (1949)
7549Ъ	K. Siegbahn, E. Kondaiah, and S. Johansson, Nature 164, 405 (1949)	13549Ь	G. T. Seaborg, R. A. James and A. Ghioreo, NNES-PPR 14B, 1554 (1949)
7549c	K. Siegbahn, Phys. Rev. 75, 1277 (1949); 77, 233 (1950)	13552	G. T. Seaborg, J. W. Gofman, and R. W. Stoughton, NNES-PPR 17B, 31 (1952) (classified)
7549d	K. Siegbahn and W. Forsling, Arkiv Fysik 1, 505	13S52a	G. T. Seaborg, Phys. Rev. <u>85</u> , 157 (1952)
	(1949)	13853	G. T. Seaborg, R. A. Glass, and S. G. Thompson, J. Am. Chem. Soc. (to be published) (1953)
7549 <b>e</b>	K. Siegbahn and A. Hedgran, Phys. Rev. <u>75</u> , 523 (1949)	14550	A. W. Sunyar, D. Alburger, G. Friedlander, M. Goldhaber, and G. Scharff-Goldhaber, Phys.
7550	K. Siegbahn and M. Deutsch, Arkiv Fysik 2, 9 (1950); Phys. Rev. 77, 680 (1950)	14S50a	Rev. 79, 181 (1950)
7550a	K. Sinabahn and H. Slätis, Arkiv Fysik I, 559 (1950)		A. W. Sunyar, D. Alburger, G. Friedlander, M. Goldhaber, and G. Scharff-Goldhaber, Phys. Rev. 78, 326 (1950) (A)
7550Ъ	K. Siegbahn and S. der Toit, Arkiv Fysik 2, 211 (1950)	14550ъ	A. W. Sunyar, G. Friedlander, and M. Goldhaber,
7551	K. Siegbahn, reported in M. Sier' ha Commen orative Volume, p 199 (Uppsala, 1951)	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	reported in Brookhaven National Laboratory Unclassified Report BNL-39 (Jan. 1950)
7552	K. Siegbahn, Arkiv Fysik 4, 223 (1952)	14851	A. W. Sunyar, Phys. Rev. 83, 864 (1951)
8531	E. Stahel, Z. Physik <u>68</u> , 1 (1931); Helv. Phys. Act. <u>8</u> , 651 (1935)	14551a	A. W. Sunyar and J. W. Mihelich, Phys. Rev. <u>81</u> , 300 (1951) (A)
8543	E. Stahel and W. Johner, J. phys. et radium 5. 97 (1943)	14552	A. W. Sunyar, J. W. Mihelich, G. Scharff-Goldhaber, M. Goldhaber, N. S. Wall, and M. Deutsch, Phys. Rev. 86, 1023 (1952)
9548	D. Saxon, Phys. Rev. 73, 811 (1948)	14552a	A. W. Sunyar, private communication (Oct. 1952)
9548a	D. Saxon, Phys. Rev. 74, 1264 (1948) (A)	14552Ъ	A. W. Sunyar, D. E. Alburger, G. Friedlander,
9548b	D. Saxon, Phys. Rev. 74, 849 (1948)		M. Goldhaber, and G. Scharff-Goldhaber, unpublished data quoted in (18G52)
9549	D. Saxon and J. Richards, Phys. Rev. <u>76</u> , 982 (1949)	15837	W. R. Smythe and A. Hemmendinger, Phys. Rev. 51, 178 (1937)
9549a	D. Saxon and J. Richards, Phys. Rev. <u>76</u> , 186 (1949) (A)	16551	W. J. Sturm and V. Johnson, Phys. Rev. 83, 542
9549Ь	D. Saxon and R. Heller, Phys. Rev. 75, 909 (1949)		(1951)

17541 17546	G. Scharff-Goldhaber, Phys. Rev. <u>59</u> , 937 (1941) (A) G. Scharff-Goldhaber and G. S. Klaiber, Phys. Rev.	24552	E. Segrè, Phys. Rev. <u>86</u> , 21 (1952); some values recalculated according to more recent half-life determinations (HPS)
	<u>70,</u> 229 (1946)	25851	J. C. Sullivan, G. L. Pyle, M. H. Studier,
17550	G. Scharff-Goldhaber, E. der Mateosian, M. McKeown, and A. W. Sunyar, Phys. Rev. <u>78</u> , 325 (1950) (A)	23371	P. R. Fields, and W. M. Manning, Phys. Rev. 83, 1267 (1951)
17551	G. Scharff-Goldhaber and M. McKeown, Phys. Rev.	26536	A. H. Snell, Phys. Rev. 49, 555 (1936)
	82, 123 (1951)	26537	A. H. Snell, Phys. Rev. 51, 143 (1937) (A)
17S51a	G. Scharff-Goldhaber, reported in Brookhaven National Laboratory Unclassified Report BNL-103	26537a	A. H. Snell, Phys. Rev. 52, 1007 (1937)
	(June 1951)	26542	A. H. Snell et al., reported in Metallurgical
17S51 <b>b</b>	G. Scharff-Goldhaber, E. der Mateosian, M. Goldhaber, G. W. Johnson, and M. McKeown, Phys. Rev. 83, 480 (1951)	26543	A. H. Snell, M. B. Sampson, and J. S. Levinger, Metallurgical Laboratory Classified Report CP-1176
17552	G. Scharff-Goldhaber, E. der Mateosian, and J. W.	34.043	(Dec. 1943)
	Mihelich, Phys. Rev. 85, 734 (1952) (A)	26547	A. H. Snell, J. S. Levinger, E. P. Meiners, Jr., M. B. Sampson, and R. G. Wilkinson, Phys. Rev.
17S52a	G. Scharff-Goldhaber, private communication (Oct. 1952)		72, 545 (1947); NNES-PPR 9, 603 (1951)
18537	G. J. Sixoo and S. A. Wytxes, Physica 4, 791 (1937)	26S47a	A. H. Snell, V. A. Nedsel, H. W. Ibser, J. S. Levinger, R. G. Wilkinson, and M. B. Sampson,
18\$43	G. J. Sizoo and L. F. C. Friele, Physica 10, 57		Phys. Rev. 72, 541 (1947)
	(1943)	26550	A. H. Snell, F. Pleasonton, and R. V. McCord, Phys. Rev. 78, 310 (1950)
19551	G. J. Sayag, Compt. rend. 232, 2091 (1951)	27546	H. S. Sommers, Jr. and R. Sherr, Phys. Rev. 69,
20552	B. F. Scott, NNES-PPR 17B, 638 (1952) (classified)		21 (1946)
21551	L. M. Slater and G. T. Seaborg, unpublished data (Aug. 1951)	28540	R. Sherr, Phys. Rev. <u>57</u> , 937 (1940)
21552	L. M. Slater and F. Asaro, private communication	28541	R. Sherr, K. T. Bainbridge, and H. H. Anderson, Phys. Rev. <u>60</u> , 473 (1941)
	(Aug. 1952)	28548	R. Sherr, H. R. Muether, and M. G. White,
22542	K. Starke, Naturwiss. 30, 107, 577 (1942)		Phys. Rev. 74, 1239 (1948) (A)
23545a	W. H Sullivan, Phys. Rev. 68, 277 (1945)	28549	R. Sherr, H. R. Muether, and M. G. White, Phys. Rev. 75, 282 (1949)
23546	W. H Sullivan, N. R. Sleight, and E. M. Gladrow, Phys. Rev. 70, 778 (1946)	28552	R. Sherr and J. Gerhart, Phys. Rev. <u>86</u> , 619 (1952) (A)
23547	W. H Sullivan, J. A. Swartout, and H. E. Wyatt, reported in Oak Ridge National Laboratory Classified	29541	A. K. Solomon, Phys. Rev. 60, 279 (1941)
	Report Mon N-243 (Feb. 1947)	29547	A. K. Solomon, R. G. Gould, and C. B. Anfinsen,
23551	W. H Sullivan, N. R. Sleight, and E. M. Gladrow, NNES-PPR 9, 832 (1951)		Phys. Rev. 72, 1097 (1947)
23S51a	W. H Sullivan, N. R. Sleight, and E. M. Gladrow,	29548	A. K. Solomon and L. E. Glendenin, Phys. Rev. 73, 415 (1948)
220611	NNES-PPR 9, 820 (1951)	29550	A. K. Solomon, Phys. Rev. 79, 403 (1950)
23S51b	W. H Sullivan, N. R. Sleight, and E. M. Gladrow, NNES-PPR 9, 842 (1951)	30541	J. H. C. Smith and D. B. Cowie, J. Appl. Phys.
23S51c	W. H Sullivan, N. R. Sleight, and E. M. Gladrow,	31050	12, 78 (1941)
226614	NNES-PPR 9, 817 (1951)	31550	K. H. Sun, F. A. Pecjak, R. A. Charpie, and J. F. Nichaj, Phys. Rev. <u>78</u> , 338 (1950) (A)
23551d	W. H Sullivan, N. R. Sleight, and E. M. Gladrow, NNES-PPR 9, 808 (1951)	31S51	K. H. Sun, B. Jennings, W. E. Shoupp, and A. J. Allen, Phys. Rev. 82, 267 (1951)
23S51e	W. H Sullivan, N. R. Sleight, and E. M. Gladrow, NNES-PPR 9, 1953 (1951)	32551	W. E. Stephens, J. Halpern, and R. Sher, Phys. Rev. 82, 511 (1951)
23551f	W. H Sullivan, N. R. Sleight, and E. M. Gladrow, NNES-PPR 9, 838 (1951)	33550	S. C. Snowdon, Phys. Rev. 78, 299 (1950)
23S51g	W. H Sullivan, N. R. Sleight, and E. M. Gladrow,	34552	G. Schrank and J. R. Richardson, Phys. Rev. 86,
230318	NNES-PPR 9, 1949 (1951)	34032	248 (1952)
23851h	W. H Sullivan, N. R. Sleight, and E. M. Gladrow, NNES-PPR 9, 1945 (1951)	35547	W. Spats, N. Goldstein, C. Huddleston, and E. Goldfarb, reported in Argonne National Laboratory
235511	W. H Sullivan, N. R. Sleight, and E. M. Gladrow, NNES-PPR 9, 824 (1951)	36539	Classified Report CP-3750 (Feb. 1947)  N. K. Saha, Trans. Bose Res. Inst. (Calcutta) 14,
23S51j	W. H Sullivan, O. Johnson, and R. Nottorf, NNES-	26.00	57 (1939-1941); Chem. Abstracts 42, 450i (1948)
23S51k	PPR 9, 984 (1951)  W. H Sullivan and S. Katcoff, NNES-PPR 9, 1015	36851	N. K. Saha and K. Gopalakrishnan, Proc. Nat. Inst. Sci.India 17, 301 (1951)
24620	(1951)	37536	M. B. Sampson, L. N. Ridenour, and W. Bleakney, Phys. Rev. <u>50</u> , 382 (1936)
24839	E. Segrè, R. S. Halford, and G. T. Seaborg, Phys. Rev. <u>55</u> , 321 (1939)	37536a	M. B. Sampson and W. Bleakney, Phys. Rev. 50, 732 (1936)
24540	E. Segrè and C. S. Wu, Phys. Rev. <u>57</u> , 552 (1940)	38551	W. K. Sinclair and A. F. Holloway, Nature 167,
24540a	E. Segré, J. W. Kennedy, and G. T. Seaborg, unpublished work (1940)	39851	365 (1951)
24841	E. Segrè and G. T. Seaborg, Phys. Rev. 59, 212		J. H. Sreb, Phys. Rev. 81, 469 (1951)
34646	(1941)	39551a	J. H. Sreb, Phys. Rev. <u>81</u> , 643 (1951)
24549	E. Segrè and C. Wiegand, Phys. Rev. 75, 39 (1949)	40548	A. Ssalay and E. Csongor, Phys. Rev. 74, 1063 (1948)
24549a	E. Segrè, unpublished data quoted in E. Segrè and A. C. Helmhols, Revs. Modern Phys. <u>21</u> , 271 (1949)	41549	L. Seidlits, E. Bleuler, and D. J. Tendam, Phys. Rev. 76, 861 (1949)

42536	R. Sagane, Phys. Rev. 50, 1141 (1936)	60551	J. M. Siegel and L. E. Glendenin, NNES-PPR 9, 549 (1951)
42538	R. Sagane, S. Kojima, G. Miyamoto, and M. Ikawa, Phys. Rev. <u>54</u> , 542 (1938)	61546	E. P. Steinberg and D. W. Engelkemeir, reported in J. Am. Chem. Soc. 68, 2411 (1946)
42538a	R. Sagane, S. Kojima, G. Miyamoto, and M. Dawa, Phys. Rev. <u>54</u> , 970 (1938)	61548	E. P. Steinberg, J. A. Seiler, A. Goldstein, and
42539	R. Sagane, Phys. Rev. 55, 31 (1939)		A. Dudley, U. S. Atomic Energy Commission Declassified Document MDDC-1632 (Jan. 1948)
42539a	R. Sagane, S. Kojima, and G. Miyamoto, Proc. PhysMath. Soc. Japan <u>21</u> , 728 (1939)	61550	E. P. Steinberg and L. E. Glendenin, Phys. Rev. 78, 624 (1950)
42S39b	R. Sagane, S. Kojima, G. Miyamoto, and M. Dawa, Proc. PhysMath. Soc. Japan <u>21</u> , 660 (1939)	61551	E. P. Steinberg and D. W. Engelkemeir, NNES- PPR 9, 566 (1951)
42540	R. Sagane, S. Kojima, G. Miyamoto, and M. Ikawa, Phys. Rev. <u>57</u> , 1179 (1940)	61S51a	E. P. Steinberg and M. S. Freedman, NNES-PPR 9, 1378 (1951)
42540a	R. Sagane, S. Kojima, G. Miyamoto, and M. Ikawa, Proc. PhysMath. Soc. Japan 22, 174 (1940)	61S51b	E. P. Steinberg, NNES-PPR 9, 750 (1951)
42S40b	R. Sagane, S. Kojima, G. Miyamoto, and M. Ikawa, Phys. Rev. 57, 750 (1940)	61\$51c	E. P. Steinberg and L. E. Glendenin, NNES-PPR 9, 877 (1951)
42541	R. Sagane, G. Miyamoto, and M. Ikawa, Phys. Rev.	62551	F. R. Scott, Phys. Rev. 84, 659 (1951)
42552	59, 904 (1941)  R. Sagane, Phys. Rev. 85, 926 (1952)	63546	N. Sugarman and N. E. Ballou, reported in J. Am. Chem. Soc. 68, 2411 (1946)
44551	R. K. Sheline, R. B. Holtzman, and C. Y. Fan,	63547	N. Sugarman, private communication (April 1947)
	Phys. Rev. 83, 919 (1951)	63547a	N. Sugarman, J. Chem. Phys. 15, 544 (1947)
44S51a	R. K. Sheline, Phys. Rev. 82, 954 (1951)	63548	N. Sugarman and H. Richter, Phys. Rev. 73, 1411 (1948)
44852	R. K. Sheline and R. W. Stoughton, Phys. Rev. 87, 1 (1952)	63549	N. Sugarman, J. Chem. Phys. <u>17</u> , 11 (1949)
44S52a	R. K. Sheline, Phys. Rev. 87, 557 (1952)	63S49a	N. Sugarman, Phys. Rev. 75, 1473 (1949)
45548	A. D. Schelberg, M. B. Sampson, and A. C. G. Mitchell, Rev. Sci. Instr. 19, 458 (1948)	63550	N. Sugarman and H. Richter, J. Chem. Phys. 18, 174 (1950)
46549	G. A. Sawyer and M. L. Wiedenbeck, Phys. Rev. 76, 1535 (1949)	63551	N. Sugarman, N. E. Ballou, D. W. Engelkemeir, and W. H. Burgus, NNES-PPR 9, 1163 (1951)
46550	G. A. Sawyer and M. L. Wiedenbeck, Phys. Rev. 79, 490 (1950)	63552	N. Sugarman, Phys. Rev. 86, 604 (1952) (A)
47549	R. W. Stout, Phys. Rev. 75, 1107 (1949)	64541	R. E. Siday, Proc. Roy. Soc. (London) <u>178A</u> , 189 (1941)
48550	F. W. Spiers, Nature 165, 356 (1950)	65538	F. Strassmann and E. Walling, Ber. deut. chem. Ges. 71B, 1 (1938)
49551	V. L. Sailor and J. J. Floyd, Phys. Rev. <u>82</u> , 960 (1951)	65540	F. Strassmann and O. Hahn, Naturwiss. 28, 817 (1940)
50550	L. Simons, Soc. Scien. Fennica Comm. PhysMath. 15, No. 9 (1950)	66540	W. Seelmann-Eggebert, Naturwiss. 28, 451 (1940)
50852	L. Simone, Phys. Rev. 86, 570 (1952)	66543	W. Seelmann-Eggebert and H. J. Born, Naturwiss. 31, 59 (1943)
51542	G. P. Smith, Phys. Rev. 61, 578 (1942)	66S43a	W. Seelmann-Eggebert, Naturwiss. 31, 510 (1943)
52550	B. N. Sorensen, B. M. Dale, and J. D. Kurbatov, Phys. Rev. 79, 1007 (1950)	66S43b	W. Seelmann-Eggebert, Naturwiss. 31, 491 (1943)
53845	R. P. Schuman, reported in Metallurgical Laboratory Classified Report CN-2929 (May 1945)	66546	W. Seelmann-Eggebert, Naturwiss. 33, 279 (1946)
53 <b>545a</b>	R. P. Schuman, reported in Metallurgical Laboratory Classified Report CN-2799 (April 1945)	66547	W. Seelmann-Eggebert and F. Strassmann, Z. Naturforsch. <u>Za</u> , 80 (1947)
53546	R. P. Schuman, reported in J. Am. Chem. Soc. 68, 2411 (1946)	67551	A. F. Stehney and N. Sugarman, U. S. Atomic Energy Commission Declassified Document AECD-3047 (Jan. 1951); Phys. Rev. (in press) (1952)
53851	R. P. Schuman and A. Camilli, Phys. Rev. 84,	68548	F. B. Shull, Phys. Rev. 74, 917 (1948)
53S5la	158 (1951)  R. P. Schuman, NNES-PPR 9, 783 (1951)	69538	H. Scheichenberger, Anz. Akad. Wiss. Wien, Mathnaturw. Klasse <u>75</u> , 108 (1938)
54546	J. A. Swartout, G. E. Boyd, A. E. Cameron, C. P. Keim, and C. E. Larson, Phys. Rev. 70,	70551	B. Selikson and J. M. Siegel, NNES-PPR 9. 699 (1951)
54547	232 (1946)  J. A. Swartout, reported in Oak Ridge National Laboratory Classified Report Mon N-243 (Feb. 1947)	71537	D. W. Stewart, J. L. Lawson, and J. M. Cork, Phys. Rev. <u>52</u> , 901 (1937)
55850	K. Strauch, Phys. Rev. 79, 487 (1950)	71539	D. W. Stewart, Phys. Rev. 56, 629 (1939)
55851	K. Strauch, Phys. Rev. 81, 973 (1951)	72549	L. Slack, C. H. Braden, and F. B. Shull, Phys. Rev. <u>75</u> , 1965 (1949)
56851	L. A. Smith, R. N. H. Haslam, and J. G. V. Taylor, Phys. Rev. 84, 842 (1951)	72 <b>54</b> 9a	L. Slack, G. E. Owen, and H. Primakoff, Phys. Rev. 75, 1448 (1949)
57549	L. M. Silver, Phys. Rev. 76, 589 (1949) (A); Can. J. Physice <u>29</u> , 59 (1951)	73851	F. J. Shore, W. L. Bendel, and R. A. Becker, Phys. Rev. <u>83</u> , 688 (1951)
58538	C. V. Strain, Phys. Rev. 54, 1021 (1938)	73852	F. J. Shore, H. N. Brown, W. L. Bendel, and R. A. Becker, Phys. Rev. 87, 202 (1952) (A)
59548	L. S. Skagge, J. S. Laughlin, A. O. Hanson, and J. J. Orlin, Phys. Rev. 73, 420 (1948)	74551	K. Shure and M. Deutsch, Phys. Rev. 82,
60846	J. M. Siegel and L. E. Glendenin, reported in J. Am. Chem. Soc. <u>68</u> , 2411 (1946)	74S51a	K. Shure, Ph. D. Thesis, Massachusetts Institute of Technology (May 1951)
			of Technology (May 1951)

75549	F. Suzor, Ann. phys. 4, 269 (1949)	95550	E. Shapiro and C. E. Mandeville, Phys. Rev. 78, 319 (1950) (A)
76551 76551a	N. R. Sleight, NNES-PPR 9, 805 (1951)  N. R. Sleight, T. B. Novey, and L. E. Glendenin,	96547	J. W. Stout and W: M. Jones, Phys. Rev. 71, 582 (1947)
	NNES-PPR 9, 846 (1951)	97550	G. F. Snelling and E. W. Titterton, British
76S51b	N. R. Sleight and W. H Sullivan, NNES-PPR 9, 928 (1951)		Atomic Energy Commission Unclassified Report AERE-G/M-55 (Sept. 1950)
77547	J. A. Seiler, reported in Argonne National Laboratory Classified Report ANL-4000 (Aug. 1947)	98548	M. V. Scherb and C. E. Mandeville, Phys. Rev. 73, 1401 (1948)
77551	J. A. Seiler, NNES-PPR 9, 860 (1951)	99539	K. Sinma and F. Yamasaki, Phys. Rev. <u>55</u> , 320 (1939)
7755la	J. A. Seiler, NNES-PPR 9, 910 (1951)	100551	N. A. Schuster and G. E. Pake, Phys. Rev. 81,
77S51b	J. A. Seiler and L. Winsberg, NNES-PPR 9. 1206 (1951)	101551	886 (1951)  K. F. Smith, Nature 167, 942 (1951)
77S51c	J. A. Seiler and L. Winsberg, NNES-PPR 9, 1225 (1951)	102550	G. L. Stukenbroeker and J. R. McNally, Jr.,
78550	A. Storruste, Phys. Rev. 79, 193 (1950)	103551	J. Opt. Soc. Am. 40, 336 (1950)  W. W. Schoof and R. D. Hill, Phys. Rev. 83,
79550	A. J. Saur, P. Axel, L. G. Mann, and J. Ovadia, Phys. Rev. 79, 237 (1950) (A)	104553	892 (1951) (A)
80552	P. C. Stevenson and H. G. Hicks, private communication (April 1952)	104552	A. de Shalit, O. Huber, and H. Schneider, Helv. Phys. Acta 25, 279 (1952)
81542	R. N. Smith, Phys. Rev. <u>61</u> , 389 (1942)	105552	H. Schneider, O. Huber, F. Humbel, and A. de Shalit, Helv. Phys. Acta 25, 259 (1952)
82S48	R. Steffen, O. Huber, F. Humbel, and W. Zunti, Helv. Phys. Acta 21, 194 (1948)	106552	P. Stähelin, Phys. Rev. 87, 374 (1952)
82549	R. M. Steffen, O. Huber, and F. Humbel, Helv.	107549	L. Ya. Shavtvalov, Zhur. Eksptl.' i Teoret. Fis. 19, 633 (1949)
62551	Phys. Acta 22, 167 (1949)  R. M. Steffen, Phys. Rev. 83, 166 (1951)	107551	L. Ya. Shavtvalov, Zhur. Eksptl. i Teoret. Fiz. 21. 1123 (1951)
82551a	R. M. Steffen, Phys. Rev. 82, 827 (1951)	108551	P. M. Sherk and R. D. Hill, Phys. Rev. 83, 1097 (1951)
82552	R. M. Steffen, private communication (Oct. 1952)	109552	R. Sher, H. J. Kouts, and K. W. Downes, Phys.
83551	E. J. Schillinger, Jr., B. Waldman, and W. C. Miller, Phys. Rev. 83, 320 (1951)	110551	Rev. 87, 523 (1952)  J. Sharpe and G. H. Stafford, Proc. Phys. Soc.
84549	C. W. Stanley and S. Katcoff, J. Chem. Phys. 17, 653 (1949)		(London) 64A, 211 (1951)
84551	C. W. Stanley and L. E. Glendenin, NNES-PPR 9, 947 (1951)	111550	B. Smaller, J. May, and M. Freedman, Phys. Rev. 79, 940 (1950)
85551	D. T. Stevenson and M. Deutsch, Phys. Rev. 83, 1202 (1951)	112551	H. D. Sharma, Ph. D. Thesis, University of California Radiation Laboratory Unclassified Report UCRL-1265 (May 1951)
85S5la	D. T Stevenson and M. Deutsch, Phys. Rev. 84, 1071 (1951)	113552	W. L. Stirling and M. Goodrich, Phys. Rev. 87, 176 (1952) (A)
86552	D. Schiff, Phys. Rev. 85, 727 (1952) (A)	114551	F. N. Spiess, Ph.D. Thesis, University of California Unclassified Report UCRL-1494
87552	F. H. Schmidt and G. L. Keister, Phys. Rev. 86, 632 (1952) (A) and private communication (Oct. 1932)		(Oct. 1951)
88551	V. S. Shpinel, Zhur, Eksptl.' i Teoret, Fiz. 21, 853 (1951)	115552	<ul> <li>A. Sorruste, Ph. D. Thesis, University of Oslo (1952)</li> <li>J. B. Swan and R. D. Hill, Phys. Rev. 88, 831 (1952)</li> </ul>
88551a	V. S. Shpinel and N. V. Forasontov, Zhur. Eksptl.	116552a	J. B. Swan, W. M. Portnoy, and R. D. Hill,
	i Teoret. Fis. <u>21</u> , 1376 (1951)		Bull. Am. Phys. Soc. 27, No. 5, Abstract V4 (1952)
88S51b	V. S. Shpinel, Zhur. Eksptl. 'i Teoret. Fiz 21, 1370 (1951)	117552	D. A. Silverston, Proc. Phys. Soc. (London) <u>65A</u> , 344 (1952)
89552	R. Stump, Phys. Rev. <u>86</u> , 249 (1952)	118539	L. Szilard and W. H. Zinn, Phys. Rev. <u>55</u> , 799 (1939)
90552	C. L. Scoville, S. C. Fults, and M. L. Pool, Phys. Rev. 85, 1046 (1952)		
91552	A. B. Smith, Phys. Rev. 86, 98 (1952)		
91S52a	A. B. Smith, A. C. G. Mitchell, and R. S. Caird, Phys. Rev. 87, 454 (1952)	1 <b>T</b> 05	J. J. Thomson, Phil. Mag. 10, 584 (1905)
91552b	A. B. Smith and A. C. G. Mitchell, private communication (Oct. 1952)	2T47	D. H. Templeton, J. J. Howland, Jr., and I.
91S52c	A. B. Smith, R. S. Caird, and A. C. G. Mitchell, Phys. Rev. 88, 150 (1952)	2T47a	Periman, Phys. Rev. 72, 766 (1947)  D. H. Templeton, J. J. Howland, Jr., and L.
91552d	A. B. Smith and A. C. G. Mitchell, Phys. Rev. 87,	2T47b	Periman, Phys. Rev. 72, 758 (1947)  D. H. Templeton, R. H. Goeckermann, J. J.
92548	1128 (1952)  L. R. Shepherd and J. M. Hill, Nature 162, 566 (1948)		Howland, Jr., and I. Perlman, unpublished data (Jan. 1947)
92548a	L. R. Shepherd, Research (London) 1, 671 (1948)	2T48	D. H. Templeton and I. Perlman, Phys. Rev. 73, 1211 (1948)
93550	B. J. Stover, Phys. Rev. 80, 99 (1950)	2T48a	D. H. Templeton, A. Ghiorso, and I. Perlman,
93851	B. J. Stover, Phys. Rev. 81, 8 (1951)		unpublished data (June 1948)
94850	W. Steuber, Ph.D. Thesis, University of Illinois (1950)	2750	D. H. Templeton, Phys. Rev. 78, 312 (1950)



- 3T49 S. G. Thompson, A. Ghiorso, J. O. Rasmusser and G. T. Seaborg, Phys. Rev. 76, 1406 (1949)
- 3T50 S. G. Thompson, A. Ghiorso, and G. T. Seaborg, Phys. Rev. <u>77</u>, 838 (1950)
- 3T50a S. G. Thompson, A. Ghiorso, and K. Street, Jr., private communication (1950)
- 3T50b S. G. Thompson, A. Ghiorso, and G. T. Seaborg, Phys. Rev. 80, 781 (1950)
- 3T50c S. G. Thompson, K. Street, Jr., A Ghiorso, and G. T. Seaborg, Phys. Rev. 78, 298 (1950)
- 3T50d S. G. Thompson, K. Street, Jr., A. Ghiorso, and G. T. Seaborg, Phys. Rev. 80, 790 (1950)
- 3T50e S. G. Thompson, K. Street, Jr., A. Ghiorso, and F. L. Reynolds, Phys. Rev. <u>80</u>, 1108 (1950)
- 3T51 S. G. Thompson, K. Street, Jr., A. Ghiorso, and F. L. Reynolds, Phys. Rev. 84, 165 (1951)
- 3T52 S. G. Thompson, E. K. Hulet, and A. Ghiorso, private communication (Aug. 1952)
- 4T49 J. Teillac, Compt. rend. 229, 650 (1949)
- 4T50 J. Teillac, Compt. rend. 230, 1056 (1950)
- 4T52 J. Teillac, Ann. phys. 7, 396 (1952)
- 4T52a J. Teillac, P. Falk-Vairant, and C. Victor, J. phys. et radium 13, 143 (1952); Compt. rend. 233, 1025 (1951)
- 4T52b J. Teillac, P. Falk-Vairant, and C. Victor, Compt. rend. 234, 1051 (1952)
- 5T26 J. Thibaud, Ann. phys. 5, 73 (1926)
- 6T36 R. L. Thornton, Phys. Rev. 49, 207 (1936) (A)
- 6T37 R. L. Thornton and J. M. Cork, Phys. Rev. 51, 383 (1937) (A)
- 6T37a R. L. Thornton, Phys. Rev. 51, 893 (1937)
- 6T38 R. L. Thornton, Phys. Rev. 53, 326 (1938) (A)
- 6T47 R. L. Thornton and R. W. Senseman, Phys. Rev. 72, 872 (1947)
- 7751 E. P. Tomlinson, H. W. Fulbright, and J. J. Howland, Jr., Phys. Rev. 83, 223 (1951) (A)
- 7T52 E. P. Tomlinson and S. L. Ridgway, Phys. Rev. 88, 170 (1952) (A)
- 8T49 W. Thiel and A. H. Jaffey, reported in Argonne National Laboratory Classified Report ANL-4370 (Nov. 1949)
- 9T42 San-Tsiang Tsien, J. phys. et radium 3, 1 (1942); Compt. rend. 217, 685 (1943)
- 9T43 San-Teiang Teien, Compt. rend. 216, 765 (1943)
- 9T43a San-Tsiang Tsien, Compt. rend. 217, 599 (1943)
- 9T46 San-Tsiang Tsien, Phys. Rev. 69, 38 (1946)
- 9T46a San-Tsiang Tsien, M. Bachelet, and G. Bouissières, Phys Rev. 69, 39 (1946)
- 10T49 C. M. Turner, Phys. Rev. 76, 148 (1949), U. S. Atomic Energy Commission Unclassified Document AECU-432 (July 1949)
- llT48 M. Ter-Pogossian, J. E. Robinson, and C. S. Cook, Phys. Rev. 75, 995 (1948)
- llT49 M. Ter-Pogossian, J. E. Robinson, and H. Goddard, Phys. Rev. <u>76</u>, 453 (1949) (A)
- 11T49a M. Ter-Pogossian, C. S. Cook, C. H. Goddard, and J. E. Robinson, Phys. Rev. <u>76</u>, 909 (1949)
- 11T50 M. Ter-Pogossian, C. S. Cook, F. T. Porter, K. H. Morganstern, and J. Hudis, Phys, Rev. 80, 360 (1950); 81, 285 (1951)
- 11T51 M. Ter-Pogossian and F. T. Porter, Phys. Rev. 81, 1057 (1951)
- 12T49 A. V. Tollestrup, W. A. Fowler, and C. C. Lauriteen, Phys. Rev. 76, 428 (1949)
- 13T47 H. G. Thode and R. L. Graham, Can. J. Research 25A, 1 (1947)

- 13T48 H. G. Thode, J. Macnamara, F. P. Lossing, and C. B. Collins, J. Am. Chem. Soc. <u>70</u>, 3008 (1948)
- 13T48a H. G. Thode, Nucleonics 3, No. 3, 14 (1948)
- 13T49 H. G. Thode, Research 2, 154 (1949)
- 14T41 A. A. Townsend, Proc. Roy. Soc. (London) 177A, 357 (1941)
- 15T50 J. F. Turner, reported in British Atomic Energy Commission Report AERE-PR-18 (Oct. 1950)
- 15T51 J. F. Turner and P. E. Cavanagh, Phil. Mag. 42, 636 (1951)
- 16T46 R. Tangen, Kgl. Norske Videnskab. Selskab. Skr. No. 1 (1946)
- 17T47 C. A. Tobias and C. Levinthal, private communication (Jan. 1947)
- 17T48 C. A. Tobias, private communication (Sept. 1948)
- 18T51 H. K. Ticho, Phys. Rev. 84, 847 (1951)
- 18T52 H. K. Ticho, D. Green, and J. R. Richardson, Phys. Rev. 86, 422 (1952) and private communication (Oct. 1952)
- 19T47 R. C. Thompson and D. R. Miller, private communication (Jan. 1947)
- 19T48 R. C. Thompson and D. R. Miller, private communication (Jan. 1948)
- 20T 39 A. W. Tyler, Phys. Rev. 56, 125 (1939)
- 21T47 A. Turkevich, reported in Argonne National Laboratory Classified Report ANL-4010 (Sept. 1947)
- 21T51 A. Turkevich and J. B. Niday, Phys. Rev. 84, 52 (1951)
- 21T5la A. Turkevich and J. B. Niday, Phys. Rev. 84, 1253 (1951)
- 21T51b A. Turkevich, E. P. Steinberg, B. Finkle, and N. Sugarman, NNES-PPR 9, 1070 (1951)
- 22T51 J. Tobailem, Compt. rend. 233, 1360 (1951)
- 23T51 S. I. Taimuty, Phys. Rev. 81, 461 (1951)
- 24T45 B. Trumpy and J. J. Orlin, Bergens Museums Arbok, Naturv. Rekke Nr. 7 (1945)
- 25T47 D. J. Tendam and H. L. Bradt, Phys. Rev. 72, 527 (1947) (A)
- 25T47a D. J. Tendam and H. L. Bradt, Phys. Rev. 72, 1118 (1947)
- 26T51 D. A. Thomas, S. K. Haynes, C. D. Broyles, and H. C. Thomas, Phys. Rev. 82, 961 (1951)
- 27T49 G. M. Temmer, Phys. Rev. 76, 424 (1949)
- 28T38 G. F. Tape and J. M. Cork, Phys. Rev. 53, 676 (1938) (A)
- 29T40 L. A. Turner, Phys. Rev. 58, 679 (1940)
- 30T49 S. Thulin, I. Bergström, and A. Hedgran, Phys. Rev. 76, 871 (1949)
- 30T51 S. Thulin, Phys. Rev. 83, 860 (1951)
- 30T52 S. Thulin and I. Bergström, Phys. Rev. <u>85</u>, 1055 (1952)
- 30T52a S. Thulin, Phys. Rev. 87, 684 (1952)
- 30T52b S. Thulin, Arkiv Fysik 4, 363 (1952); reported in M. Siegbahn Commemorative Volume, p 163 (Uppsala, 1951)
- 30T52c S. Thulin, Arkiv Fysik (in press) (1952)
- 31T48 J. Townsend, M. Cleland, and A. L. Hughes, Phys. Rev. 74, 499 (1948)
- 32T50 C. C. Thomas, Jr. and E. O. Wiig, J. Am. Chem. Soc. 72, 2818 (1950)
- 33T51 S. E. Turner and L. O. Morgan, Phys. Rev. 81, 881 (1951)
- 34T52 Y. Tomosawa, M. Umesawa, and S. Nakamura, Phys. Rev. 86, 791 (1952)
- 35T49 C. H. Townes, J. M. Mays, and B. P. Dailey, Phys. Rev. 76, 700 (1949)

36T51	F. S. Tompkins, M. Fred, and W. F. Meggers, Phys. Rev. <u>84</u> , 168 (1951)	2W48	G. Wilkinson and H. G. Hicks, Phys. Rev. 74, 1733 (1948)
37T52	D. E. Tilley, Abstract 77, June Meeting, Roy. Soc. Canada (1952)	2W48a	G. Wilkinson, Phys. Rev. 73, 252 (1948)
38 <b>T4</b> 9	B. V. Thosar, Proc. Phys. Soc. (London) 62A, 739 (1949)	2 W 4 9	G. Wilkinson and H. G. Hicks, Phys. Rev. 75, 1687 (1949)
39T52	H. Tyren, unpublished data (March 1952)	2W49a	G. Wilkinson and H. G. Hicks, Phys. Rev. 75, 1370 (1949)
40T52	B. L. Tucker and E. C. Gregg, Phys. Rev. <u>87,</u> 907 (1952)	2 W 49b	G. Wilkinson and H. G. Hicks, Phys. Rev. <u>75</u> , 696 (1949)
41T50	A. P. Tudge and H. G. Thode, Can. J. Research 28B, 567 (1950)	2W49c	G. Wilkinson, Phys. Rev. 75, 1019 (1949)
42T52	A. L. Thompson, private communication (Oct. 1952)	2W50	G. Wilkinson, Phys. Rev. 79, 1014 (1950)
46176	A. D. Thompson, private communication (ecc. 1774)	2 W 5 0 a	G. Wilkinson and H. G. Hicks, University of California Radiation Laboratory Unclassified Report UCRL-751 (June 1950)
		2 W 5 0 b	G. Wilkinson and H. G. Hicks, Phys. Rev. <u>80,</u> 491 (1950)
IV 38	R. J. Voskuyl, Ph.D. Thesis, Harvard University (1938)	2 W 5 Oc	G. Wilkinson and H. G. Hicks, Phys. Rev. <u>79,</u> 815 (1950)
2 V 3 6	S. N. Van Voorhis, Phys. Rev. 50, 895 (1936)	2W50d	G. Wilkinson and H. G. Hicks, University of California Radiation Laboratory Unclassified Report
2 V 36a	S. N. Van Voorhis, Phys. Rev. 49, 889 (1936) (A)		UCRL-744 (June 1950)
2V40	S. N. Van Voorhis, private communication (1940)	2W50e	G. Wilkinson, Phys. Rev. 80, 495 (1950)
3V45	A. F. Voigt, private communication (Jan. 1945)	2 W 5 Of	G. Wilkinson, reported in Massachusetts Institute of Technology Unclassified Report NP-1879
3V48	A. F. Voigt and B. J. Thamer, Phys. Rev. 74, 1264 (1948) (A)		(Oct. 1950)
4V49	F. W. Van Name, Jr., Phys. Rev. <u>75</u> , 100 (1949)	2 W 5 0 g	G. Wilkinson and H. G. Hicks, Phys. Rev. <u>77,</u> 314 (1950)
5V51	G. Vendryes, Compt. rend. 232, 1549 (1951)	2W51	G. Wilkinson and H. G. Hicks, Phys. Rev. 81, 540 (1951)
5V51a	G. Vendryes, Compt. rend. 233, 391 (1951)	3W48	R. J. Walen, Compt. rend. 227, 1090 (1948);
6V39	G. E. Valley and R. L. McCreary, Phys. Rev. 56, 863 (1939)		J. phys. et radium 10, 95 (1949)
6V41	G. E. Valley and H. H. Anderson, Phys. Rev. <u>59</u> . 113 (1941) (A)	4W43	R. Wilkinson and J. S. Levinger, reported in Metallurgical Laboratory Classified Report CP-641 (May 1943)
6 V 4 1 a	G. E. Valley, Phys. Rev. 59, 686 (1941)	4W44	R. Wilkinson, W. Rall, and E. Meiners, reported in Metallurgical Laboratory Classified Report
6 <b>V4</b> 1b	G. E. Valley, Phys. Rev. 60, 167 (1941) (A)		CP-2090 (Sept. 1944)
7V38	O. Viktorin, Proc. Cambridge Phil. Soc. 34, 612 (1938)	4W51	R. G. Wilkinson and W. Rall, NNES-PPR 9, 1124 (1951)
8V51	N. F. Verster, G. J. Nijgh, R. Van Lieshout, and C. J. Bakker, Physica <u>17</u> , 637 (1951)	4W5la	R. G. Wilkinson, W. Rall, L. C. Miller, and L. F. Curtiss, NNES-PPR 9, 1128 (1951)
9V5Z	D. M. Van Patter, Massachusetts Institute of Technology Unclassified Report MIT-NSE-Tech. Rep.	4W52	R. G. Wilkinson, private communication (Oct. 1952)
	57 (Jan. 1952)	5 W 39	A. G. Ward, Proc. Cambridge Phil. Soc. 35, 322 (1939)
10V52	H. T. Vlaar and A. H. W. Aten, Jr., Physica 18, 275 (1952)	5 W 39a	A. G. Ward, Proc. Cambridge Phil. Soc. 35, 523 (1939)
11V52	P. J. Van der Haack, A. E. de Vries, and A. H. W. Aten, Jr., Physica 18, 20 (1952)	5W42	A. G. Ward, Proc. Roy. Soc. (London) 181A, 183 (1942)
12V52	A. Van der Weil and A. H. W. Aten, Jr., Physica	6W50	J. L. Wolfson, Phys. Rev. 78, 176 (1950)
	18. 356 (1952)	6W52	J. L. Wolfson, private communication (Oct. 1952)
13V52	G. Vierra and L. Salgueiro, Compt. rend. 234, 1765 (1952)	7 <b>W4</b> 8	M. Weissbluth, T. M. Putnam, and E. Segrè, private communication (July 1948)
14V52	C. Victor, J. Teillac, P. Falk-Vairant, and G. Bouissières, J. phys. et radium (to be published) (1952)	8W49	Q. Van Winkle, R. G. Larson, and L. I. Katsin, J. Am. Chem. Soc. <u>71</u> , 2585 (1949)
15V52	R. Vestergaard and E. Haeffner, Arkiv Fysik <u>3,</u> 557 (1952)	9W45	D. Williams and P. Yuster, Los Alamos Scientific Laboratory Classified Report LAMS-195 (Jan. 1945)
		9W46	D. Williams and P. Yuster, Phys. Rev. <u>69.</u> 556 (1946)
		10W51	J. C. Wallmann, Ph.D. Thesis, University of California Radiation Laboratory Classified Report UCRL-1255 (April 1951)
1 <b>W42</b>	A. C. Wahl and G. T. Seaborg, Metallurgical Project Classified Report (work performed at Berkeley) CN-266 (Sept. 1942)	11 <b>W46</b>	E. F. Westrum, Jr., R. W. Greenlee, and J. C. Hindman, Metallurgical Laboratory Classified Report CC-3894 (Nov. 1946)
1 <b>W48</b>	A. C. Wahl and G. T. Seaborg, Phys. Rev. 73, 940 (1948); NNES-PPR 14B, 21 (1949)	11W51	E. F. Westrum, Jr., Phys. Rev. <u>83</u> , 1249 (1951)
1W52	A. C. Wahl and N. A. Bonner, Phys. Rev. 85, 570 (1952)	12W51	D. West and J. K. Dawson, Proc. Phys. Soc. (London) 64A, 586 (1951)
2W47	G. Wilkinson, Nature 160, 864 (1947)	12W52	D. West, J. K. Dawson, and C. J. Mandleberg, Phil. Mag. <u>43</u> , 875 (1952)



R. M. Williamson and H. T. Richards, Phys. Rev. 76, 614 (1949) 14W49 15W41 J. A. Wheeler, Phys. Rev. 59, 27 (1941) 16W40 C. S. Wu, Phys. Rev. 58, 926 (1940) C. S. Wu and G. Friedlander, Phys. Rev. 60, 747 (1941) 16W41 C. S. Wu and E. Segrè, Phys. Rev. <u>61</u>, 203 (1942) (A) 16W42 C. S. Wu and E. Segrè, Phys. Rev. 67, 142 (1945) 16W45 C. S. Wu, W. W. Havens, Jr., and L. J. Rainwater, Phys. Rev. 74, 1248 (1948) (A) 16W49 C. S. Wu and L. Feldman, Phys. Rev. 76, 698 C. S. Wu, C. H. Townes, and L. Feldman, Phys. Rev. <u>76</u>, 692 (1949) 16W49a 16W49b C. S. Wu and L. Feldman, Phys. Rev. 76, 693 (1949) 16 W 49 c C. S. Wu and L. Feldman, Phys. Rev. 76, 696 (1949) 16W51 C. S. Wu and L. Feldman, Phys. Rev. 82, 457 (1951) C. S. Wu, B. M. Rustad, V. Perez-Mendez, and L. Lidofsky, Phys. Rev. 87, 1140 (1952) 16W52 A. S. Weil and J. R. Dunning, Columbia University Document CUD-9 (Feb. 1948) 17W48 S. D. Warshaw, Phys. Rev. 80, 111 (1950) 18W50 S. D. Warshaw, J. J. L. Chen, and G. L. Appleton, Phys. Rev. 80, 288 (1950) 18W50a 19 W 34 L. Wertenstein, Nature 133, 564 (1934) 20W41 S. B. Welles, Phys. Rev. 59, 679 (1941) M. G. White, L. A. Delsasso, J. G. Fox, and E. C. Creuts, Phys. Rev. <u>56</u>, 512 (1939) 21W39 21W41 M. G. White, E. C. Creutz, L. A. Delsasso, and R. R. Wilson, Phys. Rev. <u>59</u>, 63 (1941) W. W. Watson and E. Pollard, Phys. Rev. <u>57</u>, 1082 (1940) (A) 22W40 R. Wilson and G. R. Bishop, Proc. Phys. Soc. (London) 62, 457 (1949). Value recalculated in 23W49 23W50 R. Wilson, Phys. Rev. 79, 1004 (1950) J. R. White and A. E. Cameron, Phys. Rev. 74, 991 (1948) 24W48 H. Wäffler and O. Hirsel, Helv. Phys. Acta 21, 25W48 H. Waffler, Helv. Phys. Acta 23, 239 (1950) 25W 50 J. J. Wilkins and F. K. Goward, Proc. Phys. Soc. 26W51 (London) 64A, 849 (1951) Y. Watase and J. Itoh, Proc. Phys. - Math. Soc. 27W39 Japan 21, 626 (1939) . Watase, Proc. Phys. -Math. Soc. Japan 23, 27W41 618 (1941) P. K. Weimer, J. D. Kurbatov, and M. L. Pool, Phys. Rev. 60, 469 (1941) 28W41 P. K. Weimer, J. D. Kurbatov, and M. L. Pool, Phys. Rev. 66, 209 (1944) 28W44 29W52 G. Wagner and E. O. Wiig, J. Am. Chem. Soc. 74, 1101 (1952) 30W 37 H. Walke, Phys. Rev. 52, 663 (1937) 30W 37a H. Walke, Phys. Rev. 52, 400 (1937) 30W37b H. Walke, Phys. Rev. 52, 777 (1937) 30W 37c H. Walke, Phys. Rev. 52, 669 (1937) H. Walke, E. J. Williams, and G. R. Evans, Proc. Roy. Soc. (London) 171A, 360 (1939) 30W39

> H. Walke, F. C. Thompson, and J. Holt, Phys. Rev. <u>57</u>, 177 (1940)

30W40

S. C. Wright, Phys. Rev. 77, 742 (1950) (A)

13W50

**CHAP. 1.2** 30W40a H. Walke, Phys. Rev. 57, 163 (1940) H. Walke, F. C. Thompson, and J. Holt, Phys. Rev. <u>57</u>, 171 (1940) 30 W 40b M. A. Waggoner, M. L. Moon, and A. Roberts, Phys. Rev. 80, 420 (1950) 31W50 M. A. Waggoner, M. L. Moon, and A. Roberts, Phys. Rev. <u>78</u>, 295 (1950) 31W 50a M. A. Waggoner, Phys. Rev. 82, 906 (1951); 80, 489 (1950) 31W51 32W52 W. J. Worthington, Jr., Phys. Rev. 87, 158 (1952) H. W. Wilson and S. C. Curran, Phil. Mag. 40, 33W49 631 (1949) 33W50 H. W. Wilson, Phys. Rev. 79, 1032 (1950) 33W51 H. W. Wilson, Phys. Rev. 82, 548 (1951) 33W5la H. W. Wilson and S. C. Curran, Phil. Mag. 42, 762 (1951) 33W52 H. W. Wilson and G. M. Lewis, Proc. Phys. Soc. (London) 65A, 656 (1952) 34W42 G. L. Weil, Phys. Rev. 62, 229 (1942) L. L. Woodward, D. A. McCown, and M. L. Pool, Phys. Rev. 74, 870 (1948) 35W48 L. L. Woodward, D. A. McGown, and M. L. Pool, Phys. Rev. <u>74</u>, 761 (1948) 35W48a F. P. W. Winteringham, Nature 167, 155 (1951) 36W51 37W45 M. L. Wiedenbeck, Phys. Rev. 68, 237 (1945) 37W45a M. L. Wiedenbeck, Phys. Rev. 68, 1 (1945) 37W45b M. L. Wiedenbeck, Phys. Rev. 67, 92 (1945) 37W46 M. L. Wiedenbeck, Phys. Rev. 70, 435 (1946) 37W47 Wiedenbeck and K. Y. Chu, Phys. Rev. 72, 1164 (1947) D. R. Wiles, B. W. Smith, R. Horsley, and H. G. Thode, Chalk River Laboratory Classified Report CRC-493 (Jan. 1952) 38W52 F. Wagner, Jr. and M. S. Freedman, Phys. Rev. 86, 631 (1952) (A) 39W52 39 W 52a F. Wagner, Jr. and M. S. Freedman, Phys. Rev. (to be published) (1952) F. Wagner, Jr., M. S. Freedman, and D. Engelkemeir, U. S. Atomic Energy Commission Declassified Document AECD-3304 (Feb. 1952) 39 W 52b F. Wagner, Jr., M. S. Freedman, D. W. Engelkemeir, and L. B. Magnusson, Phys. Rev. (to be published) (1953) 39W53 E. J. Wolicki, B. Waldman, and W. C. Miller, Phys. Rev. 82, 486 (1951) 40W51 41W43 B. Waldman and M. L. Wiedenbeck, Phys. Rev. 63, 60 (1943) (A) B. Waldman, W. C. Miller, and D. Gideon, Phys. Rev. <u>76</u>, 181 (1949) (A) 41W49 42W47 A. Wattenberg, Phys. Rev. 71, 497 (1947) 43W48 R. R. Williams, Jr., J. Chem. Phys. 16, 513 (1948) 43W51 R. R. Williams, Jr., NNES-PPR 9, 220 (1951) 44W51 W. E. Winsche, L. G. Stang, Jr., and W. D. Tucker, Nucleonics  $\underline{8}_i$ , No. 3, 14 (1951) A. H. Williams and M. L. Wiedenbeck, Phys. Rev. 78, 822 (1950) 45W50 K. E. Weimer, M. L. Pool, and J. D. Kurbatov, Phys. Rev. <u>63</u>, 59 (1943) (A) 46W43 K. E. Weimer, M. L. Pool, and J. D. Kurbatov, Phys. Rev. 64, 43 (1943) (A) 46W43a 46 W 4 3 b K. E. Weimer, M. L. Pool, and J. D. Kurbatov, Phys. Rev. 63, 67 (1943)

A. H. Wapstra, Phys. Rev. 86, 561 (1952)

A. H. Wapstra, Phys. Rev. 86, 562 (1952)

47W52

CHAP.	1.2		REACTOR PHYSICS
48W50	B. Weaver, Phys. Rev. 80, 301 (1950)	1248	B. Zajac, E. Broda, and N. Feather, Proc. Phys. Soc. (London) 60, 501 (1948)
49W49	D. Walker, Proc. Phys. Soc. (London) 62A, 799 (1949)	1252	B. Zajac, Phil. Mag. 43, 264 (1952)
49W49a 50W52	D. Walker and E. W. Fuller, Nature 164, 226 (1949)  J. Walker, Proc. Phys. Soc. (London) 65A, 449	2249	A. S. Zavel'skii, G. Ya. Umarov, and S. K. Matushevskii, Zhur. Eksptl' i Teoret. Fis. 19. 1136 (1949)
51W51	(1952) L. Winsberg, NNES-PPR 9, 1273 (1951)	3243	W. H. Zinn, A. Wattenberg, and J. West, reported in Metallurgical Laboratory Classified Report CP-781 (July 1943)
51W51a 51W51b	L. Winsberg, NNES-PPR 9, 1284 (1951) L. Winsberg, NNES-PPR 9, 1302 (1951)	4242	Zlotowski and J. H. Williams, Phys. Rev. <u>62,</u> 29 (1942)
51 <b>W</b> 51c	L. Winsberg, NNES-PPR 9, 1311 (1951)	5248	D. J. Zaffarano, B. D. Kern, and A. C. G. Mitchell, Phys. Rev. 74, 582 (1948)
51W51d 51W52	L. Winsberg, NNES-PPR 9, 1292 (1951)  L. Winsberg, private communication (Oct. 1952)	5Z48a	D. J. Zaffarano, B. D. Kern, and A. C. G. Mitchell, Phys. Rev. 74, 105 (1948)
52W51	W. E. Wright and M. Deutsch, Phys. Rev. 82, 277 (1951)	5251	D. J. Zaffarano and F. I. Boley, Phys. Rev. 83, 223 (1951) (A).
53W41	C. M. Witcher, Phys. Rev. 60, 32 (1941)	6Z45	W. Zunti and E. Bleuler, Helv. Phys. Acta 18, 263 (1945)
54W51	T. Wiedling and A. Carlsson, Phys. Rev. 83, 181 (1951)	7252	W. Zobel, reported in Purdue University Progress Report II (June 1952)
55W51	A. Wennerblom, K. E. Zimen, and E. Ehn, Svensk Kem. Tid. 63, 207 (1951)	8249	H. Zeldes, A. R. Brosi, G. W. Parker, G. M. Hebert, and G. E. Creek, reported in Oak Ridge
56W52	B. T. Wright, Phys. Rev. (to be published) (1952); Bull. Am. Phys. Soc. 27, No. 5, Abstract Q2 (1952)		National Laboratory Classified Report ORNL-286 (June 1949)
57W52	J. Welker, A. Schardt, J. J. Howland, Jr., and G. Friedlander, private communication (Nov. 1952)	8Z50	H. Zeldes, B. H. Ketelle, and A. R. Brosi, Phys. Rev. <u>79</u> , 901 (1950)
58 <b>W</b> 52	T. Westermark, Phys. Rev. 88, 573 (1952); private communication (Oct. 1952)	8251	H. Zeldes, B. H. Ketelle, and A. R. Brosi, reported in Oak Ridge National Laboratory Classified Report ORNL-1036 (Sept. 1951)
		82.52	H. Zeldes, B. H. Ketelle, A. R. Brosi, C. R. Fults, and R. F. Hibbs, Phys. Rev. 86, 811 (1952)
		9249	K. E. Zimen, Z. Naturforsch. 4a, 95 (1949)
1747	L. Yaffe and C. E. MacKintosh, Can. J. Research 25B, 371 (1947)	10250	E. L. Zimmerman, E. B. Dale, D. G. Thomas, and J. D. Kurbatov, Phys. Rev. <u>80</u> , 908 (1950)
1748	L. Yaffe and J. M. Grunlund, Phys. Rev. <u>74</u> , 696 (1948)	11243	R. V. Zumstein, J. D. Kurbatov, and M. L. Pool, Phys. Rev. <u>63</u> , 59 (1943) (A)
1748a	L. Yaffe and K. M. Justus, Can. J. Research <u>26B</u> , 734 (1948)	12240	E. Zingg, Helv. Phys. Acta 13, 219 (1940)
1749	L. Yaffe, M. Kirsch, S. Standil, and J. M. Grunlund, Phys. Rev. <u>75</u> , 699 (1949)		
1 <b>Y49a</b>	L. Yaffe, B. W. Sargent, M. Kirsch, S. Standil, and J. M. Grunlund, Phys. Rev. 76, 617 (1949)		
1750	L. Yaffe and W. H. Stevens, Phys. Rev. <u>79</u> , 893 (1950)		
1751	L. Yasse, R. C. Hawkings, W. F. Merritt, and J. H. Craven, Phys. Rev. 82, 553 (1951)		
2Y35	D. M. Yost, L. N. Ridenour, and K. Shinohara, J. Chem. Phys. 3, 133 (1935)		
3Y38	T. Yasaki and S. Watanabe, Nature 141, 787 (1938)		
4742	T. Yuasa, Compt. rend. 215, 414 (1942)		
4Y52	T. Yuasa, Compt. rend. 235, 366 (1952)		
5447	F. Yu, D. Gideon, and J. D. Kurbatov, Phys. Rev. 71, 382 (1947)		
5Y48	F. Yu and J. D. Kurbatov, Phys. Rev. 74, 34 (1948)		

F. Yu. L. Cheng, and J. D. Kurbatov, Phys. Rev. 75, 1287 (1949) (A)

J. N. Young, M. L. Pool, and D. N. Kundu, Phys. Rev. 83, 1060 (1951)

R. S. Yalow and M. Goldhaber, Phys. Rev. 67, 59 (1945)

H. Yamasaki and K. Sinma, Sci. Papers Inst. Phys. Chem. Research (Tokyo) 37, 10 (1940)

5**T**49

6**T4**5

7**Y**51

8740

Table 1.2.17 — Thermal Cross Sections*

(AECU 2040, Neutron Cross Sections, May 15, 1952; and Supplement 1 to AECU 2040, November 20, 1952)

		Reaction Cr	t	Scattering Cross Sections				
Element	Isotope (%)	(2200 : σ _{abs}	m/sec)‡	$\sigma_{ m act}$	σ _{coh} (sign)	$\sigma_{\rm fa} \left( \frac{A+1}{A} \right)^2$	ō,	
		2.bs		vact				
1H		$0.330 \pm 0.007$			$1.79 \pm 0.02$ (-)	$81.4 \pm 0.4$	38 ± 4 (gas	
	H ¹ (~100)							
	H ² (0.015)	0.46 ± 0.1 mb	12 <b>y</b>	0.57 ± 0.01 mb	$5.4 \pm 0.3 (+)$	$7.5 \pm 0.1$		
₂ He					1.1 ± 0.2 (+)	$1.3 \pm 0.2$	$0.8 \pm 0.2$	
	He³ (0.00013)	mp 5200 ± 300						
	He ⁴ (~100)	0		0				
ă.		70 ± 1			0.40 ± 0.03 (-)	1.2 ± 0.3	1.4 ± 0.3	
•	Li ⁶ (7.5)	(nct 910)			6 ± 3 (+)			
	Li [†] (92.5)		0.98	33 ± 5 mb	0.80 ± 0.05 (-)	2.0 ± 0.5		
₄Be	Be ⁹ (100)	10 ± 1 mb	2.7 × 10	0 ⁶ y 9 ± 3 mb	7.54 ± 0.07 (+)	7.54 ± 0.07	7 ± 1	
هر		750 ± 10				4.4 ± 0.2	4 ± 1	
,,,,	B ¹⁰ (18.8)	(na: 3990)				2.9 ± 0.2	•-•	
	2 (20.4)	np <0.2				J.0 - J.2		
	B ¹¹ (81.2)	•	0.03s	<50 mb		4.4 ± 0.3		
c		4.5 mb			5.45 ± 0.07 (+)	5.51 ± 0.05	40402	
<b>,</b> €	C ¹² (96.9)	4.5 MD			3.43 ± 0.07 (*)	3.31 = 0.03	4.0 - 0.2	
	C ¹³ (1.1)		5800y	1.0 ± 0.3 mb	4.5 ± 0.6 (+)	5.5 ± 1.0		
	C ^M (5800y)	<200	2.48	<1 μb	2.0 - 0.0 (*)	0.0 - 2.0		
		1.50 + 0.05		•	110.054		10 ± 1	
¹ M	N ^M (99.6)	1.78 ± 0.05 np 1.70 ± 0.05			$11.0 \pm 0.5 (+)$	11.4 ± 0.5	10 = 1	
	M (33.0)	mp 1.70 ± 0.05 my 0.10 ± 0.05						
	N ¹⁵ (0.37)	my0.10 2 0.03	7.48	<b>24</b> ± 8μb				
_	(0.01)							
*O	O# 100 mm	<0.2 mb			4.2 ± 0.3 (+)	4.24 ± 0.02	4.2 ± 0.3	
	O ¹⁶ (99.76) O ¹⁷ (0.037)		F000-	C ⁴ 0.5 ± 0.1				
	O ¹⁸ (0.20)		5800y 29s	0.21 ± 0.04 mb				
,P	F ¹⁰ (100)	<10 mb	128	9 ± 2 mb	$3.8 \pm 0.3 (+)$	$4.0 \pm 0.1$	4.1 ± 0.3	
plie		<2.8				$2.9 \pm 0.2$	$2.4 \pm 0.3$	
	Ne ²⁶ (90.9)							
	Ne ²¹ (0.26)							
	Ne ²³ (8.8)		40s	36 ± 15 mb				
12Ma	Na ²² (100)	$0.49 \pm 0.02$	15h	$0.54 \pm 0.03$	$1.55 \pm 0.05 (+)$	$3.6 \pm 0.3$	$\textbf{4.0} \pm \textbf{0.5}$	
₁₃ Mg		59 ± 4 mb			$3.6 \pm 0.3 (+)$	3.8 ± 0.2	$3.6 \pm 0.4$	
	Mg ^M (78.6)	33 ± 10 mb						
	Mg ²⁶ (10.1)	270 ± 90 mb						
	Mg ^M (11.3)	60 ± 60 mb	9.6m	50 ± 10 mb				
13A1	Al ²⁷ (100)	$0.215 \pm 0.008$	2.3m	0.21 ± 0.04	$1.5 \pm 0.1 (+)$	$1.6 \pm 0.1$	1.4 ± 0.1	
16 <mark>91</mark>		$0.13 \pm 0.03$			$2.0 \pm 0.2 (+)$	2.4 ± 0.2	$\textbf{1.7} \pm \textbf{0.3}$	
	81 ²⁸ (92.22)	80 ± 30 mb						
	81 ³⁰ (4.70)	$0.27 \pm 0.09$						
	81 ³⁶ (3.08)	$0.41 \pm 0.41$	2.7h	$0.12 \pm 0.03$				

Table 1.2.17 — (Continued)

			ross Sections m/sec):	t	=	Cross Section	ons i
Element	Isotope (%)	σ _{abs}	•	σ _{act}	σ _{coh} (sign)	$\sigma_{\rm fa} \left(\frac{A+1}{A}\right)^2$	$\bar{\sigma}_{s}$
ışP	P ³¹ (100)	0.19 ± 0.03	14.3d	0.23 ± 0.05	3 ± 1 (+)	3.6 ± 0.3	10 ± 2
ieS		0.49 ± 0.02			1.20 ± 0.08 (+)	1.2 ± 0.2	1.1 ± 0.2
	S ³² (95.1)						
	S ³³ (0.74)						
	S ³⁴ (4.2)		87d	0.26 ± 0.05			
	S ³⁶ (0.016)		5m	$0.14 \pm 0.04$			
ırCl		31.6 ± 1.0			12.1 ± 0.8 (+)	15 ± 3	
	Cl ³⁵ (75.4)	np 0.30 ± 0.10	87d	S35 0.17 ± 0.04			
			4 × 10 ⁸ y	40 ± 25			
	Cl ³⁷ (24.6)		38m	0.56 ± 0.12			
10A		0.62 ± 0.04				0.9 ± 0.2	1.5 ± 0.5
10	A [™] (0.35)		34d	6 ± 2		*** **-	
	A ³⁸ (0.08)		265y	0.8 ± 0.2			
	A ⁴⁴ (99.6)		1.8h	0.53 ± 0.02			
19K	A ⁴¹ (1.8h)	1.97 ± 0.06	> 3.5y	>0.06	1.5 ± 0.1 (+)	2.0 ± 0.2	1.5 ± 0.3
1944	K ³⁹ (93.1)	1.87 ± 0.15	2 × 10 4y	3 + 2	1.5 2 0.1 (1)	2.0 2 0.2	1.5 - 0.5
	K (55.1)	70 ± 20	2 ^ 10 y				
	(0.012)	np <1					
	K ⁴¹ (6.9)	1.19 ± 0.10	12.4h	1.0 ± 0.2			
C-		0.43 ± 0.02			3.0 ± 0.1 (+)	3.2 ± 0.3	9 ± 2
20Ca	Ca ⁴⁶ (96.9)	0.43 ± 0.02 0.22 ± 0.04	8.5d	<0.1 mb	3.0 ± 0.1 (+)	3.1 ± 0.3	9-2
	Ca (90.5) Ca42 (0.64)	40 ± 3	6.34	CO.1 IIID	3.0 2 0.1 (*)	0.1 - 0.5	
	Ca ⁴³ (0.14)	40 3 3					
	Ca ⁴⁴ (2.1)		152d	0.63 ± 0.12	0.40 ± 0.03 (+)		
	Ca ⁴⁴ (0.0032)						
	Ca ⁴⁸ (0.18)		8.5m	1.1 ± 0.1			
21Sc	Sc 45 (100)	23 ± 2	208	10 ± 4	13 ± 1 (+)		
41			85d	12 ± 6			
			(20s → i	35d)			
₂₂ Ti		5.6 ± 0.4			1.4 ± 0.3 (-)	4.0 ± 0.4	6 ± 2
•	Ti ⁴⁶ (8.0)	0.6 ± 0.2					
	Ti ^{4†} (7.8)	1.6 ± 0.3					
	Ti ⁴⁸ (73.4)	8.0 ± 0.6					
	Ti ⁴⁹ (5.5)	$1.8 \pm 0.5$					
	Ti ²⁰ (5.3)	<0.2	6m	0.14 ± 0.03			
₂₂ V		4.7 ± 0.2			32 ± 8 mb (-)	5 ± 1	5 ± 1
-	V ⁵⁰ (0.2)						
	V ⁶¹ (99.8)		3.9m	4.5 ± 0.9			
_M Cr		2.9 ± 0.1			1.7 ± 0.1 (+)	4.1 ± 0.3	3.0 ± 0.5
Ma.	Cr ⁵⁰ (4.4)	16.3 ± 1.3	26.5d	11 ± 5	(17		
	Cr ⁵² (83.7)	0.73 ± 0.06		-			
	Cr ⁵³ (9.5)	17.5 ± 1.4					
	Cr ⁵⁴ (2.4)	<0.3					

Table 1.2.17 — (Continued)

			cross Sections m/sec)‡	st	Scattering Cross Sections			
Element	Isotope (%)	σ _{abs}	σ ₂₀	t	σ _{coh} (sign) σ _i	$a\left(\frac{A+1}{A}\right)^2$	σ̄s	
29 <b>M</b> n	Mn ⁵⁶ (100)	12.6 ± 0.6	2.6h	12.9 ± 0.5	1.7 ± 0.1 (-)	2.0 ± 0.1	2.3 ± 0.3	
₂₆ Fe		ηα 5 ± 3 mb			11.4 ± 0.3 (+)	11.7 ± 0.3	11 ± 1	
	Fe ⁵⁴ (5.9)	2.2 ± 0.2	2.9y	$0.7 \pm 0.3$	2.20 ± 0.13 (+)	$2.5 \pm 0.3$		
	Fe ⁵⁶ (91.6)	$2.6 \pm 0.2$			$12.6 \pm 0.4 (+)$	$12.8 \pm 0.2$		
	Fe ⁵⁷ (2.20)	$2.4 \pm 0.2$			$0.64 \pm 0.04 (+)$	$2.0 \pm 0.5$		
	Fe ⁵⁸ (0.33)	$2.5 \pm 2.0$	47d	$0.7 \pm 0.2$				
		ηα < 1.5 mb						
₂₇ Co	Co ^{so} (100)	34.8 ± 2.0	10.7m	14 ± 3	1.00 ± 0.06 (+)	7 ± 1	5 ± 1	
			5.3 <b>y</b>	20 ± 3				
			(99.7%	of 10.7m - 5.3y)				
≫Ni		4.5 ± 0.2			13.4 ± 0.3 (+)	17.6 ± 0.3	17.5 ± 1.	
	NI 56 (67.9)	4.2 ± 0.3			25.9 ± 0.3 (+)	24.4 ± 0.5		
	NI ⁶⁶ (26.2)	2.7 ± 0.2			$1.1 \pm 0.1 (+)$	1.0 ± 0.1		
	Ni ⁶¹ (1.2)	1.8 ± 1.3						
	N1 ⁶² (3.7)	15 ± 3			$9.5 \pm 0.4$ (-)	9 ± 1		
	NI ⁶⁴ (1.0)		2.6h	2.6 ± 0.4				
	N1 ⁶⁵ (2.6h)		56h	6 ± 3				
<b>⊯</b> Cu		3.59 ± 0.12			7.0 ± 0.4 (+)	$7.7 \pm 0.3$	7.2 ± 0.7	
	Cu ⁶³ (69.0)	4.3 ± 0.3	12.9h	$3.9 \pm 0.8$				
	Cu ⁶⁶ (31.0)	2.11 ± 0.17	4.3m	1.8 ± 0.4				
₩Zn		1.06 ± 0.05			4.3 ± 0.3 (+)	4.1 ± 0.2	3.6 ± 0.4	
	Zn ⁶⁴ (48.9)		250d	$0.5 \pm 0.1$				
			12.9h	Cu ⁶⁴ <10 ⁻⁵				
	Zn ⁶⁶ (27.8)	ηα < 20 μέο						
	Zn ⁶⁷ (4.1)	$\eta \alpha 6 \pm 4 \mu b$						
	Zn ⁶⁸ (13.ಕ)	ησι < 20 μέο	1 <b>4</b> h	$0.10 \pm 0.03$				
			52m	$1.0 \pm 0.2$				
	Zn ⁷⁰ (0.63)		2.2m	85 ± 20 mb				
31Ga		$2.71 \pm 0.12$				$7.5 \pm 0.5$	4 ± 1	
	Ga ⁸⁹ (60.2)	$2.0 \pm 0.2$	20m	$1.4 \pm 0.3$				
	Ga ⁷¹ (39.8)	$4.9 \pm 0.4$	14h	$3.4 \pm 0.7$				
₂₂ Ge		2.35 ± 0.20			8.8 ± 0.5 (+)	8.6 ± 0.5	3 ± 1	
	Ge ⁷⁰ (20.4)	$3.3 \pm 0.3$	11 <b>d</b>	3 ± 2				
	Ge ¹² (27.4)	$0.94 \pm 0.09$						
	Ge ¹³ (7.8)	$13.7 \pm 1.1$						
	Ge ⁷⁴ (36.6)	$0.60 \pm 0.06$	82m	$0.45 \pm 0.08$				
	Ge ⁷⁶ (7.8)	$0.35 \pm 0.07$	598	30 ± 20 mb				
			12h	$0.2 \pm 0.1$				
			(none o	of 59s - 12h)				
33 ^{A8}	As ⁷⁵ (100)	4.1 ± 0.2	27h	4.2 ± 0.8	$5.0 \pm 0.3 (+)$	7 ± 1	6 ± 1	
_M Se		11.8 ± 0.4			10.0 ± 0.6 (+)	9 ± 1	13 ± 1	
-	Se ⁷⁴ (0.87)	48 ± 7	115 <b>d</b>	24 ± 6				
	Se ⁷⁶ (9.0)	82 ± 7	188	7 ± 3				
	Se ⁷⁷ (7.6)	40 ± 4						

Table 1.2.17 — (Continued)

			Cross Sections	<b>s</b> †	Scattering Cross Sections			
Element	Isotope (%)	σ _{abs}	) m/sec)‡	σ _{act}	σ _{coh} (sign)	$\sigma_{fa} \left( \frac{A+1}{A} \right)^2$	ō,	
	Se ⁷⁸ (23.5)				COIL -			
	Se ¹⁰ (23.5)	0.4 ± 0.4	£0	30 ± 10 mb				
	Se** (49.8)	$0.59 \pm 0.06$	59m					
	Se st (9.2)	2.0 ± 1.4	17m 67s	0.5 ± 0.1 50 ± 25 mb				
	Se (5.2)	2.0 1 1.4	25m	4 ± 2 mb				
				of Isomers unknown)				
*Br		6.5 ± 0.5			5.7 ± 0.4 (+)	6.1 ± 0.2	6 ± 1	
<b>3</b>	Br ⁷⁹ (50.5)	. 10.4 ± 1.0	4.4h	2.9 ± 0.5	0.1 - 0.2 (.)	0.1 - 0.2	•	
	24 (00.0)	10.4 - 1.0	18m	8.5 ± 1.4				
	Br ⁸¹ (49.5)	2.6 ± 0.4	36h	3.5 ± 0.5				
			-	0.0 = 0.0				
*Kr	10	28 ± 5					7.2 ± 0.7	
	Kr ⁷⁸ (0.35)		34h	$0.3 \pm 0.1$				
	Kr ** (2.27)	95 ± 15						
	Kr ⁸² (11.6)	45 ± 15						
	Kr ⁸⁸ (11.6) Kr ⁸⁴ (57.0)	205 ± 10 <2	4.45	0.10 . 0.00				
	KF** (57.0)	<2	4.4h	0.10 ± 0.03 60 ± 20 mb				
			10y	4h → 10y)		•		
	Kr ⁸⁵ (10y)	<15	(10% 4.	<b>4</b> 0 → 10y)				
	Kr ⁸⁸ (17.4)	<2	78m	60 ± 20 mb				
	Kr ⁸⁷ (78m)	-	2.3h	<470				
₂₇ Rb	85	$0.70 \pm 0.07$			3.8 ± 0.3 (+)	5.5 <b>± 0.5</b>	12 ± 2	
	Rb ⁸⁵ (72.2)		19.5d	0.72 ± 0.15				
	Rb ^{\$7} (27.8) Rb ^{\$8} (18m)		17.5m	0.12 ± 0.03				
	KD** (18m)		15m	<200				
_M Sr		$1.16 \pm 0.06$			4.1 ± 0.3 (+)	$12.5 \pm 1.0$	10 ± 1	
	8r ^m (0.55)							
	8r ⁸⁸ (9.8)		2.7h	$1.3 \pm 0.4$				
	8r ⁸⁷ (7.0)							
	8r (82.7)		53d	5 ± 1 mb				
	8r ** (53d)		25y	<110				
	Sr ⁹⁰ (25y)		9.7h	1.0 ± 0.6				
₩Y	Y ³⁰ (100)	$1.38 \pm 0.14$	61h	1.2 ± 0.3			3 ± 2	
ø ^Z r		$0.18 \pm 0.02$			$5.0 \pm 0.3 (+)$	7.0 ± 0.5	8 ± 1	
	Zr ⁹⁰ (51.5)	$0.1 \pm 0.1$						
	Zr ⁹¹ (11.2)	$1.52 \pm 0.12$						
	Zr ⁹² (17.1)	$0.25 \pm 0.12$						
	Zr ⁸⁴ (17.4)	$0.08 \pm 0.06$	65d	$0.1 \pm 0.05$				
	Zr ⁸⁶ (2.80)	$0.1 \pm 0.1$	17h	$0.2 \pm 0.1$				
41Nb	Nb ⁹³ (100)	1.1 ± 0.1	6.6m	1.0 ± 0.5	6.0 ± 0.4 (+)	6.4 ± 0.3	5 ± 1	
<b>aM</b> o		2.4 ± 0.2			5.7 ± 0.4 (+)	6.1 ± 0.2	7 ± 1	
	Mo ⁸² (15.7)	<0.3	7h	<6 mb	v.z (·/		4	
	Mo ⁸⁴ (9.3)		•	<del>-</del>				
	Mo ⁸⁶ (15.7)	13.4 ± 1.3						



Table 1.2.17 — (Continued)

		Reaction Cross		ns†	Scatteri	ng Cross Section	ons i
Element	Isotope (%)	(2200 m/s		Pact	σ _{coh} (sign)	$\sigma_{12}\left(\frac{A+1}{A}\right)^{2}$	ō _s
	Mo ⁹⁶ (16.5)	1.2 ± 0.6					
	Mo ⁹⁷ (9.5)	2.1 ± 0.7					
	Mo [№] (23.9)	0.4 ± 0.4	67h	0.13 ± 0.05			
	Mo ¹⁰⁰ (9.5)	0.5 ± 0.5	15m	$0.20 \pm 0.05$			
<b>₄</b> Ru		2.46 ± 0.12				6.2 ± 0.5	6 ± 1
<b>~</b>	Bu ⁹⁶ (5.7)	2.40 - 0.12	2.8d	10 ± 4 mb		0.2 - 0.3	0-1
	Ru ⁸⁶ (2.22)		2.00	10 1 4 1110			
	Ru ⁹⁴ (12.8)						
	Ru 100 (12.7)						
	Ru ¹⁰¹ (17.0)						
	Bu 162 (31.3)		42d	1.2 ± 0.3			
	Ru 184 (18.3)		4h	0.7 ± 0.2			
_							
4 Rh	Rh ¹⁶³ (100)	150 ± 7	4.3m	12 ± 2	4.5 ± 0.5 (+)		6 ± 1
			448	140 ± 30			
<b>₩</b> Pd		8.0 ± 1.5			$5.0 \pm 0.3$ (+)	$4.8 \pm 0.3$	3.6 ± 0.6
	Pd ¹⁶² (0.8)						
	Pd ¹⁸⁴ (9.3)						
	Pd 165 (22.6)						
	Pd ¹⁸⁶ (27.1)						
	Pd ¹⁰⁰ (26.7)		13h	11 ± 3			
	Pd ¹⁹⁹ (13.5)		26m	$0.4 \pm 0.1$			
47Ag		60 ± 3			$4.6 \pm 0.3$ (+)	7 ± 1	6 ± 1
	Ag ¹⁸⁷ (51.9)	30 ± 2	2.3m	44 ± 9	8.7 ± 0.5 (+)	10 ± 1	
	Ag 162 (48.1)	84 ± 7	270d	2.8 ± 0.5	$2.3 \pm 0.2 (+)$	6 ± 1	
			24.58	110 ± 20			
uCd		2400 ± 200					7 ± 1
<b>W</b>		(not 1/v, × 1.3)					
	Cd ¹⁶⁶ (1.22)	( 4 . )	6.7h	1.0 ± 0.5			
	Cd ¹⁰⁰ (0.92)						
	Cd ¹⁹⁹ (12.4)		49m	0.2 ± 0.1			
	Cd ¹¹¹ (12.8)						
	Cd ¹¹² (24.0)		5 <b>y</b>	20 ± 10 mb			
	Cd ¹¹³ (12.3)	(19,500, not 1/v, × 1.3)					
	Cd ¹¹⁴ (28.8)		43d	0.14 ± 0.03			
			2.3d	1.1 ± 0.3			
	Cd ¹¹⁶ (7.6)		2.7h	$1.4 \pm 0.3$			
ملي		190 ± 10					2.2 ± 0.5
	In ¹¹³ (4.2)	100 - 10	50d	56 ± 12			
	-1 (4·6)		728	2.0 ± 0.6			
	<b>in¹¹⁵ (95.8)</b>		54m	145 ± 15			
			138	52 ± 6			
_M Sn	- 112	$0.65 \pm 0.05$			4.6 ± 0.3 (+)	4.9 ± 0.5	4 ± 1
	Sn ¹¹² (0.95)		30m	20 ± 10 mb			
			112d	$1.3 \pm 0.3$			

Table 1.2.17 — (Continued)

			C <mark>ross Sec</mark> tions 0 m/sec) <b>‡</b>	st .	Scatteri	ng Cross Section	ons i
Element	Isotope (%)	σ _{abs}	σ _{111/} sec/ ₁	act	σ _{coh} (sign)	$\sigma_{fa} \left( \frac{A+1}{A} \right)^2$	σ̄s
Sn	Sn ¹¹⁴ (0.65)						
(Cont'd.)	Sn ¹¹⁵ (0.34)						
	Sn ¹¹⁶ (14.2)		14.5d	6 ± 2 mb			
	Sn ¹¹⁷ (7.6)						
	Sn ¹¹⁸ (24.0)		245d	10 ± 6 mb			
	Sn 119 (8.6)						
	Sn ¹²⁰ (33.0)		>400d	1 ± 1 mb			
			27h	0.14 ± 0.03			
	Sn ¹²² (4.7)		40m	0.16 ± 0.04			
			126d	1.0 ± 0.5 mb			
	Sn 134 (6.0)		(Order	of Isomers unknown)			
			10d	4 ± 2 mb			
			(None	of 10m -> 10d)			
9.		5.5 ± 1.0			3.7 ± 0.3 (+)	4.2 ± 0.3	4.3 ± 0.5
₁₁ Sb	Sb ¹²¹ (57.2)	5.7 ± 0.5	2.8d	6.8 ± 1.5	3.7 - 0.3 (*/	4.2 - 0.3	4.5 - 0.5
	Sb (57.2)	3.9 ± 0.3	2.ou 21m	30 ± 15 mb			
	30 (42.0)	3.9 ± 0.3	1.3m	30 ± 15 mb			
			60d	2.5 ± 0.5			
				2.5 ± 0.5 1m & 1.3m - 60d unknown)			
			( 10 01 2	III & 1.3III ~ 600 dibdiowii,			
₽Te		$4.5 \pm 0.2$			$4.2 \pm 0.3 (+)$	$4.5 \pm 0.3$	5 ± 1
	Te ¹³⁰ (0.091)	70 ± 70					
	Te ¹²² (2.5)	$2.7 \pm 0.9$	100d	$1.0 \pm 0.5$			
	Te ¹²³ (0.88)	390 ± 30					
	Te ¹³⁴ (4.6)	$6.5 \pm 1.2$	58d	5 ± 3			
	Te ¹²⁵ (7.0)	$1.50 \pm 0.15$					
	Te ¹³⁶ (18.7)	$0.8 \pm 0.2$	90d	70 ± 20 mb			
			9.3h	0.8 ± 0.2			
	Te ¹²⁸ (31.8)	$0.3 \pm 0.3$	32d	15 ± 5 mb			
			72m	0.13 ± 0.03			
	Te ¹³⁰ (34.4)	0.5 ± 0.3	30h	<8 mb			
			25m	0.22 ± 0.05			
sə ^I	I ¹²⁷ (100)	$6.7 \pm 0.6$	27m	$6.3 \pm 1.3$	3.4 ± 0.2 (+)	$3.8 \pm 0.4$	3.6 ± 0.5
	$I^{129}$ (3 × $10^7$ y)		12.5h	11 ± 4			
	I ¹⁹¹ (8d)		2.4h	600 ± 300			
ыXe		.35 ± 5					4.3 ± 0.4
Marc	Xe ^{1M} (0.096)	,50 - 0					
	Xe ¹³⁶ (0.090)						
	Xe ¹²⁸ (1.92)	<5					
	Xe ¹²⁰ (26.4)	45 ± 15					
	Xe ¹³⁰ (4.08)	<5					
	Xe ¹³¹ (21.2)	120 ± 15					
	Xe ¹³² (26.91)	<5	5.3d	0.2 ± 0.1			
	Xe ¹³⁴ (10.4)	<5	9.2h	0.2 ± 0.1			
	Xe ¹³⁵ (9.2h)	3.5 × 10 ⁶ †	g. a.i				
	Xe ¹³⁶ (8.93)	<5					

Table 1.2.17 — (Continued)

		Reaction Cro	oss Section n/sec)‡	st	Scattering Cross Sections				
Element	Isotope (%)	σ _{abs}	σ _{act}		σ _{coh} (sign)	$\sigma_{fa} \left( \frac{A+1}{A} \right)^2$			
<b>ss</b> Cs	Cs ¹³³ (100)	29.0 ± 1.5	3h	16 ± 4 mb	3.0 ± 0.2 (+)	7 ± 1	20 ± 5		
			2.3y	26 ± 5					
			(~100%	3h - 2.3y)					
	Cs ¹³⁶ (2 × 10 ⁶ y)		13.7d	15 ± 8					
	Cs ¹³⁷ (37y)		33m	<2					
_{se} Ba		1.17 ± 0.10			3.5 ± 0.3 (+)	5 ± 1	8 ± 1		
_	Ba ¹³⁹ (0.101)		12.0d	30 ± 10 mb					
	Ba ¹³² (0.097)		>20y	6 ± 3					
	Ba ¹³⁴ (2.42)	2 ± 2							
	Ba ¹³⁵ (6.6)	5.6 ± 0.9							
	Ba ¹³⁶ (7.8)	$0.4 \pm 0.4$							
	Ba ¹³⁷ (11.3)	4.9 ± 0.4							
	Ba ¹³⁶ (71.7)	0.68 ± 0.10	86m	$0.5 \pm 0.1$					
	Ba ¹³⁸ (85m)		12.8h	4 ± 1					
ș, La		8.9 ± 0.3			8.7 ± 0.5 (+)	9.3 ± 0.8	18 ± 8		
	La ¹³⁶ (0.089)								
	La ¹³⁰ (99.9)		<b>40</b> h	8.4 ± 1.7					
	La ¹⁴⁰ (40h)		3.6h	3 ± 2					
<b>⊌</b> Ce		0.70 ± 0.08			2.7 ± 0.3 (+)	4 ± 1	9 ± 6		
Mac	Ce 136 (0.19)	25 ± 25				•			
	Ce ¹³⁶ (0.26)	9 ± 6	140d	<0.4					
	Ce ¹⁴⁰ (88.4)	0.63 ± 0.06	28d	0.3 ± 0.1	2.8 ± 0.2 (+)	2.8 ± 0.5			
	Ce ¹⁴² (11.08)	1.8 ± 0.3	33h	1.0 ± 0.2	2.6 ± 0.3 (+)	2.6 ± 0.5			
<b>p</b> Pr	Pr ¹⁴¹ (100)	11.2 ± 0.6	19h	11 ± 3	2.4 ± 0.3 (+)	4 ± 1			
	•				85.04(1)	15 4 5	<b>05 A 5</b>		
₩Nd	Nd 142 (27.1)	44 ± 2			6.5 ± 0.4 (+)	15 ± 5	25 ± 5		
	Nd ¹⁴³ (12.2)	18.5 ± 2			7.5 ± 0.6 (+)				
	Nd ¹⁴⁴ (23.9)	290 ± 30 4.8 ± 0.5			10+02(4)				
	Nd ¹⁴⁵ (8.3)	52 ± 4			1.0 ± 0.2 (+)				
	Nd (8.3)	9.8 ± 0.8	11d	1.8 ± 0.6	9.5 ± 0.5 (+)				
	Nd (17.2)	3.3 ± 1.0	1.7h	3.7 ± 1.2	5.5 2 0.5 (1)				
	Nd ¹³⁰ (5.6)	2.9 ± 1.5	2	0.7 - 1.2					
€i Pm	Pm ¹⁴⁷ (4y)	2.00	5.3d	60 ± 20					
_e Sm		6500 ± 1000							
_		(not 1/v, × 1.5)							
	Sm ¹⁴⁴ (3.1)		60d	<0.25					
	8m ¹⁴⁷ (15.0)								
	Sm ¹⁴⁸ (11.2)								
	8m 149 (13.8)	50,000 ± 20,000¶							
	Sm 150 (7.4)								
	Sm ¹⁵¹ (122y)	7,000 ± 2,000¶							
	Sm 152 (26.7)		47h	150 ± 40	2.5 ± 1.0	0 (-)			
	Sm 154 (22.5)		25m	5.5 ± 1.1					

Table 1.2.17 — (Continued)

		Reaction Cro (2200 m		st	Scattering Cross Section		
Element	Isotope (%)	σ _{abs}		act	σ _{coh} (sign)	$\sigma_{fa} \left( \frac{A+1}{A} \right)^2$	$\bar{\sigma}_{8}$
€)Eu		4500 ± 500					
		(not 1/v, × 0.95)					
	Eu ¹⁵¹ (47.8)	9000 ± 3000¶	9.2h	1400 ± 300¶			
	Eu ¹⁵² (5.3y)	5500 ± 1500¶					
	Eu ¹⁵³ (52.2)	420 ± 100¶					
	Eu ¹⁵⁴ (5.4y)	1500 ± 400¶					
	Eu ¹⁵⁵ (1.7y)	14,000 ± 4000¶					
⊌Gd		<b>44</b> ,000 ± 2000					
		(not $1/v_1 \times 0.85$ )					
	Gd ¹ (0.20)		<b>225d</b>	<125			
	Gd ¹⁵⁴ (2.15)						
	Gd ¹⁵⁵ (14.8) Gd ¹⁵⁶ (20.6)	70.000 ± 20.000¶					
	Gd ¹⁵⁷ (20.6) Gd ¹⁵⁷ (15.7)	160,000 ± 60,000¶					
	Gd (15.7) Gd (24.8)	180,000 ± 80,0001	18h	4 ± 2			
	Gd ¹⁶⁶ (21.8)		3.6m	1.5 ± 0.5			
€5 ^T b	Tb ¹⁸⁸ (100)	44 ± 4	73d	>22			
_{ee} Dy		1100 ± 150					
	Dy 186 (0.052)	1100 - 100					
	Dy ¹⁵⁸ (0.090)						
	Dy 100 (2.29)						
	Dy 161 (18.9)						
	Dy 162 (25.5)						
	Dy ¹⁶³ (25.0)						
	Dy 184 (28.2)		1.3m	2600 ± 300¶			
			2.4h	<1000¶			
			(1.3m -	- 2.4h)			
	Dy 185 (2.4h)		81h	5000 ± 2000¶			
etHo	Ho ¹⁶⁵ (100)	64 ± 3	27h	60 ± 12			
eeEr		166 ± 16					
-	Er162 (0.136)						
	Er ¹⁶⁴ (1.56)						
	Er ¹⁶⁶ (33.4)						
	Er 167 (22.9)						
	Er ¹⁶⁸ (27.1)						
	Er ¹⁷⁶ (14.9)		7h	>7			
es Tm	Tm 169 (100)	118 ± 6	129d	130 ± 30			
<b>™</b> Yb		36 ± 4					12 ±
	Yb ¹⁶⁸ (0.140)		33d	11,000 ± 3000¶			
	Yb ¹⁷⁶ (3.03)						
	Yb ¹⁷¹ (14.3)						
	Yb ¹⁷² (21.8)						
	Yb ¹⁷² (16.1)						
	Yb ¹⁷⁴ (31.8)		4d	60 ± 40			
	Yb ¹⁷⁶ (12.7)		1.8h				

Table 1.2.17 — (Continued)

			Cross Section 0 m/sec)‡	st		ng Cross Secti	ions f
Slement	Isotope (%)	σ _{abs}	σ ₂₀	et	$\sigma_{coh}$ (sign)	$\sigma_{fa} \left( \frac{A+1}{A} \right)^2$	σ̄s
71 Lu		108 ± 5					
	Lu ¹⁷⁵ (97.4)		3.7h	25 ± 10			
	Lu ¹⁷⁶ (2.60)		6.7d	4000 ± 800			
12Hf		115 ± 15				8 ± 1	
13.111	Hf ¹⁷⁴ (0.18)	1500 ± 1000				8 = 1	
	Hf 176 (5.2)	15 ± 15					
	Hf ¹⁷⁷ (18.4)	380 ± 30					
	Hf ¹⁷⁸ (27.1)	75 ± 10					
	Hf ¹⁷⁹ (13.8)	65 ± 15					
	Hf ¹⁹⁰ (35.4)	13 ± 5	46d	10 ± 3			
Тъ	Ta ¹⁸¹ (100)	21.3 ± 1.0	16 Am	30 ± 10 mb	6.1 ± 0.4 (+)	6 4 1	5 ± 1
13 ^{Ta}	12 (100)	21.3 1 1.0	16.4m 122d	21 ± 7	6.1 ± U.4 (+)	6 ± 1	3 - 1
				16.4m - 122d)			
			(~100%	16.4m → 122d)			
NW		19.2 ± 1.0			2.74 ± 0.05 (+	) 5.7 ± 0.6	5 ± 1
	W¹ ⁸⁶ (0.14)	60 ± 60	120 <b>d</b>	10 ± 10			
	W ¹⁸² (26.4)	19 ± 2					
	W ¹⁸³ (14.4)	11 ± 1					
	₩¹ ⁸⁴ (30.6)	2.0 ± 0.3	77d	2.1 ± 0.6			
	W ¹⁸⁵ (28.4)	34 ± 3	25h	40 ± 10			
	W ¹⁸⁷ (25h)		65d	90 ± 40			
11 ^{Re}		84 ± 4					14 ± 4
	Re ¹⁸⁵ (37.1)	100 ± 8	90h	100 ± 20			
	Re ¹⁸⁷ (62.9)	63 ± 5	18h	75 ± 15			
_N Os		$14.7 \pm 0.7$				15 ± 2	11 ± 3
	Os ¹⁸⁴ (0.018)		97d	<200			
	Os ¹⁸⁶ (1.58)						
	Os ¹⁸⁷ (1.64)						
	Os ¹⁸⁶ (13.3)						
	Os 188 (16.1)						
	Os ¹⁹⁰ (26.4)		15 <b>d</b>	8 ± 3			
	Os ¹⁹² (41.0)		32h	1.6 ± 0.4			
	Os ¹⁸³ (32h)		700d	60 ± 20			
mir		440 ± 20					
	Ir ¹⁹¹ (38.5)		1.4m	260 ± 100			
			70d	700 ± 200			
			(1.4m -	→ 70d)			
	<b>Ir¹⁸³ (</b> 61.5)		19h	130 ± 30			
19Pt		8.1 ± 0.4			11.2 ± 0.7 (+)	12 + 1	10 ±
18- ,	Pt 199 (0.012)	0.1 - 0.4			22.2 2 011 (1)		20 3
	Pt (0.012)		4.3d	90 ± 40			
	Pt ¹⁸⁴ (32.8)						
	Pt ¹⁹⁵ (33.7)						
	Pt ¹⁹⁶ (25.4)		18h	1.1 ± 0.3 (ground state)			
	,			J			

Table 1.2.17 — (Continued)

		Reaction C		ions†	Scatteri	ing Cross Sect	ions f
Element	Isotope (%)	σ _{abs}	m/sec)‡	~act	σ _{coh} (sign)	$\sigma_{fa} \left( \frac{A+1}{A} \right)^2$	₹ s
	Pt ¹⁹⁶ (7.2)		31m	3.9 ± 0.8			
₁₉ Au	Au ¹⁹⁷ (100)	94 ± 1	2.7d	96 ± 10	7.3 ± 0.1 (+)		9.3 ± 1.0
	Au ¹⁹⁸ (2.7d)		3.3d	16,000 ± 8,000¶			
e Hg		380 ± 20			22 ± 2 (+)		10 ± 5
M		(not 1/v, × 0.95)			22 - 2 (.,		10 - 0
	Hg ¹⁹⁶ (0.151)	3100 ± 1000 †					
	Hg ¹⁹⁸ (10.0)						
	Hg ¹⁸⁰ (16.9)	2500 ± 800\$					
	Hg ²⁰⁰ (23.1)	<60					
	Hg ²⁰¹ (13.2)	< 60					
	Hg ²⁰² (29.8)		44d	3.0 ± 0.8			
	Hg ²⁸⁴ (6.8)		5.5m	0.43 ± 0.10			
at Ti		3.3 ± 0.5			10 ± 2 (+)	10.0 ± 0.5	14 ± 2
B1 • •	Tl ²⁶³ (29.5)	11.0 ± 0.9	2.7y	8 ± 3	20 - 2 (.)	10.0 - 0.0	14 - 2
	Tl ²⁰⁵ (70.5)	0.77 ± 0.08	4.2m	0.10 ± 0.03			
	21 (1010)		•				
as Pb	•••	0.17 ± 0.01			$11.5 \pm 0.7 (+)$	$11.1 \pm 0.2$	11 ± 1
	Pb ²⁸⁴ (1.5)	0.8 ± 0.6					
	Pb ²⁶⁶ (23.6)	26 ± 5 mb					
	Pb ²⁶⁷ (22.6)	0.69 ± 0.05					
	Pb ²⁰⁰ (52.3)	<30 mb	3.3h	0.6 ± 0.2 mb			
<b>s</b> Bi	Bi ²⁰⁰ (100)	32 ± 3 mb	5 <b>d</b>	17 ± 3 mb	$9.4 \pm 0.1 (+)$	$9.4 \pm 0.1$	9 ± 1
"Ra	Ra ²²³ (11.2d)				<100		
_	Ra ²²⁶ (1620y)			15 ± 3	:0.1 mb		
	ыя ²²⁸ (б.7у)		<10m	36 ± 5	<2		
_{so} Ac	Ac ²²⁷ (18.6y)	500 ± 35			<2		
se Th	Th ²²⁷ (18.6d)				1500 ± 1000		
	Th ²²⁸ (1.90y)				<0.3		
	Th ²²⁹ (8 × 10 ³ y)				45 ± 11		
	Th ²³⁰ (8.0 × 10 ⁴ y)		25.5h	45 ± 10	<1 mb		
	Th ²³² (100)	7.0 ± 0.4	23.5m	$7.7 \pm 0.4$	<0.2 mb	12.5 ± 0.2	13 ± 2
	(1.39 × 10 ¹⁶ y)						
	Th ²²³ (23.5m)		24.1d	1400 ± 200			
	Th ²³⁴ (24.1d)		<10m	1.8 ± 0.5	<0.01		
₂₁ Pa	Pa ²³⁰ (17.3d)				1500 ± 250		
<b>N</b>	$Pa^{221} (3.4 \times 10^4 y)$		1.3d	260 ± 50	10 ± 5 mb		
	Pa ¹³² (1.3d)				700 ± 150		
	Pa ²²⁸ (27.4d)		1.2m	37 ± 14	<0.1		
			+ 6.7h				
	Pa ²²⁴ (UX ₂ ) (1.2m)				<500		
	(UZ) (6.7h)				<5000		
92 ^U					3.92**		$\sigma_t - \sigma_{abs} = 8.2$
	U ²³⁶ (20.8d)				25 ± 10		at 2200 m/s
	U ²³¹ (4.2d)				25 ± 10 250 ± 100		

Table 1.2.17 - (Continued)

			Reaction Cro (2200 n	oss Sections† n/sec)‡		Scattering Cross	Sections
Element	Isotope (%, T1/2)	$\sigma_{abs}$	$\sigma_{\mathbf{a}_{\mathbf{c}}}$	et	$\sigma_{ m fission}$	$\sigma_{fa} \left( \frac{A+1}{A} \right)^2$	$ar{\sigma}_8$
••U	U ²²² (70y)			-	80 ± 20		
(Cont'd.)	U ²³⁴ (0.0057)	89 ± 7	8.8 × 10 ⁸ y	72 ± 10	<0.65		
	(2.5 × 10 ⁸ y)		_				
	U ²³⁶ (0.714)	650**	2.5 × 10 ⁷ y	101**	549**		
	$(8.8 \times 10^8 \text{y})$				$\nu = 2.5 \pm 0.1**$		
	U ²²⁸ (99.3)	2.80**					
	(4.50 × 10 ⁸ y)						
	U ²³⁹ (23.5m)		14h	22 ± 5			
89Np	Np ²³⁴ (4.4d)				900 ± 300		
	Np ²³⁶ (22h)				10 ⁶		
	Np ²³⁷ (2.5 × 10 ⁶ y)		2.1d	150 ± 15	19 ± 3 mb		
	Np ²³⁶ (2.1d)				1600 ± 100		
	Np ²³⁰ (2.3d)				3		
₩Pu	Pu ²²⁸ (89.6y)		2.4 × 10 ⁴ y	425 ± 75	18 ± 2		
	Pu ²³⁰ (2.4 × 10 ⁴ y)		6.6 × 10 ³ y	361††	664††		
					$\nu = 3.0 \pm 0.1 \dagger \dagger$		
					neutrons per fission		
	Pu ^{Mi} (~12y)		~5 × 10 ⁸ y	400 ± 50	1080 ± 100		
	Pu ³⁴² (~5 × 10 ⁵ y)		5h	40 ± 20			
_M Am	Am ³⁴¹ (47.5y)		16h	700 ± 200	$3.2 \pm 0.2$		
			500y	<50			
			(20% 16h — 500y)				
	Am ^{362m} (16h)				2000 ± 1000		
	Am ³⁴² (500y)	8000 ± 1000			3500 ± 1000		
	Am ³⁴³ (~10 ⁴ y)		~25m	50 ± 25	<25		
_M Cm	Cm ³⁴³ (27đ)				20,000 ± 10,000		
	Cm ³⁶² (162.5d)				<5		

*This table contains the "best values" of several types of slow-neutron cross sections based on a careful consideration of all available data. Most of the cross sections have been measured several times, sometimes by different methods, and the error quoted in the table (standard error) is estimated from the consistency of the results as well as from the errors quoted for the individual measurements. The types of cross sections in the table correspond closely to methods of measurements, and the cross sections themselves are the actual measured, rather than derived quantities, as far as possible. All values given for an element refer to the natural mixtures of isotopes (that is, they are atomic cross sections), while those given for specific isotopes are isotopic cross sections. All cross sections, unless marked "mb" (millibams), are in barns. The cross sections in this table are unclassified; those given for elements of atomic number 88 and above, and for Xe²⁵⁶, have been declassified

†The "reaction cross sections" refer to all cases in which the neutron is not re-emitted, that is, to (n,y), (n,p), and  $(n,\alpha)$  reactions. Practically all the reaction cross sections are for (n,y)'s, and the few that are not are so marked. The absorption cross sections,  $\sigma_{abs}$ , are those particular reaction cross sections that are measured by observing the reaction itself in which the neutron is absorbed. The principal method used is the reactor oscillator, which measures the effect on the reactivity of a reactor caused by the absorption of the neutron. Reactor oscillator results from Argonne, Oak Ridge, and Harwell are represented in the table. In some cases, (n,p) and  $(n,\alpha)$  reactions have been measured in cloud chambers and counters, while other absorption cross sections have been estimated from the changes in isotopic abundances after long reactor irradiations. In several instances, the principal case being boron, the absorption cross section has been obtained from the total cross section by sub-

traction of scattering. The activation cross sections,  $\sigma_{act}$ , are those determined from the radioactivity of the product nucleus, usually the result of an  $(n,\gamma)$  reaction, and in a few cases, which are specially marked, by (n,p) or  $(n,\alpha)$  reactions. The activation cross sections always refer to particular isotopes and hence are isotopic cross sections; for monoisotopic elements, they are atomic cross sections as well. The absorption cross section, if measured for a single isotope or monoisotopic element, should agree with the activation cross section if the latter includes all activities produced. The activation cross sections for isomeric states are sometimes difficult to measure, and the results may be difficult to explain in tables. In this table, the upper (metastable) state is listed above the ground state (where the order is known), and the cross sections refer to the direct formation of each state. In those cases for which the amount of an isomeric activity would be increased indirectly by decay of another (shorter-lived) state, the percentage of the parent state that augments the activity is given. An example is cobalt for which there is a 20-b cross section for direct formation of the 5-yr activity and a 14-b cross section for the 11-min activity, practically all of which decays into its 5-yr daughter

† The reaction cross sections listed are those for a neutron velocity of 2200 m/sec even though the actual measurements were usually made with neutrons of wide energy spread. It should be remembered that thermal flux (nv) values are always stated for a velocity of 2200 m/sec (even though the neutrons may be above room temperature); hence, the cross section at this velocity must be used in calculations of reaction rate. In some cases, such as irradiation with well thermalized neutrons, it is quite simple to obtain the 2200-m/sec value from experimental results. In other cases, such as activation cross sections for reactor neutrons, it is difficult, and for still others, such as isotopic cross sections measured by the mass spectrometer, it is almost impossible. Each reaction cross section, unless marked "not 1/v" will have the same reaction rate in a Maxwell distribution as a 1/v absorber with the same 2200-m/sec cross section. In other words, the unmarked cross sections are either strictly 1/v in the thermal region or indistinguishable from 1/v within the accuracy quoted. The few marked "not 1/v" will have an effective 2200-m/sec cross section in a Maxwell distribution (at, or within about 100°C of, room temperature) obtained by multiplication of the 2200-m/sec value by the factor shown. This effective cross section when used with a thermal nv will give the correct reaction rate in a Maxwell distribution. For a few cases in which the 2200-m/sec value could not be determined, the cross sections are still included but are marked "reactor neutrons"

§ The scattering cross sections are usually constant with energy in the thermal region, except for crystal effects, and are hence not quoted for 2200 m/sec. The coherent cross section,  $\sigma_{coh}$ , is listed with the sign of the amplitude, where the positive sign corresponds to hard sphere scattering. The coherent scattering is that part of the total "bound-atom cross section" which contributes to such interference effects as Bragg scattering and mirror reflection. The "bound-atom cross section" is the cross section that would be observed if the atoms were completely bound (hence no thermal diffuse scattering) and yet scattered completely independently. Such a cross section, of course, is not observable experimentally but is calculated by applying the reduced mass correction,  $(A + 1/A)^2$ , to the free-atom cross section,  $\sigma_{1a}$ , which is the scattering cross section measured in the energy region (usually 10-20 ev) where the atom can be considered as a "free atom." No free-atom values are listed when the presence of resonances near thermal prevents the calculation of the bound-atom cross section. If there are no sources of incoherent scattering, such as spin dependent, isotopic, or inelastic incoherent scattering, then the measured value of  $\sigma_{coh}$  should be equal to  $\sigma_{fa} (A + 1/A)^2$ , as it is for Be as an example, compared to H in which  $\sigma_{coh}$  is much less than the bound-atom cross section. Sometimes the only scattering cross section that has been measured for a particular element is that averaged over the Maxwell distribution. This average scattering cross section  $\overline{\sigma}_s$ , will depend on the crystalline form of the sample and even upon the size of the crystal grains, but it is listed because of utility in certain practical applications

It is the purpose of the compilation to list only the actual directly measured quantities, even though it is possible in some cases to infer certain cross sections from other measurements. For instance, the calculated boundatom cross section, which is sometimes known quite accurately, could be listed as the coherent cross section if it is assumed that there are no sources of incoherent scattering. However, only the measured value of the coherent scattering (a measurement of  $\sigma_{coh}$  itself, or both  $\sigma_{fa}$  and the incoherent cross section) is given in the column for σ_{cob} even though in some cases the value inferred from the bound-atom cross section has smaller error. An example is fluorine, where the bound-atom value is more accurate than  $\sigma_{coh}$  and an assumption of negligible incoherent scattering would seem justified. Nevertheless, only the measured coherent cross section is listed in the ocoh column. Again, for the activation cross sections, it could be inferred that the more accurate absorption value, measured with the reactor oscillator, is correct to list for activation as well, if it is certain that only one activity is produced. Here, an example is Al²⁷ where the activation agrees with the absorption but is not as accurate. The principle of listing only the directly measured quantities in the appropriate columns is again followed in this case. Some judgment is thus necessary in using the table, especially in those cases where values of different types of cross sections, which presumably should agree, do not. For instance, it would be safe to use the more accurate absorption value, 0.19 ± 0.03 b, for the production of 14.3-day P2, even though the directly measured activation cross section is 0.23 ± 0.05 b. On the other hand, the cross section for production of 87-day  $S^{35}$  by the Cl³⁵ (n,p) reaction has been measured as 0.30 ± 0.10 b by direct observation of the reaction (in a



cloud chamber) and as 0.17 ± 0.04 b by activation. In this case, it is certainly not clear that one value is right and the other wrong, hence a weighted average probably should be used. The preparation of the cross section compilation has brought to light a number of such disagreements, and work has already begun to improve the measurements in these cases

- ¶Reactor neutrons
- ** AEC Release April 7, 1952

‡‡ AEC Release April 7, 1952; cross sections for an approximately Maxwellian neutron spectrum with a most probable neutron velocity of 2200 m/sec

#### REFERENCES

- 1. Feshbach and Weisskopf, Phys. Rev., 76, p 1550, 1949.
- 2. B. T. Feld, H. Feshbach, M. L. Goldberger, H. Goldstein, and V. F. Weisskopf, Final Report of the Fast Neutron Data Project, AEC Report NYO-636.
- 3. Bethe, Elementary Nuclear Theory, p 6. From data on  $\alpha$ -decay.
- 4. M. G. Mayer, Phys. Rev., 74, p 235, 1948.
- 5. K. Way, Phys. Rev., 75, p 1448, 1949.
- 6. R. F. Van Wye and J. S. Beckerley, Nucleonics, 9, p 17, Oct. 1951.
- 7. Rubinson, Jour. Chem. Phys., 17, p 542, 1949.
- 8. Rev. Mod. Phys., 15, p 209, 1950.
- 9. Periman, Ghiorso, and Seaborg, Phys. Rev., 77, p 26, 1950.
- 10. Weisskopf and Blatt, Theoretical Nuclear Physics, John Wiley and Sons, Inc., New York, 1952.
- 11. Katz and Penfold, Rev. Mod. Phys., 24, p 1, 1952.
- 12. H. Bethe, BNL-T-7.
- 13. W. A. Aroux, B. G. Hoffman, and F. C. Williams, AECU-663.
- 14. Private Communication from M. Nelkin.
- 15. D. C. Brunton and G. C. Hanna, Can. Jour. Res., A28, p 190, 1950.
- 16. M. Deutsch and M. Ramsey, MDDC-945, 1945.
- 17. B. Finkle, E. Hoagland, S. Katcoff, and N. Sugarman, Report CC-2076, 1944: reproduced in Reference (18).
- 18. C. D. Coryell and N. Sugarman, Radiochemical Studies: The Fission Products, McGraw-Hill Book Co., Inc., New York, 1951.
- 19. Neutron Cross Sections, AECU-2040, May 15, 1952, and Supplement, Nov. 20, 1952.
- 20. BNL-170, May 15, 1952 (classified).
- 21. S. Untermyer and J. T. Weills, Heat Generation in Irradiated Uranium, ANL-4790, Feb. 25, 1952.
- 22. KAPL-377 (classified) and KAPL-394 (classified).
- 23. KAPL-183 (classified).
- 24. K. Way and E. P. Wigner, Phys. Rev., 73, p 1318, 1948.
- 25. Hornyak et al, Rev. Mod. Phys., 22, p 291, 1950.
- 26. Ergebnisse der Exakten Wissenschaften, vol. 25. Julius Springer, Berlin, 1951.
- 27. D. Jackson, Nat. Res. Council of Canada, Rep. No. 2610.
- 28. Rev. Mod. Phys., 19, p 199, 1950.
- 29. Arnold, Jurnez, Schafer, Swickard, and Zabel, LA-1339.
- 30. D. J. Hughes, Reactor Neutron Physics, Addison-Wesley Press, Inc., Cambridge (to be published).
- 31. Fermi, Strum, and Sachs, Phys. Rev., 71, p 589, 1947.
- 32. M. Lax, Rev. Mod. Phys., 23, p 287, 1951.
- 33. R. J. Finklestein, Phys. Rev., 72, p 907, 1947.
- 34. E. Meklonian, Phys. Rev., 76, p 1750, 1949.
- 35. D. D. Philips and R. W. Davis, AEC Report LA-740, 1949.
- 36. L. E. Beghiam, M. A. Grace, G. Preston, and H. Halban, Phys. Rev., 77, p 286L, 1950.
- 37. Byster and Carter, private communication from Los Alamos.
- 38. H. H. Barschall, M. E. Battat, W. C. Bright, E. R. Graves, T. Jorgensen, and J. H. Manley, Phys. Rev., 72, p 881, 1947.
- 39. L. Szilard, S. Bernstein, B. T. Feld, and J. Ashkin, Phys. Rev., 73, p 1307, 1948.
- 40. H. F. Dunlap and R. N. Little, Phys. Rev., 60, p 693, 1941.
- 41. Philips, LA-1142 (classified).
- 42. Deleted
- 43. P. H. Stelson and W. M. Preston, Phys. Rev., 86, p 132, 1952.
- 44. C. E. Mandeville, C. P. Swann, and F. J. Seymour, Phys. Rev., 86, p 861, 1952.
- 45. Phys. Rev., 87, p 366, 1952.
- 46. Fowler and Slye, Phys. Rev., 77, p 787, 1950.
- 47. Martin and Diven, Phys. Rev., 86, p 565, 1952.
- 48. Forbes, AECU-1883.
- 49. Graves, LAMS-1300 (classified).
- 50. A. H. Snell, LA-1371.
- 51. Cohen, Phys. Rev., 81, p 184, 1951 and Nucleonics, 8, p 29, Feb. 1951.
- 52. D. J. Hughes, CF-3490, 1946 (classified).
- 53. Goldstein et al, CP-3574, 1946 (classified).
- 54. Charpie, Sun, and Jennings, Phys. Rev., 76, p 1255, 1949.

# SELECTED READING LIST

NEUTRON CROSS SECTIONS, T. W. Bonner, H. Goldstein, W. W. Havens, Jr., D. J. Hughes, L. Kaplan, C. O. Muchlhause, A. H. Snell, J. R. Stehn, T. M. Snyder, R. F. Taschek, A. Wattenberg, C. W. Zobel; BNL-170 (classified) and AECU-2040.

NUCLEAR DATA, K. Way et al., National Bureau of Standards publication 499 and supplements.

FINAL REPORT OF THE FAST NEUTRON DATA PROJECT, B. T. Feld, H. Feshbach, M. L. Goldberger, H. Goldstein, V. F. Weisskopf: AEC Report NYO-636.

RADIOCHEMICAL STUDIES: THE FISSION PRODUCTS, C. D. Coryell and N. Sugarman.

K. Way, Mon-P-192 (classified).

THEORETICAL NUCLEAR PHYSICS, J. M. Blatt and V. F. Weisskopf, to be published, John Wiley and Sons, Inc., New York (1952).

INTRODUCTORY NUCLEAR PHYSICS, D. Halliday, John Wiley and Sons, Inc., New York (1950).

EXPERIMENTAL NUCLEAR PHYSICS, E. Segré et al, John Wiley and Sons, Inc., New York (to be published).

### CHAPTER 1.3

# Kinetic Theory of Neutrons

H. Soodak, F. Adler, and E. Greuling

The fundamental relation of neutron kinetics is the continuity equation which expresses the law of neutron conservation in the volume element, dr dv, of phase space, viz.:

Time rate of increase of neutron density = Production - Absorption - leakage

Thus, in the steady state, the Boltzmann equation is:

$$0 = \mathbf{S}(\underline{\mathbf{r}},\underline{\mathbf{v}}) + \Lambda(\underline{\mathbf{r}},\underline{\mathbf{v}},\underline{\mathbf{v}}') \ \mathbf{v}'\mathbf{n}(\underline{\mathbf{r}},\underline{\mathbf{v}}') - \mathbf{v}\sigma\mathbf{n}(\underline{\mathbf{r}},\mathbf{v}) - \operatorname{div} \ \mathbf{v} \ \mathbf{n}(\underline{\mathbf{r}},\underline{\mathbf{v}})$$
(1a)

where  $n(\underline{r},\underline{v})$  is the density of neutrons in phase space, and S is the total source, being the sum:

$$\mathbf{S}(\mathbf{r},\underline{\mathbf{v}}) = \mathbf{S}^{\text{ext}}(\underline{\mathbf{r}},\underline{\mathbf{v}}) + \nu \ \Gamma(\underline{\mathbf{r}},\underline{\mathbf{v}},\underline{\mathbf{v}}') \ \mathbf{v}'\mathbf{n}(\underline{\mathbf{r}},\underline{\mathbf{v}}')$$
 (1b)

of the external source  $S^{\text{ext}}$  and the fission source. The integral operators  $\Gamma$  and  $\Lambda$  refer respectively to fission and to scattering-in. To treat the time-dependent case, it is necessary to replace the left side of Eq. (1a) by  $\partial/\partial t$  n( $\underline{r},\underline{v},t$ ) and, if desired, to correct  $\Gamma$  to include the delay times of the delayed neutrons.

For slowing-down without space variation, the Boltzmann equation reduces to Eq. (2)* and is treated later in this chapter. The reduction in the case of one-velocity theory leads to Eq. (17) of this chapter. Even these highly idealized problems involve integral equations of considerable complexity.

General methods are considered which are useful in attacking integral and integro-differential equations. One consists of expanding the integrands into a Taylor series or into suitable eigenfunctions (e.g., the spherical harmonics method) and results in a system of ordinary or partial differential equations. Treating Eq. (17) by the spherical harmonics expansion (in the  $P_1$  approximation), for example, leads to the equations of elementary diffusion theory.

A second method, useful in treating Eq. (17) when scattering is isotropic, proceeds by reformulating that equation into an integral equation.

In another approach, useful in treating Eq. (2), the exact kernel is approximated by a "synthetic kernel" which is chosen such that the integral equation reduces to a differential equation. Various slowing-down theories, for example the Fermi age theory, can be represented by such synthetic kernels.

In the discussion of space and energy variation in this chapter, simultaneous approximations of diffusion and slowing-down are generally required to yield manageable equa-

^{*}This reduction is carried out by placing div  $\underline{n}\underline{v} = 0$  and integrating over the various directions of the velocity vector.

tions such as those of the Fermi age theory. These equations are further simplified by the group-diffusion approximation and are thus reduced to a convenient form for solution by computing machines. The diffusion of thermal neutrons also is treated.

The results contained in this chapter pertain to media consisting of homogeneous regions and also of simple geometries. Although mention is made of the variational technique, the major application of this technique as well as of perturbation and iteration methods is deferred until the discussion of reactors in Chapter 1.4.

Table 1.3.1 lists definitions and notations used in this chapter.

Table 1.3.1 — Table of Symbols

σ	Macroscopic cross section	S(E) dE	Rate of production of neutrons in
$\sigma_{\mathbf{c}}$	Capture not leading to fission		dE about E per unit volume
$\sigma_{\mathbf{f}}$	Fission	p(E)	"Resonance" escape probability =
$\sigma_{\mathtt{a}}$	$\sigma_{c} + \sigma_{f}$		q(E) divided by the total
$\sigma_{\mathbf{s}}$	Total scattering		source strength
$\sigma_{\mathbf{i}}$	Inelastic scattering	f	$(\nu \sigma_f - \sigma_a)/\sigma$ ; 1 + f is the multiplica-
$\sigma_{tr}$	Transport cross section		tion in neutron number per collision
$\left. egin{array}{c} \sigma_{\mathbf{t}} \\ \sigma \end{array}  ight\}$	Total cross section = $\sigma_a + \sigma_s$	k	Multiplication constant: the ratio
n nv)	Neutrons per unit volume		of fission neutrons produced per neutron absorbed in infinite
φ	Flux or track length per unit vol-		medium. (Also the Boltzmann
7 }	ume per unit time		constant)
$\mathbf{F}_{0}$	•	V	Average number of neutrons
F F	Directional flux		emitted per fission
J	Current density = $\Omega$ F	1	Mean free path = $1/\sigma$
ψl		λ	Extrapolation length (also used
<b>#</b> u]	Collision density = $\sigma_t \phi$		for mean free path and for ex-
$\frac{\mathbf{v}}{\mathbf{\Omega}}\mathbf{v}$	Neutron velocity		ponent in asymptotic solution in Tables 1.3.4 and 1.3.5)
u J	$\ln E_0/E$ , where $E_0$ is a constant	D	Diffusion coefficient; constant of
	energy		proportionality between neutron
τ	Fermi age variable		current and gradient $\phi$
q	Slowing-down density: $q(\underline{r},E)$ is	L	Diffusion length
	the rate per unit volume at	K	Reciprocal asymptotic attenuation
	which neutrons slow down to		distance (used as 1/L or in
	below energy E		dimensionless units as $1/L\sigma$ )
g(E,E') dE	Slowing-down kernel: probability	μ	Cosine of angle between neutron velocity and the z axis;
	of neutrons scattered at E' to		$\sigma_a/\xi(\sigma_a+\sigma_s)$ is denoted by $\mu$ in
	land in dE about E		Table 1.3.6
G(E,E')	Probability of neutrons scattered	l	
	at E' to land below E	μο	Cosine of the scattering angle in
Ę	Average loss in logarithm of en-		the laboratory system
	ergy per scattering	$\overline{\mathbf{v}}$	Unit vector in direction of neu-
α	Minimum value of E/E' where E	D.	tron velocity
	is the energy after a scattering	P _l	Legendre polynomial of degree l.
	at E	$\left[\begin{array}{c} \mathbf{K}_{0} \\ \mathbf{r} \end{array}\right]$	Bessel functions defined as in "British Association Mathe-
€	$\frac{1}{2\xi^2}$ times the average square	I _o J	matical Tables" Vol. VI, Part I
	of the loss in logarithm of en-	ω	Used as angular frequency and as
	ergy per scattering		Fourier transform variable
	· -		

# SLOWING-DOWN WITH NO SPACE VARIATION (Harry Soodak)

### **BASIC EQUATIONS**

Consider the problem of slowing-down in an infinite homogeneous medium of uniform composition in the presence of a uniform source S(E).* The neutron balance equation is:

$$\psi(\mathbf{E}) = \int_{\mathbf{E}}^{\infty} \frac{\sigma_{\mathbf{S}}(\mathbf{E}')}{\sigma(\mathbf{E}')} g(\mathbf{E}, \mathbf{E}') \ \phi(\mathbf{E}') \ d\mathbf{E}' + \mathbf{S}(\mathbf{E})$$
 (2)

The slowing-down density, q, is defined by:

$$\mathbf{q}(\mathbf{E}) = \int_{\mathbf{E}}^{\infty} \frac{\sigma_{\mathbf{S}}(\mathbf{E}')}{\sigma(\mathbf{E}')} \mathbf{G}(\mathbf{E}, \mathbf{E}') \ \phi(\mathbf{E}') \ d\mathbf{E}'$$
 (3)

where the integrated kernel, G, is:

$$G(\mathbf{E}, \mathbf{E}') = \int_0^{\mathbf{E}} g(\mathbf{E}'' \mathbf{E}') d\mathbf{E}''$$
 (4)

with G(E,E) = 1. It follows that:

$$\frac{\mathbf{dq}(\mathbf{E})}{\mathbf{dE}} = \frac{\sigma_{\mathbf{a}}}{\sigma} \ \psi(\mathbf{E}) - \mathbf{S}(\mathbf{E}) \tag{5}$$

which is a neutron balance equation equivalent to Eq. (2). If the cross sections  $\sigma_S$ ,  $\sigma$  and kernel g are given, then Eq. (2) is subject to numerical analysis to obtain  $\Psi(E)$  for any source function S(E). The slowing-down density is then obtainable by numerical integration of Eqs. (5) or (3).

The "resonance" escape probability, p(E), is defined by:

$$p(\mathbf{E}) = \frac{q(\mathbf{E})}{\int_{\mathbf{E}}^{\infty} S(\mathbf{E}) d\mathbf{E}}$$
 (6)

and is primarily useful when E is below the lowest energy source neutrons.

## ISOTROPIC ELASTIC SCATTERING

The kernels g and G are given in Table 1.3.2 for the case of elastic scattering which is isotropic in the center-of-mass system.

### GENERAL SOLUTIONS

If hydrogen (M = 1) is the only slowing-down element, the integral equation (2) reduces to the differential equation:

$$\frac{\mathbf{d}\psi(\mathbf{E})}{\mathbf{d}\mathbf{E}} + \frac{\sigma_{\mathbf{g}}}{\sigma} \frac{\psi(\mathbf{E})}{\mathbf{E}} - \frac{\mathbf{d}\mathbf{S}(\mathbf{E})}{\mathbf{d}\mathbf{E}} = 0 \tag{7}$$

^{*}All text equations are written in terms of the unambiguous variable E. The equations in terms of the logarithmic energy variables u are easily obtainable from the text equations.

[†]These formulas are valid also for uniform composition media of variable density with a non-uniform source as long as there is no neutron loss by leakage, where  $\psi$ , q, and S are to be interpreted as being volume integrals.

if  $u' \le u \le u' + \ln^{1/\alpha}$ G(n,u') 0 if  $u \ge u' + \ln^{1/\alpha}$ e-(u-u')/€ if u ≥ u'  $\frac{1}{\epsilon} e^{-(u-u')/\epsilon \xi}$  if u >e-(u-u') if u > u' - 0 1 if u ≤ u' 1 if  $u \le u'$ 1 if u s u'  $\{\varrho(n-n)\}$ e - (n-n,)  $1-\alpha$  $\frac{1}{\sigma_s} \sum_i \ \sigma_s^{(i)} \ G^{(i)}$ Where g^(i) and G^(i) are the single element kernels for the ''i'th element > E ≤ E' Table 1.3.2 — Elastic Kernels in Terms of E and of u = ln (constant/E)  $E - \alpha E'$  if  $\alpha E'$   $(1 - \alpha) E'$ G(E,E') 0 if  $E \leq \alpha E'$ 1 if  $E \geq E'$ If E S E' 1 If E > E' छ। छ  $\frac{1}{1-\alpha} e^{-(u-u')} \text{ if } u' \leq u \leq u' + \ln^{1/\alpha}$ if u ≥ u' g(n,n')  $\{\varrho'(u-u') + \varrho(u-u')\}$  $\frac{1}{\xi}e^{-(u-u')/\xi} \text{ if } u \geq u'$  $e^{-(u-u)}$  if  $u \ge u'$  $\frac{1}{\epsilon^2 \xi} e^{-(u-u')/\xi \xi}$ 0 otherwise oifu<u/> 0 if u < u' 0 if u < u'  $\frac{1}{\sigma_s} \sum_i \sigma_s(i) g(i)$  $\frac{1}{1-\alpha}\frac{1}{E}$ , if  $\alpha E' \le E \le E'$ g(E,E') if E ≤ E' 0 otherwise E > E' fi 0 三百 Greuling-Goertzel (G. G.) elements, arbiarbitrary mass Hydrogen (M = 1) Case trary masses Single element, Mixtures of Wigner Fermi

Digitized by Google

which in conjunction with Eq. (5) leads to:

$$\mathbf{q}(\mathbf{E}) = \mathbf{E}[\boldsymbol{\psi}(\mathbf{E}) - \mathbf{S}(\mathbf{E})] \tag{8}$$

and:

$$\frac{\mathbf{dq(E)}}{\mathbf{dE}} - \frac{\sigma_{\mathbf{a}}}{\sigma} \frac{\mathbf{q(E)}}{\mathbf{E}} + \frac{\sigma_{\mathbf{S}}}{\sigma} \mathbf{S(E)} = 0 \tag{9}$$

Solutions of these equations are presented in Table 1.3.3.*

Table 1.3.3 — Exact Hydrogen Solutions and Solutions for Synthetic Kernels

Case	Unit point source, $S(E) = \delta(E - E_0)$	Arbitrary source, S(E)	
Hydrogen	$\mathbf{q}(\mathbf{E}) = \frac{\sigma_{s} (\mathbf{E}_{0})}{\sigma (\mathbf{E}_{0})} e^{-\int_{\mathbf{E}}^{\mathbf{E}_{0}} \sigma_{s}^{*} \frac{d\mathbf{E}}{\mathbf{E}}}$	$q(E) = \int_{E}^{\infty} \frac{\sigma_{\frac{3}{2}}(E')}{\sigma(E')} S(E') e^{-\int_{E}^{E'} \frac{\sigma_{a}}{\sigma} \frac{dE}{E} dE'}$	
Exact solution	$\psi(\mathbf{E}) = \frac{\mathbf{q}(\mathbf{E})}{\mathbf{E}} + \delta(\mathbf{E} - \mathbf{E}_{\theta})$	$\psi(E) = \frac{q(E)}{E} + S(E)$	
Single element	$\mathbf{q}(\mathbf{E}) = \frac{\sigma_1 (\mathbf{E}_0)}{\overline{\sigma} (\mathbf{E}_0)} e^{-\frac{1}{\xi} \int_{\mathbf{E}}^{\mathbf{E}_0} \frac{\sigma_3}{\overline{\sigma}} \frac{d\mathbf{E}}{\overline{\mathbf{E}}}$	$q(E) = \int_{E}^{\infty} \frac{\sigma_{i}(E')}{\overline{\sigma}(E')} S(E') e^{-\frac{1}{\xi} \int_{E}^{E'} \frac{\sigma_{a}}{\overline{\sigma}} \frac{dE}{E}} dE$	
Fermi, Wigner, G. G.	$\phi(\mathbf{E}) = \frac{\sigma(\mathbf{E})}{\overline{\sigma}(\mathbf{E})} \left[ \frac{\mathbf{q}(\mathbf{E})}{\xi \mathbf{E}} + \epsilon \delta(\mathbf{E} - \mathbf{E_0}) \right]$		
	$\overline{\sigma} = \sigma_{\underline{a}} + \epsilon \sigma_{\underline{a}}$	$\overline{\sigma} = \sigma_{\mathbf{a}} + \epsilon \sigma_{\mathbf{a}}$	

For heavier moderators (M > 1), the integral equation does not reduce because of the sharp cut-off in the kernel, g. The reduction to a differential equation can be made, however, if the kernel, g, is approximated by the synthetic kernels given in Table 1.3.2.

All three approximate kernels, g, are correctly normalized and give the correct value of the average logarithmic energy loss. The G.G. kernel gives also the correct value of the average of the square of the logarithmic energy loss. These statements are referred to below as "matching of moments."

These synthetic kernels all lead to:

$$\mathbf{q}(\mathbf{E}) = \xi \ \mathbf{E} \left[ \frac{\sigma_{\mathbf{g}} + \epsilon \ \sigma_{\mathbf{g}}}{\sigma} \ \psi(\mathbf{E}) - \epsilon \ \mathbf{S}(\mathbf{E}) \right] \tag{10}$$

$$\frac{d\mathbf{q}(\mathbf{E})}{d\mathbf{E}} - \frac{\sigma_{\mathbf{a}}}{\xi(\sigma_{\mathbf{g}} + \epsilon \sigma_{\mathbf{a}})} \frac{\mathbf{q}(\mathbf{E})}{\mathbf{E}} + \frac{\sigma_{\mathbf{S}}}{\sigma_{\mathbf{S}} + \epsilon \sigma_{\mathbf{a}}} \mathbf{S}(\mathbf{E}) = 0 \tag{11}$$

$$\frac{\mathbf{d}}{\mathbf{dE}} \left( \mathbf{E} \frac{\sigma_{\mathbf{S}} + \epsilon \sigma_{\mathbf{a}}}{\sigma} \psi \right) - \frac{\sigma_{\mathbf{a}}}{\xi (\sigma_{\mathbf{S}} + \epsilon \sigma_{\mathbf{a}})} \frac{\left( \mathbf{E} \frac{\sigma_{\mathbf{S}} + \epsilon \sigma_{\mathbf{a}}}{\sigma} \psi \right)}{\mathbf{E}} + \mathbf{S} \left( \frac{1}{\xi} - \epsilon \right) - \epsilon \mathbf{E} \frac{\mathbf{dS}}{\mathbf{dE}} = 0$$
(12)

^{*}Placzek¹ gives an exact solution for the case of an element of arbitrary M > 1 with no capture. This definitive paper contains most of the results quoted in the discussion, "Isotropic Scattering." References appear at end of chapter.

where  $\epsilon$  is given by:

$$\epsilon \text{ (Fermi)} = 0$$

$$\epsilon \text{ (Wigner)} = 1$$

$$\epsilon \text{ (G. G.)} = \frac{1 - \alpha \left[1 + \ln \frac{1}{\alpha} + \frac{1}{2} \ln^2 \frac{1}{\alpha}\right]}{(1 - \alpha) \xi^2}$$

$$= 1 \text{ for hydrogen}$$

$$\approx \frac{2}{3} \text{ for M} >> 1$$
(13)

Solutions of these equations are given in Table 1.3.3. It is to be noted that the Wigner and G. G. approximations are exact for hydrogen and that all three approximations are correct asymptotically in the case of no absorption.

## **MIXTURES**

For mixtures, the simplest procedure is to approximate the correct kernel g by the moment matched synthetic kernels,* in order to reduce Eq. (2) to a differential equation. This procedure can be expected to give poor results in a mixture of elements of significantly different masses.† A method for handling a mixture of hydrogen and a heavy element in the presence of absorption has been suggested by Goertzel³ who treats the hydrogen kernel exactly and the heavy element kernel by the Fermi approximation and thus arrives at a pair of coupled differential equations. These equations have been treated by a perturbation method.⁴

#### ASYMPTOTIC SOLUTIONS

For energies below those of the source neutrons, Eq. (2) reduces to the homogeneous form (S = 0) for which exact solutions exist for several cases. Also, an approximate solution (by Hurwitz) exists (more accurate than the Fermi, Wigner, and G. G.) for the case of a single-element moderator with slowly varying  $\sigma_a/\sigma$ . These solutions are given in Table 1.3.4.

The magnitude of the asymptotic solutions is determined by the slowing-down density just below the energy of the lowest-energy-source neutrons. In many cases of interest, absorption is negligible at the source energies, and as a result, the slowing-down density at high energies can be taken as the total source-strength.

Table 1.3.6 presents a comparison of results obtained by the Fermi, Wigner, G. G. approximations with the correct asymptotic results for the case of constant  $\sigma_2/\sigma$  (for this case, the Hurwitz method is exact); Fig. 1.3.1 presents a comparison of Fermi, G. G., Hurwitz, and exact (numerical, from Eq. 2) results for a smoothly varying  $\sigma_2/\sigma(\sigma_S = \text{const.}, \sigma_A = \text{const.}/\nu)$ .

## FLUCTUATIONS NEAR SOURCE ENERGY

For monoenergetic source neutrons (energy  $E_0$ ) in a single-element moderator (M > 1), the collision density undergoes damped oscillations in the first few collision intervals before approaching the asymptotic form.‡ A schematic diagram of  $\psi(E)$  for the case of no

[†]The paper by Placzek¹ contains most of the results in the discussion "Slowing Down with No Space Variation."



^{*}Thus for the Fermi approximation, Eqs. (10) through (13) still hold where  $\xi$  is the average logarithmic energy loss for the mixture. For the G. G. approximation, see Edlund.²

[†]Note the behavior of a mixture of hydrogen and a heavy element in Table 1.3.4. These transition effects do not appear in the synthetic kernel approximation.

**Table 1.3.4**— Asymptotic Solutions (Exact and Approximate) (Normalized such that  $q(E_0) = 1$  where  $E_0$  is some high energy)

Case	$\psi(\mathbf{E})$	q(E)
No absorption; single element or non-hydrogeneous mixture	<u>1</u> ξΕ	1
No absorption; hydrogen plus a single element of mass M:	$\frac{1}{\xi E} + \frac{r-1}{\left(r - \frac{1-c}{\frac{1}{\alpha}-1}\right) \left(\ln \frac{1}{\alpha}\right) - 1} \left(\frac{E}{E_0}\right)^r \frac{1}{E}$	1
$\mathbf{c} = \frac{\sigma_{\mathbf{g}} (\mathbf{H})}{\sigma_{\mathbf{g}} (\mathbf{H}) + \sigma_{\mathbf{g}} (\mathbf{M})}$ $\bar{\xi} = \mathbf{c} + (1 - \mathbf{c}) \xi$	where r is defined by: $\frac{r}{1-c} = \frac{\left(\frac{1}{\alpha}\right)^r - 1}{\frac{1}{r} - 1}$	
Π 1 – c << ξ	$\begin{vmatrix} 1 - c & \frac{1}{\alpha} - 1 \\ \approx \frac{1}{E} \end{vmatrix}$	1
If M >> 1 and c << ξ	$\approx \frac{1}{\xi E} \left\{ 1 + \frac{c}{\xi} \left[ \left( \frac{E}{E_0} \right)^{1 + \frac{C}{\xi}} - 1 \right] \right\}$	1
If M >> 1 and c >> ξ	$\approx \frac{1}{E} + \left(\frac{1}{\xi} - \frac{1}{c}\right) \left(\frac{E}{E_0}\right)^{1 + \frac{c}{\xi}} \frac{1}{E}$	1
Single element or non-hydrogenous mixture: $\sigma_8/\sigma \ll 1$	$\approx \frac{1}{\xi E} e^{-\int_{E}^{E_0} \frac{\sigma_a}{\xi \sigma_s} \frac{dE}{E}}$	$\approx e^{-\int_{E}^{E_0} \frac{\sigma_a}{E\sigma_a} \frac{dE}{E}}$
$\sigma_i/\sigma = \text{constant}$ , single element	$\lambda \frac{o}{\sigma_a} \left( \frac{E}{E_0} \right)^{\lambda} \frac{1}{E}$	$\left(\frac{E}{E_0}\right)^{\lambda}$
	where $\lambda$ is defined by: $\frac{\sigma_s}{\sigma} \frac{\left(\frac{1}{\alpha}\right)^{\lambda-1} - 1}{(1-\alpha)(\lambda-1)} = 1$	
	values of $\lambda$ are given in Table 1.3.5	
$\sigma_2/\sigma =$ slowly varying, single element; Hurwitz' solution	$\frac{1}{\sqrt{\xi}} \frac{f(\lambda)}{\sqrt{df/d\lambda}} e^{-\int_{\mathbf{R}}^{\mathbf{E}_0} \lambda} \frac{d\mathbf{E}}{\mathbf{E}}$	$\frac{1}{\sqrt{\xi}} \frac{f(\lambda) - 1}{\lambda \sqrt{df/d\lambda}} e^{-\int_{E}^{R_0} \lambda \frac{dE}{E}}$
	where $\lambda$ is defined as above, and	the normalization assumes that
	$f(\lambda) = \frac{\left(\frac{1}{\alpha}\right)^{\lambda-1} - 1}{(1-\alpha)(\lambda-1)}$	$\sigma_{\mathbf{a}}(\mathbf{E}_{0}) \approx 0$

Table 1.3.4 -- (Continued)

Case	ψ( <b>E</b> )	q(E)
Single, narrow absorption resonance at energy E _r	$\frac{1}{\xi E}$ for $E > E_r$	1 for E > E _r
Non-hydrogen mixture; Wigner solution is exact for this case	$\frac{1}{\xi E} e^{-\frac{1}{\xi} \int_{\text{res}} \frac{\sigma_a}{\sigma} \frac{dE}{E}} \text{ for } E < E_r$	$e^{-\frac{1}{\xi}\int_{res} \frac{\sigma_a}{\sigma} \frac{dE}{E}}$ for $E < E_r$
$\sigma_a/\sigma_s = \text{const/v}$ ; hydrogen	$\frac{1}{E} \frac{1}{\left(1 + \frac{\sigma_a}{\sigma_s}\right)^2}$	
σ _a /σ _s = const/v; hydrogen single element of mass M	$\frac{1}{\xi E} e^{-\left\{ \left(M + \frac{1}{3}\right) \frac{\sigma_a}{\sigma_s} - \frac{1}{3} M \left(\frac{\sigma_a}{\sigma_s}\right)^2 \right\}}$	
	where terms in $\left(\frac{\sigma_a}{\sigma_s}\right)^2$ and $M\left(\frac{\sigma_a}{\sigma_s}\right)^3$ are neglected	

Table 1.3.5 — The Exponent,  $\lambda$ , in the Asymptotic Solution for Constant  $\sigma_s/\sigma$  (Weinberg and Noderer, CF-51-5-98, Vol. I)

M	$\sigma_{\rm a}/\sigma_{\rm s}$	λ*
12	0.0005	0.003168
	.005	.031588
	.05	.306496
	.1	.593757
	.2	1.118817
50	.0005	0.012663
	.005	.126248
	.05	1.225912
100	.0005	0.025162
	.005	.250831

*For  $\sigma_a/\sigma_s << 1$  and  $\lambda \ln 1/\alpha << 1$ 

then: 
$$\lambda \approx \frac{\sigma_a}{\xi \sigma_s + \sigma_a} \left[ 1 + \frac{\sigma_a/\sigma_s}{\left(\frac{\sigma_a}{\sigma_s} + \xi\right)^2} \frac{(1 - \xi)^2 (1 - \alpha)}{2\alpha} \right]$$

which, for a heavy element,  $1 - \alpha << 1$ , reduces to:

$$\lambda \approx \frac{\sigma_a}{\xi \sigma_s + \sigma_a} \left[ 1 + \frac{\xi \sigma_a / \sigma_s}{\left(\frac{\sigma_a}{\sigma_s} + \xi\right)^2} \right]$$

Table 1.3.6 — Comparison of Resonance Escape Probabilities
in the Energy Range $E_1$ to $E_2$ where $\ln E_1/E_2$ = 5 and $\sigma_a/\sigma_s$ Is Constant.
$[p = q(E_2)/q(E_1) = (E_2/E_1)^{\mu}]$

C	ase	Asymptotic and Hurwitz	Fermi	Wigner	G. G.
М	$\sigma_{\rm a}/\sigma_{\rm s}$	μ = λ	$\mu = \frac{\sigma_{\mathbf{a}}}{\xi \sigma_{\mathbf{s}}}$	$\mu = \frac{\sigma_a}{\xi(\sigma_s + \sigma_a)}$	$\mu = \frac{\sigma_a}{\xi(\sigma_s + \epsilon \ \sigma_a)}$
12	0.005 .05 .1	0.85390 .2160 .0514 .00372	0.85346 .2050 .0420 .00177	0.85412 .2211 .0561 .00508	0.00376
50	0.005	0.5319 .00218	0.5308 .00178	0.5325 .00240	
100	0.0005 .005	0.88178 .2853	0.88176 .2841	0.88182 .2859	

absorption is graphed in Fig. 1.3.2 and compared to the asymptotic solution  $\psi_a(E)$ . The discontinuity in  $\psi$  at  $E = \alpha E_0$  is a result of the sharp cut-off in the kernel g(E,E'). Approximate magnitudes of the deviation  $D = |(\psi - \psi_a)/\psi_a|$  for large M are  $D(E_0) = 50\%$ ,  $D(\alpha E_0) = 35\%$ ,  $D(\alpha^2 E_0) = 2\%$ , and  $D(\alpha^3 E_0) = 0.3\%$ . The deviations decrease with M and vanish for hydrogen.

It may be noted that such oscillations are also caused by a sharp absorption resonance, since the effect is that of a negative source.

# **EXACT SOLUTIONS FOR SPECIAL SOURCES**

From Eq. (2), a source, S(E), can be readily constructed for any specified solution,  $\psi(E)$ . For example, if the simple asymptotic form in a non-capturing medium,  $\psi = 1/\xi E$ , is to hold exactly up to  $E_0$ , and then vanish for higher energies, the required source is:

$$S = \frac{1}{\xi(1-\alpha)} \left( \frac{1}{E_0} - \frac{\alpha}{E} \right)$$

on the interval  $\alpha E_0$  to  $E_0$ ; otherwise, S = 0.

#### GENERAL SCATTERING

Although precise knowledge of the slowing-down kernels for inelastic scattering and non-isotropic elastic scattering is not available, statements may be made (Chapter 1.2) concerning their approximate forms and, in particular, about the values of  $\xi$  for these processes. Aside from the procedure of substituting these kernel forms into Eq. (2) for numerical computations, the following approximation methods are available.

For a single element with a single process such as elastic scattering, the synthetic kernel method discussed under "Isotropic Elastic Scattering—General Solutions" may be applied.

For a single element with elastic and inelastic scattering, or for a mixture, the methods of "Isotropic Elastic Scattering-Mixtures" may be applied.

A different approximation, suggested by the inelastic scattering process, is to replace the correct kernel, g, by the form:

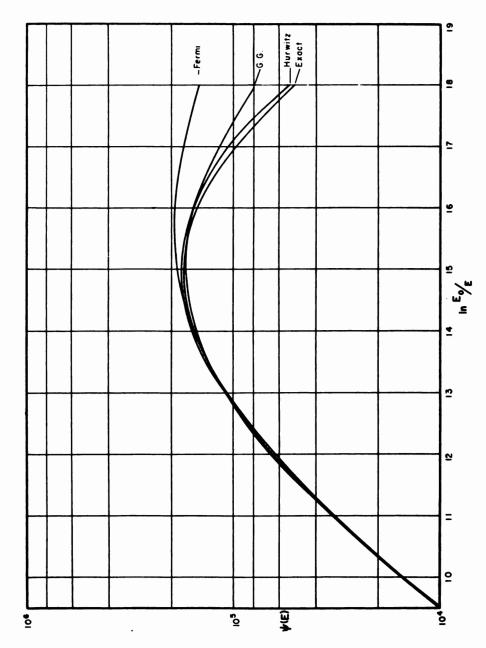


Fig. 1.3.1—Fermi, G. G., and Hurwitz, and Exact Solutions for  $\psi(E)$  for Slowing-down in Deuterium. Private communication from Bell and Goad, Los Alamos. The ratio of absorption to scattering cross sections  $(\sigma_a/\sigma_i)$  was taken equal to 0.001  $(E_\phi/E)^{1/2}$ .

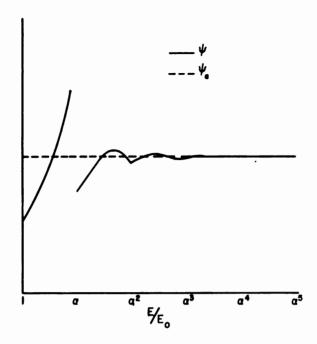


Fig. 1.3.2 — Exact  $\psi$  Versus Asymptotic  $\psi_a$  for a Point Source at E₀. Reprinted from Placzek, Phys. Rev. 69, (1946).

$$\mathbf{g}(\mathbf{E}',\mathbf{E}) = \sum_{i} \mathbf{a}_{i} \, \mathbf{5} \left[ \mathbf{E} - (\mathbf{E}' - \mathbf{E}_{i}) \right] \tag{14}$$

which assumes the scattering to result in discrete energy jumps,  $E_i$ , with probabilities,  $a_i$ . This approximation results in a simple numerical procedure on Eq. (2).

Combination treatments are also possible; for example, computations have been made using a three-delta function kernel for inelastic scattering, with elastic scattering handled in a conventional manner.

Another type of approximation uses a sum of separable terms,  $\Sigma_i U_i (E')v_i(E)$  for g(E',E).

## THERMAL DISTRIBUTIONS

In a non-capturing medium, neutrons which have been slowed down to thermal equilibrium acquire a Maxwellian velocity distribution (Table 1.3.7).

In a capturing medium, the absorption of neutrons leads to a "hardening" of their velocity distribution. This has been studied by Wigner and Wilkins for the case of atomic hydrogen with constant scattering cross-section and a 1/v absorber (Fig. 1.3.3). Cohen notes that the results of Wigner and Wilkins indicate an increase in the mean velocity of the neutrons by a factor of  $1 + 1.2 \sigma_a(kT)/\xi\sigma_s + \ldots$ , and this has been compared with experiment to some extent.

This hardening of the velocity spectrum may be reported by giving an effective neutron temperature such that a Maxwellian distribution at this new higher temperature would exhibit the correct average neutron velocity. In this sense, thermal neutron temperatures in reactors exceed moderator temperatures by the order of 50°C.

Quantity	Value or formula
Normalized velocity distribution = n(v)	$\frac{4}{\sqrt{\pi}} \left(\frac{M}{2kT}\right)^{3/2} v^2 e^{-\frac{Mv^2}{\alpha kT}}$
Most probable speed = $\alpha$	$\sqrt{\frac{2  \text{kT}}{\text{M}}}$
Normalized energy distribution = n(E)	$\frac{2}{\sqrt{\pi}} (kT)^{-\frac{3}{2}} E^{\frac{1}{2}} e^{-E/kT}$
Most probable energy	$\frac{1}{2}$ kT
Energy at which the flux n(E)v(E) is a maximum	kT
Average speed = $\overline{\mathbf{v}}$	$1.128 \ \alpha = \frac{2}{\sqrt{\pi}} \ \alpha$
Root mean square speed = c	$1.225 \alpha = \sqrt{\frac{3}{2}} \alpha$
Average energy	3 / ₂ kT = 1 / ₂ M c ²
Fraction of particles having speed above v	$\frac{2}{\sqrt{\pi}} \left( x e^{-x^2} + \int_x^{\infty} e^{-x^2} dx \right) \text{ where } x = v/\alpha$
$\overline{\overline{\sigma}}$ for $\sigma = 1$ $\sigma = 1/v$ $\sigma = 1/v^2$ $\sigma = 1/v^n$	$ \begin{array}{c} 1 \\ 1/\overline{v} \\ 1/\alpha^2 \\ \frac{1}{\alpha^n} \Gamma\left(2 - \frac{n}{2}\right) \end{array} $

Table 1.3.7 - Maxwellian Distributions and Averages

The average velocity  $\overline{\mathbf{v}}$  of the distribution comes up in connection with effective neutron cross-section values:

$$\bar{\bar{\sigma}} = \frac{\int \sigma n v dE}{\int n v dE}$$
 (15)

For a 1/v absorber (i.e.,  $\sigma = b/v$ ), one obtains  $\overline{\overline{\sigma}} = b/\overline{v}$  regardless of the distribution function, n. Averages of other functions over a Maxwellian are given in Table 1.3.7.

# ONE-VELOCITY THEORY (Felix Adler)

# INFINITE HOMOGENEOUS REGION

# SPECIAL FORMS OF THE BOLTZMANN EQUATION

Integro-differential Formulation

In this discussion, it is assumed that the neutrons diffuse without changing their energy,

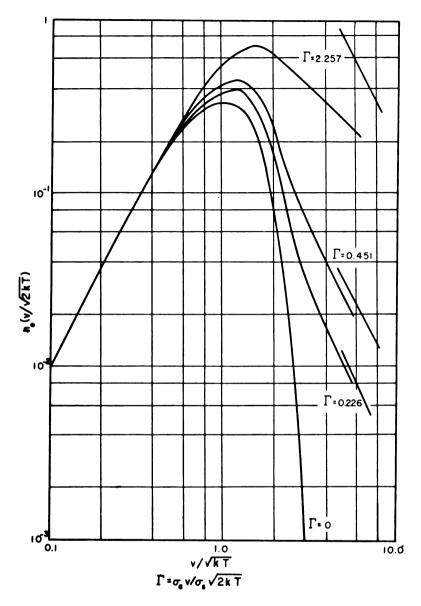


Fig. 1.3.3 — Absorption Hardening in Hydrogen Gas According to Wigner and Wilkins. Reprinted from AECD-2275.

i.e., the kernel of the Boltzmann equation reduces to:

$$\delta(\mathbf{v} - \mathbf{v}') \ \sigma_{S}(\mathbf{v}, \Omega, \Omega')$$

In an isotropic medium,  $\sigma_S(v, \underline{\Omega}, \underline{\Omega}')$  depends only on the angle between the directions of the incident and the scattered neutron and is independent of the azimuth of scattering:

$$\sigma_{\mathbf{S}}(\mathbf{v},\underline{\Omega},\underline{\Omega}') = \sigma_{\mathbf{S}}(\mathbf{v},\mu_{0}) = \sum \frac{2l+1}{2}\sigma_{\mathbf{S}l}(\mathbf{v})P_{l}(\mu_{0})$$
(16)

where:

$$\mu_0 = \Omega \cdot \Omega'$$

and:

$$\sigma_{S1}(v) = \int_{-1}^{+1} \alpha_{S}(v, \mu_{0}) P_{1}(\mu_{0}) d\mu_{0}$$

The cross section for scattering, without energy loss, a neutron of speed v from the direction  $\Omega'$  into the solid angle  $d\Omega$  about the direction  $\Omega$  is  $\sigma_s(v,\Omega,\Omega')d\Omega$ .

The total scattering cross-section is  $\sigma_s = \sigma_{s_0}$ .

The Boltzmann equation is:

$$\frac{1}{\mathbf{v}}\frac{\partial \mathbf{F}}{\partial t} = -\operatorname{div}\underline{\Omega}\mathbf{F} - \sigma\mathbf{F}(\underline{\mathbf{r}},\underline{\Omega},t) + \int_{\Omega'}\mathbf{F}(\underline{\mathbf{r}},\underline{\Omega'},t)\sigma_{\mathbf{S}}d\underline{\Omega'} + \mathbf{S}(\underline{\mathbf{r}},\underline{\Omega},t)$$
(17)

Many results have been derived for the special case where:

$$\mathbf{F}(\mathbf{r}, \mathbf{\Omega}) = \mathbf{F}(\mathbf{z}, \boldsymbol{\mu})$$

i.e., slab geometry.

From the expansion of  $\sigma_S$  and the addition theorem of Legendre functions, one finds for steady state:

$$\mu \frac{\partial \mathbf{F}(\mathbf{z}, \boldsymbol{\mu})}{\partial \mathbf{z}} + \sigma \mathbf{F}(\mathbf{z}, \boldsymbol{\mu}) = \frac{1}{2} \sum_{l} (2l + 1) \sigma_{Sl} \mathbf{P}_{l}(\boldsymbol{\mu}) \int_{-1}^{+1} \mathbf{P}_{l}(\boldsymbol{\mu}') \mathbf{F}(\mathbf{z}, \boldsymbol{\mu}') d\boldsymbol{\mu}' + \mathbf{S}(\mathbf{z}, \boldsymbol{\mu})$$
(18)

For isotropic scattering, Eq. (17) reduces to:

$$\frac{1}{v}\frac{\partial \mathbf{F}}{\partial t} + \mu \frac{\partial \mathbf{F}}{\partial z} + \sigma \mathbf{F} = \frac{1}{2}\sigma_{S_0} \int_{-1}^{+1} \mathbf{F}(\mathbf{z}, \mu', t) d\mu' + \mathbf{S}(\mathbf{z}, \mu, t)$$
(19)

Boltzmann's equation can also be written as an integral equation; the formulation as an integral equation is particularly useful in approximation methods, e.g., the iteration method, the end-point method, and the variational method. 10,11,12

The Integral Equation Formulation

The integral equation for the steady-state collision density  $\psi(\underline{r},\underline{\Omega})$  is based on the first collision probability density:

$$K(|\underline{r} - \underline{r}'|) = \frac{\sigma}{4\pi |\underline{r} - \underline{r}'|^2} e^{-\sigma} |\underline{r} - \underline{r}'|$$
 (20)

 $K(|\underline{r} - \underline{r}'|)$  is the probability for a neutron starting from  $\underline{r}'$  to suffer its first collision at  $\underline{r}$ . For a distributed isotropic source,  $S(\underline{r}')$ , the number of neutrons per unit volume suffering their first collision at  $\underline{r}$  is:

$$\psi_1(\mathbf{r}) = \iiint d\mathbf{r}' S(\mathbf{r}') K(|\mathbf{r} - \mathbf{r}'|)$$
 (21)

All collisions can be treated as first collisions by assuming that a neutron suffering any type of collision is absorbed and that (1 + f) new neutrons appear at the same point; i.e., for a scattering collision, f = 0; for real capture, f = -1; and for fission,  $f = \nu - 1$ . In this



picture, an additional source of neutrons appears in each element of volume, viz.,  $(1 + f)\psi_1(r)$ .

Capture, scattering, and fission collisions can all occur at the same point; the number of new neutrons appearing is therefore:

$$1 + f(\underline{\mathbf{r}}) = \frac{\sigma_{\mathbf{S}}(\underline{\mathbf{r}}) + \nu \sigma_{\mathbf{f}}(\underline{\mathbf{r}})}{\sigma(\mathbf{r})}$$
 (22)

with:

$$\sigma = \sigma_s + \sigma_c + \sigma_f$$

For inhomogeneous media,  $f(\underline{r})$  depends on position, e.g., is different in core and tamper of a reactor. In this picture,  $\psi_1(r)$  is the collision density, and:

$$\psi(\mathbf{r}) = \iiint d\mathbf{r}' \mathbf{K}(|\mathbf{r} - \mathbf{r}'|)[\mathbf{S}(\mathbf{r}') + \{1 + \mathbf{f}(\mathbf{r}')\}\psi(\mathbf{r}')]$$
(23)

Equation (23) can be generalized to include time-dependent neutron distributions; the number of first collisions occurring at time (t) at a distance (s) from the source depends on the source strength at a time (t - s/v):

$$\psi(\mathbf{r},t) = \iiint d\mathbf{r}' \mathbf{K} (|\mathbf{r} - \mathbf{r}'|) [\mathbf{S}(\mathbf{r}',t') + \{1 + \mathbf{f}(\mathbf{r}')\} \psi(\mathbf{r}',t')]$$
(24)

where:

$$t' = t - |\mathbf{r} - \mathbf{r}'|/v$$

If:

$$\psi(\mathbf{r},t) = \psi(\mathbf{r}) e^{\alpha t}$$

and:

$$S(r,t) = S(r) e^{\alpha t}$$

Eq. (24) reduces to Eq. (23) with the  $\sigma$  in the kernel replaced by  $\sigma + \alpha/v$ .

When S, f, and  $\psi$  in Eq. (23) are either functions only of z (slab symmetry) or of r (spherical symmetry), similar one-variable integral equations result:

$$\psi(\mathbf{z}) = \int_{-\infty}^{+\infty} d\mathbf{z}' \mathbf{K}_{\mathbf{p}|} (|\mathbf{z} - \mathbf{z}'|) [\mathbf{S}(\mathbf{z}') + \{1 + \mathbf{f}(\mathbf{z}')\} \psi(\mathbf{z}')]$$
(25)

$$\mathbf{r}\psi(\mathbf{r}) = \int_{-\infty}^{+\infty} \mathbf{dr'} \mathbf{K}_{\mathbf{pl}}(|\mathbf{r} - \mathbf{r'}|) \mathbf{r'}[\mathbf{S}(\mathbf{r'}) + \{1 + \mathbf{f}(\mathbf{r'})\}\psi(\mathbf{r'})]$$
 (26)

where:

$$\mathbf{K}_{\mathbf{p}\mathbf{l}}(|\rho|) = \int_{|\rho|}^{\infty} \mathbf{d}\mathbf{r} [2\pi \mathbf{r} \mathbf{K}(|\mathbf{r}|)] \tag{27}$$

is the normalized plane kernel (i.e.,  $\int_{-\infty}^{+\infty} d\rho K_{pl}(|\rho|) = 1$ ). Table 1.3.8 contains the explicit transport kernel Eq. (27). The negative values of r' encountered in Eq. (26) require one to define S(r'), f(r'), and N(r') as even functions of r'.

Integral equations of the Milne type (transport kernels) for semi-infinite or infinite media are often solved by means of Fourier transforms and the use of the convolution theorem for

Geometry	Notation	Normalization	Kernels
Point source	$\mathbf{K}( \underline{\mathbf{r}}-\underline{\mathbf{r}}' )$	$\int_0^\infty 4\pi R^2 K(R) dR = 1$	$\frac{\sigma e^{-\sigma \underline{r}-\underline{r}' }}{4\pi( \underline{r}-\underline{r}' )^2}$
Plane source	$\mathbf{K_{pl}}( \mathbf{z} - \mathbf{z}' )$	$\int_{-\infty}^{\infty} K_{\rm Pl} ( z ) dz = 1$	$\frac{\sigma}{2}  \mathbf{E_1}(\sigma   \mathbf{z} - \mathbf{z}' )$
			$\mathbf{E}_{1}(\mathbf{z}) = \int_{\mathbf{z}}^{\mathbf{w}} \frac{\mathbf{e}^{-\mathbf{t}}}{\mathbf{t}}  \mathbf{dt}$
Line source	K ₁ (s)	$\int_0^\infty 2\pi s K_1(s) ds = 1$	$\frac{\sigma^2}{2\pi} \int_1^\infty K_0(\sigma st) dt$
			s = ⊥ distance from line source
Cylindrical shell source at r'	<b>K</b> _c ( <b>r</b> , <b>r</b> ')	$\int_0^\infty 2\pi r K_c(r,r')dr = 1$	$\frac{\sigma^2}{2\pi} \begin{cases} \int_1^{\infty} K_0(\sigma rt) I_0(\sigma r't) dt, \ r > r' \\ \int_1^{\infty} K_0(\sigma r't) I_0(\sigma rt) dt, \ r < r' \end{cases}$

Table 1.3.8 — Transport Kernels

Fourier transforms. Let  $F\{g(x)\}$  be the Fourier transform of g(x), then one obtains for an infinite medium:

$$\mathbf{F}\{\psi(\mathbf{z})\} = \mathbf{F}\{\Im(\mathbf{z})\} \quad \frac{\left[\tanh^{-1}(\kappa/\sigma)\right]/(\kappa/\sigma)}{1 - \frac{(1+f)\tanh^{-1}(\kappa/\sigma)}{(\kappa/\sigma)}} \tag{28}$$

If the scattering is anisotropic in the laboratory system and the cross section is expanded as a series of Legendre functions, an integral equation formulation conveniently solved numerically by iteration is still possible.¹³ A trial function, e.g., a quadratic, is iterated according to Eq. (23), and the moments calculated from the iterated trial function are matched.

# Variational Formulation

In the steady state when S=0, the integral equation of transport theory, Eq. (23), can also be formulated as a variational principle for the eigenvalue,  $\lambda$ ;  $\delta\lambda=0$  where:

$$\lambda = \frac{\iiint d\mathbf{r} \iiint d\mathbf{r}' \psi(\mathbf{r}) \tau(\mathbf{r}) \mathbf{K}(|\mathbf{r} - \mathbf{r}'|) \tau(\mathbf{r}') \psi(\mathbf{r}')}{\iiint d\mathbf{r} \psi^{2}(\mathbf{r}) \tau(\mathbf{r})}$$
(29)

and:

$$\tau(\mathbf{r}) = 1 + \mathbf{f}(\mathbf{r})$$

The equivalence of Eq. (23) to  $\delta x = 0$  can be shown by the usual methods. For applications of Eq. (29) in general perturbation arguments, see Chapter 1.4.

The advantage of the variational method is that very simple trial functions give good results for  $\lambda$ .

For example, if  $\tau(\underline{r})$  is constant in a sphere and zero outside, a parabolic trial function  $\psi(r) = 1 - Cr^2$ , where C is chosen to make  $\lambda$  an extremum, is often sufficient.

Sometimes (e.g., in lattice problems) it is possible to approximate  $\psi(\mathbf{r})$  by assuming that it is piecewise constant in appropriately chosen regions (e.g., fuel or moderator).

The variational method has been very successful in problems involving complicated geometries and kernels. It can also be extended to inhomogeneous integral equations. ¹⁴ In this case, the variation does not always lead to a true minimum but sometimes to a saddle point.*

## THE DIFFUSION APPROXIMATION

## Expansion In Spherical Harmonics

The Boltzmann equation can frequently be approximated by expansions in spherical harmonics, e.g., for anisotropic scattering, in two media problems where the media have different total mean free paths and in many cases where boundaries are not plane. 16,17 Results and special formulae are discussed later under "Homogeneous Regions in Contact." One can obtain the elementary diffusion approximation from Eq. (18) by expanding the flux and source distributions in Legendre Polynomials:

$$S(z,\mu) = \frac{1}{2} \sum_{l} (2l + 1) S_{l}(z) P_{l}(\mu)$$
 (30)

$$\mathbf{F}(\mathbf{z},\mu) = \frac{1}{2} \sum_{l} (2l+1) \mathbf{F}_{l}(\mathbf{z}) \mathbf{P}_{l}(\mu)$$
 (31)

and by using the orthogonality properties of the Legendre Polynomials:

$$\frac{1+1}{2l+1}\frac{d\mathbf{F}_{l+1}}{dz} + \frac{1}{2l+1}\frac{d\mathbf{F}_{l-1}}{dz} + \sigma\mathbf{F}_{l} = \sigma_{sl}\mathbf{F}_{l} + \mathbf{S}_{l}$$
(32)

In principle, Eq. (32) constitutes an infinite system of ordinary linear differential equations. In the spherical harmonics method, the system is cut off after a certain harmonic n, and the remaining finite system of equations is solved for  $F_1(z)$ . This is called the  $P_n$ -approximation. Thus, the Boltzmann equation, i.e., an integro-differential equation, is replaced by a system of ordinary linear differential equations. This reduction is also possible when the cross sections depend on position.

## The P₁-Approximation

The first and simplest approximation is the ordinary diffusion approximation, where the expansion of  $F(z,\mu)$  is broken off after the second term, i.e., it is assumed that  $F(z,\mu)$  is almost isotropic and S is isotropic.

This approximation is valid if the following conditions are satisfied:

- (1) Sources are far away, i.e., several mean free paths from the region considered.
- (2) Boundaries of the medium are several mean free paths away from the region considered.
  - (3) The probability of capture is small compared to the probability of scattering. From Eq. (32), one obtains with  $\sigma_a = \sigma_c + \sigma_f =$  the total absorption cross section:

$$\frac{d\mathbf{F}_{1}}{d\mathbf{z}} + \sigma_{\mathbf{a}}\varphi = \mathbf{S}_{0}$$

$$\mathbf{F}_{1} = -\frac{1}{3(\sigma - \sigma_{\mathbf{a}})} \frac{d\varphi}{d\mathbf{z}} \equiv -\frac{\mathbf{l}^{\mathbf{tr}}}{3} \frac{d\varphi}{d\mathbf{z}}$$
(33)

^{*} For the exact conditions, compare Davison. 15

where:

$$\varphi = \mathbf{F_0} = \mathbf{n}\mathbf{v} \tag{34}$$

By definition,  $F_1$  is the net neutron current. An alternative expression for the neutron current can be found by computing the number of neutrons per second passing through an element of surface dS perpendicular to the z axis from above the xy plane, using the transport kernel [cf. Eq. (20)]:

$$\mathbf{J}_{+}d\mathbf{S} = d\mathbf{S} \int_{0}^{\infty} d\mathbf{r} \int_{0}^{2\pi} d\psi \int_{0}^{\pi/2} d\theta \, \phi(\underline{\mathbf{r}}) \sigma_{\mathbf{S}} \, \frac{e^{-\sigma \mathbf{r}} \cos\theta \sin\theta}{4\pi}$$
 (35)

where  $e^{-r\sigma}$  is the probability that neutrons leaving  $d\underline{r}$  in the direction to dS are not lost on the way and  $\phi(\underline{r})\sigma_{S}\cos\theta \ dS/4\pi\underline{r}^{2}\ d\underline{r}$  is the number of neutrons being scattered in the appropriate direction at r.

Expanding the flux in a Taylor series one obtains for  $o_a \ll \sigma_g$ :

$$\mathbf{J}_{\pm} = \left[ \frac{1}{4} \phi \pm \frac{\mathbf{l}^{\mathrm{tr}}}{6} \frac{\partial \phi}{\partial \mathbf{z}} + \dots \right]_{\mathbf{z}=0} + \dots$$
 (36)

for the number of neutrons passing into the lower (+) or upper (-) regions, and for the net current into the upper region:

$$\mathbf{J} = \mathbf{J}_{-} - \mathbf{J}_{+} = \frac{\mathbf{1}^{\mathrm{tr}}}{\mathbf{3}} \left. \frac{\partial \phi}{\partial \mathbf{z}} \right|_{\mathbf{z}=0} + \dots \tag{37}$$

after making the transport correction of replacing the scattering length by the transport length ltr.

The three dimensional forms* of Eq. (33) are:

$$\underline{J}(\underline{r}) = -\frac{1^{tr}}{3} \operatorname{grad} \varphi(\underline{r})$$
 (38)

$$\operatorname{div} J(\mathbf{r}) + \sigma_{\mathbf{a}} \varphi(\mathbf{r}) = S_0(\mathbf{r})$$

The first equation is a statement of Fick's law, viz., that the neutron current is proportional to the gradient of the flux density and through it the diffusion coefficient is defined as:

$$D \equiv l^{tr}/3 \tag{39}$$

The second equation is simply a statement of the continuity equation for the steady state. The transport mean free path is defined as:

$$1^{tr} = 1/[\sigma - \sigma_{s1}] \tag{40}$$

for weakly absorbing media:

$$1^{tr} = 1_{s}/[1 - \bar{\mu}_{0}] \tag{41}$$

^{*}Eq. (38) can be derived  16  from Eq. (17) by taking moments with respect to  $\underline{\Omega}$  and making diffusion theory assumptions.



Useful Formulations of the Diffusion Equation

For a multiplying medium the source density in Eq. (38) is:

$$S_0(\mathbf{r}) = S^{\text{ext}}(\mathbf{r}) + \nu \sigma_f \phi(\mathbf{r}) \tag{42}$$

For calculations using the elementary one-group diffusion theory, Eq. (38) is most conveniently formulated as:

$$\nabla^2 \phi(\mathbf{r}) + \mathbf{L}_{\mathbf{m}}^{-2} \phi(\mathbf{r}) + (3/1^{tr}) S^{\text{ext}} = 0$$
 (43)

where:

$$L_{m}^{-2} = 3 \sigma_{a}(k-1)/l^{tr}$$
 (44)

and k, the so-called one-group multiplication constant, is defined as:

 $k \equiv \nu \sigma_f / \sigma_a$ 

The solutions of problems of neutrons in a single medium have been reported in systematic form by Wallace and Le Caine. 17

For solving elementary diffusion theory problems by an integral, Eq. (38) is written as:

$$\eta^{-1}\nabla^2\psi(\mathbf{r}) - \psi(\mathbf{r}) + \mathbf{S}^{\mathbf{ext}}(\mathbf{r}) + \{1 + \mathbf{f}(\mathbf{r})\}\psi(\mathbf{r}) = 0$$
(45)

where  $\psi$  is the collision density, and:

$$\eta^2 \equiv 3\sigma/i^{tr} \tag{46}$$

For generalizations to multigroup and age theory, Eq. (38) is written as an obvious continuity equation:

$$(\mathbf{l}^{tr}/3)\nabla^{2}\phi(\underline{\mathbf{r}}) - \sigma_{a}\phi(\underline{\mathbf{r}}) + \mathbf{S}^{ext}(\underline{\mathbf{r}}) + \nu\sigma_{f}\phi(\underline{\mathbf{r}}) = 0$$
(47)

Integral Equations of Diffusion Theory

By the use of Green's theorem, Eq. (45) can be recast in the same form as the transport integral Eq. (23):

$$\psi(\underline{\mathbf{r}}) = \iiint d\underline{\mathbf{r}}' \mathbf{K}_{\mathbf{p}}^{\mathbf{D}}(\eta | \underline{\mathbf{r}} - \underline{\mathbf{r}}' |) [\mathbf{S}^{\mathbf{ext}}(\underline{\mathbf{r}}') + \{1 + \mathbf{f}(\underline{\mathbf{r}}')\} \psi(\underline{\mathbf{r}}')]$$
(48)

where  $K_p^D(\eta |\underline{r} - \underline{r}'|)$  is the solution of:

$$\eta^{-2}\nabla^{2}K_{p}^{D} - K_{p}^{D} + \frac{\delta(|\underline{r} - \underline{r}'|)}{4\pi|\underline{r} - \underline{r}'|^{2}} = 0$$
(49)

while in transport theory the kernel is given by Eq. (20). Alternatively, one can obtain from Eq. (47):

$$\mathbf{q}_{\mathbf{k}} \, \phi(\underline{\mathbf{r}}) = \iiint d\underline{\mathbf{r}}' \, \mathbf{K}_{\mathbf{p}}^{\mathbf{D}}(\kappa | \underline{\mathbf{r}} - \underline{\mathbf{r}}' |) [\mathbf{S}^{\mathbf{ext}}(\underline{\mathbf{r}}') + \nu \sigma_{\mathbf{f}} \, \phi(\underline{\mathbf{r}}')]$$
(50)

where:

$$\kappa^2 = 3\sigma_0 / l^{tr}$$
.

Equation (50) can be generalized to age and multigroup formulations of the fission source term.

In the general case, too, the relations (25) to (27) between kernels for different geometries hold.

Table 1.3.9 lists useful diffusion kernels.

Geometry Notation Normalization Kernels  $\int_0^\infty 4\pi \ R^2 K_p^D(\kappa R) dR = 1$ Point source  $\mathbf{K}_{\mathbf{p}}^{\mathbf{D}}(\kappa | \mathbf{r} - \mathbf{r}' |)$  $\frac{\kappa^2 e^{-\kappa |\underline{r}-\underline{r}'|}}{4\pi |\underline{r}-\underline{r}'|}$  $\mathbf{K}_{\mathrm{pl}}^{\mathrm{D}}(\kappa|\mathbf{z}-\mathbf{z}'|)$   $\int_{-\infty}^{+\infty} \mathbf{K}_{\mathrm{pl}}^{\mathrm{D}}(\kappa|\mathbf{z}|)d\mathbf{z} = 1$ Plane source ke-k|z-z'|  $\int_0^\infty 2\pi s \ \mathbf{K}_1^{\mathrm{D}}(\kappa s) \mathrm{d}s = 1$  $\frac{\kappa^2}{2\pi} \mathbb{K}_0(\kappa_B)$ Line source  $\mathbf{K}_{1}^{\mathrm{D}}(\kappa\mathbf{s})$  $s = \bot$  distance from line source  $\int_0^\infty 2\pi r \, \mathbf{K}_c^D(\kappa \, \mathbf{r}, \, \kappa \, \mathbf{r}') d\mathbf{r} = 1$ Cylindrical  $\mathbf{K}_{c}^{\mathrm{D}}(\kappa \, \mathbf{r}, \, \kappa \mathbf{r}')$  $K_0(\kappa r) I_0(\kappa r'), r > r'$   $K_0(\kappa r') I_0(\kappa r), r < r'$ shell source at r'

Table 1.3.9 — Diffusion Kernels

## Variational Formulation

Elementary diffusion theory for  $S^{\text{ext}} = 0$  can also be formulated in terms of a variational principle; in exact analogy with Eq. (29), we obtain that  $\lambda$  should be minimized:

$$\lambda = \frac{\iiint d\underline{\mathbf{r}}' \iiint d\underline{\mathbf{r}} \ \psi(\underline{\mathbf{r}})\tau(\underline{\mathbf{r}})K_{\mathbf{p}}^{\mathbf{D}}(\eta|\underline{\mathbf{r}} - \underline{\mathbf{r}}'|)\tau(\underline{\mathbf{r}}')\psi(\underline{\mathbf{r}}')}{\iiint d\mathbf{r} \ \psi^{2}(\mathbf{r})\tau(\mathbf{r})}$$
(51)

One-group Boltzmann and diffusion equations are self-adjoint. The generalization of Eq. (51) to non-self-adjoint problems, and the role of the adjoint are discussed in Chapter 1.4.

Time-dependent Diffusion Theory

If the neutron density is time dependent, the equation of neutron conservation is:

$$\frac{1}{v} \frac{\theta \phi(\underline{r},t)}{\partial t} = \frac{1}{3} \nabla^2 \phi(\underline{r},t) - \sigma_a \phi(\underline{r},t) + S(\underline{r},t)$$
 (52)

The time-dependent equation is solved, for example, by a Fourier-transform in the space coordinates and either a Fourier (steady state) or a Laplace transform (transients) in time.

An integral equation, analogous to Eq. (50) is obtained from Eq. (52) by use of the time dependent Green's function in the form:



$$\sigma_{\mathbf{a}}\phi(\underline{\mathbf{r}},t) = \iiint d\underline{\mathbf{r}}'dt'\kappa^{2}D \frac{e^{-\left[\frac{|\underline{\mathbf{r}}-\underline{\mathbf{r}}'|^{2}}{4D(t-t')}+\kappa^{2}D(t-t')\right]}}{\left[4\pi D(t-t')\right]^{\frac{3}{2}}} S(\underline{\mathbf{r}}',t')$$
(53)

It is interesting to compare the retardation time ( $t_{ret} = x/v$ ) entering in the integral equation and the "diffusion time" ( $t_{dif} = x^2/2D$ ) at which the neutron intensity at x reaches its maximum:

$$\frac{t_{\mathbf{ret}}}{t_{\mathbf{dif}}} = \frac{2}{3} \frac{1^{\mathbf{tr}}}{\mathbf{x}}$$

At distances  $r \gg F^r$  from the source, the retardation time is negligible compared to the diffusion time. Since most experiments involve the neutron distribution far from the source, it is usually permissible to ignore the retardation and to describe the time-dependent diffusion equation by means of an equation linear in  $\vartheta/\vartheta t$ .

However, if retardation effects are to be considered, a new derivation of the basic diffusion equation and of Fick's law is necessary.

Proceeding as before, the result is that the neutron current is no longer proportional to the gradient of the flux but to a linear combination of time rate of change of current and gradient of flux.

Therefore the time-dependent diffusion equation will here contain  $\partial^2/\partial t^2$ , i.e., it is a telegrapher's equation:

$$\frac{1}{\sigma v^2} \frac{\partial^2 \mathbf{F}_0(\underline{\mathbf{r}}, t)}{\partial t^2} + \left[ 1 + \frac{\sigma_a}{\sigma} \right] \frac{1}{v} \frac{\partial \mathbf{F}_0(\underline{\mathbf{r}}, t)}{\partial t} = \frac{1}{3\sigma} \nabla^2 \mathbf{F}_0(\underline{\mathbf{r}}, t) - \sigma_a \mathbf{F}_0(\underline{\mathbf{r}}, t) + \mathbf{S}(\underline{\mathbf{r}}, t)$$
(54)

The solutions of Eq. (54) possess a well-defined wave front, followed by a long tail of disturbance owing to the term linear in  $\partial/\partial t$ . The existence of the wave front is obvious; a neutron traveling with speed v requires at least a time r/v to reach a point at a distance r from the source. As r increases, the probability of a neutron reaching r without a collision becomes smaller and smaller.

Validity of the P₁-Approximation

The generalized Fick's Law:

$$\mathbf{J}(\mathbf{z}) = -\mathbf{\dot{\mathbf{f}}}^{\mathrm{r}} \frac{\mathrm{d}}{\mathrm{d}\mathbf{z}} \left[ \overline{\mu^{2}} \mathbf{F}_{0}(\mathbf{z}) \right]$$
 (55)

where:

$$\overline{\mu^2} = \int_{-1}^{+1} d\mu \mu^2 F(z,\mu) / F_0(z) = \frac{1}{3} + \frac{2}{3} [F_2(z) / F_0(z)]$$
 (56)

can be derived from Eq. (18) without any restrictive assumption whatsoever. Therefore, elementary diffusion theory is valid if  $\mu^2$  is independent of position.

Thus, if  $F_2(z)/F_0(z)$  is independent of position, elementary diffusion theory is rigorously correct; the spatial variations of  $F_2(z)/F_0(z)$  give a rough measure for the error involved in using elementary diffusion theory near a source or a boundary.

Numerical comparison of diffusion theory and exact results as well as prescriptions to extend the range of validity of results obtained from elementary diffusion theory are given in the following.

## SOLUTIONS OF TRANSPORT AND DIFFUSION PROBLEMS IN INFINITE MEDIA

Exact Solutions for the Transport Equation

Isotropic Scattering ( $\sigma = v = 1$ )

The exact solutions of the transport Eq. (26) are characterized by a parameter  $\kappa$ , defined by:

$$\frac{\tan^{-1}\kappa}{\kappa} = \frac{1}{1+f} \quad (f>0) \tag{57}$$

$$\frac{\tanh^{-1}\kappa}{\kappa} = \frac{1}{1+f} \qquad (f < 0)$$

For point sources, they have (in the asymptotic region) the form:

$$n^{as}(\mathbf{r}) = C_f \frac{e^{-\kappa \mathbf{r}}}{4\pi r} \qquad (f < 0) \tag{59}$$

$$n^{as}(\mathbf{r}) = \mathbf{A} \frac{e^{i\kappa \mathbf{r}}}{4\pi \mathbf{r}} + \mathbf{B} \frac{e^{-i\kappa \mathbf{r}}}{4\pi \mathbf{r}} \qquad (\mathbf{f} > 0)$$
 (60)

In non-multiplying media,  $\kappa$  is the decay or attenuation constant, and the diffusion length is defined as:

$$L = 1/\kappa\sigma \quad \text{(conventional units)} \tag{61}$$

In multiplying media,  $\kappa$  is essentially the inverse multiplication length,  $L_m$ .

For small f:

$$\kappa \approx \sqrt{3|f|} \sigma$$
 (conventional units) (62)

Exact solutions have been obtained for constant f < 0 by the Fourier transform methods for plane sources  $S(z) = \delta(z)$ , and point sources  $S(r) = \delta(r)/4\pi r^2$ , in the form:

$$n(\mathbf{r}) = C_f \frac{e^{-\kappa \mathbf{r}}}{4\pi \mathbf{r}} + \epsilon_g (\mathbf{r}) \frac{e^{-\mathbf{r}}}{4\pi \mathbf{r}^2}$$
 (63)

$$n(z) = C_f \frac{e^{-\kappa |z|}}{2\kappa} + \epsilon_{\rho 1}(|z|) \frac{E_1(|z|)}{2}$$
(64)

The first term represents the asymptotic solution. The non-asymptotic part of  $\psi(\mathbf{r})$  is the product of the transport kernel  $e^{-\mathbf{r}}/4\pi r^2$  weighted by  $\epsilon_8(\mathbf{r})$ , i.e., the number of neutrons having suffered no collisions since leaving the source times  $\epsilon_8(\mathbf{r})$ . For small  $\mathbf{r}$ ,  $\epsilon_8(\mathbf{r}) \sim 1$ , and  $C_f$  is:

$$C_{f} = \frac{2\kappa^{2}(1-\kappa^{2})}{(1+f)(\kappa^{2}+f)}; f \neq 0$$
 (65)

 $C_f$  and  $1-\kappa$  are tabulated for representative values of f in Table 1.3.10. Figure 1.3.4 shows  $\epsilon_S(r)$  as a function of (r) for representative values of (f). It is worth noting that for r > 1,  $\epsilon_S$  and  $\epsilon_{pl}$  are virtually identical.

Table 1.3.10 — Characteristic Numbers for the Asymptotic Transport	Solution
--------------------------------------------------------------------	----------

(M.	Goldstein	et al,	AECD-1943)

f	1 – <b>κ*</b>	C _f *
0.0	1.00000	3.00000
1	0.47457	2.52237
<b>2</b>	.28959	2.05112
3	.17137	1.59003
4	.92668 (-1)	1.14595
5	.42496 (-1)	0.73190
6	.14376 (-1)	.37327
7	.25862 (-2)	.11620
8	.90878 ( <b>-4</b> )	.90940 (-2)
9	.41223 (-8)	.16489 (-5)
-1.0	.00000	.00000

^{*} The notation x(-n) means  $x(10)^{-n}$ 

Anisotropic Scattering (conventional units)

For slightly anisotropic scattering, where  $\sigma_8(\mu) = \sigma_{S0} + 3\sigma_{S1}\mu/2$  and  $\sigma_{S1} = \bar{\mu}_0\sigma_{S0}$ , the asymptotic solution of the Boltzmann equation can be found by using a trial solution:

$$\mathbf{F}(\mathbf{z},\mu) = \mathbf{C} \frac{\mathbf{A} + \overline{\mu}_0 \mu}{1 \pm (\kappa \mu/\sigma)} \, \mathbf{e}^{\pm \kappa \mathbf{z}} \tag{66}$$

Note that any separable solution:

$$\mathbf{F}(\mathbf{z}, \boldsymbol{\mu}) = \mathbf{f}(\mathbf{z})\mathbf{g}(\boldsymbol{\mu})$$

must have the form of Eq. (66).

The constants  $\kappa$  and A are determined by the condition that the Boltzmann equation is identically satisfied by terms containing  $\mu$  in the zeroth and first power:

$$(\sigma_{s0}/\kappa)\tanh^{-1}(\kappa/\sigma) = \frac{1 + 3\bar{\mu}_0(\sigma_{s0}\sigma_a/\kappa^2)}{1 + 3\bar{\mu}_0(\sigma_{s0}\sigma/\kappa^2)}$$

$$(67)$$

$$\mathbf{A} = \pm \left(\sigma_{s0} \overline{\mu}_{0} / \kappa\right) \frac{1 - (\sigma / \kappa) \tanh^{-1} (\kappa / \sigma)}{1 - (\sigma_{s0} / \kappa) \tanh^{-1} (\kappa / \sigma)}$$
(68)

This approach can be extended to arbitrary scattering law, provided  $F(z,\mu)$  can be factored into a product  $f(z)g(\mu)$ ;  $\overline{\mu^2}$  is then a constant, i.e., Fick's law holds [cf., Eq. (56)], and a diffusion type equation will be valid for  $F_0(z)$ .

For isotropic scattering,  $(\bar{\mu}_0 = 0)\kappa$  reduces to the value given previously, and:

$$\mathbf{F}(\mathbf{z},\mu) = \text{constant } \frac{e^{\pm \kappa \mathbf{z}}}{1 \pm (\kappa \, \mu/\sigma)} \tag{69}$$

so that:

$$\overline{\mu^2} = \sigma \; \sigma_{\!_{\bf a}}/\kappa^2$$

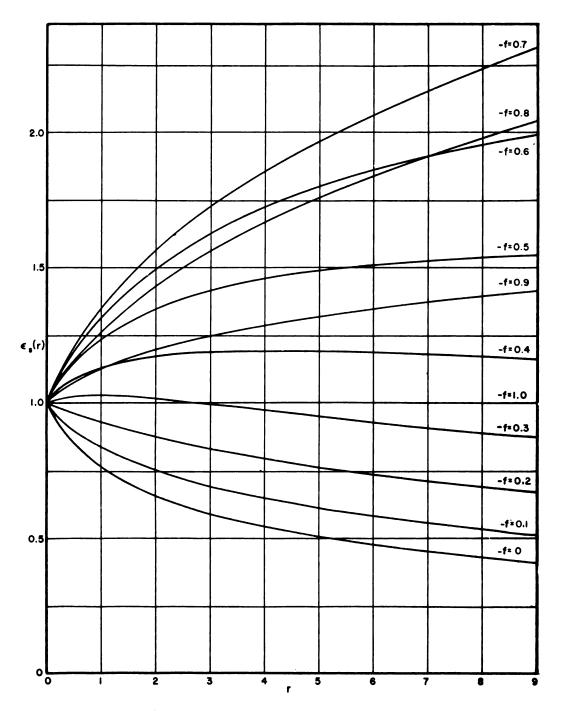


Fig. 1.3.4 — Coefficients of the Non-asymptotic Part of the Flux from a Point Source. From M. Goldstein et al, AECD-1943, LADC-506.

Applications of Results of Transport Theory in Diffusion Theory

Asymptotic Transport and Diffusion Flux

The correction to n^{as}(r) given in Eq. (63) is negligible for r larger than a few mean free paths.

nas (r) satisfies a diffusion-type equation for an anisotropic as well as isotropic scattering law. From an expression for the angular distribution in the asymptotic region, e.g., Eq. (69), one can prove that in the asymptotic region Fick's law is valid. Redefining D of Eq. (39) as:

$$D^* \equiv \sigma_{\mathbf{a}}/\kappa^2 \tag{70}$$

the equations for the asymptotic region become:

$$\underline{J}(\underline{r}) = -D^* \operatorname{grad} n^{28}(r)v \tag{71}$$

and:

$$-\nabla^{2}\mathbf{F}_{0}^{as}(\underline{\mathbf{r}}) + \kappa^{2}\mathbf{F}_{0}^{as}(\underline{\mathbf{r}}) = \frac{\kappa^{2}}{\sigma_{a}}\left[\mathbf{S}^{ext}(\underline{\mathbf{r}}) + \nu\sigma_{f}\mathbf{F}_{0}^{as}(\underline{\mathbf{r}})\right]$$
(72)

i.e.,  $\mathbf{F}_{0}^{\mathbf{as}}(\underline{\mathbf{r}})$  satisfies the basic equation of elementary diffusion theory for  $\phi(\underline{\mathbf{r}})$  given in Eq. (47).

The only effect of anisotropic scattering on the results contained in Eqs. (71) and (72) is to change the value of  $\kappa$ . ¹⁸

The validity of the diffusion equation (72) for the asymptotic flux  $F_0^{as}(\underline{r})$  is the basis for increasing the range of validity of results of elementary diffusion theory by applying suitable standard results of transport theory.

## Prescriptions

The following prescriptions are frequently useful to get better approximations:

- (1) Use the exact asymptotic equation (e.g., for strong absorption medium) by replacing diffusion coefficient D and diffusion length  $\sqrt{1^{tr}/3\sigma_a}$  of elementary diffusion theory by D* and L defined in Eqs. (70) and (61), respectively. If absorption is appreciable, use prescription (2).
- (2) Fictitious source: For strongly absorbing media, replace the actual source term in the diffusion equation by a fictitious source  $S^*(r)$ :

$$\mathbf{S}^*(\underline{\mathbf{r}}) = 2 \frac{\sigma_{\mathbf{a}}}{\sigma_{\mathbf{s}}} \frac{1 - (\kappa/\sigma)^2}{(\kappa/\sigma)^2 - (\sigma_{\mathbf{a}}/\sigma)} \mathbf{S}(\underline{\mathbf{r}})$$
 (73)

(3) Neutron density near a source: For a point source, replace  $\delta(\underline{r})$  by the first collision density of neutrons  $\psi_1 = \sigma e^{-\sigma r}/4\pi r^2$ , and write a diffusion equation for the density of neutrons having experienced one or more collisions, using  $\psi_1$  as a source.

If only prescription 1 is used and none of the others the asymptotic diffusion and transport solutions will differ by the constant factor given in Eq. (73). Actually, the distance from the source at which the diffusion theory solution becomes valid increases with increasing capture. For  $f \rightarrow -1$ , this distance tends to  $\infty$  and the diffusion-theory solution is to be replaced by the first-collision density.

## Time-dependent Diffusion Equation

For a source  $S(z,t) = \delta(z)e^{i\omega t}$ , the solution of the diffusion equation is a damped wave:

$$n(z,t) = \frac{1}{2D\sqrt{\kappa^2 + \frac{i\omega}{D}}} e^{-z} \sqrt{\frac{\rho^2 + \kappa^2}{2} + i\omega} \left( t - z \sqrt{\frac{\rho^2 - \kappa^2}{2}} \right)$$
 (74)

where:

$$\rho^2 = \sqrt{\kappa^4 + \left(\frac{\omega}{D}\right)^2}$$

For the initial-value problem, where F(z,t) at t=0 is prescribed as  $f_0(z)$  and where  $f_0(z) \neq 0$  in a limited region, the neutron flux appears instantaneously at all points in space and persists indefinitely; there is no wavefront or retardation.

The solution  $F_0^{\text{ret}}(z)$  for the generalized (telegrapher's) equation (54) in the same case contains terms  $e^{-\sigma vt/2}$  f(z ± vt/ $\sqrt{3}$ ) representing the waves traveling with a velocity v/ $\sqrt{3}$ .

The term representing the tail starts contributing at each point after the initial wavefront has reached it.

#### HOMOGENEOUS REGIONS IN CONTACT

#### **BOUNDARY CONDITIONS**

**Boundary Conditions in Transport Theory** 

The boundary condition for the Boltzmann equation is:  $F(x,\mu)$  must be continuous for all values of  $\mu$  at a plane interface between two media.

Let  $F^+(0,\mu)$  and  $F^-(0,\mu)$  denote the flux at the right and left of a boundary at z=0, then:

$$\mathbf{F}^{+}(\mathbf{0},\mu) = \mathbf{F}^{-}(\mathbf{0},\mu) \tag{75}$$

Using the spherical harmonic expansion, the boundary condition can be written as:

$$\mathbf{F}_{1}^{+}(0) = \mathbf{F}_{1}^{-}(0) \tag{76}$$

for all 1. Corresponding boundary conditions hold at curved interfaces.

 $F(x,\mu)$  does not have to be continuous if the boundary is itself a neutron source or absorber.

If one of the media, e.g., z < 0, is vacuum, the above boundary conditions are meaning-less. There are no collisions in the vacuum and no neutron flow from vacuum into the medium, unless sources to the left of (z = 0) are prescribed. A vacuum acts as a perfect (black) absorber and Eq. (75) is replaced by:

$$\mathbf{F}(\mathbf{0}, \boldsymbol{\mu}) = \mathbf{0} \tag{77}$$

for  $\mu > 0$  (vacuum for z < 0).

Boundary Conditions in Diffusion Theory

In elementary diffusion theory ( $P_1$  approximation),  $F_0(z)$  is a solution of a second-order differential obtained from Eq. (33). Both neutron flux,  $F_0$ , and current, J, given by Fick's law, must be continuous across an interface between two media.

For a boundary between a medium and vacuum, it is postulated that the net inward flow vanishes:



$$J_{-}(0) = \int_{0}^{1} \phi(0,\mu)\mu d\mu = 0$$
 (78)

Evaluating J_0 by means of Eq. (36) one obtains for a plane interface the extrapolation length  $\lambda^D$  of elementary diffusion theory:

$$\lambda^{D} \equiv \left[ \varphi(\mathbf{z}) / \left( \frac{\mathrm{d}\varphi}{\mathrm{d}\mathbf{z}} \right) \right]_{\mathbf{z}=0} = \frac{2}{3} \, l^{\mathrm{tr}} \tag{79}$$

 $\lambda^D$  is the distance beyond the boundary at which the extrapolated neutron flux would vanish according to elementary diffusion theory. In calculations,  $\lambda^D$  is usually replaced by the extrapolation length obtained from transport theory.*

Application of Transport Theory Results in Diffusion Theory ( $\sigma = 1$ )

For semiinfinite media (z > 0), the logarithmic derivative of  $F_0$  at the boundary, commonly called the extrapolation length  $(\lambda)$ , is defined by:

$$1/\lambda = \frac{\mathrm{d}}{\mathrm{d}z} \log \left. \mathbf{F}_0^{as}(z) \right|_{z=0} \tag{80}$$

Tables 1.3.11 and 1.3.12 give  $\lambda$  computed from transport theory.

For anisotropic scattering, the significant results are:

- (1) For a linear scattering law ( $\sigma_{S_2} = 0$ ) and no absorption, the emerging angular distribution, the extrapolation length measured in units of the transport mean free path, and  $F_0(0)$  are the same as for the isotropic case.
- (2) For a quadratic scattering law ( $\sigma_{S3} = 0$ ), the maximum variation in  $F_0(0)$  is about 1.3 percent, and the variation in  $\lambda$ , measured in units of the transport mean free path, is about 0.44 percent.

For spheres and cylinders of radius (a),  $\lambda$  is defined by:

$$\frac{1}{\lambda} = \frac{d}{dr} \log \left| \mathbf{F}_0^{aB}(\mathbf{r}) \right|_{\mathbf{r}=\mathbf{a}} \tag{81}$$

Graphs of  $\lambda$  for black spheres and cylinders imbedded in a non-absorbing medium are given in Figs. 1.3.6 and 1.3.7.

Curves II are the following approximations, good for a > 3:

$$\lambda_{\text{sphere}} = 0.7104 + 0.5047 \text{ a}^{-1} + 0.2336 \text{ a}^{-2} - 0.25 \text{ a}^{-3} \log \text{ a} - 0.1704 \text{ a}^{-3}$$
 (82)

$$\lambda_{\text{cylinder}} = 0.7104 + 0.2524 \, \text{a}^{-1} + 0.0949 \, \text{a}^{-2} - 0.078 \, \text{a}^{-3} \, \log \, \text{a} - 0.0256 \, \text{a}^{-3}$$
 (83)

Curves I are good only for very small a:

$$\lambda_{\text{sphere}} = \frac{4}{3} - \frac{5}{9} a + \dots \tag{84}$$

$$\lambda_{\text{cylinder}} = \frac{4}{3} - \left(1 - \frac{16}{3\pi^2}\right) \text{ a log a } -0.2164\text{a} + \dots$$
 (85)

^{*}Cf. below and Tables 1.3.11 and 1.3.12.

[†]In most reactor applications, this extrapolation length is but slightly different from the distance between the actual reactor boundary and the place where the analytic continuation of the interior, asymptotic solution vanishes.

Table 1.3.11 — Extrapolation Length and Related Results for Standard Cases with Plane Geometry (Milne's Problem)

(J. C. Mark, MT-26, May 1947; G. Placzek and W. Seidel, MT-5, June 1943; C. Mark, MT-50, April 1944)

Problem and restrictive assumptions	Extrapolation length, λ	Related results
No capture; scattering isotropic; normalization $J=-1$	$\sigma_{\lambda} = \mathbf{z_0} = 0.7104$	$F_0(0) = \sqrt{3}$ $F_0(z) = \sqrt{3} \left\{ 1 - \frac{1}{2} z\sigma \log z\sigma + 1.2788 z\sigma + \frac{1}{16} (\sigma z)^2 \log^2 (z\sigma) - 0.3822 (\sigma z)^2 \log \sigma z + 0.7068 (z\sigma)^2 + 0 \left[ (\sigma z)^3 \log^3 \sigma z \right] \right\} $ (near surface)
No capture; quadratic scattering law	$\sigma_{tt} \lambda = z_0 \left[ 1 + 0.011 \left( \frac{\sigma_{12}}{\sigma_{10}} \right) + 0.001 \left( \frac{\sigma_{12}}{\sigma_{10}} \right)^2 \right]$	$F_0(0) = \sqrt{3} \left( 1 - 0.322 \frac{\sigma_{52}}{\sigma_{50}} \right)$
Capturing and multi- plying medium; linear scattering law: $\sigma_s(\mu_0) = \frac{\sigma_{s0}}{2} (1 + 3b\mu_0)$	See Table 1.3.12 for deviations from good approximation:* $z_0' \approx \frac{z_0}{1+f}$	$F_0^{as}(z) = \frac{1+f}{\kappa'} \sin \kappa' (z + z'_0)$ For $\kappa'$ , see Table 1.3.12

 $[\]mathbf{z}_0$  is the distance to the plane on which the asymptotic solution vanishes, in units of the scattering length

Table 1.3.12—Diffusion Length and Extrapolation Length for Milne's Problem for Anisotropic Scattering

(Davison¹⁹)

(x')2 1 + f $(1 + f)z_0'$ 0 1 - 3b-1 0.2 0.7843 - 1.2197b-0.99982 + 0.00350b.7300 - 0.1624b-.9714 + .1660b.4 .6 .7154 + .3305b-.8233 + .4009b.8 .7113 + .5757b-.5047 + .3902b1.0 .7104 + .7104b 1.2 .7106 + .7897b 0.6965 - 0.8201b.7117 + .8386b 1.4 1.5871 - 2.0921b.7130 + .8693b2.6732 - 3.8270b1.6 .7142 + .8881b1.8 3.9554 - 6.0305b.7152 + .8998b 2.0 5.4341 - 8.7063b2.2 .7162 + .9059b 7.1096 - 11.856b2.4 .7173 + .9084b8.9819 - 15.483b 2.6 .7184 + .9092b11.051 - 19.585b 2.8 .7194 + .9077b 13.318 - 24.166b.7203 + .9047b 3.0 15.781 - 29.224b

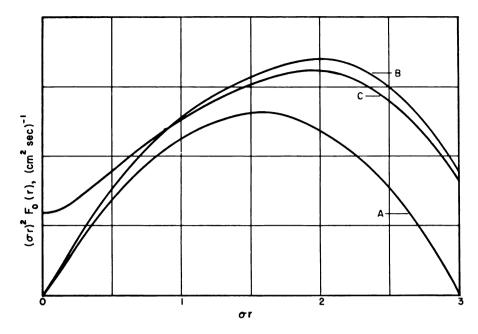


Fig. 1.3.5 — Flux from a Unit Source at the Center of a Non-absorbing Sphere of Radius Equal to Three Mean-free-paths. From R. E. Marshak, H. Brooks, And H. Hurwitz, Jr., Nucleonics, Vol. 4, No. 5, May 1949.

Curves III represent the probable shape of the dependence of  $\lambda(a)$ , indicated by spherical harmonics calculations. 19-25

The corresponding asymptotic solutions in the no-capture case as well as the plane boundary case are:

$$\mathbf{F_0^{as}(z)} = \left(\frac{d\mathbf{F_0^{as}}}{dz}\right)_{z=0} (z + \lambda) \qquad \text{(plane)}$$

$$rF_0^{as}(r) = F_0^{as}(\infty)\left(r - \frac{a^2}{a+\lambda}\right)$$
 (sphere) (87)

$$\mathbf{F_0^{as}(r)} = \left(\frac{d\mathbf{F_0^{as}}}{d\mathbf{r}}\right)_{\mathbf{a}} \left[\mathbf{a} \log \left(\mathbf{r/a}\right) + \lambda\right] \quad \text{(cylinder)}$$

A diffusion-equation solution satisfying the boundary condition equation (80) gives the same result as transport theory does a few mean free paths away from the free boundary, since  $F_0^{as}$  satisfies the diffusion equation (72).

In many cases adequate results can be obtained by use of simple diffusion theory together with the known (from transport theory) values of  $\lambda$  for the given geometry.

Explicit use of transport theory is necessary, for example, to calculate the true flux and current near a strong absorber or near a free boundary.

Figure 1.3.5 plots solutions of the diffusion equation for the case of a bare sphere with a unit source at the center and f=0,  $R\sigma=3$ . Curve A is the solution of the straightforward diffusion equation (boundary condition  $F_0(R)=0$ ). Curve B is obtained by using an extrapolation prescription, and Curve C is the result of using both prescription (3) as well as an extrapolation length.

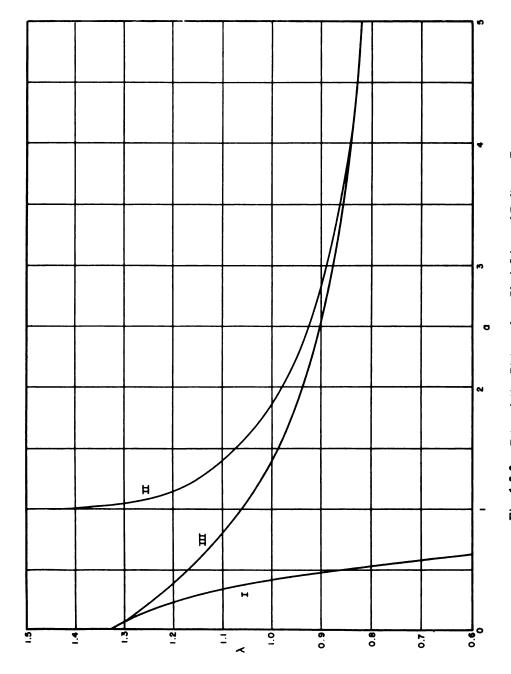


Fig. 1.3.6 — Extrapolation Distance for a Black Sphere of Radius a. From B. Davison and S. Kushneriuk, MT-214, Mar. 1946.

394

Digitized by Google

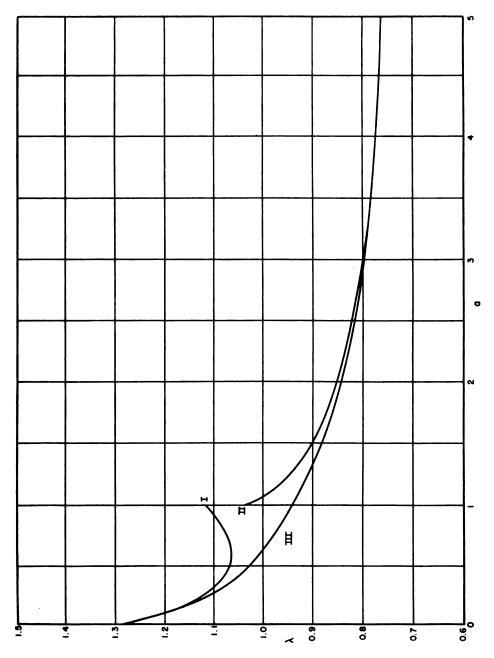


Fig. 1.3.7 — Extrapolation Distance for a Black Cylinder of Radius a. From B. Davison and S. Kushneriuk, MT-214, Mar. 1946.

In Fig. 1.3.8,  $F_0(z)$  and  $F_0^{as}(z)$  are shown for the no-capture case near a plane boundary to vacuum.

# SOLUTIONS OF DIFFUSION AND TRANSPORT PROBLEMS IN BOUNDED REGIONS

The methods of particular interest in criticality calculations, viz., the variational method, the perturbation method, the iteration method, and the Serber-Wilson method, are discussed in Chapter 1.4.

The spherical harmonics method and its modifications²⁶⁻²⁹ summarized below are useful both in flux and reactor criticality calculations. The  $P_1$ -approximation contains all the results of diffusion theory.

The Wiener-Hopf method and the related end-point method³⁰⁻³³ are useful in deriving the general results of transport theory.

# The Spherical-harmonics Method

The basic idea of this method is to approximate the Boltzmann integrodifferential equation by a system of ordinary differential equations.

For slab geometry, the solutions to the system of linear differential equations (32) without source for the total flux  $F_0$  and the higher angular moments are given in the  $P_{2n-1}$ -approximation for isotropic scattering by:

$$F_{1}(z) = \sum_{i=1}^{n} G_{1}(\nu_{i}) \left[ A_{i} e^{\nu_{i} z} + B_{i}(-1)^{1} e^{-\nu_{i} z} \right]$$

$$1 = 0, 1, \dots, 2n - 1$$
(89)

For spherical geometry, the differential equations are in the  $P_{2n-1}$ -approximation:

$$(1+1)\left(\frac{d}{dr} + \frac{1+2}{r}\right) \mathbf{F}_{1+1}(r) + 1\left(\frac{d}{dr} - \frac{1-1}{r}\right) \mathbf{F}_{1-1}(r) + (21+1)[\mathbf{F}_{1}(r) - \mathbf{S}_{1}(r)] - (1+f) \mathbf{F}_{0}(r) \delta_{10} = 0$$
 (90)

The solutions  $F_l(r)$  for  $S_l = 0$  are given by:

$$\mathbf{F}_{l}(\mathbf{r}) = \sum_{i=1}^{n} \mathbf{G}_{l}(\nu_{i})[\mathbf{A}_{i} \mathbf{H}_{l}(\nu_{i} \mathbf{r}) + (\leftarrow 1)^{l} \mathbf{B}_{i} \mathbf{H}_{l}(-\nu_{i} \mathbf{r})]$$
(91)

The functions  $G_1(\nu)$  are defined by the recursion formula:

$$lG_{l}(\nu) + \frac{2l-1}{\nu}G_{l-1}(\nu) + (l-1)G_{l-2}(\nu) = 0$$
(92)

and explicitly:

$$G_0 = 1$$

$$G_1 = f/\nu$$

$$G_2 = -\frac{1}{2\nu^2} (\nu^2 + 3f)$$
 (93)

$$G_3 = \frac{1}{6\nu^3} \left[ (5 - 4f)\nu^2 + 15f \right]$$



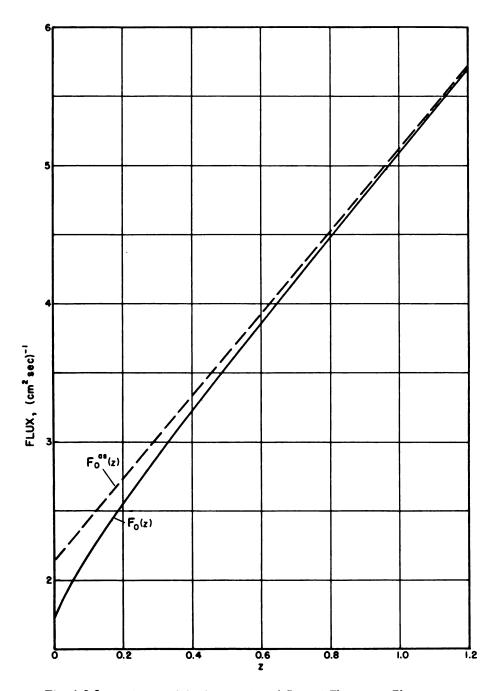


Fig. 1.3.8 — Behavior of the Asymptotic and Correct Flux near a Plane Boundary of a Semi-infinite Non-absorbing Medium. Data from C. Mark, Phys. Rev. 72, 1947.

The functions  $H_1$  are related to the Bessel functions of purely imaginary argument of the second kind  $(K_{1+1/2})$  by:

$$H_1(-x) = -\sqrt{\frac{2}{\pi x}} K_{1+\frac{1}{2}}(x)$$
 (94)

Numerical values for the  $\nu_{i}$  for use in the P₃-approximation are given in Table 1.3.13.

Table 1.3.13 —  $\nu_1$  and  $\nu_2$  for the P₃-approximation (Mark⁶³)

f	$^{\pm  u}_1$	±ν ₂
-0	0	1.972
-0.1	0.526	2.055
2	.712	2.146
3	.835	2.242
4	.923	2.341
5	.989	2.443
6	1.040	2.544
7	1.080	2.646
8	1.113	2.746
9	1.139	2.844
-1.0	1.161	2.941

The  $\nu_i$  for the  $P_{2n-1}$ -approximation are defined as roots of:

$$G_{2n}(\nu) = 0 \tag{95}$$

The smallest positive root of Eq. (95) is an approximation to  $\kappa$  defined by Eq. (58). In regions containing isotropic sources (S₀), the solutions for slab geometry are:

$$\mathbf{F}_{1}(\mathbf{z}) = (\mathbf{F}_{1}(\mathbf{z}))_{\text{no source}} + \mathbf{p}_{1}(\mathbf{z})$$
 (96)

where:

$$p_{1}(z) = \sum_{i=1}^{n} C_{i} G_{1}(\nu_{i}) [e^{\nu_{i}z} u(\nu_{i}, z) + (-1)^{i} e^{-\nu_{i}z} u(-\nu_{i}, z)]$$
(97)

The  $c_i$  depend only on the  $\nu_i$ ; for the  $P_3$ -approximation:

$$c_{1} = \frac{5(11\nu_{1}^{2} - 21)}{9(\nu_{1}^{2} - \nu_{2}^{2})}$$

$$c_{2} = \frac{5(11\nu_{2}^{2} - 21)}{9(\nu_{2}^{2} - \nu_{1}^{2})}$$
(98)

The  $u(\nu,z)$  are defined by:

$$u(\nu,z) \equiv \frac{1}{2\nu} \int^{z} S_{0}(t) e^{-\nu t} dt$$
 (99)

For spherical geometry, the solutions for the  $F_1(r)$  are:

$$\mathbf{F}_{1}(\mathbf{r}) = (\mathbf{F}_{1}(\mathbf{r}))_{\text{no source}} + \mathbf{p}_{1}(\mathbf{r})$$
(100)

where:

$$\mathbf{p}_{l}(\mathbf{r}) = \sum_{i=1}^{n} \mathbf{c}_{i} \mathbf{G}_{l}(\nu_{i}) [\mathbf{H}_{l}(\nu_{i}\mathbf{r})\mathbf{u}(\nu_{i},\mathbf{r}) + (-1)^{l} \mathbf{H}_{l}(-\nu_{i}\mathbf{r})\mathbf{u}(-\nu_{i},\mathbf{r})]$$
(101)

The  $c_i$  are defined by Eq. (98) and the  $u(\nu_i r)$  are defined by:

$$u(\nu,r) = \frac{1}{2} \int_{0}^{r} S_0(t) t e^{-\nu t} dt$$
 (102)

The arbitrary constants  $A_i$  and  $B_i$  occurring in Eqs. (89) and (91) are determined by the boundary conditions of Eq. (76).

For a semi-infinite medium only one exponentially increasing term is allowed, and  $A_i = 0$  for  $i = 2, 3, \ldots n$ .

At a free surface (z = a), the following alternative boundary conditions have been used:

(1) 
$$\int_0^1 \mathbf{F}(\mathbf{a},\mu)\mu^{2l+1} d\mu = 0, \ l = 0,1,\ldots, \ n-1$$
 (103)

- (2) The second medium is considered as a real pure absorber (f = -1);  $F(a, \mu)$  is computed in the second medium by the spherical harmonics method and boundary-condition equation (76) is applied.
- (3)  $F(a,\mu)$  is required to vanish for a sufficient number of different values of  $\mu_i$  to determine all constants. The values of  $\mu_i$  selected are the n negative roots of  $P_{2n}(\mu) = 0$ .

It has been shown by Davison that conditions (2) and (3) are exactly equivalent. If media of various "greyness" are to be compared, prescription (2) may present an advantage.

A generalized spherical harmonics method applicable in principle to any geometry has been developed by Mark by using expansions in general tensor harmonics. From these expansions, angular moments for cylindrical geometry are obtained.

In any geometry, the flux  $F_0$  satisfies in the  $P_{2n-1}$ -approximation the equation:

$$\prod_{i=1}^{n} (\nabla^2 - \nu_i^2) \mathbf{F_0}(\underline{\mathbf{r}}) = 0 \tag{104}$$

This equation factors and the constituent parts of  $F_0$  which give its spatial dependence are solutions of Helmholtz equations:

$$(\nabla^2 - \nu_i^2) f_i(\underline{r}) = 0 \tag{105}$$

It is worth noting that the form of the solutions  $f_i(\underline{r})$  depends on the geometry of the medium, but that the parameters  $\nu_i$  entering the arguments of the solutions are independent of the geometry. They depend only on the order of the approximation used and on the value of f; for any geometry, they are obtained from Eq. (95).

For slab and sphere geometries, only  $2n ext{ } F_l$ 's and  $2n ext{ } arbitrary ext{ } constants ext{ } occur ext{ } in the P_{2n-1}$ -approximation, whereas n(n+1) functions of (r) and n(n+1) arbitrary constants occur in cylinder geometry.

Odd order approximations have been used more frequently; for the use of even-order approximations, see Mark.²⁶

It has been suggested²⁵ that, in the determination of extrapolation lengths, the even-order approximations converge to the exact result from above and the odd-order approximations converge from below.

Numerical work has shown that, in general, the third-order approximation leads to definite improvements over the first-order approximation and that higher approximations usually lead to smaller corrections.

Modified Spherical-harmonics Method (Wick's Method)

The basic idea of this method is to approximate the integral:

$$\int_{-1}^{+1} d\mu \ \mathbf{F}(\mu, \mathbf{z})$$

occurring in the transport-theory equation by the use of an appropriate numerical integration formula. Wick chooses the Gauss integration formula:³⁴

$$\int_{-1}^{+1} d\mu \ \mathbf{F}(\mu, \mathbf{z}) = 2 \sum_{m=0}^{n} \mathbf{R}_{m} \mathbf{F}(\mathbf{z}, \mu_{m})$$
 (106)

where the  $\mu_m$  are defined as the (n + 1) roots of:

$$\mathbf{P}_{n+1}(\mu)=0$$

and the  $R_m$  are listed through n = 5 in reference (35).

For n = 1:

$$R_0 = R_1 = 1/2$$

Equation (19) reduces to a system of ordinary differential equations:

$$\mu_i \frac{d\mathbf{F}(\mathbf{z}, \mu_i)}{d\mathbf{z}} + \mathbf{F}(\mathbf{z}, \mu_i) = (1 + \mathbf{f}) \sum_{m=0}^{n} \mathbf{R}_m \mathbf{F}(\mathbf{z}, \mu_m)$$
 (107)

n being the order of approximation. The angular dependent solution of Eq. (107) is different from that given by the spherical harmonics method. In Wick's method:

$$\mathbf{F}(\mathbf{z},\mu) = \frac{1+\mathbf{f}}{2} \sum_{i=1}^{n+1} \frac{\mathbf{A}_i}{1+\nu_i \mu} e^{\nu_i \mathbf{z}}$$
 (108)

where the  $A_i$  are to be determined from the boundary conditions and, for n odd, the  $\nu_i$  are the roots of Eq. (95).

## The End-point Method

The mathematical technique used in the end-point method is to solve the integral equations of transport theory and the approximations to these equations by means of the Wiener-Hopf technique.

The basic idea of the Wiener-Hopf technique is to use the Laplace or Fourier transform of the neutron density. The transform of the neutron density can be expressed in terms of functions depending on f and the boundary conditions. It is frequently possible to determine the transforms by using Liouville's theorem and related arguments of the theory of complex variables. It is often very easy to derive simple results for the asymptotic neutron density and for the density near an interface by using the so-called Tauberian theorems.

The idea of the end-point method is to treat the behavior of the solution near each boundary as if no other boundaries existed. If the boundaries are far apart, the assumptions of the end-point method are certainly valid, and one-boundary Wiener-Hopf solutions for



different regions can be combined in such a way that the asymptotic components coincide. It has been shown³⁶ that the method gives reasonable results if the distance between boundaries is only a few tenths of a mean attenuation distance.

The end-point method is applicable in one-dimensional problems (slab and spherical geometries) and is used in treating multiregion transport problems.

## SPACE AND ENERGY VARIATIONS

(Eugene Greuling and Harry Soodak)

## FERMI AGE THEORY

## **AGING**

If the diffusion approximation is made on the leakage term, there results the continuity equation:

div D grad 
$$\varphi(\mathbf{r}, \mathbf{E}) - \sigma_{\mathbf{a}} \varphi(\mathbf{r}, \mathbf{E}) + \frac{\partial \mathbf{q}(\mathbf{r}, \mathbf{E})}{\partial \mathbf{E}} + \mathbf{S}(\mathbf{r}, \mathbf{E}) = 0$$
 (109)

with:

$$D = \frac{1}{3\sigma_{tr}} \tag{110}$$

Combining this with the result of the Fermi slowing-down approximation, Eqs. (10) and (13):

$$\mathbf{q} = \xi \sigma_{\mathbf{s}} \mathbf{E} \varphi \tag{111}$$

leads, in the case of space-independent cross sections, to:

$$\nabla^{2}\mathbf{q}(\mathbf{r},\tau) - 3\sigma_{\mathbf{a}}\sigma_{\mathbf{tr}}\mathbf{q}(\mathbf{r},\tau) + \frac{\partial\mathbf{q}(\mathbf{r},\tau)}{\partial\tau} + \mathbf{S}(\mathbf{r},\tau) = 0$$
 (112)

where the age variable  $(\tau)$  is defined* by:

$$d\tau = \frac{1}{3\xi\sigma_8\sigma_{tr}}\frac{dE}{E} \tag{113}$$

and:

$$\mathbf{S}(\mathbf{r},\tau) = 3\xi\sigma_{\mathbf{S}}\sigma_{\mathbf{tr}}\mathbf{E}\ \mathbf{S}(\mathbf{r},\mathbf{E}) \tag{114}$$

The age or age difference  $\tau(E,E')$  between two energy values is defined by:

$$\tau(\mathbf{E}, \mathbf{E}') = \int_{\mathbf{E}}^{\mathbf{E}} \frac{1}{3\xi \sigma_{\mathbf{S}} \sigma_{\mathbf{tr}}} \frac{d\mathbf{E}''}{\mathbf{E}''} \tag{115}$$

^{*}  $\tau$  is here defined as an increasing function of E rather than a decreasing function. If the latter alternative is chosen, the right side of Eq. (113) and the term  $\partial q/\partial \tau$  of Eq. (112) should be changed in sign.

Eq. (112) may be rewritten as:

$$\nabla^2 \mathbf{q'}(\mathbf{r},\tau) + \frac{\partial \mathbf{q'}(\mathbf{r},\tau)}{\partial \tau} + \mathbf{p}^{-1}(\mathbf{E},\mathbf{E}_0) \ \mathbf{S}(\mathbf{r},\tau) = \mathbf{0}$$
 (116)

with:

$$\mathbf{q} = \mathbf{p}(\mathbf{E}, \mathbf{E}_0) \mathbf{q'} \tag{117}$$

where:

$$p(E,E_0) = e^{-\int_E^{E_0} \frac{\sigma_a}{\xi \sigma_s} \frac{dE}{E}}$$
(118)

and  $E_0$  is any energy value. It is seen that, for a monoenergetic source, the solution with absorption is simply the solution without absorption multiplied by the infinite-medium resonance escape probability (as given by the Fermi slowing-down theory).

Tables 1.3.14 and 1.3.15 present some important solutions^{37,38} of the age equation in the case of single homogeneous regions. It is assumed that, for the finite regions, the extrapolated boundary (see below, "Finite Regions and Boundary Conditions") is independent of energy. It is seen that the second moment of the slowing-down distribution (the mean square distance between birth position and position of crossing a given energy value) is:

$$\overline{\mathbf{r}^2} \left( \mathbf{E}, \mathbf{E}_0 \right) = 6\tau \left( \mathbf{E}, \mathbf{E}_0 \right) \tag{119}$$

Two media problems are difficult to solve because of the complicated boundary conditions (see below). Some solutions to such problems exist. Bellman, Marshak, and Wing, have reported the solution to the problem of a monoenergetic source displaced from the plane interface between two semi-infinite non-absorbing media in which the ratio of scattering cross sections is independent of energy, and a similar problem has been reported on earlier by Friedman. 40

Table 1.3.14 — Aging in Infinite Homogeneous Medium

$$[\tau = \tau(E, E_0); p = p(E, E_0)]$$

Source	<b>q</b> ( <u><b>r</b></u> , <b>E</b> )	Comments
Point source At $r = 0$ , $E = E_0$ $S = \frac{\delta(\underline{r})}{4\pi r^2} \delta(E - E_0)$	$p \frac{e^{-\frac{t^2}{4\tau}}}{(4\pi \tau)^{\frac{1}{2}}}$	$\overline{r^2}(E,E_0) = 6\tau$
Plane source At $x = 0$ , $E = E_0$ $S = \delta(x) \delta(E - E_0)$	$p \frac{e^{-\frac{X^2}{4\tau}}}{(4\pi\tau)^{\frac{1}{2}}}$	$\overline{x^2} = \frac{1}{3} \overline{r^3} = 2\tau$
"Laplacian" source At E = E ₀ S = $\delta$ (E - E ₀ ) f( $\underline{r}$ ) Where $\nabla^2$ f( $\underline{r}$ ) = - $B^2$ f ( $\underline{r}$ )	$f(\underline{\mathbf{r}}) e^{-\int_{E}^{E_0} \frac{\sigma_a^{eff}}{\xi \sigma_s} \frac{dE}{E}}$	$\sigma_a^{\text{eff}} = \sigma_a + DB^2$

Table 1.3.15 — Aging in Finite Homogeneous Medium

$$[\tau = \tau(E, E_0); p = p(E, E_0)]$$

	T
Case	q( <u>r</u> ,E)
Point source in sphere of extrapolated radius = a	$q(\underline{r},E) = \frac{p}{2a^2r} \sum_{m=1}^{\infty} m \sin \frac{m\pi r}{a} e^{-\frac{m^2r^2}{a^2}\tau}$
$\mathbf{S} = \frac{\delta(\underline{\mathbf{r}})}{4\pi \underline{\mathbf{r}}^2}  \delta(\mathbf{E} - \mathbf{E}_0)$	$= p \frac{e^{-\frac{t^2}{4\tau}}}{(4\pi\tau)^{\frac{1}{2}}} \left[ 1 + 2 \sum_{m=1}^{\infty} \left( \cosh \frac{amr}{\tau} \right) \right]$
	$-\frac{2am}{r}\sinh\frac{amr}{\tau}\bigg)e^{-\frac{m^2a}{\tau}}$
Plane (non-uniform) source in infinite column of extrapolated dimensions = a,b	$q(\underline{r},E) = p \sum_{l,m=1}^{\infty} q_{lm} \sin \frac{l\pi x}{a} \sin \frac{m\pi y}{b}$
$S = \delta(E - E_0) \ \delta(z) \sum_{l,m=1}^{\infty} S_{lm} \sin \frac{l\pi x}{a} \sin \frac{m\pi y}{b}$	where: $q_{1m} = S_{lm} \frac{e^{-\frac{z^2}{4\tau}}}{(4\pi\tau)^{1/2}} e^{-\pi^2\tau \left(\frac{l^2}{a^2} + \frac{m^2}{b^2}\right)}$
Point source in infinite  column of extrapolated dimensions = a,b	Solution obtained from preceding one, with
$S = \delta(E - E_0) \delta(z) \delta(x - x_0) \delta(y - y_0)$	$S_{1m} = \frac{4}{ab} \sin \frac{i\pi x_0}{a} \sin \frac{m\pi y_0}{b}$
	or:
	$q = p \frac{e^{-\frac{x^2}{4\tau}}}{(4\pi\tau)^{\frac{1}{2}}} \sum_{1,m=-\infty}^{+\infty} \left[ e^{-\frac{(x-x_0+2a1)^2}{4\tau}} \right]$
	$-e^{-\frac{(x+x_0+2a))^2}{4\tau}}\right]\cdot\left[e^{-\frac{(y-y_0+2bm)^2}{4\tau}}\right]$
	$-e^{-\frac{(y+y_0+2bm)^2}{4\tau}}$
"Laplacian" source vanishing at extrapolated boundary:	$q(\underline{r}, E) = f(\underline{r}) e^{-\int_{E}^{E_0} \frac{\sigma^{eff}}{\xi \sigma_s} \frac{dE}{E}}$
$S = \delta(E - E_0) f(\underline{r})$ $\nabla^2 f(\underline{r}) = -B^2 f(\underline{r})$	where
$f(\underline{r}) = 0$ at extrapolated boundary	$\sigma_{\rm a}^{\rm eff} = \sigma_{\rm a} + {\rm DB}^2$

# AGING FOLLOWED BY DIFFUSION

In thermal reactors, the aging process continues until thermal energies are reached, and the thermal neutrons then diffuse (see "Thermal Distributions," above and "Diffusion of Thermal Neutrons," below). If it is assumed that the change from aging to diffusion occurs at a definite energy  $(E_{th})$ , the thermal-neutron flux  $(\varphi_{th})$ , satisfies:

$$\operatorname{div} \mathbf{D_{th}} \operatorname{grad} \varphi_{th}(\underline{\mathbf{r}}) - \sigma_{\mathbf{a},th} \varphi_{th}(\underline{\mathbf{r}}) + q(\mathbf{r}, \mathbf{E}_{th}) = 0$$
 (120)

the solution to which in the case of an infinite homogeneous medium, can be expressed, cf., Eq. (50) and Table 1.3.9, as:

$$\varphi_{th}(\underline{\mathbf{r}}) = \int \frac{e^{-\kappa|\underline{\mathbf{r}}-\underline{\mathbf{r}}'|}}{4\pi D_{th}|\underline{\mathbf{r}}-\underline{\mathbf{r}}'|} q(\mathbf{r}', \mathbf{E}_{th}) d\underline{\mathbf{r}}'$$
(121)

where:

$$\kappa = \left(\frac{\sigma_{a,th}}{D_{th}}\right)^{1/2} = \frac{1}{L}$$
 (122)

and is the reciprocal diffusion length.

Solutions^{17,37,38} of the problem of aging followed by diffusion for some interesting fast-neutron sources in simple geometries are presented in Tables 1.3.16 and 1.3.17. The extrapolated boundary is assumed to be energy-independent. It is seen that the second moment (the mean square distance between birth position and position of death by thermal absorption) is given by:

$$\overline{\mathbf{r}^2} \ (\mathbf{E}_{th}, \mathbf{E}_0) = 6[\tau(\mathbf{E}_{th}, \mathbf{E}_0) + \mathbf{L}^2] = 6\mathbf{M}^2$$
 (123)

where M² is called the "migration area" and M is the migration length.

Figure 1.3.9 plots  $r^2 \varphi_{th}$  for a point source in an infinite medium; Fig. 1.3.10 plots  $4\pi \int_0^r r^2 \varphi_{th} dr$ , the thermal flux within (r); and Fig. 1.3.11 plots  $4\pi \int_0^a r^2 \varphi_{th} dr$  for a point source at the center of a sphere of extrapolated radius (a).

Table 1.3.16—Aging Followed by Diffusion in Infinite Homogeneous Medium

$$[\tau = \tau (E_{th}, E_0); p = p (E_{th}, E_0)]$$

Source	φ +h (Γ)	Comments
Point source at: r = 0, E = E ₀	$ \varphi_{th}(\underline{r}) = \frac{p}{8\pi D_{th}r} \left\{ e^{-\kappa r} \left[ 1 - erf\left(\kappa\sqrt{\tau} - \frac{r}{2\sqrt{\tau}}\right) \right] \right\} $	$r^2 = 6 (\tau + L^2) = 6M^2$ $L^2 = \frac{1}{\kappa^2} = D_{th}/\sigma_{a,th}$
$S = \frac{\delta(r)}{4\pi r^2} \delta(E - E_0)$	$-e^{KI}\left[1-\mathrm{erf}\left(\kappa\sqrt{\tau}+\frac{\Gamma}{2\sqrt{\tau}}\right)\right]\right\}$	
	$\varphi_{\rm th}(\underline{\mathbf{r}}) \approx \frac{\mathrm{e}^{\kappa^2 \tau}}{4\pi D_{\rm th} \mathbf{r}}  \mathrm{e}^{-\kappa \mathbf{r}} - \frac{\sqrt{\tau/\pi}}{2\pi D_{\rm th} \mathbf{r}^2}  \mathrm{e}^{-\mathbf{r}^2/4\tau}$	
	for r ≫ 2κτ	
Plane source at: $x = 0$ , $E = E_0$ $S = \delta(x) \delta(E - E_0)$ $\varphi_{th}(x) = p$	$\varphi_{\rm th}(x) = p \frac{e^{\kappa^2 \tau}}{4\kappa D_{\rm th}} \left\{ e^{-\kappa x} \left[ 1 + \operatorname{erf}\left(\frac{x}{2\sqrt{\tau}} - \kappa\sqrt{\tau}\right) \right] \right\}$	$\overline{x^2} = \frac{1}{3} \overline{r^2}$
	$+ e^{\kappa x} \left[ 1 - \operatorname{erf} \left( \frac{x}{2\sqrt{\tau}} + \kappa \sqrt{\tau} \right) \right] \right\}$	
"Laplacian" source at:	$\varphi_{th}(\mathbf{r}) = \frac{1}{\sigma_{eff,h}^{eff,h}} \mathbf{q} (\mathbf{r}, \mathbf{E}_{th})$	$\sigma_a^{\text{eff}} = \sigma_a + DB^2$
$\mathbf{E} = \mathbf{E_0}$	- a,m	and thus
$S = \delta(E - E_0) f(\underline{r})$ where	$=\frac{f(r)}{\sigma^{\frac{1}{2}}}e^{-\int_{E_{th}}^{E_{0}}\frac{\sigma_{th}^{\text{an}}}{\xi\sigma_{a}}\frac{dE}{E}}$	$\sigma_{\rm a,th}^{\rm aff}={\rm D_{th}}\;(\kappa^2+{\rm B}^2)$
where $\nabla^2 f(\underline{r}) = -B^2 f(\underline{r})$	σα, th	

Table 1.3.17 — Aging Followed by Diffusion in Finite Homogeneous Media  $[\tau = \tau(E_{th}, E_0); \ p = p(E_{th}, E_0); \ \kappa^2 = \sigma_{a,th}/D_{th}]$ 

	(6/1 P P(201)26/1 02.07 201)
Case	$arphi_{ m th}({ m r})$
Point source at center of sphere of extrapolated radius = a	$\varphi_{th}(\underline{r}) = \frac{p}{2D_{th}r} \sum_{m=1}^{\infty} \frac{m}{\kappa^2 a^2 + m^2 \pi^2} e^{-\frac{m^2 \pi^2}{a^2} \tau} \sin \frac{m \pi r}{a}$
$S = \frac{o(\mathbf{r})}{4\pi r^2} \delta(\mathbf{E} - \mathbf{E}_0)$	$= \frac{p}{8\pi D_{th} r} \sum_{m=-\infty}^{\infty} \left\{ e^{-\kappa (r+2am)} \left[ 1 - erf \left( \kappa \sqrt{\tau} - \frac{r+2am}{2\sqrt{\tau}} \right) \right] \right\}$
	$-e^{\kappa(r+2am)}\left[1-erf\left(\kappa\sqrt{\tau}+\frac{r+2am}{2\sqrt{\tau}}\right)\right]$
	$\varphi_{th}(\underline{r}) \approx \frac{p e^{\kappa^2 \tau}}{4\pi D_{th} r} \left( e^{-\kappa r} - e^{-2a\kappa} e^{\kappa r} \right) \text{ for } r \gg 2\kappa \tau \text{ and } r \gg 1/2$
Plane (non-uniform) source in infinite column of extrapolated dimensions = a,b $S = \delta(E - E_0) \ \delta(z)$ $\times \sum_{l,m=1}^{\infty} S_{lm} \sin \frac{l\pi x}{a} \sin \frac{m\pi y}{b}$	$\varphi_{th}(\underline{r}) = p \sum_{l,m=1}^{\infty} \varphi_{lm} \sin \frac{l\pi x}{a} \sin \frac{m\pi y}{b}$
	where:
	$\varphi_{\rm lm} = \frac{S_{\rm lm}  e^{\kappa^2 \tau}}{4  \omega D_{\rm th}^{\kappa}} \left\{ e^{-\omega \kappa z} \left[ 1 +  erf \left( \frac{z}{2\sqrt{\tau}} -  \omega \kappa \sqrt{\tau} \right) \right] \right\}$
	$+ e^{\omega \kappa z} \left[ 1 - erf\left(\frac{z}{2\sqrt{\tau}} + \omega \kappa \sqrt{\tau}\right) \right]$
	and:
	$\omega = \sqrt{1 + \frac{\pi^2}{\kappa^2} \left( \frac{l^2}{a^2} + \frac{m^2}{b^2} \right)}$
Point source in infinite column of	Solution obtained from preceding one, with
extrapolated dimensions = a,b	4 . laxa . lava
$S = \delta(E - E_0) \delta(z) \delta(x - x_0) \delta(y - y_0)$	$S_{lm} = \frac{4}{ab} \sin \frac{l\pi x_0}{a} \sin \frac{l\pi y_0}{b}$
"Laplacian" source vanishing at extrapolated boundary	$\varphi_{th}(\underline{r}) = \frac{1}{\sigma_{a,th}^{eff}} q(\underline{r}, E_{th})$ where $\sigma_{a}^{eff} = DB^2 + \sigma_{a}$
$\mathbf{S} = \delta(\mathbf{E} - \mathbf{E}_0) \ \mathbf{f}(\underline{\mathbf{r}})$	f(m) all of the co
$\nabla^2 f(\underline{r}) = -B^2 f(\underline{r})$	$\varphi_{th}(\underline{r}) = \frac{f(\underline{r})}{\sigma^{eff}} e^{-\int_{E_{th}}^{E_0} \frac{\sigma_{eff}^{eff}}{E}} e^{-\int_{E_{th}}^{E_0} \frac{\sigma_{eff}^{eff}}{E}} \qquad \text{where } \sigma_{a,th}^{eff} = D_{th}(B^2 + \kappa^2)$
	ı va.th

# IMPROVEMENTS ON FERMI AGE THEORY

The inaccuracy of age theory is reflected in the gaussian distribution of Table 1.3.14, the moment formula, Eq. (119), the resonance escape formula, Eq. (118), and the effective escape integral in the third row of Table 1.3.14. The deviation from the gaussian distribution and the special case of hydrogenous media are considered below. The moment and escape-integral difficulties, although interrelated, are treated consecutively below.

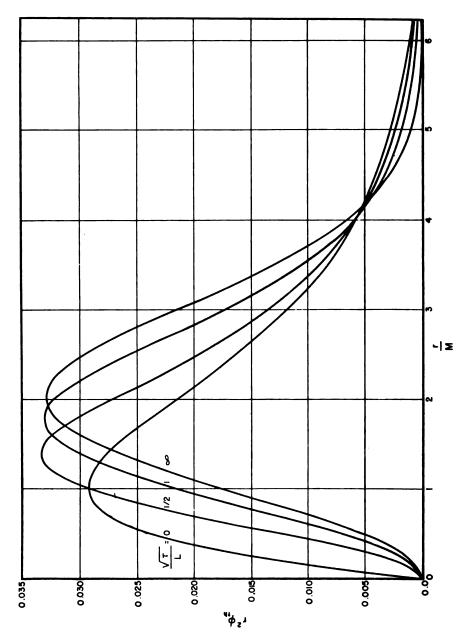


Fig. 1.3.9 — Aging Followed by Diffusion in Infinite Medium Owing to Point Source of Fast Neutrons;  $r^2\phi_{th}(r)$  vs Position. Reprinted from Wallace and Le Caine, MT-12, NRC-1480.

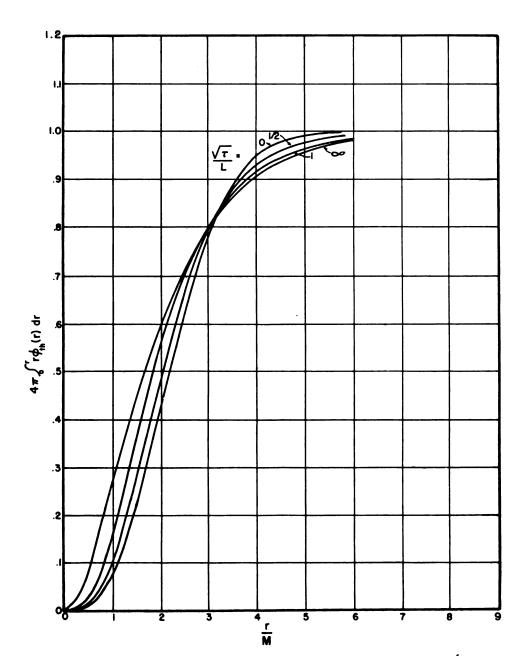


Fig. 1.3.10 — Aging Followed by Diffusion in Infinite Medium Owing to Point Source of Fast Neutrons;  $4\pi\int_0^r r^2 \varphi_{th}(r) dr$  vs Position. Reprinted from Wallace and Le Caine, MT-12, NRC-1480.

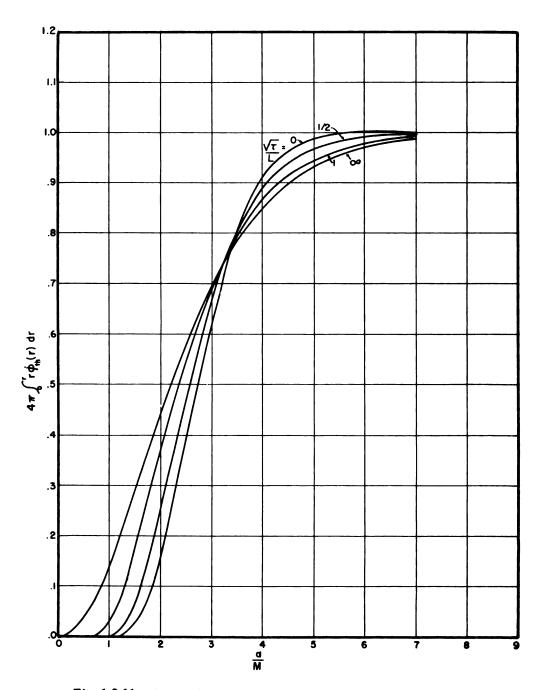


Fig. 1.3.11 — Aging Followed by Diffusion Owing to Central Point Source of Fast Neutrons in Finite Sphere of Extrapolated Radius a;  $4\pi \int_0^1 r^2 \varphi_{th}(r) dr$  vs a. Reprinted from Wallace and Le Caine, MT-12, NRC-1480.

## MOMENT IMPROVEMENTS IN THE ABSENCE OF ABSORPTION

Equations (119) and (115) generally underestimate the second moment owing to a point source. As shown by Young,  41,42  this is a result of the incorrect energy spectrum of age theory, the correct moment in the absence of absorption for an arbitrary source, S(E), being given by:

$$\overline{\mathbf{r}_{\mathbf{q}}^{2}}(\mathbf{E}) = 2 \int_{\mathbf{r}}^{\bullet} 1 \, \varphi(\mathbf{E}) \, d\mathbf{E}$$
 (124)

where  $\varphi(E)$ , is the flux in an infinite homogeneous medium resulting from an integrated source strength of 1 per unit volume. For isotropic scattering in the laboratory system, Eq. (124) is exact with:

$$1 = \frac{1}{\sigma_{\rm S}\left(\rm E\right)}$$

while for non-isotropic scattering, it is approximate with:

$$1 = 1/\sigma_{tr}(\mathbf{E})$$

For the source:

$$S(E) = \frac{1}{\xi (1-\alpha)} \left( \frac{1}{E_0} - \frac{\alpha}{E} \right)$$

in the interval  $\alpha E_0$  up to  $E_0$ , the flux (see "Exact Solutions for Special Sources" above) is given exactly by:

$$\varphi(\mathbf{E}) = \frac{1}{\xi \ \sigma_{\mathbf{S}} \ \mathbf{E}}$$

and the resulting second moment is simply  $6\tau(E,E_0)$ , the age-theory result for a monoenergetic source at  $E_0$ .

For the monoenergetic source, however, to which Eq. (119) applies, the exact spectrum  $\varphi(E)$  (see "Fluctuations near Source Energy," above) differs from the asymptotic spectrum:

$$\varphi_{\mathbf{a}}(\mathbf{E}) = \frac{1}{\xi \, \sigma_{\mathbf{c}} \, \mathbf{E}}$$

in the first few collision intervals and also at the source energy  $E_0$ , where:

$$\varphi(\mathbf{E_0}) = \frac{1}{\sigma_{\mathbf{S}}(\mathbf{E_0})} \delta(\mathbf{E} - \mathbf{E_0})$$

Thus, Eq. (124) leads to:

$$\overline{\mathbf{r}_{\mathbf{q}}^{2}} (\mathbf{E}, \mathbf{E}_{\mathbf{0}}) = \frac{2l(\mathbf{E}_{\mathbf{0}})}{\sigma_{\mathbf{S}}(\mathbf{E}_{\mathbf{0}})} + 6\tau(\mathbf{E}, \mathbf{E}_{\mathbf{0}}) + 2\int_{\mathbf{E}}^{\mathbf{E}_{\mathbf{0}}} l[\varphi(\mathbf{E}) - \varphi_{\mathbf{a}}(\mathbf{E})] d\mathbf{E}$$
(125)

which gives the mean square distance between birth position at  $E_0$  and position of crossing the energy, E.

Another second moment  $(r_{\varphi}^2)$ , the mean square distance between birth position and position of collision at energy E, is given in the Fermi, Wigner, and G. G. approximations (see "Slowing Down with No Space Variation," above) by:

$$\overline{\mathbf{r}_{\varphi}^{2}}(\mathbf{E}) = \overline{\mathbf{r}_{q}^{2}}(\mathbf{E}) + \frac{2\epsilon}{\sigma_{s}(\mathbf{E})\sigma_{tr}(\mathbf{E})}$$
(126)

for energies (E) below the source energies. Equations similar to Eq. (126)* are usually written and, in the case of a monoenergetic source, used in conjunction with Eq. (125) modified by neglecting the difference between the exact and asymptotic flux. This procedure gives  $r_{\varphi}^2$  to within 1 percent of the result of an exact computation† in carbon.

## ESCAPE-INTEGRAL IMPROVEMENTS

Equations (3) and (4) in the Fermi, Wigner, and G. G. approximations imply:

$$\epsilon \frac{\partial \mathbf{q}(\underline{\mathbf{r}}, \underline{\mathbf{E}})}{\partial \underline{\mathbf{E}}} = \frac{\mathbf{q}(\underline{\underline{\mathbf{r}}}, \underline{\mathbf{E}})}{\xi \underline{\mathbf{E}}} - \sigma_{\underline{\mathbf{S}}}(\underline{\mathbf{E}}) \varphi(\underline{\underline{\mathbf{r}}}, \underline{\mathbf{E}})$$
(127)‡

which for the Fermi case ( $\epsilon = 0$ ) is identical to Eq. (111) and leads to age theory. The combination of Eq. (127) with the diffusion equation (109) gives for space-independent cross sections:

$$\nabla^{2}\mathbf{q} - 3\sigma_{\mathbf{a}}\sigma_{\mathbf{tr}}\mathbf{q} + (1 + \epsilon \frac{\sigma_{\mathbf{a}}}{\sigma_{\mathbf{s}}}) \frac{\partial \mathbf{q}}{\partial \tau} - \frac{\epsilon}{3\sigma_{\mathbf{s}}\sigma_{\mathbf{tr}}} \frac{\nabla^{2}\partial \mathbf{q}}{\partial \tau} + \mathbf{S}(\underline{\mathbf{r}}, \tau) = \mathbf{0}$$
 (128)

rather than Eq. (112).

The solution of Eq. (128) cannot be expressed as a product, as in Eq. (117), of the escape integral and the solution without absorption. For a monoenergetic laplacian or mode source (cf. Tables 1.3.14 and 1.3.15), the solution can be obtained by replacing  $\nabla^2$  by  $-\mathbf{B}^2$  and then using Table 1.3.3. The result is:

$$\mathbf{q}(\underline{\mathbf{r}},\mathbf{E}) = \mathbf{f}(\underline{\mathbf{r}}) \left[ \frac{1}{1 + \epsilon \frac{\sigma_{\mathbf{a}} + \mathbf{D}\mathbf{B}^{2}}{\sigma_{\mathbf{s}}}} \right]_{\mathbf{E} = \mathbf{E}_{\mathbf{0}}} \mathbf{e}^{-\int_{\mathbf{E}}^{\mathbf{E}_{\mathbf{0}}} \frac{\sigma_{\mathbf{a}}^{\text{eff}}}{\xi \sigma_{\mathbf{s}}} \frac{d\mathbf{E}}{\mathbf{E}}$$
(129)

where:

$$D = \frac{1}{3\sigma_{tr}(E)}$$

and:

$$\sigma_a^{\text{eff}} = \frac{\sigma_a + DB^2}{1 + \epsilon \frac{\sigma_a + DB^2}{\sigma_s}}$$
 (130)

For a point monoenergetic source, an ad hoc alternative⁴⁵ to the use of Eq. (128), which retains the simplicity of the age-theory result Eq. (117) (Tables 1.3.14 through 1.3.17), con-

$$\overline{\mathbf{r}^2} = \overline{\mathbf{r}_q^2} + \frac{2}{[\sigma_*(\mathbf{E})]^2}$$

^{*}Weinberg and Noderer 43 write, in essence, the formula:

[†] Marshak⁴⁴ fits the scattering cross section by a sum of powers of the energy, and proceeds according to the methods described below in "Exact Space-dependence of Slowing-down Density."

[‡] Eq. (127) results in Eq. (10) when Eq. (2) is valid, that is, when there is no leakage.

sists of replacing Eq. (118) by a more accurate infinite-medium escape integral (Tables 1.3.3, 1.3.4, and 1.3.6) and replacing  $\tau(E,E_0)$  as given by Eq. (115) by one-sixth of the measured (or more accurately computed)  $\overline{r_0^2}$  (E,E₀). More general source solutions are obtainable from these ad hoc solutions by superposition.

## **EXACT SPACE DEPENDENCE OF SLOWING-DOWN DENSITY**

## DEVIATIONS FROM THE GAUSSIAN DISTRIBUTION

In an infinite nonabsorbing medium having only elastic scattering with energy-independent cross section, results more exact than those from Fermi theory have been obtained.

A Laplace transform (i.e., multiply by  $e^{-\eta u}$  and integrate from 0 to  $\infty$ ) of the Boltzmann equation for the collision density leads to an equation similar to Eq. (17). This "one-velocity" problem has been treated by the spherical-harmonic method.⁴⁶

An alternative method^{47,48} involves a further Fourier transform with respect to the space variable, z (i.e., multiply the equivalent one-velocity equation by  $e^{izy}$  and integrate from  $-\infty$  to  $+\infty$ ), before spherical-harmonic expansions are made. The resulting infinite sequence of equations is then solved approximately, and the Fourier and Laplace inversions are performed—the latter by the method of steepest descents. For a plane, isotropic, monoenergetic (E₀) source, with z the distance from the plane in units of the mean free path:

$$\mathbf{u} = \ln(\mathbf{E}_{\mathbf{0}}/\mathbf{E})$$

$$\mathbf{u'} = \frac{\mathbf{M}}{2} \mathbf{u}$$

where M is the mass of the scattering nuclei, and:

$$\tau = u/3 \xi \overline{\mu}_0$$

is the Fermi age, the resulting slowing-down density can be written (for z < u') as:

$$\mathbf{q}(\mathbf{z},\tau) = \mathbf{k}(\mathbf{z}/\mathbf{u}') \frac{e^{-\frac{\mathbf{z}^2}{4\tau} \phi(\mathbf{z}/\mathbf{u}')}}{\sqrt{4\pi\tau}}$$
(131)

where  $\phi$  and K are as shown in Table 1.3.18.

The first-mentioned spherical-harmonics method, carried through the  $P_2$ -approximation, leads to a less accurate but simpler result for  $M \gg 1$ , namely;

$$q(z,\tau) = \left[1 + (\frac{1}{4}u)F(z^{2}/\tau)\right] \frac{e^{-\frac{z^{2}}{4\tau}}}{\sqrt{4\pi\tau}}$$
(132)

where:

$$\mathbf{F}(\mathbf{z}^2/\tau) = (\mathbf{B}_1 - 2\mathbf{B}_0) - (2\mathbf{B}_1 - \mathbf{B}_0)(\mathbf{z}^2/\tau) + (\mathbf{B}_1/4)(\mathbf{z}^2/\tau)^2 \dots$$

$$B_0 = -\frac{4}{15M} (1 - \frac{7}{3M} + ...)$$

$$B_1 = \frac{18}{5M} (1 - \frac{2}{3M} + \ldots)$$

Equation 132 was first obtained by Placzek⁴⁹ using the method of moments.

In Fig. 1.3.12, a comparison between theory, Eq. (132), and an experimental measurement  50  in graphite is shown. An Sb $^{124}-$ Be photoneutron source (E $_0\approx 20$  kev) was used, and the saturated activity, A $_S$  (which is almost proportional to q), of indium foils was measured out to about 60 cm from the source. In this energy range, the neutron mean free path is essentially constant. For comparison, the gaussian age-theory result is also shown in Fig. 1.3.12.

## ASYMPTOTIC SPACE DEPENDENCE

At very large distances ( $z > \frac{M}{2}$  u), Wick has shown that  $q \sim e^{-z}$ . Numerical work done for M = 12 by Marshall, a student of Wick, yields the following asymptotic result:

$$q(u,z) \sim e^{-z} \left[ 1 - 1.44 \left( \frac{u}{z} \right)^{\frac{1}{2}} + 0.250 \left( \frac{u}{z} \right) + \cdots \right]$$
 (133)

for the same problem as considered previously.

Wick et al also consider energy-dependent cross sections, finding that in a nonabsorbing medium the asymptotic space variation is as  $z^b e^{-z}$ , where z is measured in units of the mean free path at the source energy and b depends upon how rapidly the mean free path decreases with decreasing energy.

In a multiplying medium with k (number of neutrons produced per neutron absorbed) slightly less than unity, the general asymptotic solution for the fission density at distance z from a plane source (of unit fission rate per unit area) is:⁵¹

$$f(z) = \frac{1}{2m\sqrt{1-k}} e^{-z\sqrt{1-k}/m}$$
 (134)

where m² is the mean square migration distance of the neutrons, cf. Eq. (123), from fission birth to where they in turn produce fissions.

By the use of Eq. (27), point sources can be handled from the results for plane sources, e.g.:

$$\mathbf{q}(\mathbf{r},\tau) = -\left[\frac{1}{2\pi z} \frac{\partial \mathbf{q}(\mathbf{z},\tau)}{\partial \mathbf{z}}\right]_{\mathbf{z} = \mathbf{r}} \tag{135}$$

## HYDROGENOUS MEDIA

## SLOWING-DOWN DISTRIBUTION

When a large fraction of the neutron energy may be lost in a single collision, as is the case for neutron-proton collisions, the Fermi age-diffusion equation (112) should be replaced by Eq. (128) with  $\epsilon=1$  for hydrogen scattering. For hydrogen, Eq. (128) is exact except for the diffusion approximation that leads to the  $\nabla^2$ q term. A solution of Eq. (128) with  $\sigma_a=0$ , discussed below and shown in Fig. 1.3.13, which takes into account the energy variation of  $\sigma_S$  and  $\sigma_{tr}$  in H₂O does not give a gaussian slowing-down space distribution. If the Fermi age-diffusion equation (112) is used for hydrogen, i.e.,  $\epsilon=0$  in Eq. (128), a gaussian distribution is obtained (cf. Table 1.3.14).

Despite the non-applicability of Eq. (112) for hydrogen, Wick has shown that, for constant cross section, for M=1, and for non-absorbing media, the collision density of neutrons  $(\psi_0)$  slowed down through a logarithmic energy range u is very close to the gaussian distribution up to distances of u mean free paths; see Fig. 1.3.14, Table 1.3.18, and Eq. (131). The deviation from age theory (curve B of Fig. 1.3.14) becomes very large only at distances greater than u mean free paths (factor of ten at 2u mean free paths: curve A). Asymptotically,  $\psi_0$  behaves as shown in curve C.



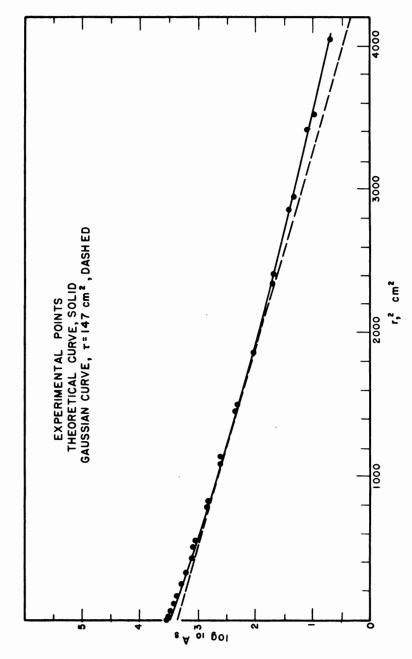


Fig. 1.3.12 — Slowing-down Density to Indium Resonance in Graphite from an Sb¹²⁴-Be Photoneutron Source. From L. D. Roberts, J. E. Hill, and G. McCammon, ORNL-201, 1950.

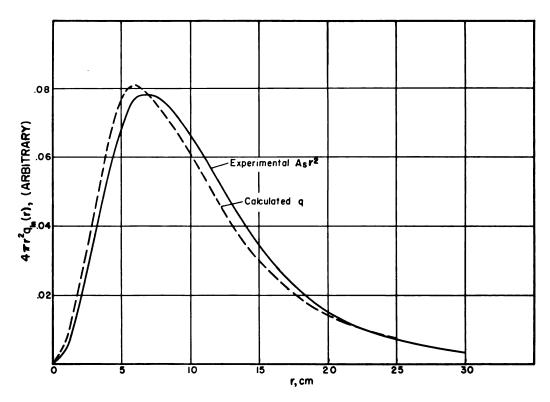


Fig. 1.3.13 — Comparison of Indium Resonance Activity with Theoretical Slowing-down Density in H₂O from a Fission Point Source. Submitted by N.D.A., Aug. 28, 1952.

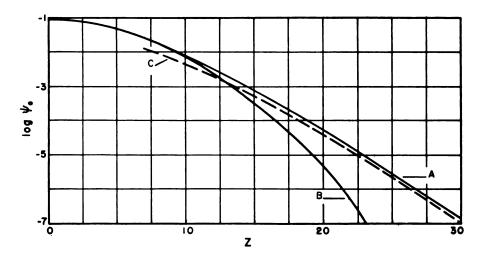


Fig. 1.3.14 — Deviation of Collision Density,  $\psi_0(z)$ , from the Gaussian Distribution (B) of Neutrons Slowing Down in an Infinite Medium of Constant Mean Free Path, l. From G. C. Wick, Phys. Rev. 75, 1949. Source energy =  $e^{10}E$ ; distance from plane source = zl; curve A is asymptotic to Curve C at very large distances.

Mass M	K(Z/u')	φ(Z/u')
1		$1 - \frac{11}{240} \left(\frac{Z}{u'}\right)^2 + \frac{73}{32,256} \left(\frac{Z}{u'}\right)^4 .$
9	$1-2.225\left(\frac{Z}{u'}\right)^2+12.39\left(\frac{Z}{u'}\right)^4$	$1 - 1.080 \left(\frac{Z}{u'}\right)^2 + (3.169) \left(\frac{Z}{u'}\right)^4$
12		$1 - 1.142 \left(\frac{Z}{u'}\right)^2 + (3.538) \left(\frac{Z}{u'}\right)^4$
60	$1-2.80\left(\frac{Z}{u'}\right)^2$ + 19.20 $\left(\frac{Z}{u'}\right)^4$	$1 - 1.350 \left(\frac{Z}{u'}\right)^2 + (4.908) \left(\frac{Z}{u'}\right)^4$

Table 1.3.18—Coefficients Giving Deviations from the Gaussian Slowing-down Density

(Adapted from Bethe, Tonks, and Hurwitz⁴⁷)

The distribution of fission neutrons moderated in  $H_2O$  to In resonance energy, 1.44 ev, as measured, differs significantly from the gaussian distribution over the entire range of distances from a point source (cf. curves A and D of Fig. 1.3.15).

The solution of Eq. (128) for a point fission source in  $H_2O$ , where the presence of oxygen is taken into account by including its scattering in the transport cross section, is obtained by taking the three-dimensional Fourier transform with respect to the variable  $\underline{r}$  which is the distance from source.

The transformed function  $Q(E,\omega)$  is given in Table 1.3.3 for hydrogen by the following substitution of symbols:

$$q(E) \rightarrow Q(E,\omega)$$

$$\sigma(E') \rightarrow \sigma_{\rm g}(E') + \omega^2/3 \,\sigma_{\rm tr} \qquad (136)$$

$$\psi(E) \rightarrow \psi(E,\omega)(1 + \omega^2/3 \,\sigma_{\rm g}\sigma_{\rm tr})$$

The solution  $Q(1.44,\omega)$  was obtained by numerical integration for several  $\omega$  values. The slowing-down distribution at In resonance was obtained by numerical integration of the Fourier inverse transforms after correcting Q for the small amount of slowing-down by oxygen:

$$q_{In}(r) = \left[1/(2\pi^2 r)\right] \int_0^{\infty} Q(1.44,\omega) \omega \sin(\omega r) d\omega$$
 (137)

Figure 1.3.13 shows a comparison of  $q_{\rm In}(r)$  with the experimentally measured, saturated In-foil activities  $(A_g)$ . This method is not suitable for obtaining the asymptotic behavior of q(r). Because of the sharp resonance of In, the activity  $(A_g)$  is directly proportional to the collision density at 1.44 ev rather than to the number of neutrons crossing 1.44 ev, which is  $q_{\rm In}$ . According to Eq. (126):

$$\overline{\mathbf{r}_{\varphi}^2} = \overline{\mathbf{r}_{\mathbf{q}}^2} + 2.5 \, \mathrm{cm}^2$$

Thus, the theoretical  $4\pi r^2 \sigma_S \phi$  curve would appear shifted slightly towards the experimental curve.

## r OF HYDROGENOUS MEDIA

Substances such as water or paraffin slow down neutrons very effectively because their hydrogen content is high. By ignoring the slowing-down effect of the heavy elements in a

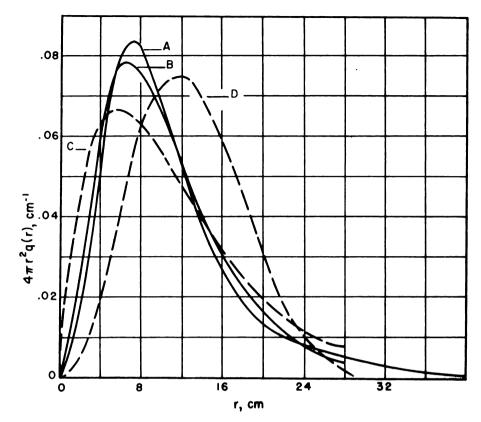


Fig. 1.3.15 — Slowing-down Distributions from a Point Fission Source in  $H_2O$ . Reprinted from S. Glasstone and M. C. Edlund, The Elements of Nuclear Reactor Theory, D. Van Nostrand Co., Inc., New York, 1952. (A) = experimental, to Indium resonance; (b) = convolution of three diffusion kernels; (C) = one diffusion kernel; (D) = gaussian kernel.

hydrogenous medium, very good values may be obtained for  $\overline{r_{\phi}^2}$  in terms of the behavior of the three-dimensional Fourier-transformed collision density  $\psi(u,\omega)$  at  $\omega=0$ ,  $u\neq 0$ ; that is:

$$\overline{\mathbf{r}_{\phi}^2} = -3\left[\left(\frac{\mathrm{d}^2\psi}{\mathrm{d}\omega^2}\right)\!\!/\!\psi\right]_{\omega=0} \tag{138}$$

Marshak⁵⁸ has indicated a method of obtaining  $\psi(u,0)$  and its second derivative as a function of u exactly. The resulting formula⁵⁴ for  $\overline{r_{\varphi}^2}$  is:

$$\overline{\mathbf{r}}_{\phi}^{2} = 2 \left\{ \frac{1^{2}(0)}{C(0)} + \frac{1^{2}(\mathbf{u})}{C(\mathbf{u})} + \int_{0}^{u} \frac{1^{2}(\mathbf{u}')}{C(\mathbf{u}')} d\mathbf{u}' + 1(0) 1(\mathbf{u}) \mathbf{F}(\mathbf{0}, \mathbf{u}) \right. \\
+ 1(\mathbf{u}) \int_{0}^{u} 1(\mathbf{u}') \mathbf{F}(\mathbf{u}', \mathbf{u}) d\mathbf{u}' + 1(0) \int_{0}^{u} 1(\mathbf{u}') \mathbf{F}(\mathbf{0}, \mathbf{u}') d\mathbf{u}' \\
+ \int_{0}^{u} 1(\mathbf{u}') \int_{0}^{u'} 1(\mathbf{u}'') \mathbf{F}(\mathbf{u}'', \mathbf{u}') d\mathbf{u}'' d\mathbf{u}' \right\}$$
(139)

Digitized by Google

where.

$$F(x,y) = \exp + \left[ \frac{-3}{2} (y-x) + \int_{x}^{y} C(t)dt \right]$$

 $l(u) = total mean free path at energy E = E_0e^{-u}$ 

C(u) = l(u)/hydrogen mean free path

## THE GROUP METHOD

Although more generally applicable,* the group method is here described in terms of the diffusion equation (109).

## THE FLUX EQUATIONS

Division of the energy scale into N intervals  $(E_0,E_1)$ ,  $(E_1,E_2)$ ,...  $(E_{i-1},E_i)$ ,...  $(E_{N-1},E_N)$  with  $E_0$  the highest and  $E_N$  the lowest energy, and integration of Eq. (109) over the ith interval results in:

$$\operatorname{div} \mathbf{D}_{i} \operatorname{grad} \Phi_{i}(\mathbf{r}) - \sigma_{2i} \Phi_{i}(\mathbf{r}) + q_{i-1}(\mathbf{r}) - q_{i}(\mathbf{r}) + \mathbf{S}_{i}(\mathbf{r}) = 0 \tag{140a}$$

where:

$$\Phi_{\mathbf{i}}(\underline{\mathbf{r}}) = \int_{\mathbf{E}_{\mathbf{i}}}^{\mathbf{E}_{\mathbf{i}-1}} \varphi_{\mathbf{i}}(\underline{\mathbf{r}}, \mathbf{E}) d\mathbf{E}$$
 (140b)

and:

$$\mathbf{S}_{\underline{\mathbf{I}}}(\underline{\mathbf{r}}) = \int_{E_1}^{E_{1-1}} \mathbf{S}(\underline{\mathbf{r}}, \mathbf{E}) d\mathbf{E}$$
 (140c)

are the integrated flux and source in the ith group, and  $D_i$  and  $\sigma_{ai}$  are proper average quantities. The quantities  $q_{i-1}$  and  $q_i$  are the slowing-down densities, as given by Eq. (3),† at the energies  $E_{i-1}$  and  $E_i$ , and may be written as:

$$\mathbf{q}_{i}(\underline{\mathbf{r}}) = \mathbf{q}(\underline{\mathbf{r}}, \mathbf{E}_{i}) = \sum_{i=1}^{i} \mathbf{s}_{ij} \Phi_{j}(\underline{\mathbf{r}})$$
 (141)

where the  $s_{ij}$  are defined by Eqs. (3), (140b), and (141). If the interval  $E_{i-1}$ ,  $E_i$  is larger in extent than a collision interval, then  $s_{ij}$  is the only non-vanishing coefficient.

Equations (140) may be written as:

$$\operatorname{div} D_{i} \operatorname{grad} \Phi_{i}(\underline{r}) - \sigma_{i} \Phi_{i}(\underline{r}) + \sum_{i=1}^{i-1} \sigma_{ij} \Phi_{j}(\underline{r}) + S_{i}(\underline{r}) = 0$$
 (142a)

where:

$$\sigma_{\mathbf{i}} = \sigma_{\mathbf{a}\mathbf{i}} + \mathbf{s}_{\mathbf{i}\mathbf{i}} \tag{142b}$$

^{*}Safonov⁵⁶ treats the many-velocity transport equations. Davison⁵⁶ discusses two-group transport theory and the two-group Serber method. Feynman, Welton et al⁵⁷ use the group method in their work.

[†]Where  $\frac{\sigma_1}{\sigma} \psi = \sigma_1 \varphi$ 

and:

$$\sigma_{ij} = S_{i-1,j} - S_{ii}$$
 (142c)

In Eq. (142a), the term  $\sigma_i \Phi_i$  represents the total loss out of group i by absorption and slowing-down, and the terms  $\sigma_{ij}\Phi_i$  in the summation represent the scattering into group i from group j. In the high-energy group, i = 1, the summation is to be replaced by zero. In the low-energy group, i = N, all the quantities  $s_{Nj}$  are taken as zero, since there is no lower group into which the neutrons can slow down.

The boundary conditions as obtained from Eqs. (157) and (158) are:

(144a)

(144b)

Black boundary

$$\begin{cases} \frac{1}{\Phi_{i}} \frac{\partial \Phi_{i}(\underline{r})}{\partial n \text{ormal}} = \frac{1}{\lambda} \approx \frac{1}{3(0.71)D_{i}} \\ \\ \text{or} \\ \\ \Phi_{i}(\underline{r}) = 0 \text{ at extrapolated boundary} \end{cases}$$

Recipe (159) for choosing a single extrapolation length, 2.13Deff, for all energies applies to the group method as

$$D^{eff} = \frac{\sum_{i=1}^{N} D_i \Phi_i(r)}{\sum_{i=1}^{N} \Phi_i(r)}$$
 at boundary

As an example of Eqs. (142), the two-group equations are:

div 
$$D_1$$
 grad  $\Phi_1(\underline{r}) - (\sigma_{a_1} + s_{11}) \Phi_1(\underline{r}) + S_1(\underline{r}) = 0$  (146a)

$$\operatorname{div} D_2 \operatorname{grad} \Phi_2(\mathbf{r}) - \sigma_{a2}\Phi_2(\mathbf{r}) + \mathbf{s}_{11}\Phi_1(\mathbf{r}) + \mathbf{S}_2(\mathbf{r}) = \mathbf{0}$$
 (146b)

where, in a thermal reactor, group 2 represents the thermal group and group 1 represents the slowing-down or fast group. For this case, the source term  $S_2(r)$  is usually zero.

SLOWING-DOWN DENSITY EQUATIONS

When the Fermi approximation is used, Eq. (141) is replaced by:

$$\mathbf{q}_{\mathbf{i}}(\mathbf{r}) = \xi \sigma_{\mathbf{s}} \mathbf{E}_{\mathbf{i}} \, \boldsymbol{\varphi}_{\mathbf{i}}(\mathbf{E}) \tag{147}$$

which is to be inserted into Eq. (140a). In this approximation, it is possible to express the group equations in terms of q rather than  $\phi$ . Thus Eq. (112) leads to:

$$\left(\frac{\mathbf{D}}{\xi \sigma_{\mathbf{S}}}\right)_{\mathbf{i}} \nabla^{2} \mathbf{Q}_{\mathbf{i}} - \left(\frac{\sigma_{\mathbf{a}}}{\xi \sigma_{\mathbf{S}}}\right)_{\mathbf{i}} \mathbf{Q}_{\mathbf{i}} + \mathbf{q}_{\mathbf{i}-\mathbf{i}} - \mathbf{q}_{\mathbf{i}} + \mathbf{S}_{\mathbf{i}} = \mathbf{0}$$
(148a)

where:

$$Q_i = \int_{E_i}^{E_{i-1}} q(\underline{r}, E) \frac{dE}{E}$$
 (148b)

 $S_i$  and  $q_i$  are defined as before, and  $(D/\xi \sigma_S)_i$  and  $(\sigma_a/\xi \sigma_S)_i$  are proper averages. Boundary conditions are obtained from Eq. (143) and Eq. (144) through the relation:

$$\Phi_{i} = \int_{E_{i}}^{E_{i-1}} \frac{q}{\xi \sigma_{s}} \frac{dE}{E} = \left(\frac{1}{\xi \sigma_{s}}\right)_{i} Q_{i}$$
 (148c)

Similarly, Eq. (116) leads to:

$$\nabla^{2}\mathbf{Q}_{i}'(\underline{\mathbf{r}}) + \mathbf{q}_{i-1}'(\underline{\mathbf{r}}) - \mathbf{q}_{i}'(\underline{\mathbf{r}}) + \mathbf{S}_{i}'(\underline{\mathbf{r}}) = 0$$
(149a)

where:

$$\mathbf{Q}_{\mathbf{i}}'(\underline{\mathbf{r}}) = \int_{\mathbf{E}_{\mathbf{i}}}^{\mathbf{E}_{\mathbf{i}-1}} \mathbf{q}'(\underline{\mathbf{r}},\mathbf{E}) \, \frac{\mathrm{d}\tau}{\mathrm{d}\mathbf{E}} \, \mathrm{d}\mathbf{E} \tag{149b}$$

and:

$$S_{i}'(\underline{r}) = \int_{E_{i}}^{E_{i-1}} \frac{s(\underline{r},\tau)}{p(E,E_{0})} \frac{d\tau}{dE} dE$$
 (149c)

Boundary conditions are obtained through the relation:

$$\Phi_{i}(\underline{r}) = \int_{E_{i}}^{E_{i-1}} \frac{p(E, E_{0})}{D} q'(\underline{r}, E) \frac{d\tau}{dE} dE = \left(\frac{p}{D}\right)_{i} Q'_{i}(\underline{r})$$
(149d)

where  $\left(\frac{p}{D}\right)_i$  is a proper average.

Equations (148) and (149) apply only to the slowing-down process. When there is a thermal group into which neutrons slow down, the quantity  $q_N$  is not zero but is rather the source of thermal neutrons. Equations similar to Eqs. (148) and (149) may be written for the more general age equation (128).

#### CHOICE OF PARAMETERS

Aside from computational considerations, the major questions in applying the group method are (1) the choice of the parameters  $D_i$ ,  $\sigma_{ai}$ ,  $(D/\xi\sigma_s)_i$ , and the like and (2) the treatment of the  $q_i$  terms.

An answer to both questions may be obtained by assuming a form for the energy dependence of  $\varphi(r,E)$  within each group. Thus, if  $\varphi$  is assumed to behave as 1/E within each group, the parameters entering into the general group equations (142) are:

$$D_{i} = \frac{\int_{E_{i}}^{E_{i-1}} D(E) \frac{dE}{E}}{\ln E_{i-1}/E_{i}}$$
(150a)

$$\sigma_{\mathbf{a}\mathbf{i}} = \frac{1}{\ln E_{\mathbf{i}-1}/E_{\mathbf{i}}} \int_{E_{\mathbf{i}}}^{E_{\mathbf{i}-1}} \sigma_{\mathbf{a}} (\mathbf{E}) \frac{d\mathbf{E}}{\mathbf{E}}$$
(150b)

$$\mathbf{s}_{ij} = \frac{1}{\ln E_{i-1}/E_i} \int_{E_i}^{E_{j-1}} \sigma_{\mathbf{S}}(\mathbf{E}') \ \mathbf{G}(\mathbf{E}_i, \mathbf{E}') \ \frac{\mathbf{d}\mathbf{E}'}{\mathbf{E}'} \tag{150c}$$

In Eq. (150c), any of the (exact or approximate) kernels of Table 1.3.2 may be used. Thus, in Fermi theory:

$$\mathbf{s_{ij}} = \frac{\xi \sigma_{S}(\mathbf{E_i})}{\ln \mathbf{E_{i-1}}/\mathbf{E_i}}$$

and:

$$s_{ij} = 0$$
 for  $i \neq j$ 

In the q equations (148) for Fermi theory, the assumption that  $q(\underline{r}, E)$  depends linearly on  $\ln E$  results in:

$$Q_{i} = \frac{1}{2} (q_{i-1} + q_{i}) \ln \frac{E_{i-1}}{E_{i}}$$
 (151)

in terms of which, qi may be solved for and substituted into Eq. (148a).

The solutions thus obtained may be improved by iteration. Thus, for example, the  $\Phi_i(\underline{r})$  resulting from the "1/E" parameters correspond to:

$$\varphi_{\mathbf{i}}(\underline{\mathbf{r}},\mathbf{E}) = \frac{\mathbf{f}_{\mathbf{i}}(\underline{\mathbf{r}})}{\mathbf{E}}$$

leading to discontinuities in  $\varphi(\underline{r}, E)$  at space boundaries and group boundaries. Improvements can be made by recalculating the parameters in terms of a new spectrum (rather than 1/E) obtained by a free-hand smoothing out of the discontinuities.

## **GROUP DIFFUSION KERNELS**

Consider the problem of slowing-down without absorption in an infinite homogeneous medium with a point monoenergetic source at  $\underline{r} = \underline{r}_0$ ,  $\underline{E} = \underline{E}_0$ . Assuming that each group interval is larger in extent than a collision interval  $(q_i = s_{ii}\Phi_i)$ , the group equations may be written as:

$$l_{1}^{2}\nabla^{2}q_{1} - q_{1} + \delta(\underline{r} - \underline{r}_{0}) = 0$$

$$l_{2}^{2}\nabla^{2}q_{2} - q_{2} + q_{1} = 0$$

$$l_{N}^{2}\nabla^{2}q_{N} - q_{N} + q_{N-1} = 0$$
(152a)

where:

$$\mathbf{q}_{\mathbf{i}}(\underline{\mathbf{r}}) = \mathbf{q}(\underline{\mathbf{r}}, \mathbf{E}_{\mathbf{i}}) = \mathbf{s}_{\mathbf{i}\mathbf{i}}\Phi_{\mathbf{i}}(\underline{\mathbf{r}}) \tag{152b}$$

and:



$$1_{i}^{2} = \frac{D_{i}}{s_{1i}} = \frac{1}{\kappa_{1}^{2}} \tag{152c}$$

The energy Ei is, as before, at the bottom of group i.

The solutions of Eq. (152a) are:

$$\mathbf{q}_1(\mathbf{r}) = \mathbf{k}_1(\mathbf{r}, \mathbf{r}_0) \tag{153a}$$

$$q_{2}(\underline{r}) = \int k_{2}(\underline{r},\underline{r}^{(1)}) k_{1}(\underline{r}^{(1)},\underline{r}_{0}) d\underline{r}^{(1)}$$

$$= \frac{l_{1}^{2}}{l_{1}^{2} - l_{2}^{2}} k_{1}(\underline{r},\underline{r}_{0}) + \frac{l_{2}^{2}}{l_{2}^{2} - l_{1}^{2}} k_{2}(\underline{r},\underline{r}_{0})$$
(153b)

$$\begin{aligned} \mathbf{q}_{N}(\underline{\mathbf{r}}) &= \int k_{N}(\underline{\mathbf{r}},\underline{\mathbf{r}}^{(1)}) \ k_{N-1} \ (\underline{\mathbf{r}}^{(1)},\underline{\mathbf{r}}^{(2)}) \ \dots \ k_{2}(\underline{\mathbf{r}}^{(N-2)},\underline{\mathbf{r}}^{(N-1)}) \\ &\times k_{1}(\underline{\mathbf{r}}^{(N-1)},\underline{\mathbf{r}}_{0}) \ d\underline{\mathbf{r}}^{(1)} \ \dots \ d\underline{\mathbf{r}}^{(N-1)} \\ &= \sum_{i=1}^{N} \ \frac{(l_{i}^{2})^{N-1}}{\prod_{j\neq i} (l_{1}^{2}-l_{j}^{2})} \ k_{1}(\underline{\mathbf{r}},\underline{\mathbf{r}}_{0}) \end{aligned} \tag{153c}$$

where, according to Table 1.3.9, the point diffusion kernel is given by:

$$\mathbf{k}_{\mathbf{i}}(\underline{\mathbf{r}},\underline{\mathbf{r}}_{\mathbf{0}}) = \frac{e^{-|\underline{\mathbf{r}}-\underline{\mathbf{r}}_{\mathbf{0}}|/1\mathbf{i}}}{4\pi \mathbf{1}_{\mathbf{i}}^{2}|\underline{\mathbf{r}}-\underline{\mathbf{r}}_{\mathbf{0}}|} \tag{154}$$

The solution for  $q_N(\underline{r})$  is thus the convolution of all N diffusion kernels. The expressions giving  $q_N$  as a super-position of the individual kernels are generally true, being valid as well for the infinite plane kernel (Table 1.3.9) and for the finite kernels,* provided the problem is spatially homogeneous, i.e., that the macroscopic cross sections are independent of position in the reactor.

In the presence of absorption, the solution  $q_N^a(r)$  is related to  $q_N(r)$  by:

$$\mathbf{q_{N}^{a}} = \mathbf{q_{N}} \quad \prod_{i=1}^{N} \quad \left(\frac{1}{1 + \frac{\sigma_{ai}}{\mathbf{s_{ii}}}}\right) \tag{155}$$

The second moment:

$$\overline{\mathbf{r}_{\mathbf{q}_{N}}^{2}} = |\underline{\mathbf{r}} - \underline{\mathbf{r}_{0}}|_{\mathbf{q}_{N}}^{2}$$

*The finite point kernel,  $k_p^f(\underline{r},\underline{r}_0)$ , for example, is defined by the equation:

$$1^{2}\nabla^{2}k_{p}^{f}(r,r_{0})-k_{p}^{f}(r,r_{0})+\delta(r-r_{0})=0$$

and by the boundary condition:

$$\mathbf{k}_{\mathbf{p}}^{\mathbf{f}}(\mathbf{r},\mathbf{r_0})=0$$

whenever  $\underline{r}$  is at the extrapolated boundary. Although not a displacement kernel,  $k_p^f(\underline{r},\underline{r_0})$  is symmetric. Thus:

$$\mathbf{k}_{\mathbf{p}}^{\mathbf{f}}(\mathbf{r},\mathbf{r}_{\mathbf{0}}) = \mathbf{k}_{\mathbf{p}}^{\mathbf{f}}(\mathbf{r}_{\mathbf{0}},\mathbf{r})$$

of the point source solution is given by:

$$\overline{r_{q_N}^2} = 6 \left( l_1^2 + l_2^2 + \ldots + l_N^2 \right) \tag{156}$$

Fermi age theory* may be considered as the limit of group theory, as represented by Eqs. (152) as the group intervals:

$$\Delta \mathbf{E_i} = \mathbf{E_{i-1}} - \mathbf{E_i}$$

approach zero and the number of groups approaches infinity. Use of Eq. (147) gives in the limit:

$$\frac{1}{s_{ii}} \rightarrow \frac{1}{\xi \sigma_{B}} \frac{\Delta E_{i}}{E_{i}}$$

leading to:

$$l_i^2 \rightarrow \frac{D}{\xi \sigma_B} \frac{\Delta E_i}{E_i} \rightarrow \Delta \tau_i$$

from which it follows that Eq. (152a) approaches the age Eq. (112) in the absence of absorption. Thus, Eq. (156) results in:

$$\overline{\mathbf{r_0^2}} \rightarrow 6 \sum \Delta \tau_1 = 6 \tau(\mathbf{E}, \mathbf{E_0})$$

and Eq. (155) leads to:

$$\mathbf{q^a} \rightarrow \mathbf{q} \Pi \frac{1}{1 + \frac{\sigma_a}{\xi \sigma_s} \frac{\Delta \mathbf{E}}{\mathbf{E}}} = \mathbf{q} \mathbf{p}(\mathbf{E}, \mathbf{E_0})$$

A comparison of 1-group, 3-group, and age theory fits vs the measured  $q_{in}(\underline{r})$  in water is shown in Fig. 1.3.15.

## FINITE REGIONS AND BOUNDARY CONDITIONS

## **BOUNDARY CONDITIONS**

Generalizing the one-velocity results of the discussion of "Homogeneous Regions in Contact" to the many-velocity case, the boundary conditions may be approximated by the following formulas:

$$\begin{vmatrix} \frac{1}{\varphi} & \frac{\partial \varphi(\mathbf{r}, \mathbf{E})}{\partial \text{ normal}} \end{vmatrix} = \frac{1}{\lambda} \approx \frac{1}{0.71/\sigma_{\text{tr}}(\mathbf{E})} = \frac{1}{0.71\lambda_{\text{tr}}}$$
or
$$\varphi(\mathbf{r}, \mathbf{E}) = 0 \text{ at extrapolated boundary}$$
(158)

Black boundary

(158)

^{*}Note that only in the Fermi approximation does the assumption (152b) remain valid as the group intervals approach zero.

ï

ented by

ves in it

1 abstr

where the extrapolated boundary is approximately  $0.71\lambda_{tr}$  removed from the actual boundary. In regions larger in extent than a few transport paths (size  $\gg \lambda_{tr}$ ), an accurate and enormously simplifying approximation is to choose an effective extrapolation length or extrapolated boundary as valid for all energies. A simple and physically reasonable choice* is that which correctly gives the total leakage. This leads in the case of condition (157) to a valve  $\lambda_{tr}^{eff}$  given by:

$$\lambda_{\text{tr}}^{\text{eff}} = \frac{\int \lambda_{\text{tr}}(\mathbf{E}) \ \varphi(\underline{\mathbf{r}}, \mathbf{E}) \ d\mathbf{E}}{\int \varphi(\underline{\mathbf{r}}, \mathbf{E}) \ d\mathbf{E}} \bigg|_{\text{at boundary}}$$
(159)

The black-boundary conditions on  $q(\underline{r}, E)$  and  $q(\underline{r}, \tau)$  are, in Fermi age theory, Eq. (111), identical with those on  $\varphi(\underline{r}, E)$ . In the Wigner and G. G. approximations, Eq. (127), the q boundary conditions are more complicated, involving a combination of q and  $\partial q/\partial E$ :

Interface 
$$\begin{cases} \varphi(\underline{r}, \mathbf{E}) = \text{continuous} \end{cases}$$
 (160) 
$$\mathbf{D} \text{ grad } \varphi(\underline{r}, \mathbf{E}) = \text{continuous}$$
 (161)

These conditions also apply in age theory to  $q(\underline{r}, E)$  but not directly to  $q(\underline{r}, \tau)$  when  $\tau$  is a different function of energy in the two media.

Improvements on Eqs. (157) and (158) are given in Tables 1.3.11 and 1.3.12 and Eqs. (81) to (88).

## THE IMAGE METHOD

Finite-region problems, involving the black-boundary condition (158), may often be solved in terms of the infinite-medium solutions.

Thus, for example, the solution in Table 1.3.15 of the aging in an infinite column owing to a point source at  $x_0$ ,  $y_0$ , z=0 is represented as a sum of the infinite-medium solutions corresponding to the actual source and to its images at:  $(x_0+2a1, y_0+2bm)^+$ ,  $(x_0-2a1, y_0-2bm)^+$ ,  $(x_0+2a1, y_0-2bm)^-$ , and  $(x_0-2a1, y_0+2bm)^-$ , where (1) and (m) run from  $-\infty$  to  $+\infty$ . The image sources all have the same strength as the actual source and have signs indicated by the superscript. The magnitudes and positions of the images are arranged so that they negate the contribution of the actual source to the solution at the boundary.

Another example is the problem of a plane source in a semi-infinite medium. The solution in this case is the sum of the infinite-medium solutions for the actual source and for its mirror image, the latter with a negative sign.

Problems involving spherical symmetry may be attacked by transforming to the equivalent plane problem, and then applying images. The solution in Table 1.3.15 of the point source at the center of a finite sphere may be obtained in this manner. The equivalent source and its images are dipoles in this case.

## DIFFUSION OF THERMAL NEUTRONS

Wigner and Wilkins ("Thermal Distributions," above) have treated the problem of the energy spectrum of thermal neutrons in the absence of diffusion. The absence of similar

^{*}A better, but more complicated choice for  $\lambda_{tr}^{eff}$  is the spectral average of  $\lambda_{tr}$  weighted with the proper adjoint function (cf. perturbation theory in 1.4 and the importance function in 1.6),

results on the more difficult problem of thermal diffusion restricts the following to simple considerations only.

## **DIFFUSION EQUATIONS**

Assuming no low-energy-source neutrons, the diffusion equation (109) for a homogeneous medium may be written as:

$$D\nabla^{2}\varphi(\underline{\mathbf{r}},\mathbf{E}) - \sigma_{\mathbf{a}}\varphi(\underline{\mathbf{r}},\mathbf{E}) + \frac{\partial \overline{\mathbf{q}}(\underline{\mathbf{r}},\mathbf{E})}{\partial \mathbf{E}} = 0$$
 (162)

where D and  $\sigma_a$  depend on the neutron energy and, for energies within the thermal region (E  $\sim$  KT), on the temperature* of the medium. The quantity  $\overline{q}(r,E)$  is still defined by Eq. (3) for E above the thermal range. For energies within the thermal range, it is defined as the net number† of neutrons crossing below the energy E and is no longer given by Eq. (3). Integration of Eq. (162) between the limits E = 0 and  $E = E_{th} \equiv$  an energy above which thermal effects are unimportant, I results in:

$$D_{th}\nabla^2\Phi_{th}(\underline{\mathbf{r}}) - \sigma_{\mathbf{a},th}\Phi_{th}(\underline{\mathbf{r}}) + q(\underline{\mathbf{r}},E_{th}) = 0$$
 (163a)

where:

$$\Phi_{\text{th}}(\underline{\mathbf{r}}) = \int_0^{E_{\text{th}}} \varphi(\underline{\mathbf{r}}, \mathbf{E}) d\mathbf{E}$$
 (163b)

and is the total thermal flux:

$$D_{th} = \frac{1}{\Phi_{th}(\underline{r})} \int_{0}^{E_{th}} D(\underline{E}) \varphi(\underline{r}, \underline{E}) d\underline{E}$$
 (163c)

$$\sigma_{\mathbf{a},\text{th}} = \frac{1}{\Phi_{\text{th}}(\underline{\mathbf{r}})} \int_{0}^{E_{\text{th}}} \sigma_{\mathbf{a}}(\mathbf{E}) \varphi(\underline{\mathbf{r}},\mathbf{E}) d\mathbf{E}$$
 (163d)

and  $q(\underline{r},E_{th})$  is obtainable by previously discussed methods.

The boundary conditions that are generally used are the group conditions (143) and (144).

## ENERGY-INDEPENDENT CROSS SECTIONS

When D(E) and  $\sigma_a(E)$  do not depend on the energy, the thermal flux satisfies the one-velocity diffusion equation. For this case, in fact, all the one-velocity results of the discussion of "One-velocity Theory" are valid⁵⁸ for  $\Phi_{th}(\underline{r})$ . According to Eq. (162), the spec-

 $[\]uparrow$ This ambiguity in the choice of  $E_{th}$  is a necessary consequence of any such simple considerations.  $\uparrow$ Eq. (163c) is valid only if  $D_{th}$  is a slowly varying function of position. Note that this happens whenever the spectrum changes with position.



^{*}The cross sections depend on the velocity distribution of the target nuclei, especially for light nuclei.

 $[\]uparrow$ A thermal neutron may increase in energy following a collision. Thus, g(E,E') and G(E,E') are no longer zero for E' < E.

trum  $\phi(E)$  in a Laplacian mode* is the same as the spectrum obtained without diffusion in a medium of effective cross section:

$$\sigma_a^{\text{eff}} = \sigma_a + DB^2$$

being close to Maxwellian if  $\sigma_a^{eff}/\sigma_s \ll 1$ .

## **ENERGY-DEPENDENT CROSS SECTIONS**

Statements may be made concerning the case of energy-dependent cross sections if the spectrum is assumed to be uniform throughout space. This assumption leads to space-independent parameters given by Eqs. (163c and d) in terms of which the diffusion length† L is given as:

$$L^2 = D_{th}/\sigma_{a,th} \tag{164}$$

The spectrum is close to Maxwellian for  $\sigma_a(E)/\sigma_s(E)\ll 1$ . The above remarks concerning Laplacian modes also apply here. The stronger assumption of "complete amnesia" leads to a spectrum of the form  $\sigma_s/(\sigma_s+\sigma_a)$  times a Maxwellian, at positions removed from a localized source of thermal neutrons. Maxwellian averages of  $1/v^n$  cross sections are listed in Table 1.3.7.

Two interesting cases in which the assumption of a uniform spectrum is very poor are (1) the diffusion in a block of high-atomic-weight material (such as uranium) in which case⁶⁰ the neutrons of each energy diffuse practically independently, resulting in a hardening effect for a 1/v absorber, and (2) the diffusion in a large block of crystalline matter with very small absorption cross section, (such as a graphite thermal column), in which case,^{61,62} the softening effect of the very low scattering cross section; may overbalance the absorption hardening and lead to the production of "cold" neutrons.

#### REFERENCES

- 1. Placzek, Phys. Rev. 69, 1946, p 426.
- 2. Edlund, ORNL-1154, p 63 (classified).
- 3. Goertsel, TAB-53, July 1950 (classified).
- 4. Shapiro and Preiser, ORNL-1176, Nov. 1951 (classified).
- 5. Young, CF-47-11-551, p 14 (classified).
- 6. Shapiro, unpublished.
- 7. Wigner and Wilkins, AECD-2275.
- 8. Cohen, HKF-102, pp 3.15 (classified).
- 9. Biehl and Cohen, TID-72, p 93 (classified).
- 10. Marshak, Prankel, and Nelson, LADC-79.
- 11. M. H. L. Pryce, MSP-2 (classified).
- 12. K. Puchs, MS-85.
- 13. B. Carlson, ABCD-2835.
- 14. Marshak, Phys. Rev. 71, 1947, p 688.
- 15. B. Davison, Phys. Rev. 71, 1947, p 694.
- 16. G. Placzek and G. M. Volkoff, MT-4, April 1943 (classified).
- 17. P. R. Wallace and J. Le Caine, NRC-1480.
- 18. A. M. Weinberg and L. C. Noderer, CF-51-5-98 (classified).
- 19. B. Davison, CRT-358, NRC-1636, June 1946.
- 20. B. Davison, MT-88.
- 21. B. Davison, MT-93.
- 22, B. Davison, MT-97 (classified).

^{*} $\nabla^2 \varphi = -B^2 \varphi$ , D being independent of position.

[†]Equation (164) is more often used to obtain  $D_{th}$  in terms of experimental values of  $\sigma_{a,th}$  and  $L^2$ . the energies below which Bragg scatterings disappear.

- 23. B. Davison, MT-135,
- 24. B. Davison, MT-207.
- 25. B. Davison and S. Kushneriuk, MT-214.
- 26. C. Mark, NRC-1588.
- 27. C. Mark, NRC-1589.
- 28. G. C. Wick, Z. Physik, 121, 1943, p 702.
- 29. S. Chandrasekhar, Radiative Transfer, Oxford Univ. Press, New York, 1951.
- 30. S. Frankel and E. Nelson, LADC-76.
- 31. S. Frankel and E. Nelson, LADC-79.
- 32. S. Frankel and S. Goldberg, AECD-2058.
- 33. G. Placzek and W. Seidel, Phys. Rev. 72, 1947, p 550.
- 34. H. Margenau and G. M. Murphy, The Mathematics of Physics and Chemistry, D. Van Nostrand Co., Inc., New York, 1943, p 462.
- 35. H. Margenau and G. M. Murphy, The Mathematics of Physics and Chemistry, D. Van Nostrand Co., Inc., New York, 1943, p 464, Table 6.
- 36. Frankel and Goldberg, loc. cit., p 34.
- 37. P. R. Wallace and J. Le Caine, MT-12.
- 38. Nucleonics 4, Feb. and March 1949.
- 39. Bellman, Marshak, and Wing, Phil. Mag., Series 7, 40, March 1949, p 297.
- 40. F. L. Priedman, CP-1073, Oct. 27, 1943.
- 41. Young, loc. cit., p 5.
- 42. L. Halpern and J. G. Beckerly, Lecture Notes from Fermi, AECD-2664, p 61.
- 43. Weinberg and Noderer, loc. cit., vol. 1, p III-43.
- 44. R. E. Marshak, Rev. Mod. Phys. 19, July 1947, p 235.
- 45. Weinberg and Noderer, loc. cit., p III-44.
- 46. R. E. Marshak, H. Brooks, and H. Hurwitz, Jr., Nucleonics 5, No. 2, Aug. 1949, pp 59-68.
- 47. H. A. Bethe, L. Tonks, and H. Hurwitz, Jr., Phys. Rev. 80, 1950, p 11.
- 48. G. C. Wicks, Phys. Rev. 75, 1949, p 738.
- 49. G. Placzek, A-25, 1941.
- 50. L. D. Roberts, J. E. Hill, and G. McCammon, ORNL-201, 1950.
- 51. G. Placzek and Volkoff, Can. Jour. Res. A25, 1947, p 276.
- 52. G. Geortzel and M. Nelkin, unpublished data.
- 53. R. E. Marshak, Rev. Mod. Phys. 19, No. 3, 1947, p 185.
- 54. E. Fermi, Recerca sci. 7, 1936, p 13.
- 55. Safonov, R-233 (classified).
- 56. B. Davison, LT-18.
- 57. Feynman, Welton, et al, LA-524 (classified).
- 58. Weinberg and Noderer, loc. cit., p I-19.
- 59. Weinberg and Noderer, loc. cit., p I-39.
- 60. Weinberg and Noderer, loc. cit., p I-36.
- 61. Halpern and Beckerly, loc. cit., p 1-30
- 62. Hughes, Pile Neutron Research, Chapters 9 and 10.
- 63. J. C. Mark, The Spherical Harmonics Method I and II, CRT-338, NRC-1589, June 1947.

## SELECTED READING LIST

THE ELEMENTS OF NUCLEAR REACTOR THEORY, S. Glasstone and M. C. Edlund, D. Van Nostrand Co., Inc.

THEORY OF NEUTRON CHAIN REACTIONS, A. M. Weinberg and L. C. Noderer, 2 volumes.

INTRODUCTION TO THE THEORY OF DIFFUSION AND SLOWING-DOWN OF NEUTRONS, R. E. Marshak, H. Brooks, and H. Hurwitz, Jr., Nucleonics 4, No. 5, 1949, pp 10-28; 4, No. 6, 1949, pp 43-49; 5, No. 1, 1949, pp 53-60; 5, No. 2, 1949, pp 59-68.

THEORY OF SLOWING-DOWN OF NEUTRONS BY ELASTIC COLLISION WITH ATOMIC NUCLEI, R. E. Marshak, Rev. Mod. Phys. 19, 1947, p 185.

TRANSPORT THEORY OF NEUTRONS, B. Davison, LT-18.

ON THE THEORY OF THE SLOWING DOWN OF NEUTRONS IN HEAVY SUBSTANCES, G. Placzek, Phys. Rev. 69, 1946, p 423.

## CHAPTER 1.4

# Reactor Statics; Theory and General Results

Harry Soodak

#### REACTORS WITHOUT SPACE VARIATION

## **CRITICALITY**

In terms of the neutron-energy spectrum (see Chapter 1.3), the critical equation for an infinite homogeneous medium is:

$$k = \frac{\int_0^\infty \nu \sigma_f \, \text{nv dE}}{\int_0^\infty \sigma_B \, \text{nv dE}} = 1 \tag{1}$$

If the neutrons are created at a single energy which they retain until absorbed, Eq. (1) reduces to:

$$k = \nu F = 1$$

where:

$$F = utilization = \sigma_f/\sigma_a$$

if  $\nu$  and F are independent of energy, this holds regardless of the fission-source spectrum and the slowing-down processes. If fissions are caused only by thermal neutrons,  $k = \nu pF = 1$  applies, where p is the probability of escaping capture while slowing down. Allowing for fast-fission multiplication by a factor  $\epsilon$ , the last relationship becomes:

$$k = \nu \epsilon pF = 1$$

which* is familiar in thermal reactors.

#### AIDS TO COMPUTATION

Determination† of systems or compositions satisfying Eq. (1) or obtaining relatively good values for k despite inaccuracies in determining the slowing-down spectrum is facilitated

^{*}Frequently written as:  $k = \eta \epsilon pf = 1$  where  $\eta = \nu \left(\frac{\sigma_f}{\sigma_a}\right)_{\text{fuel}}$  and  $f = \frac{\sigma_a \text{ (fuel)}}{\sigma_a \text{ (total)}}$ 

[†]In special cases, such as those noted below Eq. (1), this may follow directly; in general, it does not, and repeated trials or other procedures are needed.

by perturbation, variation, and iteration techniques (cf. the last part of this chapter). The following illustrates the use of perturbation methods in adjusting fuel content to make a system critical. Assuming  $\nu$  to be constant and splitting off the thermal group (Chapter 1.3) yields the steady-state balance equations:

$$\frac{\partial n(\mathbf{E})}{\partial t} = \mathbf{0} = \nu \chi(\mathbf{E}) \int_{\mathbf{E}_{1b}}^{\infty} \varphi \sigma_{\mathbf{f}} d\mathbf{E}' + \nu \chi(\mathbf{E}) \varphi_{\mathbf{th}} \sigma_{\mathbf{f}_{\mathbf{th}}} + \int_{\mathbf{E}_{1b}}^{\infty} \mathbf{g}(\mathbf{E}, \mathbf{E}') \sigma_{\mathbf{g}} \varphi(\mathbf{E}') d\mathbf{E}' - \sigma \varphi$$
 (2)

$$\frac{\partial n_{th}}{\partial t} = 0 = \int_{E_{th}}^{\infty} G(E_{th}, E) \sigma_{s} \varphi(E) dE - \sigma_{a_{th}} \varphi_{th} = q_{th} - \sigma_{a_{th}} \varphi_{th}$$
(3)

where:

$$\sigma = \sigma_s + \sigma_a + \sigma_f$$

 $\varphi(E) = vn(E)$  and  $\chi(E)$  is the normalized fission spectrum. In this case, the criticality condition is:

$$k = p\nu \frac{\sigma_{f_{th}}}{\sigma_{a_{th}}} + (1 - p)\nu \frac{\int_{E_{th}}^{\infty} \sigma_{f} \varphi dE}{\int_{E_{th}}^{\infty} \sigma_{a} \varphi dE} = 1$$
(4)

where:

$$p = \sigma_{a_{th}} \varphi_{th} / \left( \int_{E_{th}}^{\infty} \sigma_{a} \varphi dE + \sigma_{a_{th}} \varphi_{th} \right)$$

The equations adjoint to Eqs. (2) and (3) are:

$$\frac{1}{v\sigma}\frac{\partial m(E)}{\partial t} = 0 = v \frac{\sigma_f}{\sigma} \int_{E_{th}}^{\infty} m\chi dE + \frac{\sigma_s}{\sigma} \int_{E_{th}}^{E} m(E')g(E',E)dE' - m + \frac{\sigma_s}{\sigma} G(E_{th},E)m_{th}$$
 (5)

$$\frac{1}{v_{th}\sigma_{a_{th}}}\frac{\partial m_{th}}{\partial t} = 0 = \nu \frac{\sigma_{f_{th}}}{\sigma_{a_{th}}} \int_{E_{th}}^{\infty} m\chi dE - m_{th}$$
 (6)

The solution of these equations is:

$$m_{th} = \frac{\sigma_{f_{th}}}{\sigma_{a_{th}}} \ \nu \overline{m} \tag{7a}$$

$$\mathbf{m}(\mathbf{E}) = \nu \overline{\mathbf{m}} \left\{ \int_{\mathbf{E}_{th}}^{\mathbf{E}} \sigma_{\mathbf{f}}(\mathbf{E}') \varphi(\mathbf{E}', \mathbf{E}) d\mathbf{E}' + q(\mathbf{E}_{th}, \mathbf{E}) \frac{\sigma_{\mathbf{f}_{th}}}{\sigma_{\mathbf{a}_{th}}} \right\}$$
(7b)

$$\overline{m} = \int_{E_{11}}^{\infty} m(E)\chi(E) dE$$
 (7c)

where  $\phi(E',E)$  and  $q(E_{th},E)$  are, respectively, the flux distribution at E' and thermal slowing-down density resulting from a unit source  $\delta(E'-E)$  at energy E.



The first-order perturbation formula comparing two critical reactors differing only in fuel content is:

$$\delta \mathbf{R} = \mathbf{0} = \frac{\delta \nu}{\nu} + \frac{\int_{E_{th}}^{\infty} \varphi \delta \sigma_{\mathbf{f}} d\mathbf{E} + \varphi_{\mathbf{th}} \delta \sigma_{\mathbf{f}_{\mathbf{th}}}}{\int_{E_{th}}^{\infty} \varphi \sigma_{\mathbf{f}} d\mathbf{E} + \varphi_{\mathbf{th}} \sigma_{\mathbf{f}_{\mathbf{th}}}} - \frac{\int_{E_{th}}^{\infty} m \varphi \delta \sigma_{\mathbf{a}} d\mathbf{E} + m_{\mathbf{th}} \varphi_{\mathbf{th}} \delta \sigma_{\mathbf{a}_{\mathbf{th}}}}{\nu \overline{\mathbf{m}} \left[ \int_{E_{th}}^{\infty} \varphi \sigma_{\mathbf{f}} d\mathbf{E} + \varphi_{\mathbf{th}} \sigma_{\mathbf{f}_{\mathbf{th}}} \right]}$$
(8)

where the  $\delta\sigma$  represent the change in the labeled cross section owing to the changed fuel content,  $\delta\nu$  is the change in the value of  $\nu$  required to satisfy the criticality condition* Eq. (4), and  $\varphi$  and m correspond to the calculated case for which the obtained  $\nu$  is different from its physical value. It has been assumed in Eq. (8) that the effect of the change in scattering cross section is negligible. On the basis of this assumption, Eq. (8) may also be used to estimate the change in critical mass owing to changing the fuel type. In this case,  $\delta\nu$  is the change in actual  $\nu$  value. If the fission spectrum is different, the term  $1/\overline{m} \int m\delta\chi(E)dE$  must be added to the right side of Eq. (8). This term may also be viewed as the effect on reactivity, R, resulting from the use of a fission spectrum inaccurate by  $\delta\chi(E)$ .

#### ONE-VELOCITY REACTORS

For one-velocity reactors without any external source, Eq. (17) in Chapter 1.3 can be used with S replaced by the fission source:

$$S(\underline{r},\underline{\Omega},t) = \frac{1}{4\pi} \sigma_{f} \int F(\underline{r},\underline{\Omega},t) d\underline{r}$$

and the integral equation, Eq. (23) in Chapter 1.3, is true with  $S(\underline{r}') = 0$  and with 1 + f defined as in Eq. (22), Chapter 1.3:

$$1 + f = \frac{\sigma_{S} + \nu \sigma_{f}}{\sigma}; \quad \sigma = \sigma_{f} + \sigma_{c} + \sigma_{s}$$
 (9)

## BARE REACTORS

## THE ITERATIVE METHOD

The critical radius of a bare sphere can be computed to any degree of accuracy by an iterative method used by Placzek and reported by Carlson. The method, applicable as well for anisotropic scattering, uses a polynomial trial function in Eq. (26), Chapter 1.3, and matches the moments of the trial function and its first iterate. Results obtained by use of a quadratic trial function are given in Table 1.4.1, for the case of a linear scattering law in the laboratory system. The parameter  $\alpha$  is defined as:

$$\alpha = 3 \cos \theta \, \sigma_{\rm e} / \sigma \tag{10}$$

where  $\cos \theta$  is the average cosine of the angular deflection in scattering.

^{*}The criticality condition is here regarded as the determining equation for  $\nu$  even though the value thus obtained generally differs from the known physical value.

¹References appear at end of chapter.

Table 1.4.1 — Bare-sphere Critical Radius ( $\sigma$ a) in Units of Mean Free Path ( $1/\sigma$ ) as Computed by Quadratic Iteration

(LADC-756)

f	$\alpha^* = -1.0$	$\alpha$ * = -0.5	$\alpha$ * = 0.0	$\alpha$ * = 0.5	$\alpha$ * = 1.0
0.0	•••	•••	•••	•••	• • •
.1	4.333	4.585	4.895	5.276	5.770
.2	2.846	2.997	3.178	3.396	3.678
.4	1.8081	1.8907	1.9871	2.1015	2,2408
.6	1.3593	1.4140	1.4769	1.5498	1.6364
.8	1.0993	1.1388	1.183 <b>8</b>	1.2350	1.2946
1.0	0.9269	0.9570	0.9909	1.0290	1.0728
1.2	.8031	.8270	.8535	0.8831	0.9167
1.4	.7094	.7289	.7503	.7740	.8005
1.6	.6359	.6521	<b>.6</b> 697	.6892	.7108
1.8	.5766	.5902	.6050	.6212	.6393
2.0	.5276	.5394	.5520	.5656	.5808
<b>e0</b>	.0000	.0000	.0000	.0000	.0000

$$*\alpha = \frac{3\sigma_s}{\sigma} \overline{\cos \theta}$$

## THE END-POINT METHOD

The end-point method considers the asymptotic (away from boundaries) solution satisfying:

$$\nabla^2 \varphi + (\kappa \sigma)^2 \varphi = 0 \tag{11}$$

where, for linear anisotropy:

$$(1+f)\frac{\tan^{-1}\kappa}{\kappa} - \frac{\alpha f}{\kappa^2} \left(1 - \frac{\tan^{-1}\kappa}{\kappa}\right) = 1$$
 (12)

The method then proceeds to calculate the extrapolated end point,  $z_0$ . The shape of  $\phi$  and the critical size for a few simple geometries* are as presented in Table 1.4.2. Values of  $z_0$  as a function of 1 + f and of  $b = \sigma_s \overline{\cos \theta}/(\sigma_s + \nu \sigma_f)$  are given in Table 1.3.11 where, for f significantly different from zero, terms in  $b^2$  have been neglected.

## THE SERBER-WILSON METHOD

The Serber-Wilson method is the only method mentioned that generalizes for reflected reactors and is discussed later.

## COMPARATIVE ACCURACY OF THE METHODS³

The error in critical radius of a bare sphere: (a) for the end-point method, increases from 0 to  $\sim$ 0.2% as 1 + f increases from 1 to 3; (b) for the Serber-Wilson method, increases

^{*} The method is strictly applicable only in the case of the bare sphere. Compare Ref. (2).

Table 1.4.2 — Asymptotic Flux and Critical Size for Simple Geometries

Case	Flux	Critical size
Sphere (radius a)	sin Kor	$\sigma \mathbf{a} = \frac{\pi}{\kappa} - \mathbf{z_0}$
Slab (thickness 2a)	cos Kox	$\sigma a = \frac{\pi}{2\kappa} - z_0$
Cylinder (radius a)	J ₀ (κστ)	$\sigma a = \frac{2.405}{\kappa} - z_0$

rapidly from 0 to  $\sim$ 4% as 1 + f increases from 1 to 1.2, and then remains nearly constant at  $\sim$ 4% for higher values of 1 + f; (c) for the iterative method with a quadratic trial function, decreases from  $\sim$ 0.2% to 0 as 1 + f increases from 1.2 to  $\infty$ ; the iterative method breaks down for f near zero.

## THE TRANSPORT APPROXIMATION*

The transport approximation reduces an anisotropic problem to the far simpler isotropic problem. The "isotropic equivalent" scattering cross section is chosen to be:

$$\sigma_{\rm tr} = \sigma_{\rm g} (1 - \overline{\cos \theta}) \tag{13}$$

Thus, the anisotropic case may be treated by the above methods with:

$$\sigma = \sigma_{f} + \sigma_{c} + \sigma_{tr}$$

$$1 + f = \frac{\sigma_{tr} + \nu \sigma_{f}}{\sigma}$$
(14)

 $\overline{\cos \theta} = 0$ 

Results obtained in this approximation by use of quadratic iteration are compared in Fig. 1.4.1 to those of Table 1.4.1 for the case of linear scattering in a bare sphere. That the transport approximation is very accurate for f near zero (reactors greater in size than a few mean free paths) in the case of linear scattering is also exhibited by Table 1.3.11.

## REFLECTED REACTORS

The end-point method can be applied to reflected reactors in the special case that core and reflectors all have the same total cross section. Derivations of equations and numerical tables are reported by Frankel and Goldberg⁴ for the case of isotropic scattering. Anisotropic scattering may be treated by the transport approximation.

The Serber-Wilson method is more general than the end-point method in that equality of total cross section in the various media is not required. The case of isotropic scattering and spherical symmetry has been extensively reported.^{5,6,7,8} Other geometries and anisotropic scattering are discussed by Davison,⁷ pp 94 and 155. Anisotropic scattering may be treated by the transport approximations.

^{*}Compare Chapter 1.3.

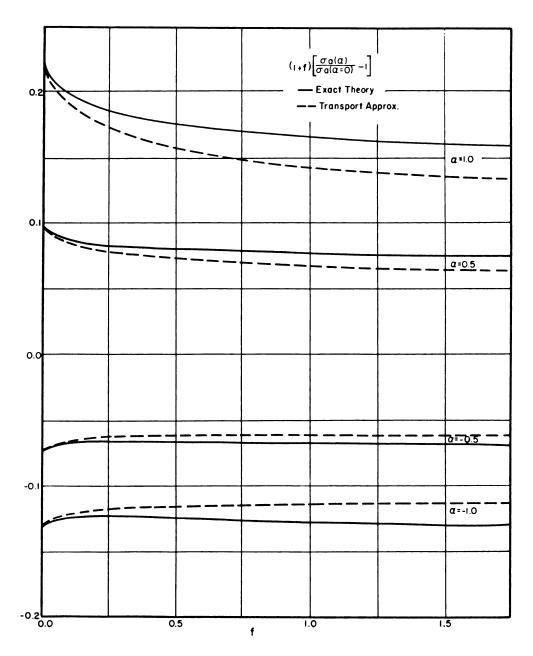


Fig. 1.4.1 — Comparison of Bare-sphere Critical Sizes with and without Transport Approximation for Linear Scattering Laws for Various Amounts of Anisotropy. Reprinted from LA-1061 (LADC-756). The quantity  $1+f=\sigma_s+\nu\,\sigma_f/\sigma$  times the fractional change in critical radius due to anisotropy as computed by quadratic iteration is plotted against f for various values of  $\alpha=3(\sigma_s/\sigma)\,\overline{\cos\theta}$ , with and without the transport approximation.

The accuracy of the Serber-Wilson method is greater in the case of reflected reactors than for bare reactors. The method underestimates the critical radius, the error⁶ (less than 2 percent) being nearly the same under a wide variety of conditions.

## THE SERBER-WILSON METHOD

The Serber-Wilson method deals with the asymptotic solutions in each region which, for spherical symmetry, are:

$$\varphi_{\rm c} = A_{\rm c} \frac{\sin \kappa_{\rm c} \sigma_{\rm c} r}{\kappa_{\rm c} \sigma_{\rm c} r} \tag{15}$$

$$\varphi_{i} = A_{i} \frac{e^{-\kappa_{i}\sigma_{i}r}}{\kappa_{i}\sigma_{i}r} + B_{i} \frac{e^{+\kappa_{i}\sigma_{i}r}}{\kappa_{i}\sigma_{i}r}$$
(16)

where  $\phi = vn(r)$  is the flux, "c" denotes the core, and "i" denotes the ith reflector. The cross section,  $\sigma$ , is the total cross section given by Eq. (14) in the transport approximation. In the same approximation,  $\kappa_c$  and  $\kappa_i$  are given by:

$$\frac{\tan^{-1}\kappa_{c}}{\kappa_{c}} = \frac{1}{1 + f_{c}} \tag{17}$$

$$\frac{\tanh^{-1}\kappa_{i}}{\kappa_{i}} = \frac{1}{1+f_{i}} \tag{18}$$

Extension to the case of a multiplying  $(f_i > 0)$  reflector presents no added difficulty. Neutron conservation implies continuity of the current density j(r):

where for any Laplacian mode, j(r) is given by:*

$$j(r) = -\frac{|f|}{\kappa^2 \sigma} \operatorname{grad} \varphi \tag{20}$$

Thus:

$$j_{c}(r) = A_{c} \frac{f}{\kappa^{2} \sigma r} \left( \frac{\sin \kappa \sigma r}{\kappa \sigma r} - \cos \kappa \sigma r \right)$$
 (21)

$$j_{i}(\underline{\mathbf{r}}) = \frac{|\mathbf{f}|}{\kappa^{2}\sigma\mathbf{r}} \left[ \mathbf{A}_{i} e^{-\kappa\sigma\mathbf{r}} \left( 1 + \frac{1}{\kappa\sigma\mathbf{r}} \right) - \mathbf{B}_{i} e^{+\kappa\sigma\mathbf{r}} \left( 1 - \frac{1}{\kappa\sigma\mathbf{r}} \right) \right]$$
 (22)

where subscripts have been omitted from the right sides.

In place of the boundary conditions on the flux  $\phi$  (cf, Chapter 1.3), the method uses the "Serber condition" which requires that the integral Eq. (23), Chapter 1.3, be satisfied at the center of symmetry. This, however, gives only one equation, and this is sufficient only in the case of a bare reactor or a single infinite reflector. In other cases, the missing

^{*}Eq. (20) is a generalization of Eqs. (70) and (71), Chapter 1.3, being valid for f > 0 as well as for f < 0.

equations are supplied by satisfying the Serber condition "in detail."* In the spherical case under consideration, the Serber condition "in detail" reduces to the Wilson conditions that:

 $\phi(r,-1) = continuous$  at boundaries

 $\phi(r,-1) = 0$  at outer boundary

where  $\phi(\mathbf{r},-1)$  is the radially inward flux at  $\mathbf{r}$  computed as if the media to the left and right of the boundary each extended to infinity. For the asymptotic solutions,  $\phi(\mathbf{r},-1)$  is given by:

$$4\pi\varphi_{c}(\mathbf{r},-1) = \mathbf{A}_{c} \frac{(1+\mathbf{f})}{\kappa} e^{\sigma \mathbf{r}} \mathbf{I}_{m} \mathbf{E}_{1}(\sigma \mathbf{r}[1-\mathbf{i}\kappa])$$
(23)

$$4\pi\varphi_{\mathbf{i}}(\mathbf{r},-1) = \frac{(1+\mathbf{f})}{\kappa} e^{\sigma \mathbf{r}} \left\{ \mathbf{A}_{\mathbf{i}} \mathbf{E}_{\mathbf{i}}(\sigma \mathbf{r}[1+\kappa]) + \mathbf{B}_{\mathbf{i}} \mathbf{E}_{\mathbf{i}}(\sigma \mathbf{r}[1-\kappa]) \right\}$$
(24)

For criticality computations, it is sufficient to apply the conditions:

$$\mathbf{F}(\sigma\mathbf{r},\mathbf{f}) = \frac{4\pi\varphi(\mathbf{r},-1)}{\mathbf{j}_{(\text{normal})}(\mathbf{r})} = \text{continuous at inner boundaries}$$
 (25)

$$\phi(\mathbf{r},-1)=0$$
 at outer boundary. (26)

## NUMERICAL RESULTS

Numerical results are easily obtained in the case of a single reflector, whether finite or infinite. The critical equation for this case is:

$$\mathbf{F}_{c}(\sigma_{c} \mathbf{a}, \mathbf{f}_{c}) = \mathbf{F}_{1}(\sigma_{1} \mathbf{a}, \mathbf{f}_{1}, \gamma) \tag{27a}$$

where:

$$a = core radius$$
 (27b)

$$\gamma a = \text{outer radius}$$
 (27c)

The parameter  $A_c$  does not appear in  $F_c$ , and the parameters  $A_1$  and  $B_1$  are eliminated from  $F_1$  by use of condition (26).

Figure 1.4.2 plots  $F_c$  as a function of  $\sigma_c$ a for values of  $f_c$  ranging from 0.02 up to 2.0. Figure 1.4.3 plots  $F_1$  for an infinite reflector ( $\gamma = \infty$ ) as a function of  $\sigma_1$ a for values of  $f_1$  ranging from 0 to -0.8. Figures 1.4.4 to 1.4.8 plot for  $f_1 = 0$ , -0.02, -0.05, -0.1, and -0.2  $F_1$  as a function of  $\sigma_1$ a for several values of  $\gamma$  ranging from 1.1 to  $\infty$ .

If any of the  $F_1$  plots is superposed[‡] on Fig. 1.4.2 with the  $\sigma a$  axes coinciding but with the origin ( $\sigma_1 a = 0.1$ ,  $F_1 = 0.1$ ) of the  $F_1$  graph located at the point§ ( $\sigma_c a = 0.1$   $\sigma_c / \sigma_1$ ,  $F_c = 0.1$ ) of the  $F_c$  graph, then the solution for any given value of  $f_1$  and for any given  $f_c$  and  $\gamma$ 

^{*} Davison, 7 p 92.

 $[\]dagger \; E_1(x) = \int_1^{\infty} \frac{e^{-xt}}{x} \, dt, \; \text{and} \; I_m \; \text{signifies the imaginary part.}$ 

[‡] When either curve is redrawn as a transparency.

[§] This brings the two graphs into the same distance scale, the  $\sigma a$  scales being logarithmic.

is obtained from the  $\sigma_c$  a value or the  $\sigma_1$ a value at the point of intersection of the corresponding curves. The critical radius is given by:

$$\mathbf{a} = \frac{(\sigma_{c}\mathbf{a})}{\sigma_{c}} = \frac{(\sigma_{1}\mathbf{a})}{\sigma_{1}}$$

Sweeney, Goldstein, and Carlson⁹ present an extensive tabulation of functions in terms of which  $F(\sigma a, f)$  may be expressed.

## **DIFFUSION THEORY***

The one-velocity diffusion-theory equation for a homogeneous region is:

$$D\nabla^2 \varphi + (k-1) \sigma_a \varphi = 0 \tag{28}$$

where:

$$\mathbf{k} = \frac{\nu \sigma_{\mathbf{f}}}{\sigma_{\mathbf{a}}} = \frac{\nu \sigma_{\mathbf{f}}}{\sigma_{\mathbf{c}} + \sigma_{\mathbf{f}}} \tag{29}$$

is the multiplication constant. Thus:

$$\nabla^2 \varphi + B^2 \varphi = 0 \tag{30}$$

where:

$$B^2 = \frac{(k-1)\sigma_a}{D} = \frac{f\sigma}{D} \tag{31}$$

The buckling, B², is positive in a multiplying region, in which:

$$B^2 = (k\sigma)^2 \tag{32a}$$

and negative in a non-multiplying region, in which:

$$\mathbf{B}^2 = -(\mathbf{k}\sigma)^2 \tag{32b}$$

It follows that Eq. (28) gives correct asymptotic solutions for a linear scattering law if  $\kappa$  is given by Eq. (12) or by the equivalent  $\dagger$  equation for a non-multiplying medium. These equations lead to  $\dagger$  the following expressions for B² which for  $0 \le \overline{\cos \theta} \le 0.2$  are accurate to better than 1 percent in the stated f ranges:

$$0 \le f \le 1.5$$
  $B^2 = 3f\sigma^2 \left(1 - \frac{\sigma_8}{\sigma} \overline{\cos \theta}\right) (1 + 0.8060f)$  (33a)

$$-0.6 \le f \le 0$$
  $B^2 = 3f\sigma^2 \left(1 - \frac{\sigma_S}{\sigma} \overline{\cos \theta}\right) (1 + 0.7848f)$  (33b)

$$\dagger (1+f) \frac{\tanh^{-1}\kappa}{\kappa} + \frac{\alpha f}{\kappa^2} \left( 1 - \frac{\tanh^{-1}\kappa}{\kappa} \right) = 1$$

‡ Goldberger, unpublished. An equation usually written for f < 0 and  $\cos \theta = 0$  is:

$$-B^2 = 3\sigma \sigma_a \left(1 - 0.8 \frac{\sigma_a}{\sigma}\right) = -3f\sigma^2(1 + 0.8f)$$

^{*}See Chapter 1.3, "One-velocity Theory."

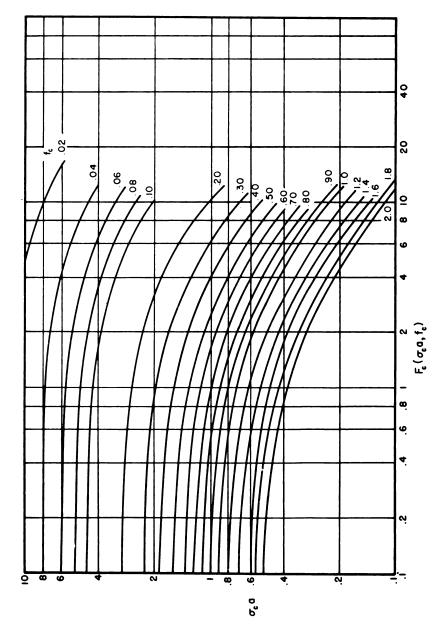


Fig. 1.4.2 —  $F_c(\sigma_c a, f_c)$  as Function of  $\sigma_c a$  for Various Values of  $f_c$ . From A.E.R.E. T/R-587.

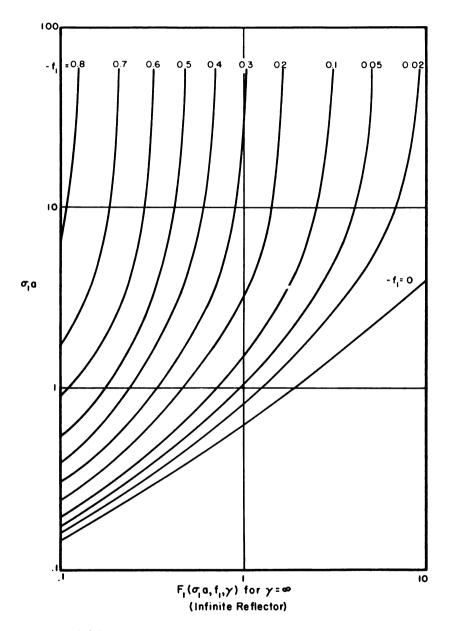


Fig. 1.4.3 —  $F_1(\sigma_1 a f_1, \gamma)$  for  $\gamma = \infty$  (Infinite Reflector) as Function of  $\sigma_1 a$  for Various Values of f. From A.E.R.E. T/R-586.

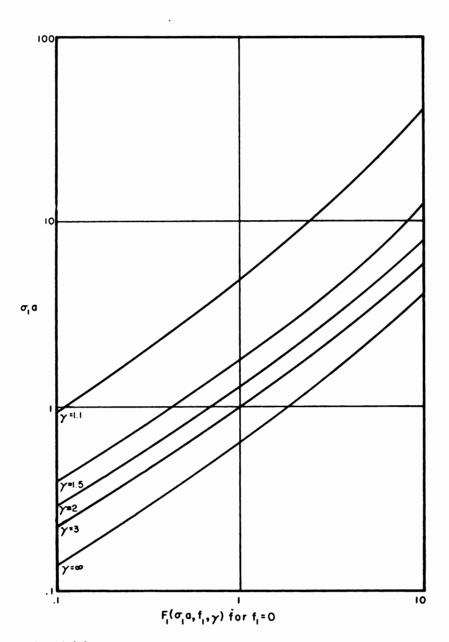


Fig. 1.4.4 —  $F_1(\sigma_1 a, f_1, \gamma)$  for  $f_1$  = 0 as Function of  $\sigma_1 a$  for Various Values of  $\gamma$ . From A.E.R.E. T/R-587.

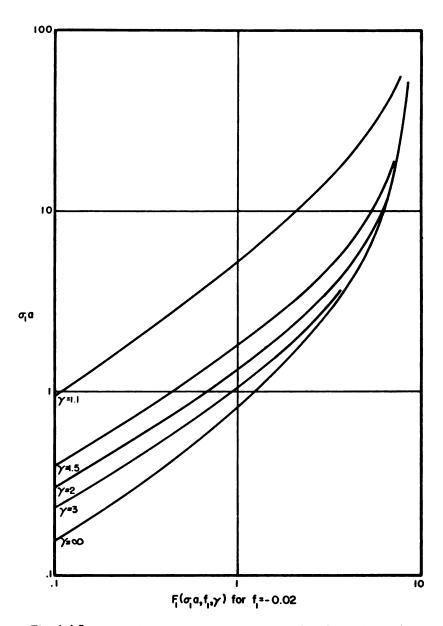


Fig. 1.4.5 —  $F_1(\sigma_1 a, f_1, \gamma)$  for  $f_1 = -0.02$  as Function of  $\sigma_1 a$  for Various Values of  $\gamma$ . From A.E.R.E. T/R-587.

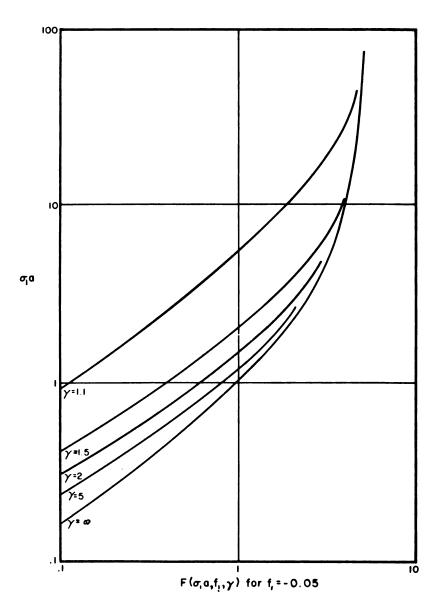


Fig. 1.4.6 —  $F_1(\sigma_1 a, f_1, \gamma)$  for  $f_1$  = -0.05 as Function of  $\sigma_1 a$  for Various Values of  $\gamma$ . From A.E.R.E. T/R-587.

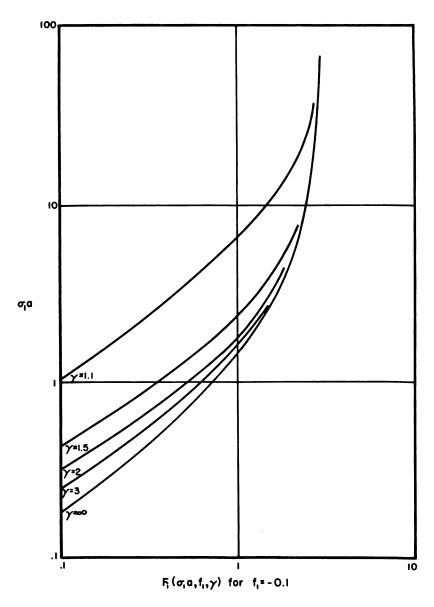


Fig. 1.4.7 —  $F_1(\sigma_1 a, f_1, \gamma)$  for  $f_1$  = -0.1 as Function of  $\sigma_1 a$  for Various Values of  $\gamma$ . From A.E.R.E. T/R-587.

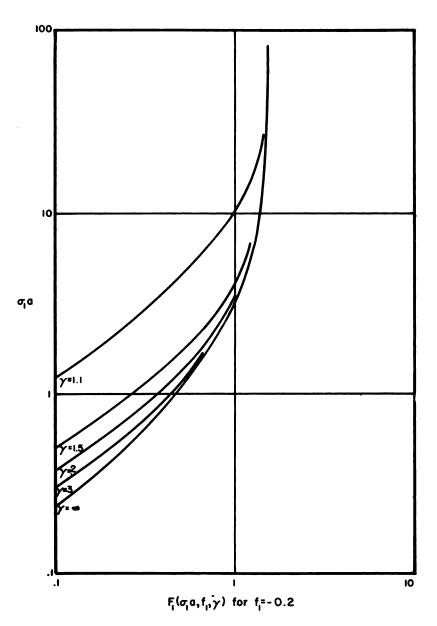


Fig. 1.4.8 —  $F_1(\sigma_1 a_i f_1, \gamma)$  for  $f_1 = -0.2$  as Functions of  $\sigma_1 a$  for Various Values of  $\gamma$ . From A.E.R.E. T/R-587.

The current density, j, is given by:

$$j = -D \operatorname{grad} \phi \tag{34}$$

and the boundary conditions are continuity of  $\phi$  and j (normal) at interfaces, and  $\phi = 0$  at an extrapolation length outside a black boundary. The diffusion constant, D, is given by:*

$$D = \frac{f\sigma}{B^2} (35)$$

### BARE REACTORS

In general, there are a discrete infinity of positive  $B^2$  values for which the solutions of Eq. (30) satisfy the  $\phi=0$  boundary condition. The lowest of these  $B^2$  values belongs to the fundamental  $\phi$  mode and is called the geometric buckling,  $B_g^2$ . The higher modest cannot correspond to the steady-state solution because they call for negative neutron densities. The critical equation is:

$$B_g^2 = B_m^2 \tag{36}$$

where the material buckling,  $B_m^2$ , is given by Eq. (31).

Table 1.4.3 presents, for some geometries, the fundamental mode along with the corresponding value of  $B_g^2$ . The actual reactor fills the volume of the geometrical shapes considered except for an extrapolation distance from the boundaries.‡ Other geometries which have been treated are the spheroid, ¹⁰ the right hexagonal cylinder; ¹¹ a truncated cone, ¹² and spherical segments. ¹³ The spherical sector is also treated elsewhere. ¹⁴

# Variational Principle

The geometric buckling may be obtained by a simple variational formula:

$$\delta I = 0$$

$$I = \int \varphi \nabla^2 \varphi d\underline{r} - B_g^2 \int \varphi^2 d\underline{r} = \int (grad \varphi)^2 d\underline{r} - B_g^2 \int \varphi^2 d\underline{r}$$
(37)

where:

$$\phi = \phi(\alpha_i)$$

is a trial function satisfying the  $\phi = 0$  boundary condition for all values of the parameters  $\alpha_i$ . The elimination of the  $\alpha_i$  from the equations:

$$\frac{\partial \mathbf{I}}{\partial \boldsymbol{\alpha}_i} = \mathbf{0}$$

^{*} In the P₁ approximation (Chapter 1.3), D =  $\lambda_{rr}/3$ .

[†]Only the fundamental has no zeros inside the extrapolated boundary. The higher modes decay in time and are useful as expansion functions in dynamic considerations.

[‡] This statement does not have a clear meaning for most of the considered geometries.

Table 1.4.3 - Fundamental Mode Solution and Geometric Buckling for Some Geometries; All

	Dimensions Are Extrapolated	apolated	
	(Adapted from Weinberg and Noderer, Ch. V)	Noderer, Ch. V)	
			Comments concerning volume, V, for given
Geometry	Mode, $\phi$	Buckling	buckling
Infinite slab (thickness a)	COS TX	$B_g^2=\pi^2/a^2$	
Infinite right circular cylinder (radius a)	J ₆ (2.405 r/a)	$B_g^2 = (2.405)^2/a^2$	·
Sphere (radius a)	sin 11/a 11/a	$B_g^2 = \pi^2/a^2$	$V_{sphere} = \frac{4}{3} \frac{\pi^4}{B^3}$
Rectangular parallelepiped (dimensions a, b, c)	$\cos \frac{\pi x}{a} \cos \frac{\pi y}{b} \cos \frac{\pi z}{c}$	$B_g^2 = \pi^2 \left( \frac{1}{a^2} + \frac{1}{b^3} + \frac{1}{c^2} \right)$	V is minimum for a = b = c, cube, V _{cube} = 1.240 V _{sphere}
Finite right circular cylinder (height H, radius a)	$\cos \frac{\pi a}{H} J_0 (2.405 r/a)$	$B_g^2 = \frac{\pi^2}{H^3} + \frac{(2.405)^2}{a^2}$	V is minimum for H = 1.85a; V _{sq cyl} = 1.142 Vsphere
Sector of a sphere where $\alpha$ is such that	$P_n(\cos\theta) \frac{J_{\mu,h}(\mu_h r/a)}{\sqrt{\mu_h r/a}}$	B ² = \\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	
$P_{\rm D}$ (cos $\alpha$ ) = 0 for. some integer n.	$\mu_n$ is first root of $J_{n_k} \psi(\mu_n) = 0$		
Hemisphere $(\alpha = \frac{\pi}{2}, n = 1)$ from above	μ ₁ = 4.49	$B_g^2 = \frac{(4.49)^2}{a^4}$	V hemisphere = 1.46 Vsphere
Sector of a cylinder of height H and cross-section	cos πε cosnθ Jn (μητ/a)	B	
(°)°	$\mu_{\rm n}$ is first root of $J_{\rm n}$ ( $\mu_{\rm n}$ ) = 0		
where $\alpha = \frac{\pi}{2l_n} (n = integer)$			
Right elliptic cylinder height H, semi-major axis a, eccen-	$\cos \frac{\pi s}{H} \sum_{m=0}^{\infty} A_{1m} \cos 2m\theta J_{1m} (B_g \Gamma)$		
a digital		0.8 (2.51) ³ /a ³ 0.85 (2.63) ³ /a ³ 0.9 (2.84) ³ /a ³ 0.94 (3.12) ³ /a ³	
Sphere of radius a with central black cavity of radius b	<u>1</u> sin # <u>r - b</u> r	$B_g^2 = \frac{r^2}{(a-b)^2}$	$a = \frac{\pi}{B_g} + b$

results in a value for  $B_g^2$  as a function of the geometry.* A numerical example is given for a sphere of radius "a":

$$B_g^2 a^2 = 14.0$$

for a trial function:

$$\phi = \alpha_1(\mathbf{r} - \mathbf{a})^2$$

and gives:

$$B_g^2 a^2 = 11.6$$

for a trial function:

$$\phi = \alpha_1(\mathbf{r} - \mathbf{a})^2 + \alpha_2(\mathbf{r} - \mathbf{a})^4$$

the correct result being:

$$B_{\sigma}^2 a^2 = \pi^2 = 9.87$$

Effect of Density on Critical Size

In the case that the reactor undergoes a uniform compression or dilation so that the final shape is geometrically similar to the initial shape, the following theorem is valid for all cases, including multivelocity reflected reactors.

THEOREM: In any critical system, if the density of all components is reduced (increased) uniformly, then to make the system again critical, all linear dimensions must be increased (reduced) by the same factor. Thus, if  $\rho$  is the factor by which the density is multiplied, all cross sections are multiplied by  $\rho$ , linear dimensions are divided by  $\rho$ , and the mass is divided by  $\rho^2$ .

For a reactor composed of a fluid contained in a tank of fixed shape, a uniform fluid-density change alters the geometry of the reactor. Tank shapes may be chosen¹⁶ so that the slope of the reactivity vs density curve is positive, negative, or zero.

# REFLECTED REACTORS

As in the Serber-Wilson method, the flux  $\phi$  in each homogeneous region is the solution of Eq. (30), which for spherical symmetry has the form given in Eqs. (15) and (16). The boundary conditions are simplified in that  $\phi$  is continuous and  $\phi = 0$  at extrapolated boundary replace the Serber conditions. The continuity of j (normal) is retained in order to conserve neutrons. For criticality computations, it is sufficient to use the conditions:

$$\frac{\phi}{j \text{ (normal)}} = \text{continuous at boundaries} \tag{38a}$$

$$\phi = 0$$
 at extrapolated boundary (38b)

Use of the diffusion theory relations in the transport approximation:

$$\mathbf{j_{+n}} = \frac{\varphi}{4} - \frac{\mathbf{D}}{2} \frac{\partial \varphi}{\partial \mathbf{n}} \tag{39a}$$

^{*}Some care must be taken in order to obtain the buckling in the fundamental mode, rather than in one of the higher modes.

$$j_{-n} = \frac{\varphi}{4} + \frac{D \partial \varphi}{2 \partial n}$$

$$(j_n = j_{+n} - j_{-n})$$
(39b)

where n denotes normal, + denotes outward, and - denotes inward, results in rewriting Eq. (38a) as:

a = continuous

where the albedo, a is given by:

$$a \equiv \frac{j_{-n}}{j_{+n}} = \frac{\frac{\varphi}{2j_{n}} - 1}{\frac{\varphi}{2j_{n}} + 1}$$
 (40a)

or:

$$\frac{\varphi}{2j_p} = \frac{1+a}{1-a} \tag{40b}$$

Tables 1.4.4 through 1.4.6 list for plane, spherical, and cylindrical geometries, the encountered  $\phi$ 's along with the corresponding formulas for j and  $\phi$ /j. In these tables as in the following remarks, the symbol B is defined as:

$$B = \sqrt{|B^2|} \tag{41}$$

so that it is real and positive in non-multiplying as well as multiplying media.

Table 1.4.4 — Useful One-group Functions; Plane Geometry, Coordinate x (Note: w = Bx) φ/j j  $\frac{1}{DR}$  cot w DB sin w cos w  $-\frac{1}{DR} \tan w$ sin w -DB cos w  $\frac{1}{DB} \frac{\cot w + \alpha}{1 - \alpha \cot w}$  $A(\cos w + \alpha \sin w)$ ADB( $\sin w - \alpha \cos w$ ) DB e-w  $\frac{1}{DB} \frac{1 + \alpha e^{2w}}{1 - \alpha e^{2w}}$  $A(e^{-w} + \alpha e^{w})$ ADB( $e^{-w} - \alpha e^{w}$ ) sinh B(b-x)DB cosh B(b - X)  $\frac{1}{DB}$  tanh B(b - X)

Table 1.4.5 — Useful One-group Functions; Spherical Geometry,

Coordinate r (Note: w = Br)

$$\frac{\sin w}{w} \qquad DB\left(\frac{\sin w}{w^2} - \frac{\cos w}{w}\right) \qquad \frac{1}{DB\left(\frac{1}{w} - \cot w\right)}$$

$$\frac{\cos w}{w} \qquad DB\left(\frac{\cos w}{w^2} + \frac{\sin w}{w}\right) \qquad \frac{1}{DB\left(\frac{1}{w} + \tan w\right)}$$

$$A\left(\frac{\sin w}{w} + \alpha \frac{\cos w}{w}\right) \qquad ADB\left[\frac{\sin w}{w}\left(\frac{1}{w} + \alpha\right) - \frac{\cos w}{w}\left(1 - \frac{\alpha}{w}\right)\right] \qquad \frac{1 + \alpha \cot w}{DB\left[\left(\frac{1}{w} + \alpha\right) - \left(1 - \frac{\alpha}{w}\right)\cot w\right]}$$

$$\frac{e^{-w}}{w} \qquad DB\left(\frac{e^{-w}}{w}\left(1 + \frac{1}{w}\right)\right) \qquad \frac{1}{DB\left(1 + \frac{1}{w}\right)}$$

$$A\left(\frac{e^{-w}}{w} + \alpha \frac{e^{w}}{w}\right) \qquad ADB\left[\frac{e^{-w}}{w}\left(1 + \frac{1}{w}\right) - \alpha \frac{e^{w}}{w}\left(1 - \frac{1}{w}\right)\right] \qquad \frac{1 + \alpha e^{2w}}{DB\left[\left(1 + \frac{1}{w}\right) - \alpha\left(1 - \frac{1}{w}\right)e^{2w}\right]}$$

$$\frac{\sinh B(b - r)}{Br} \qquad DB\left[\frac{\cosh B(b - r)}{Br} + \frac{\sinh B(b - r)}{B^2r^2}\right] \qquad \frac{1}{DB\left[\coth B(b - r) + \frac{1}{w}\right]}$$

Table 1.4.6 — Useful One-group Functions; Cylindrical Geometry, Coordinate r
(w = Br; notation is that of Brit. Assoc. Math. Tables)

φ	j	φ/ <b>j</b>
J ₀ (w)	DB J ₁ (w)	$\frac{1}{DB} \frac{J_0(w)}{J_1(w)}$
Y ₀ (w)	DB Y ₁ (w)	$\frac{1}{DB} \frac{Y_0(w)}{Y_1(w)}$
$A[J_{\theta}(w) + \alpha Y_{\theta}(w)]$	ADB $[J_i(W) + \alpha Y_i(w)]$	$\frac{1}{DB}\frac{J_0(w) + \alpha Y_0(w)}{J_1(w) + \alpha Y_1(w)}$
K ₀ (w)	DB K ₁ (w)	$\frac{1}{DB}\frac{K_0(w)}{K_1(w)}$
$A[K_{\theta}(w) + \alpha I_{\theta}(w)]$	ADB $[K_1(\mathbf{w}) - \alpha I_1(\mathbf{w})]$	$\frac{1}{DB} \frac{K_0(\mathbf{w}) + \alpha I_0(\mathbf{w})}{K_1(\mathbf{w}) - \alpha I_1(\mathbf{w})}$

## Effect of the Reflector

Some general remarks may be made concerning the effect of a single reflector on the critical size. Consider the spherical case, Table 1.4.5. column 1 of the table pertains to the core, column 6 to a reflector of outside radius b and thickness b-a=t, and column 4 to an infinite reflector. For a thin reflector ( $t\ll 1/B$ ),  $\phi/j$  reduces to  $t/D_1$ , the reflector thickness in units of the diffusion constant,  $D_1$ . If further,  $t/a\ll 1$ , use of column 1 and of the critical condition:

$$\left(\frac{\varphi}{\mathbf{j}}\right)_{\mathbf{c}} = \left(\frac{\varphi}{\mathbf{j}}\right)_{\mathbf{l}} \qquad \begin{array}{c} \mathbf{c} \to \mathbf{core} \\ \mathbf{1} \to \mathbf{reflector} \end{array}$$
 (42)

leads to a reflector saving  $(\delta = a - a_0 = a - \pi/B_c)$  of:

$$\delta \approx t \, \frac{D_c}{D_t}$$

For a thick reflector (t  $\gg 1/B$ ), column 6 goes over into column 4 in which:

$$(\phi/j)_1 = \frac{1}{D_1(B_1 + 1/a)}$$

For a "perfect" reflector,  $B_1a \ll 1$ , or  $B_1 \ll B_c$ :

$$(\phi/j)_1 = \frac{a}{D_1}$$

and the reflector savings in the case:

$$D_1 = D_C$$

is:

$$\delta = \frac{1}{2} a_0$$

For an "equivalent" reflector:

$$D_1 = D_c$$
,  $B_1 = B_c$ ,  $a = \frac{3}{4} a_0$ , and  $\delta = \frac{1}{4} a_0$ 

For a reflector in which  $B_1a \gg 1$  or  $B_1 \gg B_c$ :

$$(\phi/j)_1 = \frac{1}{D_1 B_1}$$

showing that the characteristic parameter is D1B1.

### Numerical

As in the Serber-Wilson method, numerical results are easily obtained for the simple geometries in the case of a single reflector, whether finite or infinite. Thus, the following graphs may be drawn:



- (1)  $\frac{\phi}{i}$  (w_c, D_cB_c) for the core as a function of w_c = B_c a for various values of D_cB_c
- (2)  $\frac{\phi}{j}$  (w₁,D₁B₁, $\gamma$ ) for the reflector as a function of w₁ = B₁a for values of D₁B₁ and  $\gamma$

where  $\gamma$  is the ratio of the outer boundary coordinate to the inner boundary coordinate, both measured from the center of symmetry. The w scales should be logarithmic, in order that superposition of the two graphs with the w axes coinciding leads to the same distance scale on the w = Br axes. The w values at the point of intersection of the (1) and (2) curves give the critical coordinate a through the relations:

$$\mathbf{a} = \frac{\mathbf{w_c}}{\mathbf{B_c}} = \frac{\mathbf{w_1}}{\mathbf{B_1}}$$

In multi-reflector problems, the value of  $\phi/j$  at the core boundary may be computed by starting with the outermost reflector, column 6 of Table 1.4.5. Matching  $\phi/j$ 's with the next outermost reflector, column 5, results in the value of  $\alpha$  for that region. This process may be continued until the core radius is reached, assuming that the geometry and reflector properties are fixed in advance. The final  $\phi/j$  may then be matched to the core, column 1 or the above-mentioned graph, to obtain allowable combinations of  $D_c$  and  $B_c$ . If all boundaries except the core boundary are fixed in advance, the above process results in a  $\phi/j$  which is a function of the core radius. This function may then be matched to  $(\phi/j)_c$  for a known core composition to yield the core radius.

A matrix method which may be used in place of the above procedure is presented below in the treatment of two-group theory.

#### OTHER GEOMETRIES

Geometries more complicated than the plane, spherical, and cylindrical have been treated without resort to numerical integration of the differential equations. Accurate results exist for the infinitely reflected spheroid¹⁰ and hemisphere,¹⁷ when the core and reflector have the same total cross section. The result in the hemisphere case is:

$$a_{hemi}$$
 is slightly less than 1.3 $a_{sphere}$ 

where the a's are the critical radii in the infinitely tamped problem. Also, an accurate perturbation formula has been given¹⁸ for the critical volume of a nearly spherical core inside an infinite reflector of the same total cross section.

The variational method, described above, may be extended in order to obtain the critical conditions for reflected reactors. Perturbation theory¹⁹ on the diffusion equations may be used to evaluate the flux distribution in a reactor not differing overmuch in geometry from spherical symmetry, for example.

Problems such as (1) a finite cylindrical core surrounded on all sides by an infinite or finite cylindrical reflector and (2) a parallelepiped core surrounded on all sides by an infinite or finite parallelepiped reflector are often treated in the following approximation. The description given applies to a cylindrical core (radius a, height 2h) with infinite reflector. The total volume is divided into the regions listed in Table 1.4.7 along with the assumed flux in each region and the corresponding buckling conditions. The region labeled ZR is not used in the calculation. The diffusion boundary conditions are applied to the C-Z boundary and to the C-R boundary. They are:

$$\frac{1}{D_c B_{cz}} \cot B_{cz} h = \frac{1}{D_1 B_z}$$

$$\frac{1}{D_{_{\! C}}B_{_{\! C}r}}\frac{J_0(B_{_{\! C}r}a)}{J_1(B_{_{\! C}r}a)} = \frac{1}{D_1B_{_{\! T}}}\,\frac{K_0(B_{_{\! T}}a)}{K_1(B_{_{\! T}}a)}$$

Table 1.4.7 — Approximate Method for Difficult Cylindrical Geometry

Region	φ	Buckling condition
Core, C r ≤ a  z  ≤ h	$J_0(B_{cr} r) \cos B_{cz} Z$	$B_c^2 = B_{cr}^2 + B_{cz}^2$
Core, Z $r \leq a$ $ z  \geq h$	$J_0(B_{cr} r) e^{-B_z Z}$	$-\mathbf{B_1^2} = \mathbf{B_2^2} - \mathbf{B_{cr}^2}$
Core, R $r \ge a$ $ z  \le h$	$K_0(B_r r) \cos B_{cz} Z$	$-B_1^2 = B_1^2 - B_{cz}^2$
Core, ZR $r \ge a$ $ z  \ge h$	Not used	Not used

Assuming, for example, that  $D_c$ ,  $B_c^2$ ,  $D_1$ ,  $B_1^2$ , and h are fixed in advance, the two boundary conditions and the three buckling conditions enable the determination of the five unknowns, A,  $B_{cr}$ ,  $B_{cz}$ ,  $B_z$ , and  $B_r$ .

The method as just described is often simplified by guessing a value for  $B_{cz}$  or for  $B_{cr}$ . Such guesses may be easily related to guessed values for the reflector savings  $\delta h$  or  $\delta a$ .

#### MANY-VELOCITY REACTORS

# THE ONE-VELOCITY OR FEYNMAN-WELTON METHOD

Reference 20 is a comprehensive report on this method and makes use of the transport approximation.* Anisotropic scattering may be treated by the spherical harmonic method. An extension of the method in the case of hydrogenous systems has been reported by Davison.²¹ The case of the bare-slab reactor with a linear scattering law has been treated by Selengut²² in an accurate approximation for not-too-thin reactors and is discussed below.

### **CONSTANT CROSS SECTIONS**

The following two theorems are of interest for the method even though assumptions they contain are very restrictive.

THEOREM 1. If the cross sections, angular dependence of scattering, fission spectrum, and  $\nu$ , are all independent of neutron energy, then the energy-integrated flux,  $\int_0^{\infty} \text{vn}(\underline{\mathbf{r}},\underline{\Omega},\mathbf{E})$  dE, satisfies the one-velocity Boltzmann equation.

THEOREM 2. If further, the reactor consists of a bare core or of a core surrounded by reflectors which cannot alter the neutron energy,† then the direction-integrated flux:

$$\phi(\underline{\mathbf{r}},\mathbf{E}) = \int vn(\underline{\mathbf{r}},\underline{\Omega},\mathbf{E})d\Omega$$

is separable into:

$$\phi(\mathbf{r}, \mathbf{E}) = \mathbf{F}(\mathbf{r})\mathbf{G}(\mathbf{E})$$

^{*}See also Davison, Chapter VII.

[†] No fission and no slowing-down.

where F(r) is the space distribution of the one-velocity problem. When scattering is isotropic, the spectrum G(E) satisfies the critical condition:

$$(\sigma_S + \nu \sigma_f)G(E) = \nu X(E)\sigma_f \int_0^\infty G(E)dE + \sigma_S \int_0^\infty g(E,E')G(E')dE'$$

These theorems and the results below for variable cross sections illustrate the wide applicability of one-velocity theory.

# VARIABLE CROSS SECTIONS (IN TRANSPORT APPROXIMATIONS)

The case of energy-dependent cross sections can be easily treated only for a bare core or a core surrounded by a reflector which cannot change the neutron energy (no slowing-down and no fission). Reflectors which do change the neutron energy may be handled by two-group theory, as discussed later.

Consider a core fission cross section,  $\sigma_f$ , a capture cross section,  $\sigma_c$ , a cross section  $\sigma_s$  for scattering with energy change, and a cross section  $\sigma_e$  for scattering with neglected energy change. The core is surrounded by a reflector in which:

$$\sigma_{\rm S}=0$$
 and  $\sigma_{\rm f}=0$ 

Let:

$$\sigma_{\mathbf{r}}^{(\mathbf{E})} = \sigma_{\mathbf{f}}^{(\mathbf{E})} + \sigma_{\mathbf{c}}^{(\mathbf{E})} + \sigma_{\mathbf{s}}^{(\mathbf{E})} \tag{43}$$

be called the removal cross section.

The balance equation in terms of the removal density A(r,E) in the core:

$$\mathbf{A}(\underline{\mathbf{r}},\mathbf{E}) = \sigma_{\mathbf{r}}(\mathbf{E})\phi(\underline{\mathbf{r}},\mathbf{E}) \tag{44}$$

may be written as:

$$\mathbf{A}(\underline{\mathbf{r}},\mathbf{E}) = \int_{\mathbf{core}} \mathbf{P}(\underline{\mathbf{r}},\underline{\mathbf{r}}',\mathbf{E}) \ \mathbf{S}(\underline{\mathbf{r}}',\mathbf{E}) d\underline{\mathbf{r}}'$$
(45)

where the source S is given by:

$$\mathbf{S}(\underline{\mathbf{r}},\mathbf{E}) = \nu \chi(\mathbf{E}) \int_0^{\infty} \frac{\sigma_{\mathbf{f}}(\mathbf{E}')}{\sigma_{\mathbf{r}}(\mathbf{E}')} \mathbf{A}(\underline{\mathbf{r}},\mathbf{E}') d\mathbf{E}' + \int_0^{\infty} \mathbf{g}(\mathbf{E},\mathbf{E}') \frac{\sigma_{\mathbf{S}}(\mathbf{E}')}{\sigma_{\mathbf{r}}(\mathbf{E}')} \mathbf{A}(\underline{\mathbf{r}},\mathbf{E}') d\mathbf{E}'$$
(46)

and the kernel  $P(\underline{r},\underline{r}',E)$  represents the probability that a neutron released at  $\underline{r}'$  with energy E is absorbed (with  $\sigma_a$ ) at  $\underline{r}$  without intervening energy loss. The kernel P thus includes the effect of the "elastic" scattering  $\sigma_e$  in both the core and reflector.

Consider now a fictitious one-velocity problem at energy E with the reflector having the same cross sections ("elastic" and capture) as in the actual problem and with the core having the same fission and "elastic" cross sections as in the actual problem and with a capture cross section given by  $\sigma_c(E) + \sigma_s(E)$ . The removal cross section in this one-velocity problem is then the same as in the actual problem, given by Eq. (43), and the source density may be written as  $\mu(E)A^{(1)}(r,E)$  where  $A^{(1)}$  is the one-velocity removal density and  $\mu(E)$  is the number of neutrons released per neutron removed. The one-velocity balance equation is then:

$$\mathbf{A}^{(1)}(\mathbf{r},\mathbf{E}) = \mu(\mathbf{E}) \int_{\text{core}} \mathbf{P}(\mathbf{r},\mathbf{r}',\mathbf{E}) \mathbf{A}^{(1)}(\mathbf{r}',\mathbf{E}) d\mathbf{r}'$$
(47)

with eigenfunctions  $A_n(r,E)$ ,  $n = 0,1,2, \ldots$ , and with eigenvalues:

$$\mu_{\mathbf{n}}(\mathbf{E}) = \frac{\nu_{\mathbf{n}}(\mathbf{E})\sigma_{\mathbf{f}}(\mathbf{E})}{\sigma_{\mathbf{n}}(\mathbf{E})} \tag{48}$$

where  $\nu_n(E)$  is the value of  $\nu$  required to balance the n'th mode of the one-velocity problem. The value of  $\nu_0(E)$  and the space distribution  $A_0(r,E)$  in the fundamental mode may be obtained by the methods discussed in "One-velocity Reactors." The values in the higher modes are similarly obtainable.

The kernel  $P(\underline{r},\underline{r}',E)$  may be written as:

$$\mathbf{P}(\underline{\mathbf{r}},\underline{\mathbf{r}}',\mathbf{E}) = \sum_{n=0}^{\infty} \frac{1}{\mu_n(\mathbf{E})} \mathbf{A}_n(\underline{\mathbf{r}},\mathbf{E}) \mathbf{A}_n(\underline{\mathbf{r}}',\mathbf{E})$$
(49)

where the modes  $A_n(\underline{r},E)$  form a normalized orthogonal* set when integrated over the core:

$$\int_{\text{core}} \mathbf{A}_{n}(\underline{\mathbf{r}}, \mathbf{E}) \mathbf{A}_{m}(\underline{\mathbf{r}}, \mathbf{E}) d\underline{\mathbf{r}} = \delta_{nm}$$
(50)

Various approximate solutions of the many-velocity problem, Eqs. (44), (45), and (46), may be obtained by making approximations in the kernel P or by expanding A(r,E) into:

$$\mathbf{A}(\mathbf{r},\mathbf{E}) = \sum_{n} \mathbf{G}_{n}(\mathbf{E}) \mathbf{A}_{n}(\mathbf{r},\mathbf{E})$$

and keeping as many terms as desired.

Thus, in the "first upper approximation," it is assumed that:

$$\phi(\mathbf{r},\mathbf{E}) = \frac{\mathbf{A}(\mathbf{r},\mathbf{E})}{\sigma_{\mathbf{r}}(\mathbf{E})} = \mathbf{G}(\mathbf{E})\mathbf{A}_{\mathbf{0}}(\underline{\mathbf{r}},\mathbf{E})$$
 (51)

which when substituted into Eqs. (45) and (46) leads to (after multiplication by  $A_0(\underline{r}, E)$  and integration over  $\underline{r}$ ) the critical equation:

$$\nu_{\mathbf{g}}(\mathbf{E})\sigma_{\mathbf{f}}(\mathbf{E})G(\mathbf{E}) = \nu\chi(\mathbf{E}) \int \sigma_{\mathbf{f}}(\mathbf{E}')G(\mathbf{E}')\mathbf{A}_{\infty}(\mathbf{E},\mathbf{E}')d\mathbf{E}' + \int \mathbf{g}(\mathbf{E},\mathbf{E}')\sigma_{\mathbf{g}}(\mathbf{E}')G(\mathbf{E}')\mathbf{A}_{\infty}(\mathbf{E},\mathbf{E}')d\mathbf{E}'$$
(52)

where:

$$\mathbf{A}_{\infty}(\mathbf{E}, \mathbf{E}') = \int_{\text{core}} \mathbf{A}_{0}(\mathbf{r}, \mathbf{E}) \mathbf{A}_{0}(\mathbf{r}, \mathbf{E}') d\mathbf{r}$$
 (53)

In the simplest, or "first lower approximation," it is further assumed that:

$$\mathbf{A}_{\mathbf{0}}(\mathbf{r},\mathbf{E}) = \mathbf{A}_{\mathbf{0}}(\mathbf{r},\mathbf{E}') = \mathbf{A}_{\mathbf{0}}(\mathbf{r}) \tag{54}$$

from which it follows that  $A_{\infty} = 1$ . Equation (52) may be solved as follows, the results being written for  $A_{\infty}(E,E') \approx 1$  as in the first lower approximation. Choose the normalization for G(E) such that:

$$\nu \int_0^{\infty} \sigma_f(\mathbf{E}') G(\mathbf{E}') d\mathbf{E}' = 1$$
 (55)

and solve for G(E) from the integral equation:

^{*}A discussion of orthogonality is given by Davison, Chapter VII.

[†]Approximate methods for solution of such equations are discussed in Chapter 1.3.

$$\nu_0(\mathbf{E})\sigma_f(\mathbf{E})G(\mathbf{E}) = \chi(\mathbf{E}) + \int_0^\infty g(\mathbf{E}, \mathbf{E}')\sigma_S(\mathbf{E}')G(\mathbf{E}')d\mathbf{E}'$$
(56)

The value of  $\nu$  is then determined by Eq. (55).

Both these approximations are exact in the case of constant cross sections. In this case, integration over energy of Eq. (52) gives:

$$\nu_0(\mathbf{E})\sigma_{\mathbf{f}}(\mathbf{E}) = \nu\sigma_{\mathbf{f}}(\mathbf{E}) + \sigma_{\mathbf{s}}(\mathbf{E})$$

thus proving Theorem 2 (above).

There are good, although not entirely rigorous, arguments leading to the statement that the upper and lower approximations lead to upper and lower estimates for  $\nu$ . This statement is borne out by test calculations which further indicate that the errors owing to these approximations are less than a few percent in a variety of cases. Detailed discussions of accuracy and of procedures leading to higher approximations are discussed in the referenced reports.

### INELASTIC REFLECTORS IN TWO-GROUP THEORY

Practical equations are obtained in two-group theory for the case of reflectors which slow neutrons down. The results given below may be extended to include the effects of fission in the reflector. In the following, all symbols have the same meaning as above: The subscripts 1 and 2 refer respectively to the fast and slow groups; the subscript 21 refers to inelastic scattering from group 1 to group 2; and the asterisk refers to the reflector. Thus:

$$\sigma_{r1} = \sigma_{f1} + \sigma_{c1} + \sigma_{21}$$

and:

$$\sigma_{r2} = \sigma_{f2} + \sigma_{c2}$$

In the reflector:

$$\sigma_{f1}* = \sigma_{f2}* = 0$$

The balance equations are:

$$\mathbf{A}_{1}(\underline{\mathbf{r}}) = \int_{\text{core}} \mathbf{P}_{1}(\underline{\mathbf{r}},\underline{\mathbf{r}}') \, \mathbf{S}_{1}(\underline{\mathbf{r}}') d\underline{\mathbf{r}}' \tag{57}$$

$$\mathbf{A_2}(\underline{\mathbf{r}}) = \int_{\text{core}} \mathbf{P_2}(\underline{\mathbf{r}},\underline{\mathbf{r}}') \, \mathbf{S_2}(\underline{\mathbf{r}}') d\underline{\mathbf{r}}' + \int_{\text{core}} \mathbf{P_{21}^*}(\underline{\mathbf{r}},\underline{\mathbf{r}}') \, \mathbf{S_1}(\underline{\mathbf{r}}') d\underline{\mathbf{r}}'$$
 (58)

where:

$$\mathbf{S_1} = \nu \, \chi_1 \left[ \frac{\sigma_{\mathbf{f}\,1}}{\sigma_{\mathbf{r}\,1}} \, \mathbf{A_1} + \frac{\sigma_{\mathbf{f}\,2}}{\sigma_{\mathbf{r}\,2}} \, \mathbf{A_2} \right] \tag{59}$$

and:

$$S_2 = \nu \chi_2 \left[ \frac{\sigma_{f1}}{\sigma_{r1}} A_1 + \frac{\sigma_{f2}}{\sigma_{r2}} A_2 \right] + \frac{\sigma_{21}}{\sigma_{r1}} A_1 \tag{60}$$

where  $\chi_1$  and  $\chi_2$  are the fraction of fission neutrons released in groups 1 and 2, and where the kernel  $P_{21}^*$  represents the probability that a group 1 neutron released at  $\underline{r}'$  in the core

is absorbed as a group 2 neutron at  $\underline{r}$  in the core after having been inelastically scattered in the reflector.

The one-velocity problems, defined as above, give for the fundamental mode:

$$\mathbf{A}_{01}(\underline{\mathbf{r}}) = \mu_{01} \int \mathbf{P}_{1}(\underline{\mathbf{r}},\underline{\mathbf{r}}') \mathbf{A}_{01}(\underline{\mathbf{r}}') d\underline{\mathbf{r}}'$$

$$\mathbf{A}_{02}(\underline{\mathbf{r}}) = \mu_{02} \int \mathbf{P}_{2}(\underline{\mathbf{r}},\underline{\mathbf{r}}') \mathbf{A}_{02}(\underline{\mathbf{r}}') d\underline{\mathbf{r}}'$$

In the simplest lower approximation, it is assumed that:

$$A_{01}(\underline{r}) = A_{02}(\underline{r}) = A_{0}(\underline{r})$$

$$\phi_{1}(\underline{r}) = \frac{A_{1}(\underline{r})}{\sigma_{r1}} = G_{1}A_{0}(\underline{r})$$
(61)

$$\phi_2(\underline{\mathbf{r}}) = \frac{\mathbf{A}_2(\underline{\mathbf{r}})}{\sigma_{\mathbf{r},2}} = \mathbf{G}_2 \mathbf{A}_{\mathbf{0}}(\underline{\mathbf{r}}) \tag{62}$$

$$\int_{core} P_{21}^* (\underline{\mathbf{r}},\underline{\mathbf{r}}') \mathbf{A}_0(\underline{\mathbf{r}}') d\underline{\mathbf{r}}' = \gamma \mathbf{A}_0(\underline{\mathbf{r}})$$
(63)

where  $\gamma$  is discussed below.

These assumptions lead to a pair of homogeneous equations in  $G_1$  and  $G_2$  with the solubility conditions that

$$\nu = \frac{\mu_{01}\mu_{02}\sigma_{r1}\sigma_{r2}}{\chi_{1}(\sigma_{f2}\sigma_{21} + \sigma_{f1}\sigma_{r2}\mu_{02} + \sigma_{f2}\sigma_{r1}\mu_{01}\mu_{02}\gamma) + \chi_{2}\sigma_{r1}\sigma_{f2}\mu_{01}}$$
(64)

and with:

$$\frac{G_2}{G_1} = \frac{\mu_{01}\sigma_{r1}}{\nu\chi_1\sigma_{r2}} - \frac{\sigma_{l1}}{\sigma_{r2}}$$
 (65)

Several approximate formulas for  $\gamma$  are discussed, ²⁰ all having the form:

$$\gamma = \left(1 - \frac{1}{\mu_{01}}\right) \frac{\sigma_{T1}^4}{\sigma_{T1}^6} Q_2 \tag{66}$$

where  $Q_i$  is the average probability that a neutron liberated in the tamper at velocity 2 (via inelastic scattering) is absorbed in the core. Use of the asymptotic solutions of one-velocity theory gives for  $Q_i$ :

$$Q_2 = \frac{a^3}{3} \frac{h_1^2 h_2^2}{(h_1 + h_2)(1 + h_1 a)(1 + h_2 a)} \frac{\sigma_{r2}}{\sigma_{r2}^*} \left(1 - \frac{1}{\mu_{02}}\right)$$
(67)

where a is the core radius and h₁ and h₂ are determined from:

$$\frac{h_1/\sigma_1^*}{\tanh^{-1}h_2/\sigma_2^*} = \frac{\sigma_{e_1}^*}{\sigma_1^*}$$
 (68)

$$\frac{h_2/\sigma_2^*}{\tanh^{-1}h_2/\sigma_2^*} = \frac{\sigma_{e,2}^*}{\sigma_2^*}$$
 (69)

ally saze

ode:

th the side

ns of 🐲

where the  $\sigma_e^*$ 's are the "elastic" scattering cross sections and the  $\sigma^*$ 's are the total cross sections being the sum of removal plus elastic cross sections. Thus, for:

$$1 - \sigma_e^*/\sigma^* = \frac{\sigma_r^*}{\sigma^*} \ll 1$$
,  $h \approx \sqrt{3\sigma^*\sigma_r^*}$ 

# NON-ISOTROPIC SCATTERING

The effect of non-isotropic scattering on the preceding results is illustrated by the case of linear anisotropy in a bare-slab reactor.²² Using the first lower approximation, the direction-dependent flux:

$$\phi(x,E,\mu) = vn(x,E,\mu)$$

may be written as:

$$\phi(\mathbf{x}, \mathbf{E}, \mu) = \mathbf{R}[\mathbf{e}^{i\mathbf{k}\mathbf{x}} f(\mathbf{E}, \mu)] \tag{70}$$

where R[x] denotes the real part of x. The direction-integrated flux:

$$\phi(\mathbf{x},\mathbf{E}) = \int_{-1}^{1} d\mu \ \phi(\mathbf{x},\mathbf{E},\mu)$$

has the form:

$$\phi(\mathbf{x}, \mathbf{E}) = \mathbf{H}(\mathbf{E}) \cos \mathbf{K} \mathbf{x} \tag{71}$$

where:

$$K = \frac{\pi}{2n} \tag{72}$$

and a is the distance from the center of the reactor to the extrapolated boundary, assumed the same for all energies. The current density:

$$\mathbf{j}(\mathbf{x},\mathbf{E}) = \int_{-1}^{1} \mu \, d\mu \, \phi(\mathbf{x},\mathbf{E},\mu)$$

has the form:

$$j(x,E) = J(E) \sin Kx. \tag{73}$$

Substitution of Eq. (70) into the Boltzmann equation results in a pair of coupled integral equations for H(E) and J(E) which may be written as follows:

$$\mathbf{H}(\mathbf{E}) = \mathbf{G}_{\mathbf{a}}(\mathbf{E}) - \mathbf{G}_{\mathbf{1}}(\mathbf{E}) \tag{74}$$

$$\mathbf{J}(\mathbf{E}) = \frac{1-\beta}{\alpha\beta} \ \mathbf{G}_0(\mathbf{E}) + \frac{1}{\alpha} \ \mathbf{G}_1(\mathbf{E}) \tag{75}$$

$$\beta(\mathbf{E}) = \frac{\tan^{-1} \alpha(\mathbf{E})}{\alpha(\mathbf{E})} \tag{76}$$

$$\alpha(\mathbf{E}) = \mathbf{K}/\sigma(\mathbf{E}) \tag{77}$$

where  $\sigma(E)$  is the total cross section, and  $G_0$  and  $G_1$  satisfy:

$$\frac{\sigma(E)}{\beta(E)}G_0(E) = \nu\chi(E) \int_0^\infty dE' \ \sigma_f(E')[G_0(E') - G_1(E')]$$

+ 
$$\int_0^{\infty} g(E,E') dE' \sigma_B(E') [G_0(E') - G_1(E')]$$
 (78)

$$\frac{\alpha(\mathbf{E})\sigma(\mathbf{E})}{1-\beta(\mathbf{E})} \mathbf{G}_{\mathbf{i}}(\mathbf{E}) = \int_{0}^{\infty} \frac{3\bar{\mu}_{\mathbf{0}}(\mathbf{E}')}{\alpha(\mathbf{E}')} \mathbf{g}(\mathbf{E},\mathbf{E}')\sigma_{\mathbf{g}}(\mathbf{E}') \left[ \frac{1-\beta(\mathbf{E}')}{\beta(\mathbf{E}')} \mathbf{G}_{\mathbf{0}}(\mathbf{E}') + \mathbf{G}_{\mathbf{i}}(\mathbf{E}') \right] d\mathbf{E}'$$
(79)

The equations are written in terms of  $G_0$  and  $G_1$  because  $G_1$  goes to zero as  $\prod_i (E)$ , the average cosine of the angle of scattering, goes to zero. Thus,  $G_1$  is a measure of the effect of anisotropy.

The above equations correctly reduce to Eq. (52) (with  $A_{\infty}=1$ ) in the case of isotropic scattering. It is to be noted that  $\sigma(E)/\beta(E)=\nu_0(E)\sigma_f(E)$ , where  $\nu_0(E)$  is the value of  $\nu$  required to maintain criticality in a one-velocity reactor at energy E, the removal cross section being  $\sigma_r=\sigma_f+\sigma_c+\sigma_s=\sigma$ .

Equations (78) and (79) may be solved* for  $G_0$  and  $G_1$  in the normalization:

$$\nu \int_0^{\infty} dE' \, \sigma_f(E') [G_0(E') - G_1(E')] = 1 \tag{80}$$

and  $\nu$  may then be obtained from Eq. (80). Using this normalization for a reactor consisting of hydrogen and an element which scatters isotropically without energy loss, Eqs. (78) and (79) reduce to:

$$\frac{\sigma(\mathbf{E})}{\beta(\mathbf{E})} \mathbf{G_0}(\mathbf{E}) = \chi(\mathbf{E}) + \sigma_{\mathbf{e}}(\mathbf{E}) \left[ \mathbf{G_0}(\mathbf{E}) - \mathbf{G_1}(\mathbf{E}) \right] + \int_0^{\infty} \frac{d\mathbf{E}'}{\mathbf{E}'} \sigma_{\mathbf{SH}}(\mathbf{E}') \left[ \mathbf{G_0}(\mathbf{E}') - \mathbf{G_1}(\mathbf{E}') \right]$$
(81)

$$\frac{\alpha(\mathbf{E})\sigma(\mathbf{E})}{1-\beta(\mathbf{E})} \mathbf{G}_{1}(\mathbf{E}) = 2 \int_{0}^{\infty} \frac{d\mathbf{E}'}{\alpha(\mathbf{E}')\mathbf{E}'} \sigma_{SH}(\mathbf{E}') \left[ \frac{1-\beta(\mathbf{E}')}{\beta(\mathbf{E}')} \mathbf{G}_{0}(\mathbf{E}') + \mathbf{G}_{1}(\mathbf{E}') \right]$$
(82)

which may be converted (by differentiation) into a pair of coupled differential equations.

#### UNIFORM MEDIA

Reactors in which the core and reflector have uniform scattering and moderating properties, with the fuel affecting only the absorption, afford certain simplifications in the theory and have received considerable attention. Unless specified otherwise, the fuel will be assumed to be distributed uniformly in the core; non-uniform distributions will be considered separately later.

# GAUSSIAN SLOWING-DOWN

The case of a spherical thermal reactor in an infinite medium with Gaussian slowing-down has been treated by Volkoff.²³ The notation is given in Table 1.4.8.

The method starts with the equations of elementary diffusion theory:

$$\frac{d^2 f_1(r)}{dr^2} - \frac{f_1(r)}{L_1^2} = -\frac{g(r)}{D} \quad 0 \le r \le a$$
 (83A)

$$\frac{d^{2}f_{2}(r)}{dr^{2}} - \frac{f_{2}(r)}{L_{a}^{2}} = -\frac{g(r)}{D} \ a \le r \le \infty$$
 (83B)

^{*} Approximate methods for solution of such equations are discussed in Chapter 1.3.

Table 1.4.8 - Notation for Discussion of Volkoff's Work

Symbol	Definition		
r	Distance from center of symmetry		
a _o	Critical radius of unreflected reactor		
a	Critical radius of reflected reactor		
sub 1	Indicates core		
sub 2	Indicates reflector		
f	r times thermal flux		
g	r times slowing down density		
D	Thermal diffusion constant		
L	Thermal diffusion length		
L,	Slowing-down length		
M	$\sqrt{L^2 + L_3^2}$ , migration length		
γ	L _s /L		
k	Multiplication constant $[k_1 > 0, k_2 < 0]$		
P( x )	Slowing-down density at position x owing to a plane source at $x = 0$		
<b>S</b> ( <b>r</b> , <b>r</b> ')	$\frac{1}{4\pi r r'} [P( r-r' ) - P( r+r' )] = slowing-down density at r owing$		
	to a unit spherical shell source at r'		
<b>Φ</b> (ν)	Fourier transform of P(y) where $y =  x /L_s$		

with the conditions:

$$f_1(0) = 0 = f_2(\infty)$$

$$f_1(a) = f_2(a)$$

$$\frac{df_1(r)}{dr}\Big|_{r=a} = \frac{df_2(r)}{dr}\Big|_{r=a}$$
(84)

where g(r) is given by:

$$\frac{g(\mathbf{r})}{D} = \frac{rk_1}{L_1^2} \int_0^a 4\pi \mathbf{r}' d\mathbf{r}' f_1(\mathbf{r}') S(\mathbf{r}, \mathbf{r}') + \frac{rk_2}{L_2^2} \int_a^{\infty} 4\pi \mathbf{r}' d\mathbf{r}' f_2(\mathbf{r}') S(\mathbf{r}, \mathbf{r}')$$
(85)

which may be written in terms of the plane kernel P as:

$$\frac{g(\mathbf{r})}{D} = \frac{k_1}{L_1^2} \int_{-a}^{+a} f_1(\mathbf{r}') P(|\mathbf{r} - \mathbf{r}'|) d\mathbf{r}' + \frac{k_2}{L_2^2} \left\{ \int_{-\infty}^{-a} f_2(\mathbf{r}') P(|\mathbf{r} - \mathbf{r}'|) d\mathbf{r}' + \int_{a}^{+\infty} f_2(\mathbf{r}') P(|\mathbf{r} - \mathbf{r}'|) d\mathbf{r}' \right\}$$
(86)

where the range of definition of g,  $f_1$ , and  $f_2$  has been extended to negative values of r by regarding them as odd functions.

The actual three region (image) problem as contained in Eqs. (83), (84), and (86) is now approximated by a two-region problem formed by extending the reactor image to  $-\infty$ . Thus, Eq. (83A) is to hold for  $-\infty \le r \le a$ , Eq. (83B) holds for  $a \le r \le \infty$ , and Eq. (86) is replaced by:

$$\frac{g(r)}{D} = \frac{k_1}{L_1^2} \int_{-\infty}^{a} f_1(r') P(|r - r'|) dr' + \frac{k_2}{L_2^2} \int_{a}^{\infty} f_2(r') P(|r - r'|) dr'$$
 (87)

This two-region problem is solved by the Wiener-Hopf method and is shown by test computation to be a very accurate approximation to the actual three-region problem. The two-region criticality* results are given below.

The critical radius is given by:

$$a = a_0[1 - \epsilon_{th} - \epsilon_f] \tag{88}$$

where ao is the bare critical radius, given by:

$$\mathbf{a_0} = \frac{\pi \mathbf{L_S}}{\nu_1} \tag{89}$$

 $\epsilon_{
m th}$  is the fractional reflector savings owing to thermal neutrons entering the core from the reflector:

$$\epsilon_{\rm th} = \frac{1}{\pi} \tan^{-1} \frac{\nu_1}{\nu_2} \tag{90}$$

 $\epsilon_{\mathbf{f}}$  is the fractional savings owing to fast neutrons entering the core:

$$\epsilon_{f} = \frac{1}{\pi} [I(\nu_{1}, \gamma_{1}) - J(\nu_{1}, \nu_{2}, \gamma_{2})]$$
 (91)

and:

$$I(\nu_1, \ \gamma_1) = \frac{\nu_1}{\pi} P \int_0^{\infty} \frac{dx}{x^2 - \nu_1^2} l_n \frac{x^2 - \nu_1^2}{x^2 + \gamma_1^2 (1 - k_1 \Phi(x))}$$

$$J(\nu_1, \ \nu_2, \ \gamma_2) = \frac{\nu_1}{\pi} P \int_0^{\infty} \frac{dx}{x^2 - \nu_1^2} l_n \frac{x^2 + \nu_2^2}{x^2 + \gamma_2^2 (1 - k_2 \Phi(x))}$$
(92)

where P denotes the Cauchy principal value of the integral. The quantities  $\nu_1$  and  $\nu_2$  are the values of the infinite medium buckling (using  $L_8$  as the unit of length) and are the positive real roots of:

$$k_{1} = \frac{1}{\Phi(\nu_{1})} \left( 1 + \frac{\nu_{1}^{2}}{\gamma_{1}^{2}} \right)$$

$$k_{2} = \frac{1}{\Phi(i\nu_{2})} \left( 1 - \frac{\nu_{2}^{2}}{\gamma_{2}^{2}} \right)$$
(93)

If the reflector contains no fuel, then  $k_2=0$  from which it follows that  $\nu_2=\gamma_2$  and  $J(\nu_1, \nu_2, \gamma_2)=0$ . In this case:

$$\epsilon_{th}(\mathbf{k}_2 = 0) = \frac{1}{\pi} \tan^{-1} \frac{\nu_1}{\gamma_2}$$

$$\epsilon_{f}(\mathbf{k}_2 = 0) = \frac{1}{\pi} I(\nu_1, \gamma_1)$$
(94)

^{*} Flux and slowing-down distributions are discussed in Ref. (24) where the deviations from the asymptotic solutions are investigated in the neighborhood of the core reflector interface.



For a Gaussian slowing down kernel:

$$P(|x|) = \frac{1}{2\sqrt{\pi}L_{\pi}} e^{-x^2/4L_{\pi}^2}$$
 (95)

the transform  $\Phi(\nu)$  is given by:

$$\Phi(\nu) = e^{-\nu^2} \tag{96}$$

Figure 1.4.9 plots  $\epsilon_{\rm th}(k_2=0)$  as a function of K =  $(M_1/L_s)\nu_1$  for various values of  $L_2/m_1$ . Figure 1.4.10 plots  $\epsilon_{\rm f}(k_2=0)$  as a function of K for various values of  $\gamma_1$  and also exhibits contours of constant  $k_1$ .

For a finite reflector, the modification of the above is discussed in Ref. (25). For comparison with two-group results, see French and Hurwitz.²⁶

#### GENERAL KERNELS

The formal work of the preceding section applies immediately to a general displacement slowing-down kernel provided that  $\Phi(\nu)$  of Eq. (96) is replaced by the appropriate transform. Applications to multigroup kernels are given by Volkoff and LeCaine.²⁷

The major simplification arising for thermal reactors from the presence of a uniform slowing-down medium in a finite or infinite region can be clearly stated: Let  $S(\underline{x})$  be the source distribution of fission-energy neutrons. Then, the slowing-down density at thermal  $q(\underline{x})$  may be written:

$$q(x) = \int k(x, x') S(x') dx'$$
(97)

where  $k(\underline{x},\underline{x}')$  characterizes the medium but is independent of the fuel distribution. Then, for uniform media:

$$k(x,x') = k(x',x)$$

If the medium is infinite in extent, in addition k(x,x') depends only on |x-x'|.

If the thermal-diffusion coefficient, D, is uninfluenced by the fuel distribution, the reactor criticality equations may be written as:

$$\mathbf{q}(\mathbf{x}) = \int \mathbf{k}(\mathbf{x}, \mathbf{x}') \eta \sigma_{\alpha f}(\mathbf{x}') \Phi(\mathbf{x}') d\mathbf{x}'$$
(98)

$$(-\nabla \cdot D\nabla + \sigma_{am})\phi = q - \sigma_{af} \phi$$
 (99)

using the Green's function, g, defined by:

$$(-\nabla \cdot D\nabla + \sigma_{am})g(\underline{\mathbf{x}},\underline{\mathbf{x}}') = \sigma_{am}\delta(\underline{\mathbf{x}} - \underline{\mathbf{x}}')$$
(100)

one has:

$$\sigma_{\mathbf{am}} \phi = \int \mathbf{g}(\underline{\mathbf{x}}, \underline{\mathbf{x}}') [\mathbf{q}(\underline{\mathbf{x}}') - \sigma_{\mathbf{af}}(\underline{\mathbf{x}}') \phi(\underline{\mathbf{x}}')] d\underline{\mathbf{x}}'$$

$$= \int \mathbf{h}(\underline{\mathbf{x}}, \underline{\mathbf{x}}') \sigma_{\mathbf{af}}(\underline{\mathbf{x}}') \phi(\underline{\mathbf{x}}') d\underline{\mathbf{x}}'$$
(101)

which defines h as:

$$h(\underline{x},\underline{x}') = \eta \int g(\underline{x},\underline{x}'')k(\underline{x}'',\underline{x}')d\underline{x}'' - g(\underline{x},\underline{x}')$$
(102)

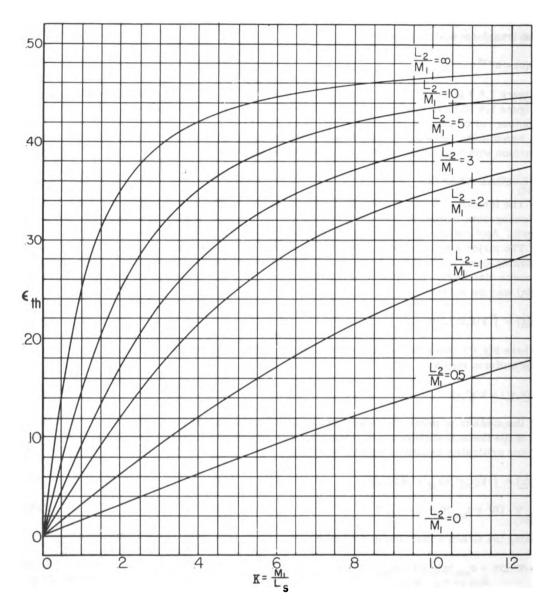


Fig. 1.4.9 — The Fractional Reflector Savings Owing to Thermal Neutrons. Reprinted from CRT-391. The curves give  $\epsilon_{th}$  as a function of K =  $M_1\nu_1/L_8$  for various values of  $L_2/M_1$  for a non-multiplying reflector ( $k_2=0$ ).

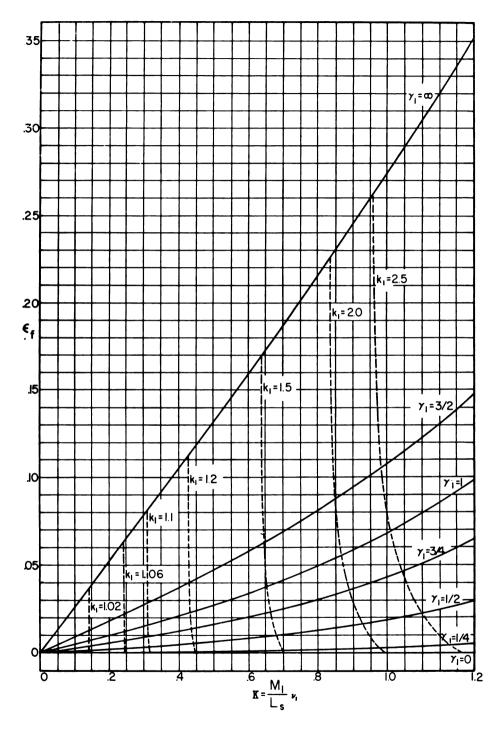


Fig. 1.4.10 — The Fractional Reflector Savings Owing to Fast Neutrons. Reprinted from CRT-91. The curves give  $\epsilon_f$  as a function of  $K=M_1\nu_1/L_s$  for various values of  $\gamma_1$  for a non-multiplying reflector ( $k_2=0$ ).

Owing to the uniformity of the medium, the kernel h is symmetric:

$$h(\underline{x},\underline{x}') = h(\underline{x}',\underline{x})$$

for a wide class of kernels k in finite media. In infinite media, all k, h depends only on  $|\underline{x} - \underline{x'}|$  and is clearly symmetric.

This formulation, as in Eq. (101), is a useful starting point for various considerations such as variational calculations, flat flux, and flat power.

The work of Greuling²⁸ on infinite spherical water systems illustrates variational calculations. He uses a variational principle for  $\eta$  obtained from Eq. (101) above by multiplication with  $\sigma_{\rm af}\phi$  and integrating:

$$\sigma_{am} \int \phi^2 \sigma_{af} d\underline{x} = \int \int \sigma_{af}(\underline{x}) \phi(\underline{x}) h(\underline{x},\underline{x}') \sigma_{af}(\underline{x}') \phi(\underline{x}') d\underline{x}'$$
(103)

The value of  $\eta$  (as contained in h) given by this expression is stationary with respect to variations in  $\phi$ . Greuling used a parabolic trial function for  $\phi$ . Garabedian and Weinberg²⁹ have extended Greuling's work to finite reflectors and slab geometry.

#### **MODE METHODS**

Suppose the infinite-region slowing-down kernel  $k(|\underline{x}-\underline{x}'|)$  satisfies the linear differential equation:

$$Lk(|\mathbf{x} - \mathbf{x}'|) = \delta(\mathbf{x} - \mathbf{x}') \tag{104}$$

Then, in many cases of interest, the slowing-down kernel for a finite region V,  $K(\underline{x},\underline{x}')$ , satisfies the same equation and vanishes for  $\underline{x}$  or  $\underline{x}'$  on the surface S(V). In such a case, q(x) defined by:

$$\mathbf{q}(\mathbf{\underline{x}}) = \eta \int_{\mathbf{V}} \mathbf{K}(\mathbf{\underline{x}},\mathbf{\underline{x}}') \sigma_{\mathbf{af}} \phi(\mathbf{\underline{x}}') d\mathbf{\underline{x}}'$$
 (105)

may be evaluated³⁰ without specific knowledge of K as follows. Let the  $\psi_n(\underline{x})$  be a complete set of linearly independent solutions of:

$$(\nabla^2 + B_n^2)\psi_n = 0$$

$$\psi_n(\underline{s}) = 0 \text{ if } \underline{s} \text{ on } S$$
(106)

normalized so that:

$$\int_{\mathcal{U}} |\psi_n|^2 \mathrm{d}\tau = 1$$

Then, with:

$$f_{\underline{a}} = \int \psi_{\underline{n}}(\underline{x}) \sigma_{\underline{a}\underline{f}} \phi(\underline{x}) d\underline{x}$$
 (107)

$$\overline{k}(B) = 4\pi \int_0^\infty k(r) \frac{\sin Br}{Br} r^2 dr$$
 (108)

one has:

$$\Sigma_{\mathbf{n}} \mathbf{f}_{\mathbf{n}} \psi_{\mathbf{n}}(\underline{\mathbf{x}}) = \sigma_{\mathbf{a}\mathbf{f}} \phi(\underline{\mathbf{x}})$$

$$\mathbf{q}(\underline{\mathbf{x}}) = \eta \int_{\mathbf{V}} \mathbf{K}(\underline{\mathbf{x}}, \underline{\mathbf{x}}') \sigma_{\mathbf{a}\mathbf{f}} \phi(\underline{\mathbf{x}}) d\underline{\mathbf{x}}'$$

$$= \eta \sum_{\mathbf{n}} \mathbf{f}_{\mathbf{n}} \overline{\mathbf{k}} (\mathbf{B}_{\mathbf{n}}) \psi_{\mathbf{n}}(\underline{\mathbf{x}})$$
(109)

The criticality condition may be formulated as follows. From Eqs. (99) and (109):

$$\phi(\underline{\mathbf{x}}) = \sum_{\mathbf{n}} \frac{\eta \overline{\mathbf{k}}(\mathbf{B_n}) - 1}{\sigma_{\mathbf{am}} + \mathbf{D}\mathbf{B_m^2}} \; \mathbf{f_n} \psi_{\mathbf{n}}(\underline{\mathbf{x}})$$

from which, using Eq. (107):

$$f_{n} = \sum_{m} \left( \int_{V} \psi_{n} \sigma_{af} \psi_{m} d\underline{x} \right) \frac{\eta \overline{k}(B_{m}) - 1}{\sigma_{am} + DB_{m}^{2}} f_{m}$$
(110)

This yields the critical condition in the form of the vanishing of the infinite determinant:

$$0 = \left| \left( \int_{V} \psi_{\mathbf{n}} \sigma_{\mathbf{af}} \psi_{\mathbf{m}} d\underline{\mathbf{x}} \right) \frac{\eta \overline{\mathbf{k}} (\mathbf{B}_{\mathbf{m}}) - 1}{\sigma_{\mathbf{am}} + \mathbf{D} \mathbf{B}_{\mathbf{m}}^{2}} - \delta_{\mathbf{nm}} \right|$$
(111)

For small reactors, only a few modes need be considered.

# BARE REACTORS \$1,52,52,54

If  $\sigma_{af}$  is independent of position, as in a bare homogeneous reactor:

$$\int_{\mathbf{V}} \psi_{\mathbf{n}} \sigma_{\mathbf{a} \mathbf{f}} \psi_{\mathbf{m}} \, d\underline{\mathbf{x}} = \sigma_{\mathbf{a} \mathbf{f}} \delta_{\mathbf{n}, \mathbf{m}}$$

and only the fundamental mode (smallest  $B^2$ ) is of interest. The critical determinant, Eq. (111), reduced to:

$$\eta \overline{\mathbf{k}}(\mathbf{B}) = 1 + \frac{\sigma_{\mathbf{am}} + \mathbf{D}\mathbf{B}^2}{\sigma_{\mathbf{af}}}$$

or, with:

$$k = \frac{\sigma_{af}}{\sigma_{af} + \sigma_{am}} \cdot \eta$$

and:

$$L^2 = \frac{D}{\sigma_{af} + \sigma_{am}}$$

then:

$$k = \frac{1 + L^2 B^2}{\overline{k}(B)} \tag{112}$$

This is the usual form. For small B2:

$$\overline{k}(B) = 4\pi \int_0^\infty k(r) \frac{\sin Br}{Br} r^2 dr$$

$$= \sum_{n=0}^\infty \frac{(-1)^n}{(2n+1)!} \overline{r^{2n}} (B^2)^n$$

$$\approx 1 - \frac{1}{6} \overline{r^2} B^2$$
(113)

so that:

$$k \simeq 1 + \left(L^2 + \frac{1}{6} r^2\right) B^2 = 1 + M^2 B^2$$
 (114)

which is the familiar expression in terms of the migration area M2.

**K**(B) may often be computed from microscopic data. Thus, the familiar Fermi theory result for a bare thermal reactor with Gaussian slowing-down may be found in most any of the standard references. Many people have constructed nomograms from which the buckling can be readily evaluated.

Hydrogen moderated machines have been treated^{36,37} by representing the leakage as a fictitious absorption; the slowing-down then being treated correctly. The addition of heavier moderators and inelastic³⁸ slowing have been considered.

Selengut³⁹ gives a more exact transport approach for hydrogen machines, employing an approximate boundary condition. Davison²¹ considers hydrogeneous systems with and without reflectors.

# NON-UNIFORM FUEL LOADINGS

For the general case of arbitrary fuel loading, Eq. (98) or (105) is solved with Eq. (99) by numerical methods. Often the iterative method is useful (cf. discussion at the end of this chapter).

Two special cases of non-uniform fuel loading are of special interest in thermal reactors:

- (1) Uniform volume power density in core, or  $\sigma_{af}\phi$  = constant in core.
- (2) Uniform power density in core per unit fuel mass, or  $\phi$  = constant in core. For uniform power density per unit volume, ⁴⁰ from Eq. (101):

$$\phi = \text{const.} \times \int_{\text{core}} h(\underline{\mathbf{x}},\underline{\mathbf{x}}') d\underline{\mathbf{x}}'$$
 (115)

and:

$$\sigma_{\rm af} = \frac{\sigma_{\rm am}}{\int_{\rm core} h(\underline{x}, \underline{x}') d\underline{x}'}$$
 (116)

Goertzel⁴¹ has shown that in idealized thermal reactors the smallest critical mass is attained with a non-uniform loading that makes the thermal flux flat in the core. Both infinite and finite reflectors have been treated in multi-group formulation. In the case of water systems, the flat flux loading saves about 0.3 of the fuel requirement, but in a graphite system,⁴² the reduction is only a few percent.

^{*}We assume  $4\pi \int_0^{\infty} k(r)r^2 dr = 1$ .

When the core is restricted to a smaller size, the flat-flux solution calls for a shell of fuel at the core boundary in addition to a continuous distribution in the interior. Reactors having only the shell loading have also been studied;⁴² in a two-group thermal model, such machines are possible only if  $\eta-1>\sqrt{\tau/L}$ , and hence a shell reactor of this sort is not possible in light water. In a graphite system, the fuel needed for a shell reactor is about 30 percent greater than for a uniform core reactor.

# MULTIPLE REGIONS

# TWO-GROUP CALCULATIONS*

When a reactor consists of several regions, each of which is homogeneous, one- or two-group models may be handled with reasonable effort. Occasionally, three-group reactors have been discussed also by the method outlined below. The present discussion, however, is restricted to two-group reactors.

The standard two-group equations in the simple geometries may be written in any region

$$-\frac{D_{f}}{r^{\mu}}\frac{d}{dr}r^{\mu}\frac{d}{dr}\phi_{f} + (\sigma_{sD} + \sigma_{af})\phi_{f} = \nu\sigma_{fs}\phi_{s}$$

$$-\frac{D_{s}}{r^{\mu}}\frac{d}{dr}r^{\mu}\frac{d}{dr}\phi_{s} + \sigma_{as}\phi_{s} = \sigma_{sD}\phi_{f}$$
(117)

The subscripts f and s refer to the fast and slow groups, respectively. Within a region the cross-sections and diffusion coefficients, are constants.  $\mu = 0$ , 1, or 2 for slab, cylindrical, or spherical symmetry. For cylinders of finite height, unreflected at top and bottom, the correct equations contain:

$$-\left(\frac{D}{r}\frac{d}{dr}r\frac{d}{dr}+D\frac{d^2}{dz^2}\right)\Phi$$

as the leakage term. When the form  $\Phi = \phi(\mathbf{r}) \cos \pi z/H$ , where H is the extrapolated height, is substituted, equations of the form of Eq. (117) result, where  $\sigma_{af}$  and  $\sigma_{as}$  are the actual cross sections corrected for the longitudinal leakage. This separation may also be applied to vertically reflected cylinders where the extrapolated height involves an intelligent guess of the vertical reflector savings. Similar separations are possible for finite slabs.

The boundary and interface conditions are

(1) At center of core $\dagger$  (r = 0):

$$\frac{\mathrm{d}\phi_{\mathbf{f}}}{\mathrm{d}\mathbf{r}} = \frac{\mathrm{d}\phi_{\mathbf{g}}}{\mathrm{d}\mathbf{r}} = 0$$

(2) At outer extrapolated edge of reflector (r = a):

$$\phi_f = \phi_g = 0$$

(3) At interfaces between media  $(r = \alpha_i, i = 1, 2, ..., n - 1)$ :

^{*}Chapter 1.3 contains some discussion of the group equations.

 $[\]dagger$  In slab geometry this condition is implied by the symmetry about r = 0.

$$\phi_f$$
,  $\phi_s$ ,  $D_f \frac{d\phi_f}{dr}$ ,  $D_s \frac{d\phi_s}{dr}$  continuous

The general solution of the homogeneous equations (117) will give rise to four arbitrary constants in each of the n regions. Boundary conditions (1) and (2) yield four equations on these constants, and the interface conditions yield 4(n-1) so that the 4n arbitrary constants satisfy 4n conditions. Thus, the problem can be solved only in special cases. The critical equation expresses the conditions under which a solution can be found.*

Since the condition that 4n homogeneous equations in 4n variables have a solution is the vanishing of the determinant of coefficients, one could obtain a 4n degree determinant as the critical condition. A matrix approach⁴³ assures the vanishing of a  $2 \times 2$  determinant as the critical condition (N  $\times$  N determinant in N-group theory).

The matrix method will now be described. In each region, the general solution of Eq. (117) may be written as a linear superposition of solutions of the equation:

$$\left(\frac{1}{r^{\mu}}\frac{d}{dr}r^{\mu} + \kappa^{2}\right)\psi_{\mu}(\kappa r) = 0 \tag{118}$$

where  $\kappa^2$  satisfies the characteristic equation:

$$\begin{vmatrix} \mathbf{D_f} \kappa^2 + \sigma_{SD} + \sigma_{af} & -\nu \sigma_{fS} \\ -\sigma_{SD} & \mathbf{D_S} \kappa^2 + \sigma_{aS} \end{vmatrix} = 0$$
 (119)

Equation (119) has two roots for  $\kappa^2$ , to be written  $\kappa_1^2$ ,  $\kappa_2^2$ . For each root, Eq. (118) has two linearly independent solutions, to be written F and G. These are tabulated in Table 1.4.9 for various  $\mu$ .

In the core, one may write (with 'denoting derivative with respect to argument†) for the solution of Eq. (117) subject to the central boundary conditions (and thus involving two arbitrary constants):

$$\begin{pmatrix} \phi_{S} \\ D_{S} \frac{d\phi_{S}}{d\mathbf{r}} \\ \phi_{f} \\ D_{f} \frac{d\phi_{f}}{d\mathbf{r}} \end{pmatrix} = \begin{pmatrix} \mathbf{F}(\kappa_{1}\mathbf{r}) & \mathbf{F}(\kappa_{2}\mathbf{r}) \\ D_{S}\kappa_{1}\mathbf{F}'(\kappa_{1}\mathbf{r}) & D_{S}\kappa_{2}\mathbf{F}'(\kappa_{2}\mathbf{r}) \\ R_{1}\mathbf{F}(\kappa_{1}\mathbf{r}) & R_{2}\mathbf{F}(\kappa_{2}\mathbf{r}) \\ R_{1}D_{f}\kappa_{1}\mathbf{F}'(\kappa_{1}\mathbf{r}) & R_{2}D_{f}\kappa_{2}\mathbf{F}'(\kappa_{2}\mathbf{r}) \end{pmatrix} \begin{pmatrix} C_{1} \\ C_{2} \end{pmatrix}$$

$$(120)$$

where:

$$R_{i} = \frac{\sigma \nu_{fs}}{D_{f} \kappa_{i}^{2} + \sigma_{SD} + \sigma_{af}}$$

$$= \frac{D_{s} \kappa_{i}^{2} + \sigma_{as}}{\sigma_{SD}}$$
(121)

^{*}Form sheets and instructions for carrying out two-group calculations by hand have been published by Spinrad and Kurath, ANL-4352.

[†] i.e.  $d/dr \psi(\kappa r) = \kappa \psi'(\kappa r)$ .

Equation (120), which is a matrix equation, will be abbreviated as:

$$\psi_{\text{core}}(\mathbf{r}) = \mathbf{M}_{\text{core}}(\mathbf{r}) \begin{pmatrix} \mathbf{C}_1 \\ \mathbf{C}_2 \end{pmatrix}$$
 (122)

It is further possible to construct a propagation matrix M(r,r') in any region which has the property:

$$\psi(\mathbf{r}) = \mathbf{M}(\mathbf{r}, \mathbf{r}') \ \psi(\mathbf{r}') \tag{123}$$

This matrix is given by:

$$\mathbf{M}(\mathbf{r},\mathbf{r}') = \mathbf{A}\mathbf{B}\mathbf{C}(\mathbf{r}) \ \mathbf{C}^{-1}(\mathbf{r}') \ \mathbf{B}^{-1} \ \mathbf{A}^{-1} \tag{124}$$

where:

$$A = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & D_{S} & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & D_{f} \end{pmatrix}, \qquad A^{-1} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & D_{S}^{-1} & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & D_{f}^{-1} \end{pmatrix}$$

$$B = \begin{pmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ R_{1} & 0 & R_{2} & 0 \\ 0 & R_{1} & 0 & R_{2} \end{pmatrix}, \qquad B^{-1} = \begin{pmatrix} R_{2} & 0 & -1 & 0 \\ 0 & R_{2} & 0 & -1 \\ -R_{1} & 0 & 1 & 0 \\ 0 & -R_{1} & 0 & 1 \end{pmatrix} \frac{1}{R_{2} - R_{1}}$$

$$C(\mathbf{r}) = \begin{pmatrix} \mathbf{F}(\kappa_{1}\mathbf{r}) & \mathbf{G}(\kappa_{1}\mathbf{r}) & 0 & 0 \\ \kappa_{1}\mathbf{F}'(\kappa_{1}\mathbf{r}) & \kappa_{1}\mathbf{G}'(\kappa_{1}\mathbf{r}) & 0 & 0 \\ 0 & 0 & \mathbf{F}(\kappa_{2}\mathbf{r}) & \mathbf{G}(\kappa_{2}\mathbf{r}) \\ 0 & 0 & \kappa_{2}\mathbf{F}'(\kappa_{2}\mathbf{r}) & \kappa_{2}\mathbf{G}'(\kappa_{2}\mathbf{r}) \end{pmatrix}$$

$$C^{-1}(\mathbf{r}) = \begin{pmatrix} \frac{1}{\kappa_{1}\mathbf{W}(\kappa_{1}\mathbf{r})} & 0 & 0 & 0 \\ 0 & 0 & \frac{1}{\kappa_{1}\mathbf{W}(\kappa_{2}\mathbf{r})} & 0 & 0 \\ 0 & 0 & \frac{1}{\kappa_{2}\mathbf{W}(\kappa_{2}\mathbf{r})} & 0 \\ 0 & 0 & 0 & \frac{1}{\kappa_{2}\mathbf{W}(\kappa_{2}\mathbf{r})} \end{pmatrix}$$

$$(125)$$

$$\times \begin{pmatrix} \kappa_1 \mathbf{G}'(\kappa_1 \mathbf{r}) - \mathbf{G}(\kappa_1 \mathbf{r}) & 0 & 0 \\ -\kappa_1 \mathbf{F}'(\kappa_1 \mathbf{r}) & \mathbf{F}(\kappa_1 \mathbf{r}) & 0 & 0 \\ 0 & 0 & \kappa_2 \mathbf{G}'(\kappa_2 \mathbf{r}) - \mathbf{G}(\kappa_2 \mathbf{r}) \\ 0 & 0 & -\kappa_2 \mathbf{F}'(\kappa_2 \mathbf{r}) & \mathbf{F}(\kappa_2 \mathbf{r}) \end{pmatrix}$$

Table 1.4.9 — Solutions of Equation (118)						
μ	Geometry	$\mathbf{F}( ho)$	$\mathrm{G}( ho)$	$\mathbb{W}( ho)$		
0 ·	Slab	cos ρ	$oldsymbol{sin} oldsymbol{ ho}$	1		
1	Cylinder	$J_0( ho)$	$\mathbf{Y_0}(\mathbf{\rho})$	$\frac{2}{\pi \rho}$		
2	Sphere	$\frac{\sin}{\rho}$	$-\frac{\cos \rho}{\rho}$	$\frac{1}{\rho 2}$		

where:

$$\mathbf{W}(\rho) = \mathbf{F}(\rho)\mathbf{G}'(\rho) - \mathbf{F}'(\rho)\mathbf{G}(\rho) \tag{126}$$

and is the Wronskian of the functions F and G. It can be shown from Eq. (118) that  $W(\rho) = \text{const. } \rho^{-\mu}$ . In this notation:

$$\mathbf{M}_{\text{core}}(\mathbf{r}) = \mathbf{A} \mathbf{B} \begin{pmatrix} \mathbf{F}(\kappa_1 \mathbf{r}) & \mathbf{0} \\ \kappa_1 \mathbf{F}'(\kappa_1 \mathbf{r}) & \mathbf{0} \\ \mathbf{0} & \mathbf{F}(\kappa_2 \mathbf{r}) \\ \mathbf{0} & \kappa_2 \mathbf{F}'(\kappa_2 \mathbf{r}) \end{pmatrix}$$

The usual two-group diffusion treatments are given in the standard texts.^{35,44} Friedman⁴⁵ has considered two coupled Boltzman equations. Adler⁴⁶ considers the reduction of a two-group system to an equivalent one-group, with attention to boundary conditions. For additional references the reader should see the treatments of Spinrad,⁴⁷ and Wigner and Friedman.⁴⁸

In terms of the propagation matrices, one has:

$$\psi(\mathbf{a}) = \begin{pmatrix} 0 \\ D_{\mathbf{S}} \frac{d\phi_{\mathbf{S}}}{d\mathbf{r}} \\ 0 \\ D_{\mathbf{f}} \frac{d\phi_{\mathbf{f}}}{d\mathbf{r}} \end{pmatrix}_{\mathbf{r}=\mathbf{a}} = \mathbf{M} \begin{pmatrix} C_{1} \\ C_{2} \end{pmatrix}$$
(127)

where the matrix M is the product:

$$\mathbf{M} = \mathbf{M}(\mathbf{a}_1 \alpha_{n-2}) \mathbf{M}(\alpha_{n-2}, \alpha_{n-2}) \dots \mathbf{M}(\alpha_2, \alpha_1) \mathbf{M}_{core}(\alpha_1)$$
(128)

and is of the form:

$$\mathbf{M} = \begin{pmatrix} \beta_1 & \gamma_1 \\ \beta_2 & \gamma_2 \\ \beta_3 & \gamma_3 \\ \beta_4 & \gamma_4 \end{pmatrix}$$

It follows that:



$$\begin{vmatrix} \beta_1 & \gamma_1 \\ \beta_2 & \gamma_3 \end{vmatrix} = 0 \text{ is the critical condition.}$$

Alternate methods reducing the  $4n \times 4n$  problem are possible. Thus, for example, two sets of particular solutions  $\phi_f$ ,  $\phi_g$  may be chosen in the outer region. Each solution is then worked inward by matching at the interfaces until the core radius (assumed known or unknown) is reached. A linear superposition of these solutions with arbitrary coefficients may then be matched to the core solutions (also involving two unknown constants) to provide four equations in the four unknowns. The problem is thus reduced to an equivalent two region problem.

Also of interest is a "back-and-forth" or trial-and-error method. In this method as used for non-multiplying reflectors, the fast flux, which is known in the outermost region, is worked back to the core boundary, the position of which is guessed. From the known core composition, the slow flux can be calculated in the core and worked forward through the reflectors. It will not, in general, vanish at the extrapolated reactor boundary. The process is repeated with another guess of the location of the core boundary. Although tedious, the method has been used effectively in three-group calculations.

# **MULTI-GROUP CALCULATIONS***

The main method used for solution of multi-group equations with more than two-groups is a numerical iterative method.^{50,51} In a simple form, this may be described as follows. The equations are of the form:

$$-\frac{1}{r^{\mu}}\frac{d}{dr}D_{i}r^{\mu}\frac{d}{dr}\phi_{i} + \sigma_{i}\phi_{i} = \sum_{j=1}^{i-1}k_{ij}\phi_{j} + f_{i}S$$
(129)

where:

$$S = \nu \sum_{i} \sigma_{fj} \phi_{j} \tag{130}$$

and  $S/\nu$  is the fission density. The value of  $\nu$  for which Eqs. (129) and (130) have a solution may be obtained as follows. Given an  $S^{(n)}(r)$ , Eq. (129) is solved in sequence for  $i=1,2,\ldots$  to obtain  $\phi_i^{(n)}$ . Then, substitution of these  $\phi_i^{(n)}$  in Eq. (130) yields  $S^{(n+1)}(r)$ . This process is started by guessing  $S^{(0)}(r)$  ( $S^{(0)}=1$  is good enough) and is continued

This process is started by guessing  $S^{(0)}(r)$  ( $S^{(0)}=1$  is good enough) and is continued until  $\nu$  (r) =  $S^{(n)}(r)/S^{(n+1)}(r)$  is substantially constant (independent of r). If the  $\nu$  thus obtained is not that characteristic of the fuel, the assumed composition of the reactor is varied and the computation repeated.

The  $\phi_i^{(n)}$  are usually obtained by numerical integration of the differential Eq. (129) subject to the boundary conditions:

$$\frac{d\phi_i}{dr} = 0 \quad \text{at } r = 0$$

$$\phi_i = 0 \quad \text{at } r = a \text{ (outer boundary)}$$
(131)

Standard methods may be used for the numerical integration. However, owing to the form of the boundary conditions, a particular solution of the differential equation  $\phi_{ip}$  and a homogeneous solution  $\phi_{iH}$  are both obtained by integration in the direction of increasing r. Then:

$$\phi_i = \phi_{iP} + \alpha \phi_{iH}$$

^{*}Chapter 1.3 contains some discussion of the group equations.

is again a particular solution. The value of  $\alpha$  is so chosen that:

$$\phi_i(a) = 0$$

The calculations involved in the above iteration method are tedious. The advent of modern electronic computing machines has tended to make this method become one of the most important techniques, especially for intermediate reactors. One major advantage is that arbitrary variations of reactor properties with r do not materially add to the difficulty of solution.

#### ODD SHAPES

A number of references on various shape reactors are given above under "One-velocity Reactors" and in Table 1.6.8. One should note also work by Davison⁵² on extension of the spherical harmonics method to more complex shapes.

Numerous numerical approaches, such as relaxation methods, permit attack on novel geometries, especially in one-group systems, as do the electrical network or simulator analogue machines. Weinberg⁵³ mentions source-and-sink methods for handling odd shapes, corner situations, and the like; compare also the Wheeler control volume referred to in Chapter 1.6 regarding the uses of source-sink methods for bounding solutions. The following discussion of perturbation theory also indicates methods of frequent utility.

Monte Carlo methods permit attack, especially with the aid of modern computing machines, on energy-dependent reactors having odd shapes or multiple regions.

### NON-UNIFORM MEDIA

Some instances of space-variable systems were mentioned above under "Non-uniform Fuel Loading."

Some solutions have been obtained for the one-group reactor equation with variable buckling; ^{54,55,56,57} the quantity which satisfies that equation may involve other factors in addition to the neutron flux. ⁵⁸

Goertzel⁵⁹ has investigated the conditions under which the Fermi equation for a bare reactor of variable density may be separated into space and energy equations, thus permitting solution of the problem by elementary methods. Formulae are given which apply to thermal reactors, resonance reactors, and mixed thermal-resonance reactors. He has further used a mode method⁶⁰ to study solutions of the Fermi-age equation for variable density moderator and non-uniform fuel distribution.

A transverse gap extending across a reactor has been studied theoretically and experimentally to some extent. References are given in the last part of Chapter 1.6. Empty channels such as those used for gas cooling have received considerable attention. 61,62

# PERTURBATION THEORY

# THE EIGENVALUE PROBLEM

Some of the mathematical techniques of handling eigenvalue problems are directly applicable to the reactor equations. Of specific importance are the perturbation and variation methods and the iteration methods.

The Boltzmann equation or any of its approximations may be written as:

$$\frac{\partial \mathbf{n}}{\partial t} = \mathbf{H}\mathbf{n} \tag{132}$$



where n is the neutron density,* and the operator H does not depend† on n and is therefore linear. Further, H has has the form:

$$\mathbf{H} = \nu \mathbf{J} - \mathbf{K} \tag{133}$$

where  $\nu$  is the number of neutrons per fission.

Equation (132) may be transformed into an eigenvalue problem in several ways. One method considers the normal mode solutions:

$$\frac{\partial n}{\partial t} = \lambda n$$

for which the eigenvalue  $\lambda$  satisfies:

 $\lambda n = Hn$ 

If the greatest  $\lambda$  value is zero, the reactor is critical. A second method considers the critical or steady-state problem:

$$\frac{\partial n}{\partial t} = 0$$

for which the eigenvalue  $\nu_{\rm c}$  satisfies:

$$\nu_{\rm c} \, {\rm Jn} = {\rm Kn} \tag{134}$$

The lowest  $v_c$  value is then the value of v required to maintain a steady chain reaction.

## PERTURBATION AND VARIATION METHODS

Let  $d\tau$  be the volume element such that  $\int nd\tau$  is the total number of neutrons in the reactor. Define the operator  $M^+$  adjoint to M by the requirement that:

$$\int \mathbf{u} \mathbf{M} \mathbf{v} \mathbf{d} \tau = \int \mathbf{v} \mathbf{M}^{+} \mathbf{u} \mathbf{d} \tau \tag{135}$$

for all real functions u, v that satisfy the boundary conditions on n. The operators H, J, and K are usually not self-adjoint. That is,  $H = H^+$  is not usually true.

Consider, as an example, Eq. (134) and the adjoint equation:

$$v_{c} \mathbf{J}^{+} \mathbf{m} = \mathbf{K}^{+} \mathbf{m} \tag{136}$$

and the equation for the "perturbed" problem:65

$$v_{\rm c}' \mathbf{J}' \mathbf{n}' = \mathbf{K}' \mathbf{n}' \tag{137}$$

^{*}n is a function of energy, neutron velocity direction, and position.

[†] In power reactors, the cross sections contained in H depend on the power through temperature and density effects, thus causing H to become non-linear. This case is treated in Chapter 1.6.

[†] For the form of H, J, K, cf. Chapter 1.6, "General Equations" and "Two-group, Bare, Thermal Reactor."

[§] Delayed or latent neutrons are considered in Chapter 1.6.

Multiplication of Eq. (137) by m and Eq. (136) by n' and integration of each product followed by a subtraction leads to, after use of Eq. (135):

$$\delta \nu_{\mathbf{c}} = \frac{\int \mathbf{m}(\delta \mathbf{K}) \mathbf{n}' d\tau - \nu_{\mathbf{c}}' \int \mathbf{m}(\delta \mathbf{J}) \mathbf{n}' d\tau}{\int \mathbf{m} \mathbf{J} \mathbf{n}' d\tau}$$
(138)

where δ's denote the primed quantity minus the unprimed quantity. This exact* result may be written in three approximate forms:

$$\delta \nu_{\rm c} = \frac{\int \, \mathrm{m} \delta \mathrm{Kn'} \mathrm{d}\tau - \nu_{\rm c}' \, \int \, \mathrm{m} \delta \mathrm{Jn'} \mathrm{d}\tau}{\int \, \mathrm{m} \mathrm{Jn} \mathrm{d}\tau}$$
(138a)

$$\delta \nu_{c} = \frac{\int m\delta K n d\tau - \nu_{c}' \int m\delta J n d\tau}{\int mJ n d\tau}$$
(138b)

$$\delta \nu_{c} = \frac{\int m\delta K n d\tau - \nu_{c} \int m\delta J n d\tau}{\int mJ n d\tau}$$
 (138c)

Forms (138b) and (138c) have the advantage of not requiring knowledge of the perturbed density n'. The value of  $\nu_{\rm C}'$  in some applications of Eq.(138b) is simply  $\nu$ . In some important cases, however, such as in the measurement of danger coefficients, the perturbation is localized in space, and perhaps in energy, and causes an appreciable local perturbation in n. When this occurs,  $\delta {\rm Kn'}$  or  $\delta {\rm Jn'}$  may be experimentally or computationally determined and the more correct result, Eq. (138a), becomes applicable.

The variational method of arriving at form (138c) has the added advantage of leading to a method for estimating the eigenvalue  $\nu_c$ . It is based on the fact that the equality:

$$\nu_{c} = \frac{\int mKn}{\int mJn} = \frac{\int nK^{+}m}{\int nJ^{+}m}$$
 (139)

holds when any function is used for n so long as m satisfies Eq. (136) and when any function is employed for m provided n satisfies Eq. (137). Thus, if changed or assumed values m' and n' are used in place of m and n, the change or error,  $\delta\nu_{\rm c}$ , is proportional to the product (m-m')(n-n'). Another way of stating this result is to say that expression (139) for  $\nu_{\rm c}$  is stationary with respect to variations of m and n about their correct values. Form (138c) is obtained from Eq. (139) by varying m, n, K, and J and neglecting terms containing the product  $\delta$ m  $\delta$ n.

## THE REACTIVITY

# THE ADOPTED DEFINITION

The reactivity, here denoted by R, generally means a quantity measuring the departure of a reactor from criticality, being unity for a critical reactor, greater than unity for a supercritical reactor, and less than unity for a subcritical reactor. In dynamic considerations, where R plays the role of an effective multiplication constant, the definition of the characteristic time is fixed by the definition adopted for reactivity.

^{*} The approximation  $\delta(\nu_c J) = \delta \nu_c J + \nu_c \delta J$  has been made.

A simple and useful definition* of reactivity is:

$$R = \frac{\nu}{\nu_c} \tag{140}$$

Thus, R is the eigenvalue of the equation:

$$\mathbf{RKn} = \nu \mathbf{Jn} \tag{141}$$

which is simply a rewrite of Eq. (134). Similarly, the adjoint equation:

$$\mathbf{R}\mathbf{K}^{+}\mathbf{m} = \nu \mathbf{J}^{+}\mathbf{m} \tag{142}$$

is a rewrite of Eq. (136). Thus, as in Eq. (139) the equality:

$$R = \frac{\nu \int mJnd\tau}{\int mKnd\tau}$$
 (143)

has the stationary property. Further, the relation:

$$\frac{\delta R}{R} = \frac{\delta \nu}{\nu} - \frac{\delta \nu_{\rm C}}{\nu_{\rm C}} \tag{144}$$

gives the difference in reactivity between two slightly different reactors, where  $\delta \nu_c$  is given by Eq. (138) or any of its approximate forms.

## INTERPRETATION BY IMPORTANCE

The adjoint function m as given by Eq. (136) or Eq. (142), represents the importance† of a neutron towards maintaining the chain reaction. For any neutron distribution n, not necessarily satisfying Eq. (141), the quantity  $\nu \int m J n d\tau$  is then the creation rate of importance via fission neutrons, and  $\int m K n d\tau$  is the net destruction rate of importance owing to scattering, absorption, and leakage. Thus, Eq. (143), which is correct for any n, states that the reactivity is the multiplication constant as measured by importance (rather than by neutron number). The significance of the stationary character of Eq. (143) is that the reactivity as defined depends only on the reactor characteristics  $\nu$ , J, and K and is independent of changes in the neutron distribution within the reactor.

Equation (144) may be simply interpreted when form (138c) is substituted for  $\delta\nu_c$ . The result may be arranged to state that the fractional increase of reactivity is equal to the fractional increase in creation rate of importance minus the fractional increase in destruction rate of importance.

The characteristic or effective generations time 1 is given by

$$1 = \frac{I}{\int mKnd\tau} = \frac{\int mnd\tau}{\int mKnd\tau}$$
 (145)

^{*}This is the definition used by the KAPL physics group.

[†] See Chapter 1.6 for a physical definition of this quantity. The function m is the same as the "iterated fission probability," a term employed by the KAPL group. Cf. KAPL-98 for a comparison of this with the fission probability.

in terms of which, the dynamic equation* based on Eq. (132) may be written. The quantity I is interpreted as the total importance of neutrons, and the time I is then the average turnover time of importance, being given by the total importance divided by the destruction rate of importance.† If  $\nu$  were suddenly made zero (and thus  $R \rightarrow 0$ ), there would be no further production, and as a result, the total importance I would decay as  $e^{-t/1}$ 

Equation (5) states that the importance m of a neutron in a critical reactor is equal to the average importance of the neutrons emerging from the first collision. Equations (7a) and (7b) state that the importance of a neutron is given by the importance of the first generation fission neutrons resulting from the neutron in question. Equation (7c) defines m to be the average importance of a fission neutron.

#### ITERATION METHODS

One useful method of solving:

$$\frac{\nu}{R}$$
 Jn = Kn

proceeds as follows. One guesses  $Jn_0$  and solves the equations:

$$\mathbf{K}\mathbf{n}_{k+1} = \mathbf{J}\mathbf{n}_{k}$$

for 
$$k = 0, 1, ...$$

Then:

$$\lim_{k\to\infty}\frac{n_k}{\int n_k d\tau} = n$$

and:

$$\lim_{k\to\infty} \frac{Jn_{k+1}}{Jn} = \frac{R}{\nu}$$

Clearly the method is useful only if the convergence is rapid, as is the case for small reactors. Also, owing to the form of the operator J, one can usually guess  $Jn_0$  easily. This is because  $Jn_0$  is the fission distribution multiplied by the fission spectrum. A similar approach also applies to the adjoint equations:

$$\frac{\nu}{R}$$
 J + m = K + m

Often it is useful to calculate in this way  $m_k$  and  $n_{k'}$  (for k = k' = 1 possibly) and obtain R from Eq. (143). This is usually extremely accurate even with k = k' = 1.

^{*} Chapter 1.6 treats the effect of delayed neutrons and further discusses Eqs. (132) and (144).

[†] A somewhat more physical definition by Hurwitz is that l is the weighted average of the time required by a fission neutron to produce another fission. A fission source is assumed to have a spatial distribution like the normal power distribution, and each resulting fission is weighted by the importance of the neutrons to which it gives rise.

## REFERENCES

- 1. Carlson, AECD-2835.
- 2. LADC-79.
- 3. Carlson and Peterson, LA-1061 (also LADC-756).
- 4. Frankel and Goldberg, AECD-2056 (also LADC-76).
- 5. Wilson, Birmingham Report MS-105 (classified).
- 6. Serber, LA-234 (classified).
- 7. Davison, LT-18, Chapter III.
- 8. Melvin, AERE-T/R 586 and 587.
- 9. Sweeney, Goldstein, and Carlson, LA-1364, LA-1365, and LA-1366.
- 10. Fairbrother, MS-111.
- 11. G. Wassermann, C. R. Acad. Sci. Paris, 223, 537-539, Oct. 1946.
- 12. Scalletar, MonP-33, pp 16 and 17 (classified).
- 13. CP-1456 (classified).
- 14. Murray, C- and CCC-Y-12 (classified).
- 15. Weinberg and Noderer, p V-128 (classified).
- 16. Young, MonP-427 (classified).
- 17. Preston and Davison, MS-112.
- 18. Davison, CRT-361.
- 19. Nordheim, MonP-17 (classified).
- 20. Feynman, Welton, Ashkin, Ehrlich, Peshkin, and Reines, LA-524 (classified).
- 21. Davison, AERE T/R-826.
- 22. Selengut, AECD-3024.
- 23. Volkoff, MT-21 (classified).
- 24. CRT-391.
- 25. MT-38 (classified).
- 26. French and Hurwitz, KAPL-41 (classified).
- 27. Volkoff and Le Caine, MT-30 (classified).
- 28. Greuling, LA-399 (classified) and LA-493 (classified).
- 29. Garabedian and Weinberg, MonP-434 (classified) and MonP-435 (classified).
- 30. Glasstone and Edlund, The Elements of Nuclear Reactor Theory, p 352 and following pages, Van Nostrand, 1952.
- 31. Friedman, Nuclear Reactors, AIEE series on Nucleonics for Engineers, 1949.
- 32. Glasstone and Edlund, op. cit., Chapter XIL.
- 33. Weinberg, Am. Jour. Physics, 20, p 401, 1952.
- 34. Weinberg and Noderer, Theory of Neutron Chain Reactions, ORNL CF-51-5-98 (2 classified volumes and 1 unclassified volume).
- 35. Soodak and Campbell, Elementary Pile Theory, John Wiley and Sons, New York, N. Y., 1950.
- 36. Goertzel, TAB-53 (classified).
- 37. Shapiro and Preiser, ORNL-1176 (classified).
- 38. Ibid., p 18 (classified).
- 39. Selengut, APEX-121 (classified).
- 40. J. E. Wilkins, Jr., unpublished.
- 41. Goertzel, Reactor Sci. Tech. TID-2001, April 1952 (classified).
- 42. Klahr, unpublished.
- 43. Householder and Garabedian, MonP-202 (unclassified) and MonP-246 (classified).
- 44. Glasstone and Edlund, op. cit., Chapter VIII.
- 45. Friedman, unpublished (classified).
- 46. Adler, CRT-395.
- 47. Spinrad, MonP-284 (classified).
- 48. Wigner and Friedman, CP-1662 (classified).
- 49. Nordheim, CP-2222, p 18.
- 50. Hurwitz and Ehrlich, Jour. Reactor Sci. Tech., to be published.
- 51. Safanov, RM-462 (classified), RM-570 (classified), R-233, and TID-2004 (classified).
- 52. Davison, AERE T/R-700; Flanders and Shortly, Jour. Applied Phys. 21, 1950, p 1326.
- 53. Weinberg, MonP-187 (classified).
- 54. Morehouse, CP-1069 (classified).
- 55. Chernick, BNL-126 (classified).
- 56. CF-3599 (classified).
- 57. Oak Ridge Memo CL-GY-6 (classified).
- 58. Chicago Handbook, Chapter IV E, p 9.
- 59. Goertzel, MonP-313 (classified).
- 60. Lexington Project Report 103 (classified).
- 61. Kaplan and Chemick, BNL-152, pp 29-31 (classified).
- 62. Davison, AERE T/R-738.
- 63. Brooks, KAPL-304 (classified).

# CHAPTER 1.5

# Reactor Statics; Experimental and Numerical Results

Mathew M. Shapiro

Classification of critical mass and related data involves numerous parameters and might be done in various ways. For example, reactors are frequently classified as fast, intermediate or resonance, semi-thermal, thermal, or mixed (i.e., fast in one part of the reactor and slow in another) according to their neutron energies. Another common classification is by moderator material. This will be employed here with energy types used as modifying or descriptive terms. Somewhat arbitrarily, "unmoderated" will be used to mean "unmoderated by carbon or lighter elements."

Ages for fission neutrons in a number of common moderators and water-metal mixtures are given in Tables 1.5.1 and 1.5.2; the spatial slowing-down distributions for some of these are shown in Figs. 1.5.1 to 1.5.6. Table 1.5.3 gives experimental ages for Ra-Be neutrons in some water-metal mixtures. Thermal diffusion lengths appear in Table 1.5.4.

### HOMOGENEOUS REACTORS

# MODERATED CORES

# HYDROGEN MODERATORS

By fitting the measured slowing-down distribution of fission neutrons in water with a synthetic kernel, Greuling has calculated the critical mass of water-moderated, spherical reactors having an infinite water tamper. Those results which apply to highly enriched uranium appear in Fig. 1.5.7.

The water boiler reactors (LOPO, HYPO, and SUPO) are described in Table 1.5.5. Figures 1.5.8 and 1.5.9 show thermal- and fast-flux distributions for the low-powered assembly with a BeO tamper.

Tests of various tamper materials have been made by observing their effects either on the criticality of the low-powered water boiler or on its multiplication of a natural source when a small part of the BeO tamper was replaced by the specimens. BeO bricks were removed from a 3-in. ×3-in. area extending radially from the core surface to the outside of the tamper (one foot thick) and replaced by the material to be tested. The estimated change in critical mass for the materials, when used bare and when covered by 0.030 in. of Cd. is given in Table 1.5.6 relative to bare and Cd-covered BeO.

The result of a critical experiment on the HRE is shown in Table 1.5.7.

In addition to the calculations mentioned above which are directly related to critical experiments, some additional theoretical results are of interest.

The calculated effect of varying the tamper material around a spherical core of fixed composition is shown in Table 1.5.8. The theoretical results for an infinite  $D_2O$  reflector and different fuel concentrations appear in Table 1.5.9.

Figure 1.5.10 shows the minimum critical mass of a water-tamped pure U²³⁵-H₂O spherical core as a function of core radius. The least mass (0.69 kg of U²³⁵) occurs for a radius of 16.7 cm. The shape of the fuel distribution required to minimize the mass is shown in Fig. 1.5.11. For a radius smaller than 16.7 cm, some of the fuel is lumped at the core-reflector interface. Figure 1.5.12 shows the fuel loading for a core of 13 cm radius.

#### D MODERATORS

Oak Ridge measurements for enriched U²³⁵ thermal D₂O systems with D₂O reflectors* appear in Table 1.5.10 and Argonne results for bare, natural-U, homogeneous systems in Table 1.5.11.

A number of computations performed by Nordheim and his group are given in Tables 1.5.12 through 1.5.16. These include bare,  $D_2O$ , and graphite reflectors and Pu and  $U^{236}$ - $U^{236}$  fuel. Table 1.5.17 gives  $D_2O$  reflector savings.

Calculated results for bare reactors with natural or slightly enriched U are shown in Fig. 1.5.13, and for natural U with perfectly pure D₂O in Table 1.5.18.

#### LATTICES

The term "lattice" as used herein applies to large thermal reactors usually using natural uranium.

# THEORY -

In the following discussion, the notation in Table 1.5.19 will be adopted.

VALUE OF n

In terms of basic constants, the number of neutrons from thermal fission per thermal neutron absorbed in U is:

$$\eta = \frac{\sigma_{\rm f}(25) \ N_{25} \ \nu_{25}}{\left[\sigma_{\rm f}(25) + \sigma_{\rm c}(25)\right] \ N_{25} + \sigma_{\rm c}(28) \ N_{28}} \tag{1}$$

With recent data^{7,8} as follows:

$$\nu_{25} = 2.5 \pm 0.1$$

$$\frac{\sigma_{C}(25)}{\sigma_{f}(25)} = 0.183 \pm 0.008$$

$$\sigma_{f}(25) = 549 \pm 8b$$

$$\sigma_{c}(28) = 2.80 \pm 0.07b$$

$$\frac{N_{28}}{N_{25}} = 137.8 \pm 1$$

^{*}The new Argonne experimental reactor (CP-5) is to be of this type, with about 1.1 kg of U²³⁵ held in Al plates in a core 2 ft in diameter and height surrounded by about 2 ft thickness of reflector. 6 References appear at end of chapter.

one obtains  $\eta = 1.33 \pm 0.05$  for natural U. This accuracy is not adequate for low-k reactors.

Greater accuracy may be obtained with exponential and critical experiments, in which  $\eta$  is one of the parameters involved. The value of  $\eta$  usually quoted from the early Chicago graphite exponentials, using  $\epsilon$ , p, f, and  $M^2$  values calculated by the standard formulae, is 1.315.

If measured thermal utilizations are used instead of the calculated values, Way¹¹ finds*  $\eta = 1.340 \pm 0.7\%$  which agrees well with the value obtained from homogeneous D₂O exponential experiments.¹²

#### FAST EFFECT

In addition to the thermal fissions in  $U^{235}$ , there are also a few fast fissions produced in the uranium before the fast neutrons escape from the uranium lumps. The result of this effect is to increase the number of available fast neutrons by a factor  $\epsilon$  given, according to a one-group theory with appropriate fast constants, by:

$$\epsilon - 1 = \frac{\left(\frac{\nu \sigma_{f} - \sigma_{f} - \sigma_{c}}{\sigma_{t}}\right)(\mathbf{P})}{1 - \left(\frac{\nu \sigma_{f} + \sigma_{cl}}{\sigma_{s}}\right)(\mathbf{P}')} = \frac{\mathbf{GP}}{1 - \mathbf{SP'}}$$
(2)

Here P is the probability of a fission neutron from  $U^{235}$  colliding within the lump before escaping, and the numerator, GP, thus expresses the net neutron gain from such first-flight collisions. SP fast neutrons emerge from these first collisions within the lump, and a fraction P' of these, in turn, collide before escaping. The net gain in neutrons from these second-round collisions is thus SPGP', or SP' = x times the gain in the first collision. Assuming P' to be the same for all succeeding rounds of collisions, one obtains the factor  $1 + x + x^2 + \ldots = 1/(1-x)$ , which gives the above formula.

The calculation of P and P' is a geometrical problem, with P evaluated for a source distributed like the thermal neutron flux in the lump, while for P' the source after one collision is assumed to be uniform throughout the lump. If the distribution of thermal neutrons within the lump is taken as that characteristic of diffusion into the lump, one has P as a function of  $\kappa$  and R (where R is the dimension of the lump and  $1/\kappa$  is its thermal-diffusion length) and also of the macroscopic total fast cross section,  $N\sigma_t$ , as follows:  $P = P(N\sigma_t R, \kappa/N\sigma_t)$ , with  $P' = P(N\sigma_t R, O)$ . Curves for P are given in Fig. 1.5.14.

Table 1.5.20 gives constants for natural U; the set of numbers yields results which agree with experimental results, as shown in Table 1.5.21. Values for metal rods are given in Table 1.5.22; for smaller sizes,  $\epsilon$ -1 is proportional to the radius r or, if the density be altered, to  $\rho$ r. In some early calculations, ¹³ the values of  $\epsilon$ -1 used for U₃O₈ were about 0.8 of the values for metal of the same  $\rho$ r.

In close-packed lattices (e.g., light-water moderator) fast neutrons may travel from one lump to another and give interaction effects in  $\epsilon$ . ^{14,15}

### THERMAL UTILIZATION

In the case of a homogeneous reactor, the thermal utilization is the ratio of uranium thermal absorption cross section to total thermal absorption cross section. In a heterogeneous reactor, thermal neutrons are born in the moderator and must diffuse into the fuel, so that the average thermal flux in the fuel element is lower than that in the mod-

[†]For the formulae see CP-644. For hollow cylinders see Guggenheim and Pryce, MT-199; do not use CP-644 for this case.



^{*} This is for the entire set of 44 Chicago graphite exponentials.

erator. This depression in flux decreases the thermal utilization from the value it would have in the homogeneous situation.

Most lattice calculations use a formula, Eq. (3), for f derived from simple diffusion theory. This appears 16 to give values of f about 2 percent greater than measured values.

Some compensation for the errors of simple diffusion theory can be obtained by altering certain of the constants which enter. More precise calculations using the  $P_3$  approximation are currently receiving attention.

The diffusion theory result is given here for the following configuration. A central region of radius  *   $r_0$  is filled with uranium. Following this is a sheath of absorbing but non-moderating material (e.g., steel or aluminum jacket). Following this is an air gap and finally, extending from  $r_1$  to  $r_2$ , moderator.  $r_2$  is the effective outer radius of the moderator such that the volume (and mass) of moderator is that actually associated with a cell. It is assumed that the slowing-down density into thermal is uniform throughout the moderator volume and that there is no neutron current across the outer boundary  $r_2$ . Then:

$$\frac{1}{f} - 1 = F(\kappa_0 r_0) \left( \frac{N_1 \sigma_{21} V_1 + N_2 \sigma_{22} V_2}{N_0 \sigma_{20} V_0} \right) + X (\kappa_2 r_1, \kappa_2 r_2)$$
(3)

where  $V_0$ ,  $V_1$ ,  $V_2$  are volumes;  $N_0$ ,  $N_1$ ,  $N_2$  atomic densities; and  $\sigma_{a\,0}$ ,  $\sigma_{a\,1}$ ,  $\sigma_{a\,2}$ , absorption cross sections for fuel, sheath, and moderator, respectively.  $\kappa_0$  is the reciprocal diffusion length in fuel and  $\kappa_2$  that in moderator. F and X are functions as given in Table 1.5.23 and Figs. 1.5.15 through 1.5.17. Clearly F=1, X=0 corresponds to the homogeneous case. F is the ratio of the thermal neutron density at the surface of the uranium rod to the average thermal neutron density in the rod. X measures the "excess" neutron absorption in the moderator due to the excess neutron density in the moderator over that at the moderator air interface. The rise in neutron density across the jacket (blocking effect) has been neglected. It is usually a small effect for a thin jacket layer. 17

Thermal constants are found in Table 1.5.4 and in Chapter 1.2. The derivation of Eq. (3) is such that Maxwell-averaged cross sections would be used, except as one alters the constants to compensate somewhat for the errors of diffusion theory. In graphite lattices, this is accomplished by increasing the value of the graphite capture cross-section  $\sigma_{a2}$  where it appears explicitly in Eq. (3). Thus, whereas for AGOT graphite the best value of the ratio of its capture cross-section to that of U is  $0.67 \times 10^{-3}$ , it is customary to employ in Eq. (3) a value of  $0.78 \times 10^{-3}$ ; i.e., in effect to increase the graphite capture cross section by  $\frac{1}{6}$ . This decreases f in typical graphite lattices by about 1.5%.

## RESONANCE ESCAPE PROBABILITY

In the homogeneous medium with absorption and elastic moderation, the resonance escape probability according to the Wigner slowing-down theory (cf. "Slowing Down with No Space Variation," Chapter 1.3) is of the form:

$$p = \exp\left(-\int \frac{\sigma_{ii}}{\sigma_{2i} + \sigma_{5i}} \frac{dE}{\xi E}\right) \tag{4}$$

This formula is exact for (a) moderation only by hydrogen or (b) absorption only in separated sharp lines. For U resonance capture, (b) very nearly obtains and also the ab-

^{*}In spherical or cylindrical geometry. In slab geometry, radii are to be interpreted as distances from the plane of symmetry.

sorption is confined to a fairly small energy region so that variation in  $\xi$  and  $\sigma_S$  may usually be neglected. Then:

$$p = \exp\left(-\frac{A}{\xi \sigma s}\right) \tag{5}$$

where:

$$\sigma_{\mathbf{a}} \, \operatorname{eff} = \frac{\sigma_{\mathbf{a}}}{1 + \frac{\sigma_{\mathbf{a}}}{\sigma_{\mathbf{s}}}} = \alpha \tag{6}$$

$$\int \sigma_{\mathbf{a} \text{ cff}} \cdot \frac{d\mathbf{E}}{\mathbf{E}} = \int \alpha \frac{d\mathbf{E}}{\mathbf{E}} = \mathbf{A}$$

The above cross sections are macroscopic;  $\sigma_S$  includes the scattering of the U and all lighter atoms, and  $\xi$  is weighted over all the scatterers so that  $\xi$   $\sigma_S$  gives the total slowing-down power.

The notation of Eq. (6) is also used for microscopic cross sections. It is seen that the value of A per U atom should depend only upon the total scattering cross section per U atom (assumed independent of energy). Figures 1.5.18 and 1.5.19 give experimental results for U and Th, while Table 1.5.24 gives asymptotic values for infinite dilution with moderator. The effective absorption integral for U is increased by a factor of 26 as the dilution goes from zero to infinity; for Th, the factor is 4. Table 1.5.34 gives resonance integrals for a number of other materials.

In a system with lumped fuel elements, one has volume absorption within the lump appropriate to the homogeneous material there, plus sharp-line absorption at the lump surface of neutrons coming from the moderator outside. Thus, for lumps which are not too small, one would expect:

$$\sigma_{a \text{ eff}} = \alpha + \beta \frac{S}{M} \tag{7}$$

Here  $\alpha$  is as before while, by a somewhat more complex argument,  18 ,  19 ,  20   $^{4}\beta = \rho(\alpha/\sigma_s)^2$ ; S, M, and  $\rho$  are the surface area, mass, and density of the lump, respectively. Thus, the effective absorption integral is of the form:

$$\int \sigma_{a \text{ off}} \frac{d\mathbf{E}}{\mathbf{E}} = \mathbf{A} + \mu \frac{\mathbf{S}}{\mathbf{M}}$$
 (8)

For U, Figs. 1.5.18 and 1.5.20 indicate the variation in A and  $\mu$  with scattering dilution; Table 1.5.25 gives values from experimental measurement on metal, and Table 1.5.26 includes values which have been used for compounds.

In addition to the above "self-protection" considerations, in lattice computations one also takes into account the depression in resonance neutron flux at the fuel rod of the same kind as discussed under thermal utilization. Thus:

$$\mathbf{P} = \mathbf{e}^{-1/T} \tag{9}$$

$$T = \left(\frac{N_2 V_2 (\overline{\xi} \sigma_S)_2}{N_0 V_0 \int \sigma_{a0 \text{ eff}} \frac{dE}{E}}\right) F (R_0 r_0) + X (\overline{\kappa}_2 r_1; \overline{\kappa}_2 r_2)$$
(10)

where the bar signifies resonance neutrons, 0 and 2 refer to fuel and moderator, respectively, and the cross sections are microscopic.

Values used for  $\overline{\kappa}_0$  are 0.0222  $\rho$  for  $U^7$  and 0.025  $\rho$  for  $U_3O_0$ , where  $\rho$  is density in gm/cm³. Moderator constants are given in Table 1.5.27.

AGE

An approximate formula for the age of neutrons in a lattice¹⁷ is:

$$\tau = \left| \tau_{\rm in} \frac{\sigma_{\rm in}}{\sigma_{\rm t}} P + \tau_{\rm f} \left( 1 - \frac{\sigma_{\rm in}}{\sigma_{\rm t}} P \right) \right| \left( \frac{V_{\rm t}}{V_2 + \frac{1}{2} V_0} \right)^2 \tag{11}$$

where the total volume,  $V_t$ , is comprised of the lump volume,  $V_0$ , the moderator volume,  $V_2$ , and such void volume as may be present. The age to thermal of fission neutrons in the moderator,  $\tau_f$ , is given in Table 1.5.1; the age  $\tau_{in}$  of inelastically scattered neutrons in the moderator has been estimated at 231 cm² for graphite of density 1.6. The quantity P is the same as in Eq. (2). The above formula, in effect, supposes that the lumps contribute no elastic slowing-down but have (per unit volume) the same average scattering power as the moderator.

In the presence of empty channels, neutron streaming and anisotropic effects enter (e.g., reference 7, p. 29 ff).

### THERMAL DIFFUSION AREA

If  $L_2^2$  is the moderator thermal diffusion area, the fuel lumps absorption is taken into account by using:

$$L^2 = f_2 L_2^2 \tag{12}$$

Here  $f_2$  is the thermal utilization of the moderator, i.e., the fraction of all thermal absorptions in the lattice which occur in the moderator. In the notation of Eq. (3) above:

$$f_2 = 1 - f \left[ 1 + \left( \frac{N_1 \sigma_{:11} V_1}{N_0 \sigma_{a0} V_0} \right) \mathbf{F} (\kappa_0 \mathbf{r}_0) \right]$$
 (13)

Because of the higher temperature of the neutrons in a lattice,  $L_2^2$  is somewhat greater than the values (Table 1.5.4) based on sigma-pile measurements; e.g., the neutron temperature (reference 7, p. 31) in the Oak Ridge graphite reactor is about 140°C higher than the graphite temperature, whereas in a sigma-pile, the neutron temperature is about 80°C above the graphite temperature. In materials with constant scattering cross-section,  $L^2$  is proportional to the square root of the absolute neutron temperature.

Neutron streaming and anisotropic effects appear when there are empty channels (reference 7, p. 29 ff).



## **EXPERIMENTAL AND NUMERICAL RESULTS**

#### **GRAPHITE**

A series of 44 graphite exponential experiments was carried out at Chicago during the war and subsequently analyzed by Way and Cashwell; their final report was never issued because* of difficulties in the cases containing water. Their last published note (reference 11, p. 24) on this study is:

"A summary of the data and calculations for the 44 graphite-uranium exponential pile experiments performed from 1941 through 1944 will be issued shortly in collaboration with E. D. Cashwell as CP-3124. In the early days there were many changes in the "best" values of the fundamental constants so that results for one group of exponential experiments would not be calculated with the same constants as those for another group. Now, however, calculations for all the experiments have been made in a uniform manner with the same values of the constants and the results are all directly comparable.

The chief purpose of the exponential experiments was to serve as a guide and check in developing theoretical methods of calculating k, the reproduction factor in a lattice, from the product  $\mathbf{k} = \mathbf{f} \ \mathbf{p} \ \epsilon \eta$ . The symbol f denotes the thermal utilization, p the chance of escaping resonance capture,  $\epsilon$  the fast effect and  $\eta$  the number of neutrons produced per thermal neutron captured in uranium. The theoretical methods used were so-called diffusion theory methods described in the Project Handbook Chapter IV E.

The whole group of experiments shows that 2 different values of  $\eta$  are needed to give agreement between the measured and calculated k's for the experiments in which the uranium was in the form of oxide and for those in which it was used as metal. If instead of the calculated value of f, the value found directly from a measurement of the cadmium ratio is used in the product f p  $\epsilon$   $\eta$ , fairly good agreement between experimental and calculated k can be found for all experiments using  $\eta=1.340$ . The average deviation in the value of  $\eta$  needed for perfect agreement and 1.340 is only about 0.7 percent. That a large part of this deviation is due to experimental fluctuations is shown by the fact that in a group of experiments on seven almost identical lattices the deviation was  $\sim 0.4$  percent.

This value of  $\eta$ , 1.340, is in good agreement with the value recently determined from the homogeneous P-9 exponential experiments, namely 1.335, and from values found by substitution of measured cross sections or cross section ratios in the definition for  $\eta$ .

$$\eta = \eta(25) \sigma_a(25)/\sigma_a(25 + 28) = 1.35 \text{ using } \eta(25) = 2.10,$$

$$\sigma_a(25) = 640/140$$
, and  $\sigma_c(25 + 28) = 7.13$ 

$$\eta = \eta(25) \left[ 1 + \frac{\sigma_2(28)}{\sigma_f(25)(1 + \alpha(25))} \right]^{-1} = 1.34$$

using 
$$\eta(25) = 2.10$$
,  $\sigma_a(28)/\sigma_f(25) = 0.66$ , and  $1 + \alpha(25) = 1.17$ 

The conclusion seems to be that diffusion theory methods are good for determining p and  $\epsilon$  but are adequate for calculating the thermal utilization only to within one or two percent. Moreover, it seems that the values of the constants now in use for the calculation of p and  $\epsilon$  (see above reference in Project Handbook) must be nearly correct.

^{*} Communication from Miss Way.

Figure 1.5.21 gives calculated multiplication factors for a considerable range of metal rod lattices; Figs. 1.5.22 through 1.5.27 give pf values for spheres and rods of full-density metal, half-density metal, and oxide.

Table 1.5.28 indicates the effect of fuel composition and density upon the best value of multiplication factor obtainable with rod lattices in graphite.

Reflector savings for graphite reflectors around graphite lattices are given approximately (reference 7, p. 46) by:

$$saving = 1.2L \tanh \frac{T}{L}$$
 (14)

where T is the reflector thickness and L is the reflector thermal diffusion length.

### BERYLLIUM

A sample of U metal in Be metal lattice was tested in a hole in the Argonne graphite pile.²² Each fuel lump contained 182 cc of U (radius of equivalent sphere = 3.52 cm), and the volume ratio of Be to U was 17.2. A buckling value of  $407 \times 10^{-6}$  cm⁻² was obtained from what was considered to be the best of the experimental measurements made.

Theoretical calculations have been made²³ for Be metal and oxide lattices. The ages used there are now out of date.

#### LIGHT WATER

Six lattices of slightly enriched U metal in water have recently been measured at Brookhaven. Bucklings and water reflector savings are given in Table 1.5.29, and cadmium ratios are given in Table 1.5.30. Table 1.5.31 gives results with boron poisoning added.

Twenty-four lattices of natural U in water were operated at Oak Ridge. It was concluded²⁴ that:

- (1) "The best k obtainable at room temperature with  $H_2O$  and ordinary U in a cylindrical, no-gap geometry, is probably very near 0.99.
- (2) "A k larger than unity can probably be attained by going to sufficiently high temperatures or by use of a gap geometry."

Tables 1.5.32 and 1.5.33 summarize results.



Table 1.5.1 — Age of Fission Neutrons in Various Moderators

Substance	Age to indium resonance, cm ² (BNL-170)	Estimated age from indium to thermal, cm ²	Age to thermal, cm ²	Source of information*
H ₂ O	$30.4 \pm 0.4$		01.4	ORNL-181, 1948 (E); ORNL-641, 1950 (E)
		1	31.4	MonP-219, 1946 (T)
D ₂ O(0.16% H ₂ O)	100 ± 5			CP-2796, 1945 (T); CP- 3073, 1945 (T); CP- 3453, 1946 (E); CP- 1531, 1944 (E)
			125	CP-3195, 1945 (T); MonP-269, 1947 (T)
Be (ρ = 1.85)	80 ± 2	17.2	97.2	ANL-4076, 1947 (E and T)
BeO $(\rho = 3.0)$			105 ± 10	MUC-WC-MLG-10, 1946 (T)
$C (\rho \pm 1.60)$	311 ± 3			ORNL-187, 1949 (E)
		5 <b>3</b>	364	BNL-152, 1952 (T)

^{*(}E) = experimental; (T) = theoretical

Table 1.5.2 — Age of Fission Neutrons in Water-Metal Mixtures

Metal	Vol. metal	Experimental age to indium resonance, cm ²	Theoretical age, indium resonance to thermal, cm ²	Age to thermal, cm ²	Reference
Al	0.5	49.6	2	51 <b>.6</b>	Experiment, ORNL-294, 1949
	1.0	<b>76.</b> 8	3	79.8	Theory, MonP-219, 1946
Zr	0.25	35.7	•••	•••	Experiment ORNL-641, 1950

Table 1.5.3 — Age of Ra- $\alpha$ -Be Neutrons in Water-Metal Mixtures (Munn and Pontecorvo, Canadian Jour. Res., A, 25, 157, 1947. Reference also contains spatial distribution curves for Bi- $H_2O$  systems)

Medium,	Concentration (C),		Age,
volume ratio	gm-atoms/liter	Detector	cm ²
H ₂ O	C _H = 111	Dy	55
H ₂ O*	$C_{H} = 111$	Rh (Cd difference)	54.5
H ₂ O	$C_H = 111$	In resonance	46.3
H ₂ O*	$C_H = 111$	Rh resonance	46.2
H ₂ O:Bi::1:1	$C_{H}^{"} = 56$	Dy	93.7
	$C_{Bi} = 23$		
$H_2O: Bi::2:1$	$C_{H} = 74$	In resonance	66.3
	$C_{Bi} = 15$		
$H_2O: Bi::1:1$	C _H = 56	In resonance	<b>79.</b> 5
	$C_{Bi} = 23$		
$H_2O: Bi::1:2$	$C_{H} = 37$	In resonance	<b>86.2</b>
	$C_{Bi} = 30$		
H ₂ O:Pb::1:1	$C_H = 56$	In resonance	72.8
	$C_{Pb} = 27$		
H ₂ O:Fe::1.3:1	$C_{H} = 63$	In resonance	53.2
	$C_{Fe} = 60$		

^{*} Measured with Rn- $\alpha$ -Be source by Amaldi and Fermi, Phys. Rev. 50, 899(1936)

Table 1.5.4 — Thermal Diffusion Length and Transport Mean-free-path of Various Materials

Substance $H_2O$ $D_2O(0.16\% H_2O)$ Be $(\rho = 1.85)$ BeO $(\rho = 2.69)$ Graphite (corrected	Thermal diffusion length (L), cm (BNL-170) 2.85 ± 0.03* 116 ± 4 20.8 ± 0.5 29 ± 2	free-path (thermal), cm (BNL-170) 0.48 ± 0.01 2.65 ± 0.15 1.43 ± .05 (using $\sigma_{a(th)} = 9$ mb) 0.90 (Calculated from original reference)	Source of information  L: C-55, 1942; C-63, 1942; C-82; CP-1389, 1944; CP-2601, 1945; ORNL-933, 1951  λ; ORNL-933, 1951  L: CP-3364, 1945; CP-3195, 1945 λ _Ψ : ANL-4076, 1947  λ _Ψ : ANL-4076, 1947  L: LA-160, 1944  λ _Ψ : CP-3647, 1946
	$(\sigma_{abs} = 4.4 \text{ mb}\dagger)$		HW -21793, 1952
	$52 \pm 1$ $(\sigma_{abs} = 4.8 \text{ mb†})$		BNL-77, 1950
Th $(\rho = 11.2)$	$2.7 \pm 0.3$		CL-697 (Chicago handbook)
$ThO_2 (\rho = 6)$	$4.1 \pm 0.4$		CL-697
-	$1.55 \pm 0.05$		CT-697
U,O, (ρ = 6.0)	3.7 ± 0.4		CL-697

*CP-2161, 1944, gives dL/dT = 0.0061 cm/°C in the temperature range 27° to 93°C †2200-m/sec values; obtained using a calculated value of 4.70 b for the Maxwellian average of the total cross section

Table 1.5.5 -- Critical Mass Data for Los Alamos Water-boilers

Model name and	Core		Ta	Татрег	Critical mass of	Maximum amount	Maximum
literature reference	Material	Shape	Material	Shape	U ²³⁶ (M _c ), gm	(Mmax), gm	opserved
LOPO							
AECD-3059(1/25/51)	14.76% enriched uranium as	Sphere	Beo	Pseudosphere	575		
AECD-3063(9/4/44)	14.9 liters of UO ₂ SO ₄ aqueous solution	of 12-in. diameter		~1 ft thick			
	$\rho = 1.348 (39^{\circ}\text{C})$ 1100 gm steel including $V_{32}$ -in. stainless-steel container						
AECD-3063(9/4/44)			ပ	Cube	760	~	~
				4 ft side			
LA-241(3/12/45); same as LADC-941			H ₂ O	Right cylinder,	1200 ± 50	7117	ę.
				height = 4 ft			
HYPO				•			
AECD-3059(1/25/51)	14% enriched uranium as	Sphere*	Beo	Parallelepiped	808		
	UO ₂ (NO ₃ ) ₃ aqueous solution	of 12-in.		24 × 24 × 27 in.			
	3000 gm steel including cooling	diameter		(against core)			
	coil and 1/16-inthick stain-		ပ	<b>Para</b> llelepiped			
SUPO	less-steel sphere container			60 × 48 × 60 in.			
La-1301(2/7/52), same	88.7% enriched uranium as 12.7	Sphere	ပ	Cube	777		
as AECD-3287	liters of UO ₂ (NO ₃ ) ₂ aqueous	of 12-in.		55 in. side			
	solution	diameter					
	Stainless-steel sphere container;						

• The stainless-steel sphere was filled to within 3 or 4 cm of the top. An empty 1-in,-diameter pipe passes through the core center
† When 14.5% enrichment is used, the 1-in,-diameter hole is calculated to effect the critical mass by 30 gm
† The core contains three 20-ft-long, /₄-in,-OD, /₁₆-in,-DD stainless-steel cooling coils. In addition to the 1-in, pipe in footnote (*), a 1/₁₆-in,-ID hole runs completely

through the reactor tangent to the sphere

Table 1.5.6— Effect on Critical Mass of Replacing Small Portion of BeO Tamper in Water-boiler with Other Materials

(R. E. Carter et al, La-105, July 1944)

	Δm	, gm U ²³⁶
Material	Bare	Cd covered
BeO	0	0
С	1.52	0.67
D ₂ O	1.93	.9
Pb	2.67	.5
Bi	2.74	.85
Oak	5.0	5.8
H ₂ O	5.3	4.8
Paraffin	7.0	8.7
Air	8.0	4.8
Cu	11.9	0.5
Fe	12.7	.6
WC	15.79*	3.8†
Tu	-4.54	0.6

^{*} Density = 4.91

Table 1.5.7 — Homogeneous Reactor Critical Experiment

(Reactor dimensions and materials from TID-5022; critical fuel concentration from ORNL-1318; Sept. 19, 1952)

Core		Tai	mper	Fuel concentration,
Material	Shape	Material	Shape	gm U ²³⁵ /kg H ₂ O
>90% enriched uranium as UO ₂ SO ₄ aqueous solution	18-indiameter sphere, volume = 50 liters	D ₂ O	Sphere, 39 in. OD, 10 in. thick	25

[†] **Density** = 5.56

Table 1.5.8 — Critical Radius and Amount of  $U^{25}$  in Spherical Core for Various Infinite Reflectors*

(CP-2182, Sept. 30, 1944)

Reflector	Critical radius (R), cm	Mass U ²³⁶ (G), gm
Graphite ( $\rho = 1.6$ )	16.1	600
D ₂ O	16.3	622
H ₂ O	20.7	1273
BeO		
$(\rho = 3)$	14.7	456
$(\rho = 2)$	16.3	622
Ве	15.5	535
None	27.3	2920

^{*}Enrichment = 12.5%; concentration = 2.8 × 10⁻³ U²³⁶ atoms/molecule H₂O

Table 1.5.9 — Critical Radius and Amount of U²³⁵ in Spherical Core with Infinite D₂O Reflector for Various Concentrations of 12.5% Enriched Fuel

(CP-2185, October 1944)

$Z = U^{235}$ atoms/ H ₂ O molecule (× 10 ³ )	Critical radius (R), cm	Mass U ²³⁵ (G), gm
2	18.3	668
2.4	16.1	5 <b>44</b>
2.8	14.8	794
3.2	13.8	456
3.6	13.1	438
4.0	12.6	432
5.0	11.6	421
6.0	11.2	453
10	9.5	455

Table 1.5.10 — Criticality Studies on Enriched U-D₂O Systems*
(Snell, MonP-454, and Addendum)

U ²³⁵ .	Core	Core	Core volume,	Reflecto	r thick	ness, cm	Critical mass,
gm/liter	height, cm	radius, cm	liters	Bottom	Тор	Lateral	gm U ²³⁵
10.35	61.8	20.8	84	20	62	50.2	869
5.17	61.8	30.4	180	20	62	40.6	930
2.58	100	40.4	512	20	24	30.6	1323

*Fuel in Al tubes of 1.5-in. diameter spaced 8.4, 11.9, or 16.9 cm. "No-hole" extrapolation of data from more complex arrangements. A few tenths percent H in the D

Table 1.5.11 — Exponential Experiments with  $D_2O$  and  $UO_2F_2$  Solutions*
(Wattenberg, CP-3364)

UO ₂ F ₂ concentration, gm/cm ³	Critical radius $(R_c)$ , cm	Volume of D ₂ O, liters	Mass of uranium, kg
0.0238	452	358,000	6,602
.7034	247	62,700	3,583
.1484	208	37,300	4,348
.2004	205	35,400	5,598
.2493	209	37,100	7,343
.2986	228	47,900	11,438
.3476	244	52,200	14,586

^{*} For bare spherical reactors; about 0.2% H in D

Table 1.5.12 — Spherical D₂O-U Cores with Infinite D₂O Reflector

	þ							
ss U ²³⁵ , gm	Pure U ²³⁵ 12.5 U ²³⁶ :87.5 U	411	342	329	330	350	393	527
Ma	Pure U ²³⁵	362	292	284	273	242	288	340
ıme, liters	Pure U236 12.5 U236 : 87.5 U	315	131	101	<b>84</b>	54	30	20
Volu	Pure U ²³⁶	277	112	87	70	37	22	13
ilus, cm	12.5 U ²³⁶ : 87.5 U	42.2	31.5	28.9	27.2	23.4	19,3	16.9
Rac	Pure U ²³⁶	40.4	29.9	27.5	25.5	20.7	17.4	14.6
	$Z = U^{235}$ atoms/D ₂ O molecule (× 10 ³ ) Pure U ²³⁵ 12.5 U ²³⁵ : 87.5 U	0.1	τ.	.25	e.	č.	1.0	2.0

Table 1.5.13—Critical Radius for Bare Spherical D₂O Systems (CP-2222)

	E C	Critical radius, cm	сm
$Z = U^{235}$ atoms/D ₂ O molecule (× 10 ³ )	*0 <b>=</b> 0*	α = 7*	$\alpha = 14^*$
0.15	:	65	:
.20	56.7	59.7	62.6
.23	54.4	57.8	60.5
.25	53.1	56.2	59.3
.27	51.8	55.3	58.3
.30	50.3	54.0	57.1

*  $\alpha$  = atoms U²³⁶/atoms U²³⁵

Table 1.5.14—Spherical D₂O Systems with Graphite Reflectors

(CP-2813X)

	Core radius, cm	lius, cm	Volume	Volume, liters	Mass of U236, gm	U ²³⁶ , gm
Reflector thickness, cm	$Z^* = 0.15 \times 10^{-3}$ $Z^* = 0.25 \times 10^{-3}$	$Z^* = 0.25 \times 10^{-3}$	$Z^* = 0.15 \times 10^{-3}$	$Z^* = 0.15 \times 10^{-3}$ $Z^* = 0.25 \times 10^{-3}$	$Z^* = 0.15 \times 10^{-3}$	$Z^* = 0.15 \times 10^{-3}$ $Z^* = 0.25 \times 10^{-3}$
8	40.4	32.8	276	147	540	479
50	42.9	34.8	331	176	647	574
30	46.7	37.9	426	228	833	743
20	50.4	41.2	536	294	1048	928
0	65.3	26.0	1167	736	2283	2398
* $Z = U^{136}$ atoms/ $D_2O$ molecule	olecule					

Ä
lecto
) Ref
O,
ıfinite
with Ir
ores
)-Pu (
o O
Spherical D ₂ O-Pu Cores with Infinite D ₂ O Reflect
2
1.5.1
Table 1

(CP-2203X)

			$10^3$ Z = Pu	toms/D20	molecule		
	0.1		0.25	0.3	0.5		2.0
/olume D ₂ O, liters Mass of Pu, gm	180 290	80 210	62 51 32 205 205 210	51 205	32 210	18 240	11 290

Table 1.5.16 — Laplacians for D₂O Systems (U²³⁵ Data from XP-2813X; Pu (Data from CP-2589X)

$Z = Fuel atoms/D_2O molecule (× 103)$	$U^{235} \ (\times \ 10^3)$	Pu (× 10 ³ )
0.08	1.43	1.91
.09	1.58	2.07
.10	1.72	2.23
.125	2.03	2.57
.150	2.31	2.86
.175	2.55	3.095
.20	2.77	3.32
.23	3.01	3.53
.25	3.15	3.65

Table 1.5.17 — D₂O Reflector Savings*
(Garabedian, CNL-36)

	Reflector saving, cm		
Reflector thickness, cm	Case I, 10.35 gm U ²³⁵ /liter	Case II, 5.17 gm U ²³⁵ /liter	
0	0	0	
20	15.3	15.9	
30	18.8	19.5	
40	20.6	21.6	
50	21.6		
62	22.5	23.8	
<b>60</b>	24.2	26.1	

*For 2-group theory; slightly larger savings obtained by other methods. The bare-core critical radius was  $43.6~\rm cm$  in Case I and  $50~\rm cm$  in Case II

Table 1.5.18 - Natural U with Pure D2O

(Ott, MonP-374; bare unpoisoned spherical reactors at room temperature, no H impurity in the D. This report contains a criticality nomograph for D₂O-moderated machines)

D ₂ O molecules/U ²³⁸ atom	D ₂ O volume, m ³
40	34.3
60	20.4
80+	19.0
100	20.4
120	22,5

*This case calls for  $0.164~\rm gm~U/cc$ , a total of  $3120~\rm kg~U$  or  $22~\rm kg~U^{235}$ . Addition of  $1.1~\rm kg$  Pu reduces the volume to  $13.2~\rm m^3$ , and the mass of U to  $2140~\rm kg$ . Core size reductions possible by means of a reflector were not computed

### Table 1.5.19 - Notation

- $k = Multiplication factor = \eta \in p f$
- $\eta$  = Number of neutrons produced by thermal fission for each thermal neutron absorbed in U
- $\epsilon$  = Multiplicative effect of fast fission = Total number of neutrons produced per neutron produced by thermal fission
- p = Fraction of neutrons which become thermal
- f = Thermal utilization of fuel = Thermal neutrons absorbed in U per thermal neutron captured in all materials of the lattice
- $M^2 = Migration area = \tau + L^2$
- $\tau$  = Age in lattice
- $L^2$  = Thermal diffusion length in lattice
- $B = Buckling = k-1/M^2$  for k near unity

Table 1.5.20 - Data for Fast Effect in Natural Uranium

Quantity	CL-697
$\sigma_{\rm f}$ , b	0.29
σel, b	1.5
$\sigma_{\mathbf{c}}$ , $\mathbf{b}$	<0.04
σt, b	4.3
ν	<2.55
$\frac{\kappa_0}{N_{0t}}$ , b	3.5

**Table 1.5.21** — Values of Fast Effect,  $\epsilon$  (BNL-152)

Shape*	Radius, cm	Experimental (Hill, CP-1548)	Calculated using CL-697 constants
Cylinder	1.71	1.032 ± 0.003	1.036
Sphere	3.22	$1.042 \pm 0.004$	1.041
Sphore	3.96	$1.048 \pm 0.004$	1.048

Table 1.5.22 — Fast Effect for U Metal Rods

(BNL-152)

Radius, cm	€-1
1	0.0224
1.1	.0243
1.2	.0261
1.3	.0280
1.4	.0299
1.5	.0316
1.6	.0333
1.7	.0350

**Table 1.5.23** — Formulae for F and E = X + 1 (Science and Engineering of Nuclear Power, Vol. II)

	F(x)	E(x,y)
Plane	x coth x	(y-x) coth $(y-x)$
Cylinder*	$\frac{x}{2} \frac{I_0(x)}{I_1(x)}$	$\frac{y^2-x^2}{2x}\frac{I_1(y)K_0(x)+I_0(x)K_1(y)}{I_1(y)K_1(x)-I_1(x)K_1(y)}$
Sphere	$\frac{x^2}{3} \frac{\tanh x}{x - \tanh x}$	$\frac{y^3 - x^3}{3x} \frac{1 - y \coth (y - x)}{1 - xy - (y - x) \coth (y - x)}$

 $[*]K_1$  is here defined so as to be always positive

Table 1.5.24 — Resonance Integrals for the Heavy Elements

Material	$\int \sigma_a dE/E$ , barns	Remarks
Th ²³²	81.3	Measured value from CP-3093 (1945)
Ū	<240	Sources: CP-3580 (1946), CN-442 (1943), CP-372 (1942), CP-3202 (1945)
Hf	7700	Calculated from data in ORNL-641 (1950) on Zr containing Hf

Table 1.5.25 — Resonance Integrals in Uranium

Observer	Method	Date	$A = \int \alpha(E) dE/E$ , barns	$\mu = \int \beta(E) dE/E,$ barns gm/cm ²	Reference
Creutz	Activation	1944	9.25	24.7	C-116

Table 1.5.26 — Resonance Constants in Project Calculations

Material	A, barns	$\mu/A$ , gm/cm ²	Reference
U	9.25	8/3	CP-372
$U_3O_8$	12	<b>%</b>	CP-372
UO ₂	11.51	1.92	CP-445
UF ₆	14.6	1.12	CN-442

Table 1.5.27 — Moderator Resonance Constants

(CL-697, IV E)

$\overline{\xi\sigma_s}$ , b/atom or molecule	$\bar{\kappa}_2/\rho$ ,* cm ² /gm					
38.5	0.583					
5.28	.141					
1.26	.128					
1.76	.0690					
0.76	.0672					
	38.5 5.28 1.26 1.76					

* Values given are for use with U; if the fuel is oxide or hex, multiply the values of  $\overline{\kappa}_2/\rho$  by 0.88

Table 1.5.28 - Effect of Fuel on Multiplication Factor

(Roughly assembled and rounded-off values based on Nucleonics, Jan. 1951; CP-372; CN-442; CP-445; CN-362)

Form	Density, gm/cc	$\mathbf{k}_{\text{max}}$
U	18	1.08
U	9	1.07
U	6	1.06
UO ₂	6	1.05
U ₃ O ₈	6	1.04
UF,	6	1.03
UF6	3.7	1.01
UO ₂	1	1.02

Table 1.5.29 — Water Lattices with Slightly Enriched U*

(Communication from J. Chernick, Sept. 18, 1952)

	Buc	kling,‡ cm ⁻² ×	10 ³	Reflector saving, cm							
Latticet	1st run	2d run	Average	1st run	2d run	Average					
1.5:1 1.75:1 2:1 2.5:1 3:1 4:1	3.65 ± .09 3.700 ± .055 3.304 ± .028	3.486 ± .053 3.86 ± .07 3.647 ± .025 3.271 ± .066	2.89 ± 0.05 3.470 ± .033 3.75 ± .08 3.673 ± .048 3.288 ± .018 1.86 ± .06 ⁴	7.16 ± .08 7.23 ± .26 6.81 ± .17 6.82 ± .11	7.15 ± .12 6.75 ± .20 6.99 ± .09 7.05 ± .09	7.16 ± .10 6.94 ± .23 6.90 ± .16 6.94 ± .11					

^{*}Metal rods 0.750 in. diameter and 4 ft long, 1.027 wt-% U²³⁵, 30-mil Al cladding on rods, triangular lattice array. Values reported are results of least-squares fits

§Infinite lateral water reflector

¶ Averages for this lattice are weighted because one measurement is much poorer than the other

[†]Lattice designation is volume ratio of water + Al to U

[‡] Chernick's cover letter says in part "The migration areas to be attributed to these lattices are still tentative. We get values ranging from 30-36 cm² depending on the form of the theory used to compute the thermal utilization. We hope to get better values from the analysis of intercell traverses which have just been completed. Members of the group under Karl Cohen report a value of 30 cm² if the assumption of constant reflector savings is used, 34 cm² if the variation with poison is accounted for"

Table 1.5.30 — Cadmium Ratios in Slightly Enriched Water Lattices (Communication from J. Chernick, Sept. 18, 1952)

Lattice	Gold: cadmium ratios	Indium: cadmium ratios					
1.5:1	$1.918 \pm 0.052$	2.576 ± 0.014					
2:1	$2.292 \pm .038$	$3.044 \pm .16$					
3:1	$2.884 \pm .025$	$4.30 \pm .033$					
4:1	$3.307 \pm .045$	$5.742 \pm .092$					

Table 1.5.31 — Slightly Enriched Lattices with B Poisoning

(Communication from J. Chernick, Sept. 18, 1952)

	Boron concentration,		
Lattice	B atoms/10 ³ H ₂ O molecules	Buckling × 10 ³ , cm ⁻²	Reflector saving, cm
1.5:1	0.216	$2.164 \pm 0.082$	$7.61 \pm 0.18$
1.5:1	.563	$1.107 \pm .217$	7.61 ± .46
1.5:1	.860	$0.243 \pm .05$	7.75 ± .46
2:1	.359	2.045 ± .255	7.45 ± .67
2:1	.590	$1.272 \pm .314$	7.11 ± .78
2:1	.824	$0.326 \pm .094$	$7.32 \pm .22$
3:1	.174	$2.086 \pm .052$	$6.79 \pm .20$
3:1	.345	$1.137 \pm .057$	$6.37 \pm .19$
3:1	.512	$0.019 \pm .049$	$6.59 \pm .17$
4:1	.074	$1.103 \pm .050$	7.16 ± .24
4:1	.146	$0.596 \pm .067$	$6.60 \pm .30$
4:1	.218	$054 \pm .070$	6.81 ± .32

**Table 1.5.32**—Description of Natural-U Lattices in Water (CP-2842)

Lattice	Description	Cell type	$v_{H_{I\!\!I}O}/v_{U}$	$v_{A1}/v_{U}$	r ₀ , cm	
1	Vert. rods, no gap	Sq.	1.14	0	1.50	
2	Vert. rods, no gap	Sq.	3.27	0	1.50	
3	Horiz, stacked slugs	Sq.	0.27	0	1.40	
4	Vert. rods, no gap	Hex.	1.78	0	1.50	
5	Vert. rods, no gap	Hex.	3.17	0	1.50	
6	Slugs in vert. tubes	Hex.	2.06	0.140	1.40	
7	Vert. rods, no gap	Hex.	1.36	0	1.50	
9	Slugs, cork spacer gap	Hex.	1.60	0.140	1.40	
10	Slugs, cork spacer gap	Hex.	1.70	.140	1.40	
11	Slugs in tubes, no gap	Hex.	1.42	.140	1.40	
12	Slugs in tubes, no gap	Hex.	1.57	.140	1.40	
13	Slugs in tubes, air gap	Hex.	1.92	.346	1.40	
14	Slugs in tubes, air gap	Hex.	1.56	.346	1.40	
16	Small rods, no gap	Hex.	1.80	0	1.00	
17	Small rods, air gap	Hex.	2.01	0.247	1.00	
18	Small rods, no gap	Hex.	1.50	0	1.00	
19	Small rods, no gap	Hex.	2.10	0	1.00	

Table 1.5.33 — Natural-U Lattices in Water (CP-2842)

			¹⁶ , cm ⁻² rected	L²,	, cm²	τ,	cm²	k corrected		
Lattice	δΔ/δΤ	25 <b>℃</b>	100°C	25°C	100°C	25°C	100°C	25°C	100°C	
1	1.65	478	602	2.5	2.8	54.7	57.8	0.973	0.964	
2	-14.6	4018	2321	3.4	3.7	39.9	42.6	.840	.898	
3	23.0	<b>65</b> 68	8293	2.2	2.4	131.0	133.0	.417	.325	
4	-1.41	370	264	2.8	3.1	44.0	50.2	.983	.986	
5	-8.10	3452	2844	3.4	3.7	40.1	43.0	.860	.875	
6	-3.05	637	429	2.9	3.2	44.9	47.9	.970	.978	
7	0.0	126	129	2.6	2.9	51.7	54.7	.993	<b>.9</b> 93	
9	-2.75	84	-13	2.7	3.0	48.8	51.9	. <b>9</b> 96	1.007	
10	-5.32	265	-13	2.8	2.1	47.8	51.1	.987	1.007	
11	0.34	188	218	2.6	2.9	51.0	54.0	.990	0.988	
12	46	297	268	2.7	3.0	49.2	52.2	<b>.9</b> 85	<b>.9</b> 85	
13	.89	20	120	6.0	6.6	94.5	103.0	.998	.987	
14		-27		6.1	6.7	112.0	121.0	1.003		
16		278		2.8	3.1	48.4	51.7	0.986		
17	-0.18	0	-8	6.8	7.5	110.0	120.0	1.000	1.001	
18	2.50	660	848	2.7	3.0	51.5	54.7	0.965	0.952	
19		329		2.9	3.2	46.5	49.3	.984		

Table 1.5.34—Resonance Absorption Integrals (S. P. Harris, C. O. Muehlhause, and G. E. Thomas, Phys. Rev., 79, 1950)

Chemical form used in experiment	NaF	4	<b>凸</b>	Sc ₂ O ₃	V ₂ O ₅	Mn	రి	Cu	Cn	Ga ₂ O ₃	<b>Ga</b> 30;	As	PbBr ₂	Y203	odax	Rh	νg	yg .	s
10 ⁻²⁴ Nuclei per cm² (isotopic)	$7.4 \times 10^{-6}$	$2.9 \times 10^{-4}$	$3.1 \times 10^{-4}$	$2.6 \times 10^{-5}$	$2.1 \times 10^{-6}$	$6.5 \times 10^{-6}$	$6.1 \times 10^{-6}$	$1.4 \times 10^{-4}$	$6.0 \times 10^{-6}$	$3.1 \times 10^{-6}$	$2.0 \times 10^{-6}$	$6.0 \times 10^{-6}$	$1.0 \times 10^{-5}$	$4.1 \times 10^{-5}$	$2.5 \times 10^{-6}$	$2.6 \times 10^{-6}$	$1.5 \times 10^{-6}$	Zero extrapolation	<b>6.8</b> × 10 ⁻¹
Source of $\sigma_{ m th}$	eco	•0•	<b>-</b>	•••	•	•	•••		•	-	_	•	-	_	•	-	-	_	-
Σa,‡ barns	0~	$\sim 0.05$	~0.01	0~	0~	~2	27.5		1.90	7.45	11.9	29.9	129	0.22	3.67	529	80.6	1174	891
$\Sigma_{1/\mathbf{v}, \dagger}$ barns	~0.21	60°∼	60°∼	~12.6	~2.0	~4.8	13.7		1.45	0.56	1.3	1.6	4	0.50	.52	90	17.7	38	22
$\Sigma_{a^1,*}$ barns	~0.21	~.14	~.10	~12.6	$\sim$ 2.0	~9.8	41.2		3.35	8.01	13.2	31.5	133	0.72	4.19	589	98.3	1213	913
Thermal-activation cross section $(\sigma_{th})$ , barns	0.52	.22	.23	31.6	4.93	12.1	34.3		3.62	1.40	3.36	3.87	10.9	1.24	1.31	149	44.3	97.0	56.0
ς. Σ _a 1/σth	~0.4	~,65	4.~	4.∼	4.~	~.81	1.20	0.92	.93	5.72	3.94	8.15	12.2	0.58	3.19	3.95	2.22	12.5	16.3
Observed cadmium ratio	70.3	43.1	63.8	0.69	70.6	35	23.8	30.8	30.5	5.79	7.96	4.36	3.25	47.9	9.59	7.94	13.35	3.20	2.68
Isotope	.Na 23	A127	P31	3, Sc.	, V ⁵¹	Mn 55	ပို	S TO	Son O	Sag.	Ga ¹¹	4.AS76	EBr 79	W.Y.	SON	Rh 103	,,Ag 107	Ag 100	ell al

<b>u</b>	Sp	Sp	PbI ₂	$PrO_2$	$Sm_2O_3$	Eu ₂ O ₃	HO,	HIO ₂	Ta	8	Re	Re	占	'n	ηη	Ţ	I
$1.5 \times 10^{-6}$	$1.7 \times 10^{-6}$	$1.3 \times 10^{-6}$	$1.3 \times 10^{-5}$	$1.8 \times 10^{-6}$	$4.1 \times 10^{-6}$	$8.3 \times 10^{-6}$	$8.0 \times 10^{-6}$	$2.3 \times 10^{-6}$	$2.7 \times 10^{-5}$	$3.1 \times 10^{-7}$	$6.6 \times 10^{-6}$	1.1 × 10-6	$6.9 \times 10^{-6}$	$1.1 \times 10^{-5}$	$5.0 \times 10^{-7}$	$3.0 \times 10^{-5}$	$7.3 \times 10^{-5}$
_	-	_	-	-	-	_	-	•••	-	_	-	_	_	-	Wattenberg	•00	<b>401</b>
2294	144	~124	116	5.3	1504	290	15.7	~1360	507	306	1021	245	2870	1162	1296	122	~0.69
78	က	-	က	4.0	22	552	4.0	40	10	14	40	30	400	51	37	<u>ئ</u>	~0.07
					1559												
																	~0.17
12.1	21.6	~50	19.0	0.92	11.3	0.61	1.97	~14	25.1	9.35	10.5	3.65	3.27	9.48	14.35	10.6	4.48
3.26	2.27	~1.55	2.45	30.9	3,43	45.7	14.9	~3.0	25.1	3.93	3.61	8.50	9.37	3.89	2.91	3.59	7.12
\$11uI.	Sp121	Sp123	121 127	Pr 141	Sm152	Eu151	.,Hf180	1811H1	Ta181	,W186	.Re 185	, Re 187	1.1r 191	77Ir 193	191 UA.	T1203	81 T1 ²⁰⁵

*The sum of  $\Sigma_a$  and  $\Sigma_{1/v}$ ; accurate to about 5 percent

†The cross section for absorption which takes place at energies above the Cd cut-off (~0.6 ev) in a non-resonance region is defined

as  $\Sigma_{1/\nu} = \int_{non-resonance} \sigma_a dE/E$ ; accurate to 10-20 percent  $\ddagger$  The resonance absorption integral,  $\int \sigma_a dE/E$ ; the integration extends over an energy region in the neighborhood of the resonance energy; accurate to 10-20 percent

Unpublished work of Harnes, Muehlhause, Rasmussen, Schroeder, and Thomas

¶Seren, Friendlander, and Turkel, Phys. Rev., 72, 1947

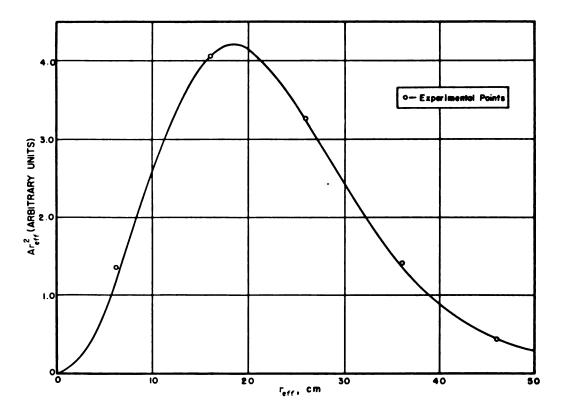


Fig. 1.5.1 — Slowing-down Distribution in  $D_2O$ . Reprinted from CP-3453, 1946. The ordinate is  $r^2$  times the number of fission neutrons slowed to 1.4 ev (indium resonance energy). The (theoretical) curve is given by:

$$\mathbf{A}(\mathbf{r}) = \frac{\mathbf{A}\mathbf{e}^{\tau_1/\tau_2}}{8\pi\mathbf{r}\tau_2} \left\{ \left[ 1 + \phi \left( \frac{\mathbf{r}}{2\sqrt{\tau_1}} - \sqrt{\frac{\tau_1}{\tau_2}} \right) \right] \mathbf{e}^{-\mathbf{r}/\sqrt{\tau_2}} - \left[ 1 - \phi \left( \frac{\mathbf{r}}{2\sqrt{\tau_1}} + \sqrt{\tau_1/\tau_2} \right) \right] \mathbf{e}^{-\mathbf{r}/\sqrt{\tau_2}} \right\} \right\}$$

and is plotted for  $\tau_1 = 58 \text{ cm}^2 \text{ and } \tau_2 = 48 \text{ cm}^2$ .  $\phi(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-y^2} dy$ .

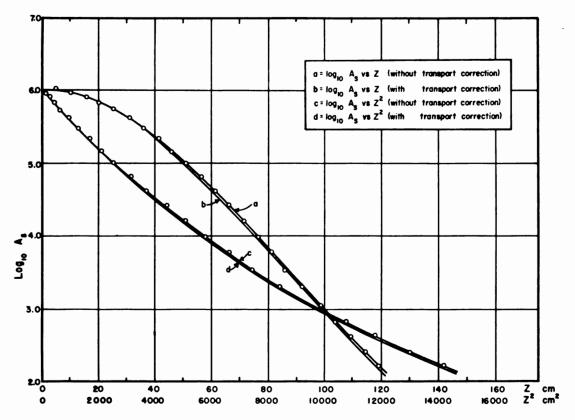


Fig. 1.5.2 — Slowing-down Distribution of Fission Neutrons from a Plane Source in Graphite. Reprinted from ORNL-187, 1949. The ordinate is the logarithm of the number of fission neutrons slowed down to 1.4 ev (indium resonance energy). If the distribution were Gaussian, curves c and d would be straight lines.

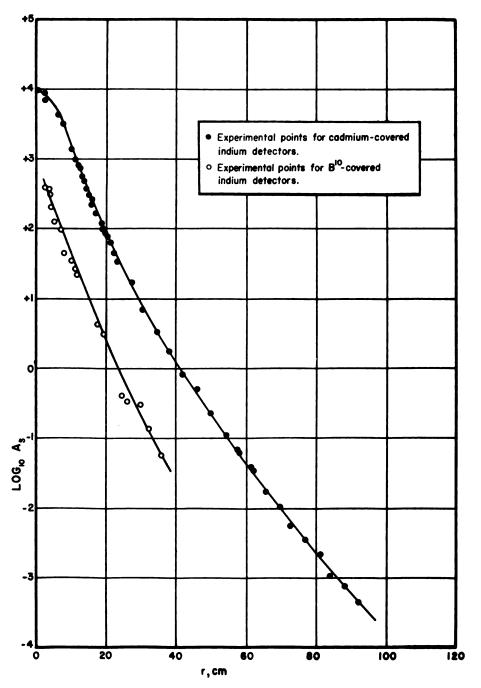


Fig. 1.5.3 — Slowing-down Distribution of Fission Neutrons in Water; Indium Resonance Activity for Point Source. Reprinted from ORNL-181, 1948.

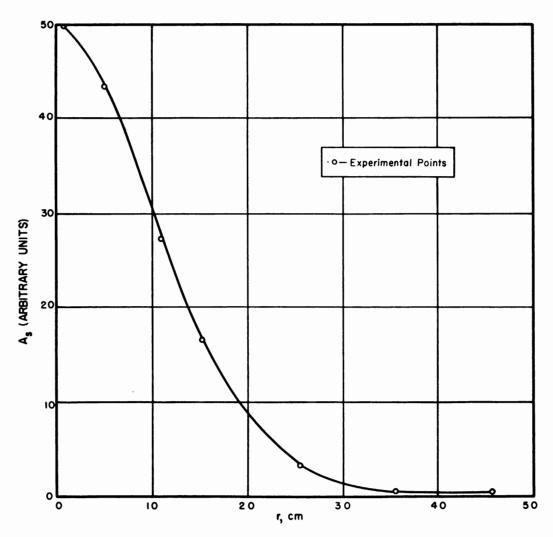


Fig. 1.5.4 — Slowing-down Distribution in Be( $\xi$  = 1.85 gm/cc). Reprinted from ANL-4076, 1947. Indium resonance activity, point fission source.

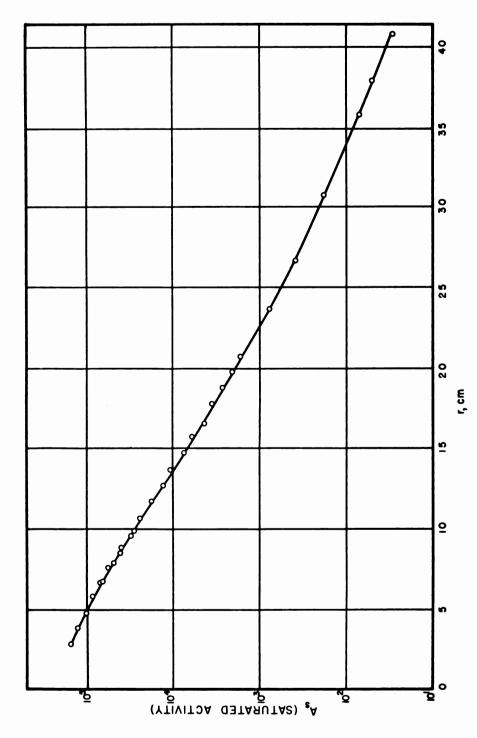


Fig. 1.5.5 — Slowing-down Distribution in Water-Zr Mixture. Reprinted from ORNL-641, 1950. Indium resonance activity, point fission source, 20% Zr by volume, 80% water. Reference also gives distributions from Ra- $\alpha$ -Be source in water and in water-Zr.

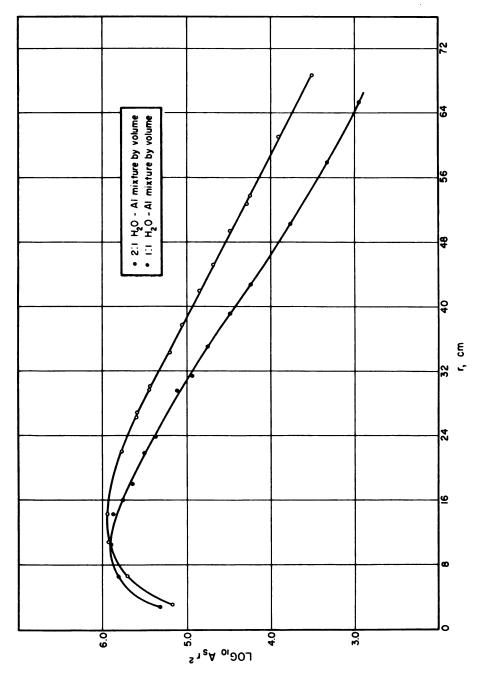


Fig. 1.5.6 — Slowing-down Distribution in Al-H₂O Mixtures. Reprinted from ORNL-294, 1949. Indium resonance activity; point fission source.

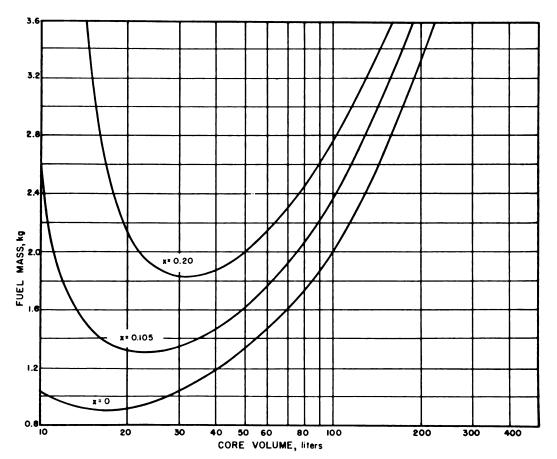


Fig. 1.5.7 — Critical Mass of Water-moderated and Tamped Spheres vs Core Volume for Highly Enriched Fuel. Reprinted from Circle Report II, Jan. 7, 1949. The quantity  $\mathbf{x}$  is the ratio of the macroscopic poison absorption cross section to the  $\mathbf{U}^{235}$  absorption cross sections.

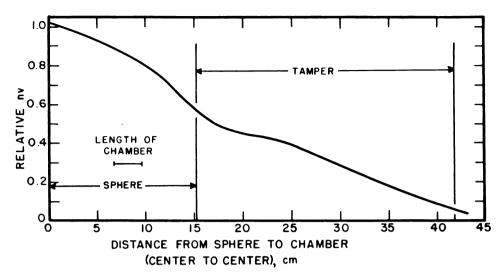


Fig. 1.5.8 — Flux Distribution in Low-powered Water Boiler as Measured with a  $U^{235}$  Chamber. Reprinted from AECD-3054, Oct. 19, 1944.

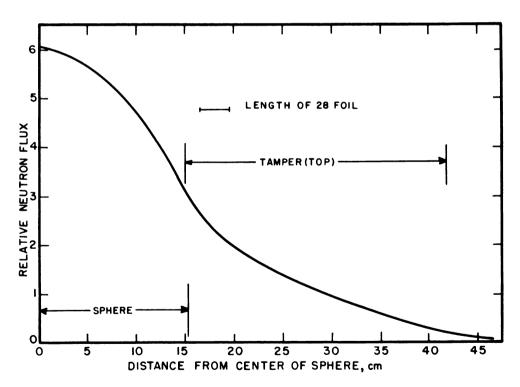


Fig. 1.5.9 — Flux Distribution in Low-powered Water Boiler as Measured with a  $U^{238}$  Chamber. Reprinted from AECD-3054, Oct. 19, 1944.

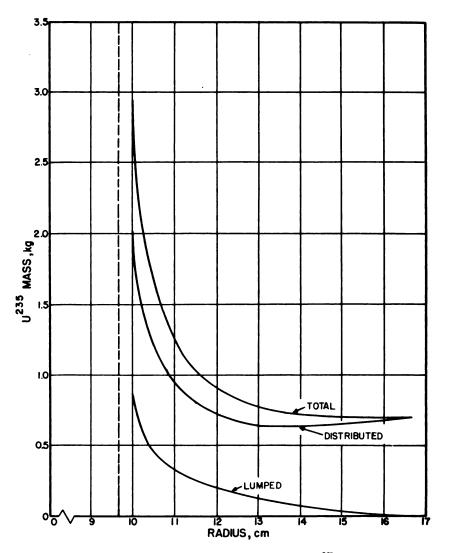


Fig. 1.5.10—Minimum Critical Mass of a Spherical, U²³⁵-H₂O Core with an Infinite Water Tamper vs Core Radius. Reprinted from Jour. Reactor Sci. Tech., April 1952. The middle curve shows the amount of fuel distributed continuously and the bottom one the amount lumped at the core-reflector interface.

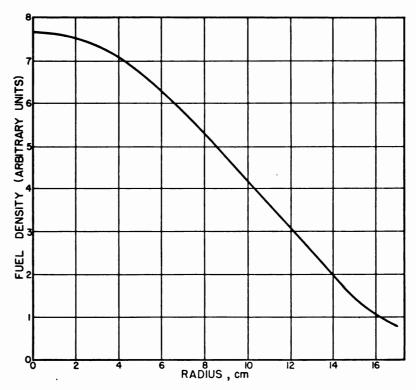


Fig. 1.5.11 — Fuel Distribution which Produces the Least Mass in a Spherical, pure  $U^{235}$ -H₂O Core with an Infinite Water Tamper. Reprinted from Jour. Reactor Sci. Tech., April 1952. The least mass occurs for a radius of 16.7 cm.

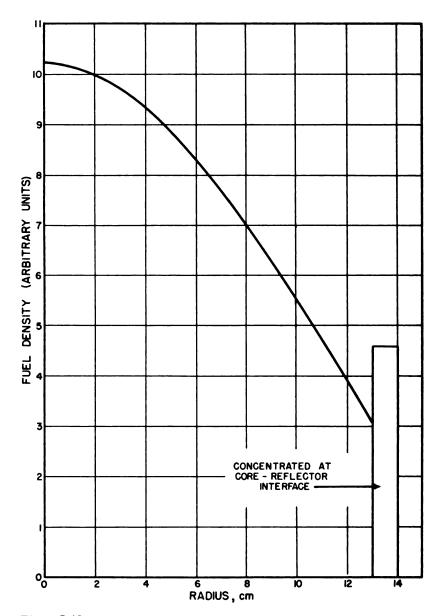


Fig. 1.5.12—Fuel Distribution which Produces the Minimum Mass in a Spherical, Pure U²³⁵-H₂O Core with an Infinite Water Tamper for a Core Radius of 13 cm. Reprinted from Jour. Reactor Sci. Tech., April 1952. This illustrates a case of smaller radius than that yielding the least mass.

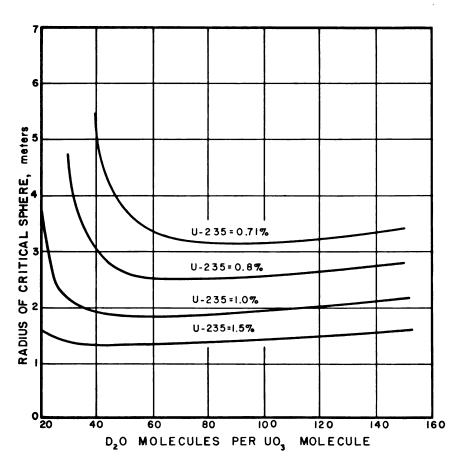


Fig. 1.5.13—Homogeneous D₂O Reactors with Natural or Slightly Enriched Uranium Fuel. Reprinted from ORNL-1096.

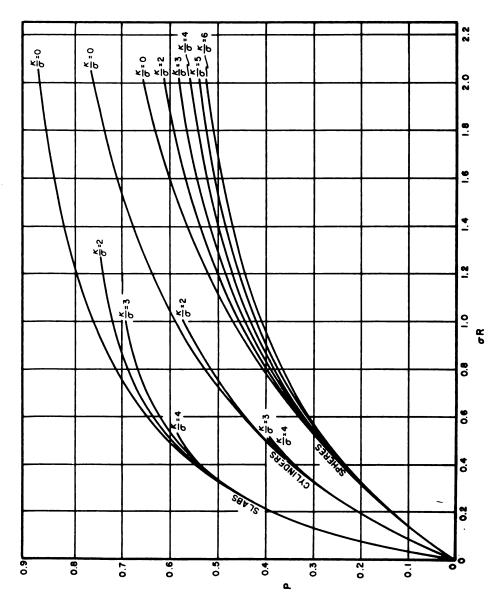


Fig. 1.5.14 — Probability of First Flight Collision within a Lump. Reprinted from CP-644. On the graph,  $\sigma$  is the macroscopic total cross section,  $N\sigma_{\rm r}$  For spheres and cylinders, R is the radius; for slabs it is the half thickness.

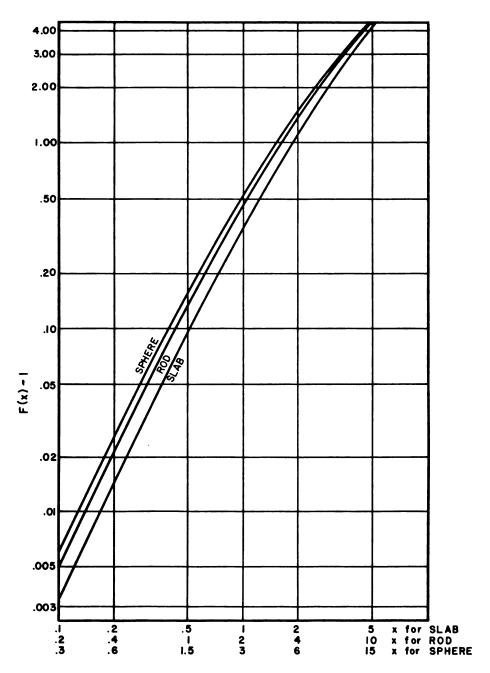


Fig. 1.5.15 — Values of F for Lattice Calculations. Reprinted from CL-697.



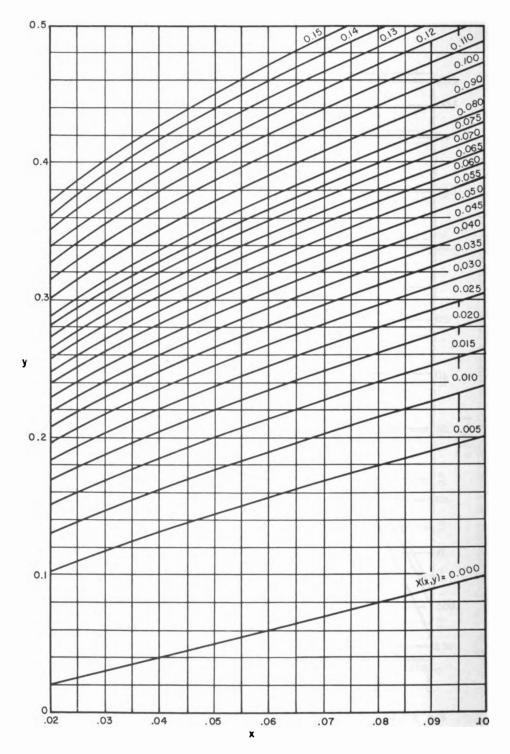


Fig. 1.5.16 — Contours of X(x,y) for Thermal Lattice Calculations. Reprinted from TPI-20(u).

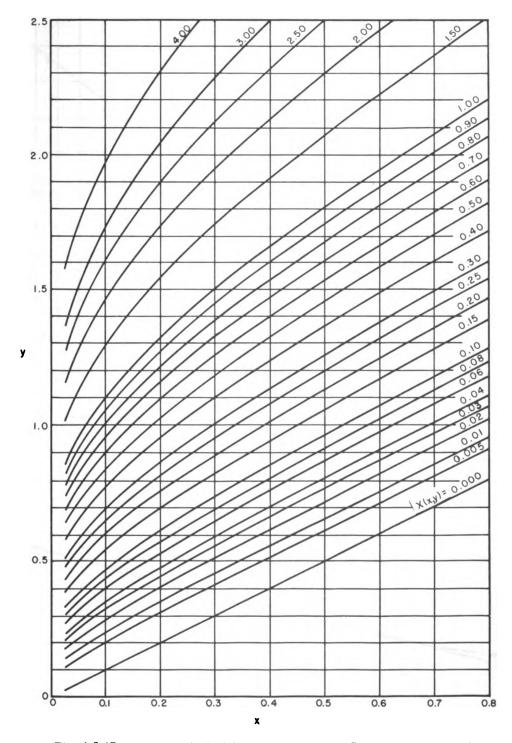


Fig. 1.5.17 — Contours of X(x,y) for Resonance Lattice Calculations. Reprinted from TPI-20 (u).

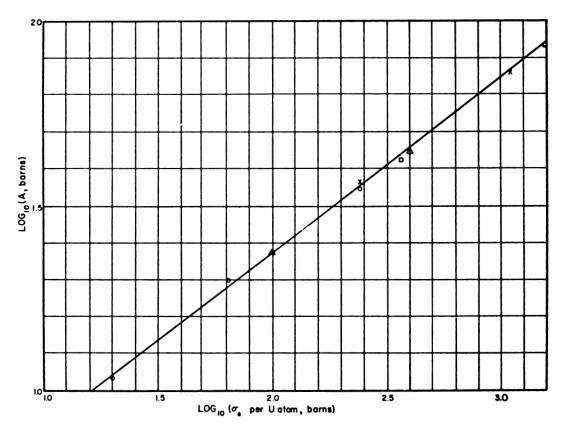


Fig. 1.5.18 — Effective Resonance Integral for U. Reprinted from Weinberg and Noderer, ORNL-51-5-98.

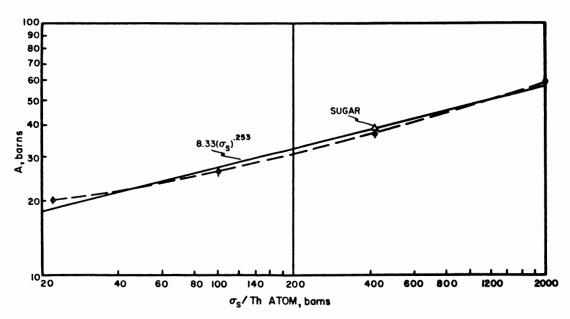


Fig. 1.5.19 — Effective Resonance Integral for Th. Reprinted from Hughes and Eggler, CP-3093.

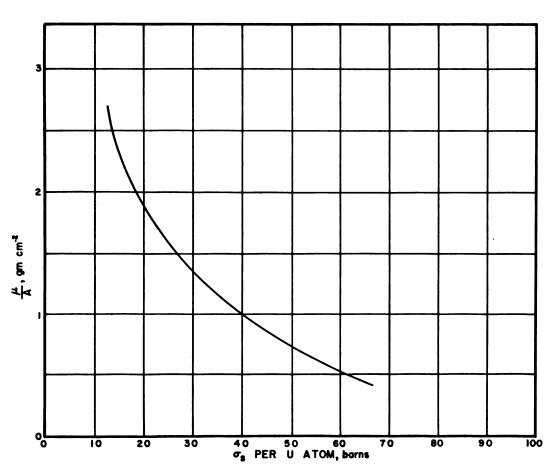
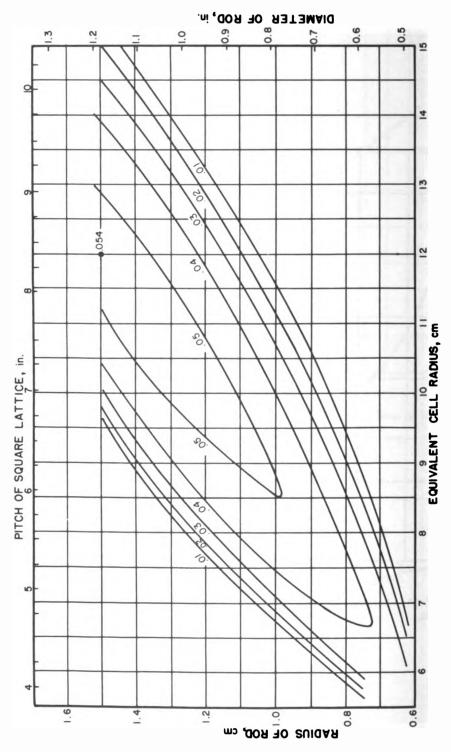


Fig. 1.5.20 — Surface Resonance Absorption in U. Reprinted from Chicago Handbook.



Guggenheim and Pryce, TPI-20(u), Aug. 1945. Graphite density 1.6 gm/cc; U metal 18.9 gm/cc; Fig. 1.5.21 -- Calculated Values of k-1 for Uranium Metal Rods in Graphite. Reprinted from early project purity of materials; 1.15-mm Al sheath on rods; no air gap. The radius of the circle which has the same area as the cell is the equivalent radius. Reference report gives similar graphs for various air-gap thicknesses and other related material.

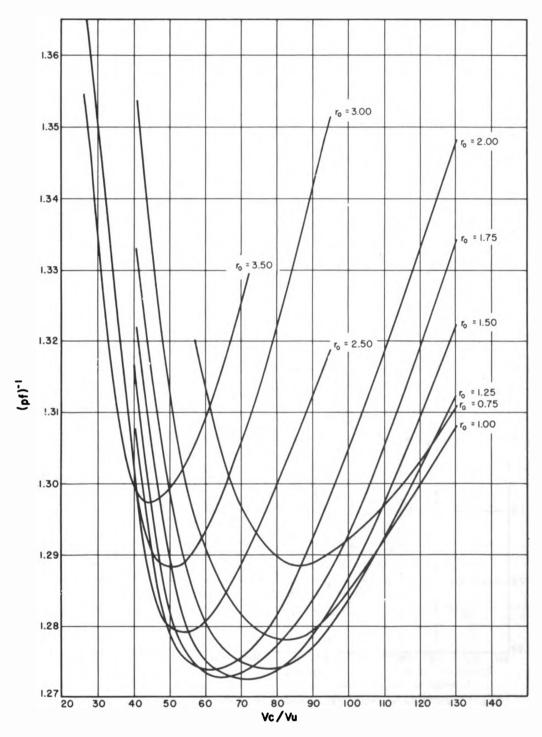


Fig. 1.5.22 — The Function pf for Uranium Metal Spheres of Density 18. Reprinted from Plass and Wigner, CP-372, Dec. 1942. Inverse of pf plotted against graphite-to-uranium volume ratio; r₀ is radius of sphere in cm. Graphite of density 1.6 gm/cc; early project purity.



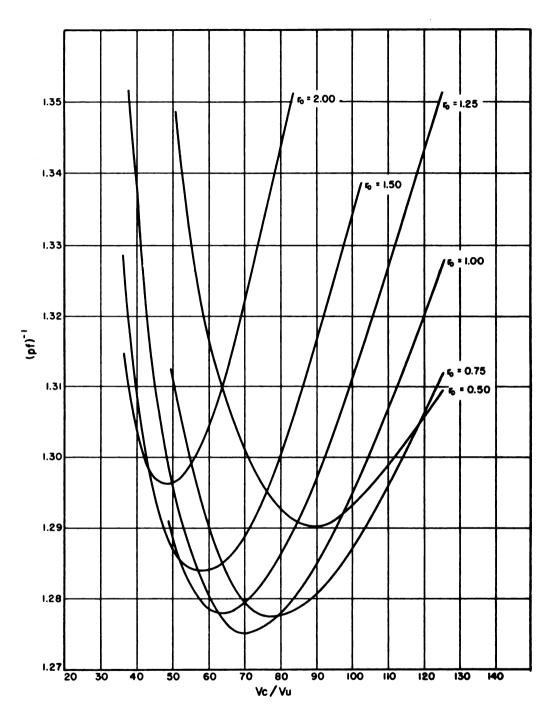


Fig. 1.5.23 — The Function pf for Uranium Metal Cylinders of Density 18. Reprinted from Plass and Wigner, CP-372, Dec. 1942. Inverse of pf plotted against graphite-to-uranium volume ratio;  $r_0$  is radius of rod in cm. Graphite of density 1.6 gm/cc; early project purity.

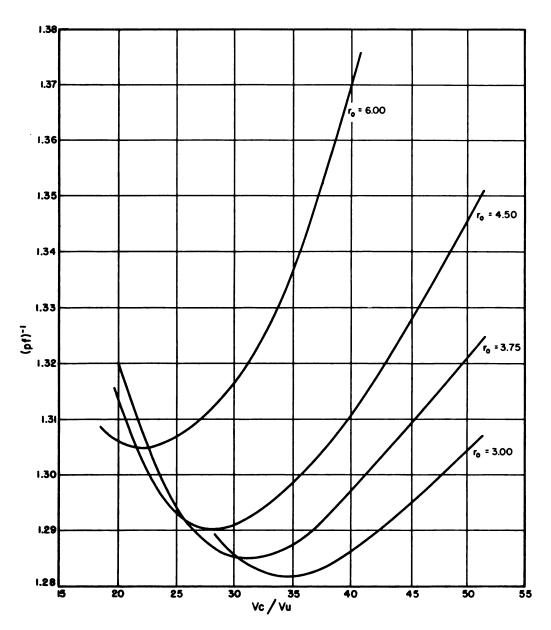


Fig. 1.5.24—The Function pf for Uranium Metal Spheres of Density 9. Reprinted from Plass and Wigner, CP-372, Dec. 1942. Inverse of pf plotted against graphite-to-uranium volume ratio; r₀ is radius of sphere in cm. Graphite of density 1.6 gm/cc; early project purity. Actually calculated for cylindrical lumps having the same volume as a sphere of the indicated radius. The difference is presumed to be very small.

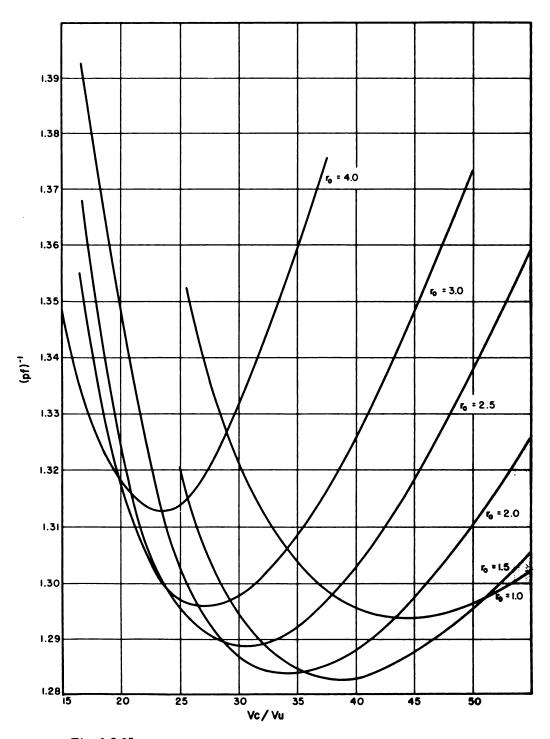


Fig. 1.5.25 — The Function pf for Uranium Metal Cylinders of Density 9. Reprinted from Plass and Wigner, CP-372, Dec. 1942. Inverse of pf plotted against graphite-to-uranium volume ratio;  $r_0$  is radius of rod in cm. Graphite of density 1.6 gm/cc; early project purity.

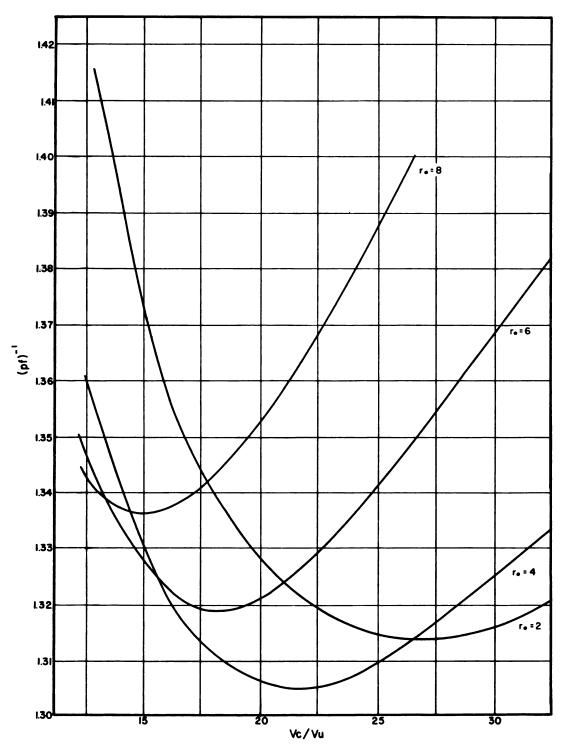


Fig. 1.5.26 — The Function pf for Uranium Oxide Spheres of Density 6. Reprinted from Plass and Wigner, CP-372, Dec. 1942. Inverse of pf plotted against graphite-uranium volume ratio;  $r_0$  is radius of sphere in cm. Graphite of density 1.6 cm/cc; early project purity. Oxide is  $U_3O_8$ .

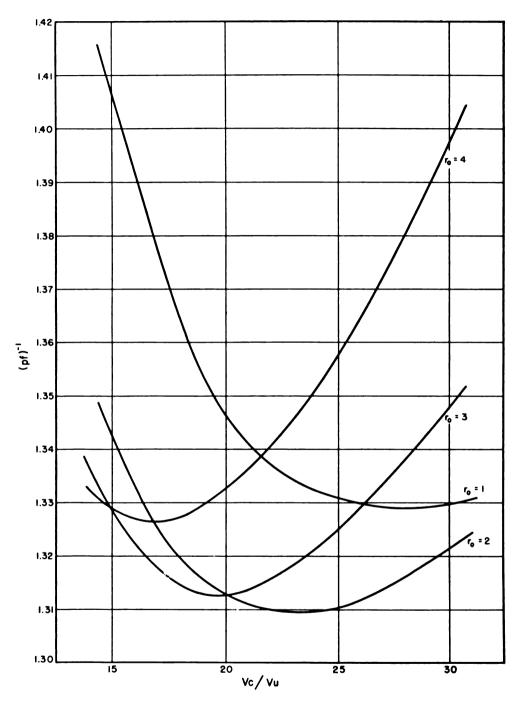


Fig. 1.5.27 — The Function pf for Uranium Oxide Cylinders of Density 6. Reprinted from Plass and Wigner, CP-372, Dec. 1942. Inverse of pf plotted against graphite-to-uranium volume ratio;  $\mathbf{r}_0$  is radius of rod in cm. Graphite of density 1.6 gm/cc; early project purity. Oxide is  $\mathbf{U}_3\mathbf{O}_8$ .

#### REFERENCES

- 1. Deleted.
- 2. Deleted.
- 3. Deleted.
- 4. Deleted.
- 5. Deleted.
- 6. TID-5022 (classified).
- 7. BNL-152 (classified).
- 8. BNL-170 (classified).
- 9. CL-697 (classified).
- 10. Deleted.
- 11. K. Way, CP-3209, Aug. 1945 (classified).
- 12. CP-3364 (classified).
- 13. Wigner and Plass, CP-372.
- 14. Clark, KAPL-743 (classified).
- 15. HKF-116, p 1.3 (classified).
- 16. K. Way, CP-3209 (classified).
- 17. TPI-20 (classified).
- 18. Weinberg and Noderer, Vol. I, Chap. IV (classified).
- 19. Wigner, CP-4.
- 20. Wigner, CP-1589 (classified).
- 21. Deleted.
- 22. CP-3407 (classified).
- 23. Weinberg and Williamson, CP-1231 (classified).
- 24. Weinberg et al, CP-2842, p 41 (classified).

## CHAPTER 1.6

# **Reactor Dynamics**

Gerald Goertzel

#### REACTOR KINETICS

The subject of reactor kinetics is concerned with the calculation of how the neutron density (prompt and delayed) within the reactor varies with time. Into the equations for this calculation are introduced the properties of the reactor as determined by temperature, density, motion of control rods, burn-up, and creation of poisons as known functions of time. Calculation of these properties will be discussed later in this chapter.

Most studies of reactor kinetics are based on an equivalent <u>space-independent one-group model</u>. Equation (1) describes this model, and the terms of these equations are interpreted for a general reactor in Eqs. (4) and (5). Problems to which the equations for the equivalent one-group space-independent model can not be adequately applied have been treated only slightly.¹

#### SPACE-INDEPENDENT ONE-GROUP MODEL

The equations of motion may be written as:

$$\frac{dn}{dt} = \frac{k-1}{l} n - \frac{k\beta n}{l} + \sum_{i} \lambda_{i} c_{i} + s$$

$$\frac{dc_i}{dt} = -\lambda_i c_i + \frac{k\beta_i n}{l}$$

where: n = total neutrons in the reactor

 $c_i$  = total delayed-neutron emitters of type i

 $\lambda_i^{-1}$  = mean life of delayed-neutron emitters of type i

s = source strength, neutrons per unit time

kn/l = rate of production of neutrons (prompt and delayed) by fission

n/l = rate of loss of neutrons, all causes

 $k\beta n/l = rate$  of creation of delayed-neutron emitters

 $[(k/l) - (k\beta/1)]n$  = rate of production of prompt neutrons by fission

 $k\beta_i n/l = rate$  of creation of delayed-neutron emitters of type i

 $\beta = \sum_{i} \beta_{i}$ 

¹References appear at end of chapter.

## GENERAL EQUATIONS

The equations describing the time behavior of a nuclear reactor may be written in the form:

$$\frac{\partial \mathbf{N}}{\partial \mathbf{t}} = (\mathbf{1} - \beta) \mathbf{f_0}(\mathbf{E}) \mathbf{J} \mathbf{N} + \sum_{\mathbf{i}} \mathbf{f_i}(\mathbf{E}) \lambda_{\mathbf{i}} \mathbf{C_i} + \mathbf{S} - \mathbf{K} \mathbf{N}$$

$$\frac{\partial \mathbf{C_i}}{\partial \mathbf{t}} = \beta_{\mathbf{i}} \mathbf{J} \mathbf{N} - \lambda_{\mathbf{i}} \mathbf{C_i}$$

$$\mathbf{f(E)} = (\mathbf{1} - \beta) \mathbf{f_0}(\mathbf{E}) + \sum_{\mathbf{i}} \beta_{\mathbf{i}} \mathbf{f_i}(\mathbf{E})$$
(2)

where:  $N(\underline{x}, E, \underline{\omega})/4\pi$  = neutron density per unit volume per unit energy per unit solid angle of velocity direction

 $\beta = \Sigma \ \beta_i$  = fraction of fission neutrons which are delayed (assumed independent of energy of neutron causing fission)

 $\beta_i$  = fraction of fission neutrons emitted by the i'th delayed-neutron emitter

 $f_0(E)$  = energy spectrum of prompt neutrons arising from fission (neutrons arising from fission are assumed to have an isotropic angular distribution),  $\int_0^\infty f_0(E)dE=1$ 

 $f_i(E)$  = energy spectrum of neutrons emitted by the i'th delayed-neutron emitter,  $\int_0^{\infty} f_i(E) dE = 1$ 

f(E) = energy spectrum of all fission neutrons

JN =  $\int \int \nu(E)\sigma_f(E)vN(\underline{x},E,\underline{\omega})dE \ d\underline{\omega}/4\pi$  = production rate of fission neutrons per unit volume per unit time

 $KN/4\pi$  = net rate at which neutrons leave the region in phase space as a result of absorption and scattering (for a one-group diffusion theory reactor model,  $KN = -v \nabla \cdot D \nabla N + \sigma_e vN$ )

 $S/4\pi$  = source density per unit volume, energy, and solid angle

 $\lambda_i^{-1}$  = mean life of the i'th-type delayed-neutron emitter

 $C_i$  = density (number per unit volume) of i'th-type delayed-neutron emitters

#### THE IMPORTANCE FUNCTION

To convert Eq. (2) to the form of Eq. (1), it is useful, at least for studying the effect of small changes in J and K, to introduce the importance function,  $W^*(\underline{x}, E, \underline{\omega})$ . For small changes in J and K, neither W nor the shape of N will change appreciably, but the magnitude of N (and of W) may change a good deal.

The importance, W, may be defined as follows. Consider a reactor slightly below critical. A source of neutrons therein will produce an equilibrium neutron-distribution, N. As the source is moved within the reactor, the shape of N will not change much, but the magnitude may. If the equilibrium total-neutron content is a measure of the magnitude,  $W(\underline{x}, \underline{E}, \underline{\omega})$  may be defined as the neutron content of the reactor resulting from a unitpoint, monoenergetic, unidirectional, neutron source at  $\underline{x}$  with energy  $\underline{E}$  and direction  $\underline{\omega}$ . The absolute magnitude of W is not of interest, but its shape is.

^{*}This function was denoted by M in Chapter 1.4.

REDUCTION OF GENERAL EQUATIONS TO EQUIVALENT ONE-GROUP SPACE-INDEPENDENT FORM

The abbreviation:

$$(f,g) = \int f g dE dx d\omega$$
 (3)

will be of use in the following. In terms of this notation, and the definition of W, the effect of the source term on the reactor behavior as given in Eq. (2) may be written as (W,S). This suggests multiplying the first of Eq. (2) by W (using  $\partial W/\partial t = 0$ ) and integrating. If one further multiplies the others of Eq. (2) by Wf_i (E) and integrates, there results:

$$\frac{\partial}{\partial t}(\mathbf{W}, \mathbf{N}) = \left\{ \mathbf{W}, \left[ (\mathbf{1} - \beta) \mathbf{f_0}(\mathbf{E}) + \sum \beta_i \mathbf{f_i}(\mathbf{E}) \right] \mathbf{J} \mathbf{N} \right\} - \sum_i \beta_i \left( \mathbf{W}, \mathbf{f_i}(\mathbf{E}) \mathbf{J} \mathbf{N} \right) + \sum_i \lambda_i \left( \mathbf{W}, \mathbf{f_i}(\mathbf{E}) \mathbf{C_i} \right) + \left( \mathbf{W}, \mathbf{S} \right) - \left( \mathbf{W}, \mathbf{K} \mathbf{N} \right)$$
(4)

$$\frac{\partial}{\partial t}(\mathbf{W}, \mathbf{f}_i \mathbf{C}_i) = \beta_i(\mathbf{W}, \mathbf{f}_i \mathbf{J} \mathbf{N}) - \lambda_i(\mathbf{W}, \mathbf{f}_i \mathbf{C}_i)$$

Equation (4) can be put into direct correspondence with Eq. (1) provided one talks of the total neutron importance (W,N) in place of the total number of neutrons n in Eq. (1). Similarly,  $(W,f_iC_i)$  is the importance of type-i delayed-neutron emitters. One then defines the effective lifetime, 1, so that (W,N)/1 is the rate of destruction of importance (W,KN) and k so that k(W,N)/1 is the rate of creation of importance (W,fJN). In terms of these concepts, the following definitions change Eq. (4) formally into Eq. (1):

$$n = (W,N)$$

$$c_{i} = (W,f_{i}C_{i})$$

$$\frac{kn}{l} = (W,f(E)JN)$$

$$\frac{n}{l} = (W,KN)$$

$$\frac{k\beta_{i}n}{l} = \beta_{i} (W,f_{i}JN)$$

$$s = (W,S)$$
(5)

From Eq. (5), it is easily seen that:

$$k = \frac{(W_1 fJN)}{(W.KN)} \tag{6}$$

or, the multiplication constant, k, is the rate of creation of importance (prompt and delayed) divided by the rate of destruction of importance. Similarly:

$$1 = \frac{(\mathbf{W}, \mathbf{N})}{(\mathbf{W}, \mathbf{K}\mathbf{N})} \tag{7}$$

or the lifetime is the total importance divided by the rate of destruction of importance. Further discussion of the meaning of l is given in Chapter 1.4.

However, in place of  $\beta_i$ , one must have:

$$\beta_{i} \frac{(\mathbf{W}, \mathbf{f}_{i} \mathbf{J} \mathbf{N})}{(\mathbf{W}, \mathbf{f}_{i} \mathbf{J} \mathbf{N})} = \epsilon_{i} \beta_{i}$$
 (8)

and, in place of  $\beta$ :

$$\epsilon \beta = \sum_{i} \epsilon_{i} \beta_{i} \tag{9}$$

The  $\epsilon_i$  are factors giving the increased importance of delayed neutrons owing to their lower energy. The  $\epsilon_i$  may often be taken as unity or, at least, as independent of i ( $\epsilon_i = \epsilon$ , all i).

Equation (1) may thus be applied to the general reactor provided that the definitions of Eqs. (6) and (7) are used for k, l and that  $\beta_l$  is replaced by  $\epsilon_l \beta_l$ . Since k-1 is a factor in the forcing term in Eq. (1), k-1 must be determined reasonably well. The choice of Eq. (6) as a definition for k, together with the specific choice of W as the weighting function, assures this; this is clear from the discussion of importance functions in Chapter 1.4. Methods for calculating W are discussed there.

# EXAMPLE: TWO-GROUP, BARE, THERMAL REACTOR

The critical equation is:

$$-\nabla \cdot \mathbf{D}_{\mathbf{f}} \nabla \mathbf{v}_{\mathbf{f}} \mathbf{N}_{\mathbf{f}} + \sigma_{\mathbf{SD}} \mathbf{v}_{\mathbf{f}} \mathbf{N}_{\mathbf{f}} = \nu \sigma_{\mathbf{f}} \mathbf{v}_{\mathbf{S}} \mathbf{N}_{\mathbf{S}}$$

$$-\nabla \cdot \mathbf{D}_{\mathbf{g}} \nabla \mathbf{v}_{\mathbf{g}} \mathbf{N}_{\mathbf{g}} + \sigma_{\mathbf{a}} \mathbf{v}_{\mathbf{g}} \mathbf{N}_{\mathbf{g}} = \sigma_{\mathbf{SD}} \mathbf{v}_{\mathbf{f}} \mathbf{N}_{\mathbf{f}}$$
(10)

A comparison with Eq. (2) shows that:

$$\mathbf{fJN} = \begin{pmatrix} 0 & \nu \sigma_f \mathbf{v}_S \\ 0 & 0 \end{pmatrix} \begin{pmatrix} \mathbf{N}_f \\ \mathbf{N}_S \end{pmatrix}$$

$$\mathbf{KN} = \begin{pmatrix} -\nabla \cdot \mathbf{D}_f \nabla \mathbf{v}_f + \sigma_{SD} \mathbf{v}_f & 0 \\ -\sigma_{SD} \mathbf{v}_f & -\nabla \cdot \mathbf{D}_S \nabla \mathbf{v}_S + \sigma_{\mathbf{a}} \mathbf{v}_S \end{pmatrix} \begin{pmatrix} \mathbf{N}_f \\ \mathbf{N}_S \end{pmatrix}$$
(11)

If  $D_f$ ,  $\sigma_{SD}$ ,  $\sigma_f$ ,  $D_s$ , and  $\sigma_a$  are independent of position, the solution for a spherical reactor of extrapolated radius a, actual radius  $a - \lambda$ , is given by:

$$\begin{pmatrix}
N_{f} \\
N_{S}
\end{pmatrix} = \frac{\sin \pi \frac{r}{a}}{r} \begin{pmatrix} \nu \sigma_{f} v_{S} \\
L_{f}
\end{pmatrix}$$

$$\begin{pmatrix}
W_{f} \\
W_{S}
\end{pmatrix} = \frac{\sin \frac{\pi r}{a}}{r} \begin{pmatrix}
L_{S} \\
\nu \sigma_{f} v_{S}
\end{pmatrix}$$
(12)

where:

$$L_{f} = \sigma_{SD}v_{f} + D_{f}v_{f}\left(\frac{\pi}{a}\right)^{2}$$

$$L_{f} = \sigma_{a}v_{s} + D_{S}v_{s}\left(\frac{\pi}{a}\right)^{2}$$
(13)

provided the critical condition:

$$\nu \sigma_f v_s \ \sigma_{SD} v_f = L_S \ L_f \tag{14}$$

is satisfied. One easily calculates:

$$\begin{split} (\textbf{W}, \textbf{IJN}) &= L_{\mathbf{S}} L_{\mathbf{f}} \int \frac{\sin^2 \frac{\pi r}{a}}{r^2} \underline{\nu \sigma_{\mathbf{f}} v_{\mathbf{S}}} \, dV \\ (\textbf{W}, \textbf{KN}) &= \nu \sigma_{\mathbf{f}} v_{\mathbf{S}} \left\{ L_{\mathbf{S}} \int \frac{\sin \frac{\pi r}{a}}{r} \left( -\underline{\nabla \cdot D_{\mathbf{f}} v_{\mathbf{f}} \nabla + \sigma_{\mathbf{SD}} v_{\mathbf{f}}} \right) \frac{\sin \frac{\pi r}{a}}{r} \, dV \right. \\ &- \nu \sigma_{\mathbf{f}} v_{\mathbf{S}} \int \frac{\sin^2 \frac{\pi r}{a}}{r} \underline{\sigma_{\mathbf{SD}} v_{\mathbf{f}}} \, dV + L_{\mathbf{f}} \int \frac{\sin \frac{\pi r}{a}}{r} \left( -\underline{\nabla \cdot D_{\mathbf{S}} v_{\mathbf{S}} \nabla + \sigma_{\mathbf{a}} v_{\mathbf{S}}} \right) \frac{\sin \frac{\pi r}{a}}{r} \, dV \right] \\ &= \nu \sigma_{\mathbf{f}} v_{\mathbf{S}} \left\{ \int \frac{\sin^2 \frac{\pi r}{a}}{r^2} \left[ \underline{\sigma_{\mathbf{SD}} v_{\mathbf{f}}} (L_{\mathbf{S}} - \nu \sigma_{\mathbf{f}} v_{\mathbf{S}}) + \underline{\sigma_{\mathbf{a}} v_{\mathbf{S}}} L_{\mathbf{f}} \right] dV \right. \\ &+ \int \left( \frac{d}{dr} \frac{\sin \frac{\pi r}{a}}{r} \right)^2 \left[ L_{\mathbf{S}} \underline{D_{\mathbf{f}} v_{\mathbf{f}}} + L_{\mathbf{f}} \underline{D_{\mathbf{S}} v_{\mathbf{S}}} \right] dV \right] \\ &(\textbf{W}, \textbf{N}) = \nu \sigma_{\mathbf{f}} v_{\mathbf{S}} (L_{\mathbf{S}} + L_{\mathbf{f}}) \int \frac{\sin^2 \frac{\pi r}{a}}{r^2} \, dV \end{split}$$

In using these equations, the underlined quantities are varied in calculating  $\delta k$ . Before such variation, the results simplify to:

$$(\mathbf{W}, \mathbf{fJN}) = \mathbf{L}_{\mathbf{S}} \mathbf{L}_{\mathbf{f}} \nu \sigma_{\mathbf{f}} \mathbf{v}_{\mathbf{S}} \int \frac{\sin^{2} \frac{\pi \mathbf{r}}{\mathbf{a}}}{\mathbf{r}^{2}} dV$$

$$(\mathbf{W}, \mathbf{KN}) = \nu \sigma_{\mathbf{f}} \mathbf{v}_{\mathbf{S}} \left[ 2 \mathbf{L}_{\mathbf{S}} \mathbf{L}_{\mathbf{f}} - \nu \sigma_{\mathbf{f}} \mathbf{v}_{\mathbf{S}} \sigma_{\mathbf{SD}} \mathbf{v}_{\mathbf{f}} \right] \int \frac{\sin^{2} \frac{\pi \mathbf{r}}{\mathbf{a}}}{\mathbf{r}^{2}} dV$$

$$(16)$$

and from Eqs. (6) and (7) (the last expression in each line uses the critical condition):

$$\mathbf{k} = \frac{\mathbf{L_{S}L_{f}}}{2\mathbf{L_{S}L_{f}} - \nu \sigma_{f} \mathbf{v_{S}} \sigma_{SD} \mathbf{v_{f}}} = 1$$

$$1 = \frac{\mathbf{L_{S} + L_{f}}}{2\mathbf{L_{S}L_{f}} - \nu \sigma_{f} \mathbf{v_{S}} \sigma_{SD} \mathbf{v_{f}}} = \frac{1}{\mathbf{L_{f}}} + \frac{1}{\mathbf{L_{S}}}$$
(17)

From Eq. (15), one may calculate the general formula for  $\delta k$  arising from small changes in a critical (k = 1) reactor:

$$\begin{split} \delta k &= \frac{\left[ W, \delta (fJ - K)N \right]}{(W,KN)} \\ &= \left[ \int \frac{\sin^2 \frac{\pi r}{a}}{r^2} \left\{ \frac{\delta (\nu \sigma_f v_s)}{\nu \sigma_f v_s} + \frac{\delta (\sigma_{SD} v_f)}{\sigma_{SD} v_f} \left( 1 - \frac{\sigma_{SD} v_f}{L_f} \right) \right. \\ &\left. - \frac{\delta (\sigma_a v_s)}{\sigma_a v_s} \frac{\sigma_a v_s}{L_s} \right\} dV - \int \left( \frac{d}{dr} \frac{\sin \frac{\pi r}{a}}{\frac{\pi}{a} r} \right)^2 \left[ \frac{\pi^2}{a^2} \frac{D_f v_f}{D_f v_f} \frac{\delta (D_f v_f)}{D_f v_f} \right. \\ &\left. + \frac{\pi^2}{L_g} \frac{D_g v_g}{D_g v_g} \frac{\delta (D_g v_g)}{D_g v_g} \right\} dV \right] / \int \frac{\sin^2 \frac{\pi r}{a}}{r^2} dV \end{split}$$

# SOLUTIONS OF THE KINETIC EQUATIONS, CONSTANT k

If s = 0 and all coefficients are constant in Eq. (1), the general solution may be obtained in terms of n and  $c_i$  at a given time by the method of Laplace transforms. Thus, if N(p) and  $C_i(p)$  are the transforms of N(t) and  $c_i(t)$ , respectively, and the initial conditions are:

$$n(0) = n_0$$

$$c_i(0) = c_{i0}$$

the transform equations are:

$$\mathbf{pN} - \mathbf{n_0} = \left(\frac{\mathbf{k} - \mathbf{1}}{1} - \frac{\mathbf{k} \epsilon \beta}{1}\right) \mathbf{N} + \sum \lambda_i \mathbf{C_i}$$

$$\mathbf{pC_i} - \mathbf{c_{i0}} = -\lambda_i \mathbf{C_i} + \frac{\mathbf{k} \epsilon_i \beta_i \mathbf{N}}{1}$$
(19)

Upon solving for N, one has:

$$\mathbf{N} = \frac{\mathbf{n_0} + \sum_{i} \frac{\lambda_i \mathbf{c}_{i0}}{\mathbf{p} + \lambda_i}}{\mathbf{p} - \frac{\mathbf{k} - 1}{1} + \frac{\mathbf{k} \epsilon \beta}{1} - \frac{\mathbf{k}}{1} \sum_{i} \frac{\lambda_i \epsilon_i \beta_i}{\mathbf{p} + \lambda_i}}$$

$$= \frac{\mathbf{n_0}}{\mathbf{k}} \frac{\frac{1}{\epsilon \beta} + \sum_{i} \left( 1 \frac{\lambda_i \mathbf{c}_{i0}}{\epsilon_i \beta_i \mathbf{n}_0} \right) \frac{\epsilon_i \beta_i}{\epsilon \beta} \frac{1}{\mathbf{p} + \lambda_i}}{\frac{1}{\mathbf{k} \epsilon \beta} + 1 - \frac{\mathbf{k} - 1}{\mathbf{k} \epsilon \beta} - \sum_{i} \frac{\epsilon_i \beta_i}{\epsilon \beta} \frac{\lambda_i}{\mathbf{p} + \lambda_i}}$$
(20)

Upon finding the inverse transform of Eq. (20), one has:

$$n(t) = n_0 \sum A(p_i)e^{p_i t}$$
 (21)

where the pi are the roots of:*

$$\frac{\mathrm{l}p}{\mathrm{k}\epsilon\beta} - \frac{\mathrm{k}-1}{\epsilon\mathrm{k}\beta} + 1 - \sum_{\mathrm{i}} \frac{\epsilon_{\mathrm{i}}\beta_{\mathrm{i}}}{\epsilon\beta} \frac{\lambda_{\mathrm{i}}}{\mathrm{p}+\lambda_{\mathrm{i}}} = 0 \tag{22}$$

and:

$$\mathbf{A}(\mathbf{p}) = \frac{1}{\mathbf{k}} \frac{\frac{1}{\epsilon \beta} + \sum_{\mathbf{i}} 1 \frac{\lambda_{\mathbf{i}} \mathbf{c}_{\mathbf{i} \mathbf{0}}}{\epsilon_{\mathbf{i}} \beta_{\mathbf{i}} \mathbf{n}_{\mathbf{0}}} \frac{\epsilon_{\mathbf{i}} \beta_{\mathbf{i}}}{\epsilon \beta} \frac{1}{\mathbf{p} + \lambda_{\mathbf{i}}}}{\frac{1}{\mathbf{k} \epsilon \beta} + \sum_{\mathbf{i}} \frac{\epsilon_{\mathbf{i}} \beta_{\mathbf{i}}}{\epsilon \beta} \frac{\lambda_{\mathbf{i}}}{(\mathbf{p} + \lambda_{\mathbf{i}})^2}}$$
(23)

Equations (21), (22), and (23) may be applied to a sudden increase in k at t = 0, where for a long time before, the reactor was operating at k = 1. In this case, Eq. (13) is modified by setting:

$$\frac{1\lambda_1 c_{10}}{\epsilon_1 \beta_1 n_0} = 1 \tag{24}$$

Solutions in this case are given in Figs. 1.6.1 and 1.6.2. If, further,  $|(k-1)/(\epsilon k\beta)| \ll 1$ , after using Eq. (24), the terms proportional to  $1/\epsilon\beta$  in Eqs. (20), (22), and (23) may be set to zero.

Setting  $1/\epsilon\beta = 0$  means that n rises suddenly at t = 0 to the value [using Eq. (20)]:

$$n(0_{+}) = \frac{\text{Lim pN(p)}}{p \to \infty}$$

$$= \frac{n_{0}}{k} \frac{1}{1 - \frac{k-1}{k \epsilon \beta}}$$
(25)

This rise is known as the "prompt jump" and occurs with a mean rise time corresponding to the most negative root of Eq. (22), a period approximately given by:

$$-\frac{1}{p} = \frac{1}{k\epsilon\beta} / \left(1 - \frac{k-1}{k\epsilon\beta}\right) \tag{26}$$

Neglecting 1 will have negligible effects on the periods other than that of Eq. (26) for  $|(k-1)/(k\epsilon\beta)| \ll 1$ . For example, (assuming specifically that  $\epsilon_l = \epsilon = 1$ ), the effect of 1 upon period is seen in Fig. 1.6.3, where the largest root of Eq. (22),  $p = 1/\tau_e$ , is plotted vs k-1 for various values of 1.

$$p \simeq \frac{(k-1)/(k\epsilon\beta)}{\frac{1}{\epsilon\beta k} + \sum \frac{\epsilon_i\beta_i}{\epsilon\beta\lambda_i}}; \sum_{i} \frac{\beta_i}{\beta\lambda_i} = 12.5 \text{ sec for } U^{235}$$

For 
$$\frac{k-1}{\epsilon \beta k} \gg 1 + \frac{l\lambda_i}{\epsilon \beta}$$
,  $p \simeq \frac{k-1-\epsilon k\beta}{l}$ 

^{*} For  $(k-1)/(\epsilon\beta k) \ll 1$ , the most positive root of Eq. (22) is:

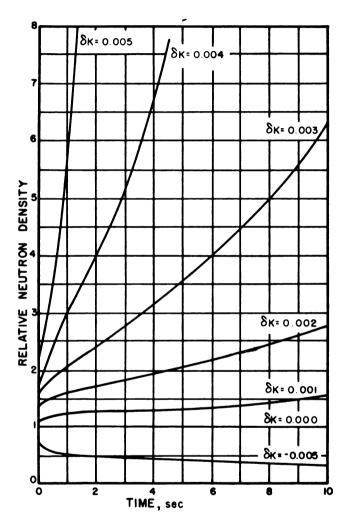


Fig. 1.6.1—Ratio of Neutron Density Following a Sudden Change in k to the Equilibrium Value Prior to the Change. Reprinted from WAPD-34, Vol. I, RM-62.

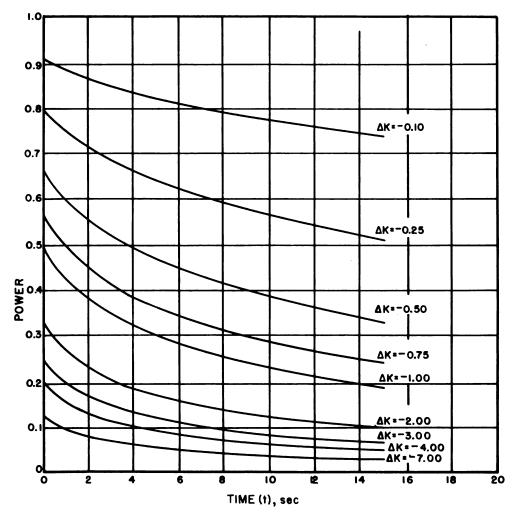


Fig. 1.6.2 — Power Following a Sudden Decrease in k. Reprinted from Reactor Physics Progress Report, KAPL-706, April 1952. Prior to changes, the power was unity.

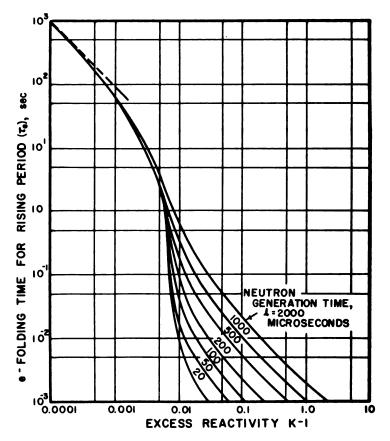


Fig. 1.6.3 — Effect of Neutron Generation Time on Reactor Period. Reprinted from M. M. Mills, Journal of Reactor Science and Technology, TID-71.

If one again makes the assumptions that  $\epsilon_i = \epsilon$ , all i, and l = 0, then Eqs. (22) and (23) may be solved graphically with graphs characteristic of the fissionable species involved but otherwise independent of the reactor. Thus, Figs. 1.6.4 to 1.6.10 give for  $U^{235}$ :

$$f(p) = \sum_{i} \frac{\beta_{i}}{\beta} \frac{\lambda_{i}}{p + \lambda_{i}} - 1$$

$$A(p) = \frac{\sum_{i} \frac{\beta_{i}}{\beta} \frac{1}{p + \lambda_{i}}}{\sum_{i} \frac{\beta_{i}}{\beta} \frac{\lambda_{i}}{(p + \lambda_{i})^{2}}}$$
(27)

as functions of p. The line with ordinate  $-(k-1)/(\epsilon k\beta)$  intersects f(p) at the  $p_i$ . The corresponding  $A(p_i)$  are immediately obtainable from the graphs.

## SOLUTIONS OF THE KINETIC EQUATIONS, k VARYING WITH TIME

In bringing a reactor to critical, k is increased gradually until the neutron flux is visible. To make the flux visible sooner in this process, neutron sources are usually located in the reactor.



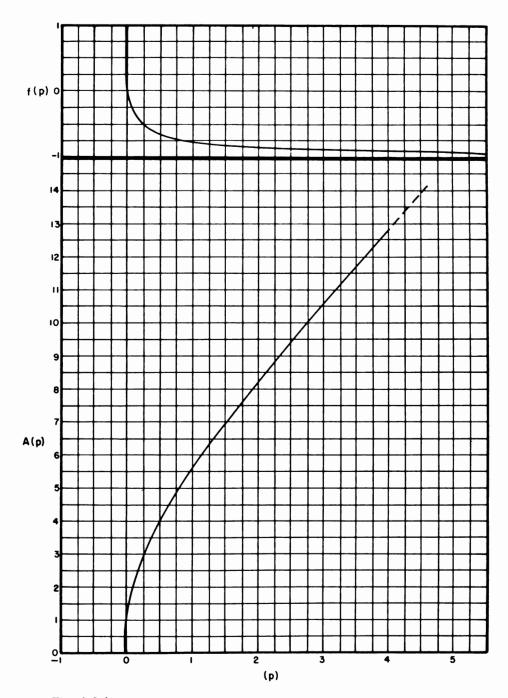


Fig. 1.6.4 — Parameters Needed to Find the Neutron Level Following a Step Change in Reactivity. Submitted by Nuclear Development Associates, Inc., Dec. 15, 1952. The figure is constructed assuming a zero neutron generation lifetime and delayed neutron characteristics for  $U^{235}$  (cf. Chapter 1.2).  $n(t) = n_0 \sum_i A(p_i) e^{p_i t}$ . The ordinate on the upper graph is the negative reactivity change in dollars. Go horizontally from  $\partial k$  to intersection with curve. Abscissa is  $p_i$ . The lower curve is  $A(p_i)$  vs p. Use of Figs. 1.6.4 to 1.6.10 yields all six values of  $p_i$  and  $A(p_i)$ .

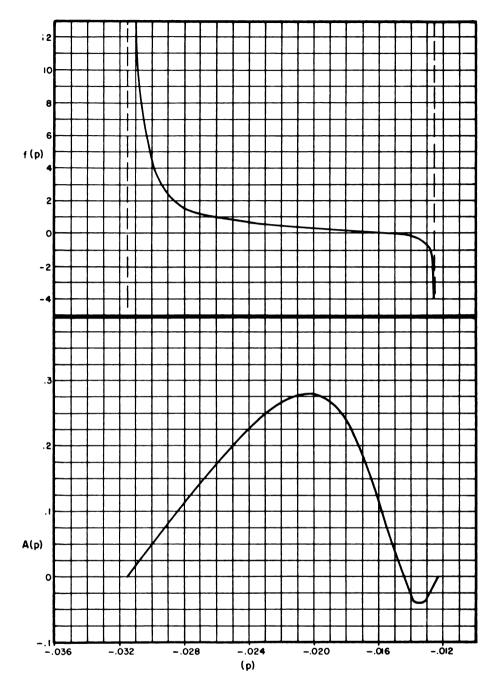


Fig. 1.6.5 — Parameters Needed to Find the Neutron Level Following a Step Change in Reactivity. Submitted by Nuclear Development Associates, Inc., Dec. 15, 1952. The figure is constructed assuming a zero neutron generation lifetime and delayed neutron characteristics for  $U^{235}$  (cf. Chapter 1.2).  $n(t) = n_0 \sum_i A(p_i) e^{p_i t}$ . The ordinate on the upper graph is the negative reactivity change in dollars. Go horizontally from  $\partial k$  to intersection with curve. Abscissa is  $p_i$ . The lower curve is  $A(p_i)$  vs p. Use of Figs. 1.6.4 to 1.6.10 yields all six values of  $p_i$  and  $A(p_i)$ .

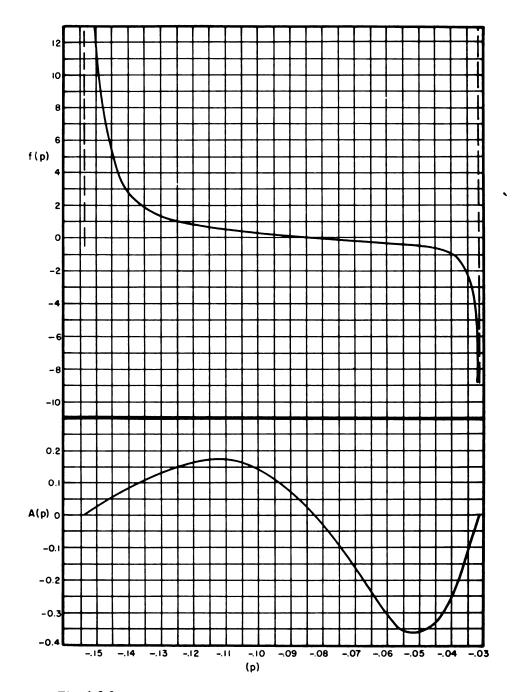


Fig. 1.6.6 — Parameters Needed to Find the Neutron Level Following a Step Change in Reactivity. Submitted by Nuclear Development Associates, Inc., Dec. 15, 1952. The figure is constructed assuming a zero neutron generation lifetime and delayed neutron characteristics for  $U^{235}$  (cf. Chapter 1.2)..  $n(t) = n_0 \sum_i A(p_i) e^{p_i t}$ . The ordinate on the upper graph is the negative reactivity change in dollars. Go horizontally from  $\partial k$  to intersection with curve. Abscissa is  $p_i$ . The lower curve is  $A(p_i)$  vs  $p_i$  Use of Figs. 1.6.4 to 1.6.10 yields all six values of  $p_i$  and  $A(p_i)$ .

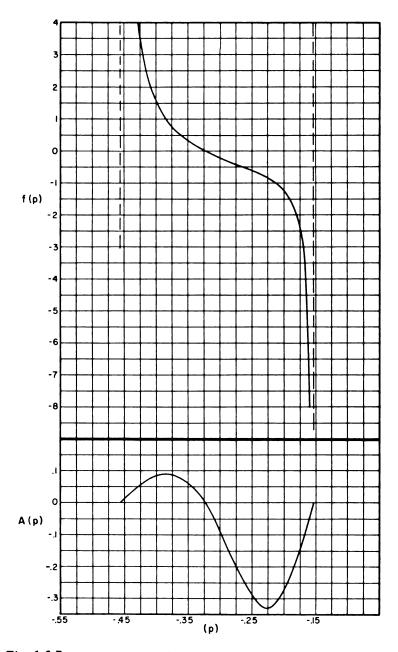


Fig. 1.6.7 — Parameters Needed to Find the Neutron Level Following a Step Change in Reactivity. Submitted by Nuclear Development Associates, Inc., Dec. 15, 1952. The figure is constructed assuming a zero neutron generation delayed neutron characteristics for  $U^{235}$  (cf. Chapter 1.2).  $n(t) = n_0 \sum_i A(p_i) e^{p_i t}$ . The ordinate on the upper graph is the negative reactivity change in dollars. Go horizontally from  $\partial k$  to intersection with curve. Abscissa is  $p_i$ . The lower curve is  $A(p_i)$  vs p. Use of Figs. 1.6.4 to 1.6.10 yields all six values of  $p_i$  and  $A(p_i)$ .

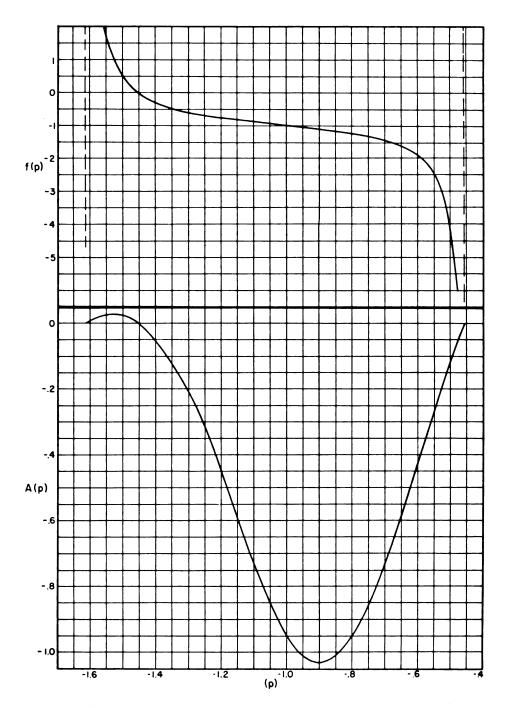


Fig. 1.6.8 — Parameters Needed to Find the Neutron Level Following a Step Change in Reactivity. Submitted by Nuclear Development Associates, Inc., Dec. 15, 1952. The figure is constructed assuming a zero neutron generation lifetime and delayed neutron characteristics for  $U^{235}$  (cf. Chapter 1.2).  $n(t) = n_0 \sum_i A(p_i) e^{p_i t}$ . The ordinate on the upper graph is the negative reactivity change in dollars. Go horizontally from  $\partial k$  to intersection with curve. Abscissa is  $p_i$ . The lower curve is  $A(p_i)$  vs p. Use of Figs. 1.6.4 to 1.6.10 yields all six values of  $p_i$  and  $A(p_i)$ .



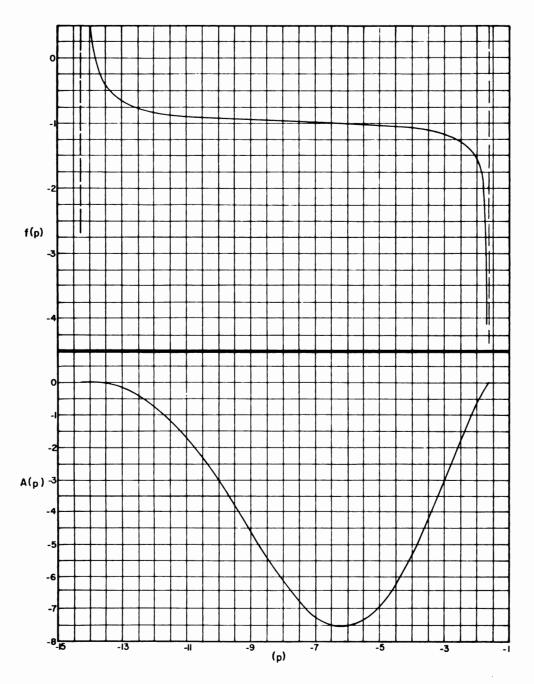


Fig. 1.6.9 — Parameters Needed to Find the Neutron Level Following a Step Change in Reactivity. Submitted by Nuclear Development Associates, Inc., Dec. 15, 1952. The figure is constructed assuming a zero neutron generation lifetime and delayed neutron characteristics for  $U^{235}$  (cf. Chapter 1.2).  $n(t) = n_0 \sum_i A(p_i) e^{p_i t}$ . The ordinate on the upper graph is the negative reactivity change in dollars. Go horizontally from  $\partial k$  to intersection with curve. Abscissa is  $p_i$ . The lower curve is  $A(p_i)$ . The lower curve is  $A(p_i)$  vs p. Use of Figs. 1.6.4 to 1.6.10 yields all six values of  $p_i$  and  $A(p_i)$ .

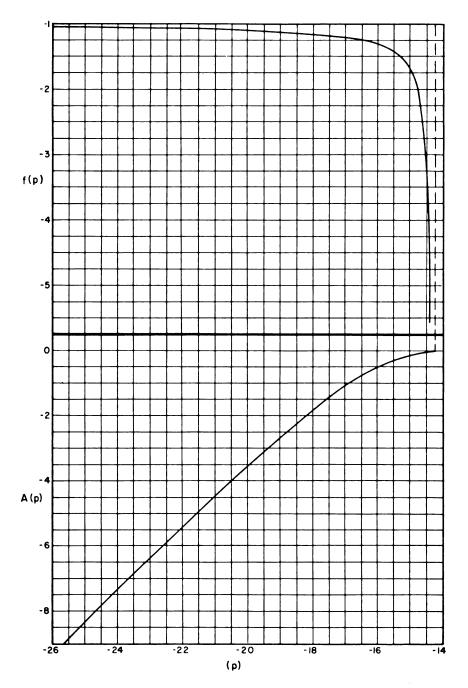


Fig. 1.6.10—Parameters Needed to Find the Neutron Level Following a Step Change in Reactivity. Submitted by Nuclear Development Associates, Inc., Dec. 15, 1952. The figure is constructed assuming a zero neutron generation lifetime and delayed neutron characteristics for  $U^{235}$  (cf. Chapter 1.2).  $n(t) = n_0 \sum_i A(p_i) e^{p_i t}$ . The ordinate on the upper graph is the negative reactivity change in dollars. Go horizontally from  $\partial k$  to intersection with curve. Abscissa is  $p_i$ . The lower curve is  $A(p_i)$  vs p. Use of Figs. 1.6.4 to 1.6.10 yields all six values of  $p_i$  and  $A(p_i)$ .

Many people^{2,3,4} have solved the kinetic equations with k = A + Bt for cases as indicated above and also for cases in which k = 1, t < 0 and k = 1 + (dk/dt)t for k > 0. An example of this latter case is given in Fig. 1.6.11.

If k = 1 + (dk/dt)t for both positive and negative times, the solution is somewhat different and depends on the source strength in the reactor.

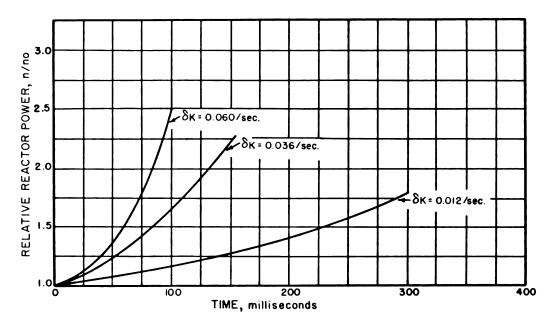


Fig. 1.6.11 — Relative Reactor Power for k Varying Linearly with Time. Reprinted from WAPD-34, Vol. I, RM-62. At time zero the reactor is critical and k commences to rise at the rate shown on each curve.

Thus, for one average neutron-delay group, neglecting the prompt lifetime, the equations for linearly varying k can be readily solved.

On the basis of the above assumptions Eq. (1) may be written:

$$0 = (\mathbf{k} - 1)\frac{\mathbf{n}}{\mathbf{l}} - \mathbf{k}\beta\frac{\mathbf{n}}{\mathbf{l}} + \lambda \mathbf{c} + \mathbf{s}$$

$$\frac{\partial \mathbf{c}}{\partial \mathbf{t}} = -\lambda \mathbf{c} + \mathbf{k}\beta\frac{\mathbf{n}}{\mathbf{l}}$$
(28)

Elimination of c gives an equation for n/l, the loss rate of neutrons. The fission rate is nearly  $n/l\nu$ . Thus, one has for n/ls:

$$[k(1-\beta)-1] \frac{d}{dt} \frac{n}{1s} + (1-\beta) \frac{n}{1s} \frac{dk}{dt} + \lambda(k-1) \frac{n}{1s} + \lambda = 0$$
 (29)

which may be solved by quadrature given k(t). In Fig. 1.6.12 n/ls vs  $(k-1)/\beta = (t/\beta)$  (dk/dt) is plotted for k=1+t dk/dt with various values of  $\beta/(dk/dt)$  (with  $\lambda=0.05$ , a value best used with  $\beta=0.004$ ). If at any time the change in k is stopped, the reactor period will be:



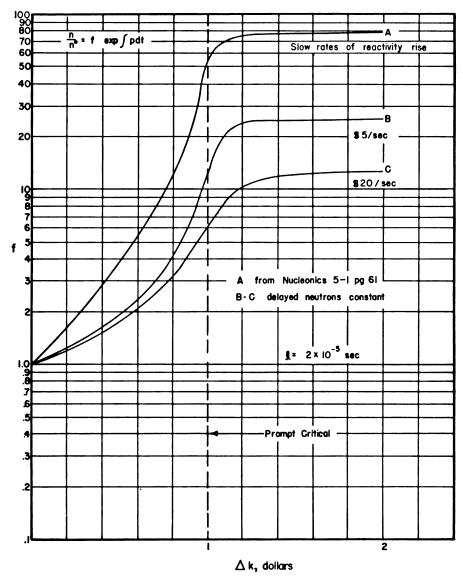


Fig. 1.6.12—Relative Reactor Power for k Varying Linearly with Time. Taken from KAPL-847 (to be published). See also, Eq. (34).

$$T = \frac{\frac{n}{ls}}{\frac{d}{dt}\frac{n}{ls}} = \frac{1 - k(1 - \beta)}{\lambda(k - 1)}$$
(30)

This period is also given in Fig. 1.6.12.

Assume the neutron flux will first be detectable after a multiplication of  $10^7$ . Then, if a reactor is started by increasing the reactivity at a rate of one dollar every 200 sec, the flux will become visible when the reactivity is  $0.77\beta$  above delayed critical (i.e.,  $0.23\beta$  below prompt critical). If the reactivity is kept constant at  $0.77\beta$ , the flux will continue to rise with a period of 6 sec. More accurate values of the period (calculated using six delay groups) can be obtained from Fig. 1.6.3 or 1.6.4.

The solution of Eq. (1), for k an arbitrary (specified) function of time, may be obtained numerically. The work is expedited by using:⁵

$$c_{i}(t) = \frac{\epsilon_{i}\beta_{i}}{l} \int_{-\pi}^{t} e^{-\lambda_{i}(t-s)} k(s)n(\epsilon)ds$$
(31)

to eliminate the ci and obtain (with zero source):

$$\frac{1}{\epsilon\beta} \frac{\partial n}{\partial t} = \frac{\left[k(1-\epsilon\beta)-1\right]n}{\epsilon\beta} + \int_{-\infty}^{t} \left[\sum_{s} \lambda_{i} \frac{\epsilon_{i}\beta_{i}}{\epsilon\beta} e^{-\lambda_{i}(t-s)}\right] k(s)n(s)ds \tag{32}$$

The sum in the brackets is, for a given species of fissionable material, a universal function of t-s if one uses the approximation  $\epsilon_i = \epsilon$ .

Plots⁶ for U²³⁵ of:

$$\mathbf{K}(\mathsf{t}) = \sum \lambda_i \, \frac{\beta_i}{\beta} \, \mathrm{e}^{-\lambda_i t}$$

$$I(t) = \int_{-\infty}^{\infty} K(s) ds$$
 (33)

$$L(t) = \int_{t}^{\infty} I(s) ds$$

are given in Fig. 1.6.13.

I(t) and L(t) are useful in numerical integration. Thus:

$$\begin{split} \int_{t_1}^{t_2} K(t-s) f(s) ds &= f(t_2) \left[ I(t-t_2) - \frac{L(t-t_2) - L(t-t_1)}{t_2 - t_1} \right] \\ & \cdot \\ & - f(t_1) \left[ I(t-t_1) - \frac{L(t-t_2) - L(t-t_1)}{t_2 - t_1} \right] \end{split}$$

if one may approximate f(t) for t in the range  $t_1$  to  $t_2$  by:

$$f(t) = f(t_1) + \frac{t - t_1}{t_2 - t_1} [f(t_2) - f(t_1)]$$

An approximate solution of Eq. (32) or Eq. (1) is given, for slowly varying k(t), by:

$$n(t) = C \sqrt{\frac{1 + \sum \frac{\epsilon_i \beta_i}{\lambda_i}}{1 + \sum \frac{\epsilon_i \beta_i / \lambda_i}{(1 + p(t) \lambda_i)^2}}} e^{\int_0^t p(t')dt'}$$
(34)

where p(t) is the most positive root of Eq. (22) with k = k(t). See Fig. 1.6.14 for applications of Eq. (34).

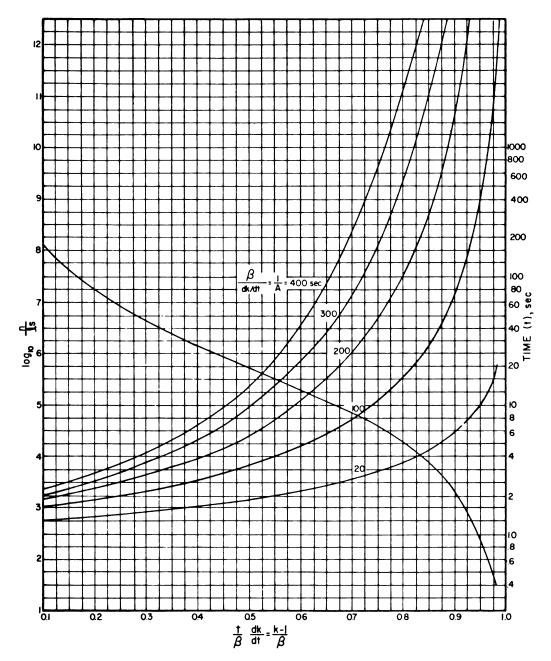


Fig. 1.6.13—Reactor Period and Ratio of Neutron Production Rate to Source Strength for k Increasing Linearly with Time. Submitted by Nuclear Development Associates, Inc., Dec. 15, 1952. Calculations were carried out with one delay group having a mean life of 20 sec. For an example see Eq. (30) et seq in the text.

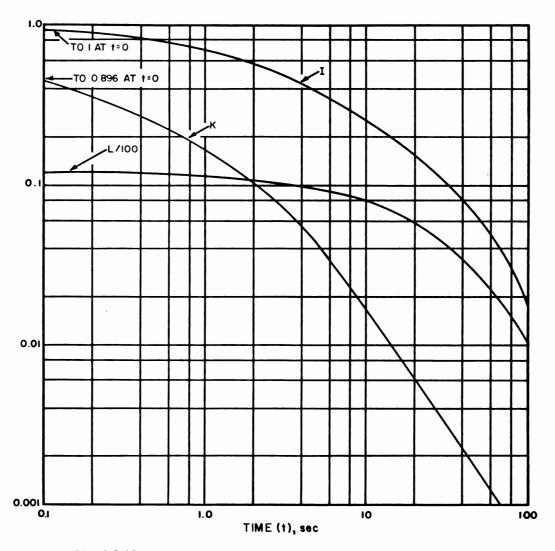


Fig. 1.6.14—Some Functions Useful when k has a Known Time Behavior. Reprinted from Reactor Physics Progress Report, KAPL-706, April 1952. See Eq. (31) et seq in the text.

## **INHOURS**

Equation (22) may be used to determine k-1 for an experimental reactor period, T=1/p:

$$k - 1 = \frac{1}{kT} + \epsilon \beta - \sum_{i} \epsilon_{i} \beta_{i} \frac{\lambda_{i}}{\frac{1}{T} + \lambda_{i}}$$

$$= \frac{1}{kT} + \sum_{i} \epsilon_{i} \beta_{i} \frac{\tau_{i}}{T + \tau_{i}}$$
(35)

where  $\tau_i = 1/\lambda_i$ . The inhour is a unit of reactivity and is defined as a constant times the right side of Eq. (35). The definition of this constant gives for the reactivity in inhours for a period T (with  $\tau_i$ , l, T in seconds):

$$I = \frac{\frac{1}{kT} + \sum_{i} \frac{\epsilon_{i} \beta_{i} \tau_{i}}{T + \tau_{i}}}{\frac{1}{3600k} + \sum_{i} \frac{\epsilon_{i} \beta_{i} \tau_{i}}{3600}}$$
(36)

Clearly, I is dimensionless and decreases as T increases. For large T, one has approximately:

$$I \simeq \frac{3600}{T}$$

$$k - 1 \simeq \frac{\sum \beta_i \tau_i}{T} \simeq \frac{\sum \beta_i \tau_i}{3600} I$$
(37)

That is, the inverse of the reactor period in hours is the reactivity in units of inhours.

### THE DOLLAR AS A UNIT OF REACTIVITY

The combination  $(k-1)/\beta$  occurs fairly often in the kinetic equations. This suggests the use of  $\beta$  as a unit of reactivity. Thus, by definition,  $(k-1)/\beta$  is the reactivity change measured in dollars (symbol \$). One one-hundredth of a dollar, as might be expected, is a cent.

#### REACTIVITY COEFFICIENTS AND RELATED TOPICS

Reactor dynamics is concerned with the solution of the equations of motion of a reactor system, including any external equipment with which there exists an interaction. It was indicated above that in most problems changes in the system can be represented in their effect on neutron behavior in the reactor, in terms of a single number, k, the multiplication constant.

In the following study of the changes in k arising from changes in the system, these changes are represented in terms of the thermodynamic variables of temperature and density,  $T(\underline{x},t)$ ,  $\rho(\underline{x},t)$ , and in terms of concentrations,  $z_i$  ( $\underline{x},t$ ),* of the various substances of which the reactor is constructed. Detailed consideration of control rods or other methods of obtaining control action is deferred until later in this chapter.

The starting point of these considerations is contained in Eq. (6). If one replaces k by  $k + \delta k$ , JN by JN +  $\delta$ (JN), and KN by KN +  $\delta$ (KN) in Eq. (6), where:

$$\mathbf{k} = \frac{(\mathbf{w}, \mathbf{fJN})}{(\mathbf{w}, \mathbf{KN})} = 1 \tag{38}$$

there results:

$$\delta \mathbf{k} = \frac{(\mathbf{W}, \mathbf{fJN}) + (\mathbf{W}, \mathbf{f\delta}(\mathbf{JN}))}{(\mathbf{W}, \mathbf{KN}) + (\mathbf{W}, \mathbf{\delta}(\mathbf{KN}))} - 1 \tag{39}$$

or, using Eq. (38):

^{*} There is clearly one variable too many since the  $\mathbf{z_i}$  determined  $\rho$ . It is nonetheless convenient to keep these variables.

$$\delta \mathbf{k} = \left\{ \frac{(\mathbf{W}, \mathbf{f} \delta(\mathbf{J} \mathbf{N}))}{(\mathbf{W}, \mathbf{f} \mathbf{J} \mathbf{N})} - \frac{(\mathbf{W}, \delta(\mathbf{K} \mathbf{N}))}{(\mathbf{W}, \mathbf{K} \mathbf{N})} \right\} \left\{ \frac{1}{1 + \frac{(\mathbf{W}, \delta(\mathbf{K} \mathbf{N}))}{(\mathbf{W}, \mathbf{K} \mathbf{N})}} \right\}$$
(40)

In Eq. (40), the second factor on the right need rarely be considered. Furthermore, unless  $\delta J$  or  $\delta K$  are concentrated in energy or position (as in a control rod), one may replace  $\delta(JN)$  and  $\delta(KN)$  in Eq. (40) by  $(\delta J)N$  and  $(\delta K)N$ , respectively. This simpler perturbation treatment yields:

$$\delta \mathbf{k} = \frac{(\mathbf{W}, \mathbf{f} \delta \mathbf{J} \mathbf{N})}{(\mathbf{W}, \mathbf{f} \mathbf{J} \mathbf{N})} - \frac{(\mathbf{W}, \delta \mathbf{K} \mathbf{N})}{(\mathbf{W}, \mathbf{K} \mathbf{N})}$$
(41)

[It may be remarked that the two denominators on the right in Eq. (41) are equal, as follows from Eq. (38).]

In applying Eq. (41), it is often useful to write  $\delta k$  as an integral over the reactor volume:

$$\delta \mathbf{k} = \int \left\{ \frac{\delta \mathbf{k}}{\delta \mathbf{T}} \, \delta \mathbf{T} + \sum_{i} \frac{\delta \mathbf{k}}{\delta \mathbf{Z}_{i}} \, \delta \mathbf{z}_{i} \right\} \, dV \tag{42}$$

This expression defines the variational derivatives  $\delta k/\delta T$ ,  $\delta k/\delta z_1$ . In Eq. (42), over-all density changes correspond to  $\delta z_i/z_i = \delta \rho/\rho$ , and the effect of such a density change is given by:

$$\delta \mathbf{k} = \int \left( \sum_{i} \mathbf{z}_{i} \frac{\delta \mathbf{k}}{\delta \mathbf{z}_{i}} \right) \frac{\delta \rho}{\rho} \, d\mathbf{V} = \int \frac{\delta \mathbf{k}}{\delta \rho} \, \delta \rho \, d\mathbf{V}$$
 (43)

which also defines  $\delta k/\delta \rho$ .

### **DENSITY EFFECTS**

Density changes in the reactor change macroscopic cross sections and diffusion coefficients. Thus, for any macroscopic cross section,  $\sigma$ :

$$\frac{\delta\sigma}{\sigma} = \frac{\delta\rho}{\rho} \tag{44}$$

whereas, a diffusion coefficient, D, varies inversely as a cross section:

$$\frac{\delta \mathbf{D}}{\mathbf{D}} = -\frac{\delta \rho}{\rho} \tag{45}$$

In computing the effect of the density change, the motion of the boundary should not be neglected. Thus, in a slab reactor, the diffusion coefficient before and after an expansion might look like Fig. 1.6.15.

In such a case,  $\delta D$  may be given as in Fig. 1.6.16. It is the positive part of  $\delta D$  which, in a diffusion-theory reactor model, gives rise to the portion of  $\delta k$  coming from the change in buckling. Similar procedures apply to cross sections and the like at core-reflector interfaces.

Consider the "Two-group, Bare, Thermal Reactor" discussed previously with density changes arising only from expansion (no removal of material as in a liquid reactor).



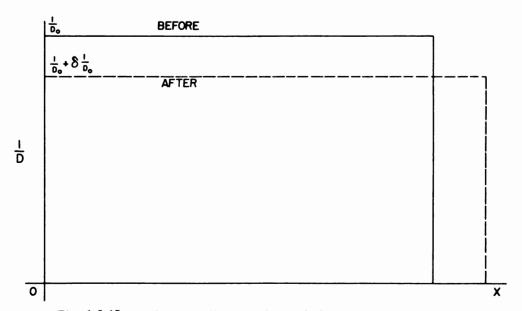


Fig. 1.6.15 — Diffusion Coefficient Before and After a Density Change. Submitted by Nuclear Development Associates, Inc. Dec. 15, 1952. The reactor is a bare slab.

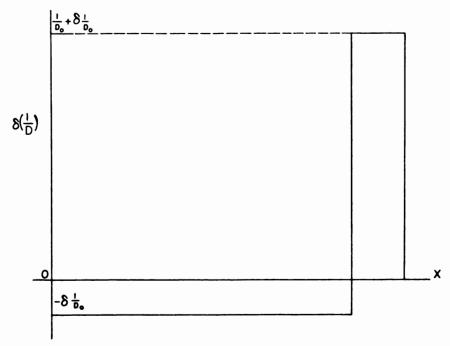


Fig. 1.6.16—Change in Diffusion Coefficient After a Density Change. Submitted by Nuclear Development Associates, Inc. Dec. 15, 1952. The reactor is a bare slab.

Clearly, from the conservation of mass law, the motion of the boundary is given by:

$$\delta a = -\frac{\int \delta \rho \ dV}{\int \rho \ dS} = -\frac{\int \delta \rho \ dV}{4\pi \rho a^2}$$
 (46)

On applying Eqs. (9), (41), (42), and (46), there results:

$$\left[ \int \left( \frac{\sin \frac{\pi}{a} r}{r} \right)^{2} dV \right] \rho \frac{\delta k}{\delta \rho} = \left[ 2 - \frac{\sigma_{SD} v_{f}}{L_{f}} - \frac{\sigma_{a} v_{s}}{L_{s}} \right] \times \left[ \left( \frac{\sin \frac{\pi r}{a}}{r} \right)^{2} \right]_{A} + \left[ \left( \frac{d}{dr} \frac{\sin \frac{\pi r}{a}}{\frac{\pi r}{a}} \right)^{2} \right]_{B} + \left[ -\left( \frac{d}{dr} \frac{\sin \frac{\pi r}{a}}{\frac{\pi r}{a}} \right)^{2} \right]_{r=a} \right]_{C} \tag{47}$$

where  $[\ ]_A$  arises from cross-section changes,  $[\ ]_B$  from diffusion-coefficient changes, and  $[\ ]_C$  from boundary motion. If  $\delta\rho$  is uniform (independent of position):

$$\delta \mathbf{k} = \delta \rho \int \frac{\delta \mathbf{k}}{\delta \rho} \, dV$$

$$= \frac{\delta \rho}{\rho} \left\{ 2 - \frac{\sigma_{\rm SD} \mathbf{v_f}}{\mathbf{L_f}} - \frac{\sigma_{\rm a} \mathbf{v_g}}{\mathbf{L_g}} \right\} \times \frac{4}{3}$$
(48)

#### DIRECT TEMPERATURE EFFECTS

The effect of temperature changes alone (in addition to the effect of the concomitant density changes) occurs through changes in the cross sections which are functions of the relative velocities of the neutrons and nuclei. The relative velocity changes with temperature for two reasons:

- (1) The absolute velocities of the nuclei change (Doppler effect).
- (2) The thermal-neutron velocity distribution changes.

If one considers a nuclear process with macroscopic cross section  $\sigma(s)$  as a function of neutron speed, if he assumes that this cross section is a function of relative speeds of neutron and atom only, and if the number of neutrons having a speed between s and s + ds is N(s)ds, then an effective cross section,  $\sigma^*(s)$ , may be so defined that:

$$\int_0^\infty \sigma^*(s) s N(s) ds \tag{49}$$

is the total number of processes under discussion that take place per unit time.

Let Q(y) dy be the probability that the speed of the nuclei is between y and y + dy; then, if the neutron and nucleus velocity vectors are randomly oriented:

$$\sigma^*(\mathbf{s}) = \int_0^\infty \frac{\mathbf{x}^2 \sigma(\mathbf{x})}{2\mathbf{s}^2} \int_{|\mathbf{x}-\mathbf{s}|}^{|\mathbf{x}+\mathbf{s}|} \frac{\mathbf{Q}(\mathbf{y})}{\mathbf{y}} \, \mathrm{d}\mathbf{y} \, \mathrm{d}\mathbf{x} \tag{50}$$

In almost all cases of interest, the distribution of nuclear speeds can be taken as Maxwellian (cf. Chapter 1.3), and Q(y) is given by:

$$Q(y) = \frac{4}{\sqrt{\pi}} \frac{1}{\alpha^3} y^2 e^{-\frac{y^2}{\alpha^2}}$$
 (51)

where:  $\alpha = (2kT/M)^{1/2}$ 

M = atomic mass

k = Boltzmann's constantT = absolute temperature

In this case:

$$\sigma^*(\mathbf{s}) = \frac{1}{\alpha \mathbf{s}^2 \sqrt{\pi}} \int_{-\infty}^{\infty} |\mathbf{x}| \sigma(|\mathbf{x}|) e^{-\left(\frac{\mathbf{x} - \mathbf{s}}{\alpha}\right)^2} \mathbf{x} \, d\mathbf{x}$$
 (52)

Clearly, the major contribution to the integral in Eq. (52) comes from x in the range  $s \pm \alpha$ . If  $|x|\sigma(|x|)$  does not change much in this range, it may be removed outside as  $s \sigma(s)$  with the result:

$$\sigma^*(s) \simeq \sigma(s)$$
 (53)

Note Eq. (53) is a precise result for 1/v cross sections.

Equation (52) is of primary interest in studying the effect on resonance capture of the spreading of sharp lines by the nuclear motion. This spread, known as "Doppler broadening," is seen clearly in Eq. (52), since  $s\sigma^*(s)$  will be of appreciable size over a range  $2\alpha$  greater than  $x\sigma(x)$ . It was seen in the discussion of lattices in Chapter 1.5 that the resonance escape probability depends upon the evaluation of the integral:

$$\int\!\frac{\sigma_a^*}{1+\frac{\sigma_a^*}{\sigma_S}}\frac{dE}{E}$$

When  $\sigma_a^*$  is varying rapidly, a factor of 1/E can be taken outside the integral sign with little error. For convenience in calculation, one can then investigate the quantity F, defined by:

$$\mathbf{F} = \int \frac{\sigma_{\mathbf{a}}^*}{1 + \frac{\sigma_{\mathbf{a}}^*}{\sigma_{\mathbf{a}}}} d\mathbf{E} / \int \sigma_{\mathbf{a}}^* d\mathbf{E}$$
 (54)

 $\sigma_a^*$  may be obtained from Eq. (52) if we use for  $\sigma_a$  the Breit-Wigner formula (cf. Eq. (26) of Chapter 1.2).

By introducing the reduced energy variable:

$$\xi = \frac{\mathbf{E} - \mathbf{E_r}}{\Gamma/2} \tag{55}$$

one may write approximately:

$$\frac{\sigma_{\rm a}^{\star}(E)}{(\sigma_{\rm a})_{\rm max}} = \psi(\xi) = \frac{1}{2\sqrt{\pi\theta}} \int_{-\infty}^{\infty} \frac{d\xi'}{1+{\xi'}^2} e^{-\frac{(\xi-{\xi'})^2}{4\theta}} d\xi'$$
 (56)

where:

$$\theta = \frac{4E_{T}kT}{A_{m}\Gamma^{2}} \tag{57}$$

 $A_m$  is the ratio of nuclear mass to neutron mass and  $E_r$  and  $\Gamma$  the energy and width of the resonance, respectively. In obtaining Eq. (56), the expansion:

$$\sqrt{\frac{2E}{\Gamma}} = \sqrt{\xi + \frac{2E_r}{\Gamma}} \simeq \sqrt{\frac{2E_r}{\Gamma}} \left( 1 + \frac{\Gamma \xi}{4E_r} \right)$$
 (58)

was used in the exponential.

For homogeneous mixtures:2

$$F \simeq \frac{2 + A(P - 1)}{P\sqrt{2(1 + P) + \gamma A^2}}$$
 (59)

where:

$$P = \sqrt{1 + \gamma A(2 - A)}$$

$$\gamma = \frac{(\sigma_a)_{max}}{\sigma_c}$$

and A is the root of:

$$A(5-4A+A^2) = 2\sqrt{\frac{\pi}{2\theta}} e^{\frac{1}{2\theta}} \operatorname{erfc}\left(\frac{1}{\sqrt{2\theta}}\right)$$

where:

$$\operatorname{erfc}(x) = 1 - \frac{2}{\sqrt{\pi}} \int_0^x e^{-\mu^2} du = \frac{2}{\sqrt{\pi}} \int_x^{\infty} e^{-\mu^2} du$$

This result is exact in the following limiting cases:

$$\begin{cases} \theta = 0 \\ \theta = \infty \end{cases} \text{ any } \gamma$$

$$\gamma = 0$$

$$\gamma = \infty$$

$$\gamma = \infty$$
any  $\theta$ 

Roe¹⁰ has treated the case of inhomogeneous mixtures, where self-absorption effects are important, in slab geometry. He considers a one-velocity problem in which the resonance absorbers are in the form of plane slabs separated by slabs of moderator. Neutrons are assumed to be produced uniformly in the moderator. In Fig. 1.6.17, F has been plotted vs  $\mu\tau N(\theta)$ . The auxiliary function  $N(\theta)$  is given in Fig. 1.6.18. Figure 1.6.19 gives the function:

$$\frac{\theta \frac{\partial \mathbf{F}}{\partial \theta}}{1 - \mathbf{N}(\theta)} = \frac{\mathbf{T} \frac{\partial \mathbf{F}}{\partial \mathbf{T}}}{1 - \mathbf{N}(\theta)}$$

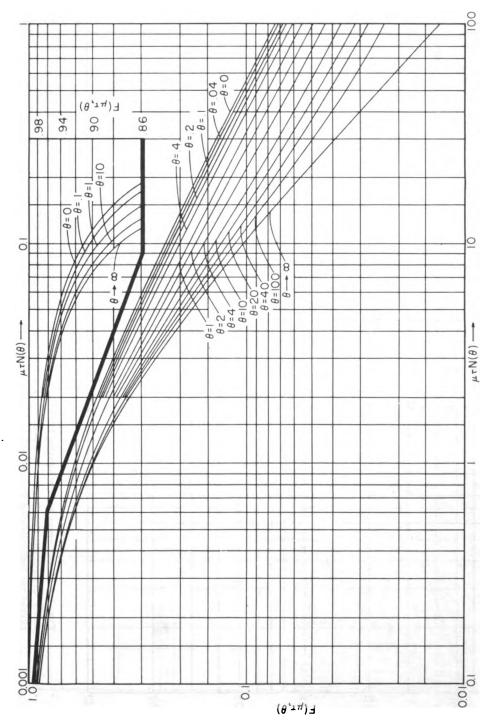
which is useful for calculating temperature effects. The quantities involved are defined as follows:

 $l_a = foil thickness$ 

1_m = moderator thickness between foils

 $\tau = \sigma_{\mathbf{a}_{\mathbf{max}}} \mathbf{l}_{\mathbf{a}}$ 

 $\sigma_{sf}$  = macroscopic scattering cross section of foil



nance Absorption. Reprinted from a personal communication from G. M. Roe at KAPL. When using curves Fig. 1.6.17 --- Curves for Calculating the Effect of Foil Self-absorption and Doppler-broadening on Resoabove the heavy line, use the ordinate scale on the right. For use of these curves see text Eq. (54) et seq.

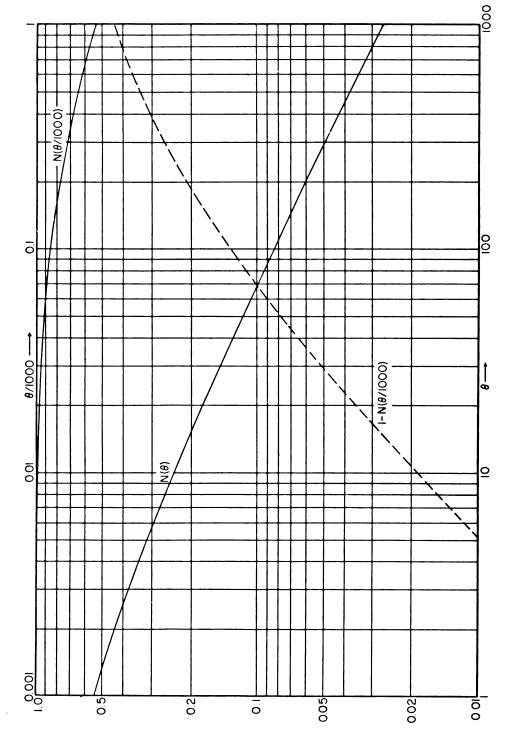
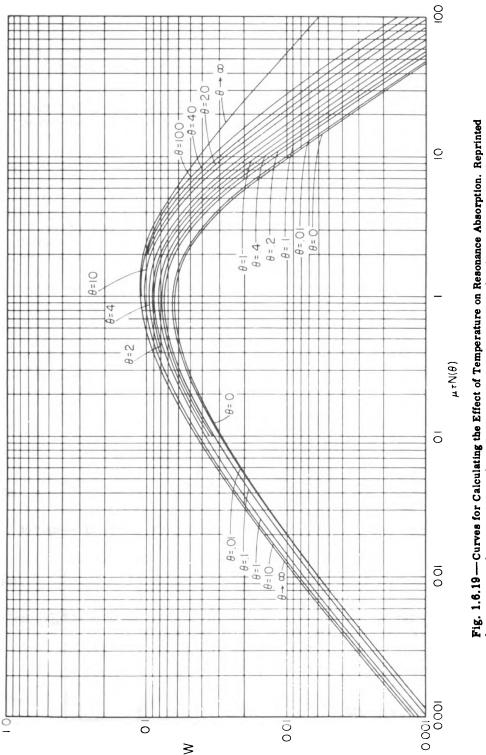


Fig. 1.6.18 — Curves for Calculating the Effect of Foil Self-absorption and Doppler-broadening on Resonance Absorption. Reprinted from a personal communication from G. M. Roe at KAPL. For use of these curves see text following Eq. (54).



from a personal communication from G. M. Roe at KAPL. W =  $[\theta(\partial F/\partial \theta)/1-N] = [T(\partial F/\partial T)/1-N]$ . See text following Eq. (54).

 $\sigma_{sm}$  = macroscopic scattering cross section of moderator

 $1/\mu = 1/\mu_0 + 2l_a\sigma_{sf}$ 

 $\mathbf{a} = (1/\epsilon)[\mathbf{l_m} + (1 - \epsilon)\mathbf{l_a}] \sigma_{sm}$ 

 $\epsilon$  = fraction of foil plane actually occupied by the foil

A plot of  $\mu_0$  vs a is given in Fig. 1.6.20.

The effect of the energy change of thermal neutrons may be calculated only on the basis of some model. The customary model assumes that the thermal neutrons are in fact represented by a density:

$$n_{th}(\underline{r}, \underline{E}) = R(\underline{r})f(\underline{E}, \underline{T})$$
(60)

where T is an appropriate mean temperature of the thermal neutrons and f(E,T) is the corresponding Boltzmann distribution of neutron energies. In a weakly absorbing medium, Eq. (60) is a good approximation, with T the moderator temperature averaged over a suitable region. For absorbing media, the thermal neutrons on the average will have higher energies than those corresponding to the moderator temperature. The determination of an appropriate temperature is discussed in Chapter 1.3.

If it is assumed that T and  $\delta$ T are known, the value of  $\delta$ R may be obtained as follows:

$$f(E,T)dE = \frac{2}{\sqrt{\pi}} e^{-\frac{\overline{E}}{kT}} \sqrt{\frac{E}{kT}} \frac{1}{kT} dE$$
 (61)

The effective value of any cross section,  $\sigma v$ , ( $\sigma$  in area per atom) as it appears in  $n_{th}v\sigma$  is given by:

$$\overline{\sigma v}(T) = \int_0^\infty f(E, T)(\sigma v)(E) dE$$
 (62)

so that:

$$\frac{\partial}{\partial \mathbf{T}}(\overline{ov}) = \int_0^{\infty} \frac{\partial \mathbf{f}}{\partial \mathbf{T}} (ov)(\mathbf{E}) d\mathbf{E}$$
 (63)

Often  $\sigma v$  is independent of energy, in which case  $\partial/\partial T(\overline{\sigma v})=0$ . If  $\sigma$  is independent of energy:

$$\frac{\partial \overline{\sigma v}}{\partial T} = \sigma \frac{\partial \overline{v}}{\partial T} \tag{64}$$

where  $\overline{v} = 2/\sqrt{\pi} \sqrt{2kT/m}$ . Another case of interest arises in the evaluation of  $\overline{D_{th}v}$ . Since  $D_{th}$  is a reciprocal scattering cross section, one is interested in:

$$\left(\frac{\overline{\mathbf{v}}}{\sigma_{\mathbf{sc}}}\right)$$

For  $\sigma_{sc}$  independent of energy:

$$\frac{\frac{\partial}{\partial \mathbf{T}} \overline{\mathbf{D}_{th} \mathbf{v}}}{\overline{\mathbf{D}_{th} \mathbf{v}}} = \frac{1}{\overline{\mathbf{v}}} \frac{\partial \overline{\mathbf{v}}}{\partial \mathbf{T}} = \frac{1}{2} \frac{1}{\mathbf{T}}$$
 (65)



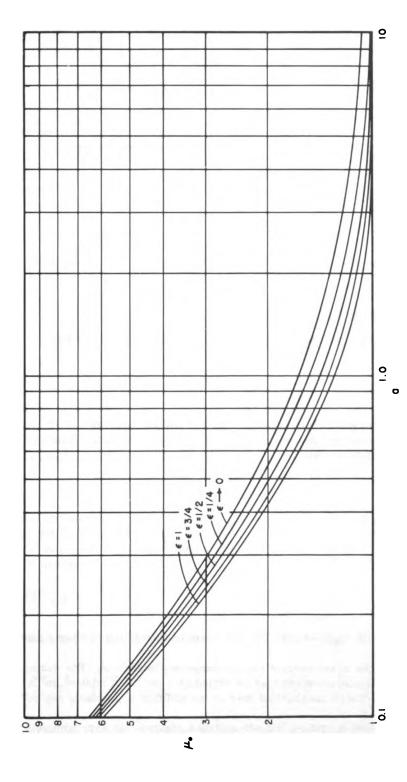


Fig. 1.6.20 -- Curves for Calculating the Effect of Foil Self-absorption and Doppler-broadening on Resonance Absorption. Reprinted from a personal communication from G. M. Roe at KAPL. For use of these curves see text following Eq. (54).

In terms of the bare two-group example previously considered, if one assumes that  $\delta T$  is independent of position, the reactivity change from these effects is given by (omitting the bar over the quantities):

$$\int \frac{\delta \mathbf{k}}{\delta \mathbf{T}} \, d\mathbf{V} = \frac{1}{\sigma_{\mathbf{f}} \mathbf{v}_{\mathbf{S}}} \frac{\partial}{\partial \mathbf{T}} \left( \sigma_{\mathbf{f}} \mathbf{v}_{\mathbf{S}} \right) - \frac{\sigma_{\mathbf{a}} \mathbf{v}_{\mathbf{S}}}{\mathbf{L}_{\mathbf{S}}} \frac{\frac{\partial}{\partial \mathbf{T}} \left( \sigma_{\mathbf{a}} \mathbf{v}_{\mathbf{S}} \right)}{\sigma_{\mathbf{a}} \mathbf{v}_{\mathbf{S}}} - \frac{\frac{\pi^{2}}{\mathbf{a}^{2}} \mathbf{D}_{\mathbf{f}} \mathbf{v}_{\mathbf{f}}}{\mathbf{L}_{\mathbf{f}}} \frac{\frac{\partial (\mathbf{D}_{\mathbf{S}} \mathbf{v}_{\mathbf{S}})}{\partial \mathbf{T}}}{\mathbf{D}_{\mathbf{s}} \mathbf{v}_{\mathbf{S}}}$$
(66)

In some cases, the last term on the right in Eq. (66) may be the major term. For  $\sigma_{SC}$  independent of energy, it contributes a negative temperature coefficient of:

$$-\int \frac{\partial \mathbf{k}}{\partial \mathbf{T}} \, d\mathbf{V} = \frac{\pi^2}{\mathbf{L_s}} \frac{\mathbf{D_s V_s}}{2\mathbf{T}} \tag{67}$$

which gives a coefficient of  $-10^{-4}$  per °C at room temperature if  $\frac{\frac{\pi^2}{a^2}D_gv_g}{L_g} = 0.06$ .

#### CONCENTRATION EFFECTS

The macroscopic cross section,  $\sigma_r$ , for any process, r, may be written as:

$$\sigma_{\mathbf{r}} = \sum_{i} \frac{\partial \sigma_{\mathbf{r}}}{\partial z_{\mathbf{i}}} \ z_{\mathbf{i}} \tag{68}$$

where  $z_i$  is the concentration (in any units) of the i'th nuclear species and  $\partial \sigma_r/\partial z_i$  is the microscopic cross section for process r in nuclear species i (in corresponding units). From this remark, it follows that:

$$\delta\sigma_{\mathbf{r}} = \sum_{i} \frac{\partial\sigma_{\mathbf{r}}}{\partial z_{i}} \delta z_{i} \tag{69}$$

or:

$$\frac{\delta \sigma_{\mathbf{r}}}{\sigma_{\mathbf{r}}} = \frac{\sum_{i} \left( \frac{\partial \sigma_{\mathbf{r}}}{\partial z_{i}} z_{i} \right) \frac{\delta z_{i}}{z_{i}}}{\sum_{i} \left( \frac{\partial \sigma_{\mathbf{r}}}{\partial z_{i}} z_{i} \right)}$$
(70)

Equation (69) or Eq. (70) together with Eq. (41) permits calculation of  $\delta k$  in a given situation.

Concentration changes in the reactor may be purposely introduced. For example, in a liquid reactor, the fuel concentration may be varied as a means of control, or in a water-moderated reactor, a control mechanism may be the addition of a soluble neutron absorber in the water.

In addition, in reactors operating at neutron fluxes greater than approximately  $10^{12}$  n/(cm²)(sec), the neutrons themselves introduce concentration changes. For the fuel concentration decreases and the fission product concentration increases as the reactor continues in operation.



Thus, if  $z_i(\underline{x},t)$  is the concentration of any stable nuclear species i not formed in fission, then owing to burn-up:

$$\frac{1}{z_i} \frac{\partial z_i}{\partial t} = -\int \int \frac{\partial \sigma_a}{\partial z_i} \mathbf{v} \, \mathbf{N} \, \frac{\mathbf{d}\underline{\omega}}{4\pi} \, \mathbf{dE} \tag{71}$$

so that:

$$\left[ \int \int \frac{\partial \sigma_{\mathbf{a}}}{\partial \mathbf{z}_{1}} \, \mathbf{v} \, \mathbf{N} \, \frac{\mathbf{d} \underline{\omega}}{\mathbf{4} \pi} \, \mathbf{dE} \right]^{-1} \tag{72}$$

is the mean life of a stable nucleus of type i at position  $\underline{x}$  at time t. In particular, Eq. (71) applies to the fissionable material concentration, provided that the reactor contains no fertile material.

If z_f is fuel concentration:

$$\int \delta z_{f} \frac{\delta k}{\delta z_{f}} dV = \frac{(W, f \frac{\delta J}{\delta z_{f}} \delta z_{f} N) - (W, \frac{\delta K}{\delta z_{f}} \delta z_{f} N)}{(W, fJN)}$$
(73)

where:

$$z_f \frac{\delta J}{\delta z_f} N = \int \int \nu(E) \sigma_f(E) \ vN \ dE \frac{d\omega}{4\pi} = JN$$
 (74)

and:

$$\frac{\delta K}{\delta z_f} N = \int \frac{\partial \sigma_a(E,\underline{x})}{\partial z_f} v N \frac{d\underline{\omega}}{4\pi}$$
 (75)

Early in the reactor's life, it is known that:

$$\delta \mathbf{z}_{\mathbf{f}} = \mathbf{AJN}$$
 (76)

where A is a constant proportional to the total energy produced by the reactor.

For the standard example introduced earlier (bare, spherical, two-group, thermal reactor), the influence of fuel burn-up may be evaluated as follows:

Define the average burn-up as:

$$\overline{\delta \mathbf{z_f}} = \frac{\int \delta \mathbf{z_f} d\mathbf{V}}{\mathbf{V}} < 0$$

Then, at least early in the reactor's life:

$$\overline{\delta z_f} = V \, \overline{\delta z_f} \, \frac{\sin \frac{\pi}{a} \, r}{r} / \int \frac{\sin \frac{\pi}{a} \, r}{r} \, dV \tag{77}$$

since, from Eq. (76), the concentration change has the same spatial dependence as neutron density. It is interesting to compare the reactivity change in this case with that for a uniform concentration change  $(\delta z_f)_u$ . From Eqs. (73), (74), and (75), it can be shown that:

$$\left(\delta k\right)_{\!u} = \frac{\left(\delta z_f\right)_{\!\!u}}{z_f} \left\{1 - f\frac{v_S\sigma_a}{L_S}\right\} = \frac{\delta M}{M} \left\{1 - f\frac{v_S\sigma_a}{L_S}\right\}$$

where f is the thermal utilization  $\sigma_{af}/\sigma_a$  and that if  $\delta z_f$  is not uniform it should be weighted with the square of the flux.* Thus:

$$\frac{\delta k}{\delta z_f} = \frac{(\delta k)_u}{(\delta z_f)_u} \frac{\sin^2 \frac{\pi r}{a} / r^2}{\int \frac{\sin^2 \pi r / a}{r^2} dV}$$
(78)

The reactivity change  $(\delta k)_B$  resulting from the distribution of depletion given by Eq. (77) is:

$$\delta k_{B} = \frac{\left(\delta k\right)_{u} \frac{\overline{\delta z_{f}}}{\left(\delta z_{f}\right)_{u}} \int \left(\frac{\sin \frac{\pi r}{a}}{r}\right)^{3} dV}{\int \frac{\sin \frac{\pi r}{a}}{r} dV \int \left(\frac{\sin \frac{\pi r}{a}}{r}\right)^{2} dV}$$

For the same total depletion:

$$\overline{\delta z_f} = (\delta z_f)_u$$

one finds:

$$\frac{\left(\delta \mathbf{k}\right)_{\mathbf{B}}}{\left(\delta \mathbf{k}\right)_{\mathbf{B}}} = \frac{2}{3\pi} \int_{0}^{\pi} \frac{\sin^{3}x}{x} \, \mathrm{d}x = 2 \tag{79}$$

so that the burned fuel has twice as much effect on the reactivity as an equal amount of uniform depletion. For a bare slab reactor, the 2 in Eq. (79) becomes  $\frac{4}{3}$ .

Another concentration effect of interest is that resulting from fission-product poisons. These may be considered as consisting of the Xe¹³⁵ chain, the Sm chain, and all the other poisons. The others may each be described approximately by the equation:†

$$\frac{\partial z_i}{\partial t} = + \gamma_i \iint \sigma_f v \, N \, \frac{d\omega}{4\pi} \, dE - z_i \iint \frac{\partial \sigma_a}{\partial z_i} v \, N \, \frac{d\omega}{4\pi} \, dE$$
 (80)

an equation which differs from Eq. (71) only by the source term. Here  $\gamma_i$  is the yield (nuclei per fission) of species i. This neglects the time necessary for the nuclei formed in fission to decay into stable (or long-lived) species i. Note that the equilibrium value of  $z_i$  may be obtained from Eq. (80) by setting  $\partial z_i/\partial t$  equal to zero. Further, in a ther-

^{*}All results based on Eq. (73) in this section are valid when the changes in concentration are not large enough to produce a major distortion of the flux pattern. Morehouse and Young¹¹ and Chernick¹² have treated exactly the case of a concentration change proportional to flux for bare slab and spherical reactors. In addition, Chernick treats a slab reactor with infinite reflector and cylindrical reactors and makes some comparisons with the flux-squared weighting discussed here.

[†]Here  $z_i$  has the same units as  $\int \int N \ dE \ d\omega/4\pi$ ; i.e., moles per unit volume or particles per unit volume.

mal reactor one obtains for the equilibrium (limiting) value of the ratio of poison cross-section from species  $z_i$  to fission cross section of the fuel:

$$\frac{\mathbf{z_i} \frac{\partial \sigma_2}{\partial \mathbf{z_i}} \mathbf{v}}{\overline{\sigma_i \mathbf{v}}} = \gamma_i \tag{81}$$

A table of fission-product yields is given in Chapter 1.2.

 $Xe^{135}$  poison has a direct fission yield,  $\gamma_x$ , which is approximately 5 percent of the yield formed via the decay chain:

The half-life of the  $T_e^{135}$  is so short that negligible error is incurred in assuming the iodine to be formed immediately. The equations then are:

$$\frac{\partial z_{I}}{\partial t} = \gamma_{I} \iint \sigma_{f} v \ N \frac{d\omega}{4\pi} \ dE - \lambda_{I} z_{I}$$

$$\lambda_{X} z_{X} + \frac{\partial z_{X}}{\partial t} = \lambda_{I} z_{I} + \gamma_{X} \iint \sigma_{f} v \ N \frac{d\omega}{4\pi} dE - z_{X} \iint \frac{\partial \sigma_{a}}{\partial z_{X}} v \ N \frac{d\omega}{4\pi} dE$$
(82)

where the loss of I by absorption of neutrons has been neglected.

As is clear from Eq. (82), the equilibrium  $X_e$  cross section is a function of the power level of the reactor. For a thermal reactor, one finds for equilibrium (or limiting) ratio of Xe cross section to the fuel thermal-absorption cross section at a given flux:

$$P \simeq \frac{z_{x} \frac{\partial \sigma_{a}}{\partial z_{x}} v}{\sigma_{a} v} = \frac{n}{\nu} (\gamma_{I} + \gamma_{x}) \frac{\frac{\partial \sigma_{a} v}{\partial z_{x}} \int N_{th} \frac{d\underline{\omega}}{4\pi}}{\lambda_{x} + \frac{\partial \sigma_{a} v}{\partial z_{x}} \int N_{th} \frac{d\underline{\omega}}{4\pi}}$$

$$= (\eta/\nu)(\gamma_{I} + \gamma_{x}) \frac{\phi}{\phi + w}$$
(83)

where  $\eta/\nu$  is the ratio of the thermal-fission cross section to the thermal-absorption cross section for the fuel.  $\int N_{th} d\omega/4\pi$  is the thermal-neutron density and  $\phi = \int \nabla N_{th} d\omega/4\pi$  is the thermal flux. w is defined as:

$$\mathbf{w} = \frac{\lambda_{\mathbf{x}}}{\frac{1}{\mathbf{v}}} \frac{\partial \sigma_{\mathbf{a}} \mathbf{v}}{\partial \mathbf{z}_{\mathbf{x}}} \tag{84}$$

In Fig. 1.6.21, P is plotted vs  $\phi$ . Clearly:

$$\int \frac{\delta \mathbf{k}}{\delta \mathbf{z_x}} \, \delta \mathbf{z_x} d\mathbf{V} = -\frac{(\mathbf{W_{th}}, \, \overline{\sigma_{af} \mathbf{v}} \, \mathbf{P} \, \mathbf{N_{th}})}{(\mathbf{W}, \mathbf{KN})}$$

$$= -\overline{\mathbf{P}} \, \frac{(\mathbf{W_{th}}, \, \overline{\sigma_{af} \mathbf{v}} \, \mathbf{N_{th}})}{(\mathbf{W}, \mathbf{KN})}$$
(85)

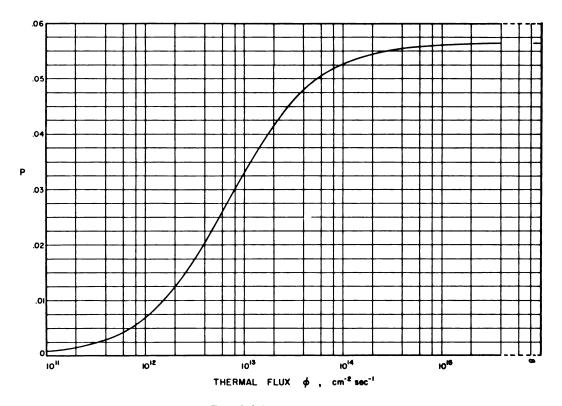


Fig. 1.6.21 —  $P(\phi)$  for Xenon.

which defines  $\overline{P}$ , the uniform poison cross-section to fuel absorption-cross-section ratio which gives the same effect on reactivity as the true ratio P.

A result equivalent to Eq. (79) for Xe¹² is more difficult to obtain. Using:

$$\phi = \phi_{\text{max}} \frac{\sin \pi r/a}{\pi r/a} \tag{86}$$

one obtains  $\overline{P}$  for the standard reactor model introduced earlier from Eqs. (85) and (83):

$$\overline{P} = \frac{\frac{\eta}{\nu} (\gamma_{I} + \gamma_{X}) \frac{a}{\pi} \int \left(\frac{\sin \pi r/a}{r}\right)^{3} \frac{1}{\frac{w}{\phi_{\max}} + \frac{\sin \pi r/a}{\pi r/a}} dV}{\int \left(\frac{\sin \pi r/a}{r}\right)^{2} dV}$$
(87)

For a bare cylinder a good approximation to  $\overline{P}$  is:

$$\overline{P} = (\eta/\nu) \left(\gamma_{I} + \gamma_{x}\right) \frac{1}{1 + 1.7 \frac{W}{\phi_{\text{max}}}}$$
(88)

As before,  $\overline{P}$   $\overline{\sigma_{af}v}$  is the cross section,  $\overline{\sigma_{a}v}$ , of a poison uniformly distributed in the reactor which produces the same reactivity effect as the actual non-uniform poison.

In this model, the reactivity changes caused by the addition of a uniform absorption cross section,  $\delta\sigma_2$ , are given by:

$$\delta \mathbf{k} = -\frac{\delta \sigma_{\mathbf{a}}}{\sigma_{\mathbf{a}}} \frac{\sigma_{\mathbf{a}} \mathbf{v}_{\mathbf{S}}}{\mathbf{L}_{\mathbf{S}}} = -\frac{\delta \sigma_{\mathbf{a}}}{\sigma_{\mathbf{a}\mathbf{f}}} \mathbf{f} \frac{\sigma_{\mathbf{a}} \mathbf{v}_{\mathbf{S}}}{\mathbf{L}_{\mathbf{S}}}$$
(89)

where  $f = \sigma_{af}/\sigma_a$  is the thermal utilization and  $\sigma_{av_s}/L_s$  is the fraction of thermal neutrons absorbed in the reactor.

When fission products have a small enough cross section (or if it is early enough in the reactor life) so that the burn-up term (the second term on the right) in Eq. (80) can be neglected, then the poison cross section is proportional to  $\phi$  and Eq. (79) is valid.*

The equations for samarium differ from those of xenon because the samarium isotope with the large thermal cross section (Sm¹⁴⁹) is stable. It is produced via the decay chain:†

The fission yield of Pm¹⁴⁹ and the thermal cross section of Sm¹⁴⁹ are given in Table 1.2.7. Equation (80) describes the concentration of Sm¹⁴⁹ and the first Eq. (82) is valid for Pm¹⁴⁹, if all quantities with the subscripts I are interpreted to refer to Pm¹⁴⁹.

## FLOWING FUEL EFFECTS13,14

In a circulating-fuel reactor, some delayed neutrons are born outside the reactor where they are lost. This results in an effective decrease in  $\nu$ , the number of neutrons per fis-fion, and in the  $\beta_i$  and  $\lambda_i$ . For a reactor in which the circulation time is small compared with the delayed lifetimes, one can obtain the resultant changes in the  $\beta_i$ . Thus, let  $\mu$  be the fraction of time spent by fuel in the reactor. Then the probability that a delayed neutron will be born in the reactor is  $\mu$ , so that the effective value of  $\beta_i$ ,  $\beta_i$ , is given by:

$$\overline{\beta_i} = \mu \beta_i \tag{90}$$

The corresponding effective number of neutrons per fission,  $\bar{\nu}$ , becomes:

$$\overline{\nu} = \nu (1 - \beta) + \nu \overline{\beta} = \nu [1 - (1 - \mu)\beta] \tag{91}$$

The  $\lambda_i$  are not affected in this case.

For the case where the circulation time is of the order of or longer than the delayedneutron mean lives, the detailed flow pattern of the fuel within the reactor and external loop is significant.

# FORMULATION OF DYNAMIC EQUATIONS

The neutron behavior of the nuclear reactor is completely specified by Eq. (1) for which (with s = 0):

$$\frac{d\mathbf{n}}{dt} = \frac{\mathbf{k} - 1 - \mathbf{k} \epsilon \boldsymbol{\beta}}{1} \mathbf{n} + \sum_{i} \lambda_{i} \mathbf{c}_{i}$$

$$\frac{d\mathbf{c}_{i}}{dt} = -\lambda_{i} \mathbf{c}_{i} + \frac{\mathbf{k} \epsilon_{i} \boldsymbol{\beta}_{i}}{1} \mathbf{n}$$
(92)

Digitized by Google 569

^{*}See footnote preceding Eq. (78).

[†] Precursors of Pm 149 with half-lives much less than 47 hours have been omitted.

These equations give n(t) for specified k(t); that is, they define the functional  $n\{k(t)\}$ . Complete solution of the problem requires equations which permit determination of that k(t) produced by the remainder of the system for n specified over past times. That is, equations to define the functional  $k\{n(t)\}$  are needed.

Part of this problem has been considered previously in the calculation of  $k\{T,\rho\}$ . The remainder of the problem is to find  $T,\rho$  given the heat source corresponding to n(t). Clearly, it is just this part of the problem which is (1) familiar in engineering and independent of neutron physics and (2) special to the individual reactor system and intractable to detailed general discussion.

The relation between n(t) and heat is discussed below where some specific, simple examples are considered. General considerations concerning the form of  $k\{n\}$  are given in the discussion of linearized equations. For a linear external system, as is often the case:

$$\mathbf{k}\{\mathbf{n}\} = \int_{-\mathbf{n}}^{\mathbf{t}} \mathbf{K}(\mathbf{t} - \mathbf{s})\mathbf{n}(\mathbf{s})\mathbf{d}\mathbf{s} + \delta\mathbf{k}(\mathbf{t}) + \mathbf{k}_{\mathbf{0}}$$
(93)

where  $\delta k(t)$  is an external forcing term. Equation (93), if valid, defines K(t-s). The stability of systems where Eq. (93) holds has been discussed by Welton. ¹⁵

#### THE REACTOR AS A HEAT SOURCE

The energy released by the fission process may be the prime purpose of the reactor, or it may be an undesired by-product. The energy distribution in kinetic energy of fission fragments and neutrons, prompt and delayed gammas, beta particles, and the like is shown in Table 1.2.11. Fission-product and beta-particle energy may be considered as a heat source at the position of the fuel. The neutron energy mainly appears as heating of the moderator, although some energy leaks out with escaping neutrons. The gamma-energy distribution is rather difficult to calculate, since the range of gamma rays is rather large. Heating by gamma rays or other particles emitted upon neutron absorption in the moderator or structure may also be important. Generally, however, for a bare homogeneous reactor, the energy production is distributed to a very good approximation as the fission source.

The presence of an energy source disturbs the temperature and density of the various parts of the reactor and produces reactivity changes as indicated in the discussion of reactivity coefficients. For a reactor with lump fuel, the major heat source is in the fuel, which will often operate at a higher temperature than the moderator. Since the moderator also has a heat source within it (gammas, neutrons slowing down, neutron capture), the power and cooling affect moderator properties and, through them, the reactivity. Furthermore, the coolant may have a marked effect on reactivity, especially in a water-cooled reactor.

The heat source density is:

$$\mathbf{P} = \mathbf{Q} \int \int \sigma_{\mathbf{f}} \, \mathbf{v} \mathbf{N} \, \frac{\mathrm{d}\omega}{4\pi} \, \mathrm{d}\mathbf{E} \tag{94}$$

where Q is the energy release per fission. Equation (94) gives the spatial distribution of that part of the fission energy appearing as kinetic energy of the fission fragments.

In the light of previous considerations [cf. Eqs. (1) and (5)], the space-independent, one-group, equivalent power may be taken as:

$$p = q \frac{kn}{l_{\nu}} \tag{95}$$



#### POWER COEFFICIENTS

A steady-state solution  $(dn/dt = dc_i/dt = 0)$  of Eq. (92) can exist only if k = 1. This implies operation at  $n(t) = n^0$ , where  $n^0$  is such that:

$$\mathbf{k}\{\mathbf{n}^{\mathbf{0}}\} = \mathbf{1} \tag{96}$$

Furthermore, if various time-independent values of n are considered,  $k\{n\}$  is a function in the ordinary sense of the variable n. The power coefficient of reactivity is defined as:

$$\mathbf{k_{n^0}} = \mathbf{n} \frac{\mathbf{d}}{\mathbf{dn}} \mathbf{k} \{ \mathbf{n} \} \bigg|_{\mathbf{n} = \mathbf{n^0}}$$
 (97)

If  $k \{n\}$  can be considered as a linear function of n, then:

$$k\{n\} = 1 + k_{n0} \frac{n - n^{0}}{n^{0}}$$
(98)

Thus, in this case:

$$\mathbf{k}\{2\mathbf{n}^{0}\}-1=\mathbf{k}_{\mathbf{n}^{0}}\tag{99}$$

That is, the power coefficient of reactivity is the reactivity change produced by doubling the neutron level in the reactor (keeping it at the new value by control-rod motion or other means which does not affect the part of the functional  $k\{n\}$  under consideration).

In any case, for the reactor system to be statically stable, it is necessary that:

$$k_{n^0} < 0$$
 (100)

The more negative  $k_n^0$ , the more stable the system. This static stability does not assure dynamic stability, but it is necessary to have dynamic stability. If Eq. (98) holds  $(k\{n\}a)$  linear functional), then  $k_{n0}$  becomes more negative as  $n^0$  increases; high-power operation leads, therefore, in a statically stable system, to greater static stability.

If Eq. (93) holds, then for constant n:

$$k\{n\} = k_0 + n \int_0^\infty K(t)dt$$

so that:

$$n^{0} = \frac{1 - k_{0}}{\int_{0}^{\infty} Kdt}$$
 (101)

$$k_n o = 1 - k_0$$

If the reactor is coupled to several independent external systems, such as a servo-operated control and the temperature-density system, the resultant partial power-coefficients may be added to obtain the resultant coefficient. A further remark is that a servo yielding integral control may be arranged to always restore the level to a predetermined  $n^0$ , independent of external variations. This implies that  $k_{n^0} = -\infty$ . Such controls are possible (cf. remarks on "Control Servomechanisms" below).

#### LINEARIZATION

For small departures of the various reactor-system variables from equilibrium values, it is possible to simplify the equations by considering the <u>tangent system</u>. This system is that of all linear systems which most closely approximates, in the neighborhood of the equilibrium point, the true system. Methods of obtaining the equations of motion of the tangent system will be discussed below under linearized equations.

The non-linearity of the equations of reactor dynamics may occur in  $k\{n\}$ . For the tangent system, however, one may always write  $k\{n\}$  in the form of Eq. (93). This nearly always yields a good approximation for a fairly wide range of operating conditions.

Even though  $k\{n\}$  is linearized, the equations are non-linear owing to the manner in which k enters Eq. (92). Specifically, the terms containing the factor kn must be approximated

If  $n = n^0 + n'$  where  $n^0$ , the equilibrium neutron inventory, is independent of time and:

$$n' << n^{\emptyset} \tag{102}$$

then one may linearize the kn term as follows. From Eq. (93):

$$\mathbf{k} \big\{ \mathbf{n^0} + \mathbf{n'} \big\} = \mathbf{n^0} \int_{-\infty}^t \mathbf{K}(\mathbf{t-s}) d\mathbf{s} + \mathbf{k_0} + \int_{-\infty}^t \mathbf{K}(\mathbf{t-s}) \ \mathbf{n'(s)} d\mathbf{s}$$

but:

 $k\{n^0\} = 1$ , since  $n^0$  is an equilibrium value, so:

$$k\{n^0 + n'\} = 1 + \int_{-\infty}^{t} K(t - s)n'(s)ds$$
 (103)

Then:

$$kn = n^{0} + n^{0} \int_{-\infty}^{t} K(t - s)n'(s)ds + n'(t) + n'(t) \int_{-\infty}^{t} K(t - s)n'(s)ds$$
 (104)

The process of linearization consists in neglecting the last term on the right in Eq. (104) by assuming that it is small compared with the other terms since it contains  $n'^2$ . This assumption becomes more valid when one notes that usually:

$$n^{0} \int_{-\infty}^{\tau} K(t-s) ds$$
 (105)

is of the order of  $\beta$ , which is small compared with unity.

If term (105) is sufficiently small in such terms of Eq. (92) as  $(k\epsilon\beta/l)n$  and  $(k\epsilon_i\beta_i/l)n$ , one may write:

$$kn \simeq n^0 + n'(t) = n \tag{106}$$

In the term (k-1)n/l, more care must be used, as is clear from Eq. (106). Thus, one uses:

$$(k-1) n \simeq n^0 \int_{-\infty}^{t} K(t-s)n'(s)ds$$
 (107)

From Eq. (106) and (107), with:

$$c_i(t) = c_i^0 + c_i'(t)$$
 (108)

one obtains the steady-state equations:

$$0 = \frac{\epsilon_{i}\beta_{i}}{l} \mathbf{n}^{0} + \sum_{i} \lambda_{i} \mathbf{c}^{0}_{i}$$

$$0 = -\lambda_{i}\mathbf{c}^{0}_{i} + \frac{\epsilon_{i}\beta_{i}}{l} \mathbf{n}^{0}$$
(109)

and the linearized equations:

$$\frac{d\mathbf{n}'}{dt} = \frac{\mathbf{n}^{\mathbf{0}}}{1} \int_{-\infty}^{t} \mathbf{K}(\mathbf{t} - \mathbf{s})\mathbf{n}'(\mathbf{s})d\mathbf{s} + \sum \lambda_{i} \mathbf{c}'_{i}$$

$$\frac{d\mathbf{c}'_{i}}{dt} = -\lambda_{i} \mathbf{c}'_{i} + \frac{\epsilon_{i} \beta_{i}}{1} \mathbf{n}'$$
(110)

Further discussion of Eq. (110) is deferred until the discussion, "Form and Solution of Linearized Equations."

#### A SIMPLE COOLING MODEL

Consider a reactor consisting of very fine fuel rods immersed in a well stirred tank of water with water flow supplying the cooling. Then, the water temperature will satisfy an equation such as (neglecting the difference between prompt and delayed heating):

$$MC\frac{dT}{dt} = q\frac{kn}{l\nu} - g C(T - T_{in})$$
(111)

where:

C is the heat capacity per unit mass of the water

M is the total mass of water in the tank

T is the water temperature

 $q(kn/l\nu)$  is the power into the water (it is assumed no holdup occurs in the fuel rods) g is the mass water flow rate through the tank.

Furthermore, the reactivity change will be of the form:

$$\mathbf{k} - \mathbf{1} = \mathbf{C}_{\mathbf{T}}(\mathbf{T} - \mathbf{T}_{\mathbf{0}}) \tag{112}$$

where:

 $C_T$  is the temperature coefficient of reactivity, direct and through the density changes  $T_0$  is the temperature for which k = 1.

Equations (92), (111), and (112) describe the dynamic behavior of the model discussed. They further may be used to describe a solid reactor cooled via coolant channels. In such a case, T is an average reactor temperature, and the term  $gC(T-T_{in})$  is interpreted as the average heat carried away by the coolant. Equation (111) is adequate in this case only if the transit time of the coolant through the reactor is small.

If the coolant is passed through a heat exchanger and back into the reactor, one may append to Eqs. (111) and (112) a further relation for the variation of  $T_{in}$ :

$$\mathbf{T}_{in}(t) = \alpha \mathbf{T}(t - \tau) + \beta; \ 0 < \alpha < 1 \tag{113}$$

The delay time  $\tau$  due to passage through the heat exchanger loop is called a "transport delay."

## SOLUTIONS OF NON-LINEAR EQUATIONS

The solution of non-linear equations is a tedious job, usually carried out numerically. Specific examples for simplified models are given below.

#### A SIMPLE COOLING MODEL

Consider a reactor coupled to the external system in such a way that a constant amount of power is removed. In this case, one may write, approximately:

$$C\frac{dT}{dt} = \alpha n - P_0$$
 (114)  
 $k - 1 = C_T(T - T_0); C_T < 0$ 

where C is the heat capacity of the reactor and Po the cooling rate, whence:

$$\frac{dk}{dt} = \frac{C_T}{C}(\alpha n - P_0) \tag{115}$$

If one further neglects  $(1/\epsilon\beta)$  dn/dt and considers only one delay group, Eq. (29) results for the neutron equation. Setting s=0 and eliminating c, one obtains [in analogy with Eq. (29)]:

$$[k(1-\beta)-1]\frac{dn}{dt} + (1-\beta)n\frac{dk}{dt} + \lambda(k-1)n = 0$$
 (116)

which together with Eq. (115) completely specifies the dynamic problem. A numerical solution may be obtained if one first eliminates the time by use of:

$$\frac{d}{dt} = \frac{dk}{dt} \frac{d}{dk}$$

Numerical solutions are given in Fig. 1.6.22 for:

$$\frac{\mathbf{C_T} \, \mathbf{P_0}}{\lambda \mathbf{C} \beta} = \mathbf{0.05}$$

This means that the reactivity increases owing to cooling by  $0.05\beta$  in a delay period ( $\lambda^{-1}$ ).

#### ACCIDENT CONSIDERATIONS

If a control rod is suddenly moved so that an excess reactivity large compared with  $\beta$  results, the behavior of the reactor for some time will be uninfluenced by the delayed neutrons. In this case, Eq. (1) may be written as:

$$\frac{\mathrm{dn}}{\mathrm{dt}} = \frac{\mathrm{k} - 1 - \beta}{1} \, \mathrm{n} \tag{117}$$

If Eq. (117) is considered in conjunction with equations describing temperature effects, one has a model to be studied for short time changes after sudden reactivity increase. In addition to Eq. (117), Ref. (17) considers Eq. (114) but with:

$$\mathbf{P_0} = \mu \mathbf{T} \tag{118}$$

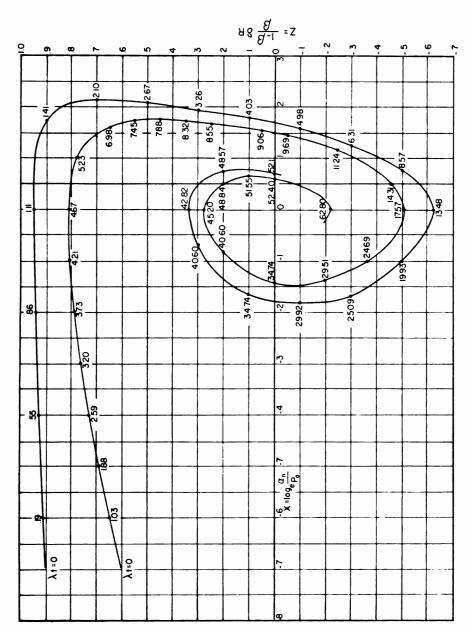


Fig. 1.6.22 — Reactivity vs Reactor Power for a Simple Cooling Model. Submitted by Nuclear Development Associates, Inc., Dec. 15, 1952. The curves are labelled with the time measured such that the reactivity would increase by one dollar in 20 delayed neutron mean lives if there in units of the mean life of delayed neutrons. The calculations assume a rate of heat removal were no heating  $(\alpha n = 0)$ .

Equations (117) and (118) together may be written in dimensionless form depending on one parameter as:

$$\frac{d^2\theta}{d\tau^2} + (c-1)\frac{d\theta}{d\tau} - c\theta = -\left(\theta\frac{d\theta}{d\tau} + c\theta^2\right)$$
 (119)

where:

$$\theta = \frac{T}{T_0 + \frac{1}{-C_T}}$$

$$\tau = \frac{1 - C_T T_0}{1} t$$

$$c = \frac{\mu}{C} \frac{1}{1 - C_T T_0}$$

A solution of Eq. (119) with c = 1 is given in Fig. 1.6.23.

Equations (114) and (119) with  $P_0 = 0$  are a special case¹⁸ of the more general system where Eq. (114) is replaced by:

$$\frac{d^{n}(\kappa - 1 - \beta)}{dt^{n}} = -\frac{\left[\int \frac{n}{n_{0}} dt\right]^{m}}{t_{0}^{n+m}}$$
(120)

which depends on one arbitrary constant,  $n_0^m t_0^{m+1}$ . Equation (114) corresponds to n=0, m=1. To discuss Eqs. (117) and (120), new variables may be introduced:

$$\mathbf{A} = \frac{\mathbf{k} - \mathbf{1} - \boldsymbol{\beta}}{\mathbf{k_0} - \mathbf{1} - \boldsymbol{\beta}}$$

$$\eta = \frac{n}{n_0 \left(\frac{t_0}{\tau}\right)^{1+(n/m)} (k_0 - 1 - \beta)^{1+(1+n/m)}}$$
(121)

$$\theta = \frac{t}{1} (k_0 - 1 - \beta)$$

In terms of these variables:

$$\frac{d}{d\theta} \log_{\theta} \eta = A$$

$$\frac{d^{n}A}{d\theta^{n}} = -\left(\int \eta d \theta\right)^{m}$$
(122)

with initial conditions:

$$A = 1 
 \eta \cong 0$$
 at t = 0

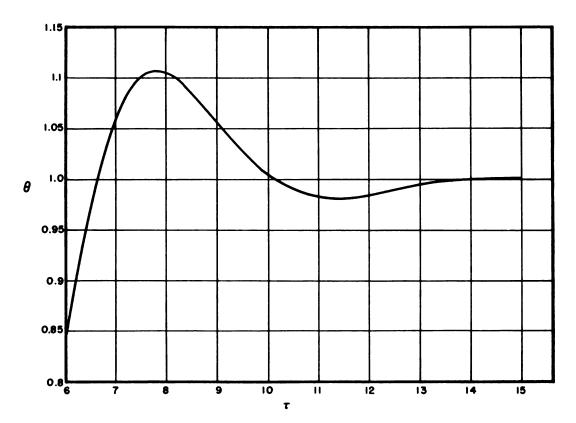


Fig. 1.6.23—Temperature vs Time for Cooling Proportional to Temperature. Reprinted from BNL-113, Aug. 1951.  $\theta$  is a dimensionless temperature and  $\tau$  a dimensionless time, cf. Eq. (119). The initial conditions were  $\theta$  = 0;  $\dot{\theta}$  = 0.01; initial reactor period (at  $\tau$  = 0) equal to the thermal relaxation time.

Total energy generated is proportional to:

$$Q = \int_0^{\infty} \eta d\theta$$
 (123)

Plots of  $\eta$  vs A for various values of n and m are given in Figs. 1.6.24 and 1.6.25. Values of Q [Eq. (123)] are marked on the curves.

For the most interesting case, n = 0, m = 1, one may state an accident theorem originally given by Nordheim. Reference to Fig. 1.6.24 shows that, for this case, the final value of A is -1; i.e., the final reactivity is as much below prompt critical as the initial was above prompt critical, or the final temperature is as much above the temperature at which  $k = 1 + \beta$  as the initial temperature was below this value.

An extension to this theorem which considers delayed neutrons  20  shows that with no cooling the final reactivity including delayed neutrons is as much below delayed critical as the initial is above delayed critical. Thus, the final reactivity is  $1-(k_0-1)=2-k_0$ , and the final temperature is as much above the temperature at which k=1 as the initial temperature is below this value.

Hurwitz²⁰ discusses a variation of the second of Eq. (122), which is written as follows:

$$\frac{d^{n}A}{d\theta^{n}} = 0 \qquad Q \leq Q_{0}$$

$$= -(Q^{m} - Q_{0}^{m}) \qquad Q > Q_{0}$$

$$Q = \int_{0}^{\theta} \eta d\theta'$$
(124)

Curves are given in the reference.

### FORM AND SOLUTION OF LINEARIZED EQUATIONS

The usefulness of studying the linearized equations, the tangent system, is a result of their much greater simplicity. The validity of such solutions is limited only by the degree of their departure from equilibrium. Stability of an equilibrium configuration means stability of the tangent system; therefore, the tangent system is most used in studying questions of stability. The process of finding the tangent system may be stated as follows.

First, an equilibrium state of the system is found by solving the non-linear equations with all time derivatives set equal to zero. The corresponding value of a dependent variable, x, is written  $x^0$ . Thus for small oscillations about the equilibrium configuration, one may write x as a steady-state part,  $x^0$ , plus an oscillating part,  $x^1$ :

$$x(t) = x^0 + x^1(t) ag{125}$$

where:*

$$|\mathbf{x}^1(\mathbf{t})| \ll |\mathbf{x}^0| \tag{126}$$

The substitution indicated in Eq. (126) is made in the equations of motion. Terms containing only quantities with superscript zero drop out because of the conditions for equilibrium. If terms containing products of first-order quantities (e.g.,  $x^1$   $y^1$ ) are neglected, then the resulting linear equations describe the tangent system.

^{*} If the system is stable, x⁽¹⁾ is bounded. Then the disturbance introduced can always be made small enough so that Eq. (126) is satisfied.

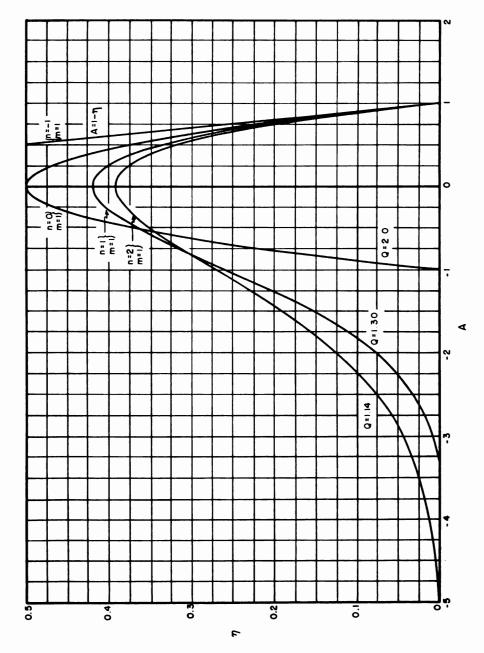


Fig. 1.6.24 — Solution to an Accident Problem with No Cooling. Reprinted from KAPL-565. A is proportional to the excess reactivity, and  $\eta$  is proportional to the neutron density. The  $n^{th}$  derivative of the reactivity is taken proportional to the  $m^{th}$  power of the time integral of the neutron density. See Eq. (120) et seq in the text.

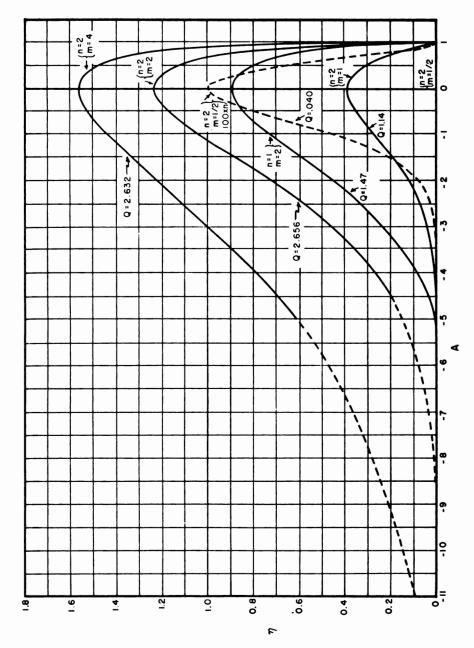


Fig. 1.6.25 -- Solution to an Accident Problem with No Cooling. Reprinted from KAPL-565. A is proportional to the excess reactivity, and  $\eta$  is proportional to the neutron density. The nth derivative of the reactivity is taken proportional to the mth power of the time integral of the neutron density. See Eq. (120) et seq in the text.

An example of this process was given earlier under "Formulation of the Dynamic Equations." Further examples follow:

$$\mathbf{x} = \mathbf{x}^0 + \mathbf{x}^1$$

$$f(x) = f(x^0) + \left(\frac{df}{dx}\right)^0 x^1 \dagger$$

$$f(\mathbf{x},\mathbf{y}) = f(\mathbf{x}^{\mathbf{0}},\mathbf{y}^{\mathbf{0}}) + \left(\frac{\partial f}{\partial \mathbf{x}}\right)^{\mathbf{0}} \mathbf{x}^{1} + \left(\frac{\partial f}{\partial \mathbf{y}}\right)^{\mathbf{0}} \mathbf{y}^{1}$$
(127)

$$\frac{dx}{dt} = \frac{dx^1}{dt}$$

$$xy = x^0y^0 + x^0y^1 + y^0x^1$$

$$\frac{x}{y} = \frac{x^0}{y^0} + \frac{x^1}{y_0} - \frac{x^0}{(y^0)^2}$$
 y¹, etc.

## LAPLACE TRANSFORMS AND TRANSFER FUNCTIONS

The linearized kinetic equations were found earlier. They are, adding a  $\delta k(t)$  forcing term:

$$\frac{d\mathbf{n}^{1}}{dt} = \frac{\mathbf{n}^{0}}{1} \int_{-\infty}^{t} \mathbf{K}(t - \mathbf{s}) \mathbf{n}^{1}(\mathbf{s}) d\mathbf{s} + \sum_{i} \lambda_{i} c_{i}^{1} - \frac{\epsilon \beta}{1} \mathbf{n}^{1} + \frac{\mathbf{n}^{0}}{1} \delta \mathbf{k}(t)$$
(128)

$$\frac{dc_{i}^{1}}{dt} = -\lambda_{i}c_{i}^{1} + \frac{\epsilon_{i}\beta_{i}}{1} n^{1}$$

Here, K(t) is defined by the linearized equation:

$$\mathbf{k}^1 = \mathbf{k}(t) - 1 = \int_{-\infty}^{t} \mathbf{K}(t - \mathbf{s}) \, \mathbf{n}^1(\mathbf{s}) d\mathbf{s}$$
 (129)

Further, the power coefficient of reactivity corresponding to K is given, as before, by:

$$\mathbf{k}_{\mathbf{n}^0} = \mathbf{n}^0 \int_0^{\infty} \mathbf{K}(\mathbf{t}) d\mathbf{t} \tag{130}$$

These equations lend themselves to convenient handling with the method of Laplace transforms. The basic transform theorem is the following:

If:

$$\bar{f}(p) = \int_0^{\infty} e^{-pt} f(t) dt$$
 (131)

Then, for t > 0:

$$f(t) = \frac{1}{2\pi i} \int_{c-i\infty}^{c+i\infty} e^{pt} \bar{f}(p)dp$$

$$\left(\frac{\mathrm{df}}{\mathrm{dx}}\right)^0 = \frac{\mathrm{df}}{\mathrm{dx}}\Big|_{x=x_0}$$



[†] The superscript o always means evaluated for the equilibrium values of the variables. Thus:

and, for t < 0:

$$\frac{1}{2\pi i} \int_{c-i\infty}^{c+i\infty} e^{pt} \bar{f}(p) dp = 0$$

where the contour is such that all poles of  $\bar{f}(p)$  lie to its left.  $\bar{f}(p)$  is called the Laplace transform of f(t).

Further results are:

$$\int_0^{\infty} e^{-pt} \frac{df(t)}{dt} dt = p\bar{f}(p) - f(0)$$
 (132)

and:

$$\int_0^{\infty} e^{-pt} \int_0^t K(t-s) n^1(s) ds dt = \overline{K}(p) \overline{n^1}(p)$$

$$\int_0^{\infty} K(t) dt = \overline{K}(0)$$
(133)

One may use these results to find a solution of Eq. (128). Thus, suppose that:

$$\begin{cases}
\delta k(t) = 0 \\
n^{1}(t) = 0 \\
c_{1}^{1}(t) = 0
\end{cases}$$
for  $t < 0$ 
(134)

i.e., that the reactor was in equilibrium for negative times. The behavior of the system for t > 0 as forced by  $\delta k(t)$  may then be found. Thus, if Eq. (128) is multiplied by  $e^{-pt}$  and integrated, one finds with the aid of Eqs. (132) and (133):

$$\overline{pn^{1}} = \sum_{i} \lambda_{i} \overline{c_{i}^{1}} - \frac{\epsilon \beta}{1} \overline{n^{1}} + \frac{n^{0}}{1} (\overline{k^{1}} + \overline{\delta k})$$

$$\overline{pc_{i}^{1}} = -\lambda_{i} \overline{c_{i}^{1}} + \frac{\epsilon_{i} \beta_{i}}{1} \overline{n^{1}}$$

$$\overline{k^{1}} = \overline{K} \overline{n^{1}}$$

Elimination of the  $\overline{c_1}$  yields the pair of equations:

$$\overline{\mathbf{n}^{1}} = \frac{\mathbf{n}^{0}\overline{\mathbf{F}}(\mathbf{p})}{\epsilon \beta} \left( \overline{\mathbf{k}^{1}} + \overline{\delta \mathbf{k}} \right) 
\overline{\mathbf{k}^{1}} = \overline{\mathbf{K}}(\mathbf{p})\overline{\mathbf{n}^{1}}$$
(135)

where:

$$\left[\overline{\mathbf{F}}\ (\mathbf{p})\right]^{-1} = \left\{\frac{\mathbf{l}\mathbf{p}}{\epsilon\beta} + 1 - \sum_{i} \frac{\lambda_{i}}{\lambda_{i} + \mathbf{p}} \frac{\epsilon_{i}\beta_{i}}{\epsilon\beta}\right\} \tag{136}$$

Equation (135) suggests an amplifier with feedback. This suggests calling  $\overline{F}(p)$  the reactor transfer function and  $\overline{K}(p)$  the external-system transfer function.



Upon eliminating  $\overline{k^1}$  in Eq. (135), one has:

$$\overline{\mathbf{n}^{1}} = \frac{\mathbf{n}^{0}/\epsilon\beta}{\overline{\mathbf{F}}^{-1} - \frac{\mathbf{n}^{0}\overline{\mathbf{K}}}{\epsilon\beta}} \overline{\mathbf{\delta}}\overline{\mathbf{k}}$$
(137)

This equation may be considered the basic formula of reactor dynamics. The properties of  $\overline{F}^{-1}$ , which are of interest in applications, are easily seen from Eq. (136) and from the plot of  $lp/\epsilon\beta - \overline{F}^{-1}(p)$  in Figs. 1.6.4 through 1.6.10 and in Fig. 1.6.26.

Equation (137), together with the equation following Eq. (131) yields the solution to the equations of motion for  $n^1(t)$ . This solution will consist of the sums of residues of  $\overline{n^1}$  e^{pt} at the various zeroes of the denominator of Eq. (137) and the poles of  $\overline{\delta k}$ .

If the singularities of n¹(p) are all simple poles, then the solution of Eq. (128) is:

$$n^{1}(t) = \frac{1}{2\pi i} \int_{c-i}^{c+i^{\infty}} e^{pt} \overline{n^{1}}(p) dp$$

$$= \sum_{i} e^{p_{i}t} \frac{d}{dp} \left( \frac{1}{\overline{n^{1}}(p)} \right) | p = p_{i}$$
(138)

When  $\overline{n^1}(p)$  has singularities which are not simple poles, the reader should consult a standard text on Laplace transforms.

The values of  $p_i$  for the zeroes of the denominator of Eq. (137) tell one about the stability of the system. Equation (138) shows that if any root has a positive real part the system is unstable while if all the roots have negative real parts, the system is stable.

### THE FORM OF $\overline{K}(p)$

As the above considerations indicate, the characteristics of the external system are completely specified by the single function  $\overline{K}(p)$ , the external-loop transfer function. This function is additive for independent external loops as, for example, Xe burnup, temperature effects, flux dependent control actuation, and the like. It is thus useful to indicate the form of  $\overline{K}$  for some simple cases. In actual systems, ²¹ the transfer function can become very complicated.

The cooling model discussed earlier will serve to indicate a form of temperature-coefficient contribution to the transfer function. The linearized forms of Eqs. (111), (112), and (113) are:

**M** C 
$$\frac{dT^1}{dt} = \frac{q}{l\nu} n^1 - gC(T^1 - T^1_{in})$$

$$\mathbf{k^1} = \mathbf{C_T} \mathbf{T^1}$$

$$T_{in}^{1}(t) = \alpha T^{1}(t - \tau)$$

Taking transforms, one finds with the aid of the second of Eqs. (135):

$$\mathbf{K}(\mathbf{p}) = \frac{\frac{\mathbf{q}}{1\nu} \mathbf{C}_{\mathrm{T}}}{\mathbf{M} \mathbf{C} \mathbf{p} + \mathbf{g} \mathbf{C} (1 - \alpha \mathbf{e}^{-\mathbf{p} \tau})}$$
(139)



REACTOR PHYSICS **CHAP. 1.6** 

The power coefficient owing to this coupling is given by:

$$k_{n^{0}} = n^{0}K (0) = \frac{n^{0}q}{1\nu} \frac{C_{T}}{gC} \frac{1}{1-\alpha}$$

$$= \frac{C_{T} (T^{0} - T_{in})}{1-\alpha}$$
(140)

In the simplest case, where  $T_{in}$  is constant and therefore  $\alpha = 0$ , Eq. (139) becomes:

$$n^0 \overline{K}(p) = \frac{k_{n^0}}{\frac{M}{g}p + 1}$$
 (141)

Equation (141) may be taken as a prototype for simple external loops. It contains two parameters, the power coefficient of reactivity and a time (M/g) which in the present example is the time for the flow rate, g, to fill the tank.

The effect of Xe burnup is also, to a good approximation, described by a transfer function of the form of Eq. (141), as can be seen by referring to Eq. (153).

The transfer coefficient for a control rod may contain the analog of the transport lag,  $\tau$ , of Eq. (139) due to finite time delay in the actuating mechanism. Even if this is not true, inertia effects must be considered. Thus, a possible description of a control loop

$$(\ddot{\mathbf{x}} + 2\xi\dot{\mathbf{x}} + \begin{bmatrix} \xi^2 + \omega^2 \end{bmatrix} \mathbf{x}) = -\frac{(\xi^2 + \omega^2)}{\mu} \operatorname{Cn} + \mathbf{D}$$

$$\mathbf{k} - 1 = \mu \mathbf{x}$$
(142)

where the X is necessary because of inertia. E is the damping constant and x the position of the rod. The transfer function is then of the form:

$$n^{0} \overline{K}(p) = \frac{-C}{1 + \frac{2\xi}{\xi^{2} + \omega^{2}} p + \frac{p^{2}}{\xi^{2} + \omega^{2}}}$$

$$k_{n^{0}} = -C$$
(143)

More complicated control systems are often desirable. A further discussion is given below.

More generally, any  $\overline{K}(p)$  may be expected to have the following characteristics:

- (1) It is real for real p.
- (2)  $\lim_{R\to\infty} \overline{K}(Re^{i\theta}) = 0$ , all  $\theta$ .
- (3) The singularities of  $\overline{K}(p)$  are a finite or infinite number of poles.

In such a case, K(p) may be decomposed into partial fractions so that a general form is:

$$n^{0} \overline{K}(p) = \frac{A_{1}}{p} + \frac{A_{2}}{p^{2}} + \dots, + \frac{A_{m}}{p_{m}} + \sum_{i} \left\{ \frac{B_{i}^{i}}{\tau_{i} p + 1} + \frac{B_{2}^{i}}{(\tau_{i} p + 1)^{2}} + \dots, \frac{B_{m_{i}}^{i}}{(\tau_{i} p + 1)^{m_{i}}} \right\}$$

$$+ \sum_{i} \left\{ \frac{C_{1}^{i}}{\frac{p^{2}}{\xi_{1}^{2} + \omega_{1}^{2}} + \frac{2\xi_{i}}{\xi_{1}^{2} + \omega_{1}^{2}}} + \frac{C_{2}^{i}}{(\frac{p^{2}}{\xi_{1}^{2} + \omega_{1}^{2}} + \frac{2\xi_{i}}{\xi_{1}^{2} + \omega_{1}^{2}} + 1)^{2}} + \dots \right\}$$

$$(144)$$

In interpreting  $\overline{K}(p)$ , it may be noted that  $k_{n_n} = \infty$  unless:

$$A_1 = A_2 = \dots, = A_m = 0$$

in which case:

$$k_{n0} = B_1^i + B_2^i + \ldots, + C_1^i + C_2^i + \ldots$$

It is instructive to discuss the meaning of the various terms of Eq. (144) by means of the differential equations which give rise to them. Each term may be thought as arising from an external-system variable. Thus,  $A_n/p^n$  arises from the system:

$$\frac{d^n}{dt^n} y^1 = n^1$$

$$\mathbf{k}^1 = \mathbf{A}_n \mathbf{y}^1$$

if we recall that by definition:

$$\mathbf{k}^1 = \int_0^t \mathbf{K}(\mathbf{t} - \mathbf{s}) \ \mathbf{n}^1 \ \mathbf{ds}$$

Similarly, the term  $B^{i}/(\tau_{i}p + 1)$  arises from:

$$\left(r_1\frac{d}{dt} + 1\right)y^1 = n^1$$
$$k^1 = B^i n^1$$

A term like:

$$1 + \frac{C_1}{\frac{2\xi}{\xi^2 + \omega^2} p + \frac{p^2}{\xi^2 + \omega^2}}$$

arises from an equation of the form of Eq. (142).

The transfer function of Eq. (139) is a simple example of one which yields an infiniteseries expansion of the form of Eq. (144).

### STABILITY CRITERIA

The question of whether the system under discussion is stable for small departures from equilibrium is answered in the positive if all the roots of the denominator of Eq. (137) have negative real parts. If this denominator is an algebraic equation of sufficiently small degree, all the roots are easily found. If not, other procedures may be desirable.

Real roots can be determined by plotting  $\vec{F}^{-1}(p)$  and  $(n^0/\epsilon\beta)\overline{K}(p)$  vs p for real p and noting the intersection. In Figs. 1.6.4 to 1.6.10, f(p) is plotted for  $U^{235}$  fuel which is (for  $\epsilon_i = \epsilon$ ):

$$\mathbf{f}(\mathbf{p}) = -\overline{\mathbf{F}}^{-1}(\mathbf{p}) + \frac{\mathbf{l}\mathbf{p}}{\epsilon\beta} \tag{145}$$

This may materially reduce the labor involved. Further, neglecting  $lp/\epsilon\beta$  will have negligible effect on the other roots in most cases.



If all the roots are real, the above procedure is enough. If not, it is useful to use the Nyquist Stability criterion. This may be stated as follows:

If one plots any function g(p) = u + iv on an argand diagram (u vs v) as  $p = i\omega + \eta$  varies on the infinite contour (shown in Fig. 1.6.27), then the number of times g(p) circles the origin is the number of poles of g(p) with positive real parts minus the number of zeroes of g(p) with positive real parts. In most applications, the location of the poles is obtained by inspection of g(p).

Thus, one may determine whether the system is stable (no zeroes of g with positive real parts) without finding the roots.

In control work,²² it is conventional to plot the quantity [cf. Eq. (137)]:

$$\frac{\mathbf{n^0}}{\epsilon \beta} \overline{\mathbf{F}}(\mathbf{p}) \ \overline{\mathbf{K}}(\mathbf{p})$$

and count the number of times the locus circles -1. It may often be more convenient to plot:

$$\overline{\mathbf{F}}^{-1} - \frac{\mathbf{n^0}}{\epsilon \beta} \, \overline{\mathbf{K}}$$

since  $\overline{F}^{-1}$  is independent of  $\overline{K}$  and may be calculated once and for all. A plot of:

$$f(i\omega) = \overline{F}^{-1} (i\omega) - \frac{i\omega l}{\epsilon \beta}$$
 (146)

is given in Fig. 1.6.26. An example of an application of this criterion is given in Fig. 1.6.27. This is concerned with determining in which half-plane lie the roots of:

$$W(p) = \frac{205 \frac{1 - e^{-p}}{p} - \frac{1}{2}e^{-p} - p - 0.625}{1.15p + 17.3}$$

Since the plot of the imaginary part of W vs the real part of W when p follows the contour shown in Fig. 1.6.28 does not enclose the origin, there are as many poles as zeroes in the right half-plane. One can see by inspection that W has no poles in the right half-plane, and hence no zeroes.

Other methods of determining stability without finding explicitly the roots of the denominator of Eq. (137) can be found in standard texts on servomechanisms and analysis of minimum-phase-shift electrical networks. The reactor transfer function has properties characteristic of the transfer function of a minimum-phase-shift electrical network. In such a case, a method of special interest is the use of a Bode diagram.

# MEASUREMENT OF $\overline{K}$ (i $\omega$ )

The reactor transfer function  $\overline{K}(p)$  can be experimentally determined in an operating reactor^{23,24} for pure imaginary p. If one oscillates a control rod at frequency  $\omega$  and constant amplitude, A, then in Eq. (128):

$$\delta \mathbf{k}(\mathbf{t}) = \mathbf{R} \mathbf{P} \boldsymbol{\epsilon} \boldsymbol{\beta} \mathbf{A} \mathbf{e}^{\mathrm{i} \omega \mathbf{t}} \tag{147}$$

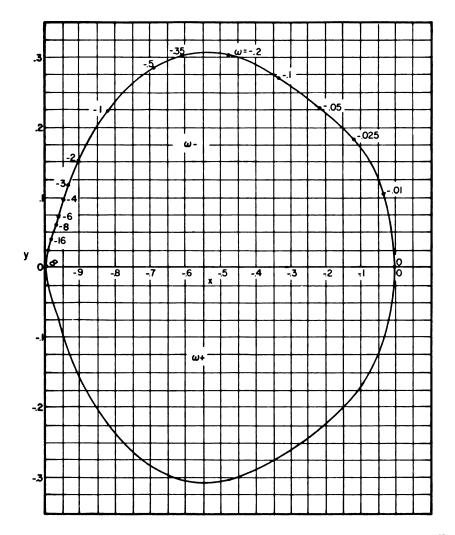


Fig. 1.6.26 — Imaginary Part of  $\Sigma$   $(\beta_1/\beta)(\lambda_1/p + \lambda_1) - 1$  vs the Real Part for  $U^{236}$ . Submitted by Nuclear Development Associates, Inc., Dec. 15, 1952. This is plotted as p traces the contour shown in Fig. 1.6.28.

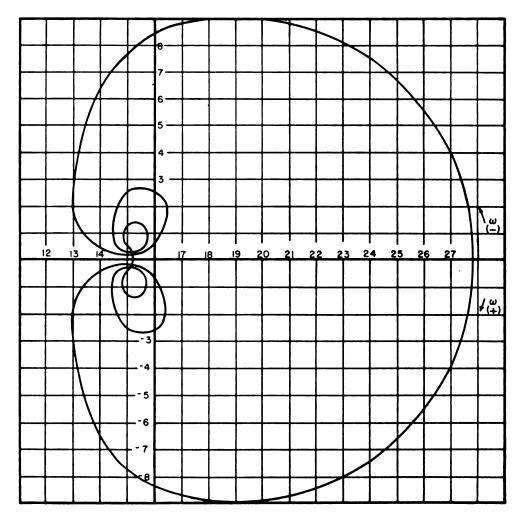


Fig. 1.6.27 — A Plot of  $205[(1-e^{-p})/(p)] - [^1/_2 e^{-p} - 0.625]/1.15p + 17.3$  as p Traces the Contour Shown in Fig. 1.6.28. Submitted by Nuclear Development Associates, Inc., Dec. 15, 1952. Since the curve does not circle the origin and the function has no poles in the right half plane, it has no zeros in the right half plane.

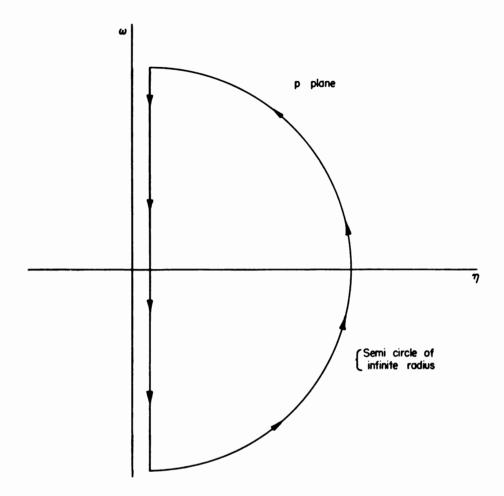


Fig. 1.6.28 — Contour of  $p = \eta + i\omega$  to be Used in Applying Nyquist Criterion. Submitted by Nuclear Development Associates, Inc., Dec. 15, 1952.

Furthermore, in such a case one will have a solution of the form:

$$\frac{n^1}{n^6} = \mathbf{Rp} \ \nu \ e^{i\omega t}$$
 
$$\mathbf{c}_1^1 = \mathbf{Rp} \ \gamma_i \ e^{i\omega t}$$
 (148)

Substituting in Eq. (128), and using:

$$\int_{-\infty}^{t} \mathbf{K}(t-s) e^{i\omega s} ds = e^{i\omega t} \tilde{\mathbf{K}}(i\omega)$$
 (149)

one finds:

$$\frac{\mathbf{A}}{\gamma}\Big|_{\mathbf{n}^0} = \overline{\mathbf{F}}^{-1} (i\omega) - \frac{\mathbf{n}^0}{\epsilon\beta} \, \mathbb{K}(i\omega) - 1 \tag{150}$$

In Eq. (150),  $A/\gamma$  is experimentally determinable as a complex number (owing to phase shift in flux response). If one measures  $A/\gamma|_{n^0}$  for  $n^0$  small (essentially  $n^0=0$ ) and for a finite  $n^0$ , there results from Eq. (150):

$$\frac{\mathbf{A}}{\gamma}\Big|_{\mathbf{n}^0=0} - \frac{\mathbf{A}}{\gamma}\Big|_{\mathbf{n}^0} = \frac{\mathbf{n}^0}{\epsilon\beta} \,\overline{\mathbf{K}}(\mathbf{i}\omega) \tag{151}$$

#### THE XENON POWER INSTABILITY

If in Eq. (82) one neglects the variation of the iodine source (owing to its long period, this is permissible for stability studies), one has as linearized equations:

$$k^1 = C \times z^1$$

$$\frac{dz^{1}_{x}}{dt} = -\lambda_{x}z^{1}_{x} - n^{\theta}v^{\frac{\partial\sigma_{a}}{\partial z_{x}}}z^{1}_{x} - z^{\theta}_{x}\left(\overline{v^{\frac{\partial\sigma_{a}}{\partial z_{x}}}}\right)n^{1}$$
(152)

whence, using the second of Eq. (135):

$$n^{0} \overline{K}(p) = -\frac{C_{x}n^{0} z_{x}^{0} \left(v \frac{\partial \sigma_{x}}{\partial z_{x}}\right)}{p + \lambda_{x}} = -\frac{1}{\lambda_{x}^{-1} p + 1} C_{x} z_{x}^{0} \left(1 - \frac{\lambda_{x}}{\lambda_{x}}\right)$$
(153)

where:

$$\lambda_{e} = \lambda_{x} + n^{0} \left( \overline{\nu \frac{\partial \sigma_{a}}{\partial z_{x}}} \right) \tag{154}$$

is the reciprocal mean life of a Xe atom in the reactor at equilibrium. The time constant in Eq. (153) is  $(\lambda_e^{-1})$ , and the power coefficient is:

$$\mathbf{k}_{\mathbf{R}^0} = -\mathbf{C}_{\mathbf{X}} \ \mathbf{z}_{\mathbf{X}}^0 \left( 1 - \frac{\lambda_{\mathbf{X}}}{\lambda_{\mathbf{R}}} \right) \tag{155}$$

which is positive, since  $C_X z_X^0$  is the k change due to equilibrium xenon poisoning, which is negative.

The effective value of the poison cross section is given by:

$$\sigma_{ap} = \overline{P} \sigma_{af}$$

where  $\overline{P}$  is obtained from Eqs. (83) and (85) [or Eq. (87)]. Using Eq. (89), one sees that for a bare thermal reactor:

$$\delta \mathbf{k} = \mathbf{C}_{\mathbf{X}} \mathbf{z}_{\mathbf{X}}^{0} = - \overline{\mathbf{P}} \mathbf{f} \frac{\sigma_{\mathbf{a}} \nu_{\mathbf{g}}}{\mathbf{L}_{\mathbf{g}}}$$
 (156)

The unstable period arising from the transfer function of Eq. (153) has been calculated²⁵ as a function of  $\phi$  under the following assumptions:

- (1) The flux and all concentrations are space independent.
- (2) One delay group with  $\beta = 0.01$ , and  $\lambda^{-1} = 10$  sec.

Their results are given in Fig. 1.6.29.

#### **CAVITY OSCILLATIONS**

Liquid homogeneous reactors and liquid-cooled and moderated reactors admit the possibility of a particular type of relatively high frequency, unstable oscillations, which may be called cavity oscillations. This phenomena has been considered by several authors.^{26,27}

Cavity oscillations arise as follows: A tank of liquid connected to a standpipe or pressurizer will have certain resonant frequencies at which it can oscillate with relatively weak damping. Coupling of these oscillations to the reactor will often be sufficient to feed energy into the oscillations and may overcome the damping, thus leading to instability.

#### REMARKS ON CONTROL SERVOMECHANISMS

Suppose a control is characterized by a parameter x such that:

$$k-1=x ag{157}$$

The question to be considered here is concerned with the selection of the functional  $x\{n\}$  characterizing the control servomechanism. If one writes this relation in terms of:

$$\mathbf{x}(t) = \int_{-\infty}^{t} n^{0}\mathbf{K}(t-\mathbf{s}) \left(\frac{\mathbf{n}(\mathbf{s})}{\mathbf{n}^{0}} - 1\right) d\mathbf{s}$$

$$\mathbf{x}(\mathbf{p}) = n^{0}\overline{\mathbf{K}}(\mathbf{p}) \left(\frac{\mathbf{n}(\mathbf{p})}{\mathbf{n}^{0}} - 1\right)$$
(158)

it is seen that  $\int_0^t K(s)ds$  is the response of x to a unit step in  $n/n^0$  at t=0. The short-time behavior of  $\int_0^t K(s)ds$  may be obtained by expanding  $(1/p)\overline{K}(p)$  in a power series in 1/p:

$$\frac{1}{p}\,\overline{K}(p)=\sum_{i=0}^{\infty}\,\frac{a_i}{p^{\,i\,+\,1}}$$

$$\int_{0}^{t} K(t)ds = \frac{1}{2\pi i} \int_{c-i\infty}^{c+i\infty} e^{pt} \overline{K}(p)dp$$

$$= \sum_{i=0}^{\infty} a_{i} \frac{t^{i}}{i!}$$
(159)

Owing to control inertia, one sees that the initial displacement  $a_0$  and initial velocity  $a_1$  will vanish so that:

$$\overline{K}(p) = \sum_{1}^{\infty} \frac{a_{1}}{p!}$$
 (160)

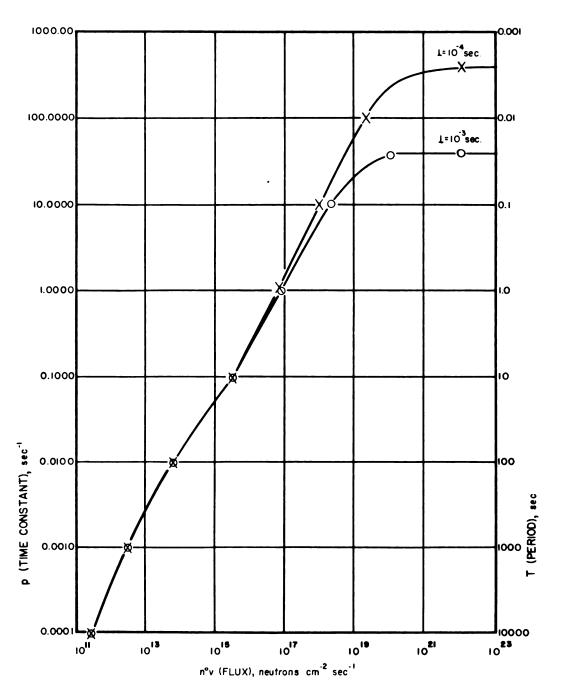


Fig. 1.6.29 — Inverse Reactor Period Owing to Xenon Power Instability. Reprinted from MonP-379. The two curves are for different values of the neutron generation time.

A simple transfer function satisfying Eq. (160) is given by:

$$n^{0} \overline{K}(p) = \frac{k_{n^{0}} (\xi^{2} \pm \omega^{2})}{p^{2} + 2\xi p + \xi^{2} \pm \omega^{2}}$$
(161)

where the plus sign means complex roots and the minus sign real roots of the denominator. In order that both roots have negative real parts (so that control is stable), one must have either the plus sign or the minus sign with  $\omega^2 < \xi^2$ . If Eq. (161) is expanded in powers of 1/p, one obtains:

$$\frac{n^0}{p} \ \overline{K}(p) = \frac{k_{n_0}(\xi^2 \pm \omega^2)}{p^3} + \dots$$
 (162)

The initial motion corresponding to this is:

$$n^{0} \int_{0}^{t} K(s)ds = k_{n^{0}} (\xi^{2} \pm \omega^{2}) \frac{t^{2}}{2!} + \dots$$
 (163)

In order to make this a rapid motion, without increasing  $k_n 0$ , one may use large  $\omega^2$  and the plus sign.

At large times, the displacement of the power owing to a change in reactivity  $\delta k$  from external sources is:

$$\frac{\delta n}{n^0} = \frac{\delta k}{k_{n^0}} \tag{164}$$

as may be seen from Eq. (128) with  $n' = c_i' = 0$ .

This is the control error. It may be reduced to zero by having  $\int_0^{\infty} K(t) dt$  be infinite, i.e., by having  $K(\infty)$  equal a non-zero constant. This means  $\overline{K}(p)$  has a pole at p = 0. One might try:

$$K(p) = \frac{c}{p} \frac{(\xi^2 + \omega^2)}{p^2 + 2\xi p + \omega^2 + \xi^2}$$
 (165)

This has the disadvantage that the control motion starts as  $t^3$  rather than as  $t^2$  as in Eq. (163). However, a suitable transfer function is obtainable by superposition of Eq. (165) and Eq. (161).

In Ref. (28), the transfer function is written as:

$$\mathbf{n}^{\mathbf{0}} \ \overline{\mathbf{K}}(\mathbf{p}) = \frac{\omega_{\mathbf{n}}^{2} \mathbf{B}}{(\mathbf{p}^{2} + 2\xi\omega_{\mathbf{n}}\mathbf{p} + \omega_{\mathbf{n}}^{2})} + \frac{\omega_{\mathbf{n}}^{2} \mathbf{B}}{\tau_{\mathbf{0}} \ \mathbf{p}(\mathbf{p}^{2} + 2\xi\omega_{\mathbf{n}} \ \mathbf{p} + \omega_{\mathbf{n}}^{2})}$$
(166)

where the notation is different than in the above. Note that  $k_{n^0} = B$  for the first part of the above expression, but is infinite for the second part. The reactor response, as the parameters in Eq. (166) are varied, is illustrated in Figs. 1.6.30 to 1.6.33 (note:  $f_n = \omega_n/2\pi$ ).

In order to understand physically the meaning of Eq. (166), it may be written in terms of a differential equation:

$$\frac{d^2}{dt^2} + 2\xi \omega_n \frac{d}{dt} + \omega_n^2 x(t) = \omega_n^2 B \left\{ \frac{n(t)}{n^0} - 1 + \frac{1}{\tau_0} \int \left( \frac{n(t)}{n^0} - 1 \right) dt \right\}$$
 (167)

It is clear that the only steady-state solution of Eq. (167) is  $n = n^0$ .

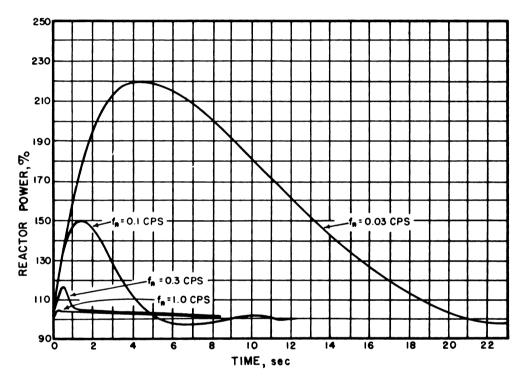


Fig. 1.6.30 — Reactor Power vs Time. Reprinted from WAPD-34, Vol. I, RM-90. The following parameters were used: Temperature coefficient = zero; disturbance =  $+0.003(1-e^{-t/0.5}) = \partial k$ ; regulator rod servo-parameters = optimum for each  $f_n$ .

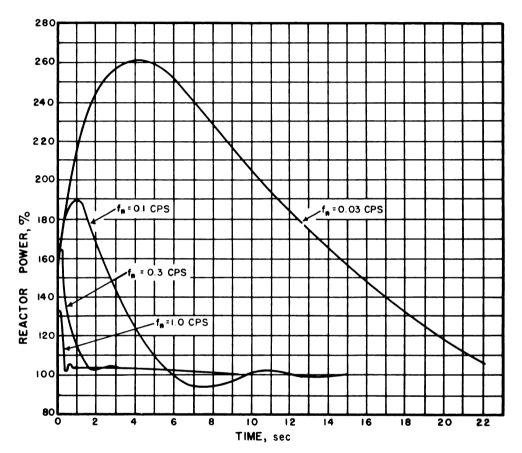


Fig. 1.6.31 — Reactor Power vs Time. Reprinted from WAPD-34, Vol. I, RM-90. The following parameters were used: Temperature coefficient = zero; disturbance =  $+0.003(1-e^{-t/0.1}) = \partial k$ ; regulator rod servo-parameters = optimum for each  $f_n$ .

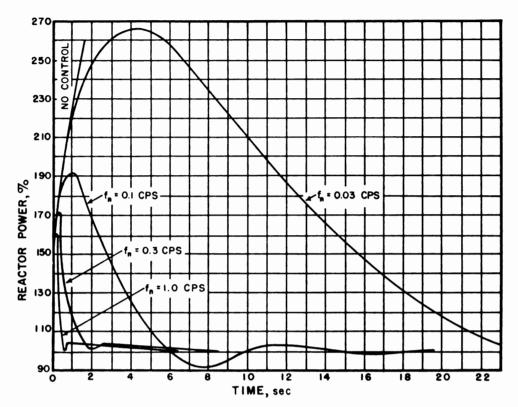


Fig. 1.6.32—Reactor Power vs Time. Reprinted from WAPD-34, Vol. I, RM-90. The following parameters were used: Temperature coefficient = zero; disturbance = +0.003 step in  $\partial k$ ; regulator rod servo-parameters = optimum for each  $f_n$ .

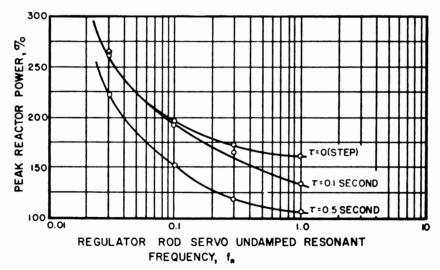


Fig. 1.6.33—Effect of Rapidity of  $\partial k$  Transient on Peak Reactor Power. Reprinted from WAPD-34, Vol. I, RM-90. The following parameters were used: Temperature coefficient = zero; disturbance =  $+0.003(1-e^{-t/\tau}) = \partial k$ ; regulator rod servo-parameters = optimum for each  $f_n$ .

#### AFTER SHUTDOWN

# XENON BUILDUP^{29,30}

The maximum concentration of xenon-135 after shutdown may, in a high-flux reactor, be several times the equilibrium value. This results in a large decrease in reactivity. The time variation of the xenon concentration after shutdown may be obtained from Eq. (82) with iodine source term placed equal to zero. If the reactor has been operating at constant power long enough so that the xenon and iodine concentrations have reached equilibrium values, the iodine concentration can be obtained from Eq. (82), and the ratio of xenon to fuel macroscopic thermal absorption cross sections can be obtained from Eq. (83). The general solutions of Eq. (82) are the same as for any other decay chain and were given in Chapter 1.2.

The xenon poisoning, P, for shutdown after reaching equilibrium at a given flux  $\phi_0$  is plotted as a function of time in Fig. 1.6.34. The peak and steady-state xenon poisoning for various reactor steady-state fluxes are given in Fig. 1.6.35. Xenon concentration trajectories for various operating maneuvers are discussed in Ref. (31).

# **HEATING AFTER SHUTDOWN**

The heat released by radioactive decay of fission products has been treated in Chapter 1.2. In most cases, heat resulting from induced radioactivity may be neglected. Results of calculations of temperature rise (without cooling) for various reactors, as a function of time after shutdown, are given in Fig. 1.6.36.

#### REACTOR TEMPERATURE COEFFICIENTS

#### **LATTICES**

Experimentally obtained temperature coefficients for natural-uranium and graphite reactors are given in Table 1.6.1; barometric coefficients, arising from neutron capture in nitrogen, are also given for air-cooled units.

The theoretical situation has been recently reviewed³² with special reference to the Oak Ridge and Brookhaven reactors, as follows: Based on the notation given in Chapter 1.5 under "Lattices," one has:

$$\frac{\delta k_{eff}}{k} = \frac{\delta \epsilon}{\epsilon} + \frac{\delta \eta}{\eta} + \frac{\delta f}{f} + \frac{\delta p}{p} - B^2 \delta M^2$$
 (168)

This ignores graphite and metal density effects, whose contribution is only of the order of  $1 \times 10^{-6}$  per °C, and supposes nitrogen effects to be handled separately. The term in  $\epsilon$  is also only of this order and may likewise be ignored.

The remaining terms all depend upon neutron (i.e., moderator) temperature except p which depends upon metal temperature via Doppler broadening of the resonance lines. The  $\eta$  term will be the same for all natural-uranium reactors; the other terms will vary from one reactor to another.

Values for  $-(1/\eta)$  d $\eta$ /dT derived from experiment and calculation range from  $4.5 \times 10^{-6}$ /°C to  $22 \times 10^{-6}$ /°C. This represents one of the largest terms in (168), and one of the most uncertain. From evaluation of the remaining terms and comparison with actual reactor results (Table 1.6.1), the authors conclude that the smaller values are to be preferred.

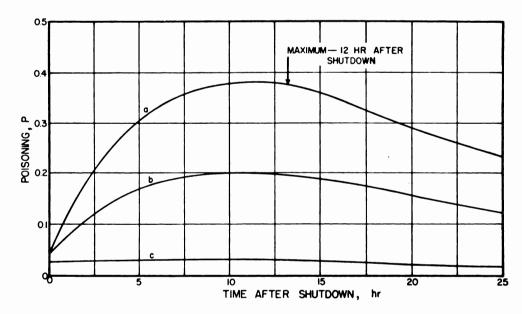


Fig. 1.6.34 — Xenon Poisoning vs Time after Shutdown. The ratio of xenon to  $U^{235}$  macroscopic thermal absorption cross sections is shown for the case where xenon and iodine are in equilibrium prior to shutdown. The curves are for different fluxes: (a)  $2\times 10^{14}$  neutrons/(cm²)(sec); (b)  $10^{14}$  neutrons/(cm²)(sec); (c)  $10^{13}$  neutrons/(cm²)(sec). Reprinted from The Elements of Nuclear Reactor Theory, by S. Glasstone and M. Edlund. Copyright, 1952. By permission from D. Van Nostrand Company, Inc., New York.

The main variation in f arises from the flattening of the thermal-neutron distribution as the temperature rises, as may be found by varying the  $\kappa$  values in Eq. (3), Chapter 1.5. For 1/v absorbers,  $\kappa$  varies as  $T^{-\frac{1}{4}}$  where T is the absolute temperature of the neutrons. Results calculated in this way are given in Table 1.6.2.

Variation in p with (metal) temperature involves the change in the effective volume resonance integral A as shown in Table 1.6.3. The effect of temperature on the surface term,  $\mu$ , is apparently not known. In the Brookhaven and Oak Ridge machines,  $\delta p/p \approx -0.12$   $\delta A/A$  [Eq. (9), Chapter 1.5] so that the contribution to Eq. (168) is some  $-(1.4 \text{ to } 2) \times 10^{-5} \text{ per }^{\circ}\text{C}$ .

The effect of (neutron) temperature on  $M^2$  is primarily exerted through the thermal diffusion area  $L^2$ , according to (for 1/v absorption, and  $f_2 = 1 - f$ ):

$$\frac{dL^2}{dT} = L^2 \left( \frac{1}{T} - \frac{f}{f_2} \frac{1}{f} \frac{df}{dT} \right) \tag{169}$$

For the Brookhaven reactor, this amounts to about 0.35 cm²/°C, while the corresponding effect on the age is about -0.05 cm²/°C. Thus,  $dM^2/dT = 0.3$  cm²/°C, and the last term in Eq. (168) is about  $-2.8 \times 10^{-5}$ /°C. A similar value is obtained for the Oak Ridge reactor.

The sum of the  $\eta$ , f, and  $M^2$  terms in Eq. (168) is to be compared with the "uniform graphite in vacuum" coefficient in Table 1.6.1; while the p term in Eq. (168) is to be compared with the "uniform metal" coefficient.



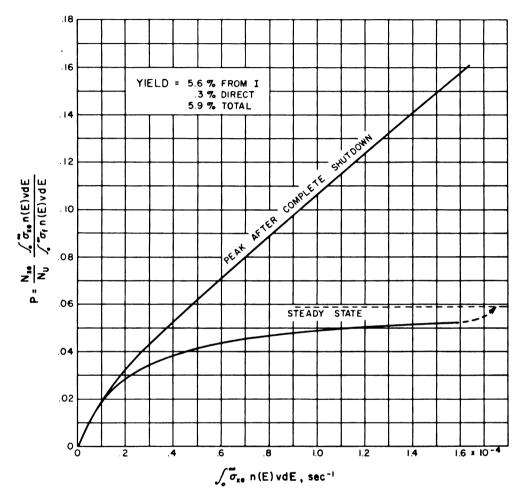


Fig. 1.6.35 — Xenon Poisoning vs Flux. Taken from H. Hurwitz, private communication. Curves show peak after shutdown and steady-state poisioning as a function of steady-state flux.

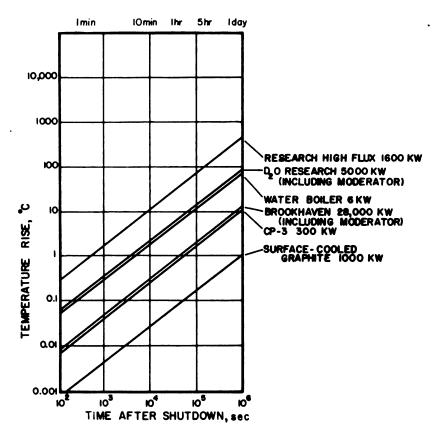


Fig. 1.6.36—Calculated Temperature Rise After Shutdown. Reprinted from M. M. Mills, Journal of Reactor Science and Technology 58, TID-71.

Table 1.6.1 — Experimental Temperature Coefficients in Graphite Lattice Reactors

Reactor	Temperature coefficient, $10^5 \Delta R/C$
Oak Ridge†	
Operating metal	-0.78
Operating graphite	-2.08
Operating total	-2.86
Uniform metal	-1.04
Uniform graphite in vacuum	-4.94
Uniform over-all in vacuum	<b>-5.9</b> 8
Uniform graphite in air	-2.9
Brookhaven,‡ 300°K	
Uniform graphite in air	$-1.82 \pm 0.26$
Uniform metal	$-1.95 \pm .13$
Uniform graphite in vacuum	-4.1

- * "Operating" coefficients are referred to temperature of hottest metal in the reactor
  - † Kaplan and Chernick; 52 barometric coefficient =  $-1.04 \times 10^{-5} \Delta k/mm$  Hg
- ‡ Communication from Irving Kaplan; barometric coefficient § =  $-0.91 \times 10^{-5}$  in k for mm Hg

§ Data converted from inhours by using 1 inhour =  $2.6 \times 10^{-6}$  in k

Table 1.6.2 — Temperature Dependence of Thermal Utilization in Lattice Reactors
(Kaplan and Chernick, BNL-152)

	$1/f \partial f/\partial T (\times 10^5/^{\circ}C)$		
T, *K	Oak Ridge	Brookhaven	
<b>30</b> 0 – <b>35</b> 0	4.1	3.3	
350-400	3.4	2.6	
400-450	2.7	2.2	

Table 1.6.3 — Temperature Effect on Volume Resonance Integral of U
(Kaplan and Chernick, BNL-152)

Author	$1/A \partial A/\partial T (\times 10^4/^{\circ}C)$
Creutz et al (CP-110)	1.7
Mitchell et al (CP-597)	1.1
Wigner (CP-4)	3
Dancoff (CP-1589)	1.2 - 1.7

#### REACTOR CONTROLS

#### ABSORBER CONTROLS

Absorbers distributed uniformly throughout the reactor change the microscopic cross sections, and the effect on reactor reactivity can be determined by methods described previously (Chapters 1.4, 1.5, and previous portions of 1.6). In practice, the absorbing material for control is frequently lumped into discrete assemblies, such as rods which move in and out of the reactor; further considerations are therefore needed.

# SINGLE CONTROL RODS

A small, thermally black rod of effective radius  $r_0$  inserted along the axis of a bare cylindrical reactor of radius R affects k by an amount approximated from 2-group theory results to be:³³

$$\Delta k = \frac{7.5}{R^2} (\tau + L^2) \left[ 0.116(1 + \frac{\tau}{L^2} - \ln \frac{2.405r_0}{R} \right]^{-1}$$
 (170)

where  $\tau$  = age, L = thermal diffusion length, and K =  $\sqrt{1/\tau + 1/L^2}$ .

The rod affects reactivity through the neutrons it absorbs and the increase it produces in the number of neutrons escaping outward from the reactor surface. For a small axial rod, the latter effect is about 0.6 of the former.*

If the rod were black to fast neutrons as well, its effectiveness would be greater by a factor which decreases from  $1 + \tau/L^2$  for very small rods to 1 for large rods.

As the rod is displaced from the central axial position, its effectiveness decreases. Figure 1.6.37 shows the effect of radial displacement as estimated by the familiar (neutron flux)² weighting rule and also as obtained from more detailed computations. Figure 1.6.38 similarly shows the effect of longitudinal displacement, i.e., of partly withdrawing the rod out the end of the reactor, as obtained from flux-squared weighting and from more elaborate calculation.

The effect of a rod is greater in reflected than in bare reactors (Fig. 1.6.39).

# EFFECTIVE ROD RADIUS

As employed in the derivation of Eq. (170),  $r_0$  is the radius at which the external diffusion solution for the neutron flux vanishes. This is somewhat less than the actual geometric radius, r, of the rod, since even with a perfectly black absorber the neutron flux merely dips downward toward the body but has not vanished by the time the surface is reached. Chapter 1.3 discusses the boundary conditions at the surface of a black body; the straight-line extrapolation distance of the external flux into the body is  $\lambda l$ , where l is the mean-free-path. For large bodies, this gives the effective radius  $(r_0 = r - \lambda l = r - 0.71l)$ , but for small bodies, the external diffusion solution being fitted curves downward below the straight line, and  $r_0$  is closer to r. One may also develop the formulae using the actual radius, r, and the surface logarithmic derivative given by  $\lambda$  without introducing  $r_0$ .

Near the tip of a partially inserted rod, its neutron absorption may be increased several fold, the so-called "lightning rod" effect. See Murray³⁸ and Wheeler.³⁹



^{*} Graphs 4 show how these two effects vary as the rod is displaced away from the reactor axis.

[†] This variation is plotted³³ for different numerical cases by 2-group theory and also compared with a result obtained by Murray from more elaborate calculations.

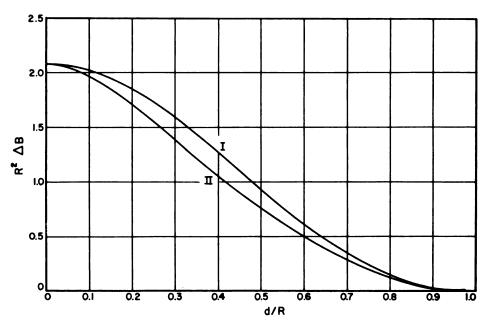


Fig. 1.6.37 — Eccentric Control Rod Effectiveness. Reprinted from Adler MT-222. Bare cylindrical reactor of radius R, rod parallel to axis and at distance d from it, effective radius of rod =  $r_0$  = 0.01R,  $\Delta B$  = change in buckling due to rod. (I)  $J_0^2$  weighting; (II) superposition calculation.

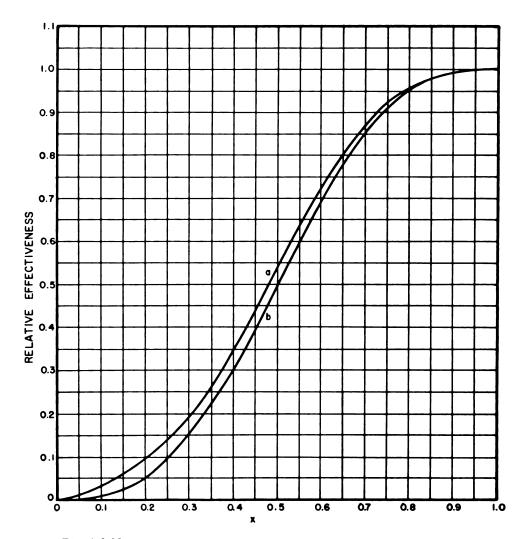


Fig. 1.6.38—Partial Withdrawal of Axial Control Rod. Reprinted from Wheeler, Principles of Nuclear Power, N-2292. Effectiveness of rod relative to effectiveness when completely inserted; x = distance of insertion + length of the cylindrical reactor. (a) Calculations by Murray for a case with reactor diameter = 90 times rod diameter = 1.77 reactor length; (b) estimate according to  $2 \int_0^x \sin^2 \pi y \, dy = x - \sin 2\pi x/2\pi$ .

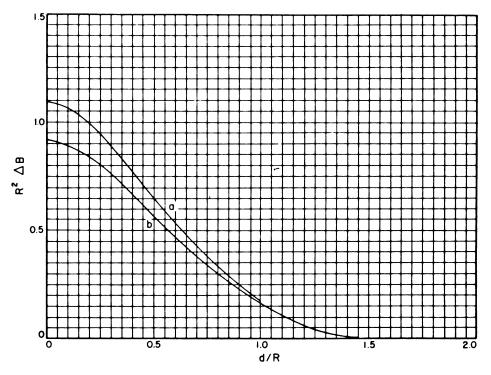


Fig. 1.6.39 — Control Rod Effectiveness in Bare vs Reflected Reactors. Reprinted from Adler, MT-222. Cylindrical core radius = R with reflector = 1.5R without reflector, same core buckling. Distance of rod from axis = d, effective radius of rod = 0.01R,  $\Delta B$  = change in buckling due to rod (a) in reactor with reflector (b) in bare reactor.

Wheeler³⁹ gives values for the effective radius,  $r_0$ , for a number of cases as reported in Table 1.6.4 for black bars and in Table 1.6.5 and Fig. 1.6.40 for bars which are not black. Table 1.6.6 gives some experimental and theoretical comparison of various bar shapes.

#### MULTIPLE CONTROL RODS

When more than one rod is present, there are interaction effects between them. A single rod lowers the relative value of the neutron density nearby but raises it farther away. Thus, the effect of a second rod will be diminished if near the first but may be enhanced if farther away; i.e., the "shadowing" may be either negative or positive.

Table 1.6.7 gives some experimental results with two rods. In the Brookhaven reactor, the reduction in effectiveness of one bank of 8 rods owing to shadowing is estimated at 16 percent;⁴¹ for two banks crossing, the reduction is 35 percent. Figure 1.6.41 shows the effectiveness per rod of a ring of 4 rods at varying distances from the reactor axis and also the effectiveness of a single rod at the same distance; the shadowing is negative when the rods are close together and becomes positive as they separate. Figure 1.6.42 again illustrates the greater effectiveness of rods in a reflected reactor.

Table 1.6.4—Effective Radius of Black Control Bars (Wheeler, N-2292, Principles of Nuclear Power, Chapter 22: Control)

Case

r₀

Large snugly imbedded rod*	$r e^{-0.711/r}$
Snugly imbedded rod†	r e-λ 1/r
Small (compared to 1) snugly imbedded bar of perimeter; s	$0.461 e^{-(8\pi 1/3s)}$
Small (compared to l), snugly imbedded rod of radius r	0.46 e ^{-(41/3r)}
Bar in a considerably larger hole of radius r ₁	r ₁ e ⁻⁽⁸ 1/3s)
Rod in considerably larger hole of radius r	r ₁ e ^{-(41/3r)}
Imbedded strip of small thickness (compared to 1) but with W comparable with or larger than 1	$W/4 \exp -[y(1 - 0.114y + 0.048y^2)]^{-1}$ where y = $W\sqrt{3}/\pi l$
Imbedded cross formed of two thin strips each of width W + $\sqrt{2}$	Same as preceding
Large imbedded rectangular bar	See Fig. 1.6.43

- *A constant in Wheeler's formula has been changed here⁵⁹
- † Obtained by a slight extension of Wheeler's argument; here  $\lambda$  is from Chapter 1.3,
- "Boundary Conditions in Diffusion Theory," for a cylindrical case
- † Perimeter determined by putting a measuring tape once about the bar and drawing it tight; in general, the tape will not touch the bar at all points

Table 1.6.5 — Effective Radius of Non-black Bars

Case

r₀

Weak absorption*

General  $r_{av} e^{-(2\pi 1/3r)}$ Small (in girth compared to 1) imbedded bar  $0.46 e^{-(2\pi 1/3A)}$ Bar in considerably larger hole  $r_1 e^{-(2\pi 1/3A)}$ Intermediate absorption†

Rod in any size hole  $r_1 e^{-(2\pi 1/3A)}$ 

* Here,  60  A is the total absorption cross section (N $\sigma_a$ ) per unit length of bar, and  $r_{av}$  is the distance from the bar axis to the point where the average neutron absorbed in the rod may be considered to have started its last flight. Webster  61  gives a formula for computing  $r_{av}$ , and also discusses the evaluation of A for fast neutrons

 $\dagger$  Here, ⁶² F is the surface-to-average neutron density for the rod a function of x = Kr and plotted in Fig. 1.5.17

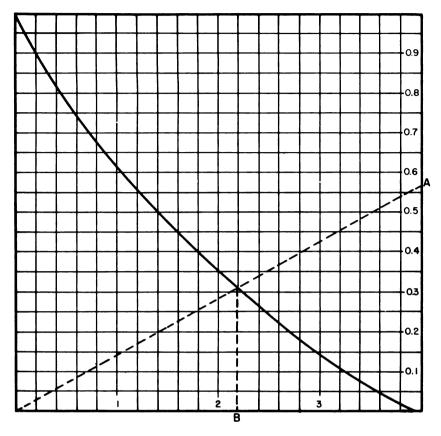


Fig. 1.6.40 — Effective Radius of Rectangular Bar. Reprinted from Wheeler, Principles of Nuclear Power, N-2292. Remove a layer of thickness 0.711 all around the bar to obtain a smaller effective rectangle of width w and thickness Aw. Plot A on right scale of graph and connect to lower left corner by a straight line intersecting curve. Below intersection, read  $B = w/r_0$  on bottom scale.

Table 1.6.6 — Effect of Control Rod Shape

(Wheeler, Principles of Nuclear Power, N-2292, Sect. 22.5.30)

			In-hole	calculation†	Imbedde	d calculation;
Shape of bar	Perimeter, cm	Observed* effectiveness relative to + bar	r ₀ , cm	Relative effective- ness	r ₀ , cm	Relative effective- ness
_	18.1	0.90	1.65	0.87	1.28	0.82
+	25.6	1.00	2.38	1.00	2.24	1.00
0	28.4	1.06	2.58	1.03	3.20	1.06

^{*} Marshall;  65  all bars had a maximum extension of 9.05 cm and were located in a square hole equivalent in area to a circle of radius  $r_1 = 5.74$  cm

[†]Using entry 5 of Table 1.6.4

 $[\]ddagger$  Using Table 1.6.4 entry 7 for - shape, entry 8 for + shape, and entry 1 (but with the original value 0.58 instead of 0.71) for 0 shape

Table 1.6.7 — Control Rod Shadowing*

(Wheeler, Principles of Nuclear Power, N-2292, Sect. 22.3.62)

Distance between rods, in.	45	90
Effect of first rod alone	0.159	0.159
Effect of second rod alone	.211	.159
Sum of individual effects	.370	.318
Observed effect of both together	.338	.303
Decrease owing to shadowing, %	8 <b>.6</b>	4.7

*Experiments by Zinn and Anderson⁶⁴ on first chain-reactor built at Chicago; controls were two strips of cadmium 2 in. wide and 8 ft long

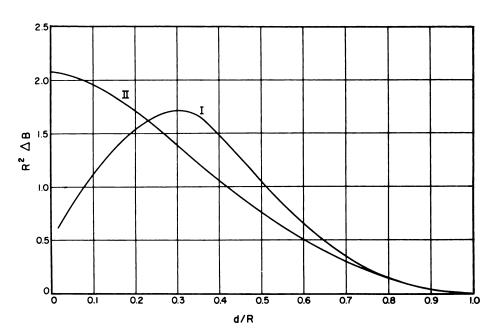


Fig. 1.6.41—Shadowing in a Ring of 4 Control Rods. Reprinted from Adler, MT-222. Bare cylindrical reactor of radius R; effective radius of rod = 0.01R; distance of rods from reactor axis = d;  $\Delta B$  = change in buckling. Graph shows (II) effectiveness of a single rod; (I) one-fourth the effectiveness of a ring of 4 rods.

()

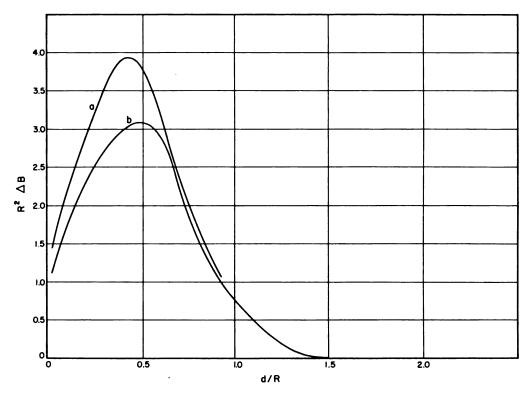


Fig. 1.6.42 — Control Rods with and without Reflector. Reprinted from Adler, MT-222. Cylindrical core of radius R with reflector, 1.5R without reflector;  $r_0 = 0.01R$ , ring of 4 rods at distance d from the core axis,  $\Delta B = \text{change}$  in buckling (a) in reflected reactor (b) in bare reactor.

# **CONTROL REGIONS**

The effect of slight spatial variations in buckling is accounted for by the flux-squared weighting rule:

$$\overline{B} = \frac{\int B \phi^2 dv}{\int \phi^2 dv}$$
 (171)

where  $\phi$  is the undisturbed neutron flux.* The statistical weight of a region of a reactor is the value of  $\int \phi^2 dv$  for that region divided by the value of the same integral taken over the entire reactor. Evidently, the weights of different regions are additive. Figure 1.6.43 shows the weights of central regions in various shapes of bare reactors.† It is seen that the efficiency of (a small amount of) control exerted in a central region is several times what it would be if spread uniformly throughout the reactor.

^{*} More generally,  42   $\phi$  is proportional to the neutron flux multiplied by  $l_{tr}$   $(1 + \tau/L^2)$ .

[†] Figure 1.6.44 gives some Bessel function integrals frequently encountered in cylindrical reactors.

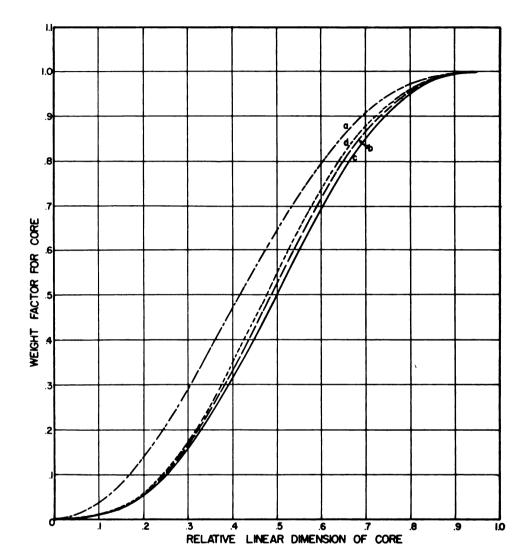


Fig. 1.6.43—Statistical Weights for Central Regions. Reprinted from Chicago Handbook. (a) Circular cylinder with full length concentric core; (b) circular cylinder with similar concentric core, i.e., core length reduced in the same ratio as the radius; (c) sphere with concentric core; and (d) parallelepiped with similar core.

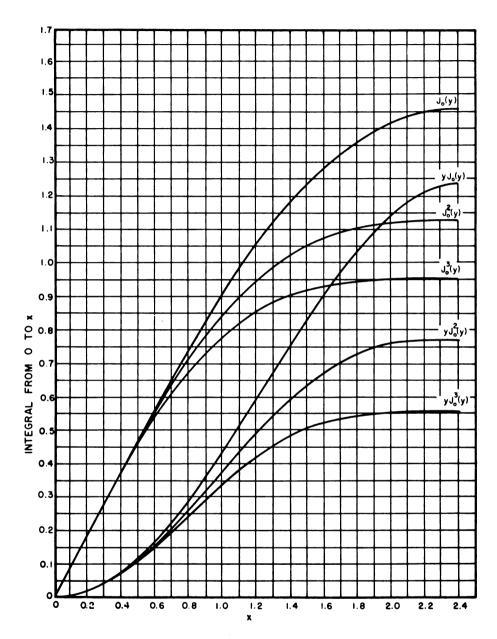


Fig. 1.6.44 — Integrals of Bessel Functions. Reprinted from Wheeler, Principles of Nuclear Power, N-2292. Shows  $\int_0^x F(y) dy$ , for F(y) as indicated on the curves.

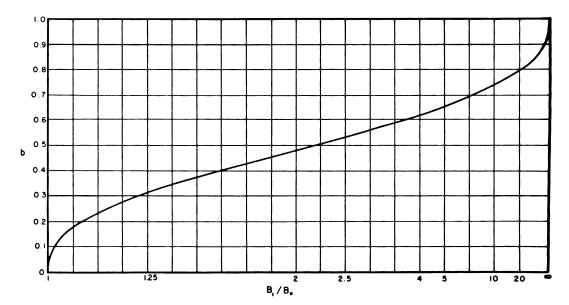


Fig. 1.6.45 — Spherical Control Region. Reprinted from Wheeler, Principles of Nuclear Power, N-2292. Concentric control region in spherical reactor; b = control region radius + reactor radius; B = total buckling.

When large amounts of control are to be applied, the neutron flux is appreciably disturbed and the flux-squared rule no longer holds.* A principle frequently followed in large control is to apply it strongly enough in a central region of the reactor so as to flatten the flux there. The size of this central region is then adjusted so as to accomplish the desired amount of control of the reactor as a whole.

Figure 1.6.45 shows the size of the flat-flux central region needed to achieve a specified degree of control in a bare spherical reactor; Figs. 1.6.46 and 1.6.47 do the same for full-length cylindrical control regions in bare, circular and rectangular reactors. Again the efficiency of control exerted in a central core is seen to be a few times larger than if spread throughout the reactor.

When flux flattening is to be accomplished by control rods, they are arranged in a regular lattice array throughout the control region, and their size and spacing are adjusted so as to just reduce the (radial) buckling  $B_1$  to zero. The resulting relationship is approximately:⁴³

$$N_0(br_0) - \frac{N_1(br_2)}{J_1(br_2)} J_0(br_0) = \frac{\tau}{L^2} i H_0^{(1)} (i K r_0)$$
 (172) †

where  $r_2$  = equivalent (area-wire) radius of the lattice cell associated with each rod,  $b^2$  =  $B_1$  = buckling neutralized by the rod, and the other quantities are as in Eq. (170). For small arguments in the Bessel functions, this becomes:^{33,44}

^{*}The corresponding weighting factor would now be the product of the disturbed and undisturbed fluxes.

[†] Described by  $\frac{B_1 - B_0}{B_1}$   $\frac{\text{total volume}}{\text{core volume}}$ 

[!] Wheeler's Figure 22.5.23 is a nomograph for solving this equation.

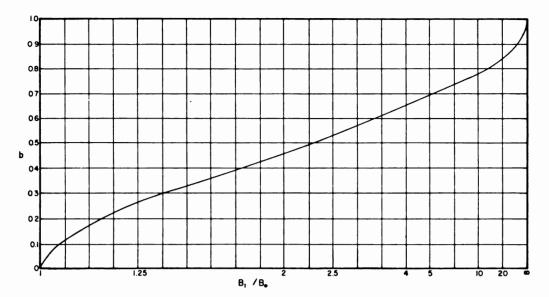


Fig. 1.6.46—Cylindrical Control Region. Reprinted from Wheeler, Principles of Nuclear Power, N-2292. Full length concentric control region in a cylindrical reactor. Radius of control region + radius of reactor = b; B = radial buckling.

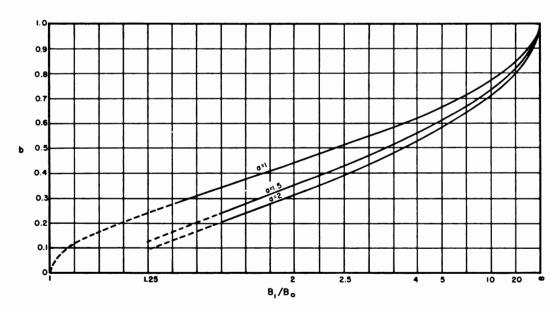


Fig. 1.6.47 — Rectangular Control Region. Reprinted from Wheeler, Principles of Nuclear Power, N-2292. Full-length rectangular control region in rectangular prism reactor. Length of reactor rectangle + width of reactor rectangle = a. Between reactor rectangle and the control rectangle within it, is a constant thickness border all around. Width of control rectangle + width of reactor rectangle = b.  $B_1$  = transverse (after longitudinal cosine component is removed) buckling outside the control region;  $B_0$  = critical uniform transverse buckling for entire reactor rectangle. Calculations approximate and less reliable where lines are dashed. The reference report also gives upper bounds to b.

$$b^{2} = \frac{2}{r_{2}^{2}} \left( \ln \frac{1.123}{br_{0}} + \frac{\tau}{L^{2}} \ln \frac{1.123}{Kr_{0}} \right)^{-1}$$
 (173)

The effective change in multiplication factor within the control region thus brought about by the rod bank is  $\Delta k = b^2(\tau + L^2)$ .

#### CONTROL BOUNDARIES

Circle of radius a

Semi-circle of radius a

 $30^{\circ}-60^{\circ}-90^{\circ}$  triangle of hypotenuse a

Equilateral triangle of altitude a

45°-45°-90° triangle of leg a

Square of side a

The action of a control rod as considered above is, in effect, to insert into the reactor a boundary (e.g., of radius  $r_0$ ) at which the thermal (or both thermal and fast) flux vanishes. Such black boundaries can be imagined in various shapes and arrangements, and (when considered to cause all neutron fluxes to vanish) hence create different shapes or volumes for the reactor. In certain geometrically simple cases,* the resulting control effect can be readily found. For example, a black sheet passing through the center of a bare spherical reactor converts it into two bare hemispheres, and the resulting effect on the buckling required can be obtained from Table 1.4.3. Table 1.6.8 gives buckling values for some additional cylindrical shapes.

Buckling relative to circle Cross section of cylinder Buckling for same area  $(2.405/a)^2$  $2(\pi/a)^{2}$ 1.0865

Table 1.6.8 — Buckling Values for Cylindrical Shapes*

 $4(\pi/a)^2$ 

 $5(\pi/a)^2$ 

 $(3.832/a)^2$ 

 $112/9 (\pi/a)^2$ 

# **GAPS**

Separation of the reactor core into halves with an adjustable gap between them for control purposes has been envisaged (sometimes with the aim of not disturbing the power pattern in planes parallel to the gap). The BNL reactor has a transverse gap (though not for control purposes) and a comprehensive review of gap theory is in preparation.

Figure 1.6.48 gives experimental results on the reactivity effect of gaps of variable thickness and shows calculated results for comparison.

[†]Chernick and Kaplan⁴⁹ include comparison of theory with experimental results of Callihan et al, ⁵⁰ on a split water-moderated machine. Reference (51) gives some discussion of gap theory.



1.2546

1.2694

1.3581

1.4637

^{*} From a preliminary and incomplete ORNL table by Sangren. The values given are for the transverse buckling only; for finite height H of the cylinder there is an additive term  $(\pi/H)^2$  in the total buckling

^{*}Wheeler⁴⁵ illustrates a number of these and, for  $\mu_1$  of cylindrical sectors in Table 1.4.3, gives the approximate expression  $1 + 1.861^{\frac{1}{10}}$ .

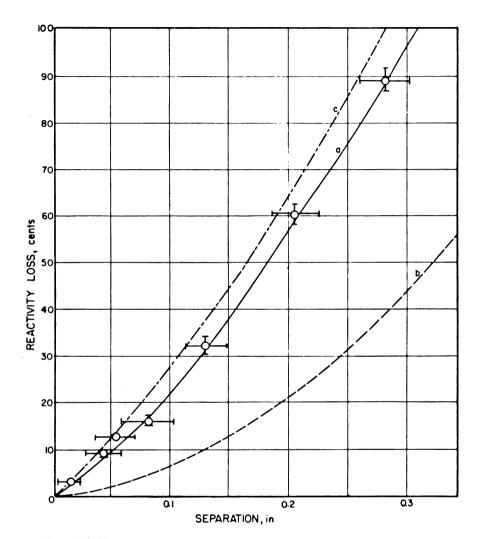


Fig. 1.6.48 — Reactivity Effect of Transverse Gap. Reprinted from Tamor, ORNL-1320. (a) Experimental results in a homogeneous 25-graphite critical experiment; (b) calculated from the theory of Goldberger and Wilkins (CP-3443); and (c) calculated from an extension of that theory.

#### REFERENCES

- 1. A. M. Weinberg, Theory of Oscillating Absorber in a Chain Reactor, AECD-2044, June 7, 1948.
- 2. Sylvan Wallach, Solutions of the Pile Kinetic Equation When the Reactivity is a Linear Function of the Time, WAPD-13.
- 3. Coveyou and Mulliken, AECD-2407.
- 4. Reactor Physics Progress Report, KAPL-706, April 1952, p 22 (classified).
- 5. Reactor Physics Progress Report, KAPL-706, April 1952 (classified).
- 6. Reactor Physics Progress Report, KAPL-706, April 1952, p 25 (classified).
- 7. H. Hurwitz, Nucleonics, July 1949, p 61.
- 8. R. R. Coveyou, YF-10-74.
- 9. Reactor Phys. Prog. Rep., loc cit, p 28.
- 10. G. M. Roe, KAPL, personal communication (classified).
- 11. Morehouse and Young, CP-1069 (A-1460) (classified).
- 12. Chernick, BNL-126 (classified).
- 13. HKF-109, p 3.19 (classified).
- 14. ORNL-730, July 6, 1950, p 64 (classified).
- 15. T. Welton, CF-52-10-107, Oct. 17, 1952 (classified).
- 16. BNL-173.
- 17. BNL-113, Aug. 1951 (classified).
- 18. KAPL-565 (classified).
- 19. Nordheim, CP-2589 (classified).
- 20. H. Hurwitz, KAPL-646, Dec. 20, 1951, p 23 (classified).
- 21. WAPD-34, Vol. I (classified).
- 22. Brown and Campbell Servomechanisms, John Wiley and Sons, New York.
- 23. Reactor Phys. Prog. Rep., loc cit, p 21.
- 24. Transfer Function of Argonne CP-2, Nucleonics 10, No. 8, Aug. 1952.
- 25. K. Donelian and J. Menke, MonP-379 (classified).
- 26. HKF-109, Chapter III (classified).
- 27. Welton, ORNL-1121 (classified).
- 28. WAPD-34 (RM-90) (classified).
- 29. Glasstone and Edlund, The Elements of Nuclear Reactor Theory, D. Van Nostrand Co., Inc., New York, 1952.
- 30, Gale Young, MonP-457 (classified).
- 31. KAPL-847, to be published (classified).
- 32. Kaplan and Chernick, BNL-152, pp 50-59 (classified).
- 33. Wigner et al, CP-1461 (classified).
- 34. Adler, MT-222.
- 35. Webster, NEPA-650 (classified).
- 36. Deleted.
- 37. CP-3581 (classified).
- 38. Murray, CP-1235.
- 39. Wheeler, N-2292 (classified), Sect. 22.6.10 to 22.6.12.
- 40. Wheeler, N-2292 (classified), Sect. 22.3.63.
- 41. Kaplan and Chemick, loc cit, p 70f.
- 42. Chicago Handbook, IVE, p 25 (classified).
- 43. Wheeler, loc cit, Sect. 22.5.22.
- 44. Chicago Handbook IVE, p 28 (classified).
- 45. Wheeler, loc cit, Fig. 22.3.69.
- 46. Wash-24 (classified).
- 47. ORNL-1177 (classified).
- 48. Bendt, MonP-385 (classified).
- 49. Chernick and Kaplan, BNL-182 (in draft form as BNL log C-6150) (classified).
- 50. Callihan et al, K-126, Fig. 14 (classified).
- 51. Kaplan and Chernick, loc cit, p 37ff.
- 52. Kaplan and Chemick, loc cit, p 58f.
- 53. Deleted.
- 54. Visner, ORNL-CF-52-9-9 (classified).
- 55. Miles et al, TID-2001, p 10 (classified).
- 56. Callihan et al, ORNL-1227 (classified).
- 57. Callihan et al, ORNL-1294 (classified).
- 58. Lichtenberger, ORNL Reactor Physics Conference, Sept. 10-12, 1952 (classified).
- 59. Kaplan and Chernick, loc cit, p 68.
- 60. Wheeler, loc cit, Sect. 22.4.18.
- 61. Webster, loc cit, p 27.
- 62. Wheeler, loc cit, Sect. 22.4.20.
- 63, Marshall, CP-718 (classified).
- 64. Zinn and Anderson, CP-510 (classified).

# Section 2 RADIATION SHIELDING

Prepared by

OAK RIDGE NATIONAL LABORATORY with parts by

NUCLEAR DEVELOPMENT ASSOCIATES and

NATIONAL BUREAU OF STANDARDS

# **Acknowledgments**

This section could not have been completed without the devoted efforts of Mrs. Lorraine Swift Abbott, the section editor. In addition to attending to the myriad details of submitting so many documents for publication, she has made real contributions to the subject matter by extensive use of the ORNL library. Her clarification of the presentations, in particular the tables of data, has materially enhanced the utility of the work.

Similar credit should be accorded to Mrs. May King Hullings; whose contributions have been catholic and competent. Much of the computing, preparation of some of the tables and graphs, some of the editing, and part of the expediting comprise her notable contributions.

For assistance in preparation of Chapter 2.2, thanks are due to Karl Z. Morgan. In Chapter 2.3, Gladys White contributed many of the tables and undertook a major share of the editorial work. Ann T. Nelms did a considerable share of the early editorial work, and Ida E. Hornstein had some part in the latter stages of the editorial work. Lewis V. Spencer and John Doggett contributed the tables of asymptotic constants so indicated, which are previously unpublished.

Permission of H. L. F. Enlund is gratefully acknowledged for the inclusion in Chapter 2.7 of his treatment of shield heating from capture-gamma rays.

The chapter on materials has been prepared with considerable assistance from Mrs. Abbott and Mrs. Hullings, aforementioned, as well as A. S. Kitzes, who reviewed the treatment of cements, concretes, and boral. H. L. F. Enlund helped by reviewing the chapter in its early stages.

The appendix on constants and conversion factors was prepared by Philip Mittelman of NDA.

Finally, the Information and Reports Division of ORNL is to be thanked for its competent work in publishing the drafts and particularly for the art work in which much effort was expended toward satisfying the needs of the individual authors.

E. P. Blizard April 24, 1953



# **Author's Preface**

In spite of some five years of research, exact calculational methods of shield design are still hopelessly complicated, and it appears likely that simpler approximations may never be adequate in many cases. As a consequence, the approach to the problem has turned to a cataloguing of solutions which have been obtained by experiment or machine calculation and to developing methods of tailoring these solutions to new problems.

In the case of gamma-ray attenuation through homogeneous media of a single element, the polynomial method of Spencer and Fano is being exploited in a joint program by the National Bureau of Standards and Nuclear Development Associates, and the early results of this program are presented in this section. Solution to more complicated gamma-ray attenuation problems for several regions or for mixtures of materials has no more than begun, and cataloguing of these results will be a much more extensive effort. Experiments such as those of Hayward and Hubbell on back-scattering and of Kirn, Kennedy, and Wyckoff¹ on oblique penetration are examples of the experiments required to solve many shielding problems which become extremely complicated in the analytical approach. It has been suggested that the Monte Carlo method lends itself well to such problems, but this has not yet been demonstrated.

The neutron attenuation problems of most interest in reactor shielding are those of the penetration of hard neutrons through large thicknesses of hydrogenous material (usually water). Enough experimental information has been gathered to check simple theories of this attenuation so that for most cases an adequate solution can be had either from basic calculations using shielding-experiment ("effective removal") cross sections or from direct geometrical transformation of an experimental result. This class of problems can include appreciable quantities of other materials (e.g., iron, lead, beryllium), provided they are located close to the source and followed by at least 50 cm of water or its equivalent.

The fast-neutron attenuation of thick nonhydrogenous shields is but poorly understood and almost unexplored experimentally. Concretes, which are intermediate in hydrogen content ( $\sim 1$  percent by weight), have been measured to some extent.

The compound problem of neutron and gamma attenuation in which neutron-induced gamma rays dominate has not been essayed analytically with any simple success. The very few calculations which have been tried have succumbed to hopeless complications and have been dropped. The experimental approach, on the other hand, has been quite adequate, especially since the development of optimization techniques. No relief seems to be in the offing, however, from the continued need for an experiment for each new situation. Eventually, perhaps enough data will be available to warrant an ordered catalogue of results from which new problems can be solved by interpolation between old experiments.

Basic information, such as cross sections and fission yields, although much of it is now available, is not by any means completely at hand, so that some of the shield designs must rest on conjecture. Although quite some effort has been spent on refining these conjectures, such as the calculations of cross sections carried out by NDA, the results are, of course, not quite as reliable as experimental results, and the latter are therefore much needed.

¹References appear at end of Preface.

#### AUTHOR'S PREFACE

In view of the unsettled state of the shielding art, this section does not offer recipes for every situation, although probably enough information is given to permit a fairly respectable reactor-shield design. In most cases, however, it will be necessary to refer to other works, in particular to experimental results too voluminous to include in a handbook.

In Chapter 2.1, the known information regarding the fission sources of neutrons and gamma rays is given. Although fission-product radiations are treated, no compilation is made of the radiations from other nuclides with the exception of capture-gamma radiations.

Chapter 2.2 treats the current opinions on radiation tolerances as used at ORNL.

For Chapter 2.3, on gamma-ray attenuation, we were most fortunate in being able to enlist the services of the National Bureau of Standards and Nuclear Development Associates, which organizations have had most to do with developing a useful method and its exploitation.

Chapter 2.4 on neutron attenuation treats a much less satisfactory art, giving a correspondingly less analytical treatment, which nevertheless is as complete as we were able to make it at the time of writing (1952).

Chapter 2.5 on geometry is essentially an introduction to the art of applying the results of experiments to new source-receiver configurations. Since this chapter was prepared (early 1952), another treatment has appeared which will also be useful.⁴

Chapter 2.6, which treats ducts through shields, gives the phenomenological treatment of this problem, taking parameters from mockup experiments rather than relying on the complicated analysis which evolves from a start with cross sections.

Chapter 2.7 on heating in shields treats a problem which must depend to some extent on the basic attenuation calculations themselves, although the region of interest for heating is generally that of much smaller attenuations for which different methods are applicable.

Chapter 2.8 shows how standard treatments of extremum problems are applied to shield design.

Chapter 2.9 on shield materials treats a very voluminous subject with an attempt at brevity. This chapter is one which is sure to grow with the nuclear energy business.

# REFERENCES

- S. Kirn, R. J. Kennedy, and H. O. Wyckoff, Oblique Attenuation of Gamma-rays from Cobalt-60 and Cesium-137 in Polyethylene, Concrete, and Lead, NBS-2125, Dec. 23, 1952.
- 2. B. T. Feld, H. Feshbach, M. L. Goldberger, H. Goldstein, and V. F. Weisskopf, Final Report of the Fast Neutron Data Project, NYO-636, Jan. 31, 1951.
- 3. H. Goldstein, Some Fast-neutron Measurements Needed for Shielding Studies, NYO-640, Aug. 24, 1951 (classified).
- 4. M. L. Storm, H. Hurwitz, Jr., and G. M. Roe, Gamma-ray Absorption Distributions for Plane, Spherical, and Cylindrical Geometries, KAPL-783, July 24, 1953 (classified).

# NOTE TO THE DECLASSIFIED EDITION

This declassified section has been prepared by deleting classified information from the original version. No effort has been made to revise or bring up to date the remaining material, which was based upon information available up to about April 1952.

As one might expect, considerable advances have been made since this section was originally written. As a guide to the literature up to October 1, 1954, the reader is referred to "Radiation Shields and Shielding; A Bibliography of Unclassified AEC Report Literature," TID-3032 and TID-3032 (Suppl. 1).



#### CHAPTER 2.1

# Sources of Radiation

# E. P. Blizard and F. C. Maienschein

# RADIOACTIVE NUCLEI

The radiations from radioactive nuclei are given in a number of unclassified reference charts¹⁻³ which are not reproduced here.

# RADIATIONS FROM FISSION

#### PROMPT NEUTRONS

The distribution of neutrons from the thermal fission of  $U^{235}$  is well approximated by Watt's^{4,5} empirical formula:

$$N(E) dE = \sqrt{\frac{2}{\pi e}} \sinh \sqrt{2E} e^{-E} dE$$
 (1)

where N(E) dE is the number of neutrons of energies E to E + dE per neutron emitted, and E is the neutron energy in millions of electron volts. The fission spectrum of the neutrons from  $Pu^{239}$  is about the same. Watt's expression (1) is given in Table 2.1.1 and Fig. 2.1.1.

E, mev	N(E), mev ⁻¹	E, mev	N(E), mev ⁻¹	E, mev	N(E), mev ⁻¹
0	0	1.3	$3.180 \times 10^{-1}$	5.0	3.849 × 10 ⁻¹
0.1	$2.027 \times 10^{-1}$	1.4	$3.073 \times 10^{-1}$	6.0	$1.808 \times 10^{-2}$
.2	$2.678 \times 10^{-1}$	1.5	$2.955 \times 10^{-1}$	7.0	$9.314 \times 10^{-3}$
.3	$3.060 \times 10^{-1}$	1.6	$2.842 \times 10^{-1}$	8.0	$4.424 \times 10^{-3}$
.4	$3.303 \times 10^{-1}$	1.7	$2.729 \times 10^{-1}$	9.0	$2.074 \times 10^{-3}$
.5	$3.454 \times 10^{-1}$	1.8	$2.602 \times 10^{-1}$	10.0	9.538 × 10 ⁻⁴
.6	$3.525 \times 10^{-1}$	1.9	$2.498 \times 10^{-1}$	11.0	4.400 × 10 ⁻⁴
<b>.7</b> .	$3.559 \times 10^{-1}$	2.0	$2.369 \times 10^{-1}$	12.0	1.995 × 10 ⁻⁴
.8	$3.543 \times 10^{-1}$	2.5	$1.839 \times 10^{-1}$	13.0	8.969 × 10 ⁻⁶
.9	$3.512 \times 10^{-1}$	3.0	$1.387 \times 10^{-1}$	14.0	3.997 × 10 ⁻¹
1.0	$3.444 \times 10^{-1}$	3.5	$1.026 \times 10^{-1}$	15.0	$1.772 \times 10^{-9}$
1.1	$3.366 \times 10^{-1}$	4.0	$7.470 \times 10^{-2}$		
1.2	$3.272 \times 10^{-1}$	4.5	$5.381 \times 10^{-2}$		

¹References appear at end of chapter.

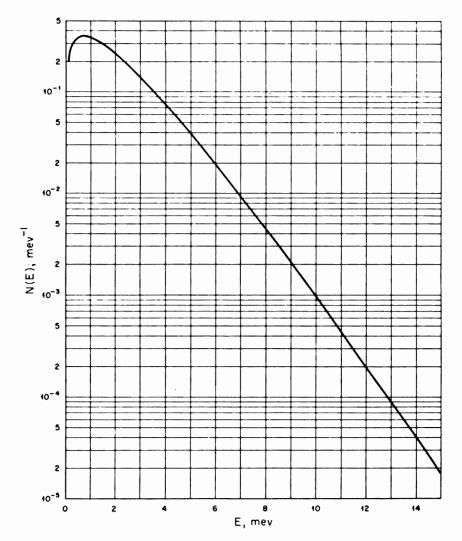


Fig. 2.1.1 — Watt's Spectrum of Fission Neutrons. Submitted by Oak Ridge National Laboratory, Sept. 10, 1952.

An approximate form for the fission spectrum for large E is:

$$N(E) dE = \frac{1}{\sqrt{2\pi e}} e^{-(E - \sqrt{2E})} dE$$
 (2)

For a fit in slope and magnitude at any energy  $E_0$ , the following form can be used for  $E_0 > 3$  mev:

$$N(E) dE = \frac{1}{\sqrt{2\pi e}} e^{\sqrt{E_0/2} - (1 - 1/\sqrt{2E_0})E} dE$$
(3)

If this form is fit at 8 mev, the result is:

$$N(E) dE \approx 1.8e^{-0.75E} dE$$
 (4)

The data which the above formulas fit include measurements of energies up to 17 mev.

SOURCES OF RADIATION CHAP. 2.1

## PROMPT GAMMA RAYS

The two measurements of prompt gamma rays of fission agree in total energy but not in average energy per photon. Neither of the two experiments is very precise, but that of Deutsch and Rotblat is usually used, although the justification for this is not convincing. Any calculation should allow for the possibility that either is correct. The data are given in Table 2.1.2.

Table 2.1.2 — Gamma-radiation Energies from Fission

Total energy per fission, mev	Average energy per photon, mev	Reference
5.1 ± 0.3	1	7
$4.6 \pm 0.1$	2.5	8

## FISSION PRODUCTS

## GAMMA RAYS

The data on the relative yields of the various fission products have been summarized elsewhere. 9,10 

The gross gamma activity of fission products can be estimated by use of the expressions listed in Table 2.1.3. Although the data are not complete for either Pu²³⁹ or U²³⁵ fission products, there is probably not much difference in the gamma-activities of their fission products.

Table 2.1.3 — Delayed Gammas from Fission Products

Rate			Fissioning	
Mev/(sec)(fission)*	C/fission	Validity	isotope	Reference
	4 × 10 ⁻¹¹ †	0-1.7 msec	Pu ²³⁹	12
	$2 \times 10^{-11}$ †	1.7 -3.4 msec	Pu ²³⁹	12
	1 × 10 ⁻¹¹	40-140 msec	U ²³⁵	13
0.90t ^{-1.20}	(constant)	10 sec - 1 day	U ²³⁵	1 <b>4</b> , 15
4.2t-1.28		20 min -3 days	U ²³⁵	14, 16
49.0t ^{-1.41}		50-100 days	U ²³⁵	14, 16

^{*}Gamma source strength, mev/sec, at t sec after one fission

For times after irradiation longer than about 3 hr, the hard gamma rays can be identified with relatively few individual emitters¹¹ shown in Table 2.1.4.

# **DELAYED NEUTRONS**

Delayed neutrons are defined as those emitted at measurable times after fission. The delayed neutrons that are important from the shielding viewpoint are listed in Table 2.1.5.

[†]Activity relative to radium source in equilibrium with its decay products

Table 2.1.4 — Fission-fragment Hard-gamma Emitters

Nuclides†	Half-life†	U ²³⁵ fission yield, %‡	Yield per decay, %‡	Energy, mev
Ru ¹⁰⁶ , Rh ¹⁰⁶	1 yr, 30 sec	0.48	2	2.917
Ce144, Pr144	275 days, 17.5 min	5.3	Weak	>D ¹⁷
•	•		2	2.185 ¹⁷
			2	2.6 ¹⁸
Eu 156	15.4 days	0.013	60	219
Ba ¹⁴⁰ , La ¹⁴⁰	12.8 days, 40 hr	6.1	3.2	2.5 ²⁰
$Te^{132}$ , $I^{132}$	77.7 hr, ²¹ 2.4 hr	4.521	2.7	$2.0^{22,23}$
Te ¹³¹ *, Te ¹³¹	30 hr, 25 min	0.45 ²¹	21.6	>D ²³
I ¹³⁵	6.7 hr	5.6	1.95	2.424
			4	1.8 ²⁵
Kr ⁸⁸ , Rb ⁸⁸	2.77 hr, 17.8 min	3.15	< 15	$2.8^{26}$
•	•		19-34	$1.85^{26}$

†If two entries occur, they refer to parent and daughter, and the latter is the hard-gamma emitter

‡Multiply third and fourth columns to obtain gamma photons per 10⁴ fissions

§Interpolated value

Table 2.1.5 — Delayed Neutrons

(D. J. Hughes, Delayed Neutrons, CF-3596, Feb. 1946)

Absolute yields per 10⁴ neutrons emitted (prompt and delayed)

		φ.σ.	(prompt and delayed)			
Half-life, sec	Energy, kev	U ²³⁵	U ²³³	Pu ²³⁹		
55 <b>.6</b>	250	2.5	1.8	1.4		
22.0	570	16.6	5.8	10.5		
4.51	412	21.3	8.6	12.6		
1.52	670	24.1	6.2			
0.43	400	8.5	1.8	11.9		
	Total	73.0	24.2	36 <b>.4</b>		

## SECONDARY SOURCES OF RADIATION

Secondary gamma radiation, produced by neutron reactions, consists of two important types: (1) capture-gamma radiation and (2) gamma rays from inelastic scattering. Secondary neutrons are produced by the photoneutron process. Secondary radiations are of considerable importance since it is because of these that a single type of shielding (e.g., water for neutrons) is often inadequate, being relatively transparent for the secondary radiation.

## CAPTURE GAMMAS

When a neutron is captured by a nucleus, a new nucleus is formed in an excited state. The excitation energy, or binding energy of the neutron in the new nucleus, may be dissipated almost at once ( $\sim 10^{-13}$  sec) by the emission of one or more gamma rays (for ex-

SOURCES OF RADIATION CHAP. 2.1

Table 2 1 6	Light Isotones	: liseful for	Suppression of	Capture Gamma	Radiation

Isotope	Charged particle reaction	Percent of radiative captures	Total absorption cross section, barns	Total energy of gamma rays, mev
Li ⁶	$(n, \alpha)$	0	910	• • •
$\mathbf{B}^{10}$	$(\mathbf{n}, \boldsymbol{\alpha})$	93	3800	0.48
N14	(n,p)	6	1.7	10.8*

*B. B. Kinsey (Ref.²⁹, Table 2.1.7) gives the spectral distribution of the harder nitrogen captive gamma rays as follows

Line	Energy, mev	Intensity relative to A
A	10.816 ± 0.015	1.00
В	$9.156 \pm .030$	0.09
С	$8.278 \pm .016$	.19
D	$7.356 \pm .012$	.56
E	$7.164 \pm .010$	.19
F	$6.318 \pm .010$	.9
G	$5.554 \pm .010$	1.5
H	$5.287 \pm .010$	2.3
I	$4.485 \pm .010$	0.8

ceptions see Table 2.1.6). For the light elements and magic* nuclei only a single gamma ray may be emitted with an energy corresponding to the binding energy. For other nuclei many gamma rays are emitted in competition with the ground-state transition. Table 2.1.7 presents a summary of capture-gamma-ray spectra that have been investigated.

The following instruments have been used for measuring capture-gamma-ray spectra:

- (1) A pair spectrometer, which utilizes magnetic deflection of electron pairs in order to determine their energies. This instrument permits high resolution and has thus shown the presence of lines in capture-gamma-ray spectra. Determination of the energy dependence of the sensitivity for this spectrometer is rather difficult.
- (2) Deuterium-loaded nuclear plates in which photoproton tracks are observed. This technique yields less resolution than the pair-spectrometer method and requires a considerable investment of time in reading the plates.
- (3) Scintillation spectrometers, which have been adapted only recently to the study of capture-gamma-ray spectra. This method may yield considerable information in the future with somewhat poorer resolution than the pair spectrometer method. The resolution would be quite adequate for shielding purposes, however, and the sensitivity should be higher.

## **INELASTIC SCATTERING GAMMAS**

The capture-gamma-ray process described above is the most important reaction for neutrons of low energy. For higher neutron energies, however, it is possible that the compound nucleus formed upon neutron capture may re-emit a neutron, leaving the residual nucleus in an excited state which subsequently decays by the emission of one or more gamma rays. In contrast to capture gamma rays, inelastic-scattering gamma rays will have a total energy less than that of the incident neutron.

^{*}Magic nuclei are those having closed, or nearly closed, shells of nucleons so that they behave much as light nuclei. Notable examples are lead and bismuth, which although they are heavy nuclei, nevertheless give a single capture gamma photon per capture, a property usually characteristic of the lighter nuclei.

Table 2.1.7 — Capture-gamma-ray Data

Target nucleus	Spectral type*	Binding energy,† mev	References
H ¹	1	2.23	27
Li [¢]	3	•••	28
Be ⁹	1	$6.797 \pm 0.008$	29
B ¹⁰	3	•••	28
C12	1	$4.948 \pm 0.008$	29
N ¹⁴	2	$10.823 \pm .012$	29
F ¹⁹	1	$6.60 \pm .03$	30
Na ²³	2	$6.961 \pm .012$	30, 31
Mg ^{24, 25, 26}	2	$7.334 \pm .012 (24)$	30
Al ²⁷	1	$7.724 \pm .10$	30, 32, 33
Si ^{28,29,30}	2	8.476 ± .13 (28)	30
P ³¹	2	$7.94 \pm .03$	34
S ³²	2	$8.64 \pm .02$	34
Cl ³⁵	2	8.56 ± .03	<b>34</b>
K38	2	$7.77 \pm .03$	31, 35, 36
Ca ⁴⁰	2	•••	36
<b>M</b> n ⁵⁵	1	$7.25 \pm 0.03$	33, 35, 37, 38
Fe ⁵⁶	1	$7.63 \pm .01$	33, 35, 37
Co ⁵³	2	$7.73 \pm .04$	35, 37
Ni ⁵⁸	1	9.01 ± .03	35
Ni ⁶⁰	1	8.55 ± .03	35
Cus, &	1	$7.91 \pm .01 (63)$	35
Br ^{79,81}	2	8.5 - 9.0	32
Ag ^{107, 109}	2	~8.0	37
Cd113	2	~ 7.5	31, 32
In ¹¹⁵	2	7.0-7.5	37
La ¹³⁹	2	7.5 - 8.0	32
w .	2	7 <b>.4</b>	39
Au ¹⁹⁷	2	9.0-9.5	32
Hg	2	8.0 - 8.5	32
Pb ²⁰⁶	1	$6.734 \pm 0.008$	36
$Pb^{207}$	1	$7.380 \pm .008$	36
Bi ²⁰⁹	1	$4.170 \pm .015$	36
U ²³⁵	2	~5‡	

^{*1,} ground-state transition predominates; 2, ground-state transition does not predominate; 3, charged-particle reaction

Only a very few measurements have been made of gamma-ray spectra from inelastic scattering. Data on gamma-ray energies and inelastic cross sections are available for 2.5-mev neutrons for several light nuclei.⁴⁰ In recent experiments with 15-mev neutrons, determinations of the energies of inelastically scattered neutrons from light and magic nuclei showed a reduction in neutron energy to about 2 mev.^{41,42} The gamma-ray energies were not experimentally determined, but by analogy with the neutron-capture process it may be presumed that light and magic nuclei will give rise to gamma rays which are harder than those of other nuclei.

[†]Isotope assignment, if any, is indicated in parentheses

[‡]E. P. Blizard, estimate only, based on calculation of gamma intensity near to an MTR-type reactor. This is gamma-ray emission on thermal neutron nonfission capture, which constitutes 15.5% of all capture processes

SOURCES OF RADIATION CHAP. 2.1

#### **PHOTONEUTRONS**

Photoneutron production, which may be considered the reverse of the neutron-capture process, comprises a secondary source of neutrons. In neutron capture, the neutron binding energy was made available to the gamma radiation. Consequently, in order for photoneutron production to take place, the incident gamma ray must have an energy at least equal to the neutron binding energy. For only two nuclei, D² (2.23 mev) and Be⁹ (1.67 mev), are these threshold energies low enough to allow an appreciable production of photoneutrons in shield materials.

Other threshold energies are listed in an extensive table published by Sher et al. ⁴³ Figure 2.1.2 shows the photoneutron cross sections for D² and Be⁹, together with the curve for Al²⁷, which is included to show the general shape of photoneutron cross-section curves for other nuclei. The curves shown in Fig. 2.1.2 are not theoretical but are merely an attempt to give a best fit to the experimental points. As may be seen from the scale used for the cross section, photoneutron cross sections are, in general, much smaller than neutron-capture or inelastic-scattering cross sections.

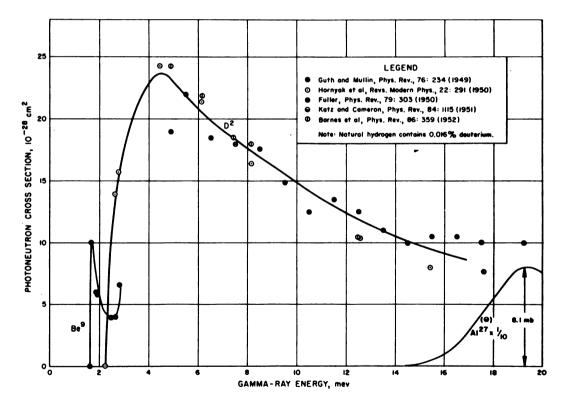


Fig. 2.1.2 — Photoneutron Cross Sections for Be³, Al²⁷, and D². Submitted by Oak Ridge National Laboratory, June 23, 1952.

#### REFERENCES

- 1. Chart of the Nuclides, prepared by Knolls Atomic Power Laboratory, General Electric Research Laboratory, 1950 edition.
- 2. W. H. Sullivan, "Trilinear Chart of Nuclear Species," John Wiley & Sons, Inc., New York, 1949,
- 3. E. Segrè, Segrè Isotope Chart, AECD-2111, April 1948; declassified July 21, 1948.
- 4. B. E. Watt, Energy Spectrum of Neutrons from Fissions Induced by Thermal Neutrons, LA-718, 52 PP. Dec. 17, 1948.
- 5. N. Nereson, Fission Neutron Spectrum of U235, Phys. Rev., 85, 600, 1952.
- 6. N. Nereson, The Fission Neutron Spectrum of Plutonium, LA-1078, 22 pp, Mar. 8, 1950; declassified July 16, 1952 (AECD-3428; LADC-1215).
- 7. M. Deutsch and J. Rotblat, Investigation of Fission Gamma Rays, LA-170, 22 pp. Nov. 13, 1944, declassified May 25, 1951.
- 8. B. B. Kinsey, R. C. Hanna, and D. Van Patter, Gamma Rays Produced in the Fission of U235, Can. J. Research, 26A: 79-98 (1948).
- 9. K. Way and N. Dismuke, Fission Product Yields, Oak Ridge National Laboratory, ORNL-280, 50 pp, May 18, 1950.
- C. D. Coryell and N. Sugarman, editors, "Radiochemical Studies: The Fission Products," pp 1381-1382 and 2018-2055, McGraw-Hill Book Company, Inc., New York, 1951.
- 11. W. K. Ergen, Hard Gamma Emitters among Fission Fragments, Aircraft Nuclear Propulsion Project, ANP-59, 25 pp, May 3, 1951.
- 12. I. Halpern and P. B. Moon, Short-Period Delayed Gammas from Fission of 25 and 49, LA-253-A, Dec. 7, 1945.
- 13. L. D. P. King and E. Fermi, quoted in reference 12.
- 14. K. Way and E. P. Wigner, The Rate of Decay of Fission Products, Phys. Rev., 73: 1318-1330 (1948); also appears as Paper 43, pp 436-458 in Coryell and Sugarman, op. cit. (10).
- 15. N. Sugarman, S. Katcoff, B. Finkle, N. Elliott, and J. D. Knight, Decay of Gross Fission Products after Short Irradiations. III. Counter Studies of y Activity and Energy, Paper 37, pp 371-386 in Coryell and Sugarman, op. cit. (10).
- L. B. Borst, Estimates of Amount of Radiation and of Accompanying Energy Liberation from Fission Products, Paper 34, pp 344-350 in Coryell and Sugarman, op. cit. (10).
- 17. D. E. Alburger, E. der Mateosian, M. Goldhaber, and S. Katcoff, Gamma-Rays in the Decay of Rh⁴⁶⁶ and Pr⁴¹¹, Phys. Rev., 82: 332 (1951).
- C. E. Mandeville and E. Shapiro, Radiations from Cerium (144) Praseodymium (144) Neodymium (144), Phys. Rev., 79: 243 (1950).
- L. Winsberg, Study of the Fission Chain 10h Sm⁽¹⁵⁶⁾-15.4d Eu⁽¹⁵⁶⁾, Paper 198, pp 1302-1310 in Coryell and Sugarman, op. cit. (10).
- B. Russell, D. Sachs, A. Wattenberg, and R. Fields, Yields of Neutrons from Photo-Neutron Sources, Phys. Rev., 73: 545-549 (1948).
- 21. A. C. Pappas and C. D. Coryell, Activities and Fission Yields in Chains of Masses 129 to 134, Phys. Rev., 81: 329 (1951).
- 22. F. C. Maienschein, J. K. Bair, and W. B. Baker, private communication with W. K. Ergen.
- 23. G. W. Parker, private communication with W. K. Ergen.
- H. A. Levy and M. H. Feldman, Hard Gamma Emitters in Fission, pp. 71-83(especially p 80) in J. A. Swartout, Chemistry
  Division Quarterly Progress Report for Period Ending June 30, 1949, Oak Ridge National Laboratory, ORNL-286, 236 pp. Sept. 14,
  1949.
- 25. A. D. Bogard, A. R. Brosi, et al, Calibration of Assay Equipment, pp 59-65 in E. H. Taylor, Report of the Chemistry Division for the Months March, April, May, 1948, Oak Ridge National Laboratory, ORNL-65, 187 pp, July 9, 1948.
- 26. M. E. Bunker, L. M. Langer, and R. J. D. Moffat, The Disintegration of Rb18, Phys. Rev., 81: 30-32 (1951).
- 27. R. E. Bell and L. G. Elliott, Gamma-Rays from the Reaction H¹(n,γ)D² and the Binding Energy of the Deuteron, Phys. Rev., 79: 282-285 (1950).
- 28. W. F. Hornyak, T. Lauritsen, P. Morrison, and W. A. Fowler, Energy Levels of Light Nuclei. III, Revs. Mod. Phys., 22: 291 (especially p 321) (1950).
- B. B. Kinsey, G. A. Bartholomew, and W. H. Walker, γ-rays Produced by Slow Neutron Capture in Beryllium, Carbon, and Nitrogen, Can. J. Phys., 29: 1-13 (1951).
- 30. B. B. Kinsey, G. A. Bartholomew, and W. H. Walker, Neutron Capture y-Rays from Fluorine, Sodium, Magnesium, Aluminum, and Silicon, Phys. Rev., 83: 519-534 (1951).
- 31. C. H. Millar, A. G. W. Cameron, and M. Glicksman, Gamma-ray Studies Using Deuterium-loaded Photographic Plates, Can. J. Res., 28A: 475-487 (1950).
- 32. B. Hamermesh, Neutron Capture Gamma-Ray Spectra, Phys. Rev., 80: 415-419 (1950).
- 33. B. Hamermesh and V. Hummel, Scintillation Counter Studies of Neutron Capture Gamma-Ray Spectra, Phys. Rev., 83: 663-664 (1951).
- 34. B. B. Kinsey, G. A. Bartholomew, and W. H. Walker, Neutron Capture γ-Rays from Phosphorus, Sulfur, Chlorine, Potassium, and Calcium, Phys. Rev., 85: 1012-1023 (1952).
- B. B. Kinsey, G. A. Bartholomew, and W. H. Walker, Transitions to the Ground States in Nuclei Excited by Slow Neutron Capture, Phys. Rev., 78: 481-482 (1950).
- 36. B. B. Kinsey, G. A. Bartholomew, and W. H. Walker, Neutron Capture γ-Rays from Lead and Bismuth, Phys. Rev., 82; 380-388 (1951).
- 37. B. Hamermesh, Odd-Even Effect in Neutron Capture Gamma-Ray Spectra, Phys. Rev., 81: 487 (1951).
- 38. R. W. Pringle and G. Isford, Scintillation Spectroscopy of the Gamma-Rays from Slow Neutron Capture in Manganese, Phys. Rev., 83: 467-468 (1951).
- 39. B. B. Kinsey, letter of Feb. 22, 1950, to E. P. Blizard.
- 40. M. A. Grace, L. E. Beghian, G. Preston, and H. Halban, The Inelastic Scattering of Fast Neutrons, Phys. Rev., 82: 969 (1951).
- 41. P. H. Stelson and C. Goodman, The Inelastic Scattering of 15-mev Neutrons by Lead, Iron, and Aluminum, Phys. Rev., 82:
- 42. B. G. Whitmore and G. E. Dennis, The Inelastic Scattering of Fast Neutrons in Lead and Bismuth, Phys. Rev., 84: 296-297 (1951).
- 43. R. Sher, J. Halpern, and A. K. Mann, Photoneutron Thresholds, Phys. Rev., 84: 387-394 (1951).



## **CHAPTER 2.2**

# Permissible Levels of Radiation

M. S. Fair

#### ROENTGEN

The roentgen is defined as "that quantity of X- or gamma-radiation such that the associated corpuscular emission per 0.001293 gm of air produces, in air, ions carrying one electrostatic unit (esu) of quantity of electricity of either sign."

The roentgen is a unit of X- or gamma-ray energy loss in 1 cc of dry air under standard conditions (0°C and 760 mm Hg). As defined, the roentgen is a unit of dose without reference to time or the energy of the ionizing radiation. Air was chosen as the absorption medium because it is convenient and because body tissue, water, and air all have approximately the same absorption value per gram for a wide range of radiation wavelength.

Within the 0.001293 gm of air, photoelectrons and Compton electrons will be formed by interaction of X- or gamma-rays with electrons of the atoms contained in the volume of air; pair electrons will be produced if the photon energy is more than twice the mass energy of the electron (>2  $\text{mc}^2 \doteq 1$  mev). The definition demands that all "associated corpuscular emission" be absorbed in air. Many of the particles will leave the volume (1 cc) in which they were formed, but they must remain in air until all their energy is dissipated. The 1-cc volume is the volume from which the secondaries originate and is not the volume from which the ions are collected.

Every ion produced by the secondaries must be measured. This means collecting all the ions formed in a volume that will be larger than the original volume of 1 cc.* This new volume will be determined by the energy of the X- or gamma-rays, which will determine the range of the secondaries. It is very important that the ions be collected before any of them have a chance to recombine. For each ionization event, two particles are produced, a positive and a negative; they are called an "ion pair." Either the positive or the negative charges may be collected and measured. Thus, it is seen that actually there are 2 esu of charge, 1 esu of positive and 1 esu of negative charge per cubic centimeter of air corresponding to a roentgen.

Since the charge on the electron is  $4.8 \times 10^{-10}$  esu, then the number of electrons per electrostatic unit is:

 $1/4.8 \times 10^{-10} = 2.083 \times 10^{9}$ 

This then is also the number of ion pairs (i.p.) per electrostatic unit, because only one partner of the ion pair is measured.

^{*}In practice, because of experimental convenience, the volume in which the secondary electrons are produced is probably many cubic centimeters of air. The resulting ions collected are divided by this volume in calculating the roentgens.

The mass of air referred to (0.001293 gm) is 1 cc of dry air at 0°C and 760 mm Hg. There are  $2.083 \times 10^9$  ion pairs per cubic centimeter per roentgen (by definition 1 r = 1 esu/cc) or:

1 
$$r = \frac{2.083 \times 10^9 \text{ i.p./cc}}{0.001293 \text{ gm/cc}} = 1.61 \times 10^{12} \left(\frac{\text{i.p.}}{\text{gm air}}\right)$$

If an average of 32.5 ev is expended by secondary electrons to form each ion pair in air, then:

1 r = 1.61 × 10¹² 
$$\frac{i.p.}{gm \ air}$$
 × 32.5  $\frac{ev}{i.p.}$  = 5.24 × 10¹³  $\frac{ev}{gm \ air}$ 

Since 1 ev is equal to  $1.6 \times 10^{-12}$  erg:

1 r = 5.24 × 10¹³ 
$$\frac{\text{ev}}{\text{gm air}}$$
 × 1.6 × 10⁻¹²  $\frac{\text{ergs}}{\text{ev}}$  = 83.8  $\frac{\text{ergs}}{\text{gm air}}$ 

To summarize:

1 r = 1 esu/cc (standard air)

 $= 2.083 \times 10^{9} \text{ i.p./cc}$ 

 $= 1.61 \times 10^{12} \text{ i.p./gm}$ 

 $= 5.24 \times 10^7 \text{ mev/gm}$ 

= 83.8 ergs/gm

 $= 6.77 \times 10^4 \text{ mev/cc}$ 

The roentgen is independent of the time required for ionization. A "dosage rate" given as roentgens per hour is commonly used. The product of the dosage rate (r/hr) and time (hr) gives the total dose.

The unit of dosage rate measured in roentgens per unit time must not be confused with gamma-ray intensity. Gamma-ray intensity is measured in energy units per unit area per unit time, such as ergs per square centimeter per second. Ionization intensity is measured in roentgens per unit time, in air.

The roentgen measures electrostatic units per cubic centimeter of air; therefore, a dose of 500 r given to a small part of the body will not have serious consequences, and as the volume exposed approaches zero, the energy absorption also approaches zero. A dose of 500 r over the entire body would represent a large absorption of ionizing energy and would probably result in death.

## **CURIE**

The curie was originally defined as that quantity of radon in radioactive equilibrium with 1 gm of radium. Since 1 gm of radium has about  $3.7 \times 10^{10}$  atoms disintegrating per second, this fact is a basis for the definition of the curie and is the unit applied to radioactive materials other than radium. Thus, 1 curie of  $P^{32}$ ,  $Na^{24}$ , or  $C^{14}$  means "the amount of the isotope necessary to provide disintegrations at the rate of  $3.700 \times 10^{20}$  atoms/sec." A useful formula for computing the activity of a given mass of a radioisotope is:

$$\mathbf{M} = \frac{130,000 \text{ G}}{\text{A T}}$$



where:

T is the half-life in days,

M is the activity in millicuries,

A is the atomic mass of the radioactive isotope,

G is the weight in micrograms.

For example, 1  $\mu$ g of Ca⁴⁵ (T = 180 days) has an activity of:

$$\mathbf{M} = \frac{130,000}{45 \times 180}$$

= 16 mC

It may be noted that the definition says  $3.700 \times 10^{10}$  disintegrations/sec and not  $3.700 \times 10^{10}$  particles emitted per second.* The number of particles emitted per second can only be obtained from a knowledge of the decay scheme. For example, Mn⁵² has a half-life of 6.5 days. It decays by positron emission in 35 percent of the transitions and by electron capture in 65 percent of the transitions. Therefore, 1 mC of Mn⁵² emits only  $0.35 \times 3.700 \times 10^7 = 1.3 \times 10^7$  particles/sec, even through there are  $3.700 \times 10^7$  d/sec.

The curie is not to be used as a measure of radiation dose delivered.

## ROENTGEN EQUIVALENT PHYSICAL (rep)

When dealing with radiations other than photons or energy dissipation in tissue rather than in air, it is incorrect in the strict sense to use the roentgen, and a new unit of ionizing radiation dose is needed. In 1942, H. M. Parker defined a unit called the roentgen equivalent physical (rep) as that quantity of ionizing radiation that dissipates 83 ergs per gram of tissue.

Recently (since 1948), it has been common practice to use a slightly larger unit with the above definition but corresponding approximately to the energy loss in water or tissue (between 90 and 100 ergs/gm, depending upon the energy of the radiation and the specific ionization of the ionizing particle) when 83.8 ergs is dissipated in a small air cavity in the medium. The roentgen equivalent physical is "that quantity of any ionizing radiation (such as X-rays, gamma-rays, electrons, protons, neutrons) which is absorbed in tissue to the extent of 93 ergs per gram of tissue."

## ROENTGEN EQUIVALENT MAN (rem)

The roentgen equivalent man is defined as "that amount of radiation absorbed in tissue which has the relative biological equivalence in man of 1 r of X- or gamma-rays."

It has been determined experimentally that the secondary ionization from recoil protons produced by fast neutrons (2 mev) is about ten times (RBE = 10) as damaging as the same amount of energy absorbed from secondary electrons produced by X-rays.

For fast neutrons:

$$1 \text{ rem} = \frac{93}{10} \frac{\text{ergs}}{\text{gm tissue}} = 0.1 \text{ rep}$$

^{*}Distinction must be made between disintegrations per second (d/sec) and counts per second (c/sec). The latter term is frequently used in connection with radioisotope counting. The relationship is c/sec = f d/sec in which f is a correction factor for scattering, absorption, geometry, and counter efficiency.

The "additivity" of different types of radiation may be illustrated as follows:

30 mr/hr gamma = 30 mrem/hr 1.5 mrep/hr fast neutron = 15 mrem/hr 3500 slow neutrons/(cm²)(sec) = 15 mrem/hr Total = 60 mrem/hr

Table 2.2.1 gives the values of RBE, rep, rem, and the corresponding approximate flux values for the maximum permissible exposure to various types of radiation. These values correspond to those recommended by the United States Radiation Protection Committee and the values recommended by the United States, Great Britain, and Canada at the Chalk River conference September 29, 1949. It should be noted that these maximum permissible exposure rates are considered to be safe for a life-time exposure. In the emergency of atomic warfare, there would be justification in permitting exposures 100 times these values. Tables 2.2.2 and 2.2.3 give the maximum permissible operating levels used to control radioactive hazards at ORNL.

#### ROENTGENS PER HOUR AT UNIT DISTANCE

Source strength can be expressed conveniently in terms of roentgens per hour at a distance of 1 meter or 1 cm. The roentgens per hour at 1 meter is sometimes called an "rhm." This unit does not require a knowledge of the decay scheme of the source. Thus, 1 rhm of Co⁶⁰ is that amount of Co⁶⁰ whose unshielded gamma-rays produce 1 r/hr (in air) at a distance of 1 meter from the source. If this source is enclosed in a spherical shield so that at 1 meter 0.1 r/hr is measured, then the source strength is 0.1 rhm.

Many radium sources are enclosed in platinum tubes of either 0.5 or 1 mm thickness.

For 0.5-mm Pt:

S = 8.4 M

For 1-mm Pt:

S = 7.8 M

where:

S is the source strength in roentgens per hour at 1 cm

and:

M is the mass of radium in milligrams

For example, suppose we are given a 10-mg radium source enclosed in a 1-mm platinum filter. To find the roentgens per hour received at 2 meters from this source, we have:

 $7.8 \times 10 = 78 \text{ r/hr at 1 cm}$ 

Using the inverse square law, at 200 cm:

$$\frac{78}{(200)^2} = \frac{78}{40.000} = 1.95 \times 10^{-3} \text{ r/hr} = 1.95 \text{ mr/hr}$$

The wall of a gamma-measuring chamber should be made of material with an effective atomic number equal to that of air, and the chamber should be filled with air. This chamber may be as large as desired if sufficient voltage is applied across the chamber. If the wall is of material having an effective atomic number different from that of air, the inner wall should be lined with graphite or other similar material. The thickness of the wall should be equal to or greater than the maximum range of the secondary electron radiation. Since the effective atomic number of live tissue is about the same as that of air, an air wall chamber gives a good measurement of body exposure for X- and gamma-radiation.



Table 2.2.1 — Maximum Permissible Exposure in Terms of Flux Corresponding to 60 mrem per Day (300 mrem/wk on a 5-day work-week basis)*

		Approximate flux to give 1 MPE in 24-hr day†			
Type of radiation	RBE	General equation;	Example		
X- or gamma-ray	1	1500/CE photons/(cm ² )(sec)	1300 photons/(cm²)(sec) of 1 mev		
Beta	1	1600/SP beta rays/(cm ² )(sec)	17 betas/(cm ² )(sec) of 1 mev max. or 32 electrons/(cm ² )(sec) of 1 mev		
Fast neutrons	10	20/D fast neutrons/(cm ² )(sec)	22 fast neutrons/(cm ² )(sec) of 2 mev		
Thermal neutrons	5		600 thermal neutrons/(cm ² )(sec) of 0.02 ev		
Alpha (internal effects only)	20	80/SP alpha rays/(cm ² )(sec)	0.003 alpha rays/(cm ² )(sec) of 5 mev§		

^{*} Table by K. Z. Morgan

‡ C = 1 ± 0.2 from 70 kev to 4 mev; it is given more exactly by the equation: C =  $0.32(\mu - \sigma_s)10^5$ 

where:  $(\mu - \sigma_s)$  = total minus Compton scattering coefficient of absorption, cm⁻¹

E = energy, mev

S = specific ionization in air

P = mass stopping power in tissue relative to air

D = constant given approximately by the equation, D =  $1.2 - e^{-0.5E}$ 

§ Average value over the short range of alpha in tissue is 0.0016 alphas/(cm²)(sec) for 5 mev

Table 2.2.2 — Maximum Permissible Exposures to Personnel from External Sources

Type of radiation	Permissible exposure
Gamma	60 mr/day or 300 mr/week*
Beta	60 mrep/day or 300 mep/week*
Slow neutron	1750 neutrons/(cm ² )(sec)(8-hr day)
Fast neutron	66 neutrons/(cm ² )(sec)(8-hr day)

### Emergency exposure

In case of fire or other emergency, "AEC Contract Policy and Operations," Jan., 1951, stipulates the following:

The permissible limit for AEC emergency radiation monitoring teams, who normally would be exposed to some radiation in the course of regular duties, was placed at 10 r. The permissible emergency exposure for persons not exposed to radiation in the normal course of their occupations was set at 25 r

 $[\]dagger$  These values of flux correspond to  $60 \times 0.093/RBE$  ergs per gram of tissue and apply to the normal flux incident to body tissue. Backscattering is taken into account only in the case of thermal neutrons

^{*} Permissible exposure to the hands and forearms only 1.5 rep/week

Table 2.2.3 — Maximum Permissible Values for Beta-Gamma and Alpha Contamination at ORNL

	Indication of magnitude			
			Sme	eart
Type of contamination	µс/сс	β-γ*	$\beta\gamma$ , counts/min	γ, counts/min
Air concentration				
Without masks	$C_{11}$ , ‡ 3 × $10^{-11}$ , $\alpha$ 1st count, $10^{-8}$ , $\beta$ , $\gamma$			
With filter-type masks	$C_{LL}, \stackrel{1}{,} 10^{-8}, \alpha$ 1st count, $10^{-5}, \beta, \gamma$			
With positive air-supply masks	$C_{LL}$ , $\ddagger > 10^{-8}$ , $\gamma$ 1st count, $> 10^{-6}$ , $\beta$ , $\gamma$ §			
Water concentration				
Leaving settling basin	$1.5 \times 10^{-3}, \beta, \gamma$			
Leaving White Oak Lake	$10^{-6}$ , $\alpha$ , $\beta$ , $\gamma$			
In Clinch River	$10^{-7}$ , $\alpha$ , $\beta$ , $\gamma$			
Thyroid count for iodine content		400 counts/min (Bi GM)		
Surface or material				
Hand count (palm or back)		700 counts/min		
Protective clothing leaving laundry		1000 counts/min		
Personal clothing to be released from impoundment		500 counts/min		
Shoes, inside		1000 counts/min		<10
Shoes, outside		10,000 counts/min		<10
Hot laboratories (tables, floors, etc.)		Post area >7.5 mr/hr	< 200	<10
Acid bottles, acid carboys, gas cylinders		None detectable	< 20	<10
Material to X-10 shops		<1 mr/hr	< 50	<10
Equipment leaving X-10		<0.5 mr/hr	< 50	<10
Commercial carriers leaving X-10		<1 mr/hr	< 50	<10
AEC controlled carriers		Safe handling	< 200	<10
Isotope containers leaving X-10		Up to 200 mr/hr	< 50	<10
Burial ground (at ground level)		<7.5 mr/hr		
Salvage materials		<0.2 mr/hr	< 20	<10
Material to stores, glass shop, etc.		None detectable	< 20	<10
Lunchrooms and offices used as such		None detectable	< 20	<10
Floors in hallways, storage rooms, cold laboratories; table tops, janitors' closets, furniture		<0,2 mr/hr	< 50	<10
Instruments for Health Physics calibration		1000 counts/min	< 50	<10

^{*}There must be no detectable alphas with such instruments as Poppy, Zeuto, or Juno

[†]Beta smears counted at approximately 10% geometry; alpha smears counted at approximately 50% geometry ‡ Long-lived count; see George Koval, Determination of Particulate Air-borne Long-lived Activity, MDDC-1503, June 22, 1945

[£] Exposure to contaminated air while wearing positive air-supply masks is governed by external exposure levels

## SELECTED READING LIST

RADIOACTIVITY UNITS AND STANDARDS, R. D. Evans, Nucleonics 1: 32, Oct. 1947.

TENTATIVE DOSE UNITS FOR MIXED RADIATIONS, H. M. Parker, Radiology 54: 257, Feb. 1950.

NATIONAL BUREAU OF STANDARDS HANDBOOKS: H23, H27, H41, H42, H47, H48, H49, H50, H51.

DETERMINATION OF PARTICULATE AIR-BORNE LONG-LIVED ACTIVITY, George Koval, MDDC-1503, 8 p, June 22, 1945, declassified Dec. 1, 1947.

NUCLEAR SCIENCE IN ENGINEERING EDUCATION: A SELECTED LIST OF REFERENCES FOR INSTRUCTORS, TID-3011, 17 pp.

MAXIMUM PERMISSIBLE DOSE, K. Z. Morgan, AIHA Quarterly, Mar. 1953.

K. Z. Morgan, National Bureau of Standards Handbook, H52 (classified).

"Standards of Radiological Protection and Control" in THE ROLE OF ENGINEERING IN NUCLEAR ENERGY DEVELOPMENT, K. Z. Morgan. Third Annual Oak Ridge Summer Symposium; Aug. 27 to Sept. 7, 1951, TID-5031, Dec. 1951, p 176.

## CHAPTER 2.3

# Gamma-ray Attenuation

U. Fano

## EXTENT OF SURVEY

## SOURCES OF RADIATION

Electromagnetic radiation of high photon energy (high frequency) usually originates from excited atomic nuclei, from excited atoms, or from electrons traversing matter and is called X-rays or gamma rays. In this chapter, "gamma rays" indicate high-energy electromagnetic radiation from any source, even though this term usually refers to radiation from nuclear sources only.

## **ENERGY OF RADIATION**

This chapter deals primarily with gamma rays having photon energies between 0.1 and 10 mev. Some information will apply to radiation with energies extending roughly one order of magnitude above or below this range.

## **ELEMENTARY PROCESSES AND MULTIPLE PROCESSES**

Gamma rays traversing matter interact with it through separate "elementary" processes. Present information on elementary processes is generally adequate for shielding applications. Each photon may experience a succession of elementary processes. The combined effect of a succession of processes upon the over-all propagation of gamma rays has been under study in recent years.

## **ELEMENTARY INTERACTION PROCESSES**

## BRIEF DESCRIPTION OF PROCESSES1

# KINDS OF INTERACTION

Basic Interaction with Atomic Electrons - (I)

The electromagnetic field of gamma rays exerts an oscillating electric force on the charge of the atomic electrons within any material and a (smaller) magnetic torque on

¹References appear at end of chapter.

their spin. Each electron reacts as an elementary particle endowed with mass and spin angular momentum and subject to forces from other constituents of the material.

Basic Interaction with Nuclear Particles (Nucleons) - (II)

The electromagnetic field of gamma rays exerts an oscillating electric force on the charge of the nuclear protons within any material and a (smaller) magnetic torque on the spins of protons and neutrons. Each nucleon reacts as an elementary particle endowed with mass and spin angular momentum and subject to forces from other nucleons.

Interaction with the Electric Field Surrounding Charged Particles (Nuclei and Electrons) – (III)

The electromagnetic field of gamma rays can induce electric currents in space in which there is also an electrostatic field. These currents are associated with the generation of electron-positron pairs.

Interaction with the Meson Field Surrounding Nucleons - (IV)

The electromagnetic field of gamma rays can induce electric currents in the space surrounding a proton or a neutron, in which there is also a meson field. These currents are associated with the generation of mesons.

## EFFECT OF INTERACTION UPON A PHOTON

Outright Absorption - (a)

A photon may disappear as a result of interaction within a material. Its energy is then taken up by the interacting system within the material.

Elastic (Coherent) Scattering-(b)

A photon may be deflected (scattered) owing to interaction with an atomic system (such as an atom or nucleus). The possibility of scattering is necessarily associated with, and quantitatively related to, the possibility of absorption. If the atomic system recoils as a whole under the impact of the photon, its internal energy is not increased, and the scattering is elastic. The effects of elastic gamma-ray interaction with different parts of the system combine "coherently" (i.e., by addition of amplitudes).

Inelastic (Incoherent) Scattering - (c)

If the scattering of a photon causes an atomic particle to recoil with respect to the others, the internal energy of the atomic system is increased and the photon energy correspondingly depleted. The effects of inelastic gamma-ray interactions with different parts of the system combine "incoherently" (i.e., by addition of intensities).

## TYPES OF PROCESSES

Different types of processes may arise from each kind of interaction (I, II, III, or IV) leading to each of the end results (a, b, or c) - i.e., 12 types of processes in all.^{2,3} Many of these processes are quite infrequent; some have not yet been observed. The following processes, whose symbol indicates mechanism and end-effect, are most important.



## Photoelectric Effect (Ia)

A photon disappears, and an atomic electron (usually from the proximity of the nucleus) leaves its atom at high speed, having absorbed the photon energy. This effect predominates for lower-energy gamma rays especially for high-Z materials. Its cross section attains 1,000-10,000 barns/atom for 0.1-mev gammas. The cross section decreases rapidly with increasing gamma energy, E, very roughly like  $E^{-3}$  for E < 0.5 mev and like  $E^{-1}$  for E > 0.5 mev. The cross section for atoms of different elements is roughly proportional to  $Z^5$  for  $E \ge 0.1$  mev. The ejected electron flies off prevalently sideways to the photon beam for  $E \ll 0.5$  mev, prevalently forward otherwise as a result of the high photon momentum.

## Compton Scattering (Ic)4

A photon is scattered inelastically and an atomic electron recoils out of an atom, much as though it had been initially free.* The energy taken up by the electron depends primarily on its recoil momentum. This effect predominates for gammas of 1-5 mev in high-Z materials and even more greatly and over a much wider energy range in low-Z materials. Its cross section approaches 1 barn per electron for 0.05-mev gammas and decreases to less than 0.1 barn at 10 mev. The recoil electron flies off prevalently in the direction of the incident photon, the more nearly so the higher the fraction of photon energy it carries away and the higher the photon energy. It never recoils backwards, of course.

## Pair Production (IIIa)

A photon of more than 1 mev disappears, and its energy transfers to an electron-positron pair which springs out of the space around an atomic nucleus or (less frequently) around an atomic electron. This effect predominates for high photon energies, especially in high-Z materials. The cross section is zero at 1 mev but rises monotonically above this energy until it levels off near 50 mev for high-Z materials and at a higher energy for low-Z. The largest cross sections approach 100 barns/atom. In the region where the cross section is rising, it varies from element to element approximately in proportion to  $\mathbb{Z}^2$ . The electron and positron are projected prevalently in the direction of the incident photon, especially when the photon energy, E, and hence its momentum, are very large. Most of the electrons and positrons are confined to directions within (0.5 mev/E) radians from the photon direction.

## Rayleigh Scattering (Ib)

Gamma rays scattered by small angles impart only a small recoil, especially when their energy is low. The recoil is then often absorbed by a whole atom or molecule so that the scattering action of different atomic electrons combines coherently. The probability of this effect is thereby enhanced and prevails greatly at low energies. Even for photon energies above 0.1 mev, Rayleigh scattering is less probable than Compton scattering by only one or two orders of magnitude. This scattering is more likely for high-Z than for low-Z materials.

## Minor Effects

Nuclear photoelectric effect (IIa) has a small cross section which approaches 1 barn/atom only for high Z and for 15- to 20-mev photons. However, this effect results most

^{*}This scattering is actually classed as elastic as long as one considers the electron as an isolated particle; on the contrary, it is classed as inelastic if the electron is considered as a <u>part</u> of the whole material.



frequently in the ejection of one or more neutrons and is made conspicuous by the high penetrating power of the neutrons. Nuclear scattering (IIIb) and Delbruck scattering (IIIb) are at present barely detectable. Meson effects (IV) become appreciable only near or above 150 mev and then only with cross sections of the order of millibarns.*

## PROBABILITY OF PROCESSES

## "NARROW-BEAM" ATTENUATION OF MONOCHROMATIC GAMMAS

The total probability that a photon of given energy suffers some interaction process while traversing a layer of matter is studied experimentally with the schematic arrangement of Fig. 2.3.1. A well collimated ("narrow") beam of homogeneous (monochromatic)

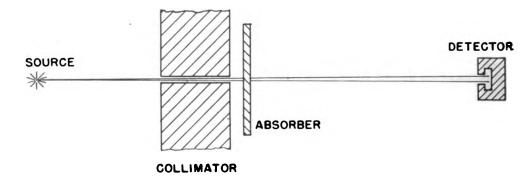


Fig. 2.3.1 — Schematic Diagram for Measurement of Narrow-beam Attenuation Coefficient.

gamma rays penetrates a layer of matter (absorber) and then reaches a detector. Absorption or appreciable deflection of a photon prevents it from reaching the detector. The attenuation of the intensity received by the detector, as the absorber thickness increases, measures the combined probabilities of outright absorption and of deflection.

# EXPONENTIAL LAW OF ATTENUATION

If a photon has a probability (p) of traversing an absorber of thickness (x) without suffering absorption or deflection, the probability on no process through a thickness 2x must be  $p^2$ . This condition implies that p depends on x according to:

$$p = e^{-\mu x}$$
 (1)

where  $\mu$  represents the "absorption coefficient" (probability of a process per unit thickness). If x is expressed in cm,  $\mu$  is expressed in cm⁻¹. "Narrow-beam" attenuation experiments verify Eq. (1) and measure  $\mu$  (see Fig. 2.3.2).

## COMPONENTS OF THE ABSORPTION COEFFICIENT

The total probability,  $\mu$ , that any process takes place per unit thickness of absorber is the sum of the probabilities of occurrence of the various kinds of processes. "Narrow-

^{*}See Rossi⁵ for a discussion of these processes.

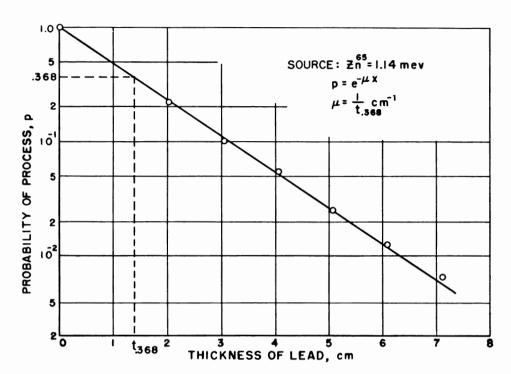


Fig. 2.3.2— An Illustration of the Experimental Verification and Measurement of Narrow-beam Attenuation Coefficients for Monoenergetic Sources. Data from C. M. Davisson and R. D. Evans, Phys. Rev. 81, 1951.

beam" experiments yield only the total  $\mu$ , but the  $\mu$ 's for the various processes are generally provided by the theory or by special experiments. The formula:

$$\mu = \mu_{\text{photo}} + \mu_{\text{scatt}} + \mu_{\text{pair}} \tag{2}$$

is often encountered, where  $\mu_{\rm photo}$  pertains to process Ia,  $\mu_{\rm scatt}$  to Ic and Ib combined (or to Ic alone),  $\mu_{\rm pair}$  to IIIa, and other processes are disregarded.

## MASS ABSORPTION COEFFICIENT

A layer of matter absorbs according to the quantity of matter it contains which is the thickness traversed, x in Eq. (1), times the density of the material. Therefore, absorber "thicknesses" are conveniently expressed on a mass basis (gm/cm²). Accordingly,  $\mu$  is often expressed in (gm/cm²)⁻¹ or cm²/gm (square centimeters per gram) and called "mass absorption coefficient."

## COMBINATION OF MASS ABSORPTION COEFFICIENTS

The probabilities that a photon suffer an interaction process with atoms of different elements in an absorber add without mutual disturbance.* Therefore, the mass absorption

^{*} Exception must be made for the effect of chemical binding upon the contribution of valence electrons to Rayleigh scattering and for the coherent combination of Rayleigh scattering by different atoms which matters only under special circumstances, particularly in crystals.

coefficient of a chemical compound or mixture is an average of the mass absorption coefficients of the constituent elements, weighted in proportion to the abundance of each element by weight. For example, for water (1 part H, 8 parts O):

$$\mu_{\rm H,O} = \frac{1}{9} \mu_{\rm H} + \frac{8}{9} \mu_{\rm O} \tag{3}$$

provided the  $\mu$ 's are expressed as mass absorption coefficients.

## HALF-VALUE LAYER

The absorber thickness  $t_{1/2}$  which has a probability  $\frac{1}{2}$  of letting through a photon undisturbed (i.e., which reduces the intensity of a "narrow beam" to  $\frac{1}{2}$ ) is called the "half-value layer" of the given absorber material for the given energy of monochromatic gammas. It follows from Eq. (1) that:

$$t_{\frac{1}{2}} = (\ln 2)/\mu = 0.693/\mu$$
 (4)  
since  $e^{-\mu t_{\frac{1}{2}}} = \frac{1}{2}$ .

# TABLES OF MASS ABSORPTION COEFFICIENTS

Data for certain important substances are given in Table 2.3.1. The same data diminished by the contribution of Rayleigh scattering (process 1b) are given in Table 2.3.2 for convenience in applications where the small-angle Rayleigh process is disregarded.

Table 2.3.1 — Mass Absorption Coefficients for Various Materials

(G. R. White, X-ray Attenuation Coefficients from 10 to 100 mev, Nat. Bu. Standards,

NBS Report-1003, May 13, 1952)

Photon energy,	Mass a	absorption coe	efficient, cm²	/gm
mev	H ₂ O	Al	Fe	Pb
0.1	0.171	0.169	0.370	5. <b>4</b> 6
.15	.151	.138	.196	1.92
.2	.137	.122	.146	0.942
.3	.119	.104	.110	.378
.4	.106	.0927	.0939	.220
.5	.0967	.0844	.0840	.152
.6	.0894	.0779	.0769	.119
.8	.0786	.0683	.0668	.0866
1.0	.0706	.0614	.0598	.0703
1.5	.0576	.0500	.0484	.0523
2.0	.0493	.0431	.0422	.0456
3.0	.0396	.0353	.0359	.0413
4.0	.0339	.0310	.0330	.0416
5.0	.0302	.0284	.0314	.0430
6.0	.0277	.0266	.0305	.0445
8.0	.0242	.0243	.0298	.0471
10.0	.0221	.0232	.0300	.0503

Table 2.3.2 — Mass Absorption Coefficients, cm²/gm, Disregarding Rayleigh Scattering Contribution

(Prepared	by	G.	R.	White)
-----------	----	----	----	--------

Photon energy,	Mass absorption coefficient, cm ² /gm							
mev	H ₂ O	Al	Fe	Pb				
0.1	0.167	0.160	0.342	5.29				
.15	.149	.133	.182	1.84				
.2	.136	.120	.138	0.895				
.3	.118	.103	.106	.355				
.4	.106	.0922	.0918	.208				
.5	.0967	.0840	.0828	.145				
.6	.0894	.0777	.0761	.114				
.8	.0786	.0682	.0668	.0837				
1.0	.0706	.0614	.0595	.0683				
1.5	.0576	.0500	.0484	.0514				
2.0	.0493	.0431	.0422	.0451				
3.0	.0396	.0353	.035 <b>9</b>	.0410				
4.0	.0339	.0310	.0330	.0416				
5.0	.0302	.0284	.0314	.0430				
6.0	.0277	.0266	.0305	.0445				
8.0	.0242	.0243	.0298	.0471				
10.0	.0221	.0232	.0300	.0503				

ENERGY DISSIPATION OWING TO INTERACTIONS ALONG A "NARROW BEAM"

## GAMMA-RAY ESCAPE SIDEWISE FROM A BEAM

The energy of photons which experience an interaction process in a material need not be entirely dissipated very near the point of interaction. The atomic particles to which the energy is transferred may travel some distance (see below). More important, part of the energy of the incident photons is carried away in various directions by photons of lower energy as a result of processes among which the following are most important.

### Fluorescence

When an "inner-orbit" atomic electron is ejected by photoelectric effect (process Ia), one of the outer atomic electrons will take its place and thereby become more tightly bound. The excess binding energy may be released in the form of an X-ray photon (fluorescence). The probability of fluorescence? (as opposed to a second electron-ejection) and the energy of the radiated photon are increasing functions of the atomic number of the material. See data in Table 2.3.3.

# Scattering

Scattered photons carry away a fraction of the incident-photon energy, in the event of a Compton process (Ic), or all of it in the event of coherent scattering (Ib). Data on the average energy fraction removed are shown in Table 2.3.4.

Table 2.3.3 — Fluorescent Yield in the K Series*
(From C. D. Broyles et al, Phys. Rev. 89, 1953)

Element	Yield	Element	Yield
8 O	0.00	34 Se	0.60
10 <b>N</b> e	.01	35 Br	.63
12 Mg	.02	38 Sr	.71
14 Si	.05	42 Mo	.77
16 S	.09	47 Ag	.83
17 Cl	.11	50 Sn	.85
18 A	.13	54 Xe	.87
20 Ca	.17	60 Nd	.89
24 Cr	.27	70 Yb	.92
26 Fe	.34	78 Pt	.94
28 Ni	.42	80 Hg	.95

* Fluorescent yield in the K series is the probability that an atom which has been ionized in the K shell will emit a photon of a frequency in the K series

82 Pb

84 Po

.95

.96

.46

.49

29 Cu

30 Zn

Table 2.3.4—Fraction of Incident-photon Energy Retained After Compton Scattering,
Averaged Over All Angles of Scattering

(Prepared by A. T. Nelms)

Initial photon energy, mev	Fraction retained by photon				
0.1	0.861				
.15	.817				
.2	.782				
.3	.729				
.4	.690				
.5	.659				
.6	.632				
.8	.592				
1.0	.560				
1.5	<b>.5</b> 05				
2.0	. <b>4</b> 69				
3.0	.423				
4.0	.394				
5.0	.373				
6.0	.357				
8.0	.333				
10.0	.316				

#### Annihilation

When a photon disappears as a result of pair production (process IIIa), the positron of the pair eventually combines with an atomic electron releasing 1 mev of energy (and sometimes more) in the form of two photons (occasionally one only).

## Bremsstrahlung

The gamma-ray energy transferred to electrons (or positrons) within a material may be re-radiated in the form of X rays (bremsstrahlung). For particles of energy above 10 mev and for high Z, this effect accounts for removal of most of the energy. At lower energies, the average energy fraction radiated by an electron (or positron) of energy E (mev) is of the order of:

where Z is the atomic number of the material.

## ENERGY TRANSPORT BY ATOMIC PARTICLES

#### **Electrons and Positrons**

Most of the energy transferred from gamma rays to a material is taken up by electrons (or positrons) and then dissipated along the path of these particles. The distance traveled by electrons (or positrons) is very small compared to the mean free path of gamma rays at energies up to a few mev but not at higher energies (see Table 2.3.5). Furthermore, the path of electrons and positrons is very tortuous, especially for high Z and at energies below 10 mev.

Table 2.3.5 — "Relative Range" of Electrons and Photons of Equal Energy in Water

[Principles of Radiological Physics, Nat. Bu. Standards, U. Fano, NBS Report-1002, May 1951 to be published as a contribution to Biological Effect of Radiations, edited by A. Hollaender, McGraw-Hill, New York)].

Energy,	
mev	$\mu R^*$
0.1	0.00
1.0	.04
10.0	.2
100.0	.6

 $*\mu$ R = Product of narrow-beam absorption coefficient of the X-rays (which may be regarded as the reciprocal of a range) and of the "true" range of electrons (measured along the track)

## **Neutrons and Other Particles**

Neutron generation absorbs only a small fraction of the incident gamma energy even under optimum conditions (see above), but the ejected neutrons travel quite far (see



Chapter 2.4). Protons and other charged fragments ejected from nuclei carry a very minor fraction of the total gamma energy and do not travel far.

# ENERGY-ABSORPTION COEFFICIENT ("TRUE ABSORPTION" COEFFICIENT)

To characterize the fraction of its energy dissipated by a narrow beam of gamma rays in traversing an absorber, the probability of each interaction process must be multiplied by the probable fraction, f, of the photon energy which is actually dissipated in the absorber as a result of the process. In the event of a photoelectric effect, the value of f discounts the fluorescence radiation; in the event of scattering, it discounts the scattered radiation; in the event of pair production, it discounts the annihilation radiation; and in all events, it discounts the (usually small) bremsstrahlung loss. Accordingly, the "energy absorption coefficient,"  $\mu_{\rm En}$ , is defined by modifying Eq. (2) in the following manner:

$$\mu_{\rm En} = f_{\rm photo} \ \mu_{\rm photo} + f_{\rm scatt} \ \mu_{\rm scatt} + f_{\rm pair} \ \mu_{\rm pair}$$
 (6)

The values of the f fractions can be estimated from theoretical and experimental data.

## TABLES OF ENERGY-ABSORPTION COEFFICIENTS

Data on  $f_{scatt}$   $\mu_{scatt}$  (for Compton processes only,  $f_{scatt}$   $\mu_{scatt}$  being often indicated by  $\sigma_a$ ) are often given in the literature. Data on  $\mu_{En}$  are often based on the assumption  $f_{photo} = f_{pair} = 1$  ( $f_{photo} \sim 1$  for low-Z materials, the choice of  $f_{pair}$  is not critical as long as  $\mu_{pair}$  is small). More accurate data are given for certain materials in Table 2.3.6.

#### GENERAL PROBLEM OF PENETRATION

A gamma-ray photon often experiences as many as 5 or 10 scattering processes before its eventual absorption. The direction of propagation thereby becomes increasingly random, and the initial straight penetration tends to go over into a diffusion process.

The penetration of gamma rays through a homogeneous medium of infinite extension is rather well understood. Much detailed information is available on this subject. However, the solution of specific problems involves some adaptation of published data. In addition, there is only meager understanding of the effects of inhomogeneities in a material and of boundaries between materials (these effects are not always large).*

The information given in the rest of this chapter pertains to gamma-ray propagation through homogeneous media of infinite extension, except where otherwise noted.

## PERTINENT PHYSICAL EFFECTS

## PRIMARY AND SECONDARY RADIATION

The interaction processes experienced by gamma rays give rise to a variety of "secondary radiations," such as scattered gammas and electrons ejected by photoelectric effect (see "Types of Process" above). The gammas emitted directly from a source are called "primaries." For primary gammas up to 10 mev, the secondaries which contribute much to penetration are themselves gammas (of lower energies), since secondary electrons do not travel far and secondary neutrons are few in number. Therefore, the study of gamma-ray attenuation deals with photons of various energies even where the primaries are monoenergetic.

^{*}See "Other Studies" discussed later in this chapter.



Table 2.3.6 — Energy-absorption Coefficients for Various Materials*
(Prepared by G. R. White and I. E. Hornstein)

Energy,	Energy-absorption coefficient, cm ² /gm							
mev	H ₂ O	Al	Fe	Pb				
0.088	0.0252	0.0445	0.312	2.46				
.10	.0253	.0371	.219	2.16				
.125	.0266	.0307	.123	1.55				
.15	.0278	.0282	.0801	1.08				
.175	.0289	.0276	. <b>0</b> 59 <b>5</b>	.779				
.20	.0299	.0275	.0485	.58 <b>6</b>				
.25	.0312	.0279	.0390	.358				
.30	.0320	.0283	.0340	<b>.24</b> 1				
.40	.0328	.0287	.0306	.136				
.50	.0330	.0287	.0293	.0904 (.0901)†				
<b>.6</b> 0	.0329	.0286	.0287 (.0286)†	.0689 (.0684)				
.70	.0326	.0283	.0280 (.0278)	.0566 (.0560)				
.80	.0321	.0278	.0274 (.0272)	.0483 (.0477)				
.90	.0316	.0274	.0268 (.0266)	.0431 (.0424)				
1.0	.0311 (.0310)†	.0270 (.0269)	.0264 (.0261)	.0391 (.0384)				
1.25	.0297 (.0296)	.0258 (.0257)	.0252 (.0248)	.0325 (.0317)				
1.5	.0284 (.0283)	.0247 (.0246)	.0241 (.0237)	.0290 (.0280)				
1.75	.0272 (.0271)	.0237 (.0236)	.0232 (.0227)	.0275 (.0260)				
2.0	.0261 (.0260)	.0229 (.0227)	.0224 (.0219)	.0265 (.0248)				
2.5	.0243 (.0241)	.0216 (.0213)	.0215 (.0209)	.0260 (.0238)				
3.0	.0229 (.0227)	.0205 (.0201)	.0210 (.0203)	.0264 (.0238)				
4.0	.0208 (.0204)	.0192 (.0188)	.0208 (.0198)	.0290 (.0253)				
5.0	.0194 (.0189)	.0185 (.0180)	.0211 (.0198)	.0317 (.0272)				
6.0	.0184 (.0178)	.0180 (.0174)	.0214 (.0200)	.0344 (.0287)				
7.0	.0176 (.0170)	.0177 (.0171)	.0219 (.0203)	.0368 (.0298)				
8.0	.0170 (.0163)	.0176 (.0169)	.0225 (.0206)	.0391 (.0309)				
9.0	.0165 (.0158)	.0175 (.0168)	.0232 (.0209)	.0410 (.0319)				
10.0	.0161 (.0154)	.0176 (.0167)	.0238 (.0213)	.0428 (.0328)				

* Values of the fractions f were estimated as follows:

 $f_{photo} = 1 - .F_K K_{cr}/h\nu$ 

$$f_{scatt} = 1 - R_C - 1/h \nu \int_0^{T_{max}} p_C (h \nu, T) T G_{Brem} (T) dT$$

$$f_{pair} = 1 - 2mc^2/h \ \nu - 1/h \ \nu \ \int_0^{h\nu - 2mc^2} \ p_p(h \ \nu, \ T^+, \ T^-) \left\{ T^+ \ G_{Brem} \ (T^+) + T^- G_{Brem} \ (T^-) \right\} dT^+$$

where:

 $K_{\alpha}$  = energy of radiation in the K series

 $I_K$  = binding energy of electron in K shell

 $R_C$  = average fraction of incident-photon energy retained by photon after Compton scattering (see Table 2.3.4)

 $p_C$  (h $\nu$ , T) = probability that Compton scattering yields recoil electron of energy T

 $p_p$  (h $^{\nu}$ ,  $T^+$ ,  $T^-$ ) = probability that pair production yields positron of energy  $T^+$  and electron of energy  $T^-$ 

G_{Brem} (T) = fraction of electron energy radiated as Bremsstrahlung (from NBS Report No. 2364)

 $\dagger$  Energy-absorption coefficients with corrections for Bremsstrahlung loss are given in parentheses. The simple law of combination of absorption coefficients for a mixture of elements, according to Eq. (3), does not hold exactly when the effect of  $G_{Brem}$  (T) is appreciable

## **FILTRATION**

Photons of different energies traveling together through an absorber, e.g., in a "narrow-beam" attenuation experiment (Fig. 2.3.1) with a non-monoenergetic source, have different probabilities of experiencing interaction processes. The gammas with higher interaction probability (i.e., the less penetrating, or "softer," ones—which usually are those of lower energy) are removed from the beam in the course of penetration faster than those with

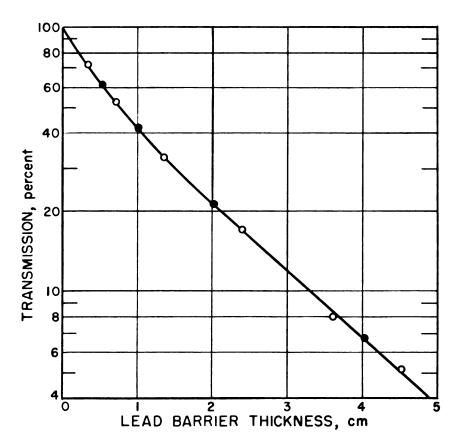


Fig. 2.3.3 — Illustration of the Experimental Measurement of Attenuation Coefficients for a Non-monoenergetic (Radium) Source. Narrow-beam conditions: ●-Kaye, Binks, and Bell; ○-H. O. Wyckoff and R. J. Kennedy, Jour. Res. Nat. Bu. Standards 42, 1949.

lower interaction probability. Thus, penetration to deep layers of the absorber has an effect of "filtration" which selects gammas with low probability of interaction (i.e., the "harder" component of the initial beam). Accordingly, the successive layers of an absorber attenuate the beam by smaller and smaller fractions. The semi-logarithmic plot of intensity vs thickness, which is a straight line for monoenergetic gammas in Fig. 2.3.2, has a decreasing slope (corresponding to a decreasing average value of the absorption coefficient  $\mu$ ) for a non-monoenergetic beam in Fig. 2.3.3.

#### BROAD-BEAM ATTENUATION

In an attenuation experiment free from the "narrow beam" limitation (see Fig. 2.3.4, in which the aperture of the collimator of Fig. 2.3.1 has been greatly increased), the loss by scattering of some gammas initially aimed at the detector is compensated in part by the

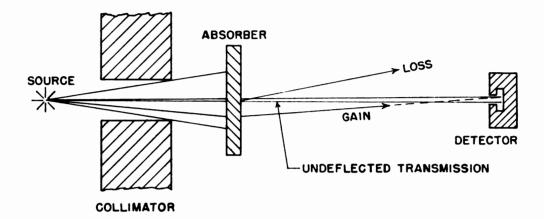


Fig. 2.3.4 — Schematic Diagram Showing "Loss" of Radiation Aimed at the Detector but Scattered Away from It, and Compensating "Gain" of Radiation Aimed in Other Directions but Scattered toward the Detector.

deflection toward the detector of gammas initially directed otherwise.* Therefore, one finds a lower attenuation under "broad-beam" than under "narrow beam" conditions, i.e., a spuriously low apparent value of the absorption coefficient. As the absorber thickness increases, the "gain" derived from the "broad-beam" condition becomes comparatively smaller (owing to the increased chance of multiple interaction processes). Therefore, the apparent value of the absorption coefficient goes up with increasing absorber thickness, as witnessed by the increasing slope of the plot in Fig. 2.3.5.† It approaches the value of the "narrow-beam" coefficient, without ever attaining it.‡

## ACCUMULATION OF SECONDARIES

Not only in the "broad-beam" experiment but also generally the presence of secondary scattered gammas influences heavily the whole process of gamma-ray penetration. Compton scattering is, on the whole, the most frequent process for medium-energy gammas in

^{*}See Davisson and Evans. An estimate of this effect, valid for rather thin absorbers and moderate beam apertures has been given, though incorrectly, by Tarrant. This remark refers mainly to the <a href="mailto:number">number</a> of photons scattered toward the detector or away from its direction, rather than to the energy retained by these photons after scattering.

[†]This may not hold when the initial energy exceeds the minimum point of the absorption coefficient curve.

Notice that the 'broad-beam' effect yields downward curvature, whereas the curvature of Fig. 2.3.3 is upward owing to the filtration effect. Concurrent departures from a monoenergetic source and from 'narrow-beam' condition tend to compensate and may fail to be observed.

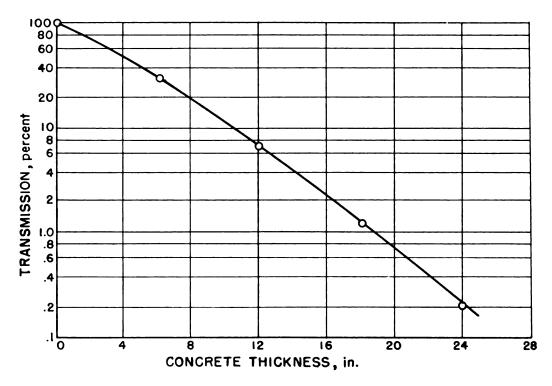


Fig. 2.3.5 — Broad-beam Attenuation Curve for Gamma Rays from Co⁶⁰. R. J. Kennedy, H. O. Wyckoff, and W. A. Snyder, Jour. Res. Nat. Bu. Standards 44, 1950.

the energy range of 0.1-10 mev, especially in low-Z materials. A photon may easily experience 5 to 10 successive Compton processes before its eventual outright absorption, which most frequently occurs in a photoelectric process. The photon energy decreases in each process. The gamma-ray energy suffers thereby a progressive degradation. The average fractional energy loss in a Compton process⁴ decreases in the course of degradation.* Therefore, the gamma photons tend to accumulate in the lower portion of the spectrum down to the energy range where outright photoelectric absorption becomes predominant.⁶

## POLARIZATION EFFECT

Gamma-ray sources usually generate unpolarized radiation, but the radiation becomes partially polarized in the course of repeated scattering. As a result, any three successive paths of a photon separated by scattering processes have a slight tendency to be coplanar. This effect tends to increase the over-all penetration but only by a few percent.

## FORMULATION OF THE COMPLETE PROBLEM

## MAPPING THE GAMMA-RAY FLUX

Given a distribution of gamma-ray sources within a material, the general problem of penetration consists of determining the intensity and spectrum of the gammas (primaries and secondaries) which flow in each direction at each point of the medium.



^{*}See also Table 2.3.3.

#### MONOENERGETIC SOURCES

It is adequate to solve the problem separately for sources of monoenergetic gammas of different energies, because any source may be regarded as the superposition of monoenergetic sources whose gammas penetrate independently.

## PENETRATION OF THE PRIMARIES

Despite the large accumulation of secondary gammas, the exponential attenuation of the primaries (as observed under "narrow-beam" conditions) usually constitutes the single most important factor affecting the gamma-ray penetration, especially since the primaries usually* have a lower  $\mu$  than any of their secondaries. At any point of a medium, the flux of the primary gammas alone can be easily calculated, since the primaries penetrate according to the simple "narrow-beam" exponential law (Fig. 2.3.2). For a point at a distance x from a gamma-ray source, the product  $\mu$ x in the exponent of  $e^{-\mu x}$  in Eq. (2) (with the value of  $\mu$  corresponding to the medium and the source energy under consideration) represents the depth of penetration expressed in "relaxation lengths." This number serves as a crude initial index of the attenuation of the gammas from the source to the point.

## BUILD-UP FACTOR

Since the main problem arises from the accumulation of secondaries, it is often convenient to focus on the ratio of the total amount of gammas at any one point to the amount of primaries only. For any specific instrument of gamma-ray detection and measurement at a given location, its actual response may be considered a result of all gammas and its ideal response a result of the primaries only. The ratio of these two responses is the "build-up factor" pertaining to the given instrument and to its location (see Fig. 2.3.6). The results of gamma-ray attenuation studies are often expressed as build-up factors.

## PARTIAL AND SIMPLIFIED PROBLEMS

Much understanding and useful information on gamma-ray attenuation is gained from the study of problems schematized so as to involve a reduced number of variables.

# ENERGY DEGRADATION ONLY ("NRL" PROBLEM†)

If a source is distributed uniformly throughout a medium, the secondaries are distributed uniformly also, and the only question concerns the accumulation of secondaries of various energies. The same problem arises with respect to the spectrum of secondaries integrated over the whole medium without reference to the source position. The solution of this problem is straightforward. The spectrum of secondaries is cut off on the low-energy side

$$N(E) = \int_{E}^{E_0} p(E, E') N(E') dE'$$
 (7)

The number of photons of energy  $E_{\emptyset}$  is given by the source strength; thereafter, the equation can be solved stepwise by carrying out the integration to lower and lower values of E. This procedure lends itself well to automatic computer operation. For exploratory numerical solutions, see Karr and Lamkin. Extensive calculations have been made incidental to more complex problems (see "Calculation of the Parameters" later in this chapter).



^{*}Except for high-Z materials and primary energies above a few mev.

[†]From an experiment by Faust and Johnson. 10

[‡]The number of photons of energy E, N(E), is determined by the number of all photons N(E') with energies E' higher than E up to the source energy  $E_0$ , multiplied by the probability p(E,E') that the next interaction process changes the energy from E' to E:

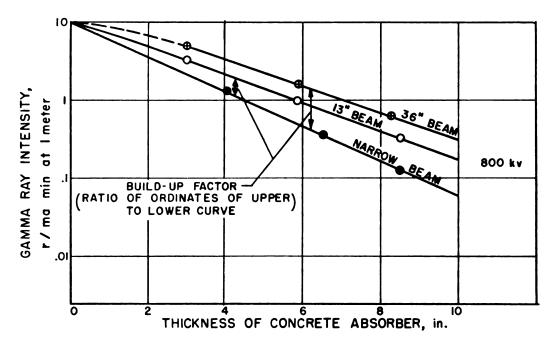


Fig. 2.3.6 — Illustration of the Build-up of Secondary X-rays Under Broad-beam Conditions. rrom H. O. Wyckoff, R. J. Kennedy, and W. R. Bradford, Nucleonics 3, No. 11, 1948.

where the probability of the photoelectric effect rises sharply and peaks above the cut-off except for high-Z materials.

## **DEGRADATION AND DEFLECTION**

Photons tend to lose track of their initial direction as a result of successive scattering processes. One may inquire about the distribution-in-direction of the gammas degraded to a certain energy, regardless of their position with respect to the source. Certain obliquity parameters of the distribution-in-direction (such as the mean obliquity of penetration) remain independent of one another in the course of successive scattering processes. Their termination reduces to a number of separate "NRL" problems.*

$$N_1 (E) = \int_0^{\pi} P_1 (\cos \vartheta) N(E, \vartheta) 2\pi \sin \vartheta d\vartheta$$

These parameters obey the equations:

$$N_{1} (E) = \int_{v}^{R_{0}} p(E, E') P_{1} (1 - \frac{mc^{2}}{E} + \frac{mc^{2}}{E'}) N_{1}(E') dE'$$
(8)

where p is the same as in Eq. (1). Since  $P_0 = 1$ ,  $N_0$  is the N(E) above and Eq. (8) reduces to Eq. (7) for 1 = 0; since  $P_1 = \cos \vartheta$ ,  $N_1$  is essentially the mean obliquity  $\cos \vartheta$ . For exploratory numerical solutions see Spencer and Jenkins. Extensive calculations have been made, incidental to more complex problems (see "Calculation of Parameters" later in this chapter).

^{*} If the number of photons of energy E traveling at an angle  $\vartheta$  with respect to the initial direction is  $N(E,\vartheta)$ , the "obliquity parameters" are the values of the Legendre polynomials  $P_1$  (cos  $\vartheta$ ) integrated over the distribution  $N(E,\vartheta)$ :

## SCHEMATIC GEOMETRIES*

Gamma-ray sources distributed in space with particular symmetries lead to distributions of secondaries with corresponding symmetries. Often the gamma distribution depends on a single space coordinate, the distance from the source. (The same simplification can be attained, regardless of source symmetry, by inquiring only about the gamma-ray distribution along one space coordinate integrated over the remaining coordinates.)

## Plane Sources

A source distributed uniformly over a plane yields a gamma-ray distribution uniform over any plane parallel to the source plane, which depends only on the distance from the source. Further simplification (without further elimination of variables) arises when the source radiation flows either perpendicularly to the source plane ("plane-collimated source" or "plane monodirectional source") or evenly in all directions ("plane isotropic source").

## Point Isotropic Source

A source concentrated at one point, which radiates evenly in all directions, yields a gamma-ray distribution uniform over every spherical surface centered in the source and dependent only on the distance from the source.

## Point-collimated Source

A source concentrated at one point which radiates in a single direction has only a cylindrical symmetry which is preserved in the distribution of secondaries. The gamma-ray flux depends on two position coordinates (axial and radial distances). Any source can be regarded as an aggregate of point-collimated sources.

## DEEP PENETRATION

The study of extremely deep gamma-ray penetrations serves (1) to treat unusually severe shielding problems and (2) to increase confidence in methods of calculation whose reliability tends to decrease as the depth of penetration increases. Deep-penetration studies have led to the establishment of certain mathematical laws and to the development of workable methods of calculation. Most practical problems can be handled by methods suited for moderate penetration (see "Moderate Penetration" below).

# QUALITATIVE ANALYSIS13

## THE MOST PENETRATING SPECTRAL COMPONENT

Usually the primary gammas are more penetrating than any of their secondaries. However, if the energy, E, of the primaries exceeds the energy,  $E_m$ , at which the "narrowbeam" absorption coefficient attains its minimum value, secondaries degraded to energy  $E_m$  constitute the most penetrating component of the whole spectrum in the medium and play the leading part in determining the deepest penetration. The value of  $E_m$  for various materials is given in Table 2.3.7.

^{*} For fuller discussion, see Chapter 2.5.

**CHAP. 2.3** 

Table 2.3.7 — Energy at Which Narrow-beam Absorption Coefficients Attain Minimum Values,  $E_{\rm m}$ 

(Pı	ena	red	bv	G.	R.	White)

Z	E _m , mev	Z	$\mathbf{E}_{m}$ , mev
4 Be	94	20 Ca	13
5 B	70	26 <b>F</b> e	9
6 C	55	30 <b>Z</b> n	7.6
7 N	45	40 Zr	5.4
8 O	40	48 Cd	4.4
9 F	34	56 Ba	3.9
10 Ne	30	74 W	3.5
13 Al	21	82 Pb	3.4
		92 U	3.3

## LIMITED EQUILIBRIUM OF SOFTER SECONDARIES

At great depths of penetration, secondaries of energy substantially lower than that of the most penetrating component tend to attain a steady state, namely to become distributed in energy and in direction in a manner which no longer varies with depth and which is essentially the same as the distribution considered above under "Degradation and Deflection."

## CRITICAL SPECTRAL RANGE

The dynamics of deep penetration are governed by an ever-increasing accumulation of secondaries with energies just below that of the most penetrating component and which are, therefore, only barely less penetrating. The spectral range which is critical in this respect narrows progressively in the course of penetration, while the spectral range in a steady state (see above) spreads to higher energies. The accumulation of secondaries follows a different trend depending on whether the most penetrating component has the energy  $E_m$  or is the primary itself, i.e., whether or not the absorption coefficient,  $\mu$ , has a minimum in the critical range.

## **CONCLUSION**

Since the lower-energy secondaries in a steady state include more and more of the spectrum as the penetration progresses and thus carry nearly the whole energy flux, the main characteristic of deep penetration is the variation of the intensity level of these secondaries as a function of depth. However, this variation is controlled by the secondaries in the critical range.

## TREND OF PENETRATION FOR SOURCE ENERGIES BELOW THE "MINIMUM" Em

## **LIMITATIONS**

The following applies only to plane-collimated, plane-isotropic, and point-isotropic sources (or combinations thereof); it also applies in principle, but hardly in practice, ¹⁴ to any plane source.



## MATHEMATICAL LAW

T

Ľ

1

The intensity of the gamma-ray flux at great depths for source energies below  $\mathbf{E}_m$  follows the trend:

$$e^{-\mu_0 x} x^K$$

where x is the distance from the source,  $\mu_0$  is the absorption coefficient of the primary gammas in the medium under consideration (expressed in units reciprocal to those of x), and K is a constant. For a plane-collimated source,  $x^K$  represents the variation of the "build-up" factors.*

## VALUES OF THE CONSTANT K

The constant K depends on the source geometry and on certain functions, A and B, of the probabilities of interaction processes for primary gammas in the medium under consideration. The values of A and B for various materials and primary energies are given in Table 2.3.8. The value of K for a plane-collimated source, as a function of A and B, is

Table 2.3.8 — Constants A and B on Which the Exponent of the Build-up Factor Depends

(Prepared by John Doggett and L. V. Spencer)

Source energy,	H ₂ O		Al		Fe		Sn		Pb		U	
mev	A	В	A	В	A	В	A	В	A	В	A	В
10	7.5	7.54	4.1	6.21								
8	6.6	6.87	4.0	5.91	0.48	4.64						
6	5.5	5.96	3.8	<b>5.4</b> 3	1.2	4.56						
4	4.0	4.91	3.3	4.68	2.0	4.25	0.40	3.61				
3	3.1	4.22	2.7	4.10	2.1	3.89	.86	3.49	0.33	2.88	0.22	2.72
2	2.1	3.38	2.0	3.33	1.8	3.30	1.4	3.13	1.7	2.65	2.0	2.48
1	0.96	2.37	0.96	2.37	0.89	2.36	1.1	2.22	1.7	1.75	1.9	1.53
0.8	.73	2.12	.73	2.12	.72	2.11	0.92	1.95	1.6	1.43	1.8	1.21
.6	.52	1.86	.52	1.86	.54	1.84	.83	1. <b>6</b> 3	1.5	1.033	1.6	0.852
.4	.32	1.58	.32	1.57	.37	1.52	.77	1.17	1.35	0.579	1.4	.449
.3	.22	1.41	.22	1.40	.32	1.32	.74	0.798	1.2	.333	1.2	.260
.2	.13	1.23	.155	1.21	.31	1.01	.72	.417	0.95	.133	0.97	.100
.15	.086	1.12	.145	1.09	.33	0.767	.70	.223	.77	.0647	.82	.0485

given in Table 2.3.9. The tabulated value of K must be reduced by 1 for a plane-isotropic source and by 2 (inverse square distance effect) for a point-isotropic source.

^{*}Notice that  $x^K$  is merely <u>proportional</u> to the "build-up" factor but is not numerically equal to this factor. The results of calculations (see Tables 2.3.11 to 2.3.14) and of an experiment show that Eq. (9) holds adequately, in some cases at least, for depths upwards of 10-15 relaxation lengths. Inspection of Tables 2.3.11 to 2.3.14 disproves the frequent notion that the build-up factor varies linearly with x at low depths.

Table 2.3.9 — The Exponent K of the Build-up Factor as a Function of C	Constants A and B
(Prepared by L. V. Spencer and John Doggett)	

						В				
A	0.02	0.05	0.1	0.25	0.5	1	2	4	6	8
0.02	0.0200	0.0516	0.1095	0.374	2.63	13.00	42.3	113.0	189.5	272
.05	.01939	.0494	.1052	.332	1.328	5.49	17.21	45.5	76.5	<b>108.9</b>
.1	.01846	.0473	<b>.09</b> 8 <b>8</b>	.293	0.871	2.98	8.84	23.0	38.5	54.7
.25	.01617	.0411	.0844	.231	.547	1.439	3.81	9.48	15. <b>69</b>	22.2
.5	.01341	.0338	.0687	.1798	.388	0.887	2.11	4.96	8.16	11.32
1	.01003	.0252	.0506	.1289	.265	.55 <b>9</b>	1.211	2.67	4.24	5.87
2			.0335	.0841	.1696	.345	0.709	1.477	2.28	3.11
4								0.821	1.173	1.67
6								.577	0.870	1.16
8								.447	.671	0.89

## TREND OF PENETRATION FOR SOURCE ENERGIES ABOVE THE "MINIMUM" Em

## **LIMITATIONS**

The following information applies to all plane sources and to point-isotropic sources (or combinations thereof).

### MATHEMATICAL LAW

The intensity of the gamma-ray flux at great depths, for source energies above  $\mathbf{E}_{\mathbf{m}}$ , follows the trend:

$$e^{-\mu_{\rm m}x + H(\mu_{\rm m}x)\frac{1}{3}}x^{-\frac{4}{3}}$$
 (10)

for plane sources and:

$$e^{-\mu_{m}x + H(\mu_{m}x)t/3} x^{-1t/6}$$
 (11)

for point-isotropic sources, where x is the distance from the source,  $\mu_m$  is the minimum value of the absorption coefficient in the medium under consideration, i.e., the value of  $\mu$  for gammas of energy  $E_m$  expressed in units reciprocal to those of x, and H is a constant which depends on the probabilities of interaction processes for gammas of energies near  $E_m$ .*

# VALUES OF THE CONSTANTS

The values of  $\mu_m$  and H for certain materials are given in Table 2.3.10.

## SEMI-ASYMPTOTIC CALCULATIONS

A method for the detailed numerical calculation of gamma-ray fluxes from plane sources or point-isotropic sources, which makes use of the mathematical laws and in which the

^{*}See the footnote following Eq. (9). The laws (10) and (11) become effective at greater depths than Eq. (9).

Table 2.3.10 — The Values of H and $\mu_{\rm m}$	for Various Materials
(Prepared by L. V. Sper	ncer)

Material	$\mu_{\rm m}$ ,* cm ² /gm	н
H ₂ O	0.0167	2.0
Al	.0216	2.1
Fe	.0300	2.8
Sn	.0351	2.6
w	.0391	2.5
Pb	.0410	2.3
U	.0425	2.1

*Values of  $\mu_m$  without Rayleigh scattering as in Table 2.3.2 were used in all calculations of broad-beam attenuation

effort required does not increase rapidly with increasing depth of penetration, has been developed through the pilot stage. Results are available for plane-collimated sources of 10.2 mev in Pb and of 5.1 mev in Fe. 15

#### MODERATE PENETRATION

Most of the detailed information available on gamma-ray penetration derives from calculations which are based, directly or indirectly, on the "polynomial method." The labor required by this method is roughly constant up to penetration depths of the order of 10-15 "relaxation lengths" and thereafter increases roughly in proportion to the cube of the penetration, which makes the method unsuitable for extreme depths. Some of the calculations have been checked by experiments, very satisfactorily. ^{17,18,10} The following paragraphs provide some information on the method, which is intended as background for the flexible utilization of its results (see "Calculation of Parameters" below).

An alternate method (successive calculation of the distributions of photons that have been scattered 1,2,3... times) has received considerable application^{20,21} especially to Pb, a high-Z material where the sequence of Compton processes ends early owing to high photoelectric absorption.

### PRINCIPLES OF THE POLYNOMIAL METHOD

## DEFINING THE GAMMA-RAY DISTRIBUTION BY SUITABLE PARAMETERS

Great labor saving, as well as additional insight, result if the gamma-ray distribution in a medium can be characterized by a few parameters only, which in turn can be calculated directly. (This should be possible, since the relevant features of any physical phenomenon are seldom very numerous.) To this end, one may seek an analytical expression for the gamma-ray distribution, which contains in principle an infinity of parameters (sufficient to describe the distribution in infinite detail) but such that in practice the values of all but a few parameters have a negligible influence on the distribution in the range of interest and may be safely disregarded.

CHAP. 2.3 RADIATION SHIELDING

#### CHOICE OF THE ANALYTICAL EXPRESSION

At a distance of  $\mu_0 x$  "relaxation lengths" (see "Penetration of the Primaries" above) from a plane source or point-isotropic source, the flux  $N(x,E,\vartheta)$  of photons of energy E traveling at an angle  $\vartheta$  with respect to the direction of the source has been usually represented as a sum of terms of the following type:

$$\mathbf{N}(\mathbf{x}, \mathbf{E}, \mathbf{J}) = \mathbf{e}^{-\mu_0 \mathbf{x}} \ \Sigma_{\mathbf{n}l} \ \mathbf{N}_{\mathbf{n}l} \ (\mathbf{E}) \ \mathbf{L}_{\mathbf{n}}(\mu_0 \mathbf{x}) \ \mathbf{P}_{\mathbf{l}} \ (\cos \mathbf{J})$$
 (11)

Here,  $e^{-\mu_0 x}$  represents the exponential attenuation of the primaries,  $L_n(\mu_0 x)$  is a polynomial of the Laguerre (or related) type,  $P_1$  (cos  $\vartheta$ ) is a Legendre polynomial, and  $N_{nl}$  (E) are the coefficients to be calculated from theory (see below). The gamma-ray flux at x, irrespective of direction,* is represented by the terms with l=0 only  $[e^{-\mu_0 x} \; \Sigma_n N_{n\theta} \; (E) \; L_n(\mu_0 x)]$  because the  $P_1$  (cos  $\vartheta$ ) for  $l\neq 0$  have average value zero. Calculation of the coefficients with n=0,1,2,3 only, setting those with n>3 equal to zero, may yield an adequate approximation for  $\mu_0 x$  as large as 10 or even 15,† in the sense that the terms with n>3 would yield no substantial correction in this range. Any other analytical expression which can be fitted by a calculation equivalent to the calculation of the  $N_{nl}$ 's would be equally acceptable, provided it converges adequately.

#### CALCULATION OF THE PARAMETERS

The parameter  $N_{00}$  is essentially the same as the number of photons N(E) of Eq. (7), and the parameters  $N_{01}$  are essentially the same as the "obliquity parameters"  $N_1$  of Eq. (8). They depend on the number of photons of certain energies and directions irrespective of their distance from the source. The parameters  $N_{n1}$  (E) depend on the same numbers of photons but weighted in proportion to certain functions of their distance from the source (polynomials of grade n). Each  $N_{n1}$  is determined by an "NRL" equation, similar to Eq. (8) but with a correction which requires previous knowledge of parameters with lower values of n.‡ Thus, the  $N_{n1}$ 's can be calculated in succession for higher and higher values of n.

# **AVAILABLE RESULTS OF CALCULATIONS**

The raw results of calculations have the form of "weighted obliquity parameters," as indicated above, calculated separately for various materials, source geometries, and source energies and tabulated for a series of secondary-photon energies. These data usually get processed and published in part, in the form of answers to specific questions, such as plots of the build-up factor for a specific instrument vs distance from the source. However, processed and published data may not answer just the type of question required for a specific application (e.g., they may not give the build-up factor for a desired type of instrument, or they may fail to give indications regarding the distribution-in-direction). In this event, the desired application may be achieved by procuring the original raw data (see below) and by reprocessing them according to need.

 $[\]ddagger$  Each  $N_{nl}$  (E) depends on the value of the same parameter for photons of energy E', which subsequently drop to the energy E, as in Eq. (8). However, the value  $\int_{E}^{E_0} P_l(E,E')N_{nl}$  (E')dE' would yield a number of photons of energy E weighted according to the distance from the source at which they are generated. The correction takes into account the average travel of photons before the next interaction process.



^{*}Notice the difference between the total flux through a point irrespective of direction and the net transport through a plane perpendicular to the source direction.

[†] The reason for the success of the representation (11) is discussed by Spencer and Fano. 16

# EXPLORATORY CALCULATIONS,

Pilot calculations have been made in sizable numbers^{0,10,22-24} and, in part, checked by experiments.¹⁷⁻¹⁰ These results serve primarily, at present, to provide a quantitative illustration of certain specific features of the gamma-ray flux.

# NDA-NBS PROGRAM (H. GOLDSTEIN, NDA)26

A comprehensive program of calculations by the polynomial method is being carried out by Nuclear Development Associates in conjunction with the Bureau of Standards. The aim of the program is directed at producing answers on gamma-ray penetration for materials, source geometries, and initial energies of interest in the shielding of reactors. Accordingly, the initial energies chosen generally cover the range from 0.5 to 10 mev. The materials involved extend over the complete periodic table, including pure Compton scatterer, H₂O, Al, Fe, Sn, W, Pb, U. For almost all of the materials and source energies, computations have been made for point-isotropic sources and, in most cases, also for plane monodirectional source geometry. In addition, for Compton scatterer, iron, and lead (the most important class of materials in practice), calculations have also been made for infinite plane sources in which the distribution of the source photons in the angle  $\theta$  from the normal to the plane is given by the Legendre polynomials  $P_n$  (cos  $\theta$ ), n = 1,2,3. Since the  $P_a$  case (plane isotropic) is directly related to the point-isotropic solution, the results cover the first four Legendre polynomials which, it is hoped, will permit approximating the answer for any arbitrary plane source, symmetric about the normal, which does not vary too rapidly with  $\theta$ .

The range of penetrations which these calculations are designed to cover is from 1 to 20 "relaxation lengths" (see "Penetration of the Primaries" above) from the source. The number of moments needed for such penetrations, and the number of cases considered, is so extensive as to preclude hand computations. Instead, the Bureau of Standards automatic computer, SEAC, has been used in all problems.

Certain simplifications in the nature of the gamma-ray interaction have been made which greatly reduce the complexity of the calculations without affecting the accuracy of the results significantly. Only three processes have been considered. Two of these, photoelectric effect and pair-production, have been assumed completely absorptive, thus neglecting such secondary effects as fluorescence, bremsstrahlung, and annihilation radiation. The third process, incoherent Compton scattering, is the only scattering treated. For the energies and materials discussed, coherent scattering is at such small angles as to be no scattering at all and has therefore been omitted from both the total absorption coefficient and the scattering kernel. Polarization effects in the incoherent scattering have also been neglected.

It is difficult to state the expected accuracy of the results, as it varies with the number of moments calculated, the type of material, the penetration, and the energy region of the scattered spectrum being considered. In general, the error in integrated quantities, such as build-up factors, will have less effect on the final calculated intensity than the normal uncertainties in the value of the absorption coefficient.

It is expected that full details of the calculation will be published in 1953 as an Atomic Energy Commission report. Complete tables of build-up factors and differential spectra will be included in the report along with illustrative examples of angular distributions. These results will not exhaust the calculations which can be made from the raw output of the machine, however. To make these more generally available, it is therefore intended to place annotated microfilm copies of the SEAC output at each of the AEC deposit libraries.

# TABLES OF BUILD-UP FACTORS (H. GOLDSTEIN, NDA)

To illustrate the type of results obtained from this program, Tables 2.3.11 to 2.3.14 present the calculated dose build-up factors with a point-isotropic source in an infinite medium composed of H₂O, Al, Fe, and Pb, respectively. The designation "dose" indicates the gamma-ray flux is to be measured in terms of roentgens per unit time, i.e., with the energy spectrum weighted in proportion to the energy absorption coefficient of air (see "General Problem of Penetration" above). Table 2.3.15 lists the values used here in computing the build-up factors given in the tables.

The accuracy of the results for Pb and Fe is estimated roughly at 5 percent, except at the greatest penetration, where the errors may be as large as 15 percent. The low-energy portion of the spectrum (which is the most difficult to calculate) contributes disproportionately to the dose build-up factor for water and aluminum. Hence, the limit of error for these materials is undoubtedly greater, probably being around 10 percent for medium penetrations, rising to 25-30 percent for the deepest penetration.

Table 2.3.11 — Dose Build-up Factor, B, for Pb, Point-isotropic Source

E ₀ , mev	2	4	7	10	15
0.5	1.42	1.69	2.00	2 <b>.2</b> 7	2.65
1	1.69	2.26	3.02	3.74	4.81
2	1.76	2.51	3.66	4.84	6.86
3	1.68	2.43	3.75	5.30	8.44
4	1.56	2.25	3.61	5.44	9.80
5.11	1.46	2.08	3.44	5.55	11.74
6	1.40	1.97	3.34	5.69	13.80
8	1.30	1.74	2.89	5.07	14.05
10	1.23	1.58	2.52	4.34	12.54

Table 2.3.12 - Dose Build-up Factor, B, for Fe, Point-isotropic Source

	$\mu_0$ r								
E ₀ , mev	2	4	7	10	15	20			
0.5	3.09	5.98	11.73	19.23	35.42	55. <b>6</b>			
1	2.88	5. <b>39</b>	10.21	16.18	28.31	42.7			
2	2.38	4.08	6.99	10.47	16.83	24.0			
3	2.12	3.44	5.74	8.35	13.25	18.8			
4	1.94	3.03	4.91	7.11	11.23	16.0			
6	1.72	2.58	4.14	6.02	9.89	14.7			
8	1.56	2.23	3.49	5.07	8.50	13.0			
10	1.42	1.95	2.98	4.35	7.5 <del>4</del>	12.4			

## EXPERIMENTAL SOURCES OF DATA

Considerable amounts of experimental data have been taken regarding various phases of gamma-ray penetration. However, most of the effort was directed to the solution of specific



	$\mu_0$ r								
E ₀ , mev	2	4	7	10	15	20			
0.5	4.24	9.47	21.5	38.9	80.8	141			
1	3.31	6.57	13.1	21.2	37.9	58.5			
2	2.61	4.62	8.05	11.9	18.7	26.3			
3	2.32	3.78	6.15	8.65	13.0	17.7			
4	2.08	3.22	5.01	6.88	10.1	13.4			
6	1.85	2.70	4.06	5. <b>4</b> 9	7.96	10.4			
8	1.68	2.37	3.45	4.58	6.56	8.52			
10	1.55	2.12	3.01	3.96	5.63	7.32			

Table 2.3.14 - Dose Build-up Factor, Br, for H2O, Point-isotropic Source

	$\mu_0$ r								
E₀, mev	1	2	4	7	10	15			
0.256	3.09	7.14	23.0	72. <b>9</b>	166	455			
.5	<b>2</b> .52	5.14	14.3	38.8	77.6	178			
1	2.08	3.50	7.21	14.6	24.0	44.7			
2	1.83	2.77	4.88	8.46	12.4	19.5			
3	1.69	2.42	3.91	6.23	8.63	12.8			
4	1.58	2.17	3.34	5.12	6.94	9.97			
6	1.46	1.91	2.80	4.08	5.33	7.34			
8	1.39	1.77	2.49	3.51	4.50	6.05			
10	1.32	1.63	2.22	3.04	3.82	5.07			

Table 2.3.15 — Energy Absorption-coefficient for Air in Thomson Units Per Electron
Utilized in the Preparation of Tables 2.3.11 Through 2.3.14

E, mev	$\mu_{\mathbf{A}}$	E, mev	$\mu_{\mathbf{A}}$
0.03	0.694	0.6	0.146
.04	.308	.8	.145
.05	.188	1	.138
.06	.143	1.5	.127
.08	.118	2	.118
.1	.116	3	.105
.15	.125	4	.0965
.2	.134	5	.0912
.3	.144	6	.0866
.4	.147	8	.0808
.5	.144	10	.0777

CHAP. 2.3 RADIATION SHIELDING

problems and therefore had a limited usefulness for the purpose of general penetration study or of reactor shielding. Other recent experiments had more general aims but represent thus far only initial stabs. Some pertinent references will be given here, grouped according to their line of endeavor.

#### DATA ON GAMMA-RAY DISTRIBUTION IN "PHANTOMS"

Radiologists need estimates of the "dose" received by various portions of a body which is exposed to a radiation beam of given area and given characteristics. Many experiments were made, mostly using mock-ups of human bodies ("phantoms"), with X-ray beams up to the million-volt range, some also with betatrons.*

#### RADIOLOGICAL SHIELDING DATA

The design of safe radiological installations³¹⁻³⁵ is related, though not too closely, to the design of reactor shielding. Until recent times, radiological shielding studies constituted nearly the sole source of information on high-energy gamma penetration.

#### **OTHER STUDIES**

#### **BACKSCATTERING**

A systematic analysis of the backscattering of a collimated beam of Co⁶⁰ gammas by the surface of a semi-infinite medium of various materials has been conducted. Typical spectra of radiation backscattered through 150° are shown in Figs. 2.3.7 to 2.3.9. The peaks above 200 kev result from single scattering. The lower-energy peak from the lead target results from fluorescence. Studies of the influence of a nearby wall upon the response of a detector have also been made. To example, Kennedy et al found when an ionization chamber was brought near a concrete barrier, remaining at a fixed distance from a Co⁶⁰ source, its reading was subject to increases of the order of 10 percent.

#### **SIDESCATTERING**

Data on the radiation scattered sidewise by a phantom exposed to an X-ray beam are given in the radiological literature.^{31,39,40}

#### ANALYSIS OF RADIATION TRANSMITTED THROUGH A BARRIER

Little experimental information seems to be available on this subject. Spectral analysis by scintillation is in progress.⁴¹

# RADIATION INTENSITY IN THE PROXIMITY OF A BOUNDARY

Measurements have been made of the transition effect at the surface of a water tank as the source and/or the detector pass from air to water. 42 

## EFFECTS OF INHOMOGENEITIES OF A MEDIUM

A study on the effect of voids in a water tank is reported in the classified literature.

^{*}For the lower-energy range see particularly Glasser, Quimby, Taylor, and Weatherwax,²⁶ Mayneord and Lamerton,²⁷ and the data of the British Hospital Physicist Assoc.;²⁶ for the higher energies, see Adams et al,²⁹ and Charleton and Breed.³⁰



1

ď.

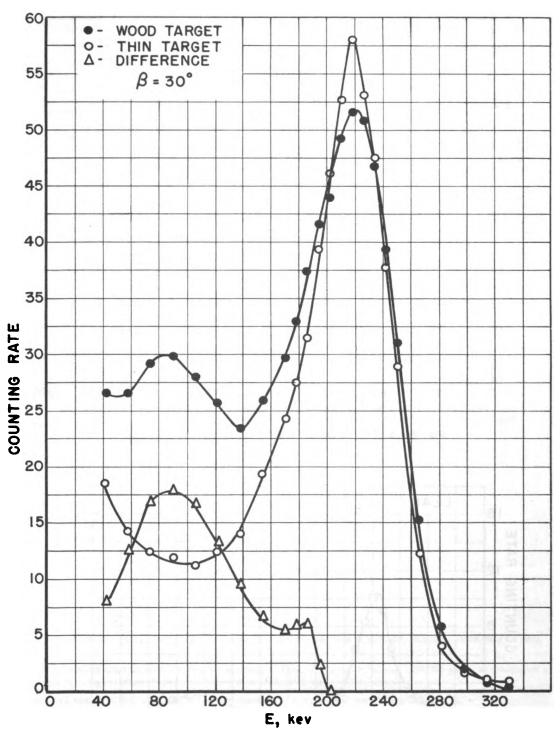


Fig. 2.3.7 — Spectrum of Gammas Backscattered from Wood.

CHAP. 2.3 RADIATION SHIELDING

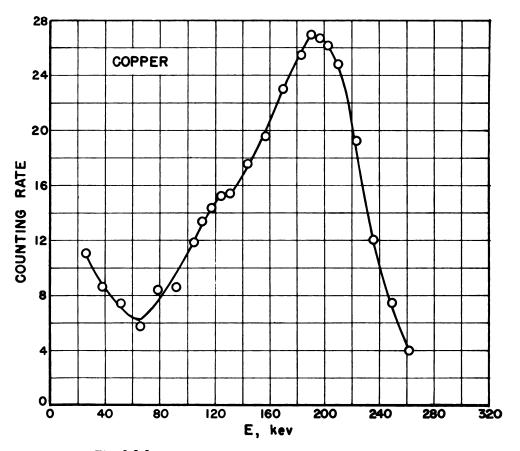


Fig. 2.3.8 — Spectrum of Gammas Backscattered from Copper.

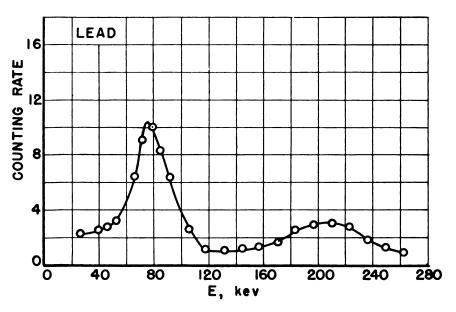


Fig. 2.3.9 — Spectrum of Gammas Backscattered from Lead.

#### REFERENCES

- 1. U. Fano, Principles of Radiological Physics, Nat. Bu. Standards, NBS Report-1002, May 1951, 231 pp.
- 2. F. K. Richtmyer and E. H. Kennard, Introduction to Modern Physics, McGraw-Hill Book Co., Inc., New York, 1947, pp 501-530.
- 3. F. Rasetti, Elements of Nuclear Physics, Prentice-Hall, Inc., New York, 1948, pp 76-98.
- A. T. Nelms, Graphs of the Compton Energy-angle Relationship and the Klein-Nishina Formula from 10 kev to 500 mev, Nat. Bu. Standards, to be published.
- 5. B. Rossi, High-energy Particles, Prentice-Hall, Inc., New York, 1952.
- 6. G. R. White, X-ray Attenuation Coefficients from 10 to 100 mev, Nat. Bu. Standards, NBS Report-1003, May 13, 1952, 93 pp.
- 7. E. H. S. Burhop, Auger Effect and Other Radiationless Transitions, Cambridge Monographs on Physics, Cambridge Press, 1952.
- 8. C. M. Davisson and R. D. Evans, Gamma-ray Absorption Coefficients, Rev. Mod. Phys. 24, 1952, p 79.
- 9. L. V. Spencer and C. Wolff, Penetration and Diffusion of Hard X-rays: Polarization Effects, Phys. Rev., to be published.
- 10. W. R. Faust and M. H. Johnson, Phys. Rev. 75, 1949, p 467.
- 11. P. R. Karr and J. C. Lamkin, Phys. Rev. 76, 1949, p 1843.
- 12. L. V. Spencer and F. A. Jenkins, Phys. Rev. 76, 1949, p 1885.
- 13. U. Fano, Penetration of K and Gamma Rays to Extremely Great Depths, Nat. Bu. Standards, Jour. Res. Nat. Bu. Standards, to be published.
- 14. Ibid. Sections 2f and B.
- 15. L. V. Spencer, Phys. Rev. 88, 1952, p 793.
- L. V. Spencer and U. Fano, Penetration and Diffusion of X-rays; Calculation of Spatial Distributions by Polynomial Expansion, Jour. Res. Nat. Bu. Standards 46, 1951, p 446.
- 17. G. R. White. Phys. Rev. 80, 1950, p 154.
- 18. E. Hayward, Phys. Rev. 86, 1952, p 493.
- 19. J. O. Elliot et al, Phys. Rev. 85, 1952, p 1048.
- 20. G. H. Peebles, Phys. Rev. 83, 1951, p 237.
- 21. G. H. Peebles and M. S. Plesset, Phys. Rev. 81, 1951, p 430.
- 22. L. V. Spencer and U. Fano, Phys. Rev. 81, 1951, p 464.
- 23. L. V. Spencer and F. A. Stinson, Phys. Rev. 85, 1952, p 662.
- 24. M. J. Berger and J. Doggett, Nat. Bu. Standards Rep. No. 2224.
- 25. H. Goldstein, J. E. Wilkins, Jr., and L. V. Spencer, Phys. Rev., in press.
- 26. O. Glasser, E. H. Quimby, L. S. Taylor, and J. L. Weatherwax, Physical Foundations of Radiology, Haeber, New York, 1944.
- 27. W. V. Mayneord and L. F. Lamerton, Atlas of X-ray Dose Distribution, Royal Cancer Hospital, London.
- 28. Brit. Jour. Radiology 25, 1952, p 88.
- 29. G. D. Adams et al. Amer. Jour. Roentgen 60, 1948, p 153.
- 30. E. D. Charleton and H. E. Breed, Amer. Jour. Roentgen 60, 1948, p 158.
- 31. H. O. Wyckoff and L. S. Taylor, X-ray Protection Design, Nat. Bu. Standards Handbook 50, May 9, 1952, 36 pp.
- 32. H. O. Wyckoff and C. B. Braestrup, X-ray and Radium Protection, Charles C. Thomas, Springfield, Ill., to be published.
- 33. H. O. Wyckoff and C. B. Braestrup, Radiology 51, 1948, p 840.
- 34. H. O. Wyckoff, R. J. Kennedy, and W. R. Bradford, Nucleonics 3, 1948, p 62.
- 35. F. S. Kirn et al, in preparation, NBS-2125.
- 36. E. Hayward and J. Hubbell, Nat. Bu. Standards Rep. No. 2264.
- 37. R. J. Kennedy, F. S. Kirn, and H. O. Wyckoff, to be published.
- 38. G. J. Hine, to be published.
- 39. C. W. Wilson and B. J. Perry, Brit. Jour. Radiology 25, 1952, p 210.
- 40. E. S. Jetter and H. Blatz, Nucleonics 10, 1952, p 43.
- 41. P. R. Bell, J. E. Richardson, and R. L. Heath, ORNL-1365.
- 42. M. A. Van Dilla and G. J. Hine, Nucleonics 10, 1952, p 54.

#### SELECTED READING LIST

X-RAY ATTENUATION COEFFICIENTS FROM 10 TO 100 MEV, Nat. Bu. Standards, G. R. White, NBS Report-1003, May 13, 1952, 93 pp.

PRINCIPLES OF RADIOLOGICAL PHYSICS, Nat. Bu. Standards, U. Fano, NBS Report-1002, May, 1951, 231 pp, (to be published as a contribution to Biological Effect of Radiations, edited by A. Hollaender, McGraw-Hill, New York).

GAMMA-RAY ABSORPTION COEFFICIENTS, C. M. Davisson and R. D. Evans, Rev. Mod. Phys. 24, 1952, p 79.

GRAPHS OF THE COMPTON ENERGY-ANGLE RELATIONSHIP AND THE KLEIN-NISHINA FORMULA FROM 10 KEV TO 500 MEV, Nat. Bu., Standards, A. T., Nelms (to be published as a NBS Circular).

SOME APPLICATIONS OF NUCLEAR PHYSICS TO MEDICINE, W. V. Mayneord, Brit, Jour. Radiology, Supplement 2, 1952.

DETERMINATION OF THE ENERGY OF BETA PARTICLES AND PHOTONS BY ABSORPTION, L. E. Glendenin, Nucleonics, 2, No. 1, 1948, p 12.



CHAP. 2.3 RADIATION SHIELDING

X-RAYS IN THEORY AND EXPERIMENT, A. H. Compton and S. K. Allison, Van Nostrand, N. Y., 1948, Chaps. III and VII. THE QUANTUM THEORY OF RADIATION, W. Heitler, Oxford, London, 2nd edition, 1944.

STATUS REPORT ON CALCULATIONS OF GAMMA RAY PENETRATION, Nuclear Development Associates, R. Aronson and H. Goldstein, NDA-15C-1, Nov. 6, 1952, 31 pp.

PENETRATION OF X AND GAMMA RAYS TO EXTREMELY GREAT DEPTHS, Nat. Bu. Standards, U. Fano (to be published in Jour. Res. Nat. Bu. Standards).

PENETRATION AND DIFFUSION OF X-RAYS, CALCULATION OF SPATIAL DISTRIBUTIONS BY POLYNOMIAL EXPANSION, Nat. Bu. Standards, L. V. Spencer and U. Fano, Jour. Res. Nat. Bu. Standards 46, 1951, p 446.

X-RAY PROTECTION DESIGN, Nat. Bu. Standards, H. O. Wyckoff and L. S. Taylor, Nat. Bu. Standards Handbook 50, May 9, 1952, 36 pp.

X-RAY AND RADIUM PROTECTION, H. O. Wyckoff and C. B. Braestrup (to be published by Charles C. Thomas, Springfield, Illinois).



#### CHAPTER 2.4

# **Neutron Attenuation**

## A. Simon

#### INTERACTION PROCESSES*

In passing through matter, a neutron will lose energy or be removed only by collisions with nuclei. If the total kinetic energy is conserved in collision with nucleus X, the reaction may be written as X(n,n)X and is called elastic scattering. However, if the re-emitted neutron leaves the target nucleus in an excited state X', the process is called inelastic scattering and may be written X(n,n)X'. Finally, the neutron may induce a nuclear reaction which leads to a different residual nucleus, Y, and new end products. If the end product is a capture gamma ray, the reaction  $X(n,\gamma)Y$  is called radiative absorption, and if a particle (or particles) emerges, a particle reaction  $[X(n,p)Y, X(n,\alpha)Z, \text{ etc.}]$  has occurred.

A table of neutron cross sections has been prepared by the AEC Cross Sections Committee and issued as AECU-2040. The data listed are for total cross sections (the sum of elastic scattering and reaction processes).

# ABSORPTION $X(n,\gamma)Y$

For low-energy neutrons (less than about 1 kev), the only reactions that occur with appreciable cross section in nuclear collisions are elastic scattering and radiative absorption. Exceptions to this are some particle reactions in very light nuclei and fission in the very heavy nuclei. Elastic scattering serves only to alter the direction and degrade the energy of the neutrons. Ultimately, except for the cases just mentioned, the neutrons are captured with the emission of one or more gamma rays.

Upon capturing a slow neutron, the resultant compound nucleus has an excitation approximately equal to the binding energy of the neutron (~8 mev). The nucleus may release this energy with the emission of a single gamma ray and go to its ground state. However, if the nucleus has some intermediate energy levels between 8 mev and its ground state, it may instead emit several lower-energy gamma rays in cascade while going to the lowest state. In light nuclei or in the so-called "magic" nuclei, the average level spacing is large, and gamma transitions are often directly to the ground state. Table 2.1.7 summarizes the current capture gamma-ray data.

The existence of capture gamma rays greatly complicates the shielding problem since it is no longer sufficient merely to slow down and capture the neutrons. Owing to the  $(n,\gamma)$  reaction, these neutrons now give rise to new sources of energetic gamma rays at the point

^{*}See also Section 1 this volume.

CHAP. 2.4 RADIATION SHIELDING

of capture. One means of suppressing these capture gamma rays is to include small quantities of a material, such as boron, which has a very high cross section for thermal neutron capture via an  $(n,\alpha)$  reaction (see "Particle Reactions X(n,p)Y and  $X(n,\alpha)Z$ ," below). It should be noted that there is another source of secondary gamma radiation. These are gamma rays that may accompany inelastic neutron scattering (see "Inelastic Scattering X(n,n)X'," below). At higher energies of the order of 1 mev, elastic and inelastic scattering and particle reactions become dominant.

# ELASTIC SCATTERING X(n,n)X

Elastic neutron scattering may occur in two ways: (1) By actual formation of a compound nucleus followed by re-emission of the neutron leaving the nucleus in its ground state. The cross section for this type of scattering shows the usual resonance structure at neutron energies below about 10 mev. (2) By so-called "potential" scattering in which the neutron does not appreciably penetrate the nuclear surface. The cross section for this process shows no resonance structure and decreases monotonically with increasing neutron energy. It should be clearly noted that the "resonance" elastic scattering and the "potential" scattering contributions are coherent. Hence, the resultant cross section is not simply the sum of the two.

For low-energy neutrons (less than about 1 mev), the angular distribution of scattering is isotropic in the center-of-mass system. As the energy increases, asymmetries appear. (The exception to this is scattering in hydrogen where spherical symmetry is observed up to 13 mev.) The angular distribution owing to the "resonance" elastic scattering is characteristic of the spins of the levels of the compound nucleus involved and is more or less isotropic. The "potential" scattering shows a strong forward peak (owing to shadow scattering or diffraction around the nucleus) which becomes more pronounced with increasing energy.

At energies of a few mev, the elastic scattering often approaches the conditions appropriate to the continuum approximation (see Chapter 1.2). That is, the compound nucleus, once formed, has so many different available modes of breakup that "resonance" elastic scattering occurs with essentially zero probability. In this case, the elastic scattering is entirely "potential," and a strong forward peak is seen. The elastic scattering cross section, then, approaches the limit of  $\pi R^2$  (where R is the nuclear radius) for high energies while the total cross section approaches the limit  $2\pi R^2$ . Experimental verification of the shadow peak has been demonstrated by Jurney et al.

Owing to the fact that total kinetic energy is conserved in elastic scattering, it is possible to write a simple relation connecting neutron scattering-angle and energy (this is given in Chapter 1.2).

# INELASTIC SCATTERING X(n,n)X'

Inelastic scattering is the result of the decay of the compound nucleus to an excited state of the target nucleus. The process is not energetically possible until the incident neutron has enough energy to raise the target nucleus to its first excited state. As a result, thresholds for this process will be generally higher in both the light and magic nuclei where level spacings are larger. Little experimental information is available on inelastic scattering. Cross sections are available for 2.5-mev neutrons for several light nuclei^{2,3} as well as for 15-mev neutrons.^{4,5,6} A compilation of inelastic scattering cross sections is being made by the AEC Cross Sections Committee.

In most cases, the excess energy of the residual nucleus is removed by the emission of one or more gamma rays. Some data on inelastic gamma rays are available. 1-6

¹References appear at end of chapter.

**NEUTRON ATTENUATION CHAP. 2.4** 

Inelastic scattering can be useful in shields since this process will degrade neutrons to an energy below the inelastic threshold. However, light materials must still be used to further degrade the neutrons, and in addition, the secondary inelastic gamma rays may constitute a problem.

## PARTICLE REACTIONS X(n,p)Y AND $X(n,\alpha)Z$

A part of the neutron cross section above about 1 mev will be made up of various particle reactions. Below this energy, these reactions are inhibited either by the energetics of the process or by the necessity of barrier penetration by the charged particles which are the reaction products.

Of particular interest in shielding are some light-particle reactions which occur with thermal neutrons. These reactions can be used to avoid gamma rays and are listed in Table 2.1.6.

#### HYDROGEN CROSS SECTION

The neutron-proton scattering cross section is isotropic up to 13 mey and has been put in a convenient form by several authors. From the work of Blatt and Jackson. 7 the cross section  $\sigma$  can be written as:

$$\sigma = \frac{3}{4} \sigma_{t} + \frac{1}{4} \sigma_{g}$$

where:

$$\sigma_{\rm t} = \frac{4\pi}{{\rm k}^2} \sin^2 \delta_{\rm t}$$

$$\sigma_{\rm S} = \frac{4\pi}{k^2} \sin^2 \delta_{\rm S}$$

$$k \cot \delta_t = -\frac{1}{a_t} + b_t k^2$$

$$k \cot \delta_8 = -\frac{1}{a_8} + b_8 k^2$$

k being the neutron wave number, and:

$$k^2 = 1.21 \times 10^{24} \text{ E cm}^{-2}$$

if E is in mev. Adequate agreement with experimental results is obtained by taking:

$$a_t = 0.54 \times 10^{-12} \text{ cm}$$
  $a_s = -2.37 \times 10^{-12} \text{ cm}$ 

$$a_a = -2.37 \times 10^{-12} \text{ cm}$$

$$b_t = 0.89 \times 10^{-13} \text{ cm}$$

$$b_t = 0.89 \times 10^{-13} \text{ cm}$$
  $b_s = 0.135 \times 10^{-12} \text{ cm}$ 

A very convenient approximation to  $\sigma$  is given by:

$$\sigma = \frac{10.97}{E + 1.66}$$

where  $\sigma$  is in barns and E is in mev. Table 2.4.1 compares the exact and approximate ex-

CHAP. 2.4 RADIATION SHIELDING

pressions for hydrogen cross section. This expression is good from 3 mev to the maximum energies of interest. Of particular interest to shielding is the steep monotonic increase of the hydrogen cross section with decreasing neutron energy. This effect makes hydrogen a very desirable component of a shield as is discussed more fully in the next chapter.

Table 2.4.1 — Comparison of Exact and Approximate Hydrogen Cross Sections

	Hydrogen cross section $(\sigma)$ , barns					
E, mev	Exact	Approximate				
0	20.3	6.6				
2	2.91	3.00				
4	1.94	1.94				
6	1.43	1.43				
8	1.14	1.14				
10	0.94	0.94				
12	.79	.80				

#### EFFECTIVE REMOVAL CROSS SECTION

If neutron reactions in matter consisted solely of particle reactions and capture, the problem of neutron attenuation would be very simple. A neutron source of a given energy  $E_0$ , in a plane geometry, would be attenuated according to a simple exponential law:

$$I \sim e^{-\Sigma(E_0)t} \tag{1}$$

where  $\Sigma(E_0)$  is the macroscopic total neutron cross section and t is the thickness of material traversed. In an actual material, however, elastic and inelastic scattering is occurring, and as a result, there are large numbers of degraded neutrons being attenuated as well. The resultant observed attenuation is no longer purely exponential. Instead, it has the general form of an exponential, corresponding to the source attenuation, times a buildup factor. Thus:

$$I \sim B(t, E_0)e^{-\sum (E_0)t}$$
 (2)

where B depends on the initial source energy,  $E_0$ , as well as on the depth of penetration. At large distances of penetration, the buildup factor might be expected to be very large since only a small fraction of the neutrons will be uncollided. For example, a total thickness of 20 mean-free-paths is not uncommon in shielding work.

The situation is changed, however, if the shield is made up partly of hydrogenous material. It has been noted (Table 2.4.1) that the hydrogen cross section increases steeply with decreasing neutron energy. As a result, once a neutron suffers a hydrogen collision, it is essentially removed from the beam. This effect is caused by: (1) the large energy loss that usually occurs in such a collision, which makes subsequent collisions much more probable, and (2) altering of the direction of travel of the neutron, which usually increases the path length necessary for the neutron to move from the source to a detector, again increasing the probability of subsequent hydrogen collisions. It is this second effect which makes even an elastic collision with the heavy nuclei more effective since there is more probability of a subsequent hydrogen collision.



NEUTRON ATTENUATION CHAP. 2,4

It is now clear from the previous description of elastic scattering that "resonance" elastic scattering, which tends to have a nearly isotropic angular distribution, is approximately equivalent to absorption. On the other hand, not all of the "potential" elastic scattering is equivalent to absorption since the neutrons in the large forward diffraction peak (shadow scattering) are essentially undeflected. It is to be expected, therefore, that the attenuation in a shield composed of heavy material as well as hydrogen will behave very much like an exponential with an "effective removal cross section" which is somewhat smaller than the total cross section. Qualitatively, this cross section,  $\sigma_r$ , is the sum of the actual reaction and capture cross sections, the inelastic cross section, and that part of the elastic scattering which is not in the "shadow" peak. Employing this definition, one obtains:

$$I \sim B(E_0, t)e^{-\sum_r t}$$
 (3)

Now, the buildup factor is expected to remain reasonably small.

The precise value of the removal cross section could not be calculated from the qualitative definitions which have been given, even if the neutron cross sections were known. Instead, it is obtained experimentally by bulk shielding measurements at a facility such as the ORNL Lid Tank. 9,10 Specific analyses are indicated later in this chapter. The use of the removal cross section in calculating the attenuation of neutron dose in a shield is discussed below under "Use of Removal Cross Section."

# ATTENUATION OF FISSION NEUTRONS IN WATER (REMOVAL CROSS SECTION FOR OXYGEN)

The most convenient hydrogenous shielding material is water. Here the oxygen plays the role of a heavy element, and it should be possible to define a removal cross section. Figure 2.4.1 illustrates the results of neutron-attenuation measurements in the Bulk Shielding Facility and Lid Tank Facility at ORNL. 9,10 All data are transformed to the case of a plane-collimated fission source of 1 watt/cm² strength. The solid curve shows the result of a calculation of the attenuation in water assuming no oxygen attenuation but properly taking into account the hydrogen cross section and buildup. The other two curves indicate attempted fits including an oxygen-removal cross section of 0.6 and 0.7 barns. It is seen that 0.7 barns gives the best fit to the BSF data. This disagreed somewhat with a determination based on thermal-neutron attenuation in the Lid Tank⁸ which gave  $\sigma_r = 0.91$  barns. The uncertainty in the oxygen measurement is a result of the particular geometry of the experiment. An ideal way to measure a removal cross section of solids is to insert a slab of the material to be tested into the water of the Lid Tank. The resulting attenuation curve at long distances behind this slab is then compared with the same curve for pure water, and a removal cross section is easily determined. This procedure was used for iron and lead. Oxygen, however, is distributed throughout the medium, and the entire water curve must be fitted by an exponential times the hydrogen attenuation. The uncertainty in this fitting leads to the uncertainty in the oxygen removal cross section.

## ATTENUATION IN LEAD

Measurements have been made in the ORNL Lid Tank of the attenuation of neutrons in water behind a series of alternating layers of Pb and H₂O.¹¹ Thermal measurements were made at distances varying from 90 to 150 cm from the source plate and for a varying number of lead slabs. These data were analyzed by Podgor,¹² and a removal cross section of 3.4 barns was found for lead. This agrees very well with an earlier determination by Albert and Welton.⁸



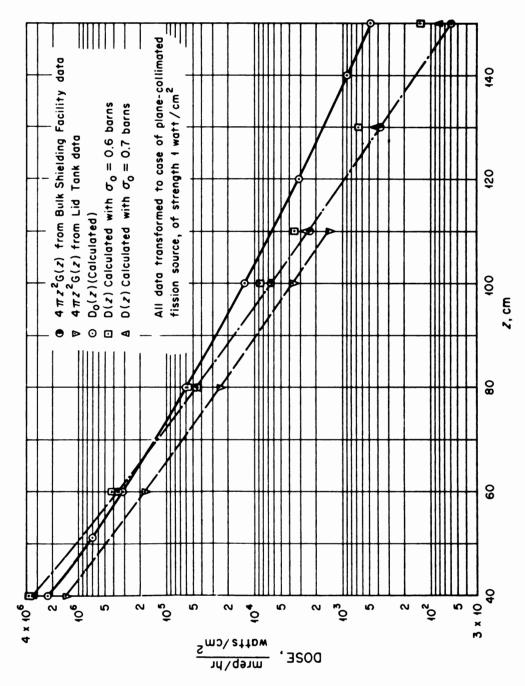


Fig. 2.4.1 — Comparison of Neutron-dose Calculations with Experimental Values for a Water Shield. Submitted by Oak Ridge National Laboratory, Nov. 7, 1952.

NEUTRON ATTENUATION CHAP. 2.4

#### ATTENUATION IN IRON

Lid Tank measurements of neutron attenuation in borated water behind a series of iron slabs has been reported.¹³ Analysis of these data¹² yields a removal cross section of 2.0 barns for iron. This also in agreement with an earlier determination.⁸

## USE OF REMOVAL CROSS SECTION

A number of removal cross sections are tabulated in Table 2.4.2. The results for Pb and Fe are probably good for the listed significant figures.

The attenuation for a mixture of a heavy material and water is now simply:

$$I = I_0 e^{-\sum_r t_h} D(t_w)$$

#### where:

 $I_0$  = effective source strength (taken to be a plane-collimated source)

 $\Sigma_r$  = removal cross section of heavy materials

th = total thickness of heavy materials

 $t_w = total thickness of water$ 

 $D(t_w)$  = attenuation in water taken from the experimental curves in Fig. 2.4.1

Table 2.4.2 — Removal Cross Sections

Substance	$\sigma_{\rm f}$ , barns/atom
Al	1.2
С	0.84
Cu	2.0
Fe	2.0
Pb	3.4

The use of these removal cross sections, together with the measured water attenuation (Fig. 2.4.1), in calculating the attenuation of neutron dose in a shield is valid as long as large thicknesses of heavy material do not occur. Large thicknesses of heavy material (i.e., with no interposition of hydrogenous material) will allow streaming-through of neutrons in the energy region below about 1 mev because heavy materials attenuate neutrons by inelastic scattering only down to the threshold for this process (around 1 mev).

Below this energy only elastic scattering occurs, and this effect is very inefficient. As a result, the attenuation of dose will be much smaller than the calculated value. The <u>fast</u> neutron flux, of course, is still correctly accounted for.

#### ATTENUATION IN CONCRETE

Experiments on the neutron attenuation of ordinary concretes have been made at the "core hole" shielding facility^{9,10} at Oak Ridge. The results of these experiments have been summarized. ¹⁶ Of particular interest in shielding are Portland concrete, boron cement, Brookhaven concrete, and W-1 concrete. Portland concrete was composed of four parts Tennessee limestone gravel, two parts river sand, and one part Portland cement. Boron

CHAP. 2.4 RADIATION SHIELDING

cement consists of equal weights of MgO and colemanite, gauged with saturated MgCl₂ solution. Brookhaven and W-1 concretes are mixtures of Portland cement and iron aggregate. Barytes concrete, a mixture of BaSO₄ aggregate and Portland cement, is also of great use in shielding today.

Table 2.4.3 lists the approximate atomic compositions of the various concretes. The water content, which is the most variable quantity in concrete mixes, is that found in the cured state. The fast-neutron attenuation lengths observed in the various shields are summarized in Table 2.4.4. An extensive bibliography of concrete shielding literature may be found in a recent Hanford report.¹⁸

Table 2.4.3 — Approximate Atomic Composition of the Various Concretes and Cements

	Elemental components, atoms/cc or moles/liter													
Material	Fe	Н	В	0	Mg	Cl	Ca	Ba	Si	Al	Mn	S	С	Total
Portland concrete	0.13	4.8		71.8	0.2		14.5		15.6	0.44		0.06	10.8	118.3
Boron cement	• • •	79.1	7.98	68.2	16.42	6.93	2.66							181.3
Brookhaven concrete	54.7	21.1		47.7	0.35		6.45		2.10	0.79	1.22	0.11		134.5
W-1 concrete	40.5	20.1	3.28	38.8	.62		12.15		3.65	1.36	0.21	.18		120.8
Barytes concrete	0.11	5.17	• • •	<b>63.</b> 5	.2	• • •	3.4	11.9	4.1	0.4	• • •	12.0	• • •	100.8

Table 2.4.4 — Measured Relaxation Lengths in Various Concretes and Cements

		Relaxation length,
Shield	Density	cm
Portland concrete	2.3	11.1
Boron cement	2.0	7.6
Brookhaven concrete	4.3	6.3
W-1 concrete	3.6	6.6
Barytes concrete	3.5	8.0

#### REFERENCES

- E. T. Jurney et al, Inelastic Collision and Transport Cross Sections for Some Light Elements, Los Alamos Scientific Lab., LA-1339, Dec., 1951, 14 pp.
- 2. M. A. Grace, L. E. Beghian, G. Preston, and H. Halban, The Inelastic Scattering of Fast Neutrons, Phys. Rev. 82, 1951, p 969.
- 3. H. H. Barschall et al, Measurement of Transport and Inelastic Scattering Cross Sections for Fast Neutrons, IL. Experimental Results, Phys. Rev. 72, 1947, p 881.
- 4. P. H. Stelson and C. Goodman, The Inelastic Scattering of 15-mev Neutrons By Lead, Iron, and Aluminum, Phys. Rev. 82, 1951, p 69.
- 5. B. G. Whitmore and G. E. Dennis, The Inelastic Scattering of Fast Neutrons in Lead and Bismuth, Phys. Rev. 84, 1951, p 296.
- 6. P. H. Stelson and W. M. Preston, The Inelastic Scattering of Fast Neutrons from Iron, Phys. Rev. 86, 1952, p 132.
- 7. J. M. Blatt and J. D. Jackson, On the Interpretation of Neutron-Proton Scattering Data by the Schwinger Variational Method, Phys. Rev. 76, 1949, p 18.
- 8. R. D. Albert and T. A. Welton, WAPD-15, Nov. 30, 1950, 39 pp (classified).
- 9. T. A. Welton and E. P. Blizard, TID-2002, Aug. 1952, p 73 (classified).
- 10, E. P. Blizard, Part II, ORNL-51-10-70 Revised, Mar. 7, 1952, 42 pp (classified).
- 11. ORNL-858, Nov. 29, 1950, p 19 (classified).
- 12. S. Podgor, ORNL-895, Jan. 23, 1951, 16 pp (classified).
- 13. ORNL-919, Feb. 26, 1951, p 105 (classified).
- 14. Deleted.
- 15. Deleted.
- 16. H. P. Sleeper, Jr., ORNL-436, Dec. 21, 1949, 48 pp (classified).
- 17. Deleted.
- 18. T. A. Linxweiler, HW-24071, April 9, 1952, 153 pp (classified).

#### CHAPTER 2.5

# Geometry

#### E. P. Blizard

Most shields are designed by comparison with others which have been measured. Since the geometries differ from one situation to another, transformations are required which will predict the radiation to be expected in one situation on the basis of an observation in another. A discussion of these transformations is based on the following fundamentals.

Flux, probably the most basic type of measurement, is variously described as "particle density times average speed," or "rate of events divided by the macroscopic cross section." It is probably described most graphically in terms of the radiation incident on a small totally absorbing sphere. For this non-directional detector, the flux is the incident radiation divided by its projected area. In case the detector is not totally absorbing, the reading will be somewhat less and can therefore be associated with a smaller effective cross-sectional area. This is the case with nuclear cross sections, the areas being so chosen that they will correctly describe the rate of occurrence of a particular event (e.g., absorption).

Biological dose is usually assumed to be proportional to the flux, and this will be exactly true if no self-shielding occurs in the receptor (e.g., man). Since it is conservative to assume no receptor self-shielding, this is usually done. The dose with no self-shielding is often referred to as the "milligoat" reading, this being the dose to be expected in a very small sphere of flesh.

<u>Current</u> is simply the radiation passing through a surface per unit surface area. This radiation is recorded on a flat detector oriented normal to some preferred direction, so that in effect the response of the detector is proportional to the cosine of the direction of arrival with the preferred direction. Current is thus a vector quantity as opposed to flux which is a scalar.

The difference between flux and current is illustrated by the response of foil detectors. Thin foils, for which self-absorption is negligible, appear to be an array of widely spaced spheres (nuclei) and hence record the flux. On the other hand a thick foil, being essentially black to the radiation, records current normal to the foil.

In shielding, the flux is of most interest, since this is usually more conservative as an estimate of the dose. Since "flux" has been used in other fields in the same connotation as "current," the term "dose" has been adopted for shielding work and unless otherwise specified is assumed to be the dose with no receptor self-shielding.

"Attenuation function" or "attenuation kernel" is defined in terms of the response of a detector to radiation from a nearby source. This function is therefore dependent on the medium, the source, the detector, and the distance between source and detector if flux is to be measured. If current is to be measured, an additional variable specifying direction is necessary.

For a dose detector a distance R from an isotropic source of unit strength, the reading would be:

CHAP. 2.5 RADIATION SHIELDING

$$D_{\mathbf{p}_{\mathbf{f}}}(\mathbf{R}) = \mathbf{G}(\mathbf{R}) \tag{1}$$

This equation is then adequate to define the dose attenuation kernel G(R). It is of course assumed throughout that dose will vary linearly with source strength. The applicability of Eq. (1) to actual cases should be carefully considered before the transformations discussed below are used; the following conditions in particular should be noted:

- (1) The detector and source(s) must be isotropic.
- (2) The medium must attenuate equally in all directions and in all regions.
- (3) Boundaries must be far removed or unimportant.

The first condition is easily met. The second often is not met, especially for the case of gamma rays in, for example, a laminated lead-water shield. The third condition is almost never met, but fortunately the boundaries usually have a constant effect so that the transformations are nevertheless not much affected.

#### TRANSFORMATIONS FOR UNSPECIFIED ATTENUATION FUNCTIONS

The first and most general class of transformations to be considered is that in which the attenuation function is totally unspecified. For this case, the attenuation function must be independent of angle, as indicated by Eq. (1).

#### POINT TO INFINITE PLANE

For an infinite plane of isotropic sources of unit strength per unit plane area embedded in an infinite medium, the dose to be expected at a distance z from the plane is:

$$D_{DI}(z,\infty) = 2\pi \int_{-\infty}^{\infty} G(R) R dR$$
 (2)

This equation is useful when G(R) is known, either from measurement or calculation. On the other hand, the measurement may have given the dose from the plane-distributed source, in which case the differentiated form of Eq. (2) is useful:

$$G(z) = -\frac{1}{2\pi z} \frac{d}{dz} D_{Pl}(z, \infty)$$
 (3)

## POINT TO PLANE DISK

In case the plane isotropic source of unit surface strength is limited to a disk of radius a, the dose at a point on the axis a distance z from the disk (see Fig. 2.5.1) is:

$$D_{p_1}(z,a) = 2\pi \int_z^{\sqrt{z^2+a^2}} G(R) R dR$$
 (4)

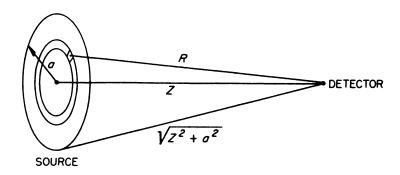


Fig. 2.5.1—Disk Source and Dose Detector. Submitted by Oak Ridge National Laboratory, Oct. 28, 1952.

#### PLANE DISK TO POINT

The inverse of the previous transformation is obtained by differentiating Eq. (4) with respect to z. This then leads¹ to the following series:

$$G(z) = \sum_{\nu=0}^{\infty} B(\sqrt{z^2 + \nu a^2})$$
 (5)

where:

$$B(z) = -\frac{1}{2\pi z} \frac{d}{dz} D_{Pl}(z,a)$$

The use of this transformation is illustrated in Fig. 2.5.2.

#### PLANE DISK TO INFINITE PLANE (HURWITZ TRANSFORMATION)

By quite similar manipulation,² the dose to be expected with an infinite plane source can be found in terms of measurements on the axis of a finite disk source. Both sources are assumed to have unit strength per unit area and to be isotropic:

$$D_{\text{Pl}}(\mathbf{z},\infty) = \sum_{\nu=0}^{\infty} D_{\text{Pl}}(\sqrt{\mathbf{z}^2 + \nu \mathbf{a}^2}, \mathbf{a})$$
 (6)

Thus, the dose at a distance "z" away from an infinite plane source is just equal to the sum of readings on the axis of a disk of radius "a" taken at z,  $\sqrt{z^2 + a^2}$ ,  $\sqrt{z^2 + 2a^2}$ , etc. In case "a" is large compared with the apparent attenuation length of the disk measurements, this will converge quickly, although not as quickly as the series represented by Eq. (5).

If the dose on the disk axis can be well represented in the region beyond some distance  $z_0$  by:

$$D_{pl}(z,a) = D_{pl}(z_0,a) e^{-(z-z_0)/\lambda}$$
 (7)

then the exact expression, Eq. (6), can be approximated for  $z \simeq z_0$  by the inequality:

$$1 + \alpha > \frac{D_{\mathrm{pl}}(\mathbf{z}, \infty)}{D_{\mathrm{pl}}(\mathbf{z}, \mathbf{a})} \simeq \frac{1}{2} + \alpha \tag{8}$$

where:

$$\alpha = \frac{2\lambda^2}{a^2} \left( \frac{z}{\lambda} + 1 \right)$$

Note that in Eq. (8) the upper limit  $(1/2 + \alpha)$  is a closer approximation to the true value of the ratio of doses. Furthermore, most experimental data vary from the condition expressed by Eq. (7) in such a way that the ratio in Eq. (8) is increased; that is, the left hand side of Eq. (7) becomes greater than the right at large values of  $z - z_0$ . Equation (8), therefore, may not give a genuine upper limit.

#### PLANE TO SPHERE

If an isotropic source of unit strength per unit area is spread on a spherical surface which is wholly within an attenuating medium, it is possible to predict the dose as a function of distance from this surface if the dose is known for the case of an infinite-plane

¹References appear at end of chapter.

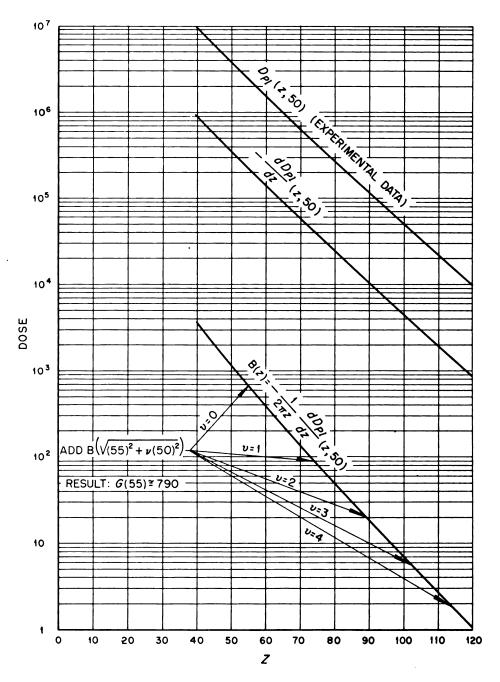


Fig. 2.5.2—Illustration of Plane Disk to Point Transformation. Submitted by Oak Ridge National Laboratory, Oct. 28, 1952.

isotropic source. Strictly, the material inside the sphere must be the same as that outside, and the source must be so thin as not to affect the attenuation. Actually, however, neither of these conditions need be very closely met, since most of the observed dose comes from radiation which travels more or less directly through the shield from the nearest source region. The dose at a distance  $r_0$  from the center of the sphere whose radius is  $r(r_0 > r)$  is:

$$D_{s}(r_{0},r) = \frac{r}{r_{0}} \left[ D_{pl}(r_{0} - r, \infty) - D_{pl}(r_{0} + r, \infty) \right]$$
(9)

where the quantities in the brackets are the doses to be expected at distances of  $r_0 - r$  and  $r_0 + r$  from infinite-plane sources of the same surface source strength.

If the attenuation length for the plane data is sufficiently small, then the second term in the square brackets can be ignored:

$$D_{s}(r_{0},r) \approx \frac{r}{r_{0}} D_{pl}(r_{0} - r,\infty)$$
(10)

when  $\lambda \ll 2r$ .

#### PLANE TO CYLINDER

There is no simple and general transformation for this case, but it can be shown that for most attenuation functions the following expression is approximately correct for the dose at a distance r from the axis of an infinitely long cylinder of radius  $r_0$  with uniform isotropic surface source strength:

$$D_{c}(r_{0},r) \approx \sqrt{\frac{r}{r_{0}}} D_{pl}(r_{0}-r,\infty)$$
(11)

Strictly, the material inside the cylinder should match that outside in attenuation, but in most applications, this will make little difference.

## TRANSFORMATIONS FOR PARTIALLY SPECIFIED ATTENUATION FUNCTIONS

# SOURCE ON A QUADRIC SURFACE

For the purposes of this derivation, the form of the attenuation function is unspecified for the distance z from the detector to the nearest source point. For other points of the source, the increased attenuation is assumed to be a pure exponential, that is:

$$G(R) \approx G(z) e^{-(R-z)/\lambda}$$
 (12)

The geometry is shown in Fig. 2.5.3.

The detector is on the Z axis, a distance z from origin; the unit strength isotropic source is assumed to be spread uniformly on a quadric surface tangent to X,Y plane. The equation of the surface near the origin is:

$$z_1 \approx -\frac{1}{2} \left( \frac{(x_1)^2}{a} + \frac{(y_1)^2}{b} \right)$$
 (13)

where  $z_1$  = distance from source surface to X,Y plane; a = radius of curvature in Y,Z plane; and b = radius of curvature in X,Z plane. The dose at (z,0,0) is then given by:

CHAP. 2.5 RADIATION SHIELDING

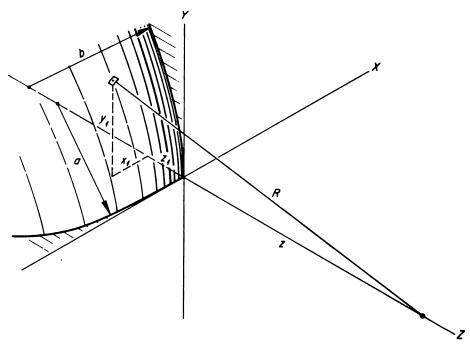


Fig. 2.5.3—Geometry for Quadric Surface Source. Submitted by Oak Ridge National Laboratory, Oct. 29, 1952. Only one quadrant shown.

$$D_{\mathbf{q}}(\mathbf{z}, \mathbf{a}, \mathbf{b}) \approx 2\pi G(\mathbf{z}) \left[ \frac{1}{\left(\frac{1}{\lambda \mathbf{z}} + \frac{1}{\lambda \mathbf{a}}\right)^{l/2}} \left(\frac{1}{\lambda \mathbf{z}} + \frac{1}{\lambda \mathbf{b}}\right)^{l/2}} + \frac{1}{2\mathbf{a}^2 \left(\frac{1}{\lambda \mathbf{z}} + \frac{1}{\lambda \mathbf{a}}\right)^{l/2}} \left(\frac{1}{\lambda \mathbf{z}} + \frac{1}{\lambda \mathbf{b}}\right)^{l/2}} + \frac{1}{2\mathbf{b}^2 \left(\frac{1}{\lambda \mathbf{z}} + \frac{1}{\lambda \mathbf{a}}\right)^{l/2}} \left(\frac{1}{\lambda \mathbf{z}} + \frac{1}{\lambda \mathbf{b}}\right)^{l/2}} \right]$$
(14)

For a,b  $\gg \lambda$ :

$$D_{q}(z,a,b) = 2\pi G(z) \left[ \frac{1}{\left(\frac{1}{\lambda z} + \frac{1}{\lambda a}\right)^{1/2}} \left(\frac{1}{\lambda z} + \frac{1}{\lambda b}\right)^{1/2}} \right]$$

For a derivation of this expression, see Welton and Blizard.³

SPECIAL CASES

For a plane surface,  $a,b \rightarrow \infty$ , and:

$$D_{pl}(z,\infty) = 2\pi z \lambda G(z)$$
 (15)

This is directly comparable to Eq. (3).

For a spherical surface, a = b = r, and for these, which are much larger than  $\lambda$ :

$$D(z,r) \cong 2\pi\lambda G(z) \frac{zr}{z+r}$$
 (15a)

The same result can be found from combination of Eqs. (3) and (10).

#### SOURCE ON A PLANE SURFACE — THE EFFECTIVE SOURCE AREA

It has been pointed out by Tonks that it is possible to define an "effective source area," an "effective cone of radiation," and an "effective solid angle of radiation" for the case of a uniform isotropic source on a plane surface (see Fig. 2.5.4).

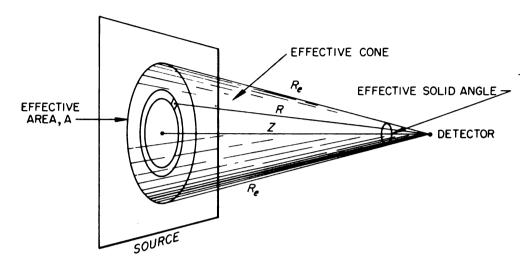


Fig. 2.5.4—Geometry of Effective Source Area. Submitted by Oak Ridge National Laboratory, Oct. 30, 1952. Cone of radiation, and solid angle of radiation.

The effective source area A is defined as that part of the plane source contained within a circle centered at the base of the perpendicular from detector to source of such size that:

$$\mathbf{D}_{\mathbf{p}_{1}}\left(\mathbf{z},\infty\right) = \mathbf{A}\mathbf{D}_{\mathbf{p}_{1}}\left(\mathbf{z}\right) \tag{16}$$

In other words, if all the sources on A were located at a point a distance z from the detector, the dose would just equal the dose from the original whole plane of sources.

Using the approximation characteristic of this section, Eq. (12), for substitution in Eq. (2), it is seen by simple integration that:

$$\mathbf{D}_{\mathbf{D}_{1}}(\mathbf{z}, \infty) = 2\pi(\lambda \mathbf{z} + \lambda^{2})\mathbf{G}(\mathbf{z}) \tag{17}$$

Or, in the light of Eqs. (1) and (16):

$$\mathbf{A} = 2\pi(\lambda \mathbf{z} + \lambda^2) \tag{18}$$

and the distance from the edge of the effective source to the detector is:

$$R_e = \sqrt{(z+\lambda)^2 + \lambda^2} \approx z + \lambda \quad \lambda \ll z$$
 (19)

In other words, the effective source area is just that circle of source which is within a distance greater by one relaxation length than the nearest point. The effective cone of radiation is thus that cone defined by A and the detector. The effective solid angle is:

$$\Omega_{e} = 2\pi \left( \frac{R_{e} - z}{R_{e}} \right) \tag{20}$$

$$pprox 2\pi \, rac{\lambda}{R_e} \qquad \lambda \ll z$$
 (20a)

The effective source area concept is often quite useful in estimating the intensity to be expected from unusual source shapes. Tonks' method consists simply in using the part of the actual source which lies within the effective source area as if it were the only source. Thus, if A is the source area which is within A, then the dose is taken to be:

$$D_{A_1}(z) = \frac{A_1}{A} D_{p_1}(z, \infty) = A_1 D_{p_1}(z)$$
 (21)

This formula must of course be used with caution, paying attention to the possibility that other sources outside the effective source area might contribute significantly by virtue of a large source density. In the computation of the effects of variations in the shield, these can be expected to be most effective when they occur within the effective cone of radiation.

#### TRANSFORMATIONS FOR THE SIMPLE ATTENUATION FUNCTIONS

For many shielding calculations, a simple form is chosen for the basic attenuation function, and with this, the geometric manipulations then become more or less straightforward. The more common situations are illustrated below.

#### THE ATTENUATION FUNCTIONS, ONE REGION

The basic attenuation function is of course the simple exponential on which is superimposed the inverse-square-law attenuation. For this assumption, the dose at a distance R from a unit strength (one per unit time) source is simply:

$$G_1(R) = \frac{e^{-\mu R}}{4\pi R^2}$$
 (22)

where  $\mu$  is called the attenuation coefficient, a characteristic of the medium, of the source, and (in most cases) of the detector. This expression applies rigorously only to unscattered radiation. Allowance is made for scattered radiation by inclusion of a so-called "buildup factor," which is a function not only of source, medium, and detector, but also of the distance from the source. This is usually expressed as follows:

$$G(\mathbf{R}) = \frac{B(\mu \mathbf{R})e^{-\mu \mathbf{R}}}{4\pi \mathbf{R}^2} \tag{23}$$

It is clear that Eq. (22) expresses a special case of Eq. (23), namely, that for which B=1. This is referred to as a unitary buildup factor.

#### BUILDUP FACTORS

While a more complete discussion of the computation of a buildup factor is not given here, a simple approximation is described. For gamma-ray attenuation in which the Compton process is dominant for the source energy, a linear buildup factor gives a reasonable approximation for large attenuations of the total energy flux. Specifically, for thick shields:



$$\mathbf{B} \approx \mu \mathbf{R} \tag{24}$$

This approximation does not fit the situation for thin shields [note that for  $\mu R < 1$ ,  $G(R) < G_1(R)$ ]. As a consequence, for shields of intermediate thicknesses, the buildup factor is taken as a sum of unitary and linear buildup factors. Most generally:

$$\mathbf{B} \approx \mathbf{1} + \mathbf{k} \mu \mathbf{R} \tag{25}$$

where k is a constant best chosen to fit the situation. For the case of gamma rays of about 1 mev on lead, k is about unity. It has been demonstrated by Goldstein⁴ that it is possible to normalize the buildup factor to ensure a proper accounting of all the energy absorption. This would result in fixing k if Eq. (25) is chosen for the form of B.

Thus, if a source of unit strength of photons of energy  $E_0$  is embedded in a material and the detector reads simply heat release, then the heating due to previously uncollided photons is:

$$\mathbf{H_0}(\mathbf{R}) = \frac{\tau (\mathbf{E_0}) \ \mathbf{E_0} \ e^{-\mu (\mathbf{E_0}) \mathbf{R}}}{4\pi \mathbf{R^2}}$$
 (26)

where  $\tau(\mathbf{E}_0)$  is the energy absorption coefficient, referred to by Heitler⁵ as  $\mu - \sigma_s$ , and  $\mu(\mathbf{E}_0)$  is the total interaction coefficient. The buildup factor for heat generation is then defined by the following equation for the heat absorption from virgin as well as scattered flux:

$$\mathbf{H}(\mathbf{R}) = \mathbf{B}(\mu \mathbf{R}) \ \mathbf{H}_0(\mathbf{R}) \tag{27}$$

From the conservation of energy, the source must in equilibrium emit as much as is absorbed, i.e.:

$$\mathbf{E_0} = 4\pi \int_{\mathbf{R}=0}^{\infty} \mathbf{R^2} \mathbf{H}(\mathbf{R}) \ d\mathbf{R}$$

or:

$$\frac{1}{\tau(E_0)} = \int_{R=0}^{\infty} B(\mu R) e^{-\mu R} dR$$
 (28)

The latter equation can thus be used to determine "k" for a variety of photon energies and materials, but it is necessary to caution that the method is not applicable to large shield thicknesses.

# **ATTENUATION FUNCTIONS, MANY REGIONS**

For many regions, the problem becomes much more difficult, but a first estimate is obtained by simply extending the basic attenuation function on the basis of the ray lengths in the several regions:

$$\mathbf{G}(\mathbf{R}) = \mathbf{B}(\mu_1 \mathbf{R}_1 + \mu_2 \mathbf{R}_2 + \mu_3 \mathbf{R}_3 + \ldots) \frac{e^{-(\mu_1 \mathbf{R}_1 + \mu_2 \mathbf{R}_2 + \ldots)}}{4\pi \mathbf{R}^2}$$
(29)

where  $\mu_1$ ,  $\mu_2$ ,  $\mu_3$ , etc., are the attenuation coefficients;  $R_1$ ,  $R_2$ ,  $R_3$ , etc., are the ray lengths for the several media; and  $R = R_1 + R_2 + R_3 + \dots$ 

## **DEFINITIONS FOR TABLES**

In the tables of intensities (Tables 2.5.2 through 2.5.4) the following terms are used:

- (1) Unit Sources:
  - (a) <u>Isotropic surface</u>:* Emitting unit per second per square centimeter of surface, equally in all directions (both sides).
  - (b) Cosine Surface:* Emitting  $(\cos\theta)/4\pi$  per second per square centimeter of surface per steradian for  $0 < \theta < \pi/2$ , and emitting 0 for  $\pi/2 < \theta < \pi$ , where  $\theta$  is the angle between the outward-drawn normal to the surface and the direction of emission.
  - (c) Volume: Emitting unity per cubic centimeter per second isotropically from a region (herein referred to as region 1 and assigned an attenuation coefficient  $\mu_1$ ). A simple integration shows that this source in a plane-limited region is identical in radiation emitted with a cosine surface source on the plane emitting  $(\cos\theta)/4\pi\mu_1$  per second per sterad per square centimeter of surface.
  - (d) Filament: Non-self-absorbing straight-line source, emitting unity per centimeter per second isotropically.
- (2) Detectors:
  - (a) Non-directional (milligoat): Described earlier in this chapter.
  - (b) Cosine: Response proportional to cosine of angle between preferred direction and direction of arrival of radiation. (As described in the preceding text, of these two detector types, the non-directional detector indicates microscopic dose, ionization in a non-absorbing region, etc., whereas the cosine detector indicates total current through a plane, leakage, the source available for production of secondary radiation such as capture gamma rays, the rate of arrival on a completely absorbing surface, etc.)
- (3) Buildup Factors:
  - (a) Unitary:  $B(\mu R) = 1$  (no built-up radiation, as in a nonscattering medium).
  - (b) Linear:  $B(\mu r) = \mu_1 R_1 + \mu_2 R_2 + \dots$  (Combinations of these two can be had by linear addition, which is left to the reader).
- (4) Distance:
  - (a) z is always used as the distance from the detector to the nearest element of source, and the preferred direction is that of this ray.
- (5) Exponential Integral Functions: † (Table 2.5.1 and Figs. 2.5.6, 2.5.7, and 2.5.8)

$$\mathbf{E}_{\mathbf{n}}(\mathbf{x}) = \int_{\mathbf{x}}^{\infty} \frac{\mathbf{e}^{-\mathbf{p}}}{\mathbf{p}^{\mathbf{n}}} \, \mathrm{d}\mathbf{p} \tag{30}$$

$$= \frac{e^{-x}}{x^n} - n E_{n+1} (x)$$
 (31)

$$\approx \frac{e^{-x}}{x^n} (x \gg 1) \tag{31a}$$

## (6) Intensity:

This term refers to the response of the detector, either nondirectional, in which case flux is meant, or cosine, in which case current is implied. The use of the term "flux" in the table is avoided in order to circumvent the ambiguity arising from its occasional

^{*} Isotropic and cosine surface sources are chosen so that both radiate equally in the outward normal direction. This is illustrated in Fig. 2.5.5.

[†] Tabulated in "Tables of Sine, Cosine, and Exponential Integrals," prepared by the Federal Works Agency, Work Projects Administration, for the City of New York, A. N. Lowan, technical director, sponsored by the National Bureau of Standards, New York, 1940: also see tables of  $-Ei(-x) = E_1(x)$  in E. Jahnke, "Jahnke-Emde Tafeln hoheren Funktionen," B. G. Teubner Co., Leipzig, 1948.

 $\{j_{i,j}\}$ 

X STATE

Ifok

riige. Nee 131

init (7.6) (118 (118)

7 X S

. ....

T. I

(18) (16) (12)

37

زيبية

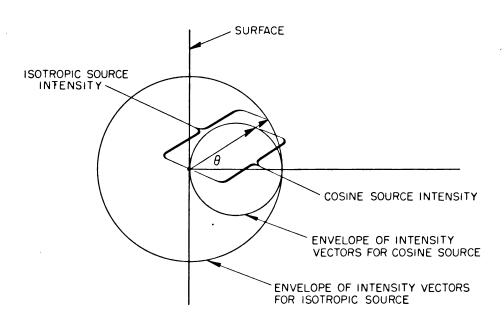


Fig. 2.5.5—Illustration of the Relative Strengths of the Isotropic Surface and Cosine Surface Sources as Used in This Chapter. Submitted by Oak Ridge National Laboratory, Oct. 28, 1952.

connotation of current. Whether number or energy (or other) flux or current is implied depends on the definition of the buildup factor and is not properly a subject for discussion under "geometry."

#### POINT TO LINE

Isotropic source distributed along a straight line, of strength unity per centimeter per second; nondirectional detector; linear build-up factor:

$$\mathbf{D}(\mathbf{z}) = \frac{\mu}{2\pi} \, \mathbf{K}_0(\mu \mathbf{z}) \approx \frac{\mu}{2\pi} \, \sqrt{\frac{\pi}{2\mu \mathbf{z}}} \, \mathbf{e}^{-\mu \mathbf{z}} \qquad (\mu \mathbf{z} \gg 1)$$
 (32)

#### SELF-ABSORBING SMALL CYLINDER

For the case of a source distributed in a cylinder for which self-absorption is important but for radius not large compared with relaxation lengths, see the referenced work. 6.7.8

#### REFERENCES FOR OTHER TRANSFORMATIONS

The foregoing transformations have been the most useful for general shield design. Occasionally, however, unusual configurations are of interest, and for these, reference is made to two project handbooks^{9,10} and to the comprehensive treatment of Wende.¹¹

Table 2.5.1— Exponential Integral Functions

x	$\mathbf{E_1}(\mathbf{x})$	$\mathbf{E_2}(\mathbf{x})$	$\mathbf{E_3}(\mathbf{x})$	x	E ₁ (x)	E ₂ (x)	E ₃ (x)
1.0	$2.19 \times 10^{-1}$	$1.485 \times 10^{-1}$	$1.097 \times 10^{-1}$	11.0	$1.400 \times 10^{-6}$	$1.180 \times 10^{-7}$	$1.000 \times 10^{-8}$
.2	$1.584 \times 10^{-1}$	$9.26 \times 10^{-2}$	$5.83 \times 10^{-2}$	.2	$1.127 \times 10^{-6}$	$9.35 \times 10^{-8}$	$7.78 \times 10^{-9}$
.4	$1.162 \times 10^{-1}$	$5.99 \times 10^{-2}$	$3.29 \times 10^{-2}$	.4	$9.08 \times 10^{-7}$	$7.40 \times 10^{-8}$	$6.06 \times 10^{-9}$
.6	$8.63 \times 10^{-2}$	$3.99 \times 10^{-2}$	$1.949 \times 10^{-2}$	.6	$7.31 \times 10^{-7}$	$5.87 \times 10^{-8}$	$4.72 \times 10^{-9}$
.8	$6.47 \times 10^{-2}$	$2.71 \times 10^{-2}$	$1.195 \times 10^{-2}$	.8	$5.89 \times 10^{-7}$	$4.65 \times 10^{-8}$	$3.69 \times 10^{-9}$
2.0	$4.89 \times 10^{-2}$	$1.877 \times 10^{-2}$	$7.53 \times 10^{-3}$	12.0	$4.75 \times 10^{-7}$	$3.69 \times 10^{-8}$	$2.89 \times 10^{-9}$
.2	$3.72 \times 10^{-2}$	$1.317 \times 10^{-2}$	$4.86 \times 10^{-3}$	.2	$3.83 \times 10^{-7}$	$2.93 \times 10^{-8}$	$2.25 \times 10^{-9}$
.4	$2.84 \times 10^{-2}$	$9.36 \times 10^{-3}$	$3.20 \times 10^{-3}$	.4	$3.08 \times 10^{-7}$	$1:848 \times 10^{-8}$	$1.376 \times 10^{-9}$
.6	$2.19 \times 10^{-2}$	$6.72 \times 10^{-3}$	$2.14 \times 10^{-3}$	.6	$2.49 \times 10^{-7}$	$1.469 \times 10^{-8}$	$1.078 \times 10^{-9}$
.8	$1.686 \times 10^{-2}$	$4.86 \times 10^{-3}$	$1.447 \times 10^{-3}$	.8	$2.01 \times 10^{-7}$	$1.165 \times 10^{-8}$	$8.61 \times 10^{-10}$
3.0	$1.305 \times 10^{-2}$	$3.55 \times 10^{-3}$	$9.92 \times 10^{-4}$	13.0	$1.622 \times 10^{-7}$	$1.168 \times 10^{-8}$	$8.45 \times 10^{-9}$
.2	$1.013 \times 10^{-2}$	$2.60 \times 10^{-3}$	$6.88 \times 10^{-4}$	.2	$1.309 \times 10^{-7}$	$9.30 \times 10^{-9}$	$6.63 \times 10^{-10}$
.4	$7.89 \times 10^{-3}$	$1.925 \times 10^{-3}$	$4.81 \times 10^{-4}$	.4	$1.057 \times 10^{-7}$	$7.40 \times 10^{-9}$	$5.20 \times 10^{-10}$
.6	$6.16 \times 10^{-3}$	$1.430 \times 10^{-3}$	$3.39 \times 10^{-4}$	.6	$8.53 \times 10^{-8}$	$5.89 \times 10^{-3}$	$4.08 \times 10^{-10}$
.8	$4.82 \times 10^{-3}$	$1.067 \times 10^{-3}$	$2.41 \times 10^{-4}$	.8	$6.89 \times 10^{-8}$	$4.69 \times 10^{-3}$	$3.21 \times 10^{-10}$
4.0	$3.78 \times 10^{-3}$	$8.00 \times 10^{-4}$	$1.726 \times 10^{-4}$	14.0	$5.57 \times 10^{-8}$	$3.74 \times 10^{-9}$	$2.54 \times 10^{-10}$
.2	$2.97 \times 10^{-3}$	$6.02 \times 10^{-4}$	$1.242 \times 10^{-4}$	.2	$4.50 \times 10^{-8}$	$2.98 \times 10^{-9}$	$1.982 \times 10^{-10}$
.4	$2.34 \times 10^{-3}$	$4.54 \times 10^{-4}$	$8.99 \times 10^{-5}$	.4	$3.63 \times 10^{-8}$	$2.38 \times 10^{-9}$	$1.559 \times 10^{-10}$
.6	$1.841 \times 10^{-3}$	$3.44 \times 10^{-4}$	$6.54 \times 10^{-5}$	.6	$2.94 \times 10^{-8}$	$1.896 \times 10^{-9}$	$1.226 \times 10^{-10}$
.8	$1.453 \times 10^{-3}$	$2.62 \times 10^{-4}$	$4.78 \times 10^{-5}$	.8	$2.37 \times 10^{-8}$	1.513 × 10 ⁻⁹	$9.66 \times 10^{-11}$
5.0	$1.148 \times 10^{-3}$	$1.993 \times 10^{-4}$	$3.51 \times 10^{-5}$	15.0	$1.919 \times 10^{-8}$	$1.207 \times 10^{-9}$	$7.62 \times 10^{-11}$
.2	$9.09 \times 10^{-4}$	$1.523 \times 10^{-4}$	$2.59 \times 10^{-5}$	.2	$1.551 \times 10^{-8}$	$9.64 \times 10^{-10}$	$6.01 \times 10^{-11}$
.4	$7.20 \times 10^{-4}$	$1.166 \times 10^{-4}$	$1.914 \times 10^{-5}$	.4	$1.255 \times 10^{-8}$	$7.70 \times 10^{-10}$	$4.73 \times 10^{-11}$
.6	$5.71 \times 10^{-4}$	$8.95 \times 10^{-5}$	$1.421 \times 10^{-5}$	.6	$1.015 \times 10^{-8}$	$6.15 \times 10^{-10}$	$3.74 \times 10^{-11}$
.8	$4.53 \times 10^{-4}$	$6.88 \times 10^{-5}$	$1.058 \times 10^{-5}$	.8	$8.21 \times 10^{-9}$	$4.92 \times 10^{-10}$	$2.95 \times 10^{-11}$ $2.33 \times 10^{-11}$
6.0	$3.60 \times 10^{-4}$ $2.86 \times 10^{-4}$	$5.30 \times 10^{-5}$	$7.91 \times 10^{-6}$ $5.92 \times 10^{-6}$	16.0	$6.64 \times 10^{-9}$	$3.93 \times 10^{-10}$ $3.14 \times 10^{-10}$	$2.33 \times 10^{-11}$ $1.842 \times 10^{-11}$
.2	$2.86 \times 10^{-4}$ $2.28 \times 10^{-4}$	$4.10 \times 10^{-5}$ $3.17 \times 10^{-5}$	$5.92 \times 10^{-6}$ $4.45 \times 10^{-6}$	.2	$5.37 \times 10^{-9}$	$3.14 \times 10^{-10}$ $2.51 \times 10^{-10}$	$1.842 \times 10^{-11}$ $1.455 \times 10^{-11}$
.4	$1.816 \times 10^{-4}$	$3.17 \times 10^{-5}$ $2.45 \times 10^{-5}$	$3.35 \times 10^{-6}$	.4	$4.35 \times 10^{-9}$	$2.01 \times 10^{-10}$	$1.455 \times 10^{-11}$ $1.152 \times 10^{-11}$
.6 .8	$1.816 \times 10^{-4}$ $1.448 \times 10^{-4}$	$1.903 \times 10^{-5}$	$2.53 \times 10^{-6}$	.6	$3.52 \times 10^{-9}$ $2.85 \times 10^{-9}$	$1.609 \times 10^{-10}$	$9.11 \times 10^{-12}$
7.0	$1.155 \times 10^{-4}$	$1.479 \times 10^{-5}$	$1.911 \times 10^{-6}$	17.0	$2.85 \times 10^{-9}$ $2.31 \times 10^{-9}$	$1.288 \times 10^{-10}$	$7.21 \times 10^{-12}$
.2	$9.22 \times 10^{-5}$	$1.479 \times 10^{-5}$ $1.150 \times 10^{-5}$	$1.449 \times 10^{-6}$	17.0	$1.867 \times 10^{-9}$	$1.032 \times 10^{-10}$	$5.70 \times 10^{-12}$
.4	$7.36 \times 10^{-5}$	$8.96 \times 10^{-6}$	$1.100 \times 10^{-6}$	.2	$1.512 \times 10^{-9}$	$8.26 \times 10^{-11}$	$4.52 \times 10^{-12}$
.6	$5.89 \times 10^{-5}$	$6.99 \times 10^{-6}$	$8.37 \times 10^{-7}$	.6	$1.312 \times 10^{-9}$ $1.225 \times 10^{-9}$	$6.62 \times 10^{-11}$	$3.58 \times 10^{-12}$
.8	$4.71 \times 10^{-5}$	$5.46 \times 10^{-6}$	$6.38 \times 10^{-7}$	.8	$9.92 \times 10^{-10}$	$5.30 \times 10^{-11}$	$2.84 \times 10^{-12}$
8.0	$3.77\times10^{-5}$	$4.27 \times 10^{-6}$	$4.87 \times 10^{-7}$	18.0	$8.04 \times 10^{-10}$	$4.25 \times 10^{-11}$	$2.25 \times 10^{-12}$
.2	$3.02 \times 10^{-5}$	$3.34 \times 10^{-6}$	$3.72 \times 10^{-7}$	.2	$6.51\times10^{-10}$	$3.41 \times 10^{-11}$	$1.786 \times 10^{-12}$
.4	$2.42 \times 10^{-5}$	$2.62 \times 10^{-6}$	$2.86 \times 10^{-7}$	.4	$5.28 \times 10^{-10}$	$2.73 \times 10^{-11}$	$1.417 \times 10^{-12}$
.6	$1.936 \times 10^{-5}$	$2.05 \times 10^{-6}$	$2.19 \times 10^{-7}$	.6	$4.27 \times 10^{-10}$	$2.19 \times 10^{-11}$	$1.124 \times 10^{-12}$
.8	$1.552 \times 10^{-5}$	$1.610 \times 10^{-6}$	$1.683 \times 10^{-7}$	.8	$3.46 \times 10^{-10}$	$1.758 \times 10^{-11}$	$8.93 \times 10^{-13}$
9.0	$1.245 \times 10^{-5}$	$1.265 \times 10^{-6}$	$1.294 \times 10^{-7}$	19.0	$2.81 \times 10^{-10}$	$1.41 \times 10^{-11}$	$7.09 \times 10^{-13}$
.2	$9.99 \times 10^{-6}$	$9.95 \times 10^{-7}$	$9.96 \times 10^{-8}$	.2	$2.28 \times 10^{-10}$	$1.132 \times 10^{-11}$	$5.63 \times 10^{-13}$
.4	$8.02 \times 10^{-6}$	$7.82 \times 10^{-7}$	$7.69 \times 10^{-8}$	.4	$1.845 \times 10^{-10}$	$9.08 \times 10^{-12}$	$4.48 \times 10^{-13}$
.6	$6.44 \times 10^{-6}$	$6.16 \times 10^{-7}$	$5.94 \times 10^{-8}$	.6	$1.496 \times 10^{-10}$	$7.29 \times 10^{-12}$	$3.56 \times 10^{-13}$
.8	$5.17 \times 10^{-6}$	$4.85 \times 10^{-7}$	$4.60 \times 10^{-8}$	.8	$1.213 \times 10^{-10}$	$5.86 \times 10^{-12}$	$2.83 \times 10^{-13}$
10.0	$4.16 \times 10^{-6}$	$3.83 \times 10^{-7}$	$3.55 \times 10^{-8}$	20.0	$9.84 \times 10^{-11}$	$4.70 \times 10^{-12}$	$2.25 \times 10^{-13}$
.2	$3.34 \times 10^{-6}$	$3.02 \times 10^{-7}$	$2.75 \times 10^{-8}$				
.4	$2.69 \times 10^{-6}$	$2.39 \times 10^{-7}$	$2.13 \times 10^{-8}$				
.6	$2.16 \times 10^{-6}$	$1.887 \times 10^{-7}$	$1.654 \times 10^{-8}$				
.8	$1.740 \times 10^{-6}$	$1.492 \times 10^{-7}$	$1.286 \times 10^{-8}$				

Table 2.5.2 — Unshielded Infinite-plane Surface Sources

Source	Detector	Intensity
Isotropic	Non-directional	Infinite
	Cosine	<b>½</b>
Cosine	Non-directional	1/2
	Cosine	1/4

Table 2.5.3 — Unshielded Volume-distributed Plane-limited Source

Source	<b>D</b> etecto <b>r</b>	Buildup $B(\mu,R)$	<b>In</b> tensity
Volume	Non-directional	1	$1/(2\mu_1)$
	Cosine	1	$1/(4\mu_1)$

Table 2.5.4 — Infinite Slab Shield of Thickness z and Attenuation Coefficient  $\mu$ : Infinite Surface or Volume Source

			Intensity	
Source	Detector	Buildup Β(μ,R)	Exact	Approximate for μz >> 1
Isotropic surface, 1/(sec)(cm²)	Non-directional	Unitary	$\frac{1}{2} \cdot \mathbf{E}_1(\mu \mathbf{z})$	$\frac{1}{2} e^{-\mu z}$
1/ (BCC/(CIII /		Linear	$\frac{1}{2} e^{-\mu z}$	$\frac{1}{2}e^{-\mu z}$
	Cosine	Unitary	$\frac{1}{2} \mu z E_2(\mu z)$	$\frac{1}{2}\frac{e^{-\mu z}}{\mu z}$
		Linear	$\frac{1}{2} \mu z E_1(\mu z)$	$\frac{1}{2} e^{-\mu z}$
Cosine surface, cosθ/4π/(sec)(cm²)(sterad)	Non-directional	Unitary	$\frac{1}{2} \mu z E_2(\mu z)$	$\frac{1}{2}\frac{e^{-\mu z}}{\mu z}$
		Linear	$\frac{1}{2}\mu z E_1(\mu z)$	$\frac{1}{2} e^{-\mu z}$
	Cosine	Unitary	$\frac{1}{2} (\mu z)^2 E_3(\mu z)$	$\frac{1}{2} \frac{e^{-\mu z}}{\mu z}$
		Linear	$\frac{1}{2} (\mu z)^2 E_2(\mu z)$	$\frac{1}{2} e^{-\mu z}$
Volume, attenuation coefficient in source = $\mu_1$	Non-directional	Unitary	$\frac{1}{2\mu_1} \; \mu z \; E_2(\mu z)$	$\frac{1}{2\mu_1}\frac{e^{-\mu z}}{\mu z}$
		Linear	$\frac{1}{2\mu_1} e^{-\mu z}$	$\frac{1}{2\mu_1}$ e- $\mu$ z
	Cosine	Unitary	$\frac{1}{2\mu_1} (\mu z)^2 E_3(\mu z)$	$\frac{1}{2\mu_1}\frac{\mathrm{e}^{-\mu z}}{\mu z}$
		Linear	$\frac{1}{2\mu_1} \left[ e^{-\mu z} - (\mu z)^2 E_3(\mu z) \right]$	$\frac{1}{2\mu_i} e^{-\mu z}$

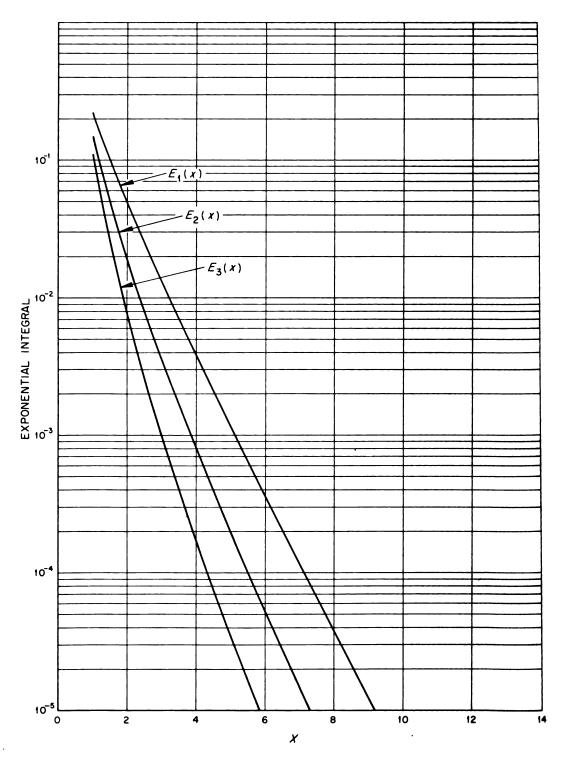


Fig. 2.5.6 — The Exponential Integral Functions  $E_1(x)$ ,  $E_2(x)$ , and  $E_3(x)$ , where  $E_n(x) = \int_x^\infty \frac{e^{-p}}{p^n} \, dp.$ 

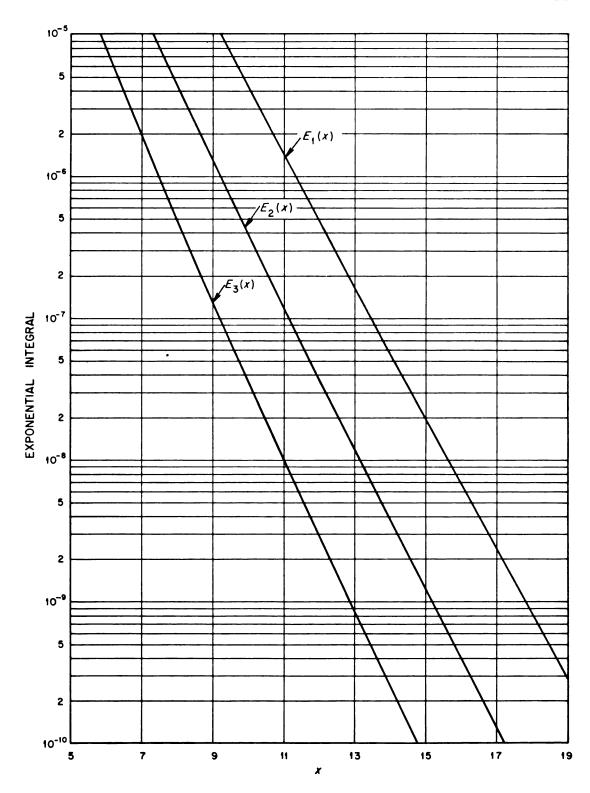


Fig. 2.5.7 — The Exponential Integral Functions  $E_1(x)$ ,  $E_2(x)$ , and  $E_3(x)$ , where  $E_n(x) = \int_x^\infty \frac{e^{-p}}{p^n} dp.$ 

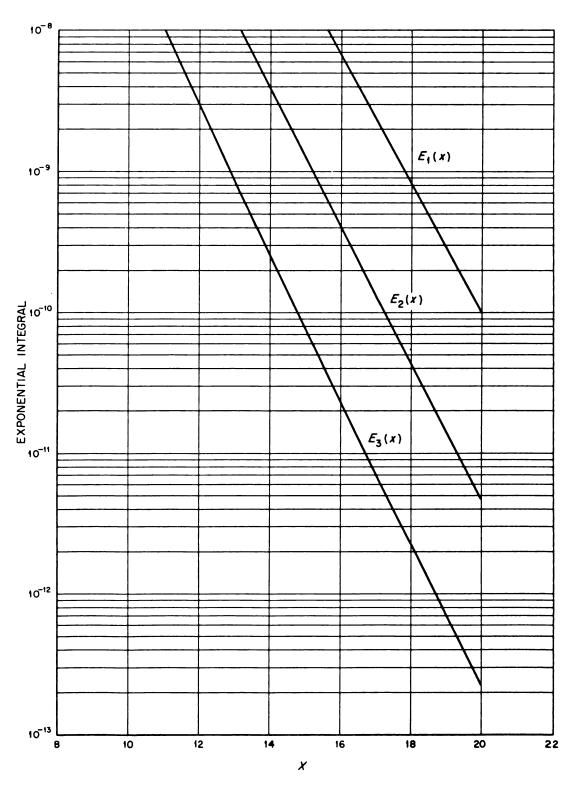


Fig. 2.5.8—The Exponential Integral Functions  $E_1(x)$ ,  $E_2(x)$ , and  $E_3(x)$ , where  $E_n(x) = \int_x^\infty \frac{e^{-p}}{p^n} \, dp.$ 

## REACTOR LEAKAGE

Often it is possible to express the distribution of source strength (usually proportional to reactor power) in the region near its surface by a simple linear equation:

$$\alpha(\mathbf{z}_1) = \alpha_0 + \alpha_1 \mathbf{z}_1 \tag{33}$$

where  $z_1$  is the distance into the core from the surface, and  $\alpha_0$  and  $\alpha_1$  are constants. In this case, the equivalent isotropic surface source (in the sense of the previous section) as recorded by a nondirectional detector (milligoat) is:

$$\sigma = \frac{\alpha_0}{\mu_1} + \frac{\alpha_1}{\mu_1} \tag{34}$$

where  $\mu_1$  is the core attenuation coefficient.

#### REFERENCES

- 1. E. P. Blizard, "Transformation from Disc to Point Source Geometry," ORNL, C. F. 52-3-219, Mar. 27, 1952.
- 2. E. P. Blizard, Part I, Oak Ridge National Laboratory, C. F. 51-10-70, p 54, 72 pp, Jan. 30, 1952 (classified).
- 3. T. A. Welton and E. P. Blizard, Reactor Sci. Tech. 2, No. 2, Aug. 1952 (classified).
- 4. H. Goldstein, Phys. Rev., in press.
- 5. Heitler "Quantum Theory of Radiation," Oxford press.
- 6. H. Castle, H. Ibser, G. Sacher, and A. M. Weinberg, CP-644, May 4, 1943 (classified).
- F. H. Murray, Fast Effects, Self-Absorption, Fluctuation of Ion Chamber Readings, and the Statistical Distribution of Chord Lengths in Finite Bodies, CP-G-2922, April 6, 1945.
- 8. S. Kushneriuk, Atomic Energy Project (Canada), 7 pp, May 6, 1947 (classified).
- 9. Chap. V, Sec. F, in Project Handbook, ed. by R. S. Mulliken, P. Morrison, et al, CL-697, Vol. II (classified).
- Appendix 8 in Materials Testing Reactor Project Handbook, ed. by J. H. Buck and C. F. Levse, Argonne National Laboratory and Oak Ridge National Laboratory, ORNL-963, 584 pp. May 7, 1951 (classified).
- 11. C. W. J. Wende, E. I. duPont deNemours and Company, Inc., M-1324 (N-609, TNX-7) 66 pp. Jan. 11, 1944 (classified).

#### CHAPTER 2.6

# **Ducts Through Shields**

#### A. Simon

The principal experimental investigations of ducts up to this time have been concerned with the effects of <u>air</u> ducts and voids on gamma-ray and neutron transmission in water. Many experiments on the attenuation of fast neutrons by long thin air ducts in water* can be understood on the basis of a phenomenological theory. This theory is presented below and is followed by a brief summary of the effect of internal voids on neutron attenuations. The effect of ducts and voids on the attenuation of gamma rays is considered in a latter part of this chapter.

## ATTENUATION OF NEUTRONS BY AIR DUCTS IN SHIELDS (THEORY)

The attenuation of neutrons by a long, thin, circular duct can be calculated by an albedo approach. It is assumed that the walls of the duct reradiate neutrons with an intensity proportional to the flux incident upon the wall. The constant of proportionality is the albedo, and it is assumed that the reradiation is partly isotropic and partly cosine distribution about the normal to the wall. If the reradiated flux into a unit solid angle  $d\Omega$  is written:

$$\frac{d\mathbf{F}}{d\Omega} = \frac{\mathbf{A} + 2\mathbf{B} \cos \theta}{2\pi} \alpha' \mathbf{F}_{inc}$$

where:

 $F_{inc}$  = flux incident on wall  $\alpha'$  = albedo of wall

and since by conservation of neutrons there follows:

$$A + B = 1$$

it can be shown¹ that the total flux at the end of a long, thin duct of length l and radius  $\delta$  is given by:

$$\mathbf{F} = \frac{\mathbf{N}_0}{2\pi l^2} \left( 1 + \frac{\mathbf{A} \alpha'}{1 - \alpha'} + \frac{4\mathbf{B}\delta\alpha'}{\mathbf{I}(1 - \alpha')} \right) \tag{2}$$

^{*}These experiments have not yet been published in a single report; most, however, have been re-Ported in various ORNL and ANP (classified) quarterly reports over the period from 1949 to 1952. ¹References appear at end of chapter.

CHAP. 2.6 RADIATION SHIELDING

Here,  $N_0$  is the total (isotropic) source strength at the mouth of the duct. The first term represents the uncollided (non wall-scattered) flux.

The fast-neutron albedos for water and concrete have been measured at the Bulk Shielding Facility at ORNL.² It was found that the albedos for both were of the order of 0.1. This result, coupled with the fact that A and B are less than or equal to unity, allows one to neglect all but the first term to a reasonable approximation. Hence, the flux at the mouth of a straight duct is caused by just the uncollided neutrons to within a few percent:

$$\mathbf{F} = \frac{\mathbf{N_0}}{2\pi^{12}} \tag{3}$$

An interesting by-product of this result is the prediction that one should be able to collimate a source of fast neutrons without greatly distorting the spectrum.

The effect of a single bend in a duct can be calculated by making a simple assumption. The flux entering the region of the bend, as shown in the previous paragraph, is just the uncollided flux arriving from the source. This dose of neutrons is completely absorbed in the walls of the bend, and as a result, a reradiated flux leaves the walls with a source strength proportional to the albedo of the medium. The exact effect of the complicated scatterings at the corner is unknown; however, it will be assumed that the reradiated flux is emitted uniformly from a region of area  $A_t$  in the vicinity of the bend and with an angular distribution given by:

$$\frac{\mathrm{d}\mathbf{F}}{\mathrm{d}\Omega} = \frac{\alpha'\mathbf{D}}{\mathbf{A}_{+}} \frac{\mathbf{A} + 2\mathbf{B} \, \cos\theta}{2\pi} \tag{4}$$

where: D = total uncollided neutron dose entering the region of the bend  $\alpha' = albedo$  of the walls

By conservation of neutrons:

$$A + B = 1$$

On the basis of this assumption, the total dose at the end of a duct consisting of two long, thin, straight sections of length  $l_1$  and  $l_2$  (both of radius  $\delta$ ) joined at an angle  $\theta$  can be shown to be:

$$\mathbf{F} = \mathbf{N_0} \left( \frac{\delta^2}{2l_1^2} \right) \left( \frac{\alpha \delta^2}{2l_2^2 \sin \theta} \right) (\mathbf{A} + 2\mathbf{B} \sin \theta) \tag{5}$$

Here:

 $N_0$  = total (isotropic) source strength at the mouth of the duct  $\alpha$  = "effective albedo," a constant which is proportional to the actual albedo of the walls

The factor  $1/\sin\theta$  arises from the fact that the region of wall at the bend which is visible from the end of the duct is approximately proportional to this quantity. Figure 2.6.1 illustrates this point.

Equation (5) may be generalized to cover the broad case of n+1 straight sections of length  $l_i$  ( $i=1,2,\ldots,n+1$ ) joined at angles given by  $\theta_{i,i+1}$  where the subscripts denote the angle between the appropriate straight sections. The result is:



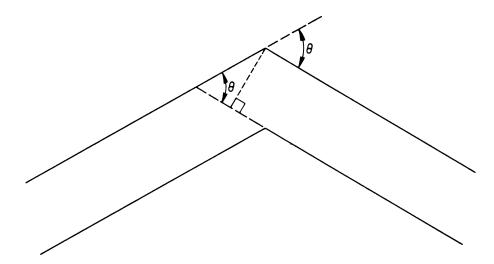


Fig. 2.6.1 — Dependence of Visible Wall Region at a Bend on the Angle of Bend. Submitted by Oak Ridge National Laboratory, Nov. 7, 1952.

$$D = N_0 \left( \frac{\delta^2}{2l_1^2} \right) \left[ \frac{\alpha \delta^2 (A + 2B \sin \theta_{1,2})}{2l_2^2 \sin \theta_{1,2}} \right] \cdot \cdot \cdot \cdot \left[ \frac{\alpha \delta^2 (A + 2B \sin \theta_{n, n+1})}{2l_{n+1}^2 \sin \theta_{n, n+1}} \right]$$
(6)

In the special case of equal lengths of straight sections with equal bends, this becomes:

$$D = N_0 \left(\frac{\delta^2}{2l^2}\right) \left(\frac{\alpha \delta^2}{2l^2 \sin \theta}\right)^n (A + 2B \sin \theta)^n$$
 (7)

or, since A + B = 1:

$$\mathbf{D} = \mathbf{N_0} \left( \frac{\delta^2}{2l^2} \right) \left( \frac{\alpha \delta^2}{2l^2 \sin \theta} \right)^{\mathbf{n}} \left[ 1 - \mathbf{B} \left( 1 - 2 \sin \theta \right) \right]^{\mathbf{n}} \tag{8}$$

It should be noted that Eq. (8) is not valid for angles that are so small that neutrons can go directly from one mouth of the duct to the other. In addition, the formula breaks down at angles small enough so that a large section of the wall of the bend ( $>A_t$ ) can be seen from the end of the next leg. In this region of  $\theta$ , the predicted dose should be an overestimate of the measured effect.

The constant  $\alpha$  and B in Eq. (8) are to be determined from experiment. Their values depend on the nature of the source spectrum used as well as the type of detector. The present experiments at the Lid Tank and Thermal Column at ORNL use a fission source and detect the neutrons by means of a BF₃ counter positioned at a water-equivalent of 10,20 or 30 cm behind the mouth of the duct. These results can be fitted by taking B  $\cong$  0 (i.e., pure isotropic reradiation by the walls of the duct). The value of  $\alpha$  depends on the counter position and is listed in Table 2.6.1.

The large values of  $\alpha$  that are needed are undoubtedly the result of using a BF₃ detector. Such a detector heavily weights the contribution of those neutrons which can be thermalized in 10, 20, or 30 cm of water. On the other hand, the measured albedos of water and concrete² were obtained by use of a dosimeter. It is quite probable that the wall albedos

18 M. 18 M. 12:23 12:23

1:5

132

. . .

jeur.

:::E

Ľ.

ا د قائل

Table 2.6.1 — "Effective Albedo" Determined by BF₃ Measurements

Water-equivalent distance	
between counter and duct, cm	α
10	2.4
20	1.0
30	0.56

for lower-energy neutrons are considerably higher than those for the fast flux. The decrease in the value of  $\alpha$  as the water-equivalent distance increases is in line with this picture.

It is to be expected that future experiments on duct attenuation using a dosimeter as a detector will give lower values of  $\alpha$ .

#### INTERNAL VOIDS

A simplified analysis of the effect of internal voids in shields on neutron transmission has been given by Tonks.³ A method of estimating the effect of areas of weaker shielding is developed which is applicable to voids of many shapes. The result is given in terms of the excess attenuation over that which would be attained with a uniform shield having the minimum thickness found in the neighborhood of the void. This "minimal ray" technique should not be used if streaming through ducts exists. However, if the duct has been made sufficiently tortuous so that direct streaming is negligible compared to the general void effect (sometimes called "reduced density" effect), then this technique may prove to be of value.

The design of patches to compensate for internal voids has been considered by Bourieius.⁴

A diffusion theoretical treatment of the propagation of neutrons in an empty duct has been given by Whitcombe⁵ and later by Roe.⁶ It is not clear to what extent these treatments are applicable to fast neutrons.

# ATTENUATION OF GAMMA RAYS BY AIR DUCTS AND VOIDS

The albedos for the reflection of Co⁶⁰ gamma rays (~1.3 mev) by concrete have been measured at ORNL Bulk Shielding Facility.² By using a 50-cc standard 10¹² ion chamber, the albedo was found to be 0.04. As a result, it may be expected that the neutron attenuation theory is applicable to gamma rays insofar as the effect of a long, thin, straight duct is concerned; that is, the attenuation should be geometrical. The effect of a bend on gamma attenuation is likely to be quite different from that for neutrons.

Large-scale measurements on the effect of voids on gamma-ray attenuation in water have been performed at Brookhaven. The experiments have been interpreted by Kouts on the basis of a two-group perturbation treatment using the integral form of the transport theory.

## REFERENCES

- 1. A. Simon and C. E. Clifford, ORNL-1217, Nov. 28, 1952, 24 pp (classified).
- 2. H. E. Hungerford, ORNL-CF-52-4-99, April 16, 1952, 21 pp (classified).
- 3. L. Tonks, KAPL-107, Jan. 17, 1949, 12 pp (classified).
- 4. W. G. Bourieius, NEPA-1536, Aug. 24, 1950, 15 pp (classified).
- 5. D. W. Whitcombe, A Diffusion Solution for the Cylindrical Ducting Problem of Infinite Geometry, Oak Ridge Nat. Lab., ORNL-668, April 19, 1950, 14 pp.
- G. M. Roe, The Penetration of Neutrons Through an Empty Cylindrical Duct in a Shield, Knolls Atomic Power Lab., KAPL-712, Mar. 29, 1952, 20 pp.
- 7. W. W. Pratt and H. J. Kouts, BNL Log No. C-6456, Aug. 25, 1952, 78 pp (classified).
- 8. H. J. Kouts, BNL Log No. C-6459, Sept. 15, 1952, 19 pp (classified).



### CHAPTER 2.7

# Heat Generation in Shields

F. H. Murray

#### **GAMMA SOURCES**

The primary gamma sources (see "Sources of Radiation," Chapter 2.1) in the reactor core have a spatial density proportional to the thermal-neutron density except for modifications resulting from motion of the fuel which changes the position of fission products that emit gammas. For calculation purposes, the primary sources of fixed fuels are often assumed to be uniformly distributed throughout the core. The calculations made in the design of the reactor may furnish more detailed information concerning source distributions.

For uniform source distribution, the number of fissions per second per cubic centimeter

 $A = 3 \times 10^{13} P/V$ 

Where:

P = power, kw

V = volume, cc

assuming  $3 \times 10^{10}$  fissions per joule.

If  $\Gamma(E)$  dE is the number of photons per fission of energy E to E + dE (E measured in millions of electron volts), then A  $\Gamma(E)$  dE is the corresponding source-density in the core. Owing to the uncertainty concerning the energy distribution for very-short-period gamma emitters in the fission products,  $\Gamma(E)$  is less well-known than is the total gamma energy released per fission.

Secondary sources in the core or reflector may be comprised of capture gammas or inelastic scattering gammas, and the densities of these sources may be estimated when the neutron flux pattern in the core is known. Since part of the neutron flux results from  $(\gamma, n)$  processes, especially in Be or D, its calculation may require successive approximations in which the initial fluxes are the primary fluxes.

#### GAMMA-RAY ABSORPTION

# BUILD-UP FACTOR FOR A HOMOGENEOUS MEDIUM

The build-up factor for energy absorption of gammas may be approximated by a method* **proposed** by H. Goldstein, which proceeds as follows:

^{*} For other treatments, cf. refs. (2), (3), (4), and (5).

¹ References appear at end of chapter.

Let  $I(r, E, \overrightarrow{\Omega})$  be the energy flux at a distance r of energy E and a direction  $\overrightarrow{\Omega}$  from a point source, and let:

$$I_0(r,E) = \int_{4\pi} I(r,E,\overrightarrow{\Omega}) d\Omega$$

be the total flux in all directions. The total absorption cross section (see "Gamma Attenuation," Chapter 2.3) is very nearly:

$$\mu_{En} = \mu_{pair} + \mu_{photo} + \int \frac{d\sigma}{d\Omega} \left( \frac{E \ electron}{E} \right) d\Omega$$

The total energy absorbed per unit volume at r, from a source of Q photons of energy  $E_0$  per second, is:

$$\mathbf{W}(\mathbf{r},\mathbf{E_0}) = \int_0^{\mathbf{E_0}} \mu_{\mathbf{E}n} \, \mathbf{I_0} \, \, \mathbf{dE}$$

The uncollided flux at r is:

$$I_0^0(\mathbf{r}, \mathbf{E}_0) = \frac{\mathbf{Q} \mathbf{E}_0 e^{-\mu(\mathbf{E}_0)\mathbf{r}}}{4\pi \mathbf{r}^2}$$

where  $\mu(E_0)$  is the narrow-beam absorption coefficient for energy  $E_0$ , and the build-up factor, B, which is a function of the initial energy and the distance, is given by:

$$\mathbf{B}_{En}(\mu_0 \mathbf{r}, \mathbf{E}_0) = \frac{\int_0^{E_0} \mu_{En} \mathbf{I}_0(\mathbf{r}, \mathbf{E}) \ d\mathbf{E}}{\mu_{En}(\mathbf{E}_0) \mathbf{I}_0^0(\mathbf{r}, \mathbf{E}_0)}$$

The energy absorbed at r is then:

$$\mathbf{w}(\mathbf{r}, \mathbf{E_0}) = \mathbf{B_{En}} (\mu_0 \mathbf{r}, \mathbf{E_0}) \mu_{En}(\mathbf{E_0}) \mathbf{I_0^0}(\mathbf{r}, \mathbf{E_0})$$

We must have from the conservation of energy:

$$\int_{\text{All space}} \mathbf{w}(\mathbf{r}, \mathbf{E_0}) \ d\mathbf{V} = \mathbf{Q}\mathbf{E_0}$$

hence:

$$\int_0^{\infty} B_{En}(x, E_0) e^{-x} dx = \frac{\mu_0}{\mu_{En}(E_0)}$$

For some problems, the build-up factor, B, may be represented by a linear function:

$$1 + k\mu_0 r$$

from which:

$$k = \frac{\mu_0}{\mu_{E_D}(E_0)} - 1$$

#### **HEATING OF A REGION**

If the build-up factor, B, is known, as from the method of the previous paragraph, then it is possible to calculate the total heat absorbed in a region V with a uniform source throughout by evaluation of the following double integral (see Fig. 2.7.1):

$$W_V = \int_V dV_1 \int_V w(r_{12}) dV_2$$

or:

$$\mathbf{W_{V}} = \int_{\mathbf{A}} \mathbf{dA_{1}cos}\nu_{1} \int_{\mathbf{A}} \frac{\mathbf{dA_{2}cos}\nu_{2}}{(\mathbf{r_{A_{1}A_{2}}})^{2}} \psi(\mathbf{r_{A_{1}A_{2}}})$$

where:

$$\psi(\mathbf{r}) = \int_0^{\mathbf{r}} (\mathbf{r} - \mathbf{y}) \mathbf{y^2} \mathbf{w}(\mathbf{y}) \ d\mathbf{y}$$

For two regions, one inside the other, such as might be encountered with a core and reflector, the total heat absorbed in core and reflector (if they can be assigned about the same absorption coefficients) is:

$$W_{core+refl.} = \int_{core} dV_1 \int_{core+refl.} w(r_{12}) dV_2$$

or (see Fig. 2.7.2):*

$$W_{core+refl.} = \int_{A_2} dA_2 cos\nu_2 \left[ \int_{A_1'} \frac{dA_1' cos\nu_1' \psi(r_{A_2A_1'})}{(r_{A_2A_1'})^2} + \int_{A_1''} \frac{dA_1'' cos\nu_1'' \psi(r_{A_2A_1''})}{(r_{A_2A_1''})^2} \right]$$

Thus, the energy transmitted to the shield is just the difference between the total emitted and  $W_{core+refl}$ . For spherical core and reflector with radii  $R_2$  and  $R_1$  and  $R_2 > R_1$ :

$$\mathbf{W} = \int_{\mathbf{R_2} - \mathbf{R_1}}^{\mathbf{R_2} + \mathbf{R_1}} \phi(\mathbf{r}) \psi(\mathbf{r}) d\mathbf{r}$$

where:

$$\phi(l)dl = \int\!\!\int_{1 \leq r_{A_1A_2} \leq l + dl} \frac{dA_1 cos\nu_1 dA_2 cos\nu_2}{(r_{A_1A_2})^2}$$

or:

$$\phi(1)d1 = \frac{2\pi^2}{1^3} \left[1^4 - (R_2^2 - R_1^2)^2\right]d1$$

^{*} The direction cosines  $\nu_1$  and  $\nu_2$  are those made by the line from dA₂ to dA, with the exterior normal at dA₁ and the interior normal at dA₂, respectively. At dA₁, cos  $\nu_1^{\nu}$  is negative; cos  $\nu_2$  is positive or zero; the curve on which the line from dA₂ is tangent to the core separates the areas A₁, A₁.



CHAP. 2.7 RADIATION SHIELDING

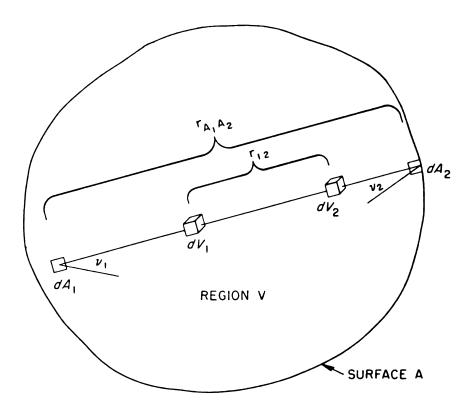


Fig. 2.7.1 — Illustration of Integration for Heating in a Region in Which Sources Are Uniformly Distributed. Submitted by Oak Ridge National Laboratory, April 1, 1953.

## SPECIAL CASES

## LOS ALAMOS REACTORS

Los Alamos measurements on the photon flux spectrum from the core of the fast reactor and the flux from a U²³⁶ slug in the glory hole of the water boiler were found to be of almost identical exponential type as functions of the energy E. The number of photons per thousand electron volts interval at 8 mev was less than the value at 0.5 mev by a factor of 10⁶ for each. The average energy was nearly 1 mev in each case. Prompt fission gammas and delayed gammas from fission products each contributed about 45 percent of the total energy of the gamma radiation; capture gammas from U²³⁶ contributed about 10 percent.

# BULK SHIELDING FACILITY REACTOR

The Bulk Shielding Facility Reactor at Oak Ridge National Laboratory includes about 3 kg  $U^{235}$ , is water moderated, and has aluminum structural members; the Al/H₂O volume ratio is about 0.7. The gamma fluxes in the surrounding pool of water at various distances from the reactor face as functions of energy are available in four Oak Ridge National Laboratory reports.  $^{7-10}$ 

#### OTHER REACTORS

Heat generation in several other reactors is described in Chapter 1.6.

Digitized by Google

D'I

٠,٠

107

***** 

المحر فدور

0: 1:

للنستة e 114.8 184.1

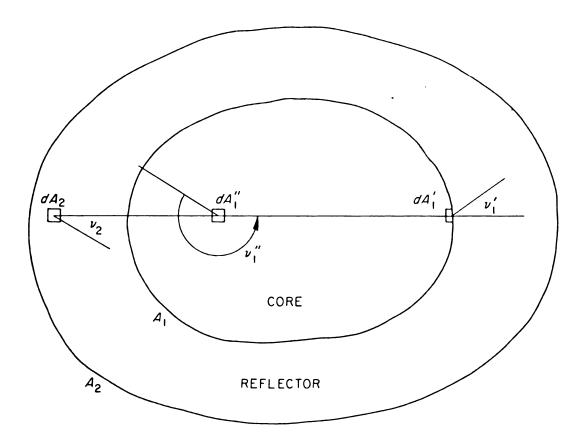


Fig. 2.7.2 — Illustration of Integration for Heating in Two Regions Owing to Sources in One Region. Submitted by Oak Ridge National Laboratory, April 1, 1953.

# **ENERGY ABSORPTION OF CAPTURE GAMMAS**

If the gamma mean-free-path is short as in heavy materials, the method of Enlund¹¹ may be used. An infinite plane source of neutrons emitting a current Io of slow neutrons into an infinite plane-limited slab produces a flux,  $\phi$ , in the material, with:

$$\phi = \frac{\mathbf{I_0}e^{-Kz}}{KD}$$

Where:

I = neutron current,  $-Dd\phi/dz$  at z = 0,  $cm^{-2}$   $sec^{-1}$   $K = \sqrt{3\Sigma_a \Sigma_t}$ ,  $cm^{-1}$ 

 $\Sigma_a$  = neutron absorption coefficient, cm⁻¹

 $\Sigma_t$  = neutron transport coefficient, cm⁻¹

D = diffusion coefficient

z = distance to point of neutron absorption, cm

Then:

$$\Sigma_a \phi(z) = \frac{\Sigma_a I_0 e^{-Kz}}{DK} = KI_0 e^{-Kz} = \text{number of neutrons absorbed at } z$$

n(E) = fraction of neutron captures which yield a gamma ray of energy E, mev

 $\mu_{En}(E)$  = energy absorption coefficient, cm⁻¹

 $\mu(E)$  = linear absorption coefficient, cm⁻¹

 $\alpha = \mathbf{K}/\mu$ 

b = distance to point of gamma energy absorption, cm

CASE I:  $K > \mu$ 

$$\Gamma(E) = n(E) \frac{EI_0}{2} \mu_{En}(E) F(\mu b, \alpha)$$

where:

$$\mathbf{F}(\mu \mathbf{b}, \alpha) = e^{-\alpha \mu \mathbf{b}} \left\{ e^{\alpha \mu \mathbf{b}} \left[ -\mathbf{E}\mathbf{i}(-\mu \mathbf{b}) \right] + \mathbf{E}\mathbf{i} \left[ \mu \mathbf{b}(\alpha - 1) \right] + \ln \frac{\alpha + 1}{\alpha - 1} \right\}$$

Then the heating in the material is:

$$H(E) = \frac{\Gamma(E)}{6.25 \times 10^{12}} \text{ watts/cm}^3$$

CASE II: 
$$K = \mu$$

$$\Gamma(E) = n(E) \frac{EI_0}{2} \mu_{En}(E) F(\mu b, 1)$$

where:

$$F(\mu b, 1) = e^{-\mu b} \{e^{\mu b} [-Ei(-\mu b)] + \ln \mu b + \ln 2\gamma\}, \ln \gamma = 0.5772$$

CASE III:  $K < \mu$ 

$$\Gamma(\mathbf{E}) = n(\mathbf{E}) \frac{\mathbf{EI_0}}{2} \mu_{\mathbf{E}n}(\mathbf{E}) \mathbf{F}(\mu \mathbf{b}, \alpha)$$

where:

$$\mathbf{F}(\mu\mathbf{b},\alpha) = \mathrm{e}^{-\alpha\mu\mathbf{b}} \left\{ \mathrm{e}^{\,\alpha\mu\mathbf{b}} \left[ -\mathrm{Ei}(-\mu\mathbf{b}) \right] + \mathrm{Ei} \left[ -\mu\mathbf{b}(1-\alpha) \right] + \ln\frac{1+\alpha}{1-\alpha} \right\}$$

Curves showing  $F(\mu b, \alpha)$  as functions of  $\mu b$  for various values of  $\alpha$  are given in Fig. 2.7.3.

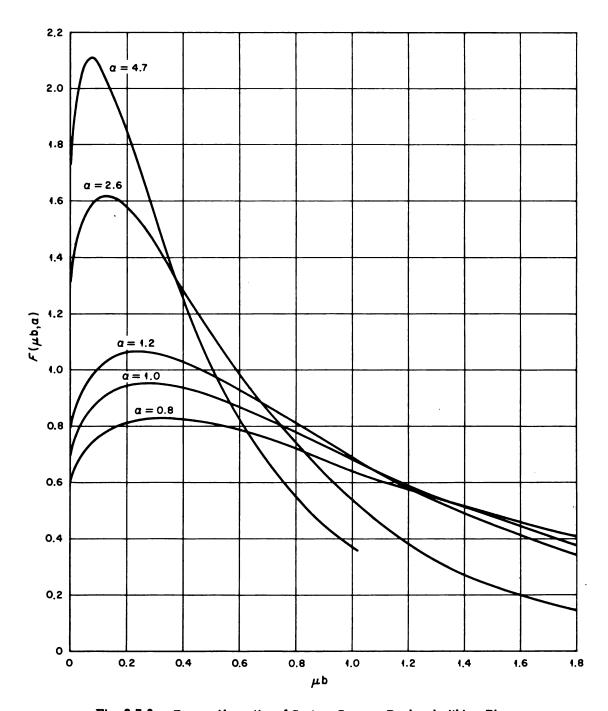


Fig. 2.7.3 — Energy Absorption of Capture Gammas Produced within a Planelimited Infinite Medium. Submitted by Oak Ridge National Laboratory, April 1, 1953.

#### REFERENCES

- 1. D. K. Holmes, ANP-58, Feb. 15, 1951, 38 pp (classified).
- 2. H. Hurwitz, J. B. Nims, and M. L. Storm, KAPL-753, July 14, 1952, 75 pp (classified).
- 3. M. L. Storm, H. Hurwitz, and G. M. Roe, KAPL-783, July 24, 1952, 92 pp (classified).
- 4. H. Hurwitz, J. B. Nims, and M. L. Storm, KAPL-800, Oct. 7, 1952, 65 pp (classified).
- 5. J. A. Rich and R. E. Slovacek, KAPL-866, Jan. 7, 1953 (classified).
- 6. J. W. Motz, Gamma-ray Spectra of the Los Alamos Reactors, Phys. Rev. 86, 1952, pp 753-754.
- 7. F. C. Maienschein, Oak Ridge Nat. Lab., CF-52-3-1, March 3, 1952, 7 pp (classified).
- 8. Ibid., CF-52-7-71, July 8, 1952, 16 pp (classified).
- 9. Ibid., CF-52-8-38, Aug. 8, 1952, 7 pp (classified).
- 10. F. C. Maienschein and T. A. Love, Oak Ridge Nat. Lab., CF-52-11-124, Nov. 17, 1952, 6 pp (classified).
- 11. H. L. F. Enlund, Energy Absorption of Capture Gammas, Oak Ridge Nat. Lab., CF-52-6-99 Supplement, Oct. 16, 1952, 4 pp.

#### **CHAPTER 2.8**

# Shield Optimization with Respect to Weight

#### E. P. Blizard

#### GENERAL THEORY

The optimization of a shield with respect to weight is here assumed to be limited simply to choosing that configuration of available materials which reduces the radiation to a tolerable level and has minimum weight. Broader considerations, such as a reduction in reactor power for the purpose of reducing shield weight with a possible concomitant increase in performance, will not be considered.

The most general expression for shield weight is taken to be an integral of the density of the shield over the whole shield:

$$W = \int_{\text{shield}} \rho(x, y, z) dV$$
 (1)

where  $\rho(x,y,z)$  is the density, dV is a volume element, and x,y,z represent coordinates to specify location within the shield.

While Eq. (1) is the most general expression of the weight, the integration may often be carried out at once, leaving the weight W as a function of relatively few parameters which defined the integration limits in Eq. (1).

Another expression, analogous to Eq. (1), for the biological dose would be excessively complicated and involve unknown cross sections. It is possible, however, to write an expression for the variation in the dose which is caused by a variation in the configuration. The most general expression allows variation both within the shield and on its surface. Although all parameters which specify the configuration should be examined in an optimization, the method is demonstrated here for a variation of one function within the shield (e.g., volume fraction of lead in a lead-water region) and another on the surface (e.g., shield thickness):

$$\delta D = \int_{\text{shield volume}} D'_{\alpha}(x,y,z) \delta \alpha(x,y,z) dV + \int_{\text{shield surface}} D'_{t}(x,y,z) \delta t(x,y,z) dS$$
 (2)

where  $\alpha(x,y,z)$  is a point function describing the shield composition, for example, the volume fraction of heavy component; t(x,y,z) is a function describing the surfaces of the shield;  $\delta t$  (x,y,z), the variation in t(x,y,z), is taken to be normal to the shield surface at (x,y,z) and positive for increase of shield thickness; dV and dS are volume and surface elements, respectively, the latter being taken at the variable (usually outer) surface; and  $D_t'$  and  $D_{\alpha}'$  are functional derivatives defined in the subsequent paragraphs.

CHAP. 2.8 RADIATION SHIELDING

Consider a small element of shield volume  $\delta V(x,y,z)$  in which the value of  $\alpha(x,y,z)$  is changed by an amount  $\delta \alpha(x,y,z)$ . If this change causes a change in the dose, D, (at the position outside the shield occupied by personnel) by an amount  $\delta_{\alpha}D$ , then the functional derivative is defined* as:

$$D'_{\alpha} = \frac{\text{Lim}}{\delta V \delta \alpha} \xrightarrow{\delta} 0 \frac{\delta_{\alpha} D}{\delta V \delta \alpha} \tag{3}$$

 $D'_{\alpha}$  is thus a true observable of an experiment. Thus, if  $\alpha$  is the volume-fraction of lead in a spherically symmetrical lead-water shield, a measurement to determine  $D'_{\alpha}$  (r) would consist of inserting a spherical lead shell of thickness  $\tau = \delta V/4\pi r^2$  in the water at r, and observing the change in the dose rate, D. The total thickness is presumed fixed. Then, since  $\delta \alpha = 1$ :

$$D_{\alpha}'(\mathbf{r}) \cong \frac{\delta_{\alpha} D}{4\pi r^{2} \tau} \tag{4}$$

The quantity usually measured in this connection is the "replacement length," 1, which is much like a relaxation length, to describe the effect of replacing water with lead. Thus:

$$l(r) = -\frac{Lim}{\tau \to 0} \frac{\tau D}{\delta_{\alpha} D} \approx \frac{\tau D}{\delta_{\alpha} D}$$
 (5)

or:

$$D'_{\alpha}(r) = -\frac{D}{4\pi r^2 l(r)}$$
 (6)

That "l" is a function of r follows from the fact that in a reactor shield the lead would be subjected to a neutron flux which would produce capture and inelastic scattering gamma rays. Clearly, the closer to the core (the smaller the radius), the greater is this secondary production. The optimization procedure will be seen to balance this disadvantage against the savings in weight for a given lead thickness.

Next, if increasing the shield thickness by  $\delta t$  over a small surface element  $\delta S$  produces a change  $\delta_t D$  in the dose, then the definition follows that:

$$D_t' = \lim_{\delta S \delta t} \frac{\delta_t D}{\delta S \delta t}$$
(7)

Thus, if a spherical shell is added to the spherically symmetrical shield of the illustration, then:

$$D_{t}'(r) = \frac{1}{4\pi r_{0}^{2}} \left( \frac{\partial D}{\partial r} \right)_{r=r_{0}}$$
 (8)

$$=-\frac{D}{4\pi r_0^2 \lambda(\mathbf{r}_0)}\tag{9}$$

where  $\lambda(\mathbf{r_0})$  is the dose relaxation length for addition of shield material at  $\mathbf{r_0}$ , the outer radius.

^{*}Strictly,  $\int_{AV} \delta \alpha dV$  should be used instead of  $\delta V \delta \alpha$  in Eq. (3).

By standard methods,* the optimization is shown to require that for all points within the shield:

$$\frac{\partial \rho}{\partial \alpha} + \frac{\Lambda}{D_0} D_{\alpha}' = 0 \tag{10}$$

and for all points on the surface:

$$\rho + \frac{\Lambda}{D_0} D_1' = \tilde{0} \tag{11}$$

where  $\Lambda$  is a LaGrange multiplier and  $D_0$  is the specified tolerance dose.

#### SPHERICALLY-SYMMETRICAL TWO-COMPONENT SHIELD

For a shield which is spherically symmetrical and consists of two components, the conditions on l(r) and  $\lambda(r)$  which will prevail when the shield is optimized are, from Eqs. (10) and (11):

$$\frac{\partial \rho}{\partial \alpha} = \frac{\Lambda}{4\pi \, r^2 l(r)} \tag{12}$$

$$\rho(\mathbf{r_0}) = \frac{\Lambda}{4\pi \mathbf{r_0^2} \lambda(\mathbf{r_0})} \tag{13}$$

or, since  $\partial \rho/\partial \alpha = \rho_1 - \rho_2$ , the difference in densities of the two components:

$$\mathbf{r^2l} \ (\mathbf{r}) = \frac{\rho(\mathbf{r_0})\mathbf{r_0}\lambda(\mathbf{r_0})}{\rho_1 - \rho_2} = \text{constant} \tag{14}$$

It has been shown³ that this result is equivalent to that of Tonks and Hurwitz,⁴ which was derived with more specific assumptions regarding the actual attenuation functions.

Equation (14) gives the condition which will prevail when a two-component shield is optimized. Although this method gives only a criterion for recognizing an optimized shield, it is always possible to use the criteria of Eqs. (10) and (11) to indicate the direction in which to change a near-optimum shield to approach the optimum.

# PARAMETER OPTIMIZATION

In case the shield configuration can be expressed simply in terms of a finite number of parameters, integration of Eqs. (10) and (11) over the shield give the simple result:

$$\frac{\partial \mathbf{W}}{\partial \alpha} + \frac{\Lambda}{\mathbf{D}_0} \frac{\partial \mathbf{D}}{\partial \alpha} = 0 \tag{15}$$



^{*}Reference (1) gives the method in detail; ref. (2) gives the general method.

¹References appear at end of chapter.

CHAP. 2.8 RADIATION SHIELDING

$$\frac{\partial \mathbf{W}}{\partial \mathbf{t}} + \frac{\Lambda}{\mathbf{D_0}} \frac{\partial \mathbf{D}}{\partial \mathbf{T}} = \mathbf{0} \tag{16}$$

where  $\alpha$  is now simply a parameter, and these equations apply for all parameters. Essentially, they say that for any shield parameter,  $\alpha$ :

$$\left(\frac{\partial \mathbf{W}}{\partial \boldsymbol{\alpha}}\right) / \left(\frac{\partial \mathbf{D}}{\partial \boldsymbol{\alpha}}\right) = \mathbf{constant} \tag{15a}$$

and this is the basic criterion to use in simple optimizations.

Example—Consider a box shield about a box source, to be shielded from a person some distance off on one of the prime axes: Clearly, the radiation leaving the near face is more effective than that leaving the sides (which is assumed not negligible because of air scattering). Furthermore, the radiation leaving the sides is more important than that leaving the far (left) face. From Eq. (15), the criterion is that:

$$\frac{\partial \mathbf{W}}{\partial \boldsymbol{\alpha}} / \frac{\partial \mathbf{D}}{\partial \boldsymbol{\alpha}} = \frac{\partial \mathbf{W}}{\partial \boldsymbol{\beta}} / \frac{\partial \mathbf{D}}{\partial \boldsymbol{\beta}} = \frac{\partial \mathbf{W}}{\partial \boldsymbol{\gamma}} / \frac{\partial \mathbf{D}}{\partial \boldsymbol{\gamma}} = \mathbf{constant}$$
 (15a,b,c)

where  $\alpha$ ,  $\beta$ , and  $\gamma$  are the three parameters as shown in Fig. 2.8.1, and  $\partial D/\partial \alpha$  is the change in the dose at the sensitive location (human figure in the sketch) with a change in

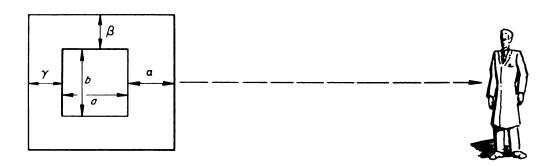


Fig. 2.8.1 — Box-shaped Shield. Submitted by Oak Ridge National Laboratory, Mar. 6, 1953.

the thickness parameter  $\alpha$ . In the simple case of exponential attenuation in the shield, with relaxation length  $\lambda$ , the derivatives would simply be:

$$\frac{\partial \mathbf{D}}{\partial \alpha} = -\frac{\mathbf{D_n}}{\lambda} \tag{17a}$$

$$\frac{\partial \mathbf{D}}{\partial \beta} = -\frac{\mathbf{D_S}}{\lambda} \tag{17b}$$

$$\frac{\partial \mathbf{D}}{\partial \gamma} = \frac{\mathbf{D} \, \mathbf{f}}{\lambda} \tag{17c}$$

where  $D_n$ ,  $D_s$ , and  $D_f$  are the dose contributions of radiation from the near, side, and far periphery of the shield, respectively.

Of course,  $\partial W/\partial \alpha$  is simply the shield density,  $\rho$ , multiplied by the near face area,  $(b + 2\beta)^2$ .

The equations which will be satisfied for an optimized shield are thus:

$$\frac{\rho(b+2\beta)^2}{D_n/\lambda} = \frac{4\rho(a+\alpha+\gamma)(b+2\beta)}{D_s/\lambda} = \frac{\rho(b+2\beta)^2}{D_f/\lambda}$$
(18)

The adjunct condition that the total dose be equal to some specified limit  $D_0$  is expressed by:

$$D_0 = D_n + D_s + D_f \tag{19}$$

## REFERENCES

- 1. E. P. Blizard, ORNL-1471, Secret.
- 2. Paul Lévy, Problems Concrets d'Analyse Fonctionelle, Gauthiers-Villars, Paris, 1951.
- 3. H. Goldstein and E. P. Blizard, Reactor Sci. Tech. 1, No. 2, Aug. 1951, 3 pp (classified).
- 4. L. Tonks and H. Hurwitz, Jr., KAPL-76, June 8, 1948, 23 pp (classified).
- 5. Deleted.
- 6. Deleted.

#### **CHAPTER 2.9**

# Shield Materials

H. E. Hungerford

#### SELECTION OF MATERIALS FOR SHIELDS

The selection of materials for shielding nuclear reactors depends upon such factors as the type of reactor, its designated power level, the physical and nuclear characteristics of the shield material under consideration, use and position of the material in the shield, and availability and cost of the material.

Shields for stationary reactors are usually made from inexpensive and easily available materials, and the shield thicknesses are governed primarily by radiation tolerances for personnel or by low background requirements for radiation experiments. Shields for mobile reactors must generally be small and light, and materials are therefore selected for special attenuation properties and placed at positions where these properties will be most effectively employed; such shields may necessarily contain uncommon and expensive materials. Reflectors, coolants, and structural materials must also be considered in shield designs.

#### TYPES OF SHIELD MATERIALS

# NEUTRON SHIELDS

The lightest neutron shields contain a high percentage of hydrogen. Ordinary water makes a cheap but effective hydrogenous shield. Many organic hydrogenous compounds and some metal hydrides make thinner snields than water does for the same amount of neutron attenuation but these materials may be heavier or more susceptible to radiation damage. Useful hydrogenous substances for shields include plastics, petroleum products, rubbers, hydrides, and wood.

Other light elements such as lithium and beryllium have high removal cross sections and therefore may be attractive as shield materials.

Good neutron-attenuation characteristics are exhibited by elements of high atomic density, such as iron, copper, tungsten and lead, but this advantage is offset by their high weight. Such substances are usually employed in a shield for other reasons and are present in conjunction with hydrogenous materials.

# **GAMMA SHIELDS**

Metals of high atomic number and high density make the most effective gamma shields, the most effective being uranium, thorium, lead, gold, and tungsten. Other fairly effective gamma-shielding metals in the medium-weight range include iron, copper, nickel, chromium, and their alloys.



CHAP. 2.9 RADIATION SHIELDING

# MATERIALS FOR SUPPRESSION OF CAPTURE GAMMA RAYS

Boron and lithium are often used within shields to suppress secondary gamma radiation arising from neutron capture by the shield material (see Table 2.1.6). Boron-containing substances include metallic boron, boron carbide, boron oxide, solutions of boron salts in water and other solvents, plastics and rubber impregnated with boron compounds, sprays and paints containing boron, and a large number of organic compounds containing boron. Lithium-bearing substances are metallic lithium, lithia, lithium hydride, and various vehicles, solvents, and other agents containing lithium compounds.

#### STRUCTURAL MATERIALS

Materials necessary for structure and support may or may not have good shielding characteristics but must be accounted for in the over-all shield design. These materials include metals, such as steel and aluminum, and non-metallic building materials, such as brick, rock, concrete, and wood.

#### MISCELLANEOUS MATERIALS

These materials include (1) moderators, such as beryllium and graphite, (2) coolants, such as air and other gases, liquid metals, water, and other fluids, and (3) component and auxiliary equipment, such as control mechanisms, pumps, heat exchangers, piping and ducting, and electronic equipment. The shielding effects of air voids must also be taken into consideration.

#### POSITION OF MATERIALS WITHIN A SHIELD

The performance of a shield depends to a large extent upon the location of its various components. Most construction materials, such as high-melting metals and alloys, concretes, and bricks, may be used with precaution in all parts of the shield. Shields constructed entirely from these materials are usually safe but also thick and bulky. Most organic substances cannot be used at all in high-flux regions of the inner (primary) shield because of radiation damage and deterioration. Likewise, many metals cannot be used in this region because of warpage, creep, fatigue, changes in crystalline structure, and similar damage resulting from the generation of high temperatures and other radiation effects. While most substances may be used in the outer (secondary) shield where less heat is generated and lower fluxes are encountered, it is important, especially in the design of light-weight shields, to employ the correct materials in their most efficient arrangement. Lamination (the use of layers of different materials) often achieves the most effective shields.

# PROPERTIES OF SHIELD MATERIALS

The following information is designed to provide physicists and engineers with a useful source of reference for the physical and nuclear properties of important shield materials. In general, only those materials not dealt with elsewhere in this Handbook are included here. Basic nuclear data are presented elsewhere in this volume, and materials of general interest in the field of reactor design are described in Volume 3. An attempt has been made in the presentation of the following tables to be clear, concise, and uniform throughout. The tables have all been carefully referenced to provide access to the sources of information.

#### NUCLEAR PROPERTIES

The nuclear properties presented in Tables 2.9.1 through 2.9.6 were selected on the basis of their usefulness to shield design. Included in these tables is information not only for complete materials, but also for compounds found in shield materials. Basic data on cross sections and the like are given elsewhere in this volume.



121.TE

1-353

g agrap, maiog kage da kagen

52:23 15: 325 14: 325

PORTE STATES STA

Control of the contro

elei Dici

Table 2.9.1 — Atomic Numbers, Atomic Weights, Densities, and Atomic Densities of the Elements

Element	Atomic number	Atomic weight	Density,* gm/cc	Atomic density† (N), atoms/cc × 10 ²²
H	1	1.008	$8.987 \times 10^{-6}$ (gas at STP)	0.00541
			0.0808 (solid at -252.7°C)	4.24
Li	3	6.940	0.53	4.60
Вe	4	9.02	1.8	12.0
В	5	10.82	2.5	13.9
С	6	12.01	3.51 (diamond)	17.6
			2.26 (graphite)	11.3
N	7	14.008	$1.25 \times 10^{-3}$ (gas at STP)	0.00537
			1.026 (solid at -196.8°C)	3.47
0	8	16.000	$1.429 \times 10^{-3}$ (gas at STP)	0.00538
			1.426 (solid at -183°C)	4.29
Na	11	22.997	0.97	2.54
Mg	12	24.32	1.74	4.31
Al	13	26.97	2.702	6.03
Si	14	28.06	2.4	5.1 <b>5</b>
P	15	30.98	1.82 (yellow)	3.54
			2.20 (red)	4.28
S	16	32.066	2.07 (rhombic)	3.89
			1.96 (monoclinic)	3.68
Cl	17	<b>35.457</b>	$3.24 \times 10^{-3}$ (gas at STP)	0.0055
			1.56 (solid at -33.6°C)	2.64
K	19	<b>39.096</b>	0.86	1.32
Ca	20	40.08	1.55	2.33
Ti	22	47.90	4.5	5.6 <b>4</b>
Cr	24	52.01	7.1	8.22
Mn	25	<b>54.9</b> 3	7.2	7.89
Fe	26	55.85	<b>7.86</b>	8.48
Co	27	<b>58.94</b>	8 <b>.9</b>	9.09
Ni	28	58.69	8.90	9.13
Cu	29	<b>63.54</b>	8.92	8. <b>46</b>
Zn	30	65.38	7.1 <del>4</del> 0	6.58
As	33	74.91	5.7	4.58
Zr	40	91.22	6.4	4.23
Ag	47	107.88	10.5	5.67
Cd	<b>4</b> 8	112.41	8.6	4.61
Sin	50	118.70	7.31 (white)	2.92
Ba	56	137.36	3.5	1.53
W	74	183.92	19.3	6.31
Au	79	197.2	19.3	5.89
Hg	80	200.61	13.546	4.07
Pb	82	207.21	11.34	3.30
Bi	83	209.00	9.8	2.82
Th	90	232.12	11.4	2.90
U	92	238.07	18.90	4.73

^{*}At 20°C, unless otherwise specified

[†] Normal state, unless otherwise specified; all values calculated

Table 2.9.2 — Calculated Mass Absorption Coefficients of Gamma Rays for the Elements

Atomic					ц	/ρ, cm²/gn	1	
number,	<b>71</b>	G	Atomic	<u> </u>				6 mey
Z	Element*	Symbol*	weight, A	0.5 mev	1 mev	2 mev	3 mev	o mev
1†	Hydrogen	н	1.008	0.173	0.126	0.0878	0.0693	0.0449
2	Helium	He	4.003	.0874	.0625	.0425	.0337	.0247
3	Lithium	Li	6.940	.0756	.0540	.0360	.0288	.0216
4†	Beryllium	Be	9.02	.0772	.0564	.0394	.0313	.0212
5	Boron	В	10.82	.0809	.0587	.0437	.0323	.0277
6†	Carbon	c	12.01	.0870	.0635	.0443	.0356	.0246
7†	Nitrogen	N	14.008	.0870	.0636	.0443	.0357	.0251 .0255
8†	Oxygen	0	16.0000	.0871	.0636	.0444	.0359	
9	Fluorine	F	19.0000	.0826	.0600	.0421	.0342	.0245
10	Neon	Ne	20.183	.0867	.0627	.0443	.0357	.0260
11†	Sodium	Na	22.997	.0835	.0608	.0427	.0348	.0255
12	Magnesium	Mg	24.32	.0863	.0625	.0440	.0362	.0267
13†	Aluminum	Al	26.97	.0844	.0614	.0431	.0353	.0266
14†	Silicon	Si	28.06	.0873	.0635	.0448	.0367	.0279
15	Phosphorus	P	<b>30.9</b> 8	.0854	.0617	.0434	.0358	.0274
16	Sulphur	S	32.066	.0879	.0636	.0448	.0368	.0287
17	Chlorine	Cl	35.457	.0846	.0611	.0430	.0357	.0278
18†	Argon	A	39.944	.0795	.0574	.0406	.0336	.0267
19	Potassium	K	39.096	.0859	.0620	.0437	.0366	.0289
20†	Calcium	Ca	40.08	.0885	.0637	.0451	.0378	.0302
21	Scandium	Sc	45.10	.0826	.0593	.0418	.0350	.0284
22	Titanium	Ti	47.90	.0818	.0588	.0413	.0347	.0285
23	Vanadium	v	50 <b>.95</b>	.0805	.0577	.0406	.0342	.0283
24	Chromium	Cr	52.01	.0827	.0589	.0417	.0351	.0293
25	Manganese	Mn	54.93	.0817	.0583	.0411	.0348	.0294
26†	Iron	Fe	55.85	.0840	.0598	.0422	.0359	.0305
27	Cobalt	Co	58. <b>94</b>	.0828	.0598	.0416	.0353	.0472
28	Nickel	Ni	58.69	.0866	.0613	.0434	.0369	.0319
29†	Copper	Cu	63.54	.0834	.0588	.0416	.0356	.0309
30	Zinc	Zn	65.38	.0841	.0585	.0418	.0357	.0314
31	Gallium	Ga	69.72	.0820	.0575	.0406	.0349	.0307
32	Germanium	Ge	72.60	.0820	.0572	.0403	.0347	.0308
33	Arsenic	As	74.91	.0824	.0573	.0403	<b>.035</b> 0	.0311
34	Selenium	Se	78. <b>96</b>	.0811	.0561	.0395	.0343	.0308
35	Bromine	Br	79.916	.0830	.0572	.0402	.0350	.0318
<b>36</b>	Krypton	Kr	83.70	.0817	.0563	.0397	.0346	.0315
37	Rubidium	Rb	85.48	.0835	.0567	.0400	.0349	.0322
38	Strontium	Sr	87.63	.0842	.0569	.0402	.0351	.0327
39	Yttrium	Y	<b>88.92</b>	.085 <b>9</b>	.0577	.0408	<b>.03</b> 58	.0335
40	Zirconium	Zr	91.22	.0864	.0578	.0409	.0360	.0338
41	Columbium	Съ	92.91	.0864	.0584	.0414	.0363	.0343
42†	Molybdenum	Mo	95.95	.0879	.0581	.0412	.0362	.0343
43	Masurium	Ma	•••	•••	•••	•••	•••	•••
44	Ruthenium	Ru	101.7	.0883	.0577	.0410	.0361	.0344
<b>4</b> 5	Rhodium	Rh	102.91	.0902	.0584	.0415	.0367	.0353
46	Palladium	Pd	106.7	.0901	.0577	.0410	.0363	.0351
47	Silver	Ag	107.88	.0920	.0586	.0416	.0369	.0358
48	Cadmium	Cd	112.41	.0912	.0576	.0409	.0363	.0354



SHIELD MATERIALS CHAP. 2.9

Table 2.9.2 — (Continued)

Atomic number,			Atomic		μ/	/ρ, cm²/gm	1	
Z	Element*	Symbol*	weight, A	0.5 mev	1 mev	2 mev	3 mev	6 mev
49	Indium	<b>I</b> n	114.76	0.0922	0.0578	0.0411	0.0364	0.0357
50†	Tin	Sn	118.70	.0923	.0573	.0407	.0361	.0356
51	Antimony	Sb	121.76	.0928	.0573	.0406	.0361	.0357
52	Tellurium	Te	127.61	.0915	.0560	.0396	.0354	.0351
53†	Iodine	I	126.92	.0954	.0579	.0408	.0364	.0364
54	Xenon	Хe	131.3	.0954	.0571	.0402	.0361	.0363
55	Cesium	Cs	132.91	.0978	.0578	.0406	.0367	.0369
56	Barium	Ba	137.36	.0978	.0572	.0402	.0363	.0367
57	Lanthanum	La	138.92	.100	.0581	.0406	.0368	.0373
58	Cerium	Ce	140.13	.103	.0591	.0411	.0373	.0380
59	Praseodymium	Pr	140.92	.106	.0601	.0417	.0380	.0388
60	Neodymium	Nd	144.27	.107	.0601	.0416	.0379	.0389
61	Promethium	Pm	~146	.109	<b>.0</b> 607	.0419	.0385	.0395
62	Samarium	Sm	150. <b>43</b>	.110	<b>.0</b> 606	.0415	.0382	.0394
63	Europium	Eu	15 <b>2</b>	.112	.0613	.0420	.0387	<b>.04</b> 00
64	Gadolinium	Gd	156.9	.113	.0608	.0416	.0383	.0397
65	Terbium	Tb	159.2	.115	.0613	.0417	.0386	.0401
66	Dysprosium	Dy	162. <b>4</b> 6	.116	.0616	.0417	.0386	.0403
67	Holmium	Ho	164.9 <del>4</del>	.118	.0620	.0419	.0388	.0406
<b>68</b>	Erbium	Er	167.2	.120	.0626	.0422	.0391	.0411
69	Thulium	Tn	169.4	.122	.0632	.0424	.0394	.0415
70	<b>Y</b> tterbium	Yb	173.0 <del>4</del>	.123	.0633	.0423	.0393	.0415
71	Lutecium	Lu	174.99	.125	.0641	.0427	.0396	.0420
72	Hafnium	Hf	178.6	.126	.0643	.0427	.0396	.0420
73	Tantalum	Ta	180.88	.128	.0650	.0430	.0399	.0424
74†	Tungsten	w	183.92	.131	.0655	.0432	.0400	.0426
75	Rhenium	Re	186.31	.134	.0662	.0436	.0402	.0429
76	Osmium	Os	190.2	.136	.0663	.0436	.0402	.0429
77	Iridium	Ir	1 <b>9</b> 3.1	.138	.0670	.0437	.0403	.0431
78†	Platinum	Pt	195.23	.142	.0676	.0444	.0407	.0435
79	Gold	Au	197.2	.145	.0687	.0449	.0409	.0440
80	Mercury	Hg	200.61	.147	.0692	.0451	.0411	.0441
81	Thallium	Tl	204.39	.149	.0695	.0452	.0410	.0442
82†	Lead	Pb	207.21	.152	.0703	.0456	.0413	.0445
83	Bismuth	Bi	<b>209</b>	.156	.0714	.0461	.0417	.0449
84	Polonium	Po	~210	.160	.0728	.0468	.0420	.0456
85	Astatine	At	~221	.157	.0709	.0454	.0409	.0442
86	Radon	Rn	222	.161	.0723	.0462	<b>.04</b> 15	.0449
87	Francium	Fr	~224	.164	.0735	.0467	.0419	<b>.04</b> 53
88	Radium	Ra	226.05	.168	.0746	.0472	.0423	<b>.04</b> 58
89	Actinium	Ac	~227	.173	.0760	.0479	.0429	<b>.046</b> 5
90	Thorium	Th	232.12	.175	.0762	.0477	.0428	.0463
91.	Protactinium	Pa	231	.183	.0784	.0489	.0443	<b>.04</b> 75
92†	Uranium	U	238.07	.185	.0779	.0483	.0435	.0471

^{*} Names and symbols of elements listed in accordance with International Atomic Weights of 1952

[†] G. R. White²; all other values are interpolated by M. K. Hullings³

Table 2.9.3 — Molecular Densities of Compounds Found in Shielding Materials and Atomic Densities of Hydrogen in the Compounds

Compound	Chemical formula	Molecular weight	Density, gm/cc	Molecular density (N), molecules/cc (× 10 ²² )	Atomic density of hydrogen in com- pound (N _H ), hydrogen atoms/cc × 10 ²²
Acetic acid	C ₂ H ₄ O ₂	60.05	1.05	1.05	4.21
Aluminum oxide	Al ₂ O ₃	101.94	4.00	2.36	•••
Ammonia*	NH ₃	17.03	0.771	2.73	8.18
Arsenous oxide	As ₂ O ₃	197.82	3.85	1.17	• • •
Barium sulfate	BaSO ₄	233.42	4.50	1.16	• • •
Beryllium carbide	Be,C	30.05	1.9	3.81	• • •
Beryllium oxide	BeO	25.02	3.02	7.27	• • •
Boron carbide	B ₄ C	55.29	2.54	2.77	• • •
Boron oxide	B ₂ O ₃	69.64	1.85	1.60	•••
Calcium carbonate	CaCO,	100.09	2.71	1.62	
Calcium oxide	CaO	56.08	3.32	3.57	• • •
Cellulose	$(C_6H_{10}O_5)_n$	162.14	1.35	0.502	5.02
Chromic oxide	Cr ₂ O ₃	152.02	5.21	2.06	• • •
Dodecane	C ₁₂ H ₂₆	170.33	0.75	0.302	6.76
Ferric oxide	Fe ₂ O ₃	159.70	5.12	1.93	• • •
Ferrous oxide	FeO	71.85	5.7	4.78	• • •
Glycerin	C ₃ H ₈ O ₃	92.09	1.26	0.824	6.59
Heavy water	D ₂ O	20.028	1.1076	3.32	6.64†
Lead oxide	PbO	223.21	9.2	2.48	•••
Limonite	2Fe ₂ O ₃ ·3H ₂ O	373.44	3.8 (ave)	0.61	• • •
Lithium borohydride	LiBH,	21.79	0.686	1.90	7.58
Lithium hydride	LiH	7.95	.820	6.21	6.21
Lucite	$(C_5H_8O_2)_n$	100.11	1.2	0.722	5.78
Magnesium chloride	MgCl,	95.23	2.32	1.14	• • •
Magnesium oxide	MgO	40.32	3.65	<b>5.4</b> 5	• • •
Neoprene	(C ₄ H ₅ Cl) _n	88.54	1.23	0.84	4.20
Octane (n)	CaH ₁₈	114.22	0.703	.371	6.68
Pentane (n)	C ₅ H ₁₂	72.15	.626	.523	6.28
Polyisoprene	$(C_5H_8)_n$	68.11	.92	.81	6.51
Polymethyl methacrylate	$(C_5H_8O_2)_n$	100.11	1.2	.722	5.78
Potassium hydroxide	кон	56.10	2.044	2.62	2.62
Potassium oxide	K ₂ O	94.19	2.32	1.48	• • •
Silicon carbide	SiC	40.07	3.17	4.76	• • •
Silicon oxide	SiO,	60.06	2.32	2.33	• • •
Sodium hydroxide	NaOH	40.00	2.13	3.20	3.20
Sodium oxide	Na ₂ O	61.99	2.27	2.21	• • •
Tetramethyl ammonium	-				
borohydride	(CH ₃ ) ₄ NBH ₄	89.00	0.813	0.550	8.80
Thorium borohydride	Th(BH ₄ ) ₄	291.53	2.59	.535	8.5 <b>6</b>
Titanium hydride	Ti H2	49.92	3.78	4.56	9.12
Titanium hydride	•	-	•		
(commercial)	Ti H,	49.92	3.25	3.92	7.84
Titanium oxide	TiO,	79.90	4.26	3.21	•••
Uranium hydride	UH ₃	241.09	10.86	2.71	8.14
Water	H ₂ O	18.016	1.00	3.35	6.69

^{*} Values given for the liquid state



[†] Deuterium atoms/cc

SHIELD MATERIALS CHAP. 2.9

:1:

15

्<del>रतः</del> १८ ं

١...

: .

.

33 18

• 3

ξ.) (2) (3)

:

1.

اقي. نخ

ڙ. اي

Table 2.9.4 — Densities of Some Additional Shielding Materials and Approximate Atomic Densities of Hydrogen in the Materials

Atomic density of hydrogen in compound (N_H), hydrogen atoms/cc  $\times$  10²² (approx.) Material Density, gm/cc Fuel oil 0.896.4 Gasoline 0.70 - 0.746.7 Natural rubber 0.92 6.51 Paraffin 0.87 - 0.917.82 - 8.014.2 - 8.0Synthetic rubber .9 - 1.2**Masonite** 1.3 4.7 Woods Ash 0.64 2.5 Balsa .16 0.61 Hickory .81 3.2 Oak, white 2.75 .71 Pine, white .67 2.5 Spruce .47 1.8 Hydrocarbons Aliphatic 0.77 - 0.806.6 - 7.14With aromatic ring .85 - 1.054.69 - 6.85With 1 alicyclic ring .823 - 0.9386.65 - 7.40Petroleum .8 - 1.07.0 - 7.7Other hydrocarbon fuels 7.0 - 7.23.4 - 6.4.81 - 1.38Esters 2.85 - 8.38Amines, amides, and other nitrogen .83 - 1.34compounds .85 - 1.272.99 - 6.45Carbonyl compounds * .85 - 0.894.74 - 6.95Silicon compounds Miscellaneous compounds with boiling .74 - 1.57point ~200°C

Table 2.9.5 — Calculated Mass Absorption Coefficients of Gamma Rays for Various Materials
Used in Shielding

		Mass absor	ption coefficie	ent (μ), cm ⁻¹
<b>Ma</b> terial	Density (ρ), gm/cc	1 mev	3 mev	6 mev
Air*	0.001294	0.0000336	0.0000254	0.0000209
Aluminum	2.7	.166	.0953	.0718
Ammonia (liquid)	0.771	.0612	.0322	.0221
Beryllium	1.85	.104	.0579	.0392
Beryllium carbide	1.9	.112	.0627	.0429
Beryllium oxide (hot-pressed blocks)	2.3	.140	.0789	.0552
Bismuth	9.80	.700	.409	. <b>44</b> 0
Boral	2.53	.153	.0865	.0678
Boron (amorphous)	2.45	.144	.0791	.0679
Born carbide (hot-pressed)	2.5	.150	.0825	.0675
Bricks				
Fire clay	<b>2.0</b> 5	.129	.0738	.0543
Kaolin	2.1	.132	.0750	.0552
Silica	1.78	.113	.0646	.0473
Carbon	2.25†	.143	.0801	.0554

^{*} Includes organic acids, aldehydes, ketones, diketones, acid anhydrides, and the like

CHAP. 2.9 RADIATION SHIELDING

Table 2.9.5 — (Continued)

		Mass absor	ption coeffici	ent (μ), cm
Material	Density (ρ), gm/cc	1 mev	3 mev	6 mev
Clay	2.2	0,130	0.0801	0,0590
Cements				
Colemanite borated	1.95	.128	.0725	.0528
Plain (1 Portland cement: 3 sand mixture)	2.07	.133	.0760	.0559
Concretes				
Barytes‡	3.5	.213	.127	.110
Barytes-boron frits‡	3.25	.199	.119	.101
Barytes-limonite‡	3.25	.200	.119	.0991
Barytes-lumite-colemanite‡	3.1	.189	.112	.0939
Iron-Portland‡	6.0	.364	.215	.181
MO (ORNL mixture)	5.8	.374	.222	.184
Portland§ (1 cement: 2 sand:	2.2	.141	.0805	.0592
4 gravel mixture)	2.4	.154	.0878	.0646
Flesh¶	1	.0699	.0393	.0274
Fuel oil (medium weight)	0.89	.0716	.0350	.0239
Gasoline	.739	.0537	.0299	.0203
Glass				
Boro-silicate	2.23	.141	.0805	.0591
Lead (Hi-D)	6.4	.439	.257	.257
Plate (ave)	2.4	.152	.0862	.0629
Iron	7.86	.470	.282	.240
Lead	11.34	.797	<b>.46</b> 8	.505
Lithium hydride (pressed powder)	0.70	.0444	.0239	.0172
Lucite (polymethyl methacrylate)	1.19	.0816	.0457	.0317
Paraffin	0.89	.0646	.0360	.0246
Rocks				
Granite	2.45	.155	.0887	.0654
Limestone	2.91	.187	.109	.0824
Sandstone	2.40	.152	.0871	.0641
Rubber				
Butenediene copolymer	0.915	.0662	.0370	.0254
Natural	.92	.0652	.0364	.0248
Neoprene	1.23	.0813	.0462	.0333
Sand	2.2	.140	.0825	.0587
Stainless steel, type 347	7.8	.462	.279	.236
Steel (1% carbon)	7.83	.460	.276	.234
Uranium	18.7	1.46	.813	.881
Uranium hydride	11.5	0.903	.504	.542
Water*	1.0	.0706	.0396	.0277
Wood				
Ash	0.51	.0345	.0193	.0134
Oak	.77	.0521	.0293	.0203
White pine	.67	.0452	.0253	.0175

^{*}G. R. White2

[†] Graphite theoretical density

[‡] Latest concrete mixtures for shielding reported by Gallaher and Kitzes.4

[§] Elemental composition, wt-%: H, 1.0; O, 52.9; Si, 33.7; Al, 3.4; Fe, 1.4; Ca, 4.4; Mg, 0.2; C, 0.1; Na, 1.6; K, 1.3

[¶] Composition, wt-%: O, 65.99; C, 18.27; H, 10.15; N, 3.05; Ca, 1.52; P, 1.02

Ġ

...

μ

(ORNL Lid Tank Measurements, corrected to Jan. 1, 1953)

Symbol	Removal cross section, barns
Al	1.2
Cu	2.0
С	0.84
Fe	2.0
Pb	3.4
	Al Cu C Fe

#### COMPOSITIONS AND PHYSICAL PROPERTIES

In the following tables, an attempt was made to give the latest and most authoritative data compiled from many sources. All information on a given material is grouped as closely together as possible. Much new and heretofore unavailable information on special materials recently developed, or now being developed, is included. The data are grouped as follows: (1) cements and concretes (Tables 2.9.7 through 2.9.24); (2) hydrogenous materials (Tables 2.9.25 through 2.9.38); and (3) miscellaneous materials (Tables 2.9.39 through 2.9.52). The last category includes metals and structural materials other than cements and concretes.

Table 2.9.7 — Compositions of Cements

						Plain c	ement§	
	Portland cement*		Colemanite borated cement, 1		1 cement: 3 sand mixture		1 cement: 2 sand mixture	
<b>M</b> aterial	Wt-% (approx.)	Vol-% (approx.)	Wt-%	Vol-%	Wt-%	Vol-%	Wt-%	Vol-%
MgO	2	2.6	28.1	13.5				•
SiO ₂	23	29.6						
Al ₂ O ₃	8	6.2						
Fe ₂ O ₃	4	2.4						
CaO	63	59.2						
Colemanite¶			28.1	20.3				
MgCl ₂			13.4	13.0				
H ₂ O			30.4	53.2	7.5	16.0	10.1	20.3
Portland cement					15.0	21.4	19.8	26.5
Sand**					77.5	62.6	70.1	53.2

^{*} Hool and Johnson⁵

[†] Rockwell and Roehrenbeck⁶

[#] Elemental composition, wt-%: B, 4.44; H, 4.06; Mg, 20.21; Cl, 10.01; O, 55.8; Ca, 5.47

[§] Plain cement percentages calculated from volume ratios of sand plus allowed water content per bag of cement

[¶] Ca,B,O,, ·5H,O

^{**} For composition of sand see Table 2.9.8

Table 2.9.8 - Composition of Sand*

Material	Wt -%	Vol-%
SiO ₂	78.1	73.7
Al ₂ O ₃	6.5	3.83
Fe ₂ O ₂	1.9	0.85
CaCO ₃	2.8	2.43
Na ₂ O	2.3	2.41
K ₂ O	1.4	1.42
H ₂ O	7.0	15.3

^{*}Average of dry compositions (corrected for water content) given by Pirsson⁸

Table 2.9.9 — Physical Properties of Cements

	Value or desc	ie or description			
	Coleman	ite borated cement*	Plain cement		
Property	Plain	With 5% Al turnings	1 cement : 3 sand mixture		
Density, gm/cc	1.95	1.99	2-2.15 (ave)†		
Specific heat, gm-cal/gm			0.20‡		
Thermal conductivity, Btu/(hr)(ft)(°F)	0.51	0.63	•		
Tensile strength, lb/sq in.			150- <b>600\$</b>		
Compressive strength, lb/sq in.	1,500	3,540	500-5600\$,¶		
Coefficient of expansion, per °F			~6 × 10 ⁻⁶ **		
Modulus of elasticity, lb/sq in.	70,000	178,000	~3,000,000**		

^{*} Rockwell and Roehrenbeck⁶

Portland cement

3.15 gm/cc for solid material

~1.5 gm/cc for loose powder

Sand

2.65 gm/cc with 7% moisture content



[†] Derived from Portland cement and sand densities as follows:

[‡] Handbook of Chemistry and Physics9

[§] Varies according to mechanical analysis (sieve sizes) of sand. The above values are quoted from Mechanical Engineers' Handbook[†]

¹ Varies according to water content. A cement mix using  $5\frac{1}{2}$  gal water per 94-lb bag of cement has a compressive strength of approximately 3500 lb/sq in  10 

^{**} From Concrete Engineers' Handbook, 1st edition, by G. A. Hool and N. C. Johnson. Copyright, 1918. By permission from McGraw-Hill Book Company, Inc., New York

SHIELD MATERIALS CHAP. 2.9

Table 2.9.10—Composition of Ordinary Concrete (Portland Concrete)*

<b>Ma</b> terial	Vol-%	Wt-%
Portland cement†	12.1	8.2
Sand‡	24.3	28.7
Gravel	48.6	56. <b>4</b>
Water	15.0	6.7

^{*}Concrete varies widely according to the mix and raw materials used. This table lists a typical compositions for a high-strength concrete with mixer's proportions of 1 cement: 2 sand: 4 gravel plus 15% water^{5,7,11}

Table 2.9.11 - Physical Properties of Ordinary Concrete (Portland Concrete)*

Property	Value or description
Density, gm/cc	2.3
Specific heat, Btu/(lb)(°F)	0.156
Thermal conductivity, Btu/(hr)(ft)(°F)	1 at 200°F
Tensile strength, lb/sq in.	~350†
Compressive strength, lb/sq in.	3500† after 28 days
Cost	~\$6.50/cu yd
Callahor and Kitzes ⁴ unless specified otherwis	

^{*}Gallaher and Kitzes* unless specified otherwise

Table 2.9.12 — Composition of MO Concrete*

	Density = 5.2 gm/cct		Density = 5.8 gm/cct	
Material	Wt-%	Vol-%	Wt-%	
MgO	7.8	12.5	5.00	
Steel punchings (¾ in.)	47.8	]	51. <b>4</b>	
Steel shot (1/8 in.)	21.6	62.4	23.1	
Steel shot $\binom{1}{20}$ in.)	14.4	j	15 <b>.4</b>	
MgCl ₂	2.4	7.7	1.4	
H ₂ O	6.0	17.4	3.7	

^{*} This concrete has been found not to stand up under weathering. A new concrete has been developed to replace MO concrete for use in shields (see Iron-Portland concrete, Table 2.9.20)

[†] For composition of Portland cement, see Table 2.9.7

[†] For composition of sand, see Table 2.9.8

[§] Elemental composition, wt-%: H, 1.0; O, 52.9; Si, 33.7; Al, 3.4; Fe, 1.4;

Ca, 4.4; Mg, 0.2; C, 0.1; Na, 1.6; and K, 1.3

[†] General Engineering Handbook 10

[†] Rockwell and Roehrenbeck⁶ reported that this MO mixture had a density of 5.8. Rockwell¹² stated that the original density was probably in error.¹³ Kitzes, Rockwell, and Gallaher¹⁴ give a density of 5.2 from an experimental determination for the mix originally reported⁶ to have a density of 5.8

[‡] T. Rockwell 12,13

Table 2.9.13 — Physical Properties of MO Concrete

	Value or d	escription	
Property	Density = 5.2 gm/cc*	Density = 5.8 gm/cc†	
Specific heat, gm-cal/gm	0.144		
Thermal conductivity, Btu/(hr)(ft)(°F)	2.4		
At 122°F		5.17	
At 527°F		3.42	
Thermal expansion coefficient, per °C	$\sim 1.0 \times 10^{-5}$	$1.1 \times 10^{-5}$	
Compressive strength, lb/sq in.		4000-5000‡	
At room temperature	4000 - 6000		
At 300℃	1200 - 3300		
At 500°C	700 – 1000		
Modulus of elasticity, lb/sq in.	$2.5 \times 10^{5}$		
Modulus of rupture, lb/sq in.	1380		
Heat evolved upon setting, watts/lb	<0.224		

^{*} Rockwell and Roehrenbeck 6  reported this MO mix to have a density of 5.8; the density was experimentally determined to be 5.2 by Kitzes et al 14 

Table 2.9.14 — Composition of Barytes Concrete

(Gallaher and Kitzes⁴)

Concrete for pouring		Concrete for pouring Co		oncrete blocks	
Material	Amount for 1 cu yd, lb	Wt-%	Amount for 1 cu yd, lb	Wt-%	
Barytes aggregate, coarse (1 in.)	2660	45.15	•••		
Barytes aggregate fine $\binom{3}{8}$ in.)	2320	39.23	•••	•••	
Barytes aggregate, medium $\binom{1}{2}$ in.)	•••	•••	5270	87.9	
Portland cement	550	9.37	500	8.3	
Water	370	6.25	230	3.8	
	(44.5 gal)		(27.5 gal)		

[†] Kitzes et al¹⁴

[‡] Developed strength after aging for 3 to 7 days; drops off rapidly because of poor aging characteristics

SHIELD MATERIALS CHAP. 2.9

Table 2.9.15 — Composition of Barytes Aggregate*
(Gallaher and Kitzes⁴)

<b>Ma</b> terial	Coarse† (1 in.), wt-%	Fine $(\frac{3}{8})$ in.), wt-%
BaSO ₄	95.9	81.6
Fe	1.0	9.85
Ca	0.5	0.9
0,	1.3	6.2

^{*}Supplied by L. A. Woods and Sons, Sweetwater, Tennessee, at \$18/ton

Table 2.9.16 — Physical Properties of Barytes Concrete
(Gallaher and Kitzes⁴)

Property	Value or description
Density, gm/cc	<b>3</b> .5
Specific heat, gm-cal/gm	
At 122°F	0.123
At 392°F	.150
Thermal conductivity, Btu/(hr)(ft)(*F)	
At 122°F	.926
At 212°F	.997
At 392°F	.866
At 482°F	.745
Compressive strength, lb/sq in.	
Age 28 days	3600
Age 112 days	4200
Shear strength, lb/sq in.	845
Expansion upon setting, in./in.	
After 2 to 3 days	8 × 10 ⁻⁴
After 28 days	$5 \times 10^{-4}$

[†] Specific gravity = 4.2

**[‡]**Specific gravity = 4.0

[§] The increase in Fe content of fine aggregate results from concentration of  $\text{Fe}_2\text{O}_3$  during crushing

CHAP. 2.9 RADIATION SHIELDING

Table 2.9.17 — Composition of Barytes-Limonite Concrete*

(Gallaher and Kitzes⁴)

Material	Amount for 1 cu yd, lb	₩t-%	Vol-%
Barytes aggregate, coarse (3/4 in.)	2210	40.4	44.5
Barytes aggregate, fine $\binom{3}{8}$ in.)	1050	19.2	} 44.5
Limonite, crushed (2Fe ₂ O ₃ ·2H ₂ O)	1220	22.3	19.8
Portland cement, Type I	610	11.1	12.0
Water	384 (46 gal)	7.0	23.7

^{*}Density, 3.25; 7-day compressive strength, 3750 lb/sq in.; other physical properties similar to barytes concrete

Table 2.9.18 — Elemental Compositions of Barytes and Barytes-Limonite Concretes

(Gallaher and Kitzes⁴)

Element	Barytes (blocks), wt-%	Barytes-Limonite, wt-%
Fe	8.78	13.66
H	0.43	1.02
0	31.03	37.70
Mg	0.38	0.23
Ca	4.53	5.37
Ba	41.93	31.97
Na	0.13	0.09
Si	1.74	1.35
Al	0.57	0.50
Mn	.07	.14
S	9.94	7.58

SHIELD MATERIALS CHAP. 2.9

Table 2.9.19 — Description of Several Concretes Recently Developed for Shielding Use (Gallaher and Kitzes⁴)

<b>M</b> aterial	Description
Iron-Portland	Dense Portland-cement concrete developed to replace MO concrete; good workability; high density (~6 gm/cc), low water content (~3%)
Colemanite-Barytes	Boron in colemanite $(2\text{CaO} \cdot 3\text{B}_2\text{O}_3.5\text{H}_2\text{O})$ acts as gamma suppressor, but high solubility of colemanite retards initial set of Portland cement; this concrete has higher density $(3.1 \text{ gm/cc})$ than ordinary concrete, high water content $(6-8\%)$ , and $1\%$ boron content
Boron Frits-Barytes*	Boron in boron frits acts as gamma suppressor, and boron frit is less soluble than colemanite; thus, detrimental effect on initial set of Portland cement is not so great; this concrete has higher density (3.1 gm/cc) than ordinary concrete, medium water content (5%), and 1% boron content
Lumnite-Colemanite- Barytes†	As an alternate to using Portland cement in barytes-colemanite concrete, lumnite was used and found to retard initial set of cement only slightly; this concrete has higher density (3.1 gm/cc) than ordinary concrete, high water content (~9.3%), and 1% boron content; curing methods were unsatisfactory
Lumnite-Portland- Colemanite Barytes†	Portland cement usually accelerates initial set of lumnite, but addition of colemanite counterbalanced this effect; this concrete has higher density (3.1 gm/cc) than ordinary concrete, high water content $(8-10\%)$ , and $1\%$ boron content

^{*}For composition of boron frits, see Table 2.9.21

[†]For composition of lumnite, see Table 2.9.22

Table 2.9.20 -- Compositions of Several Concretes Recently Developed for Shielding Use

(Gallaher and Kitzes⁴)

	Iron-Portland	land	Colemanite-barytes Boron frits-barytes	arytes	Boron frits-l	barytes	Lumnite- colemanite-barytes	arytes	Lumnite-Portland- colemanite-barytes	rtland- arytes
	Amount for	8	•	8	Amount for Amount for	6 m	Amount for	Wt-9.	Amount for	Wt-9
Material	ı cu ya, ıb	0/ - J.M		8-14	t ca ya, 10		מי יהל אם ז			?
Iron punchings*	5070	50.4								
SAE shot†										
No. 1110	2280	22.8								
No. 330	1520	15.2								
Portland cement										
Type I	890	8.9	830	14.96	099	12.0				,
Type III									460	
Water	260	2.7	310	9.9	280	2.0	413	7.9	460	8.5
	(31 gal)		(37.5 gal)		(33 gal)		(49.5 gal)		(55 gal)	
Barytes aggregate, ‡			3920	72.22						
specially graded\$										,
Barytes aggregate, ‡					3120	26.8	2990	57.2	3490	64.18
coarse $(\frac{3}{4}$ in.)								,	į	
Barytes aggregate,‡					770	14.0	695	13.3	210	3.87
fine (% in.)										
Colemanite,			400	7.14						
specially graded¶							į	,	į	,
Colemanite, dust							334	4.9	350	6.40
Boron frits**					670	12.2				
Lumnite†							795	15.2	460	8.5

*Slugs ranging from  $\frac{1}{4}$  to 1 in. in diameter; rust not removed prior to use  $\dagger$  SAE 1110 and SAE 330 shot were  $\frac{1}{4}$  and  $\frac{1}{4}$  in. in diameter, respectively  $\ddagger$  For composition of barytes aggregate, see Table 2.9.15 \$95-100% passing through No. 4 sieve size

** For composition of boron frits, see Table 2.9.21

¶100% passing through No. 16 sieve size

Digitized by Google

A THE STATE OF THE

Table 2.9.21 — Analysis of Boron Frits*

(Gallaher and Kitzes⁴)

Material	Wt-%
SiO ₂	31.00
Al ₂ O ₃	1.70
B ₂ O ₃	27.40
CaO	5.20
BaO	12.90
ZnO	6.70
Na ₂ O	12.20
K,O	1.00
F	1.90

*Boron frit is formed by fritting borax with silica and is obtained from the Chicago Vitreous Enamel Products Co., Cicero, Illinois

Table 2.9.22 — Analysis of Lumnite*

(Gallaher and Kitzes⁴)

Material	Wt-%
SiO ₂	9.1
FeO	5.9
Fe ₂ O ₃	4.7
$Al_2O_3 + TiO_2$	41.6
CaO	36.8
MgO	1.0
SO ₃	0.17
Insoluble residue	.70

*A calcium aluminate hydraulic cement manufactured by Universal Atlas Cement Co., New York, N. Y. CHAP. 2.9 RADIATION SHIELDING

Table 2.9.23 — Elemental Compositions of Several Concretes Recently Developed for Shielding Use

### (Gallaher and Kitzes⁴)

Element	Iron-Portland, wt-%	Colemanite- Barytes, wt-%	Boron Frits- Barytes, wt-%	Lumnite- Colemanite- Barytes, wt-%	Lumnite-Portland- Colemanite- Barytes, wt-%
Fe	87.50	1.03	2.19	3.07	1.87
H	0.33	0.85	0.56	1.09	1.10
В		.98	1.04	0.88	1.02
Ο	5.82	34.89	33.80	36.95	36.98
Mg	0.13	0.22	0.23	0.14	0.20
Ca	3.96	8. <b>4</b> 6	6.26	<b>5.4</b> 8	7.67
Ba		40.70	40.13	38.59	38.03
Na		0.11	1.21	0.11	0.11
Si	0.91	1.76	3.31	.96	1.49
Al	.33	0.61	0.64	1.76	1.32
Mn	.35	.01	.02	0.12	0.04
S	.05	9.63	9.15	9.06	8.97
Zn			0.66		
K			.10		
F			.23		
Ti				1.27	0.071

Table 2.9.24 — Densities and Compressive Strengths of Several Concretes Recently
Developed for Shielding Use

### (Gallaher and Kitzes⁴)

Concrete	Density, gm/cc	Compressive strength, lb/sq in.
Iron-Portland	5.8-6.0	3663 (age – 32 days)
		5288 (age – 91 days)
Colemanite-barytes	3.1 - 3.2	2500 (after 6-day cure)
Boron frits-barytes	3.1	
Lumnite-colemanite-barytes	3.1	~3500
Lumnite-Portland-colemanite- barytes	3.1	3000 (after 6-day cure)

ST.3

347

就以強以強致

9, 20

Table 2.9.25 — Physical Properties of Ammonia (Liquid), NH3

Property	Value or description*
Appearance	Pungent colorless liquid
Density, gm/cc	
Of solid (-79°C)	0.817
Of liquid (-77.7°C)	.771
Specific heat of liquid, gm-cal/gm	
At -60°C	1.047
At 0°C	1.098
At 20°C	1.125
At 100°C	1.48
Heat of vaporization, gm-cal/gm	
At -33.35°C	327.1
At -20°C	317.6
At -10°C	309.7
At 0°C	301.6
Heat of fusion $(m.p., -77.7^{\circ}C)$ ,	94.15
Heat of formation, kg-cal/mol	-11.00 (heat evolved)
Free energy of formation, kg-cal/mol	-3.94 (heat evolved)
Thermal conductivity, Btu/(hr)(ft)(°F)	0.29
Melting point, °C	-77.7
Boiling point, °C	-33.35
Solubility in water (0°C), parts per 100	89.9
Critical constants	
Temperature, *C	132.9
Pressure, lb/sq in.	1651 (112.3 atm)
Density, gm/cc	0.235

* Handbook of Chemistry, 15 Handbook of Chemistry and Physics, 9 and Chemical Engineers' Handbook 16

Table 2.9.26 - Composition of Fuel Oil*†

		Cor	nposition, wt-	-%	
Density (ave), gm/cc	C	Н	S	N	O
0.89	85.62	11.98	0.35	0.50	0.60

* Fuel oil is comprised of the crude-oil fractions distilling between 200° and 370°C; its chemical composition and specific gravity vary with the type of crude oil. Mid-Continent crude oils yield a fuel oil (specific gravity, 0.89) which is a mixture predominantly of saturated hydrocarbons with a small percentage of unsaturated chains and aromatics

† Reprinted from Mechanical Engineers' Handbook, 5th edition, edited by L. S. Marks. Copyright, 1951. By permission from McGraw-Hill Book Company, Inc., New York

Table 2.9.27 — Physical Properties of Fuel Oil

Property	Value or description*
Density (ave), gm/cc	0.89
Specific heat (21°-58°C), gm-cal/gm	<b>.5</b> 1
Thermal conductivity (13°C), cal/(sec)(cm)(°C)	$0.355 \times 10^{-3}$
Thermal expansion coefficient (24°-120°C), per °C	$.955 \times 10^{-3}$
Boiling point range, *C	210 - 360
Flash point, °C	
Open cup	250
Closed cup	100 - 200
Viscosity (15.6°C), cp	660
Susceptibility to spontaneous heating	None

^{*} Handbook of Chemistry,  15  Handbook of Chemistry and Physics,  9  and Chemical Engineers' Handbook  16 

Table 2.9.28 — Composition of Gasoline*†

		Composition, wt-%	
Density at 60°F, gm/cc	C	Н	S
0.713	84.3	15.7	•••
.739	84.9	14.76	0.08

^{*} The composition^{7,17} of gasoline varies with the method of production and the type of crude oil from which it is obtained; in general it is made up of saturated aliphatic compounds ranging from  $C_5H_{12}$  to  $C_{12}H_{26}$ , with an average composition corresponding to  $C_8H_{18}$  (octane)

Table 2.9.29 — Physical Properties of Gasoline

Property	Value or description*
Density, gm/cc	0.70 - 0.74
Specific heat (20°C), gm-cal/gm	0.5
Thermal conductivity (4°C), cal/(sec)(cm)(°C)	$0.45 \times 10^{-3}$
Boiling point, °C	38-205
Flash point (closed cup), °C	<b>-45</b>
Vapor pressure (room temp.), mm Hg	2.0
Explosive limits, % by vol. in air	
Upper	6
Lower	1.3
Susceptibility to spontaneous heating	None

^{*} Handbook of Chemistry,  15  Mechanical Engineers' Handbook,  9  and Collier's Encyclopedia  17 

[†] Reprinted from Mechanical Engineers' Handbook, ⁷ 5th edition, edited by L. S. Marks. Copyright, 1951. By permission from McGraw-Hill Book Company, Inc., New York

C.1...(2

572

Ľ

Table 2.9.30 — Composition and Physical Properties of Lucite (Plexiglass)*

Property	Value or description		
Chemical formula,	Polymethyl methacrylate, (C ₅ H ₈ O ₂ ) _n		
Appearance	Transparent colorless or whitish		
	thermoplastic; hard		
Density, gm/cc	1.18 - 1.2		
Specific heat, gm-cal/gm	0.35		
Thermal conductivity, cal/(sec)(cm)(°C)	$4-6 \times 10^{-4}$		
Thermal expansion coefficient, per °C	$7-9 \times 10^{-5}$		
Elongation at yield, %	1-10		
Tensile strength, lb/sq in.	4,000-6,000		
Flexural strength, lb/sq in.	10,000-20,000		
Compressive strength, lb/sq in.	9,000-15,000		
Heat distortion point, °C	58-93		
Decomposition (thermal) temperature, °C	170 – 250		
Water absorption, %	0.3 - 0.6		
Flammability, in./min	$\frac{1}{2}-1$ (slight)		

^{*}Reprinted from Handbook of Chemistry, 15 7th edition, edited by N. A. Lange. Copyright, 1949. By permission from Handbook of Publishers, Inc., Sandusky, Ohio

Table 2.9.31 — Composition and Physical Properties of Rubber*

	Value or description				
Property	Natural rubber	Neoprene	Butenediene copolymer		
Chemical formula	Polyisoprene, (C ₅ H ₈ ) _n	(C4H5Cl)n	C365 H727		
Density, gm/cc	0.92	1.23	0.915		
Specific heat, gm-cal/gm	<b>.4</b> 5	~0.45	.464		
Thermal conductivity, Btu/(hr)(ft)(°F)	1.07	1.07	• • •		
Elongation (gum stock), %	<b>77</b> 5	600	800		
Resilience, %	90	75	50		
Tensile strength (gum stock), lb/sq in.	3100	2800	2000		
Tear resistance, lb/sq in.	1640	1100	1000		
Creep (70°C)	26	62	• • •		
Maximum usable temperature, *C	80	65	65		
Brittle point, °C	-56	<b>-4</b> 0	<b>-4</b> 5		

^{*}Reprinted from Handbook of Chemistry, 15 7th edition, edited by N. A. Lange. Copyright, 1949. By permission from Handbook of Publishers, Inc., Sandusky, Ohio

CHAP. 2.9 RADIATION SHIELDING

Table 2.9.32 — Composition and Physical Properties of Paraffin*

Property	Value or description†
Density range, gm/cc	0.87-0.91
Specific heat (0°-20°C), gm-cal/gm	0.694
Thermal conductivity (0°C), cal/(sec)(cm)(°C)	$0.688 \times 10^{-3}$
Thermal expansion coefficient (20°C), per °C	$5.88 \times 10^{-4}$
Melting point, ‡ °C	<b>48-56</b>
Boiling point, °C	>370
Flash point, °C	
Open cup	199
Closed cup	221

^{*} Paraffin is composed of the heavy waxy components of crude-oil distillate, which are solid at room temperature. They are mainly saturated compounds with a formula ranging from  $C_{18}H_{38}$  to  $C_{35}H_{72}$  (average composition near  $C_{25}H_{52}$ )¹⁵.¹⁷

Table 2.9.33 — Typical Analyses of Surface and Ground Waters in the United States*

	Analyses of various types of water,† ppm				
Material	Type A	Туре В	Type C	Type D	Type E
Silica (SiO ₂ )	2.4	12	. 10	9.4	22
Iron (Fe)	0.14	0.02	0.09	0.2	0.08
Calcium (Ca)	5.8	36	92	96	3.0
Magnesium (Mg)	1.4	8.1	34	27	2.4
Sodium (Na)	1.7	6.5	8.2	183	215
Potassium (K)	0.7	1.2	1.4	18	9.8
Bicarbonate (HCO ₃ )	14	119	339	334	549
Sulfate (SO ₄ )	9.7	22	84	121	11
Chloride (Cl)	2.0	13	9.6	280	22
Nitrate (NO ₃ )	0.54	0.1	13	0.2	0.52
Total dissolved solids	31	165	434	983	564
Total hardness	20	123	369	351	17
as CaCO ₃					

^{*} Reprinted from Handbook of Chemistry, 15 7th edition, edited by N. A. Lange. Copyright, 1949. By permission from Handbook Publishers, Inc., Sandusky, Ohio

[†] Handbook of Chemistry and Physics, Handbook of Chemistry, Is and Collier's Encyclopedia IT

[‡] Commercial types of paraffin wax are usually designated by their melting point range, three of which are: (1) 118°-120°F; (2) 122°-124°F, and (3) 130°-132°F

[†] Type A: Natural soft water; contains around 30 ppm of dissolved solids; found in rivers and lakes of New England, New York, and mountainous regions of U. S.; high corrosive action

Type B: Intermediate-hard water; contains well over 100 ppm of dissolved solids; typical of Great Lakes and St. Lawrence waterway; may need to be softened for industrial use

Type C: Hard water from wells 30 to 60 ft deep; contains well over 300 ppm of dissolved solids; commonly used in heart of U.S. for public supplies; must be softened for domestic and industrial uses

Type D: Hard water from wells 2,000 ft deep; contains more chloride than Type C and high number of dissolved solids; not common; must be softened for industrial use

Type E: Naturally softened water from wells 300 ft deep or more; high totality of dissolved solids but hardness very low; may be highly colored; common in Atlantic and Gulf coastal plain

SHIELD MATERIALS

Table 2.9.34 — Physical Properties of Water at Various Temperatures*

(Handbook of Chemistry¹⁵)

y, cp	_		0		ω.
Viscosity, cp	1.7921		1.0050		0.3565
Cubical expansion,‡			8.18 × 10 ⁻⁵		2.81 × 10-4
Thermal conductivity, e) cal/(sec)(cm)(°C)		$1.29 \times 10^{-3}$ $1.36 \times 10^{-3}$		$1.555 \times 10^{-3}$	
Heat of vaporization gm-cal/gm	595.9		584.9	568.5	551.5 539.55
Specific heat, gm-cal/gm	1.00874		1.0000	0.99829	1.00239
Density,† gm/cc	0.99984		0.99820	0.98804	0.95835
Temperature, °C Density,† gm/cc	0 4	<b>4</b> .1	20	40.8	80 100

* Critical constants: Temperature, 0°C; pressure, 217.72 atm; density, 0.4 gm/cc

† Absolute values

## Approximate values Greatest density

Digitized by Google

CHAP. 2.9 RADIATION SHIELDING

Table 2.9.35 -- Composition of Various Types of Wood*

				Composition, wt-20	, wr-70		
Type of wood	Cellulose	Lignin	Resins and polyosest	Acetic acid	Inorganic ash‡	Moisture	Pores, vol-%
Balsa	54.2	26.5	4.93	5.80	2.12	6.47	87.7
Hickory	56.2	23.4	8.71	2.51	69.0	8.49	37.7
Spruce	41.5	28.0	25.9	1.39	.31	2.90	66.1
White ash	53.4	28.4	8.80	2.66	.34	6.40	50.8
White oak	48.7	32.7	8.25	2.57	.43	7.35	45.3
White pine	54.2	26.5	14.5	1.43	.43	2.94	49.4

† Polyoses include pentosan, hexosan, mannan, xylan, and saccharides; resins include proteins, fats, and terpenes ‡ Ash content varies; contains small amounts of K₁O, CaO, MgO, P₁O₅, Fe₂O₃, SO₃, SiO₂, and Na₂O. First three *From E. Hägglund¹⁸ and Handbook of Chemistry, ¹⁵ 7th edition, edited by N. A. Lange. Copyright, 1949. By permission from Handbook Publishers, Inc., Sandusky, Ohio compounds are the most abundant

Table 2.9.36 — Physical Properties of Various Types of Wood

Property	Balsa	Hickory	Spruce	White ash	White oak	White pine
Average density,* gm/cc	0.16	0.81	0.47	0.64	0.71	0.67
Density range,† gm/cc	0.11 - 0.20	0.11-0.20 $0.60-0.93$ $0.31-0.55$ $0.51-0.85$	0.31 - 0.55	0.51 - 0.85	0.46 - 0.85	0.31 - 070
Specific heat, ‡ gm-cal/gm	Betwe	Between 0.45 and 0.65 for most woods\$	65 for most v	\$spoon	0.5704	₽79.0
Thermal conductivity, ** cal/(sec)(cm)(°C)						
Parallel to grain					.00083	.00083
Perpendicular to grain	0.000115				.00031	.00024
Thermal expansion coefficient, per °C	2-5 × 1	$2-5 \times 10^{-6}$ for most woods §	woods \$	$9.5 \times 10^{-6}$		
Tensile strength, ** lb/sq in.					4,400	5,100
Bending stress at proportional		10,900	6,500		7,900	000,9
limit, †† lb/sq in.						4,840
Maximum crushing strength		8,970	5,590		7,040	860
(parallel to grain), †† lb/sq in.						
Maximum shearing strength, †† lb/sq in.		2,140	1,070		1,890	
Hardness, ††, ‡‡ lb						
End			630	1,680	1,420	200
Side			490	1,260	1,330	400
* Air-dried wood ¹⁵						

‡ The specific heat of practically all woods when oven-dry is 0.327 gm-cal/gm

§ Chemical Engineers' Handbook 16

** From Handbook of Chemistry, 18 7th edition, edited by N. A. Lange. Copyright, 1949. By permission from Handbook ¶Mechanical Engineers' Handbook

Publishers, Inc., Sandusky, Ohio †† Handbook of Engineering Fundamentals¹⁹

11 Load required to embed an 0.444-in. ball to 1/2 its diameter in the wood

CHAP. 2.9 RADIATION SHIELDING

Table 2.9.37 — Relationship Between Density of Wood and Volume Composition
(E. Hägglund¹⁸)

	Composition, vol-%			
Density, gm/cc	Cell walls	Pores		
0.1	6.7	93.3		
.2	13	87		
.3	20	80		
.4	27	73		
.5	34	66		
.6	40	60		
.7	47	53		
.8	53	47		
.9	60	40		

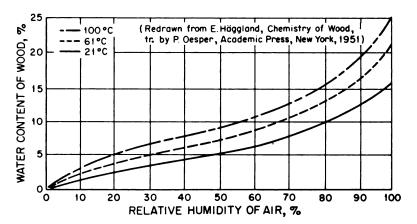


Fig. 2.9.1—Relationship Between Water Content of Air-dried Wood and Relative Humidity of the Air at Various Temperatures. Submitted by Oak Ridge National Laboratory, Mar. 16, 1953; redrawn from Häggland¹⁸

Table 2.9.38 — Composition and Physical Properties of Masonite

Pro	ner	tv	
FIU	PCI	·,	

Value or description

Composition*,†

Wood-fiber board of the Masonite Corp. produced from by-product wood chips reduced to cellulose fibers by high-pressure steam; contains ~6% hydrogen

Density,† gm/cc
Tensile strength,‡ lb/sq in.
Flexural strength,‡ lb/sq in.
Modulus of rupture,* lb/sq in.
Usefulness in shields§

1,3 7,000-8,000 12,000-13,000 5,000-15,000

Slows down fast neutrons; absorbs some thermal neutrons; has little effect on gamma rays

^{*} Brady²

[†] Quinn and Thompson²¹

[‡] Simonds, Weith, and Bigelow²²

[§] Hanford Works Technical Manual²³

Table 2.9.39 — Densities and Boiling-point Ranges of Various Organic Compounds (NEPA-1381²⁴)

Type of compound	Formula range	Density range, gm/cc	Boiling point, *C
Hydrocarbons			
Aliphatic	C ₁₆ H ₃₄ to C ₂₆ H ₅₄	0.77 - 0.80	136-242*
With aromatic ring	C14H20 to C39H72	.85-1.05	133-334*
With 1 alicyclic ring	C14H28 to C31H60	.823 - 0.938	123 - 208 *
Petroleum		.8-1.0	700 - 1000
Esters		.81 - 1.38	146 - 370
Amines, amides, and other			
nitrogen compounds		.83-1.34	180 - 350
Carbonyl compounds†		.85 – 1.27	180 - 350
Silicon compounds		.85 - 0.89	165 - 450
Miscellaneous compounds with boiling point 200°C		.74 – 1.57	187 – 215

^{*}Temperatures at 10-mm-Hg pressure

Table 2.9.40—Composition of Dry Air*

		Composition		
Component	Symbol	Wt-%	Vol-%	
Nitrogen	N ₂	75.50	78.06	
Oxygen	02	23.15	20.99	
Argon	A	1.292	0.9323	
Carbon dioxide	CO ₂	0.05	.03	
Hydrogen	H ₂	.0007	.01	
Neon	Ne	.0014	.0018	
Helium	He	.000065	.0005	
Krypton	Kr	.0003	.0001	
Ozone	Ο3	.0001	.00006	
Xenon	Xe	.00004	.000009	

^{*}Reprinted from Handbook of Chemistry, 15 7th edition, edited by N. A. Lange. Copyright, 1949. By permission from Handbook Publishers, Inc., Sandusky, Ohio

[†] Includes organic acids, aldehydes, ketones, diketones, acid anhydrides, and the like

Table 2.9.41 — Density of Air at Various Temperatures

	Density of dry air		Moist air†	
Temperature, *C	at 760 mm Hg,* gm/liter	Relative humidity, %	Vapor pressure, mm Hg	Density, gm/liter
-147	0.92‡			
-20	1.396			
0	1.293	<b>4</b> 5	2.090	1.292
		81	3.732	1.291
20	1.205	44	7.72	1.192
		74	13.05	1.183
50	1.092	<b>4</b> 5	41.63	1.070
		75	6 <b>9.3</b> 8	1.055
100	0.9458			
200	.7457			
300	.6166			
400	.52 <b>4</b> 8			

^{*}From Handbook of Chemistry, 15 7th edition, edited by N. A. Lange. Copyright, 1949. By permission from Handbook Publishers, Inc., Sandusky, Ohio

Table 2.9.42 — Compositions of Various Types of Bricks*

			Composition,	wt-% (ave)		
Type of brick	SiO ₂	Al ₂ O ₃	Fe ₂ O ₃	TiO3	MgO	CaO
Fire clay (high-heat duty)	50-57	36-42	1.5 - 2.5	1.5 - 2.5		
Kaolin (white)	52	45.4	0.6	1.7	0.2	0.1
Silica	96	1	1	•••	•••	2

^{*}Reprinted from Mechanical Engineers' Handbook, 5th edition, edited by L. S. Marks. Copyright, 1951. By permission from McGraw-Hill Book Company, Inc., New York

[†] Handbook of Chemistry and Physics 9

[‡] Liquid, value given in gm/cc

rets rt

Table 2.9.43 — Physical Properties of Various Types of Bricks*

	Fire clay		
Property	(high-heat duty)	Kaolin (white)	Silica
Density,† gm/cc	2.1	2.1	1.8
Specific heat, gm-cal/gm	0.23	0.22	0.23
Thermal conductivity, Btu/(hr)(ft2/in.)(°F)			
At 400°F	6		8
At 800°F	7	11	10
At 1200°F	8	12	12
At 2400°F	12	14	15
Mean thermal expansion coefficient, per °F	$0.27 \times 10^{-5}$	$0.23 \times 10^{-5}$	$0.46 \times 10^{-5}$ ‡
Weight of $9 \times 4^{1}/_{2} \times 2^{1}/_{2}$ in. brick, lb.	7.5	7.7	6.5
Porosity, %	20 (ave)	18	25 (ave)
Reheat shrinkage, %	0 to ±1.5 at 2550°F	-0.7 to 1.0 at 2910°F	0.5 to 0.8 at 2640°F
Deformation under load, %	2.5 to 10 at 2460°F and 25 lb/sq in.	0.5 at 2640°F and 25 lb/sq in.	
Fusion point, *F	3130 (approx.)	3200	3075 (approx.)
Spalling resistance	Good	Excellent	Poor §

^{*}Reprinted from Mechanical Engineers' Handbook, 5th edition, edited by L. S. Marks. Copyright, 1951. By permission from McGraw-Hill Book Company, Inc., New York

Table 2.9.44—Compositions of Lead and Silica Glasses

	Lead g	glass*,†	Silica	glass,‡ wt-%
Material	Wt-%	Vol-%	Plate glass§	Boro-silicate glass
Рьо	81.0	53.1		
SiO ₂	17.3	44.5	72	80.6
TiO,	1.35	1.9		
As ₂ O ₃	0.35	0.5		
CaO			15	0.8
Na ₂ O			13	3.8
K₂O				0.2
Al ₂ O ₃				2.0
B ₂ O ₃				11.9

^{*&}quot;Hi-D" glass made especially for radiation shielding by Penberthy Instrument Co., Inc., Seattle, Washington. Elemental composition, wt-%: Pb, 75.19; O, 15.65; Si, 8.08; Ti, 0.81; As, 0.27

[†] Approximate; calculated

[‡] Up to 0.56 at red heat

[§] Excellent if left above 1200°F

[†] Kernohan and McCammon²⁵

[‡] From Van Nostrand's Scientific Encyclopedia, ²⁶ 2d edition. Copyright, 1947. By permission from D. Van Nostrand Company, New York

[§] Average values for several glasses

CHAP. 2.9 RADIATION SHIELDING

Table 2.9.45 — Physical Properties of Lead and Silica Glasses

		Silic	a glass
Property	Lead glass* (Hi-D glass)	Plate glass†	Boro-silicate glass‡
Appearance	Light yellow tint; color- less in thin sections		
Density, gm/cc	6.4	2.4	2.23
Specific heat, gm-cal/gm		0.25	0.20
Thermal conductivity, cal/(sec)(cm)(°C)		$2.37 \times 10^{-3}$	$2.8 \times 10^{-3}$
Thermal expansion coefficient, per °C		$0.49 \times 10^{-6}$	$0.325 \times 10^{-5}$
Tensile strength, lb/sq in.		4,000	4,000 - 10,000
Strain point, *F		890	960
Softening point, °F		2,600	1,510
Index of refraction	1.96	1.47	1.47
Gamma shielding characteristic	Approximately equiva- lent of steel; 55% as effective as lead§		

^{*}Kernohan and McCammon²⁵

Table 2.9.46 — Composition of Various Types of Commercial Iron  $(\text{Metals Handbook}^{27})$ 

		Composition, w	rt-%	
Component	Armco ingot iron	Wrought iron (Byers No. 1)	Cast iron (gray)	Steel (SAE-1095)
Fe	99.83	98.475	92.95	97.13
0	0.11	<b>In</b> slag	• • •	• • •
S	.025	0.01	0.10	0.014
Mn	.017	.015	.65	.36
С	.012	.08	3.4	1.02
P	.005	.062	0.3	0.013
Si	Trace	.158	2.6	.08
Slag	•••	1.20		• • •
Cu	•••	•••	•••	0.05

[†] From Handbook of Chemistry, ¹⁶ 7th edition, edited by N. A. Lange. Copyright, 1949. By permission from Handbook Publishers, Inc., Sandusky, Ohio

[‡] Values for Corning No. 7740 glass¹¹

[§] Manufacturer's claim

Ξ

Table 2.9.47 — Physical Properties of Various Types of Commercial Iron

(Metals Handbook²⁷)

Property	Ingot iron	Wrought iron (Byers No. 1)	Cast iron (gray)	Carbon steel (SAE-1095)
Appearance	Pure iron is bright lust	Pure iron is bright lustrous metal; impurities change appearance (to gray or black) and physical properties	ppearance (to gray or	black) and physical properties
Density, gm/cc	7.86	7.70	6.95 - 7.35	7.83
Specific heat, gm-cal/gm	0.133*	0.1152*	0.1189*	0.116
	(18°-100°C)	(15°-100°C)	(20°-100°C)	(50°-100°C)
Thermal conductivity, cal/(sec)(cm)(°C)	~0.175 (18°C)	0.144 (18°C)	0.11	0.113 (0°C)
	~.15 (200°C)			.106 (200°C)
Thermal expansion, per °C	$11.7 \times 10^{-6}$ † (20°C)	$11.4 \times 10^{-6}$	$10.5 \times 10^{-6}$	$11.5 \times 10^{-6}$
	$12.7 \times 10^{-6}$ † (100°C)	(18°-100°C)	(0°-100°C)	(15°-75°C)
Elongation, %	45 (16°C)	25-40‡	25-30	22*
	26.5 (200°C)			
Tensile strength, lb/sq in.	49,500 (16°C)	42,000-52,000	25,000-50,000	70,000
	65,600 (200°C)			
Compression strength, lb/sq in.	19,400\$		65,000 - 160,000	
Melting point, °C	1, 539 ± 1	1,510*	1,230*	1,430*
Brinell hardness	82-1001	105	150-220	402**

* Handbook of Chemistry 15

† Alpha fron ‡ Percent in 8 in. § Percent in 2 in. ¶ Hot-rolled rods or plates ** Quenched*

Digitized by Google

Table 2.9.48 — Composition and Physical Properties of Commercial Lead (Handbook of Chemistry 15 and Handbook of Chemistry and Physics 3)

Property	Value or description
Composition of commercial lead	99.8% Pb, 0.2% As
Appearance	Soft heavy metal, malleable and
	ductile. Color, gray
Density (20°C) gm/cc	11.34
Specific heat (0°-100°C), gm-cal/gm	0.0305
Thermal conductivity (18°C), cal/(sec)(cm)(°C)	0.0827
Thermal expansion coefficient (20°C), per °C	$29.1 \times 10^{-6}$
Tensile strength, lb/sq in.	1600
Yield strength, lb/sq in.	710
Ultimate strength, lb/sq in.	2000 - 3000
Melting point, °C	327.5
Brinell hardness	~4.2 (commercial); 2.9-3.0 (pure)

Table 2.9.49 — Composition of Various Types of Natural Rock*

		Composition, wt	-%
<b>M</b> aterial	Granite	Sandstone	Limestone
S ₁ O ₂	70	85	2
Al ₂ O ₃	14	17	0.2
Fe ₂ O ₃	2	2	.4
FeO	1		
MgO	1	•••	5.0
CaO	3	1	45
CaCO ₃			46
Na ₂ O	3.5	2.5	
K ₂ O	5	2	
H ₂ O plus organic	1.5	0.5	1.4

^{*} Natural rock varies in composition from locality to locality. The above values are averages derived from  $\bf Pirsson^8$ 

SHIELD MATERIALS CHAP. 2.9

Table 2.9.50 — Physical Properties of Various Types of Natural Rock*

Property	Granite	Sandstone	Limestone
Appearance	Evenly granular; color varying from white to dark gray, depend- ing on amount of feld- spar in it	Grains of quartz held together by ce- menting agent; yellow, red, or brown color most common	Fine-grained rock, varying from whitish color to yellow, brown, or gray
Average density, gm/cc	2.65	2.4	2.7
Density range, gm/cc	2.5 - 3.1	2.24 - 2.4	2.3-2.9
Mean specific heat, gm-cal/gm	0.195	0.22	0.217
Thermal conductivity, Btu/(hr)(ft)(°F)	1.0 - 2.32	1.1	0.3 - 0.75
Coefficient of thermal expansion, per °C	$8.3\times10^{-6}$	$7-12\times10^{-6}$	9 × 10 ⁻⁶
Crushing strength, lb/sq in.	15,000-40,000	1,500 – 15,000†	3,000-40,000†
Pore vol, % of total	0.15	5 - 30	0-15

^{*} Handbook of Chemistry and Physics, * Kent's Mechanical Engineers' Handbook, * Mechanial Engineers' Handbook, * and Pirsson*

Table 2.9.51 — Composition of Stainless Steel, Type-347* (High-chromium steel)

	Comp	osition
Material	Wt-%	Vol-%
Fe	68.35	66.06
Cr	18.0	19.29
Ni	10.5	8. <b>9</b> 6
Mn	2.00	2.13
Si	1.00	3.19
C	0.08	0.15
P	.04	.15
S	.03	.07

^{*} Handbook of Chemistry 15 and Handbook of Chemistry and Physics 9

[†] Great range owing to variations in the porosity of the rock

CHAP. 2.9 RADIATION SHIELDING

Table 2.9.52 - Physical Properties of Stainless Steel, Type-347*

Property	Value or description*
Density, gm/cc	7.8
Specific heat, gm-cal/gm	0.113
Thermal conductivity, cal/(sec)(cm)(°C)	.042
Thermal expansion coefficient, per °C	$17.3 \times 10^{-6}$
Elongation, %	40
Tensile strength, lb/sq in.	85,000
Yield strength, lb/sq in.	33,000
Ultimate strength, lb/sq in.	85,000
Melting point, °C	1430 - 1470
Brinell hardness	150

^{*} Handbook of Chemistry 15 and Handbook of Chemistry and Physics 9

### BORON-CONTAINING MATERIALS

It is convenient to group the boron-containing substances separately, not only because of their importance to shield design, but also to clearly demonstrate the diversified manner in which boron may be incorporated into a shield. Data on boral, an alloy of boron and aluminum, are given in Tables 2.9.53 and 2.9.54; data on boron-bearing concretes are given in Tables 2.9.19 through 2.9.24; and data on boron, boron oxide, and boron carbide will be found in Volume 3 of this Handbook.

### BORATION OF WATER

Capture gamma-ray production within water shields may be suppressed by the addition of small amounts of boron to the water, which is accomplished by virtue of the large thermal capture cross section of boron. The relatively soft gamma ray ( $\frac{1}{2}$  mev) subsequently emitted is more easily absorbed within the shield than the harder gammas which are characteristic of capture in most other materials (Table 2.1.7).

Table 2.9.55 lists the solubilities of several boron-containing substances in water and the present boron concentrations of saturated solutions.

### BORON COATINGS FOR METALS

Recent experiments by the ceramics group at Y-12 plant, Carbide & Carbon Chemical Company, Oak Ridge, Tennessee have indicated that it is possible to coat iron to a thickness of 0.020 in. with a boron-containing glass. The method, developed for small samples, is: The sample to be coated is first cleaned and sandblasted, and a boron glass (a chemical analog of silica glass with borates replacing silicates) is prepared and ground to size (150-200 mesh). The sample is then heated to a dull red heat far above the melting range of the glass (~800°C), and the ground boron glass is flame-sprayed onto the surface.

The final product has a smooth glaze-like appearance much like a porcelanized coating. The color ranges from black or chalk gray for very thin coatings (1 mil) to whitish gray



¹References appear at end of chapter.

SHIELD MATERIALS CHAP. 2.9

or yellowish for coatings 20 mils thick and over. The coating is very brittle and will chip off under bending or deformation of the metal.

So far no coatings above about 25 mils thickness have been successful. Thicker coatings tend to peel and crack. Not much work has been done in multiple layer coatings. It is White's opinion that multiple-layer coatings would not be successful but that it may be possible to prepare sandwich-type samples built up of alternate layers of metal and coating.

This type of coating has been tried only on iron and aluminum. The coating is not successful on aluminum but may possibly be made to work on copper and on stainless steel. The coating will not withstand temperatures above the melting range of the glass (600°C).

The glass used in the sample-coating was made from the following percentages of raw materials by weight:

H₃BO₃-42.83% Pb₃O₄-54.55% ZnO- 2.61%

An analysis of the finished glass had the following composition by weight:

 $B_2O_3 - 35\%$ PbO - 62.5% ZnO - 2.5%

The flame-spraying technique works best on small samples. For large samples, a different procedure is necessary to produce even coatings. A 5- by 5-ft slab of iron is now being coated for test in the ORNL Bulk Shielding Facility. The coating is put on in a furnace.



Table 2.9.53 — Composition of Boral*

(Kitzes and Hullings; 28 original boral composition reported by McKinney and Rockwell 29)

Component	Without Al cladding, wt-%	With Al cladding $\binom{1}{4}$ in. sheet), wt-%
	Molecular composition	
Aluminum (2S)	65.0	80.0
Boron carbide	35.0	20.0
	Elemental composition	
Aluminum (2S)	65.0	80.0
Boron	27.5	15.7
Carbon	7.5	4.5

* Boral, an engineering material for absorption of thermal neutrons, is a mixture of B4C and Al. The alloy is held in an aluminum cladding  $^{20}\!/_{1000}$  in. thick, without which the material is brittle and difficult to handle. The standard boral composition, supplied by Carbide and Carbon Chemicals Company, Y-12 Plant, Oak Ridge, Tenn., shown above is available in 1/4 and  $\frac{1}{16}$  in. thick sheets. The B₄C content in the alloy can be as high as 50%; impurities less than 1%; major impurity is iron

Table 2.9.54 — Physical Properties of Boral

roperty	value of description;
Appearance	Aluminum-like alloy; can be rolled, sheared, sawed, drilled, tapped, hot-formed, diecast, welded
Density, gm/cc	2.53
Specific heat, gm-cal/gm	0.175
Thermal conductivity, Btu/(hr)(ft)(°F)	25 at 200°F
	19 at 500°F
Elongation, %	0.4
Tensile strength,* lb/sq in.	5500
Shear strength,* lb/sq in.	8240
Heat generation from $(n,\alpha)$ reaction, watts/ $(ft^2)(nv)$	$7.4\times10^{-10}$
Cost (1953)‡	\$18 per sq ft for $\frac{1}{4}$ -inthick sheets;
	\$15 per sq ft for $\frac{1}{8}$ -inthick sheets;

^{*} The strength of the sheets of boral lies in the aluminum cladding and does not vary with the composition of the B₄C-Al alloy

Property

Digitized by Google

Value or descriptiont

[†] McKinney²⁸ and Kitzes and Hullings²⁹ ‡ Rinderer³⁰

Table 2.9.55 -- Solubility of Boron-containing Substances in Water at Various Temperatures (Handbook of Chemistry⁴⁵ and Handbook of Chemistry and Physics⁹⁾

												Boron concentration;	ration;
				Solubil	Solubility in water, $gm/100 \text{ ml H}_2O$	ter, gn	100 m	1 H20				wt-% in H2O	0,
Compound	ပ္	10°C	10°C 20°C	30°C 40°C 50°C 60°C 70°C 80°C 90°C 100°C	40°C	20°C	D.09	70°C	80°C	<b>0.06</b>	100°C	<b>0.</b> 0	100°C
NH.HB.O3H.O	10 tn cc	old wate	10 in cold water: soluble in hot water	le in ho	t water							1.7 in cold water	ı
HBO.*	2.66	3.57	5.04	6.60	6.60 8.72		14.81	11.54 14.81 18.62 23.75 30.38 40.25	23.75	30.38	40.25	0.45	2.0
B,0,†	1.1	1.5			4.0		6.2		9.5		15.7		4.2
(CH,),B;		Slight	Slightly soluble in water	le in wa	ter								
LiBO,	6.0				16 at 45°C	2.c						0.19	3.0
L4,B,O, 5H,O		Very	Very soluble										
KBFA		•	4.0								6.27		0.51
K-B-O	14.7			71	Very s	Very soluble in hot water	n hot wa	ıter				1.7	
K.B.O. 5H.O				26.7	40 at 3	5°C; ve	ry solub	40 at 35°C; very soluble in hot water	t water			2.8 at 30°C	
Ag BO.			9.05 at 25°C	t 25°C								0.59 at 25°C	
NaBF.			108 at	108 at 26.5°C							210		6.7
Na,B,O			56	36 at 35°C	2.C							3.4 at 20°C	
Na,B,O, 4H,O		Solubl	Soluble in cold water; very soluble in hot water	d water;	very sa	oluble in	hot wa	ter					
Na,B,O,	1.3				8.79							0.28	
Na.B.O.5H.O								24.4	31.5	41	52.5		5.1
Na, B, O, 10 B, O	1.3	1.6	2.7	3.9		10.5	20.3					0.30 at 20°C	
NaBO2 · 3H2O · H2O2 **		3.9 at	3.9 at 15°C; 5.7 at 32°C	.7 at 32	ပ္							0.26 at 15°C	

*Solubility in glycerin, 22.2 parts per hundred at 20°C; in ether, 0.25 parts per hundred at 25°C † Soluble in glycerin

Very soluble in alcohol and ether

TSlightly soluble in alcohol Soluble in alkalis

** Decomposes above 60°C

### REFERENCES

- 1. G. D. White, Y-12 Plant, private communication.
- 2. G. R. White, X-ray Attenuation Coefficients from 10 Kev to 100 Mev, Nat. Bur. Stand., NBS-1003, May 13, 1952, 93 pp.
- 3. M. K. Hullings, Gamma-ray Total Mass Absorption Coefficients, Oak Ridge Nat. Lab., ORNL-CF-53-2-266, Feb. 12, 1953, 5 pp.
- R. B. Gallaher and A. S. Kitzes, Summary Report on Portland Cement Concretes for Shielding, Oak Ridge Nat. Lab., ORNL-1414, Feb. 7, 1953, 30 pp.
- 5. G. A. Hool and N. C. Johnson, Concrete Engineers' Handbook, 1st ed., McGraw-Hill Book Co., Inc., New York, 1947.
- 6. T. Rockwell and F. J. Roehrenbeck, ORNL-17, Mar. 24, 1948, 24 pp.
- 7. Mechanical Engineers' Handbook, 5th ed., L. S. Marks, editor, McGraw-Hill Book Co., Inc., New York, 1950.
- 8. L. V. Pirsson, Rocks and Rock Minerals, 2nd ed., revised by A. Knopf, John Wiley and Sons, Inc., New York, 1926.
- 9. Handbook of Chemistry and Physics, 34th ed., C. D. Hodgman, editor, Chemical Rubber Publishing Co., Cleveland, Ohio, 1952.
- 10. General Engineering Handbook, 2nd ed., C. E. O'Rourke, editor, McGraw-Hill Book Co., Inc., New York, 1940.
- Kent's Mechanical Engineers' Handbook, Design and Production Volume, 12th ed., C. Carmichael, editor, John Wiley and Sons, Inc., New York, 1950.
- 12. T. Rockwell to E. P. Blizard, Memo Y-El-1 (classified).
- 13. ORNL-653 (classified).
- A. S. Kitzes, T. Rockwell, and R. B. Gallaher, Summaries of Studies on Oxychloride Cement and Concrete, ORNL-709, to be published.
- 15. Handbook of Chemistry, 7th ed., N. A. Lange, editor, Handbook Publishers, Sandusky, Ohio, 1949.
- 16. Chemical Engineers' Handbook, 2nd ed., J. H. Perry, editor, McGraw-Hill Book Co., Inc., New York, 1941.
- 17. Collier's Encyclopedia, C. P. Barry, editor, P. F. Collier and Son Corp., New York, 1950.
- 18. E. Hägglund, Chemistry of Wood, trans. by P. Oesper, Academic Press, New York, 1951.
- 19. Handbook of Engineering Fundamentals, 2nd ed., O. W. Eshbach, editor, John Wiley and Sons, Inc., New York, 1952.
- 20. G. S. Brady, Materials Handbook, 7th ed., McGraw-Hill Book Co., Inc., New York, 1951.
- 21. G. F. Quinn and L. B. Thompson, CE-1125, Dec. 9, 1943 (classified).
- 22. H. R. Simonds, A. J. Weith, and M. H. Bigelow, Handbook of Plastics, 2nd ed., D. Van Nostrand Co., Inc., New York, 1949.
- 23. Hanford Works Technical Manual, HW-10475, Sept. 15, 1951 (classified).
- C. D. Newman, R. O. Bolt, J. G. Carroll, G. A. Christiansen, B. A. Fries, J. W. Kent, and E. G. Lindstrom, NEPA-1381, April 18, 1950, 31 pp (classified),
- R. H. Kernohan and G. M. McCammon, Fading Characteristics of Gamma-induced Coloration in High-density Glass, Oak Ridge Nat. Lab., ORNL-975, Mar. 20, 1951, 19 pp.
- 26. Van Nostrand's Scientific Encyclopedia, 2nd ed., D. Van Nostrand Co., Inc., New York, 1947.
- 27. Metals Handbook, 1948 ed., T. Lyman, editor, The American Society for Metals, Cleveland, Ohio, 1948.
- A. S. Kitzes and W. O. Hullings, Boral: A New Thermal Neutron Shield, Supplement 1, Oak Ridge Nat. Lab., ORNL-981, July 3, 1951, 18 pp.
- 29. V. L. McKinney and T. Rockwell, III, ORNL-242, Aug. 31, 1949 (classified).
- 30. C. Rinderer, Y-12 Plant, Carbide and Carbon Chem. Corp., Oak Ridge, Tenn., private communication.

### Appendix 1

٤٦٠

دگ با درۍ ور دغاول

(I)

n á In ä Lital n a E ali

71 K

in é

. ***** *

Conversion Factors and Miscellaneous Data

### Table A.1.1 -- Constants

(CF-51-8-10)

```
(2.99776 \pm 0.00004) \times 10^{10} cm/sec = (9.8356 \pm 0.00013)
Velocity of light (C):
                                                        \times 10^8 ft/sec
"Absolute" zero (To):
                                                     -273.16 \pm 0.01°C = -459.69 \pm 0.02°F
Faraday constant (F):
                                                     96514.0 \pm 10 abs coulombs/phys. gm equiv.
                                                     (6.02283 \pm 0.0011) \times 10^{23} molecules/chem-mole
Avogadro's number (N_0):
                                                     1.000272 \pm 0.000005
Chemical/physical mass unit:
                                                     6.6242 \times 10^{-27} \text{ erg-sec} = 4.1349 \times 10^{-15} \text{ ev-sec}
Plank's constant (h):
                                                     4.8025 \times 10^{-10} abs esu = 1.60203 \times 10^{-20} abs emu
Charge of electron (e):
                                                        = 1.60203 \times 10^{-19} abs coulombs
                                                     2.4265 \times 10^{-10} cm
Compton wavelength (A<sub>0</sub>):
Fine structure constant \left(\frac{e^2}{hc} = a\right):
                                                     0.0072977 = \frac{1}{137.030}
                                                     1.38047 \times 10^{-16} \text{ erg/deg} = 3.2982 \times 10^{-24} \text{ cal/deg}
Boltzman constant (k):
                                                        = 8.6170 \times 10^{-5} \text{ ev/deg}
                                                     5.6728 \times 10^{-5} \text{ erg/(cm}^2) (\text{deg}^4) (\text{sec})
Stefan-Boltzmann constant (\sigma):
Bohr nuclear magneton \left(\frac{e\hbar}{2M_{p}c} = \mu_{II}\right)
                                                     5.049 \times 10^{-24} \text{ erg/gauss}
```

Table A.1.2 — Conversion Factors

Multiply	Ву	To obtain
	Energy	
Btu	$6.59 \times 10^{15}$	mev
Btu	1054.8	joules
Btu	$2.930 \times 10^{-4}$	kw-hr
Btu	$3.929 \times 10^{-4}$	hp-hr
Btu	252	gm-cal
cal (15°)	$2.6126 \times 10^{19}$	e▼
cal (15°)	$4.1855 \times 10^{7}$	ergs
cal (15°)	4.1855	joules
ergs	$6.2421 \times 10^{11}$	ev
ergs	10 ⁻⁷	joules
ergs	$2.3892 \times 10^{-8}$	cal (15°)
ev	$1.60203 \times 10^{-12}$	ergs
ev	$1.60203 \times 10^{-19}$	joules
ev	$3.8276 \times 10^{-20}$	cal (15°)
gm	$5.6095 \times 10^{32}$	ev
gm	$8.9866 \times 10^{20}$	ergs
gm	$8.9866 \times 10^{13}$	joules
gm	$2.1471 \times 10^{13}$	cal (15°)
gm-cal	$2.616 \times 10^{13}$	mev
gm-cal	4.186	joules
gm-cal	$1.163 \times 10^{-6}$	kw-hr
gm-cal	$1.559 \times 10^{-8}$	hp-hr
gm-cal	$3.969 \times 10^{-3}$	Btu
hp-hr	$1.677 \times 10^{19}$	mev
hp-hr	$2.684 \times 10^6$	joules
hp-hr	0.7457	kw-hr
hp-hr	$6.413 \times 10^{5}$	gm-cal

### APPENDIX 1

Table A.1.2— (Continued)

Multiply	Ву	To obtain
	Energy	
hp-hr	2545	Btu
joules	$6.25 \times 10^{12}$	mev
joules	$2.778 \times 10^{-7}$	kw-hr
joules	$3.722 \times 10^{-7}$	hp-hr
joules	0.2389	gm-cal
joules	$9.480 \times 10^{-4}$	Btu
joules	$6.2421 \times 10^{18}$	ev
joules	$1 \times 10^7$	ergs
joules	0.23892	cal (15°)
kw-hr	$2.25 \times 10^{19}$	mev
kw-hr	$3.6 \times 10^{6}$	joules
kw-hr	1.341	hp-hr
kw-hr	$8.60 \times 10^{5}$	gm-cal
kw-hr	$3.413 \times 10^{3}$	Btu
mev	$1.6 \times 10^{-13}$	joules
mev	$4.44 \times 10^{-20}$	kw-hr
mev	$5.95 \times 10^{-20}$	hp-hr
mev	$3.82 \times 10^{-14}$	gm-cal
mev	$1.517 \times 10^{-16}$	Btu
	Time	
days	$2.738 \times 10^{-3}$	yr
days	24	hr
days	1440	min
days	$8.640 \times 10^4$	sec
hr	$1.141 \times 10^{-4}$	yr
hr	0.04167	days
hr	60	min
hr	3600	sec
min	$1.901 \times 10^{-6}$	yr
min	$6.944 \times 10^{-4}$	d <b>a</b> ys
min	$1.667 \times 10^{-2}$	hr
min	60	sec
sec	$3.169 \times 10^{-8}$	yr
sec	$1.157 \times 10^{-5}$	days
sec	$2.778 \times 10^{-4}$	hr
sec	$1.667 \times 10^{-2}$	min
yr	365.26	days
yr	8766	hr
yr 	$5.260 \times 10^5$	min
yr	$3.156\times10^7$	sec
	Length	
cm	0.01	m
cm	.3937	in.
cm	.03281	ft
ft	.3048	m
ft	30.48	cm
ft	12	in.
in.	0.0254	m
in.	2.54	cm
in.	0.0833	ft

### **PHYSICS**

### Table A.1.2—(Continued)

Multiply	Ву	To obtain
	Length	
meters	100	cm
meters	39.37	in.
meters	3.281	ft.
microns	10-6	meters
microns	10-4	cm
microns	$3.937 \times 10^{-5}$	in.
microns	$3.281 \times 10^{-6}$	ft
mici ons	3.201 × 10	**
	Volume	
cu cm	10-6	m³
cu cm	$6.102 \times 10^{-2}$	in. ³
cu cm	$2.642 \times 10^{-4}$	gal
cu cm	$3.531 \times 10^{-5}$	ft ³
cu cm	$1.308 \times 10^{-6}$	yd ³
cu ft	$2.832 \times 10^{-2}$	m³
cu ft	$2.832 \times 10^4$	cm ³
cu ft	1728	in. ³
cu ft	28.32	liters
cu ft	$3.704 \times 10^{-2}$	yd ³
cu ft	7.481	gal
cu in.	$1.639 \times 10^{-6}$	m³
cu in.	16.39	cm ³
cu in.	$5.787 \times 10^{-4}$	ft ³
cu meter	1 × 10 ⁶	cm³
cu meter	$6.102 \times 10^4$	in. ³
cu yd	$7.646 \times 10^{5}$	cm ³
cu yd	27	ft ³
cu yd	764.6	liters
cu yd	202	gal
gal	3785	cm³
gal	0.1337	ft ³
gal	3.785	liters
gal	$4.951 \times 10^{-3}$	yd ³
liters	1000	cm ³
liters	$3.531 \times 10^{-2}$	ft ³
liters	$1.308 \times 10^{-3}$	yd³
liters	0.2642	gal
		ŭ
	Angular displacement	
deg	$1.745 \times 10^{-2}$	rad
deg	$2.778 \times 10^{-3}$	LGA
rad	57.3	deg
rad	0.1592	rev
rev	360	deg
rev	6.283	rad
	Pressure	
atm	76	cm Hg
atm	1033	gm/cm²
	•	G,

### APPENDIX 1

Table A.1.2—(Continued)

<b>M</b> ultiply	Ву	To obtain
	Pressure	
atm	2177	lb/ft²
atm	14.70	lb/in. ²
cm Hg	$1.316 \times 10^{-2}$	atm
cm Hg	13.6	gm/cm²
cm Hg	27.85	lb/ft ²
cm Hg	0.1934	lb/in.²
gm/cm ²	$9.678 \times 10^{-4}$	atm
gm/cm ²	$7.356 \times 10^{-2}$	cm Hg
gm/cm ²	2.048	lb/ft ²
gm/cm²	$1.422 \times 10^{-2}$	lb/in.²
lb/ft²	$4.725 \times 10^{-4}$	atm
lb/ft²	$3.591 \times 10^{-2}$	cm Hg
lb/ft²	0.4882	gm /cm²
lb/ft²	$6.944 \times 10^{-3}$	lb/in. ²
lb/in. ²	$6.804 \times 10^{-2}$	atm
lb/in. ²	5.171	cm Hg
lb/in. ²	70.3	gm/cm ²
lb/in. ²	144	lb/ft²
	Density	
gm/cm ³	$1 \times 10^{3}$	gm/liter
gm/cm ³	62.43	lb/ft ³
gm/liter	$1 \times 10^{-3}$	gm/cm ³
gm/liter	$6.243 \times 10^{-2}$	lb/ft ³
lb/ft ³	$1.602 \times 10^{-2}$	gm/cm ³
lb/ft ³	16.02	gm/liter
	Thermal conductivity	
Btu/(hr)(*F)(ft)	$4.134 \times 10^{-3}$	gm-cal/(sec)(°C)(cm)
Btu/(hr)(°F)(ft)	12	Btu/(hr)(°F)(ft²/in.)
Btu/(hr)( $^{\circ}$ F)(ft ² /in.)	$3.44 \times 10^{-4}$	gm-cal/(sec)(°C)(cm)
Btu/ $(hr)(^{\circ}F)(ft^{2}/in.)$	$8.33 \times 10^{-2}$	Btu/(hr)(*F)(ft)
$gm-cal/(sec)(^{\circ}C)(cm)$	241.9	Btu/(hr)(°F)(ft)
$gm-cal/(sec)(^{\circ}C)(cm)$	2903	Btu/ $(hr)(^{\circ}F)(ft^{2}/in.)$
B (2.25), 2/(0.11)		,

Table A.1.3 — Radiation Dose Units

Radiation	Roentgen	Energy absorbed, roentgen equivalent physical (rep)	Biological damage, roentgen equiva- lent man (rem)	Relative biological effectiveness (rbe)
X-ray	1	1	1	•••
Gamma	1	1	1	1
Beta	•••	1	1	1
Thermal-neutron	•••	1	5	5
Fast-neutron		1	10	10
Proton	•••	1	10	10
Alpha-particle	• • •	1	20	20

Table A.1.4—Gamma Energy Flux to Dose Rate

Gan	nma energy, mev	To produce 1 r/hr, $10^5 \text{ mev/(cm}^2)(\text{sec})$	To produce 0.3 r/40-hr wk, $10^3$ mev/(cm ² )(sec)
	0.5	5	3.75
	1	5.5	4.125
	2	6	4.5
	5	8	6.0
	10	10	7.5
			•

Table A.1.5 - Neutron Flux to Dose Rate

(W. S. Snyder and J. Neufeld, Maximum Permissible Neutron Flux for Fast and Thermal Neutrons, Symposium on the Biophysical and Biological Effects of Neutrons, Mar. 17-18, 1952)

Neutron energy	To produce 1 rem/hr, $10^3 \text{ r/(cm}^2)(\text{sec})$	To produce 0.3 rem/40 hr, r/(cm²)(sec)
Thermal	240	1800
5 kev	220	1650
0.5 mev	11	82.5
2.5 mev	5.2	39
5.0 mev	3.2	24
10 mev	3.33	25

Table A.1.6 — Neutron Wavelengths for Various Energies

Energy	KT ₂₀ •	1 e <b>v</b>	1 mev
Neutron, * Å Photon, † Å	$0.28635 \times 10^{-8} \\ 0.0049068$	$0.045512 \times 10^{-8}$ $12.395 \times 10^{-8}$	$4.5501 \times 10^{-13}$ $0.012395 \times 10^{-8}$
*Entries are †Entries are	$\frac{\lambda}{\lambda} = \frac{\lambda}{2\pi} = \frac{\hbar}{p}$		

Table A.1.7 - Neutron Energy, Wavelength, Velocity, and Time of Flight*

( $\lambda = 2\pi\lambda = \text{wavelength}$ , Å (10⁻⁸ cm); E = energy, ev; v = velocity, cm/sec; t = time of flight,  $\mu \text{sec/m}$ )

λ =	6.2832X	0.28696/√E	$3.9554 \times 10^5/v$	0.0039554t
$\lambda = 0.159155 - \lambda$	• • •	$0.045512/\sqrt{E}$	62,452/v	0.00062952t
$\mathbf{E} = 0.081774 \lambda^2$	0.0020714/X ²	• • •	$5.2269 \times 10^{-13} v^2$	5226.9/t ²
$\mathbf{v} = 3.9554 \times 10^5/\lambda$	62,952/X	$1.3832 \times 10^6 \sqrt{E}$		10 ⁸ /t
$t = 252.82\lambda$	1588.5 + λ	72.297/√Ē	10 ⁸ /v	

^{*}This table is valid to  $1\frac{1}{2}$  percent for E < 10 mev

Table A.1.8 — Low-energy Neutrons

Energy, ev	Wavelength, Å	Velocity, cm/sec
0.001	9.0430	$4.3740 \times 10^4$
.01	2.8596	$1.3832 \times 10^{5}$
.02	2.0221	$1.9561 \times 10^5$
.0259*	1.7786	$2.2239 \times 10^{5}$
.03	1.6510	$2.3957 \times 10^{5}$
.04	1.4298	$2.7664 \times 10^{5}$
.05	1.2789	$3.0929 \times 10^{5}$
.06	1.1674	$3.3881 \times 10^5$
.07	1.0808	$3.6596 \times 10^{5}$
.08	1.0110	$3.9122 \times 10^{5}$
.09	0.95321	$4.1495 \times 10^{5}$
.1	.90430	$4.3740 \times 10^{5}$
.2	.63944	$6.1858 \times 10^{5}$
.4	.45215 —	$8.7480 \times 10^5$
.6	.36918	$1.0714 \times 10^{6}$
.8	.31972	$1.2372 \times 10^{6}$
1	.28596	$1.3832 \times 10^6$

^{*0.025851} ev = kT_{300*K}

### Table A.1.9 - Miscellaneous Factors and Definitions

- (1) 1 atomic mass unit (amu) =  $1.65990 \times 10^{-24}$  gm = 931.12 meV
- (2) 1 barn = nuclear unit of cross section =  $10^{-24}$  cm
- (3) 1 curie =  $3.68 \times 10^{10}$  disintegrations/sec
- (4) 1 rutherford =  $1.00 \times 10^6$  disintegrations/sec
- (5) Width of level having lifetime of 1 sec =  $4.1349 \times 10^{-15}$  ev
- (6) Lifetime of state with width of 1 ev =  $4.1349 \times 10^{-15}$  sec
- (7)  $kT_{0^{\circ}C} = 0.02354$  ev;  $kT_{15^{\circ}C} = 0.02483$  ev;  $kT_{20^{\circ}C} = 0.02526$  ev;  $kT_{300^{\circ}K} = 0.02585$  ev
- (8) Relaxation length ( $\tau$ ) is the thickness of absorber which will reduce the radiation intensity to 1/e times its initial value
  - $2.3\tau$  = distance to reduce radiation to 0.1 times its initial value

 $\tau$ cm to fall to 1/e  $I_0 = >0.906 \tau$  in. to fall to 0.10  $I_0$ 

- (9) In a reactor operating at a power level of P watts,  $P \times 3.1 \times 10^{10}$  fissions/sec occur
- (10) Conversion Factors for Gamma-ray Cross Section

 $\sigma_T$  = microscopic cross section in Thompson units per electron

 $\sigma_b$  = microscopic cross section in barns (10⁻²⁴ cm²)

 $\mu$  = linear absorption coefficient in cm⁻¹

 $\mu_m$  = mass absorption coefficient in cm²/gm

ro = classical electron radius

1 Thompson unit =  $0.665 b = \frac{8}{3} \pi r_0^2 cm^2$ 

In a medium of Z electrons/molecule and molecular weight A:

$$\sigma_b = 0.665 \ \mathbf{Z}\sigma_t$$

$$\mu_{\rm m} = \frac{0.6023}{{
m A}} \ \sigma_{
m b} = \frac{0.6023{
m Z}}{{
m A}} \times 0.665 \ \sigma_{
m t}$$

$$\mu = \rho_{\mu_m} = \frac{0.6023\rho}{A} \sigma_b = \rho_{el} \frac{\sigma_b}{Z} \times 10^{-24}$$

where:  $\rho$  = mass density in gm/cm³

 $\rho_{\rm el}$  = electron density per cm³

 $1 \text{ gm/cm}^2 = 0.4882 \text{ lb/ft}^2$ 

### Appendix 2

Reactor Summary Tables (North American Aviation, Inc.)

### Table A.2.1 — Chicago Pile No. 1 (CP-1)

	296 c cm ²
RESPONSIBLE ORGANIZATION  Design Metallurgical Laboratory, University of Chicago Construction Metallurgical Laboratory, University of Chicago Operation Metallurgical Laboratory, University of Chicago	Age (clean and cold) a
PURPOSE	Prompt neutron lifetime About 1 x 10 2 acc  ko (clean and cold) 1.055 (average) 1.032 b 1.032 b 1.032 b
Moderator	1.07d   1.07d   k (temperature)
Fo Equator	Thermal  EXPERIMENTAL FACILITIES. 1 - 4 1/8 x 4 1/8 in. removable stringer  7 - foil alots  CAPITAL INVESTMENT  ** Section of a Divergent Chain Reaction  E. Fermi. AECD-3369, 47 pp. January 4, 1952.
Consumption Average cycle time Cooling System None Auxillarry racintaries Oover density (average) Maximum density (average) Maximum moderator temperature CONTROLS Maximum moderator temperature Negligible rise Auxillarry racintaries Auxillarry racintaries Auxillarry racintaries Auxillarry (average) Auxilla	a. Estimated 5. Uranium oxide in Speer graphite c. Uranium metal in AGOT graphite d. Uranium metal in AGOT graphite

## Table A.2.2—Chicago Pile No. 2 (CP-2)

LOCATION Argonne National Laboratory Chicago, Illinois	JIG
RESPONSIBLE ORGANIZATIONS  Design Metallurgical Laboratory, University of Chicago Construction Metallurgical Laboratory, University of Chicago Operation Metallurgical Laboratory,	A A
Natural uran	P. P.
d material	N NECTOR OF STATE OF
Core  Core  Sheld  Coveration  Sheld  Over-all  Fissionable material  Consumption  Burn-up  Cooling System  Cooling System  In thick  Step ordinary concrete on sides  6 in. lead plus 40 in. wood on top  Over-all  STRATEGIC MATERIAL  Fissionable material  Consumption  Burn-up  Indefinite  Cooling System  Indefinite  None	EXPER
phere Ventilatin if TIONS 10 kw (  r utput App (average) 6.4 x 1 (average) 7.6 x 10-2 maperature About 1 nator temperature About 1	6 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
CONTROLS Shim . 1 horizontal, steel supported, cadmium strip Segulating . 2 horizontal, strip supported, cadmium strips Regulating . 3 horizontal, steel supported, cadmium strips Safety 3 horizontal, steel supported, cadmium strips Reactivity Change	

Diffusion length squared (clean and cold) 342 b cm ² 296 c cm ² 390 c cm ² 330 d cm ² Age (clean and cold) ⁸
Prompt neutron lifetime
1,032 b 1,032 b 1,039 c 1,039 c 1,070
8 k (poisons) 8 k (pressure) 8 k (pressure) NEUTRON FLUX DENSITY
Fast 4.5 x 10 ⁵ n/(cm ² )(sec)(watt)  **Expressize to the second se
horizontal core  5 x 5 ft thermal column  9 - 4 1/4 x 4 1/4 in, removable stringers
1 - 2 5/8 in. x 15 ft long vertical slot Narious monitoring slots REFERENCES Experimental Production of a Divergent Chain Reaction E. Fermi, AECD-3269, 47 pp, January 4, 1952
A Brief General Description of the Argonne Uranium- Graphite Pile (CP-2), H.E. Metcalf, CP-2459, 11 pp, Secret, Dec. 20, 1944

ntimated
anium oxide in Speer graphite
anium oxide in AGOT graphite
anium metal in AGOT graphite

# Table A.2.3 - ORNL Graphite Reactor (X-10)

LOCATION Oak Ridge National Laboratory Oak Ridge, Tennessee RESPONSIBLE ORCANIZATIONS	Coolant pressure drop through reactor 19.25 in. of H ₂ O Pumping rate 7,200 lb/min
•	Pumping power required
Operation	Shim 4 - 1 3/4 x 1 3/4 in. x 19 ft horizontal boron-steel rods
	Regulator 1 3/4 x 1 3/4 in. x 17 it normal boton size i tous Safety 4 - 1 1/2 in. dia. x 8 ft vertical boron-size i rods
MATERIALS Natural pranjum: 47.63 metric tons (tvoical)	for 3/8 in. boron-steel shot
Fuel cladding Aluminum; 0.035 in. wall, 0.060 in. end cap	nge (late 1944 loading)
Moderator (and reflector) Graphite; 612.5 metric tons	FUEL HANDLING
Coolant Varied	Charging Sluge drop into canal
Structural material	PHYSICS
Reactor atmosphere Air	Cell radius
Shield Ordinary and barytes-haydite concrete, plus waterproofing pitch	Thermal utilization (clean and cold)
PE 1.1 in. dia. re	Diffusion length squared (clean and cold)
DIMENSIONS  24 ~ 24 ~ 24 1/3 (* (including reflector)	Age (clean and cold); axial
Reflector Depends upon loading	Buckling (clean and cold) (experimental) 92 x 10-6 cm-2
	Prompt neutron lifetime About 1 x 10-3 sec
(waterproofed with pitch), 5 it of barytes-	kg (clean and cold)
	& (temperature)(graphite plus fuel)2.86 x 10-5/C.
TERIAL	8 k (poisons)(typical)
	k cc (hot and poisoned)(twoical)
Burn-up	NEUTRON FLUX DENSITY
:	Thermal: maximum
:	average
Coolant treatment	EAFERIMENTAL PACILITES 20 x 24 in. x 24 it removable axial core
drives fan (stand-by)	6 - 2 3/4 x 3/8 in. x 11 ft foil alots
2 - 3300 lb/min	4 - 1,684 in. dia. x 24 ft axial experimental holes 1 - 3 1/8 x 2 15/32 in. x 24 ft axial doughnut hole
OPERATING CONDITIONS (typical)	10 - 4 x 4 in. x 24 ft experimental holes
•	2 - 14 1/2 x 14 in. animal tunnels in top shield
: : :	entor transfer and northernsen - o
De la source	1 - 5 x 5 ft thermal column
	1 - drainable water filled core plug
3300 BTU/(e	to accommodate additional thermal
: :	Column of bulk meterial testing tank REFERENCES Graphite Uranium Production Piles. AEC Technical
Specific power: maximum	•
•	457 pp, Secret, 1951
	An Experimental and Theoretical Study
Maximum anderstor temperature	of the Subcritical BNL Reactor,
Coolent inlet temperature	J. Cherrick. et al. BNL-60, 109 no
•	Secret, June 15, 1950
Coolant velocity	a. Estimated

# Table A.2.4 — Brookhaven Graphite Research Reactor (BGRR)

	Regulator  Regulator  Regulator  Regulator  Shim and safety  Shim and safe
1	Thermal (maximum).  Thermal (maximum).  1. 12 x 12 in, x 25 it removable axial core 1. 2 channel, 25 it sample conveyor system 1. 12 x 12 in, x 25 it pneumatic tubes 1. 20 x 20 it section of removable shield blocks on top of reactor 30 - intercell 12 1/2 if the channels 2. openings into central gap 2. exposure tunnels under the reactor 20 channels 2. openings into central gap 2. exposure tunnels under the reactor 2. Stocknown Nuclear Reactor 3. Stocknown Nuclear Reactor 3. Stocknown Nuclear Reactor 3. The Brookhaven Nuclear Reactor 3. Theory and Nuclear Doratory, 5ML-18. 180 pp, Secret, June 22, 1948  Theory and Nuclear Doratory, 1952  Roppian and J. Chernick, BNL-152  Roppian and J. Chernick, BNL-152  Roppian and J. Chernick, BNL-155

### Table A.2.5 — Materials Testing Reactor (MTR)

LOCATION National Reactor Testing Station	Heat flux (average)
: :	Specific power (average) 10,000 kw/kg 25
	Maximum moderator temperature
	Coolant inlet temperature
Construction	Coolant outlet temperature
	Coolant velocity
	Coolant infet pressure
STATUS In operation since April, 1952	Coolant pressure drop through reactor
MATERIALS	Dumping rate
	· · · · · · · · · · · · · · · · · · ·
•	Shim Shim
	tode element rode
	4 - combination aluminum-cadmium box
Coolant	and beryllium rode
:	Regulator 2 - 1 1/2 in. dia. alumir re-cadmium tubing
. Alu	Safety
	Reactivity change
LATTICE TYPE	FUEL HANDLING  Demote grannling devices from to of tents
	Discharging Remote orapolino devices from top of tank. Spent
Reflector Beryllium: extends from core to 54 1/4 in. dia. cylinder	fuel lowered through discharge chute to canal
Graphite; pebble zone out to 7 1/3 ft sq x 9 ft high	beneath reactor
blocks out to 12 x 14 x 9 1/4 ft high	PHYSICS &
Shield 8 in. iron; 9 ft barytes concrete;	Resonance escape (clean and cold) 1.0
or 17 1/2 ft of H2O plus top plug	Thermal utilization (clean and cold) 0.76
Over-all	Diffusion length squared (clean and cold)
TRATEGIC MATERIAL	Age (clean and cold)
:	December neutron lifetime
Burn-up	km (clean and cold)
•	keff (clean and cold).
COOLING SYSTEM	Conversion ratio
Type Recirculated H2O	NEUTRON FLUX DENSITIES
Coolant source	Fast (maximum) 1.2 x 1014 n/(cm²)(sec)
Coolant treatment	Epithermal (maximum) 6 x 10 ¹² n/(cm ² )(sec)
rumbs	Intermal (maximum)
3 (1 atandhu) - 1000 lh/min 250 hn alactrically	CADITAL INVESTMENT
driven nositive displacement blowers	REFERENCES Materials Testing Reactor Project
Safety 2 - 850 gpm. electrically driven, centrifugal pumps	Handbook, Oak Ridge National
1 - 1000 gpm, gasoline driven, centrifugal pump	Laboratory, J.H. Buck and C.F. Leyse,
1 - 400 lb/min, electrically driven, blower	ORNL-963, 584 pp, Secret,
1 - 400 lb/min, gasoline driven, blower	May 7, 1951
1 - 150,000 gal, 170 ft head, working reservoir 1 - 150,000 gal. 150 ft head storage tank	a. Preliminary calculations
AUXILIARY FACILITIES Standby equipment 750 kva Diesel-electric generator	
SNS	
Total heat power 30,000 kw	

!

### APPENDIX 2

# Table A. 2.6 — Low-intensity Training Reactor (LITR)

Shim	Thermal utilization (clean and cold)  Thermal utilization (clean and cold)  Diffusion length squared (clean and cold)  Age (clean and cold)  Buckling (clean and cold)  Frompt neutron lifetime  kon (clean and cold)  NEUTRON FLUX DENSITIES  Fast (maximum)  Thermal (maximum)  Thermal maximum (in lattice)  Thermal maximum (in reflector)  EXPERIMENTAL FACILITIES. 2 - 3/4 in. ID pneumatic rabbit systems  CAPITAL INVESTMENT  ORK Ridge National Laboratory, W.R. Call and D.J. Mallon, ORNL-701, 138 pp. Secret  D.J. Mallon, ORNL-701, 138 pp. Secret  Oak Ridge National Laboratory, J.H. Buck  B. Freliminary calculations	
LOCATION  RESPONSIBLE ORGANIZATIONS  Design  Conk Ridge National Laboratory Construction  Ouk Ridge National Laboratory Operation  PURPOSE  STATUS  MATERIALS  Fuel  Moderator  Moderator  Out Ridge National Laboratory  Out Ridge National Laboratory  Construction  Out Ridge National Laboratory  Out Ridge National Laboratory  Experimental and research  STATUS  In operation since Feb., 1950  Moderator  Moderator  Moderator	rial Concr lial crial Concr inc inc driverses crial driverses concrete conc	Pumping rate

Digitized by  $Goog^{767}$ 

Table A. 2.7 — Bulk Shielding Reactor (BSR)

Oak Ridge National	CONTROLS
RESPONSIBLE ORGANIZATIONS Oak Ridge, Tennessee Design Oak Ridge National Laboratory	Saim
	Safety All rode
	Reactivity change
· · · · · · · · · · · · · · · · · · ·	FUEL HANDLING
STATUS	Charging Long handled grappling device
MATERIALS  Fig. 17235 se creatium ellow	Discharging Long handled grappling device:
• • • • • • • • • • • • • • • • • • • •	bHARICS
Moderator	Resonance escape (clean and cold) 1.0
Reflector Beryllium oxide and/or H2O	Thermal utilization (clean and cold) 0.76
• • • • • • • •	Diffusion length squared (clean and cold) 3.5 cm ²
:	Age (clean and cold) 64.2 cm ²
Lair	Buckling (clean and cold) 0.01 cm ⁻²
Shield	Prompt neutron lifetime
LATTICE TYPE	ko (clean and cold)
	Keff (clean and cold) 1.003
	Øk (temperature)
Reflector Depends upon loading	Øk (poisons)
	keff (hot and poisoned)
Over-all (pool)	NEUTRON FLUX DENSITIES
	Fast (average)
:	Epithermal (average) 3 x 10 ¹¹ n/(cm²)(sec)
Consumption	Thermal: maximum 2 x 10,2 n/(cm²)(qec)
:	average 1 x 10 ¹² n/(cm ² )(sec)
Average cycle time Indefinite	EXPERIMENTAL FACILITIES 40 x 20 x 20 ft pool
	CAPITAL INVESTMENT \$217,000
:	REFERENCES The New Bulk Shielding Facility
Contain source	at Oak Kidge National Laboratory,
•	W. W. Breezeste OBNI. 001 54 m
:	Secret May 3 1951
:	
:	a. Freiminary calculations
:	
•	
Median (nel temperative	
Maximum sheath temperature	
Maximum moderator temperature	
Pumping power required	_

## Table A.2.8 — Argonne Heavy Water Reactor (CP-3')

LOCATION Argonne National Laboratory, Chicago, Illinois preponeral r obcanizations	Maximum fuel temperature About 120' F
Design	
	- Pal
STATUS In operation from June 1944 to Jan. 1950 with natural uranium	Coolem veroity
s CP-3. Began operation	
	:
U ²³⁵ ;	power required
:	CONTROLS
	Shim 4 1/8 x 2 1/2 x 61 in., aluminum-jacketed
	Deciletor 1 - 7/8 in OD v 45 in aluminum-ischeted cadmium
•	vertical rod
:	Safety 2 - 4 1/8 x 2 1/2 x 64 3/4 in. aluminum-jacketed
:	cadmium, signal-arm-type rods
:	2 - 1 1/4 in. OD x 36 in. aluminum-jacketed
:	cadmium, vertica
	Reactivity change
XPE 0.850 i	Charging Manually charged initially
	Discharging Spent rods withdrawn into a lead coffin
:	PHYSICS
2 ft thick on s	Cell radius 4.35 cm
lead and 8	Resonance escape (clean and cold) 1.0
4 ft of laminated steel and masonite on top	Thermal utilization (clean and cold) 0.8
	Diffusion length squared (clean and cold)
Over A minute by 14 It high	Age (clean and cold)
	Duckling (clean and cold)
Consumption	k (clean and cold)
	keff (clean and cold) About 1,016
time	S k (temperature)
	8 k (poisons)(equilibrium xenon) About -0.005
:	keff (hot and poisoned) About 1.006
Coolant treatment Filtering	Conversion ratio
Kecompination	NEUTRON FLUX DENSITIES
ton exchange purification	Thermal maximum 3.4 x 1012 n/(cm2)(eec)
Pumps 1 - canned rotor sealed electrically driven 200 opm	average 1.7 x 1012 n/(cm2/eec)
	EXPERIMENTAL FACILITIES 4 - off-axis, 1 3/8 in. ID vertical
1 - standby, sealed,	thimbles in reactor tank
	1 - axial, 1 3/4 in. ID vertical thimble in reactor tank
Reactor atmosphere Helium, recirculated	/ - horizontal, 3 7/8 in. to 10 13/10 in. square test holes
OF EACH INC. CONDITIONS	A - Moisones, 1717, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718, 1718
Useful power output	1 - horizontal 5 x 5 ft thermal column with beam hole
	CAPITAL INVESTMENT
	긺
Heat flux: maximum 13,300 BTU/(sq ft)(hr)	on the Proposed CP-3' Reactor, Argonne
	96 pp, Secret, June 15, 1950
	a. To be replaced by CP-5 in late 1953
Specific power: maximum	

### Table A. 2.9 - Argonne Research Reactor (CP-5)

Construction Argone National Laboratory Controlled Laboratory Cont	Argonne National Laboratory	
Argonne National Laboratory Argonne National Laboratory Argonne National Laboratory ed to replace CP-3' late in 1953  235 as uranium-alumium alloy 2, 2 0 .122 in. side plates and sates, about 2, 4 x 3 in. over-all capplite; 29.5 metric tons Craphite; 29.5 metric tons Craphite; 29.5 metric tons Craphite; 29.5 metric tons Craphite; 29.5 metric tons Helium monite-iron-aggregate concrete fit across flate by 13 ft 6 1/2 in. 2 to 2 1/2 ft of D2O  m) 3 to 0 1/2 ft of D2O  Helium monite-iron-aggregate concrete ft across flate by 13 ft 6 1/2 in.  Continuous)  Recombination standby), 1000 gpm, mechanical cally driven, centrifugal pumps  Helium, recirculated  Recombination standby), 1000 gpm, mechanical cally driven, centrifugal pumps  Helium, recirculated  About 80 kw 117°F  117°F  117°F  About 5 psi		
Argonne National Laboratory ed to replace CP-3' late in 1953  (235 as uranium-alumium alloy ei, 2 - 0.122 in. side plates and lates, about 2.4 x 3 in. over-all lates, about 2.4 x 3 in. over-all CD20; 2 to 2.1/2 ft thick Craphite; 29.5 metric tons Craphite; 29.5 metric tons ei.8 moniterion-aggregate concrete llements in 6 in. equare array b  102 2 to 2.1/2 ft of D20  m) 2 2 to 2.1/2 ft of D20  m) 2 2 to 3.1/2 ft of D20  m) 2 2 to 2.1/2 ft of D20  m) 2 2 to 3.1/2 ft of D20  m) 2 2 to 3.1/2 ft of D20  m) 2 2 to 2.1/2 ft of D20  m) 3 4 to 0 graphite  Recombination standby), 1000 gpm, mechanical cally driven, centrifugal pumps  Helium, recirculated  Recombination 34,000 gpm, mechanical cally driven, centrifugal pumps  Helium, recirculated  34,000 gpm, mechanical  117° F  117° F  5.4 ft sec	tone or the country of the country o	30 hp secondary
ed to replace CP-3' late in 1953  (235 as uranium-aluminum alloy  124 2 0. 122 in. side plates and  125 as uranium-aluminum alloy  127 2 0. 122 in. on over-all  128 2 1/2 ft thick  129 2 1/2 ft thick  120 2 1/2 ft of D2O	. Argonne National Laboratory	
1235 as uranium-alumium alloy  12 0 122 in. side plates and  12 2 0 2 1/2 ft thick  12 2 0 2 1/2 ft thick  13 2 0 2 1/2 ft thick  14 12 10 2 10 2 1/2 ft of D20  15 10 2 10 2 1/2 ft of D20  16 2 10 2 1/2 ft of D20  17 2 10 2 1/2 ft of D20  18 2 10 2 10 2 1/2 ft of D20  19 2 10 2 1/2 ft of D20  10 2 1/2 in. of beavy concrete  11 2 10 0 gpm, mechanical  12 11 15 kg  13 10 0 gpm, mechanical  13 10 0 gpm, mechanical  14 10 10 10 gpm, mechanical  15 10 10 10 gpm, mechanical  16 10 10 10 10 10 10 10 10 10 10 10 10 10	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
Alumnum  Alumnum  2, 2 0 . 122 in. side plates and  ates, about 2, 4 x 3 in. over-all  D20  D20; 2 to 2 1/2 thick  Caphite; 29.5 metric tons  Caphite; 29.5 metric tons  None  Alumnum and steel  On 5 8 metric tons  I for a D20  T ft dis. x 2 ft  T co 2 1/2 ft of D20  T co 2 1/2 f	ed to replace Cr-3, take in 1933	1 - 1 1/2 in. Of
e, 2 - 0.122 in. side plates and sites, about 2. 4 x 3 in. over-all D2O; 2 to 2.1/2 ft thick Graphite; 29.5 metric tons b. 0.20 in. D2O in. D2	11235	
intes, 2 - 0.122 in. side plates and lates, about 2. 4 x 3 in. over-all lates, about 2. 1/2 it thick lates, and a lates, and	An aramam-aramammum aramammum aramam	in the state of th
ates, about 2. 4 x 3 in. over-all D2O    D2O  2. 20 2 1/2 it blick tons    Graphite; 29. 5 metric tons    Graphite; 29. 5 metric tons    Sea metric tons    Aluminum and steel    Be metric tons    Aluminum and steel    Al	The state of the s	of Ord So classical design of Ord
Craphte; 29.5 metric tons  D2O; 2 to 2 1/2 ft thick  Craphte; 29.5 metric tons  6.8 metric tons  None  Aluminum and steel  monite-iron-aggregate concrete elements in 6 in. equare array b  2 to 2 1/2 ft of D2O  m). 2 to 2 1/2 ft of D2O  m). 2 to 2 1/2 ft of D2O  m). 2 to 6 graphite  4 ft 8 1/2 in. of heavy concrete ft across flats by 13 ft 6 1/2 in.  D2O, recirculated  Recombination standby), 1000 gpm, mechanical cally driven, centridgal pumps  Helium, recirculated  Helium, recirculated  34,000 gpm, mechanical  Helium, recirculated  B700 kw 166 ft 166 ft 176 ft 117 ft 11	Je, 6 - 0.146 in. side plates and	tivity change (by safety rods)
Craphite; 29.5 metric tons  Graphite; 29.5 metric tons  6.8 metric tons  6.8 metric tons  6.8 metric tons  Aluminum and steal  Helium  monite-iron-aggregate concrete  1.2 to 2 1/2 ft of D2O  2. to graphite  4 ft 8 1/2 in. of heavy concrete  ft across flats by 13 ft 6 1/2 in.  2. to graphite  7. 2 to 2 1/2 ft of D2O  8. 2 to graphite  10.35: 1.15 kg  10.35: 1.15 kg	Dod	
Craphite; 29.5 metric tons  6.8 metric tons  6.8 metric tons  7.0 metric tons  8.1 metric tons  1.2 ft dia. x 2 ft  1.2 ft of D20  1.2 ft of B20  1.2 ft of B20  1.3 ft of B20  1.4 ft 8 1/2 in. of beavy concrete  ft across flats by 13 ft 6 1/2 in.  1.0 2 ft of graphite  1.0 3 ft of graphite  1.0 6 graphite  1.0 6 ft of D20	1)	eine. Lowered through individual acco
monite-iron aggregate concrete llements in 6 in. aquare array by the life of life of life of graphite of life of graphite of life of graphite of life of life of life of graphite of life of life of life of life of graphite of life of l		holes in tank pluo
monite-iron-aggregate concrete lements in 6 in. aquare array b  Aluminum and streat  Aluminum and streat  Aluminum and streat  2 ft dia. x 2 ft  2 to 2 1/2 ft of D2O  m). 2 ft of graphite  4 ft 8 1/2 in. of heavy concrete  ft across flats by 13 ft 6 1/2 in.  U235; 1 15 kg  0 84 g/day  CD2O, recirculated  n exchange columns (continuous)  Recombination  Recombination  Recombination  About 80 kw  34,000 BTU (leg ft)(hr)  6 kw/1  870 kw/kg 25  148°F  117°F  117°F  117°F  5.4 ft/sec		Drawn up into shielded col
Monemonite-iron-aggregate concrete elements in 6 in. aquare array belium monite-iron-aggregate concrete for a 2 to 2 1/2 ft of D2O  2 to 2 1/2 ft of D2O  2 to graphite ft across flats by 13 ft 6 1/2 in.  U235; 1.15 kg  D2O, recirculated nexchange columns (continuous)  Recombination  Readby), 1000 gpm, mechanical  (cally driven, centrifugal pumps  Helium, recirculated  About 80 kw  146°F  117°F  117°F  5, 4 ft/sec	6.8 metric tons	
monite-iron-agregate concrete ilements in 6 in. aquare array b lements in 6 in. aquare array b  2 ft dis. x 2 ft  2 to 2 1/2 ft of D2O  m). 2 to 2 1/2 ft of D2O  the second is a possible of the seco	None	nance escape (clean and cold)
monite-iron-aggregate concrete elements in 6 in. equare array b  2 to 2 1/2 ft dia x 2 ft  2 to 2 1/2 ft of D2O  3 to 6 graphite  4 ft 8 1/2 in. of heavy concrete ft across flats by 13 ft 6 1/2 in.  10 235: 1.15 kg  10 24 g/day  10 26 graphite  10 8 g/day  10 9 8 g/day  10 9 8 g/day  10 0 9 g/day  10 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	Aluminum and steel	mal utilization (clean and cold)
monite-iron-aggregate concrete elements in 6 in. aquare array b  2 ft dia. x 2 ft  2 to 2 1/2 ft of D2O  m). 2 ft of graphite 4 ft 8 1/2 in. of heavy concrete ft across flats by 13 ft 6 1/2 in.  U235: 1.15 kg  0.84 g/day	Helium	sion length squared (clean and cold) 87.5 cm
elements in 6 in. equare array b  2 to 2 1/2 ft of D20  m). 2 to 2 1/2 ft of D20  ft across flats by 13 ft 6 1/2 in.  U235; 1.15 kg  . 0.84 g/day  . 0.84 g/day  . 0.84 g/day  . 0.90, recirculated  m exchange columns (continuous)  Recombination  standby), 1000 gpm, mechanical  (cally driven, centrifugal pumps  Helium, recirculated  About 80 kw  146.F  117°F  117°F  117°F  About 5 psi	monite-iron-aggregate concrete	clean and cold)(two groups)
2 ft dia. x 2 ft  2 to 2 1/2 ft of D2O  2 to 2 graphite 4 ft 8 1/2 in. of heavy concrete ft across flats by 13 ft 6 1/2 in.  10 84 g/day  10 84 g/day  10 84 g/day  10 96 gpm, controllated  Recombination standby), 1000 gpm, mechanical (cally driven, centrifugal pumps  Helium, recirculated  34,000 gpm, go wy  1000 kw  34,000 gpm, 1000 kw  106 gpm, 117°F  117°F  117°F  118°F  118°F  24 ft sec	elements in 6 in. square array b	ling (clean and cold) 3 x 10-3 cm
2 ft dia. x 2 ft  2 to 2 1/2 ft of D2O  2) 2 ft of graphite 4 ft 8 1/2 in. of heavy concrete ft across flats by 13 ft 6 1/2 in.  10235; 1 15 kg  1024 g/day  2 D2O, recirculated  2 combination Standby), 1000 gpm, mechanical cally driven, centrifugal pumps  4 helium, recirculated  34,000 BTU (46 ft)(hr)  5 kw/1  6 kw/1  7 100 gpm  7 1000 kw  7 1000 kw  7 1000 kw  8 1000 BTU (6 kw/1)	(	upt neutron lifetime About 1 x 10-3
mb) 2 to 2 1/2 ft of D2O 4 ft 8 1/2 in. of heavy concrete ft across flats by 13 ft 6 1/2 in.  U235; 1.15 kg  0.84 g/day  0.84 g/day  0.84 g/day  0.84 g/day  0.80, recirculated Recombination standby), 1000 gpm, mechanical ically driven, centrifugal pumps  Helium, recirculated  About 80 kw  34,000 BTU/(eq ft)(hr)  34,000 BTU/(eq ft)(hr)  117°F  117°F  117°F  117°F  3.4 bout 5 psi	-	lean and cold)
4 ft 8 1/2 in. of beavy concrete ft across flate by 13 ft 6 1/2 in.  10.235; 1.15 kg  10.34 g/day  20. recirculated n exchange columns (continuous) Recombination Recombination Helium, recirculated  21.15 kg  22.00 gpm, mechanical  33.000 gpm, recirculated  34.000 BTU/(af ft)(hr)  25.000 BTU/(af ft)(hr)  26.000 BTU/(af ft)(hr)  27.000 BTU/(af ft)(hr)		clean and cold)
fit 8 1/2 in. of Littor graphine fit across flats by 13 ft 6 1/2 in.  U235: 1.15 kg  U235: 1.15 kg  0.84 g/day  controllated  exchange columns (confinuous)  Recombination  Recombinated  Recombination	_	emperature (total)
ft across flats by 13 ft 6 1/2 in.  U235; 1.15 kg  U235; 1.15 kg  0.084 g/day  0.084 g/day  1.000 gpm, mechanical  readby), 1000 gpm, mechanical  feally driven, centrifugal pumps  Helium, recirculated  About 80 kw  34,000 BTU/(eq ft)(hr)  870 kw/fg 25  117°F  117°F  About 5 psi	_	opieone)(tumical)
n exchange of the state of the	4 It 6 1/6 In. Of meany concrete	hot and noisoned
U235; 1.15 kg  0.64 g/day  0.64 g/day  1.020, recirculated  Recombination  1000 kw  1000 kw  1000 kw/l  1000	It across mate by 13 it o 1/2 in.	Internation matter
n exchange columns (continuous) standby), 1000 gpm, mechanical (cally driven, centrifugal pumps Helium, recirculated  About 80 kw 34,000 BTU/(eq ft)(hr)  BYO kw/kg 25  116°F  117°F  117°F  About 5 psi	11235. 1 16 5	
EXPERIMENTAL FACILITIES   10 - vertical thirms   steamble columns (continuous)		(everage)
EXPERIMENTAL FACILITIES   10 - vertical through	Iverage)	• • • • • • • • • • • • • • • • • • • •
EXPERIMENTAL FACILITIES   10 - vertical thims		
### EXPERIMENTAL FACILITIES		
1 - 6 in. decay   1000 gpm, mechanical   1 - 6 in. decay   1000 gpm, mechanical   1 - 6 in. decay		
1 - 6 in. d	Recombination	10 - Vertica
Helium, recirculated   20 - 1   1000 kw   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2 - 6   2	2 - paralleled (I standby), 1000 gpm, mechanical	tank; 0 - 1 In. dis.,
Helium, recirculated  1000 kw  1000 BTU/(eq ft)(hr)  1000 BTU/(eq		J. T. F. C. DER. CALL OF L. C.
		20 - Verical mimbles in graphic reliect
2 - 6  About 50 kw  6 kw/l  146°F  CAPITAL INVESTMENT  117°F  REFERENCES  Arg  Arg  Arg  Arg  Arg  Arg  Arg  Ar	•	
2 - 6 i   2 - 8 x   2 - 6 i   2 - 8 x   2 - 8 x   34,000 BTU/(eq ft)(hr)   6 kw/l   1 - 1 in. dia. ht   1 - 2 in. dia. ht   1 - 3 - 5 x   5 t thermal column   1 - 5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x   5 x	9	2 - 12 in. dia., horizontal beam bo
About 5 psi  About	:	•
About 80 kw 34,000 BTU(sq ft)(hr) 870 kw/lkg 25 148°F 146°F CAPITAL INVESTMEN 117°F REFERENCES	•	
34,000 BTU/(sq ft)(hr) 6 kw/l 148*E 146*F CAPITAL INVESTMEN 117*F REFERENCES	• • • • • • • • • • • • • • • • • • • •	
1		
148°F   2 - 5 × 5 ft   146°F   1   146°F   CAPITAL INVESTMENT   124°F   EFFENCES     124°F   S.4 ft/sec   5.4 ft/sec   About 5 psi		graphite reflector
146°F 2 × 5 ft thermal 2 · 5 × 5 ft thermal 3 · 5 · 5 ft thermal 4 · 5 · 5 · 5 · 5 · 5 · 5 · 5 · 5 · 5 ·	• • • • • • • • • • • • • • • • • • • •	I - I in. dia. horizontal pneumatic tube below latt
About 5 psi	ire	,
REFERENCES	#-9+1	2 - 5 X 5 If thermal columns with 10 5/4 in. sq axial rest no
124°F KENCES	3.11 · · · · · · · · · · · · · · · · · ·	INVESTMENT
	124.5	NCES
a About 5 pai		Argonne Research Reactor (CP-5)
		Argonne National Laboratory, J. M. West
		and J. T. Weills, ANL-4779, 23 pp, Secret
		May (, 1951

Digitized by Google

Estimated See text

### Table A.2.10 - Thermal Test Reactor (TTR)

Schenectady, New York Charging	AMO		-	<del></del>			il assemblies Sk (poisons)	-		None Thermal: maximum (central column) 3.6 x 109 n/(cm²)(sec)	EXP	18 in. dia. x 18 in.	7 x 14 ft high REFERENCES Feasibility Report for the KAPL		 	None Knolls Atomic Power Laboratory, H.B. Stewart, et al.		. Indefinite 5 watts	2.4 watte	.04 kw/kg 25	. Negligible	ling variation	cadmium rods	cadmium rods lick, iron-clad
LOCATION Knolls Atomic Power Laboratory	A - House	Construction Knolls Atomic Power Laboratory	tion	FURFUSE	Cladding	Fuel tubes			Structural material	:	LATTICE TYPE		Over-all	STRATEGIC MATERIAL Fleeionable material		COOLING SYSTEM	 Total heat power		Heat flux	• •	Maximum moderator temperature Negligible	CONTROLS Shim	7	cadmium rode 6 - 4 in. wide. 1/32 in. thick. iron-clad

## Table A.2.11-Low Power Research Reactor (LPRR)

Shim	al utilization (clean and cold) buil utilization (clean and cold) ion length squared (clean and cold) lean and cold) in theutron lifttime ean and cold) mperature) magnitude from and cold) rean and cold) rean and cold) rean and cold) magnitude man and cold) rean and cold) magnitude man and cold) magnitude	E.S 2 - 3 in. dia. bor 1 - 6 in. dia. bor 6 - 3 1/2 in. dia. bor 2 - 2 in. dia. bor 2 - 2 in. dia. vertica 6 - 3 in. dia. vertica 1 - 4 1/2 x 4 1, A Low F. Engineerin American Aviation spithermal region
OR GANIZATIONS North on ling bes	Reflector  Coolant  Coolant  Total D2O requirement  Fretile material  Structural material  Aluminum and graphite  Robertor atmosphere  Streel and iron-ore-colemanite concrete  LATICE TYPE  Core  Core  Core  Core  Concrete: 72 in.  Concrete: 72	Recirculated Ion exchange demineralis Ion exchange demineralis Not apec 86. 86. 15 16. 16. 17 18. 18. 18. 19 19. 19. 19. 19. 19. 19. 19. 19. 19.

## Table A.2.12 -- Los Alamos Water Boiler (SUPO)

RGANIZATIONS	Pumping rate
Design	Fumping power required
	COUNTY COLD Solution and address and seculation and
:	The state of the s
:	STORY (TOTAL AND
in operation, with	
	2 - 1/32 x 3 x 30 in. vertical, aluminum clad
· · ·	cadmium sheets
Coolant tubes Stainless steel, 1/4 in. OD x 1/32 in. wall	Safety 1 - 1/32 x 3 x 30 in., vertical, aluminum clad,
Moderator H2O	
Reflector	Reactivity change
Och	
auoN [minetant elisted	Charging Transfer flask with fluid
[ and and [ ring)]	Discharging Control by air pressure variation
Restroyment	SUISAH
Shiple Appropriate the part of	Resonance escape (clean and cold)
TATITATION OF THE PROPERTY OF	Thermal utilization (clean and cold)*
NOTINE	Diffusion length squared (clean and cold)
12 in. dia	Age (clean and cold) ^a
• • • • • • • • • • • • • • • • • • • •	Drown sentron lifetime
Chill Club and a charlet and a	Morphism (clean and cold)
Chiefe and and control of the state of the s	The column and column
1007	100 (clean and cold)
THE PERSON OF TH	Refil (Creation Cold).
15 4	N (termperature)(annared at one at one of the state of th
MARTERIAL	No figure and the fig
	A Chouse of the soul to see the see that the soul to see the see the see that the see
Filestona one material	Ment and the control of the control
: : : : : :	METHER ON ET HY DENGTHER
	NEO INCOMPANIANTE AND A 102 A
ume	This is a second of the second
	The man of the contract of the
	TATELLY (INSTITUTE)
• • • • • • • • • • •	TOTAL COLUMN TO THE COLUMN TABLES OF THE COLUMN TAB
Coolant treatment	Section 1 to 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	ALCU LCAURER CAREFORNIA DE LA CAREFORNIA
Referention Balin	2 - horizontal oraphite thermal columns
	(1 - 4 x 4 ft and 1 - 5 x 5 ft).
(S (typical)	with several removable stringers
	CAPITAL INVESTMENT
•	REFERENCES The Los Alamos Homogeneous Reactor,
	Supo Model, Los Alamos Scientific
Heat flux (average)	Laboratory, L.D.P. King, LA-1301,
	October, 1951
Average fuel solution temperature 180° F	
•	
•	
Coolant velocity	
ind 09	

Table A.2.13 -- Homogeneous Reactor Experiment (HRE)

LOCATION Oak Ridge National Laboratory	Innage
	Power density (average)
•	Specific power (average) About 600 kw/kg 23 in core
Design Oak Ridge National Laboratory	Fuel solution inlet temperature
:	Fuel solution outlet temperature
Operation Oak Ridge National Laboratory	Fuel solution inlet pressure
PURPOSE	Fuel solution pressure drop through reactor Negligible
	Pumping rate
	Pumping power required (total)
T.235. 1 6 0.2 1 10. so. 110. so. in mater	a loathoo
The state of the s	CONTRACTOR OF THE PROPERTY OF
	Saim
:	sheets in the form of cylindrical segments,
Reflector	tangential to core in reflector,
Total D2O requirement About 0.5 metric ton	Variation of fuel concentration
Coolant	Variation of reflector level
:	Regulator
:	the form of a cylindrical segment, tangential
Deco	to core in reflector
:	Safety Safety
	sheets in the form of cylindrical segments
	school light to a school of the breat
Total ID appear	Anna active for a company
:	Trick drimp of core tank
Sheld to the state of the state	FOEL MANDLAND
	Charging Fump injection into circulating system
	Discharging Drain to dump tanks
:	NEUTRON FLUX DENSITIES
Consumption About 1 gm/day	Thermal: average
:	EXPERIMENTAL FACILITIES None
Average cycle time Indefinite	CAPITAL INVESTMENT
	REFERENCES. Homogeneous Reactor Experiment Feasibility
Type Recirculated liquid fuel	Report Oak Ridge National Laboratory, ORNL-730,
Coolant treatment Batch processing	108 pp. Secret, July 6, 1950
Pumps Westinghouse Model 100A	
=	Homogeneous Reactor Project Quarterly Progress
2 - 1 gpm, Pulsafeeder pumps	Report, Oak Ridge National Laboratory,
Safety Natural convection cooling system	ORNL-1318, 184 pp, Secret, Sept. 19, 1952
	National Property of the Parket of the Parke
Moderator cooling Circulation of D2O through heat exchangers	
:	
OPERATING CONDITIONS	
Total heat power 1000 km	
Useful power output About 120 kw (design)	

### Α Absorption coefficients, narrow-beam, combinations for mixtures of elements, 641-642 components of, 640-641 definition for monochromatic gammas, 640 filtration effect, 648 (See also Energy-absorption coefficients and Mass absorption coefficients) Absorption of capture gammas, 705-707 Activity-mass formula, 630-631 Adjoint equation for infinite homogeneous medium, Adjoint operator, 471 Age, definition of, 401 of fission neutrons, in moderators, 485 in water-metal mixtures, 486 for lattice reactors, 482, 485 measurement of, 49-51 of Ra-α-Be neutrons in water-metal mixtures, 486 and slowing-down length, 402 of water lattices, 501 Age equation, with absorption, 402 solutions for homogeneous regions, 402-403 for variable-density medium, 470 Age theory, 401-405 continuity equation in, 401 deviation from, 412 group method for, 418-419 and group theory, 422 migration area in, 404 moment improvements without absorption, 409-410 slowing-down distance in, 409 two media problems in, 402 Aging, in finite homogeneous medium, 403 followed by diffusion, 403-408 in finite homogeneous media, 405 in infinite homogeneous medium, 404 in infinite homogeneous medium, 402 Air, composition of, 741 density of, 742 mass absorption coefficient of, 721 Albedo, 446 approach to neutron attenuation, 695 effective, 696-698 table, 698 fast-neutron, for concrete, 696, 697 for water, 696, 697 gamma-ray for concrete, 698

Albedo, wall, in single-bend duct, 696 in straight duct, 695 Alpha (see Cross sections, capture-to-fission ratio of) Alpha particles, emission in fission, 67 range of, 66-67 Aluminum,  $\sigma_e (1 - \cos \theta)$  value for, 110 Ammonia, atomic density of, 720 mass absorption coefficient of, 721 molecular density of, 721 molecular weight of, 721 physical properties of, 733 Amu (see Atomic mass unit) Analysis of U.S. waters, 736 Argonne Heavy Water Reactor, 769 Argonne Research Reactor, 770 Ash, atomic density of hydrogen in, 721 mass absorption coefficient of, 722 white, composition of, 738 physical properties of, 739 Atomic density, of elements, 717 of hydrogen, in compounds, 720 in organic compounds, 720 Atomic mass unit, definition of, 61 energy equivalent of, 61 Atomic numbers of elements, 717-719 Atomic weights of elements, 717-719 Attenuation, gamma, by air ducts and voids, 698 by single straight duct, 698 neutron, dependence of visible wall region at bend on angle of bend, 696, 697 by multiple-bend duct, 696-697 by single-bend duct, 696 by single straight duct, 695, 696 by voids, 698 Attenuation constant, for linear anisotropy, 430 (See also Diffusion length and Transport theory) Attenuation function, definition of, 677-678 Attenuation kernel (see Attenuation function)

### B

Balsa, atomic density of hydrogen in, 721 composition of, 738 physical properties of, 739 Barytes aggregate, composition of, 727 Beryllium, lattices moderated by, 484 (n, 2n) reaction in, 82-83  $\sigma_{\rm e}(1-\cos\bar{\theta})$  value for, 110 slowing-down density in, 507

Beryllium, total cross section of, 78-79, 142 use of, for neutron monochromator, 22 in neutron sources, 1 Beta decay (see Radioactive decay) Binding energy, 61, 626 of additional neutron, 62, 86-105 and packing fraction, 62 Biological dose, 677 Boiling points of organic compounds, 741 Boltzmann equation, 365 for anisotropic scattering, 380 solutions, 455 spherical harmonics in, 381 for energy-independent cross sections, 450 integral equation formulation for one-velocity theory, 378-380 integro-differential formulation for infinite homogeneous region, 376-378 for isotropic scattering, 378 kernel for, 378 plane kernel for, 379 for slab geometry, 378 time-dependent treatment of, 379 variational formulation of, 380-381 (See also Transport equation) Boral, composition of, 750 mass absorption coefficient of, 721 physical properties of, 750 Boration of water, 748 Boron, use in neutron detectors, 23-24, 29 Boron coatings for metals, 748-749 Boron-containing materials, 748-751 solubility of, 748, 751 Boron frits, composition of, 731 Boundary conditions for black medium, 423 Boundary equations, in diffusion theory, across interface between two media, 390 between medium and vacuum, 390-391 in group-diffusion method, 418 for group method, 465 for slowing down with absorption in finite regions, 422-423 for slowing-down density, for Greuling-Goertzel approximation, 423 for Wigner approximation, 423 in spherical-harmonic method, 390 in transport theory, 390 Breit-Wigner formula, for capture cross section, 71 for scattering cross section, 72 Bricks, composition of, 742 mass absorption coefficient of, 721 physical properties of, 743 Broad-beam attenuation, 649, 650 apparent absorption coefficient, 649 gamma deflection, 649 Brookhaven Graphite Research Reactor, 765 Buckling, 435 effective value of, 608 geometric, 443, 444 stationary formula for, 443 material, approximations for, 435 for heavy-water system, 494 measurement of, 55 for water lattices, 501 values for cylindrical shapes, 614 for water lattices, 499, 500

Build-up factors, 651-652, 684-685 for gamma-ray absorptions, 701-702 linear, definition of, 686 NDA-NBS calculation, tables, 660, 661 trend at great depths, 655 data, 656 unitary, definition of, 686 Bulk Shielding Reactor, 768 spectral distributions of, 704

### C

Cadmium ratio, 18, 51 for water lattices, 500 Capture gammas, absorption of, 705-707 Carbon, total cross section of, 78-79, 143 (See also Graphite) Cements, colemanite borated, composition of, 723 physical properties of, 724 composition of, 723 mass absorption coefficient of, 722 physical properties of, 724 plain, composition of, 723 physical properties of, 724 portland, composition of, 723 Chemical binding, 78-80, 144-145 Chicago Pile No. 1, 762 Chicago Pile No. 2, 763 Chopper, neutron, 19 Chromium,  $\sigma_{c} (1 - \cos \theta)$  value for, 110 Collision mechanics, 75-78, 110, 134 Collision reactions, 11, 70-84, 110-114, 128-157, 351-363 laboratory and center-of-mass coordinates for, 70 Composition, of air, 741 of barytes aggregate, 727 of barytes concrete, 726 of barytes-limonite concrete, 728 of boral, 750 of boron frits, 731 of bricks, 742 of cements, 723 of concretes, 730 of fuel oil, 733 of gasoline, 734 of glass, 743 of iron, 744 of lucite, 735 of lumnite, 731 of masonite, 740 of MO concrete, 725 of ordinary concrete, 725 of paraffin, 736 of rocks, 746 of rubber, 735 of sand, 724 of shield materials, 723-748 of stainless steel type 347, 747 of woods, 738 Compound nucleus, excitation of, 62 fission of, 68 formation of, 71, 75 cross section for, 80-81 Compounds in shield materials, 720



atomic densities of hydrogen in, 720

Compounds in shield materials, densities of, 720	Control rods, single, radial displacement of, 602, 603
molecular densities of, 720	transfer function of, 583-584, 593
removal cross sections of, 723	Conversion factors, angular displacement, 756
Compressive strength of concretes, 732	density, 757
Compton scattering, 639	energy, 754-755
probability of, 639	gamma-ray cross section, 760
removal of incident photon energy, 643, 644	length, 755-756
Concretes, barytes, composition of, 726	pressure, 756-757
elemental composition of, 728	thermal conductivity, 757
physical properties of, 727	time, 755
barytes-limonite, composition of, 728	volume, 756
compressive strength of, 728	Copper, $\alpha_{\epsilon} (1-\cos\theta)$ value for, 110
density of, 728	Counters (see Neutron detectors)
elemental composition of, 728	Critical equation, for bare thermal reactor,
boron frits-barytes, composition of, 730	in terms of migration area, 464
compressive strength of, 732	eigenvalue formulation of, 471
density of, 732	for infinite homogeneous medium, 427
description of, 729	for thermal reactor, by mode method, 463
elemental composition of, 732	for two-group theory, 466
colemanite-barytes, composition of, 730	Critical mass, 477-478, 485-495
compressive strength of, 732	data for water boilers, 488
density of, 732	minimum, for water reactor, 478, 512
description of, 729	of reactors, deuterium-moderated, 478, 491-495,
elemental composition of, 732	515
composition of, 674, 730	heavy-water-moderated, with graphite reflectors, 493
compressive strength of, 732	
density of, 732 elemental composition of, 732	with heavy-water reflector, 491-493 without reflector, 492
iron-portland, composition of, 730	· · · · · · · · · · · · · · · · · · ·
compressive strength of, 732	homogeneous, with moderated cores, 477-478, 488-495, 510-515
density of, 732	hydrogen-moderated, 477-478, 488-490, 510-514
description of, 729	water-moderated, 477
elemental composition of, 732	effect of reflector on, 478, 490
lumnite-colemanite-barytes, composition of, 730	Critical size, of bare spheres, 430
compressive strength of, 732	effect of density on, 445
density of, 732	for odd-shaped reflected reactors, 449
description of, 729	for simple geometries, 431
elemental composition of, 732	for thermal reactor, with Gaussian slowing down,
lumnite-portland-colemanite-barytes, composi-	458
tion of, 730	Cross sections, absorption, 42-45
compressive strength of, 732	measurement of, by activation method, 44
density of, 732	by change in reactor reactivity, 43-44
description of, 729	by depletion method, 44
elemental composition of, 732	by diffusion length, 45
mass absorption coefficient of, 722	by substitution method, 42-43
MO, composition of, 725	by transmission method, 42
physical properties of, 726	average values for, 376
ordinary, composition of, 725	capture, 73
physical properties of, 725	Breit-Wigner formula for, 71
Cone of radiation, 683, 684	measurement of, 47-48
Constants, 754	capture-to-fission ratio of, 69
Continuity equation, 365, 382	measurement of, 48-49
for slowing-down density, 367	definition of, 41
Control (see Reactor dynamics)	differential, in center-of-mass and laboratory
Control boundaries, 614	systems, 70
Control gaps, 614-615	effect of density on, 554
Control regions, 609-614	effective value of, 562
Control rods, effective radius of, 602, 605-607	elastic scattering, value of, 78, 110-111, 129,
for black bars, 606	135-141, 351-363
for non-black bars, 605-607	fission, 68, 117-126
flux flattening by, 612	measurement of, 47
multiple, shadowing effect for, 605, 608	free-atom, 80
shape of, relative effectiveness for, 605, 607	inelastic, data for, 80, 112-114
single, 602-605	of iron, 47
effective radius of, 602	for inverse process, 74

Digitized by Google

Cross sections, neutron, 71-74, 128-132	Diffusion equation, solutions of, 466, 468
radiative capture, 62, 130	asymptotic, 393
Breit-Wigner fit for cadmium, 83, 152	for bare reactors, 443-445
for 1-mev neutrons, 84, 130	for cylindrical geometries, 446, 447
removal, 451	near free boundary, 393
scattering, 45-46, 71-72	for plane geometries, 446
Breit-Wigner formula for, 72	for spherical geometries, 446, 447
differential, measurement of, 45	time-dependent, 389-390
for large angles, 46	useful formulations of, 383
by poor-geometry experiment, 46	validity of, 389
by recoil counters, 45-46	Diffusion kernel (see Kernel)
inelastic, 47	Diffusion length, 386, 389
measurement of, by direct spectrum method, 47	for anisotropic scattering, 392
by gamma-ray method, 47	measurement of, 52-54, 56
by transmission method, 47	thermal, 425
total, 46	for lattice reactors, 482, 487
measurement by transmission, 46	values of, 487
thermal values of, 351-363	
	for water lattices, 501
total, 41-42	Diffusion theory, boundary conditions in, acros
of beryllium, 79, 142	interface between two media, 390
of carbon, 79, 143	between medium and vacuum, 390-391
of deuterium, 145	effect of anisotropic scattering in, 389
of hydrogen, 144	extrapolation length in, 391
measurement by transmission experiment, 41	for homogeneous reactors, 435, 443-450
for total transport reaction, 74, 131	integral equations of, 383-384
transport, 78, 111	prescriptions for improving, 389
definition of, 78	near source, 389
values of, 111, 487	for strongly absorbing media, 389
Crystal effects, 78-80, 142-145	results of transport theory in, 389
Crystal monochromator, 21-22	for linear scattering law, 391
resolution of, 21	for quadratic scattering law, 391
Curie, 630-631	retardation time in, 385
Current, definition of, 677	time-dependent, 384-385
neutron (see Neutron current)	Green's function for, 384-385
	telegrapher's equation in, 385
_	transport correction to, 382
D	validity of, 385
	variational formulation of, 384
Danger coefficients, and absorption cross-section	Diffusion time, 385
measurement, 43	Doppler effect, 73, 597
for measurement of capture-to-fission ratio,	and reactivity, 556
48-49	Dosage rate, 630
Density, of air, 742	Ducts, air, 695
of compounds in shield materials, 720	albedo approach, 695
of concretes, 732	multiple-bend, 696
of elements, 717	principal investigations of, 695
of organic compounds, 741	single-bend, 696
of wood, and volume composition, 740	straight, 695
Deuterium, reactors moderated by, critical mass of,	Dynamics (see Reactor dynamics)
478, 491-495, 515	• • •
slowing down in, 370, 374	
total cross section of, 145	E
Diffusion, in crystalline matter, 425	<del></del>
of gamma rays, 646	Effective removal cross section, 670-671
hardening effect in, 425	definition of, 671
in high-atomic-weight material, 425	of iron, 723
softening effect in, 425	of lead, 723
of thermal neutrons, 423-425	specific values for, iron, 673
with energy-independent cross sections, 424-425	lead, 671
Diffusion coefficient, 382, 389	oxygen, 671, 672
correction to, 389	table, 673
effect of density on, 554	use in calculating shields, 673
thermal, effect of temperature on, 562	(See also Removal cross section)
Diffusion constant, 443	Effective source area, 683-684
Diffusion equation, for homogeneous multiplying	Einstein energy-mass formula, 61
region, 435	Elastic scattering, 668
- ·	- ·



Elastic scattering, angular distribution of, 668	Feynman-Welton method, 450-456
definition of, 667	Fick's law, 382, 387
"potential," 668, 671	validity of, 385
"resonance," 668, 671	in asymptotic region, 389
Electrons, range of, 66	Fission, 67-70, 106-110, 117-127
Elemental composition, of concretes, 732	alpha-particle emission in, 68
barytes, 728	cross sections for, 68, 117-126
barytes-limonite, 728	energy release in, 70, 110
Elementary interaction processes, 637-647	gamma-ray spectrum, 69
classification by effect on photons, 638	neutron spectrum, 69
classification by mechanism, 637-638	neutron yield, delayed, 67
probability, 640-643	spontaneous, 68
Elements, atomic densities of, 717	decay constant, 106
atomic numbers of, 717-719	thresholds, 68, 106
atomic weights of, 717-719	of uranium 235, energy distribution in, 110
densities of, 717	Fission products, 68-69, 106-108, 109, 127
mass absorption coefficients of, 718-719	delayed neutrons, 623, 624
removal cross sections of, 723	gamma rays, 623, 624
Energy absorption, of core, 703	gross activity of, 623
of core and reflector, 703	hard emitters, 623, 624
of shield, 703	half-lives of, 106-108
of spherical core and reflector, 703	kinetic energy of, 67, 68, 70, 108, 110
Energy-absorption coefficients, 702	radiation from, time dependence of, 68-69, 110
narrow-beam, 646	range of, 67, 105
,	thermal absorption cross sections of, 106-108
table, 647, 661	
Energy dissipation, 643-647	yields of, 68, 106-108, 127
energy transport, 645-646	Fission sources, 621-624 Flux, definition of, 677
by electrons, 645	· · · · · · · · · · · · · · · · · · ·
distance traveled, 645	Flux distribution, in sigma pile, 53, 54
by neutrons, 645	for water boiler, 477, 511
distance traveled, 645	Foils, thick, 677
by positrons, 645	thin, 677
distance traveled, 645	Fuel oil, atomic density of hydrogen in, 721
by protons, 646	composition of, 733
distance traveled, 646	mass absorption coefficient of, 722
sidewise gamma escape, 643-645	physical properties of, 734
annihilation, 645	
bremsstrahlung, 645	•
fluorescence, 643, 644	G
fluorescent yield, 644	<del>-</del>
scattering, 643, 644	Gamma rays, attenuation of, 637-666
scattering, 643, 644 energy fraction scattered, 644	Gamma rays, attenuation of, 637-666 capture, 624-626
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 distribution near boundary, 662 distribution in "phantoms," 662
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662 effect of inhomogeneities, 662
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56 Extrapolation distance, 399	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56 Extrapolation distance, 399 for anisotropic scattering, 392	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662 effect of inhomogeneities, 662 radiation emerging from barrier, 662 radiological shielding, 662
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56 Extrapolation distance, 399 for anisotropic scattering, 392 for black cylinders, 391, 395	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662 effect of inhomogeneities, 662 radiation emerging from barrier, 662 radiological shielding, 662 sidescattering, 662
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56 Extrapolation distance, 399 for anisotropic scattering, 392 for black cylinders, 391, 395 for black spheres, 391, 394	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662 effect of inhomogeneities, 662 radiation emerging from barrier, 662 radiological shielding, 662 sidescattering, 662 fission, 623, 624
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56 Extrapolation distance, 399 for anisotropic scattering, 392 for black cylinders, 391, 395 for black spheres, 391, 394 in diffusion theory, 391	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662 effect of inhomogeneities, 662 radiation emerging from barrier, 662 radiological shielding, 662 sidescattering, 662
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56 Extrapolation distance, 399 for anisotropic scattering, 392 for black cylinders, 391, 395 for black spheres, 391, 394	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662 effect of inhomogeneities, 662 radiation emerging from barrier, 662 radiological shielding, 662 sidescattering, 662 fission, 623, 624
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56 Extrapolation distance, 399 for anisotropic scattering, 392 for black cylinders, 391, 395 for black spheres, 391, 394 in diffusion theory, 391	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662 effect of inhomogeneities, 662 radiation emerging from barrier, 662 radiological shielding, 662 sidescattering, 662 fission, 623, 624 spectrum of, 69
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56 Extrapolation distance, 399 for anisotropic scattering, 392 for black cylinders, 391, 395 for black spheres, 391, 394 in diffusion theory, 391 effective, 423	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662 effect of inhomogeneities, 662 radiation emerging from barrier, 662 radiological shielding, 662 sidescattering, 662 fission, 623, 624 spectrum of, 69 flux-dose conversion factor, 758
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56 Extrapolation distance, 399 for anisotropic scattering, 392 for black cylinders, 391, 395 for black spheres, 391, 394 in diffusion theory, 391 effective, 423 in group method, 418	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662 effect of inhomogeneities, 662 radiation emerging from barrier, 662 radiological shielding, 662 sidescattering, 662 fission, 623, 624 spectrum of, 69 flux-dose conversion factor, 758 inelastic scattering, 625-626
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56 Extrapolation distance, 399 for anisotropic scattering, 392 for black cylinders, 391, 395 for black spheres, 391, 394 in diffusion theory, 391 effective, 423 in group method, 418 measurement of, 54-55	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662 effect of inhomogeneities, 662 radiation emerging from barrier, 662 radiological shielding, 662 sidescattering, 662 fission, 623, 624 spectrum of, 69 flux-dose conversion factor, 758 inelastic scattering, 625-626 instruments for measuring, 625
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56 Extrapolation distance, 399 for anisotropic scattering, 392 for black cylinders, 391, 395 for black spheres, 391, 394 in diffusion theory, 391 effective, 423 in group method, 418 measurement of, 54-55 for plane geometry, 392	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662 effect of inhomogeneities, 662 radiation emerging from barrier, 662 radiological shielding, 662 sidescattering, 662 fission, 623, 624 spectrum of, 69 flux-dose conversion factor, 758 inelastic scattering, 625-626 instruments for measuring, 625 prompt, 623
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56 Extrapolation distance, 399 for anisotropic scattering, 392 for black cylinders, 391, 395 for black spheres, 391, 394 in diffusion theory, 391 effective, 423 in group method, 418 measurement of, 54-55 for plane geometry, 392 in transport theory, 391	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662 effect of inhomogeneities, 662 radiation emerging from barrier, 662 radiological shielding, 662 sidescattering, 662 fission, 623, 624 spectrum of, 69 flux-dose conversion factor, 758 inelastic scattering, 625-626 instruments for measuring, 625 prompt, 623 Gamma sources, (γ,n), 701
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56 Extrapolation distance, 399 for anisotropic scattering, 392 for black cylinders, 391, 395 for black spheres, 391, 394 in diffusion theory, 391 effective, 423 in group method, 418 measurement of, 54-55 for plane geometry, 392 in transport theory, 391 Extrapolation length (see Extrapolation distance)	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662 effect of inhomogeneities, 662 radiation emerging from barrier, 662 radiological shielding, 662 sidescattering, 662 fission, 623, 624 spectrum of, 69 flux-dose conversion factor, 758 inelastic scattering, 625-626 instruments for measuring, 625 prompt, 623 Gamma sources, (γ,n), 701 inelastic-scattering, 701
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56 Extrapolation distance, 399 for anisotropic scattering, 392 for black cylinders, 391, 395 for black spheres, 391, 394 in diffusion theory, 391 effective, 423 in group method, 418 measurement of, 54-55 for plane geometry, 392 in transport theory, 391	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662 effect of inhomogeneities, 662 radiation emerging from barrier, 662 radiological shielding, 662 sidescattering, 662 fission, 623, 624 spectrum of, 69 flux-dose conversion factor, 758 inelastic scattering, 625-626 instruments for measuring, 625 prompt, 623 Gamma sources, (γ,n), 701 inelastic-scattering, 701 primary, 701
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56 Extrapolation distance, 399 for anisotropic scattering, 392 for black cylinders, 391, 395 for black spheres, 391, 394 in diffusion theory, 391 effective, 423 in group method, 418 measurement of, 54-55 for plane geometry, 392 in transport theory, 391 Extrapolation length (see Extrapolation distance)	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662 effect of inhomogeneities, 662 radiation emerging from barrier, 662 radiological shielding, 662 sidescattering, 662 fission, 623, 624 spectrum of, 69 flux-dose conversion factor, 758 inelastic scattering, 625-626 instruments for measuring, 625 prompt, 623 Gamma sources, (γ,n), 701 inelastic-scattering, 701 primary, 701 Gaps, effect on multiplication, 56
scattering, 643, 644 energy fraction scattered, 644 Energy range, 637 Exponential integral functions, definition of, 686 figures, 690-692 table, 688 Exponential law of attenuation, 640, 641 importance for penetration problem, 651 Exponential pile, 55-56 Extrapolation distance, 399 for anisotropic scattering, 392 for black cylinders, 391, 395 for black spheres, 391, 394 in diffusion theory, 391 effective, 423 in group method, 418 measurement of, 54-55 for plane geometry, 392 in transport theory, 391 Extrapolation length (see Extrapolation distance)	Gamma rays, attenuation of, 637-666 capture, 624-626 materials for suppression of, 716 emission probability, 66 experimental information on, 660, 662-664 backscattering, 662-664 distribution near boundary, 662 distribution in "phantoms," 662 effect of inhomogeneities, 662 radiation emerging from barrier, 662 radiological shielding, 662 sidescattering, 662 fission, 623, 624 spectrum of, 69 flux-dose conversion factor, 758 inelastic scattering, 625-626 instruments for measuring, 625 prompt, 623 Gamma sources, (γ,n), 701 inelastic-scattering, 701 primary, 701 Gaps, effect on multiplication, 56 Gasoline, atomic density of hydrogen in, 721

Geometry, shielding, 677-693 Glass, composition of, 743 mass absorption coefficient of, 722 physical properties of, 744 Granite, composition of, 746 mass absorption coefficient of, 722 physical properties of, 747 Graphite, lattices moderated by, 483-484, 499, 522-528 reactors moderated by, flat flux for, 465  $\sigma_{\rm e} (1 - \overline{\cos \theta})$  value for, 110 slowing down in, 412, 413 slowing-down density in, 412, 505 Group-diffusion method, 417-422 boundary conditions in, 418 choice of parameters in, 419-420 flux equations for, 417-418 iteration technique in, 420 kernels for, 420-422 slowing-down density in, equations for, 418-419 Homogeneous reactors, with variable-density moderator 470 with variable fuel distribution, 470 water-moderated, 462 (See also Critical mass and Critical size) Hydrogen, atomic density of, in compounds, 720 in organic compounds, 720 cross section, 669-670 total, 144 exact solutions for slowing down, 369 and heavy element, slowing down in, 370 reactors moderated by, 464 critical mass of, 477-478, 488-490, 510-514 scattering by, energy distribution from, 76-77 slowing down in, 367, 369 slowing-down density in, 412, 414-416 slowing-down length in 415 use in neutron detector, 32 (See also Water)

### H

Half-value layer of absorber, 642 Heat generation in shields, 701-708 Heavy-water system, material buckling for, 494 Hickory, atomic density of hydrogen in, 721 composition of, 738 physical properties of, 739 Homogeneous Reactor Experiment, 774 Homogeneous reactors, bare, 463-464 comparative accuracy of methods for, 430-431 end-point method for, 430, 431 flux in, 444 iterative method for, 429-430 critical mass of, 477-478, 485-495 diffusion theory for, 435, 443-450 hydrogen-moderated, 464 multiregion, two-group treatment of, 465-469 multivelocity, anisotropic scattering in, 455-456 approximate solutions for, 452-453 Feynman-Welton method for, 450-456 one-velocity treatment of, 450-456 with nonuniform moderator, 470 odd shapes of, 470 one-velocity treatment of, 429-450 reflected, 445-449 and cylindrical geometry, 449-450 approximate solutions for, 450 end-point method for, 431 solutions for odd shapes, 449-450 two-group theory for, 453-455 Serber-Wilson method for, 431, 433-434 thermal, mode methods for, 462-463 treatment of, for Gaussian slowing down, 456-461 for symmetric slowing-down kernel, 459 transport approximation for, 431, 432 treatment for energy-dependent cross sections, 451-453 with uniform moderator, 456-465 with flat thermal flux, 464 with minimum mass, 464 with nonuniform fuel loading, 464-465 with uniform power density, 464

### I

Image method, 423 Importance, 473-474 definition of, 532 of delayed neutron emitters, 533 and generation time, 473-474 and reactivity, 473 Indium, use as neutron detector, 25 Inelastic scattering, 668-669 cross sections, 668 definition of, 667 gamma rays in, 668-669 Intensity of radiation, 630 Interaction processes, elementary (see Elementary interaction processes) Ion pairs, 629 Iron, atomic density of, 717 composition of, 744 effective removal cross section of, 723 inelastic cross section of, 47 mass absorption coefficient of, 718, 722 physical properties of, 745  $\sigma_e (1 - \overline{\cos \theta})$  value for, 110 Isotopes, table of, 158-350

### K

Kernel, for Boltzmann equation, 378
convolution of, 421
diffusion, 383, 384
group-diffusion, 420-422
plane, for Boltzmann equation, 379
point diffusion, 421
for slowing down, 368
symmetric, slowing down by, 459
synthetic, for slowing down, 368-370, 373
solutions for, 369
use for critical mass of water reactors, 477
transport, 380
solution by Fourier transforms, 379-380
Kinetic theory of neutrons, 365-426



### L Multigroup diffusion theory, iteration method for, 469 (See also Two-group theory) Lattice reactors, 478-485, 487, 495-503, 516-528 Multiplication, interpretation of, 57 measurement of, 56-57 age for, 482, 485 diffusion length for, thermal, 482, 487 Multiplication factor, 56 effective resonance integral for, 481-482 effect of fuel on, 499 experimental and numerical results for, 483-484, effective change by control rods, 614 for homogeneous region, 435 499-501, 522-528 fast-fission effect for, 479, 483, 495-496, 516 for lattice reactors, 484 data for, 495 for lattices, effect of fuel composition on, 484, 499 interaction effects for, 479 metal-rod, 484, 522 uranium metal rods, 496 one-group, 383 values of, 496 stationary expression for, 533 multiplication factor for, 484 for uranium rods in graphite, 522 resonance escape probability for, 480-483, for water lattices, 501 497-498, 502-503, 520-521 Multiplication length, 386 surface and volume absorption in, 481 thermal utilization for, 479-480, 483, 487, 497, 517-519 N Lead, atomic density of, 717 effective removal cross section of, 723 Neutron attenuation, 667-675 mass absorption coefficient of, 719, 722 build-up factor in, 670 physical properties of, 746 in concrete, 673-674 Leakage, reactor, for shielding calculations, 693 relaxation lengths for, 674 Limestone, composition of, 746 in iron, 673 mass absorption coefficient of, 722 in large thickness of heavy material, 673 physical properties of, 747 in lead, 671 Los Alamos Water Boiler, 773 in water, 671, 672 Neutron balance (see Continuity equation) Low-intensity Training Reactor, 767 Low Power Research Reactor, 772 Neutron current, definition of, 382 Neutron detection, of fast neutrons, 40-41 Lucite, atomic density of, 720 composition of, 735 by fission chambers, 33 of slow neutrons, by activation, 25-29 mass absorption coefficient of, 722 molecular density of, 720 standardization of activation foils, 40 by threshold detectors, 33-35 molecular weight of, 720 physical properties of, 735 (See also Neutron detectors) Neutron detectors, 23-36 Lumnite, composition of, 731 for fast neutrons, 32-36 "long" counter as, 32 M photographic emulsions as, 35 proton recoil counters as, 32-33 Masonite, atomic density of hydrogen in, 721 scintillation counters as, 35-36 composition of, 740 isotopes useful for, 25 physical properties of, 740 and photographic emulsions, 30-32 and resonance scatterers, 29-30 Mass absorption coefficients, of elements, 718-719 narrow-beam, 641 for slow neutrons, 23-32 table, 642 fission counters as, 24 of shield materials, 721-722 ionization chambers as, 23-24 Materials Testing Reactor, 766 proportional counters as, 23-24 Maximum permissible contamination, 633-634 scintillation counters as, 32 Maximum permissible exposure, 633 threshold, isotopes for, 34 Maxwell-Boltzmann distribution, 425, 556-557 use of indium as, 25 (See also Neutron detection) and averages, 376 for thermal neutrons, 375, 376 Neutron energy, 759 Metals, boron coatings for, 748-749 Neutron flux, conversion to dose rate, 758 thermal, standardization of, 39

Migration area, 464

Milligoat, 677

terials, 720

for, 469

materials, 720

measurement of, 56

effect of temperature on, 598

Moderation (see Slowing down)

Molecular densities, of compounds in shield ma-

Molecular weights, of organic compounds in shield

Multigroup diffusion theory, calculation techniques

Neutron reactions, 71-84, 110-114, 128-157,

approximate formula for, 669

(n,2n), approximate formulas for, 83

cross sections for, hydrogen, angular distribution

351-363

of, 669

total, 669

total, 667 (n,α), 84, 155-157

(n,p), 84, 114

Neutron reactions, (n,2n), approximate formulas for,	Neutrons, prompt, 621-622
in beryllium, 82	thermal (see Thermal neutrons)
in copper, 82, 114	Nickel, $q_{i}(1-\cos\theta)$ value for, 110
in nickel, 82	Nuclear physics, 61-364
in thallium, 82	nomenclature in, 61, 84
in photographic emulsions, 30	Nuclear plates, deuterium-loaded, 625
radiative capture, 83-84, 130, 152-154	Nuclear reactions, kinetic energy available for, 70
(See also Cross sections and Scattering)	momentum conservation in, 70
•	
Neutron sources, 1-23	reciprocity theorem for, 74-75
gamma-ray intensity of, for Po-Be, 3-4	schematic theory of, reaction cross section from,
for Ra-Be, 3	74, 132
mock fission, 19	total cross section from, 74, 129
production of monoenergetic neutrons, 19-23	transport cross section from, 74, 131
by crystal monochromator, 21-22	Nucleus, binding energy of (see Binding energy)
by filters, 22-23	compound (see Compound nucleus)
by pulsed cyclotron, 21	cross sections of (see Cross sections)
by time-of-flight spectrometer, 19-21	level density of, 75, 80-81, 133
from reactors, 16-18	level spacings of, 62, 130
and fission plate, 16	level width of, 71
and thermal column, 16	"magic," 62
spectrum of, for Po-B, 5, 6	mass of, 61-62, 86-105, 115-116, 130
- · · · · · · · · · · · · · · · · · · ·	
for Po-Be, 4	empirical formula for, 62
for Ra-Be, 3	packing fraction of, 86-105
use of beryllium in, 1	radioactive, 621
use of polonium in, 1, 2	radius of, 61, 85
use of radium in, 1	spin of, 63, 158-350
using alpha particles, from polonium, 3-5	stability plot of, 62, 115
from radium, 1,5	stable, properties of, 61-63, 85-105, 115-116,
from radon, 4-5	130, 158-350
using gamma-ray bombardment, of beryllium, 5-6	unstable (see Radioactive decay)
of deuterium, 5-6	,
manufacture of, 10-13	
neutron energy from, 6	Ο
	•
properties of, 8-9	Oak, mass absorption coefficient of, 722
spectrum of, 7	white, atomic density of hydrogen in, 721
yield of, 8-10	composition of, 738
using particle accelerators, 11, 14-15	physical properties of, 739
and D-D reaction, 14	One-group methods (see One-velocity theory)
and (d,n) reactions, 15	One-velocity theory, 376-401
and (p,n) reactions, 15	and the second s
yields of, measurement of, absolute, 36-37	diffusion approximation in, 381-385
relative, 37-39	for homogeneous regions in contact, 390-401
use of reactor for, 37-39	in infinite homogeneous region, 376-390
for Ra-B, 5	integral equation formulation for, 378-380
from thick targets, 1,2	for multivelocity reactors, 450-456
	spherical harmonics, expansion in, 381
time dependence for, 1	(See also Boltzmann equation)
Neutron temperature, 375	Organic compounds, boiling points of, 741
measurement of, 49	densities of, 741
in various reactors, 49	mass absorption coefficients of, 721-722
Neutron time of flight, 759	in shield materials, atomic densities of hydrogen
Neutron velocity, 759	in, 720
average value of, 376	molecular weights of, 720
Neutron wavelength, 758, 759	ORNL Graphite Reactor, 764
Neutron width, for capture, 73	ORNE Grapinte Reactor, 104
for decay of nucleus, 75	
for scattering, 73	P
Neutrons, "cold," production of, 425	r
delayed, 69-70, 109, 623, 624	Packing fraction, 62
and circulating fuel, 569	and binding energy, 62
energy of, 109	experimental values of, 62, 116
,	
mean life of, 109	Pair production, 639
parents of, 109	probability of, 639
yields of, 109	Paraffin, atomic density of hydrogen in, 721
fission, 621-622	composition of, 736
spectrum of, 69	mass absorption coefficient of, 722
low-energy, 759	physical properties of, 736



Particle reactions, 669 Penetration in homogeneous media, 646	Polymethyl methacrylate (see Lucite) Potential scattering, 72
deep, 653-657	Protons, range of, 67
critical spectral range, 654	
limited equilibrium, 654	_
most penetrating spectral component, 653-654	R
primary gammas, 653	
secondaries degraded to $E_{\rm m}$ , 653, 654	Radiation, dose units, 757
trends of penetration, 654-657	permissible levels of, 629-635
factors affecting, 646, 648-650	sources of, 621-628
accumulation of secondaries, 649-650	Radiative capture, definition of, 667
broad-beam effect, 649, 650 degradation and deflection, 652	gamma-ray energies in, 667 suppression of gamma rays in 668
energy degradation only, 651-652	Radioactive decay, 63-66, 158-350
filtration effect, 648	by alpha-particle emission, 65
penetration of primaries, 651	Geiger-Nuttall law for, 65
moderate, 657-661	by beta-particle emission, 65
polynomial method, 657-658	and delayed neutrons 69-70, 109
calculation of parameters, 658	disintegration constant for, 63
choice of analytical expression, 658	by gamma-ray emission, 65-66
distribution defined by parameters, 657	half-life for, 63
exploratory calculations, 659	isotopic properties of, 66, 158-350
NDA-NBS calculations, 659	law of, 63
Perturbation theory, 470-474	mean life for, 63
and reactivity, 554	statistics of, 63
for reactivity change, 429	Radioactive decay chain, equations for, 63-65
Photoelectric effect, atomic, 639	Radium, sources, 632
probability of, 639	use in neutron sources, 1
nuclear, 639-640	Range, of alpha particles, 66-67
probability of, 639	of charged particles, 67
Photoneutrons, 627	of electrons, 66
Physical properties, of ammonia, 733	energy relations for, 66-67, 105
of barytes concrete, 727	of fission products, 67, 105
of boral, 750	of protons, 67
of bricks, 743	Reaction cross sections, (n,p) for oxygen, values of,
of cements, 724 of fuel oil, 734	114 (n.2n) ya luan of 114
of gasoline, 734	(n,2n) values of, 114  Reactivity, change of, perturbation calculation of,
of glass, 744	536
of iron, 745	coefficients of, 553-569
of lead, 746	definition of, 472-473
of lucite, 735	direct temperature effect on, 556-564
of masonite, 740	Doppler effect on 556
of MO concrete, 726	effect of burn-up on, 565
of ordinary concrete, 725	effect of concentration on, 564-569
of paraffin, 736	effect of density on, 554-555
of rocks, 747	effect of fission products on, 566
of rubber, 735	effect of flowing fuel on, 569
of shield materials, 723-748	effect of fuel content on, 429
of stainless steel type 347, 748	effect of gaps on, 614-615
of water, 737	effect of pile boundary movement on, 556
of woods, 739	and importance, 473
Pine, white, atomic density of hydrogen in, 721	iterative method for finding, 474
composition of, 738	and period, effect of generation time on, 540
mass absorption coefficient of, 722	and poisoning, effective value of, 567-568
physical properties of, 739	power coefficient of, 571, 581
Platinum filters, 632	stationary expression for, 473
Plutonium 239, delayed-neutron data for, 109	temperature of, experimental values for lattices,
Poison, concentration of, time-dependent equation	601
for, 564-565	temperature coefficients of, for lattice piles,
cross section, effective value of, 567-568	597-598, 601 unit of, dollar, 553
fission-product, time-dependent equations for, 566-567	inhour, 552-553
(See also Xenon)	upper and lower estimates for, 453
Poisson distribution law, 63	Reactor dynamics, 531-616
Polonium, use in neutron sources, 1, 2	and accidents, 574, 576-580

Reactor dynamics, and control servomechanisms,	Resonance integral, effe
591, 593-596	for uranium, 497
and coupling to external system, 569-580	of uranium, effect of
and delayed neutrons, 531 equations for, equivalent one-group space-inde-	values of, 497, 502-50 Resonance neutron flux,
pendent form of, 533-534	Resonance scattering, 7
equations of motion for, 532	Rocks, composition of,
space-independent one-group model, 531	mass absorption coef
and generation time, 473-474, 533	physical properties o
and heat sources, 570	Roentgen, 629-630
after shutdown, 597, 600	Roentgen equivalent ma
and instability caused by xenon, 590-592	Roentgen equivalent phy
Laplace transform method for, 536, 581-583	Roentgen-hour-meter,
linearization of equations for, 572-573	Rubber, composition of
solutions of, 578, 581-592	mass absorption coef
and periods, 537, 548-549, 583	natural, atomic densi
and prompt rise, 537	physical properties o
solutions of equations with constant k, 536-547	
solutions of non-linear equations for, 574-580	
solutions for step change in k, 540-547	
solutions for time-dependent k, 540, 548-552	
and stability, 571	Samarium, production is
Nyquist criterion for, 586	Sand, composition of, 72
and transfer functions, 581-583	mass absorption coef
of external system, 582-585	Sandstone, composition
measurement of, 586, 589-590	mass absorption coef
roots of, 585-586	physical properties of
and transport delay, 573	Scattering, angle of, 75
and two-group bare thermal reactor, 534-536	angular distribution o anisotropic, 77-78
(See also Reactivity) Reactor oscillator, and absorption cross-section	mean logarithmic e
measurement, 43	slowing down by, 37
and resonance absorption integral, 52	in center-of-mass and
Reactor period (see Reactor dynamics)	systems, 75, 134
Reactor statics, theory and general results of,	coherent, 79
427-475	cross section for, 71-
Reactors, exponential (see Exponential pile)	Breit-Wigner form
heterogeneous (see Lattice reactors)	elastic, 75-80, 110-11
as neutron source, 16-18	average cosine of a
summary tables, 761-774	capture, 82
(See also Homogeneous reactors)	cross-section value
Reduced mass, 70	135-141, 351-363
Reflector savings, due to fast neutrons, 461	of gamma rays, <b>63</b> 8
due to thermal neutrons, 460	isotropic, slowing d
for graphite lattices, 484	asymptotic solu
for heavy-water-moderated reactors, 494	mean logarithmic ener
for water lattices, 499, 500	values of, 110
Reflectors, control by, 614	number of collisions
effect of, 448	neutrons by, 110
elastic, 450-451	Rayleigh, of gamma
inelastic, 453-455 Relative biological equivalence, 631	probability of, ( incoherent, 79
Removal cross section, of elements, 723	inelastic, 80-82, 112-1
effective (see Effective removal cross section)	approximate formula
Resonance absorption integral, measurement of,	146-151
51-52	neutron energy di
Resonance escape probability, 367, 480-482, 498,	146-150
502-503, 520-521	total cross section
comparison of theories for, 373	Compton, of gamma
effect of temperature on, 557	tering)
Fermi theory for, 402	effect on transport of
in finite homogeneous medium, 403	of gamma rays, 638
improvements in, 410-411	slowing down by, 37
in infinite homogeneous medium, 402	isotropic, 76-77, 110
Resonance integral, 481	energy distribution
effect of temperature on, 598, 601	mean logarithmic er

Resonance integral, effective, for thorium, 520 temperature on, 601 03 481-482 72-73 746 ficient of, 722 f, 747 in, 631-633 sical, 631 632 735 ficients of, 722 ity of hydrogen in, 721 f, 735

### S

n fission, 569 ficient of, 722 of, 746 ficient of, 722 f, 747 of, 78, 110, 135-141 energy loss for, 77 73, 375 d laboratory coordinate 72 ula for, 72 1, 129, 134-145, 351-363 ngle, 110 s for, 78, 110-111, 129, own in, 367-375 itions for, 370-374 rgy loss for, 75 s to thermalize 2-mev rays, 639 839 114, 132-133, 146-151 as for, 81-82, 132-133, stribution, 80-81, 132-133, n, 81, 132, 151 rays (see Compton scatcross section, 79 3, 375 from, 76 nergy loss for, 76



Scattering, isotropic, mean scattering angle for, 76 Shield materials, compounds in, molecular densities linear law of, effect on diffusion theory, 391 quadratic law of, effect on diffusion theory, 391 concrete, descriptions of, 729 Scattering angle, mean square of, 387 mass absorption coefficients of, 722 Schematic geometries, 653 fuel oil, atomic density of hydrogen in, 721 plane sources, 653 composition of, 733 flux calculations, 656-657 mass absorption coefficient of, 722 physical properties of, 734 point-collimated source, 653 point-isotropic source, 653 gasoline, atomic density of hydrogen in, 721 flux calculations, 656-657 composition of, 734 Secondary radiation, 646 mass absorption coefficient of, 722 electrons, 646 physical properties of, 734 gammas, 646 glass, composition of, 743 accumulation in lower portion of spectrum, 650 mass absorption coefficient of, 722 critical spectral range, 654 physical properties of, 744 limited equilibrium of softer secondaries, 654 granite, composition of, 746 Self-adjoint equations, 384 mass absorption coefficient of, 722 Self-shielding, from resonance absorption, effect of physical properties of, 747 temperature on, 558 iron, atomic density of, 717 Serber-Wilson method, boundary conditions for, 434 composition of, 744 for homogeneous reactors, 431, 433-434 effective removal cross section of, 723 numerical results for, 434-442 mass absorption coefficient of, 718, 722 Shield materials, 715-752 physical properties of, 745 air, composition of, 741 iron-portland concrete, composition of, 730 density of, 742 compressive strength of, 732 mass absorption coefficient of, 721 density of, 732 ammonia, atomic density of, 720 description of, 729 mass absorption coefficient of, 721 elemental composition of, 732 molecular density of, 720 lead, atomic density of, 717 molecular weight of, 720 effective removal cross section, 723 mass absorption coefficient of, 719, 722 physical properties of, 733 barytes aggregate, composition of, 727 physical properties of, 746 barytes concrete, composition of, 726 limestone, composition of, 746 mass absorption coefficient of, 722 elemental composition of, 728 physical properties of, 727 physical properties of, 747 barytes-limonite concrete, composition of, 728 lucite, atomic density of, 720 compressive strength of, 728 composition of, 735 density of, 728 mass absorption coefficient of, 722 elemental composition of, 728 molecular density of, 720 boral, composition of, 750 molecular weight of, 720 physical properties of, 735 mass absorption coefficient of, 721 lumnite, composition of, 731 physical properties of, 750 boron coatings for metals, 748-749 lumnite-colemanite-barytes concrete, composition of, 730 boron-containing, 748-751 solubility of, 748, 751 compressive strength of, 732 boron frits, composition of, 731 density of, 732 boron frits-barytes concrete, composition of, 730 description of, 729 elemental composition of, 732 compressive strength of, 732 density of, 732 lumnite-portland-colemanite-barytes concrete, description of, 729 composition of, 730 compressive strength of, 732 elemental composition of, 732 density of, 732 bricks, composition of, 742 description of, 729 mass absorption coefficient of, 721 physical properties of, 743 elemental composition of, 732 cement, mass absorption coefficients of, 722 masonite, atomic density of hydrogen in, 721 colemanite-barytes concrete, composition of, 730 composition of, 740 physical properties of, 740 compressive strength of, 732 mass absorption coefficients of, 721-722 density of, 732 description of, 729 MO concrete, composition of, 725 elemental composition of, 732 physical properties of, 726 colemanite borated cement, composition of, 723 natural rubber, atomic density of hydrogen in, 721 physical properties of, 724 nuclear properties of, 716-722 composition of, 723-748 ordinary concrete, composition of, 725 compounds in, 720 physical properties of, 725 atomic densities of hydrogen in, 720 organic compounds in, atomic densities of hydrodensities of, 720 gen in, 720

Shield materials, organic compounds in, boiling	Slowing down, exact hydrogen solutions for, 369
points of, 741	exact solutions for special sources, 373
densities of, 741	fluctuations near source energy in, 370, 373, 375
mass absorption coefficients of, 721-722 molecular weights of, 720	Gaussian, for uniform media, 456-461 in graphite, 412, 413
paraffin, atomic density of hydrogen in, 721	in heavy moderators, 369
composition of, 736	in hydrogen, 367, 369
mass absorption coefficient of, 722	by inelastic scattering, 373, 375
physical properties of, 736	by isotropic elastic scattering, 367-375
physical properties of, 723-748	asymptotic solutions for, 370-374
plain cement, composition of, 723	kernels for, 368
physical properties of, 724	Gaussian, 459
portland cement, composition of, 723	synthetic, 368-370
position of, 716	solutions for, 369
properties of, 716-751	mean length for measurement of, 50
rocks, composition of, 746	in mixtures, 370
mass absorption coefficient of, 722	of hydrogen and heavy element, 370
physical properties of, 747	in multiplying medium, 412
rubber, composition of, 735	of neutrons, in crystal, 79
mass absorption coefficients of, 722	with no space variation, 367-376
physical properties of, 735	basic equations for, 367
sand, composition of, 724	in media of variable density, 367
mass absorption coefficient of, 722	with space variation, 401-425
sandstone, composition of, 746	treatment by symmetric kernel, 459
mass absorption coefficient of, 722	in uniform media, 456-465
physical properties of, 747	(See also Group-diffusion method) Slowing-down density, in Al-H ₂ O, 509
selection of, 715 stainless steel type 347, composition of, 747	asymptotic space dependence of, 412
mass absorption coefficient of, 722	in beryllium, 507
physical properties of, 748	comparison of point and plane source solutions
structural, 716	for, 412
for suppression of capture gamma rays, 716	continuity equation for, 367
types of, 715-716	deviations from Gaussian, 415
water, analyses of, 736	equations for, in group-diffusion method, 418-419
atomic density of, 720	exact space dependence of, deviations from Gaus-
molecular density of, 720	sian distribution, 411-413, 415
molecular weight of, 720	Fermi approximation for, 401
physical properties of, 737	in finite homogeneous medium, 403
woods, atomic densities of hydrogen in, 721	in graphite, 412, 505
composition of, 738	in heavy water, 504
density of, and volume composition, 740	in H ₂ O-Zr, 508
mass absorption coefficients of, 722	in hydrogen, 412, 414-416
physical properties of, 739	moments of, 51
water content of, and relative humidity, 740	without space variation, 367
Shields, gamma, 715	in water, 415, 422, 506
heat generation in, 701-708 neutron, 715	Slowing-down length, and age theory, 402 in group-diffusion method, for point source,
optimization of, 709-713	421-422
replacement length in, 710	in hydrogen, 415
two-component, optimization of, 711	Solid angle of radiation, 683-684
Sigma pile, 52	Solubility of boron-containing materials, 748, 751
Slowing down, with absorption, boundary conditions	Source strength, 632
for, in finite regions, 422-423	calculation of, inverse-square law for, 632
Fermi approximation for, 409-410	platinum filter, 632
Greuling-Goertzel approximation for, 370,	radium source, 632
409-410	Sources, anisotropic, 381
Hurwitz approximation for, 370	of gamma rays, 637
improvements in resonance escape probability,	special, for exact solutions in slowing
410-411	down, 373
Wigner approximation for, 370, 409-410	Spectral distribution, of Bulk Shielding
by anisotropic scattering, 373, 375, 455-456	Facility Reactor, 704
approximation methods, for, 373, 375	of Los Alamos reactors, 704
asymptotic solutions for, 371-372	Spectrometer, gamma-ray, pair, 625
in deuterium, 370, 374	scintillation, 625
for energy-dependent cross sections, 412 for energy-independent cross sections, 450	Spherical-harmonics methods, 396, 398-400 boundary conditions at free surface, 399
.o. cher By - macpellatin er obb accitons, 400	Country Conditions at thee suitable, 355



Spherical-harmonics methods, expansion of cross section in, 377 modified, 400 P₁-approximation in, 381-382 validity of, 385 P2-approximation in, 411 P3-approximation in, 398 P_n -approximation in, 381 P_{2n-1}-approximation in, 398 solutions for isotropic source, in slab geometry, 398 in spherical geometry, 399 solutions for slab geometry, 396 solutions for spherical geometry, 396 use in one-velocity theory, 381 Wick's method, 400 Spin, nuclear, values for ground state of stable nuclei, 63, 158-350 Spruce, atomic density of hydrogen in, 721 composition of, 738 physical properties of, 739 Stainless steel, type 347, composition of, 747 mass absorption coefficient of, 722 physical properties of, 748 SUPO (see Los Alamos Water Boiler) Symbols, kinetic-theory, 366

### T

Telegrapher's equation, 390

in time-dependent diffusion theory, 385 Thermal column, neutron distribution in, 18 Thermal neutrons, in capturing medium, 375 diffusion of, 423-425 with energy-dependent cross sections, 425 with energy-independent cross sections, 424-425 hardening of, 49 "hardening" of velocity distribution, 375 Maxwell-Boltzmann distribution for, 375, 376 in noncapturing medium, 375, 376 (See also Neutron flux, thermal) Thermal Test Reactor, 771 Thermal utilization, temperature dependence in lattice piles, 601 Thorium, effective resonance integral for, 520 Thorium 232, delayed-neutron data for, 109 Threshold detectors, 33-35 Time-of-flight spectrometer, 19-21 properties of, 20 resolution of, 19 Transformations, shielding, for exponential attenuation with unitary or linear build-up, point to line, 687 slab shields, 689 for partly specified attenuation functions, 681-684 source on plane surface, 683-684 source on quadric surface, 681-682 for simple attenuation functions, 684-692 for unspecified attenuation functions, 678-681 infinite plane to point, 678

plane to cylinder, 681

Transformations, shielding, for unspecified attenuation functions, plane disk to infinite plane, 679 plane disk to point, 679, 680 plane to sphere, 679, 681 point to infinite plane, 678 point to plane disk, 678 Transport equation, asymptotic solution of, for anisotropic scattering, 387 exact solutions of, by Fourier transform, 386 for isotropic scattering, 386-388 plane sources, 386 point sources, 386 separable solution of, for anisotropic scattering, 387 Transport kernel (see Kernel, transport) Transport mean free path for weakly absorbing media, 382 Transport theory, attenuation constant of, 386, 387 for anisotropic scattering, 387 approximation for, 398 boundary conditions in, 390 correction to diffusion theory, 382 end-point method in, 400-401 extrapolation length in, 391 Fourier transform in, 400 kernels for, 380 results applied in diffusion theory, 389 (See also Boltzmann equation) Two-group theory, 465-469 critical equation for, 466 matrix method for, 466

### U

Unshielded sources, cosine, 689
isotropic, 689
volume, plane-limited, 689
Uranium, resonance integral of, effect of temperature on, 601
thermal data for, 478-485, 487, 495-503, 516-528
Uranium 233, delayed-neutron data for, 109
Uranium 235, delayed-neutron data for, 109
fission of, energy distribution in, 110
Uranium 238, delayed-neutron data for, 109

### v

Variational methods, for Boltzmann equation, 380-381 for buckling, 443, 445 for diffusion theory, 384 for water-moderated reactor, 462 Voids, gamma-ray attenuation by, 698 neutron attenuation by, 698

### W

Water, analyses of, 736
atomic density of, 720
boration of, 748
comparison of slowing-down theories for, 422
heavy, reactors moderated by, reflector savings
494

Water, heavy, reactors moderated by, slowing-down density in, 504 (See also Deuterium and Heavy-water system) lattices moderated by, 484, 499-501 metal mixtures in, age for, 486 molecular density of, 720 molecular weight of, 720 physical properties of, 737 reactors moderated by, critical mass of (see Critical mass) slowing-down density in, 415, 506, 508, 509 Water boiler reactors, 477, 488 critical-mass data for, 488 Water lattices, age of, 501 buckling for, 499, 500 cadmium ratio for, 500 diffusion length for, 501 material buckling for, 501 multiplication factor for, 501

Water lattices, reflector savings for, 499, 500
Watt's formula for fission neutrons, 621-622
Woods, composition of, 738
density of, and volume composition, 740
mass absorption coefficients of, 722
physical properties of, 739
water content of, and relative humidity, 740

### X

Xenon, build-up after shutdown, 597-599 concentration in reactors, 566-567 formation in fission, 567 poisoning, effective value of, 568 equilibrium value of, 566-567 power coefficient for, 590 power instability of, 590-592

### UNIVERSITY OF CALIFORNIA LIBRARY Los Angeles

This book is DUE on the last date stamped below.

WAN 2 3 1992		
CONCO		
" 1354		
4		
Form L9-50m-7,'54(5990)	444	



**D** 000 151 651

*QC 792 U57s v.2

